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**Elliott, J. Alex; Jones, Ian D.; Page, Trevor. 2009 The importance of nutrient source in determining the influence of retention time on phytoplankton: an explorative modelling study of a naturally well-flushed lake. *Hydrobiologia*, 627 (1). 129-142. [10.1007/s10750-009-9720-1](https://doi.org/10.1007/s10750-009-9720-1)**

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1 **The importance of nutrient source in determining the influence of retention time**  
2 **on phytoplankton: an explorative modelling study of a naturally well-flushed**  
3 **lake.**

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5  
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12 Keywords: PROTECH, flushing rate, diffuse, point, Vollenweider, residence time.

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19 **This paper has not been submitted elsewhere in identical or similar form, nor**  
20 **will it be during the first three months after its submission to Hydrobiologia.**

1 **Abstract**

2 Two models were used to examine the relationship between hydraulic retention time,  
3 nutrient source and total chlorophyll in a shallow lake (Bassenthwaite Lake, UK).  
4 The first model was a derivation of the Vollenweider model and the second was the  
5 phytoplankton community model, PROTECH.

6 The adapted Vollenweider model produced two different responses to  
7 changing retention time that were phosphorus source dependent. If the phosphorus  
8 was totally from a point source, then annual mean chlorophyll steadily declined with  
9 increasing flushing rate. However, when a diffuse source was used, the chlorophyll  
10 changed little and even increased with short retention times (retention time <40 days).

11 The PROTECH model produced some similar responses but they were more  
12 season dependent. Winter mean chlorophyll always declined with decreasing  
13 retention time, regardless of nutrient source, but the summer mean curves were source  
14 dependent and similar to those produced by the adapted Vollenweider model. Further  
15 simulations with PROTECH using a standardised flow regime provided strong  
16 evidence as to the mechanisms behind these responses.

17 Analysis showed that the decline in chlorophyll with decreasing retention time  
18 was the prevalent response of the PROTECH simulations due to flushing loss of both  
19 nutrients and algae. Furthermore, the curve formed an asymptote at long retention  
20 times because other factors (e.g. light) limited growth; retention times >100 days had  
21 little effect on chlorophyll. However, with a diffuse phosphorus source and short  
22 retention times, an increase in biomass was observed when the nutrient was limiting  
23 for growth.

## 1 **Introduction**

2 The concept of lake retention (residence) time is well established in limnology, as is  
3 its importance in influencing lake ecology (Kalff, 2002). The rate at which water  
4 moves through a lake can affect the supply, and the loss, of nutrients, organic matter  
5 etc., making changes to this flushing rate a complex balance between the competing  
6 effects of gain and loss (Søballe & Kimmel, 1987). For many lakes, such changes in  
7 flushing rate are likely in the next few decades because of climate change and its  
8 associated effects on rainfall and snowmelt (IPCC, 2007). Therefore, it is important  
9 to understand the sensitivity of lakes to changes in retention time and, more  
10 importantly, the potential drivers that may lie behind any change.

11 Perhaps one of the most important mechanisms by which retention time  
12 (flushing rate) has been thought to affect phytoplankton in lakes is through  
13 determining the in-lake phosphorus ( $P$ ) concentration. Interestingly, flushing rate was  
14 originally excluded as a factor in the Vollenweider (1968) model because most of the  
15 lakes originally used to derive the empirical relationship had very long retention times  
16 (i.e. 3 of 25 had retention times  $< 1$  year; Dillon (1975)). Dillon's (1975) application  
17 of the model to a lake with a retention time of approximately 19-21 days highlighted  
18 this omission and subsequent versions of the Vollenweider model included flushing  
19 rate (Vollenweider, 1976; Larsen & Mercier, 1976; Vollenweider & Kerekes, 1980):

$$20 \quad P = \frac{L_p / q_s}{(1 + \sqrt{\tau_w})}, \quad (1)$$

21 where  $L_p$  is the annually and areally averaged phosphorus load ( $\text{mg m}^{-2} \text{y}^{-1}$ ),  $q_s$  is the  
22 water discharge height ( $\text{m y}^{-1}$ ) and  $\tau_w$  (y) is the reciprocal of the flushing rate. In this  
23 version of the model, the flushing rate acts as a surrogate for the sedimentation of  
24 phosphorus from the water column (Kalff, 2002). In a recent review, Brett &

1 Benjamin (2008) re-emphasized the importance of retention time in the Vollenweider  
2 (1976) phosphorus loading model and its many derivatives. They also highlighted  
3 that the source of phosphorus in the Vollenweider model is non-specific and may  
4 account for some of the variation in the relationship i.e. internal loading of  
5 phosphorus can affect the relationship between external phosphorus supply and in-  
6 lake phosphorus.

7 The relationship between nutrient source and retention time has long been a  
8 relatively unexplored issue, despite its potential importance being highlighted in  
9 Edmondson's (1970) review of Vollenweider (1968); the former found issue with the  
10 latter's lack of consideration as to the source of the phosphorus in Vollenweider's  
11 model. Schindler (2006) recognized the importance of this factor in a comprehensive  
12 review of the state of eutrophication science, stating that the effect that retention time  
13 has on eutrophication is poorly understood when the nutrient load to the lake is split  
14 between point (e.g. sewage waste, sediment released phosphorus) and diffuse (e.g.  
15 agriculturally derived phosphorus) sources.

16 In an initial study examining precisely this issue, Jones & Elliott (2007)  
17 adapted the Vollenweider model in Equation 1 to demonstrate the theoretical basis for  
18 this point/diffuse effect. They rewrote the model in a form that could separate inflow  
19 dependent and inflow independent phosphorus sources thus:

20 
$$P = \frac{P_i}{(1 + \sqrt{V/Q})} + \frac{M_s}{(Q + \sqrt{QV})}, \quad (2)$$

21 where  $P_i$  is the inflow phosphorus concentration ( $\text{mg m}^{-3}$ ),  $V$  is the volume of the lake  
22 ( $\text{m}^3$ ),  $Q$  is the discharge from the lake ( $\text{m}^3 \text{y}^{-1}$ ) and  $M_s$  is the annual input mass from  
23 point sources (see Jones & Elliott (2007) for a full explanation and derivation). In this  
24 study, we make the approximation that the first and second terms of the right hand

1 side of the above equation are analogous to diffuse and point source loading  
2 respectively. This simplification should be considered when interpreting the results of  
3 this study. Furthermore,  $P$  can be used to predict  $C$ , the annually averaged  
4 chlorophyll concentration ( $\text{mg m}^{-3}$ ) with this equation from Vollenweider & Kerekes  
5 (1980):

$$6 \quad C = 0.37(P^{0.91}), \quad (3)$$

7 Coupling these two equations allows the prediction of the annual mean chlorophyll of  
8 a given lake in response to different point and diffuse source ratios and retention  
9 times. Whilst it is simplistic and has its limitations, it does provide an important  
10 starting hypothesis of response for a given lake.

11 This study aims to expand upon the investigation of Jones & Elliott (2007) by  
12 testing a lake which naturally experiences a wide range of retention times. By using  
13 the phytoplankton community model, PROTECH, the study examines fully the impact  
14 of changing retention time, as well as considering the importance of annual discharge  
15 pattern, the relative effects in winter and summer and, of course, the importance of  
16 nutrient source. It compares these outputs to those predicted by Equations 2 and 3  
17 and considers the implications of any differences in response.

1 **Methods**

2 *Site description*

3 Bassenthwaite Lake (54° 39.09' N, 3° 12.93' W) is situated to the north of the English  
4 Lake District. It is relatively shallow, with a mean depth of 5.3 m and a maximum  
5 depth of 19.0 m (Ramsbottom, 1976). Thermal stratification is episodic and readily  
6 broken down, and the average annual retention time is short, c. 19 days (Thackeray et  
7 al., 2006). Based on the annual average concentration of phytoplankton chlorophyll-*a*  
8 (13.4 mg m<sup>-3</sup>, Thackeray et al., 2006), Bassenthwaite Lake may be considered  
9 eutrophic (OECD, 1982). Estimates of the relative importance of the sources for  
10 nutrients entering the lake suggest that approximately 60% of the total annual load  
11 comes from anthropogenic sources (treated sewage waste) with the rest derived from  
12 the catchment (Thackeray et al., 2006). In the UK, for example, this split can range  
13 from anywhere between 100% point source to virtually 0% (Anthony & Lyons, 2007).

14 Bassenthwaite Lake has been routinely monitored since 1991, with nutrient  
15 and phytoplankton samples taken every two weeks (the exception was during the  
16 2001 foot and mouth incident which restricted access to the rural areas of the UK).  
17 Corresponding daily meteorological measurements for wind speed, air temperature  
18 and air humidity were available from a meteorological station approximately 4 km  
19 away from the lake. Daily cloud cover measurements were available from another  
20 meteorological station near Windermere, approximately 25 km away. Daily outflow  
21 discharges were available and the inflows were assumed to be the same as these  
22 values. Previous analysis (see Elliott et al., 2006) had identified that 1996 was the  
23 year during this study period with the longest annual retention time (c. 28.25 days),  
24 therefore this year was chosen for the subsequent sensitivity analysis in order to  
25 provide the widest range of retention times, and its corresponding observed discharge

1 and meteorological data were used to drive the simulations.

2

### 3 *PROTECH model description*

4 PROTECH (**Phytoplankton Responses To Environmental CHange**) is a computer  
5 model that simulates the growth of multiple phytoplankton species types (see  
6 Reynolds et al., 2001 for full details of the equations and philosophies behind  
7 PROTECH). The biological component of the PROTECH model is the basic state  
8 variable equation determining the daily change in the chlorophyll *a* concentration (*X*)  
9 of each algal species:

$$10 \quad \Delta X/\Delta t = (r' - S - G - D) X, \quad (4)$$

11 where *r'* is the proportional growth rate over 24 h, *S* represents the losses due to  
12 settling, *G* the losses due to *Daphnia* grazing (see below for further details) and *D*  
13 those due to dilution. The growth rate for a species in the model is firstly determined  
14 by their morphology and then modified by the water temperature and daily  
15 photoperiod and can be limited further by lack of phosphorus, nitrogen or silicon.  
16 These nutrient concentrations in the water column are modified to reflect uptake due  
17 to growth and daily supply and loss via inflow/outflow exchange. For all the species  
18 simulated it is assumed that these nutrients are consumed from the water column in  
19 the following stoichiometric ratio of 82 g SiO<sub>2</sub> (only if diatom): 8.3 g nitrogen : 1.2 g  
20 phosphorus : 1g chlorophyll (Stumm & Morgan, 1981).

21 In this study eight phytoplankton species were modelled at one time and an  
22 analysis of Bassenthwaite Lake phytoplankton data was conducted in order to identify  
23 the dominant taxa that should be included in the simulations. They were *Chlorella*,  
24 *Cryptomonas*, *Aphanizomenon*, *Anabaena*, *Fragilaria*, *Aulacoseira*, *Asterionella*  
25 *formosa* Hass. and *Planktothrix* (Table 1). A species-specific movement function



1 calculates the position of each species in the column, accounting for the movement of  
2 the water and Stoke's Law (movement down the water column), as well as the  
3 motile/buoyancy properties of some phytoplankton (positive movement up the water  
4 column, dependent upon light intensity for motile species) (Table 2).

5 As mentioned above, there is a simple grazing routine in PROTECH, adopting  
6 the temperature- and food-dependent growth and reproduction relationships  
7 developed for *Daphnia* by Reynolds (1984). This simulated grazing pressure is also  
8 affected by flushing loss and was applied to only three of the eight species simulated  
9 in this study (Table 1).

10 The physical structure of the water column is defined over vertical,  
11 morphologically-dependent 0.1 m slices. The extent of mixing within the water  
12 column is calculated by following the Monin-Obukhov length calculation (Imberger,  
13 1985), which gives an instantaneous prediction of the depth at which the buoyancy  
14 forces (due to the heat flux) and the opposing dissipative forces (due to wind stress)  
15 are equal in magnitude. This point corresponds to the extent of the mixed layer,  
16 assuming initial uniformity. To test the resistance to mixing of an existing density  
17 structure, it is also necessary to apply a Wedderburn-test, which incorporates a term  
18 for the accumulated density difference between the water at the surface and at any  
19 nominated depth. At each iteration, the model works down the water column,  
20 incorporating each slice until the accumulated density difference resists the  
21 incorporation: this slice then corresponds to the depth of the thermocline (Reynolds et  
22 al., 2001).

23 The PROTECH model has had its key growth parameters verified (Elliott et al.  
24 1999b), tested for sensitivity (Elliott et al. 1999a) and been validated at numerous  
25 sites (Elliott et al., 2000; Lewis et al., 2002; Elliott & Thackeray, 2004; Elliott et al.,

1 2007; Bernhardt et al., 2008). Also, it has been successfully used to simulate  
2 Bassenthwaite Lake in a previous study (Elliott et al., 2006).

3

4 *Retention time sensitivity*

5 The biomass of the simulated phytoplankton was calculated at a daily temporal  
6 resolution in terms of an integrated 5-m concentration of chlorophyll-*a* per unit  
7 volume of lake water. This made the results comparable with observed data from  
8 Bassenthwaite Lake in 1996. The total chlorophyll output of PROTECH was  
9 compared with the observed data and tested both visually and statistically, using  
10 regression analysis for its “goodness-of-fit”.

11 This 1996 simulation was then subjected to a detailed testing by the following  
12 method. Eleven nutrient supply ratios were calculated ranging from 100% diffuse to  
13 100% point phosphorus source in 10% changes to the ratios (i.e. 90-10, 80-20, 30-70  
14 etc.) and representing ratios commonly observed in UK water bodies (Anthony &  
15 Lyons, 2007). The point source was created by altering the measured inflow SRP  
16 concentration so that the daily load was the same regardless of the changes in daily  
17 discharge (i.e. a dilution). Conversely, a diffuse source was created by not changing  
18 SRP concentration with changes in discharge, so that the daily load would change  
19 with discharge. Finally, to create scenarios that had different ratios of point and  
20 diffuse nutrient sources, the alterations outlined above were applied in different  
21 relative proportions to SRP inflow input. 100 different retention time simulations for  
22 each nutrient scenario were then run, providing a range of annual retention times  
23 between 5.7 – 260.0 days. Annual, winter (defined as January-March and November-  
24 December) and summer (August-September) mean chlorophyll were calculated for  
25 each run.

1           The previous study of Jones & Elliott (2007) suggested that the seasonal  
2 pattern of discharge might have an influence on the simulated phytoplankton, thus  
3 additional runs were made for the two extreme cases of source scenarios (100% point  
4 and 100% diffuse) using a seasonal average discharge pattern. The latter was  
5 achieved by calculating the mean daily discharge for October-March and also for  
6 April-September, and then applying those means to the relevant time period of the  
7 simulations e.g. the October-March mean was used for all the days in the simulation  
8 during those months and, again, 100 different retention time scenarios were run for  
9 the two nutrient sources. Finally, in response to the results of these stepped-flow  
10 simulations, the runs were repeated but this time the phosphorus concentration of the  
11 inflow was reduced to 20% of its original value in 10% reductions and 100 different  
12 retention time scenarios were run for each of these changed nutrient concentrations.  
13 Only the mean summer chlorophyll values are shown for these latter simulations  
14 because this period showed the greatest sensitivity to the flow changes.

## 1 **Results**

### 2 *Vollenweider model predicted response*

3 By applying Equations 2 and 3 to Bassenthwaite Lake in 1996 for a range of annual  
4 discharge rates (Q), a theoretical response of annual mean chlorophyll to changing  
5 retention time was produced for the two extreme nutrient source scenarios of 100%  
6 point (i.e.  $P_i$  set to zero) and 100% diffuse (i.e.  $M_s$  set to zero) (Fig. 1). The figure  
7 shows clearly large differences between the two theoretical loading scenarios. If the  
8 source is totally point, then the supply of phosphorus is independent of discharge and  
9 is therefore flushed out at higher discharges (shorter retention times) and the mean  
10 annual chlorophyll response follows a bow shaped curve. In contrast, with only  
11 diffuse sources the relationship is relatively flat and unchanging because the increase  
12 in phosphorus supply is balanced by the nutrient's flushing loss and sedimentation.  
13 However, there is the notable exception that at very high discharges (c. <40 days  
14 retention time) more chlorophyll is produced, as the gain of phosphorus begins to  
15 outweigh the "sedimentation of phosphorus", as approximated by Equation 2.

16

### 17 *PROTECH simulation of Bassenthwaite Lake in 1996*

18 The total chlorophyll output of PROTECH (i.e. sum of the eight species' individual  
19 chlorophyll concentrations) was compared to the observed seasonal pattern (Fig. 2).  
20 The seasonal pattern was reproduced, particularly the spring bloom, although the  
21 single high summer value was not produced by PROTECH. Regression analysis  
22 between observed and simulated confirmed the "goodness-of-fit" of the simulation  
23 ( $R^2 = 0.67$ ,  $P < 0.01$ ).

24

### 25 *Retention time sensitivity*

1 Considering initially the two extreme nutrient supply scenarios, it was clear that the  
2 response of the mean total chlorophyll to retention time changes was greatly  
3 dependent upon the period of year examined (Fig. 3). The annual mean total  
4 chlorophyll showed that nutrient source did affect the response of chlorophyll to  
5 retention time change. Both scenarios showed a decline in the annual mean with  
6 increasing discharge at short retention times, although the response curve under the  
7 100% diffuse scenario was flatter than the 100% point simulations above about 100  
8 days (Fig. 3). In the summer, the different responses between the nutrient scenarios  
9 were much more pronounced. The point source scenario produced a steady decline  
10 from the maximum mean summer total chlorophyll of 30 to 12 mg m<sup>-3</sup> (Fig. 3a) with  
11 shortening retention time, whereas the diffuse source scenario showed a steady  
12 increase in chlorophyll (Fig. 3b). It was also interesting that during the summer, for  
13 the point source scenario, a distinct step change in chlorophyll occurred at c. 90 days  
14 retention time (Fig. 3a). Finally, irrespective of nutrient source, the mean winter total  
15 chlorophyll response was virtually identical between the two nutrient scenarios,  
16 showing a slight decline with shorter retention times (Fig. 3).

17 The other nutrient source scenarios provided further information on these  
18 responses (Fig. 4). Each 10 % change in the point-diffuse ratio produced a relatively  
19 smooth transition between the two extreme mean annual chlorophyll response curves  
20 (Fig. 4a). The greatest rate of change occurred between the 100% diffuse scenario  
21 and 20-80 point-diffuse scenario. The summer mean chlorophyll values showed a  
22 similar response as the annual mean curves, with gradual changes in chlorophyll  
23 occurring as the resource ratios altered. It is interesting to note that the gain in  
24 chlorophyll that was seen at short retention times in the 100% diffuse scenario became  
25 a loss with only a 30% reduction in the diffuse source contribution (i.e. for ratios

1 greater than 30-70 point-diffuse). Finally, the abrupt change in chlorophyll at c. 100  
2 days retention time was hinted at in most ratios but was most pronounced at ratios  
3 greater than 70-30 point-diffuse.

4 For the 100% diffuse and point scenario, the day at which the total chlorophyll  
5 first and last passed  $10 \text{ mg m}^{-3}$  was recorded for all the retention time scenarios (Fig.  
6 5); these points nominally represented the start of the spring bloom and the end of the  
7 summer/autumn bloom. Irrespective of nutrient source, the onset of the spring bloom  
8 became 14 days earlier with retention times shorter than 18 days but barely advanced  
9 further with longer retention times. The end of the bloom occurred later with  
10 increasing retention time but did show a nutrient source related effect. With a point  
11 source, the bloom end levelled out 60 days later (day 335) than that observed for the  
12 shortest retention time scenario (day 272). In contrast, the diffuse source scenarios  
13 levelled out about 40 days later at day 315.

14 The seasonal average discharge pattern scenarios produced response curves  
15 that were generally similar to those in Fig. 3 (Fig. 6). There was one notable  
16 exception to this: the summer mean chlorophyll for the diffuse scenario did not  
17 continue to increase at very short retention times, but instead declined sharply (Fig.  
18 6b). This result warranted further consideration, thus the seasonal average  
19 simulations were repeated, but this time with decreasing inflow phosphorus  
20 concentrations and focusing solely on the summer means. The patterns produced  
21 were similar to those in Fig. 6 for the point source conditions (Fig. 7a), although the  
22 actual amount of chlorophyll produced naturally declined with decreasing inflow  
23 phosphorus. The same was not true for the diffuse source simulations (Fig. 7b) where  
24 the pattern of sharp decline in summer mean average seen in Fig. 6b was only  
25 apparent in the scenarios with more than 40-50% of the original inflow phosphorus

- 1 concentration. Below this amount, the mean chlorophyll had a much flatter response
- 2 with changing retention time, actually rising slightly with very short retention times in
- 3 a way similar to the summer mean curve in Fig. 3b.

## 1 **Discussion**

2 The effects on phytoplankton of changing retention time can be varied and complex  
3 (Kalff, 2002). By using models, we can try to unravel this complexity to understand  
4 quantitatively the response of phytoplankton populations to these changes. If we  
5 consider first the results from equations 2 and 3, it would appear that changes in  
6 retention time seem to be able to produce large variations in annual phytoplankton  
7 biomass, but that the source of nutrients greatly determines the extent of variation, i.e.  
8 with a 100% point nutrient source, the change is greatest (Fig. 1). With this simple  
9 model, it is easy to understand why this is the case by examining Equation 2. If the  
10 nutrient load entering a lake is wholly proportional to the inflow ('100 % diffuse'  
11 source), then as river discharge increases, more nutrients are brought into the lake, but  
12 simultaneously, more nutrients are flushed out of the lake. This can be seen in the first  
13 part of the right hand side of Equation 2, which also indicates that this balance is  
14 slightly altered by sedimentation effects, albeit ones that are approximated empirically  
15 in this Equation. Conversely, if the nutrient load to a lake is from a point source only,  
16 then an increase in river discharge brings no extra nutrients to the lake, but the  
17 consequent increase in flushing still removes in-lake nutrients (i.e. increased dilution).  
18 This is represented by the second part of the right hand side of Equation 2, where the  
19 discharge is firmly within the denominator. Following Equation 3, a decrease in in-  
20 lake nutrient concentration leads directly to a decrease in phytoplankton biomass.  
21 Interestingly, this means that the Vollenweider equation does not account for the  
22 actual removal of biomass directly from flushing but rather via the loss of in-lake  
23 phosphorus. Of course, in order to explore these predictions for Bassenthwaite Lake,  
24 we used a second, more complex, model.

25 The PROTECH simulations produced a greater range of response curves than



1 Equation 3 and were less smooth in nature. The latter reflects the interactions  
2 between the eight species with their different traits and, whilst interesting, such  
3 competitive interactions were not the focus of this study. Rather the broad overall  
4 changes were compared to the simple Vollenweider responses. The winter curves  
5 showed little response, regardless of phosphorus source; under such poor  
6 environmental conditions (low temperatures and light levels), net growth was very  
7 low. In the summer, both curves agreed with those predicted by Equation 3, with  
8 shortening retention time causing a decrease in chlorophyll under point source  
9 conditions and an increase under diffuse conditions. The explanation for this lies in  
10 one of the fundamental assumptions behind the original Vollenweider model, namely  
11 that phosphorus is controlling the amount of chlorophyll in the lake (see Equation 3).  
12 In the PROTECH simulations, growth limiting concentrations of phosphorus ( $<3 \text{ mg}$   
13  $\text{m}^{-3}$ , Reynolds (1984)) occurred only in the summer period. This meant that during  
14 the rest of the year, the supply of phosphorus to the lake was less important than the  
15 direct flushing of phytoplankton, leading to a decrease in biomass with increasing  
16 discharge. However, in the summer diffuse scenario, the increased flow brought with  
17 it vitally important extra phosphorus as well as a reduced sedimentation rate, leading  
18 to an increase in biomass; this is in accordance with the first term of the right-hand  
19 side of Equation 2.

20         Given the two different response curves for 100% diffuse or point sources and  
21 the fact that most lakes experience varying ratios of both types of nutrient source  
22 (Anthony & Lyons, 2007), it was important to see if altering the split between the two  
23 was a gradual, even transition or involved sudden changes. The evidence from this  
24 study suggested that the former was generally the case (Fig. 4) although other growth  
25 limiting factors in PROTECH made the transition with changing ratio less regular

1 with longer retention times. The ratio scenarios (Fig. 4) illustrated that the increase in  
2 chlorophyll at short retention times was dependent on the diffuse supply being  
3 dominant; with only a 20-30% reduction in the diffuse source contribution, the  
4 biomass accumulation was no longer positive under high flushing conditions. This  
5 showed that even in the summer, the loss processes associated with high discharges  
6 were generally more dominant than the benefits of increased nutrient supply and  
7 reduced sedimentation. Finally, it is worth briefly commenting on the discontinuous  
8 change in summer mean chlorophyll observed around retention times of c. 90 days  
9 (Fig. 4b). The abruptness of the change was sharpest with the increasing proportion of  
10 the point source and was caused primarily by changes in *Planktothrix* biomass.  
11 Closer analysis of this threshold showed that the increase in *Planktothrix* with longer  
12 retention times was connected to more SRP being available, allowing *Planktothrix* to  
13 gradually establish a larger population, shading out the other species and reducing the  
14 total chlorophyll. This phytoplankton type in PROTECH has demonstrated rapid-  
15 change responses like this before, such as when the model was used to investigate the  
16 intermediate disturbance hypothesis (Elliott et al., 2001) and shows how more  
17 complex models can produced more complex outcomes.

18         The timing of the start and end of the blooms showed similar patterns of  
19 response to each other and to those observed in our Blelham Tarn study (Jones and  
20 Elliott, 2007). For the starting day of the bloom, the lack of difference between the  
21 nutrient source treatments was again due to the lake being replete with nutrients and  
22 the delay simply due to the increase flushing loss under the high discharge scenarios.  
23 The marked difference between the nutrient scenarios response curves for the end of  
24 the bloom was due to the scarcity of nutrients under the conditions of diffuse source  
25 and low flow i.e. low overall nutrient supply led to more rapid bloom termination.

1 With a point source and low flow, nutrients were largely not limiting, hence the  
2 bloom was more prolonged (Fig. 5a).

3 The seasonal average discharge pattern scenarios were introduced in this study  
4 to try and correct for any potential complexity that was being caused by the specific  
5 discharge pattern being used. They produced response curves that were similar to  
6 those derived from the observed 1996 discharge pattern except for the significant  
7 exception of the summer mean chlorophyll with a 100% diffuse phosphorus source  
8 (Fig. 6b). This curve declined with shortening retention time, in marked contrast to  
9 the curve in Figure 4b. It was suspected that this difference was, again, due to the  
10 phosphorus supply and indeed this was the case; the averaged summer discharge  
11 conditions simply supplied enough phosphorus to preventing it reaching persistent  
12 limiting levels and thus the effects implied in Equation 2 did not apply. Therefore, we  
13 also ran simulations where the overall inflow phosphorus concentration was reduced  
14 and saw a reduced rate of decrease in summer mean chlorophyll with increasing  
15 discharge and low nutrient (Fig. 7), thus clearly proving how important it was to have  
16 a limiting in-lake phosphorus concentration to produce the diffuse source curve of  
17 Equation 2 (Fig. 1).

18 Drawing together these various responses, it seems clear that Equations 2 and  
19 3 have their limitations compared to the more complex PROTECH model when  
20 applied to a specific lake. Taking each nutrient source response curve in turn, the  
21 100% point source relationship seemed the more robust in that its general shape was  
22 similar between the two models used. This is perhaps unsurprising, because it has the  
23 least complex driving factor of the two; the increasing discharge just flushes out more  
24 and more nutrients and phytoplankton. This latter effect is regarded as the most  
25 typical response by phytoplankton to an increasingly flushed system (Dickman, 1969;

1 Kalff, 2002). However, for 100% point source, the PROTECH model produced an  
2 upward sloping *asymptotic* curve compared to the continually rising curve of  
3 Equation 3. This happened because PROTECH, being a single lake model that  
4 calculates daily chlorophyll values, accounts for other growth limiting factors not  
5 present in the original, statistically derived, Vollenweider model which seeks to model  
6 a huge range of lake types and provide an annual mean value. In the case of the  
7 scenarios run in this study, the most important one was light limitation caused by self-  
8 shading. This was also found to be the case by Reynolds' (1992) assessment of the  
9 Vollenweider model which showed that the chlorophyll to phosphorus yield could not  
10 increase indefinitely and that some other factor would eventually cap the chlorophyll  
11 yield (e.g. light or nitrogen availability).

12         Understanding the effect of the diffuse source was more complex. It seems  
13 clear that the Equation 3 prediction of mean chlorophyll being fairly unresponsive at  
14 long retention times is supported by PROTECH, but at lower retention times there can  
15 be a marked difference. Thus, within the scope of the scenarios tested in this lake  
16 system, only under one set of circumstances can PROTECH produce a relationship  
17 comparable to Equation 3's output and, as was shown clearly with the seasonal  
18 average flow scenarios, this was dependent on phosphorus availability being limiting.  
19 Therefore, only under these precise circumstances would the increase in flow bring  
20 sufficient net-benefit to the phytoplankton populations.

21         Relating the modelled outputs of this study to specific case-studies was quite  
22 challenging because studies focusing on such high flushing in lakes, particularly in the  
23 summer, are rare (these rates are more typical of rivers). Nevertheless, there are some  
24 examples of increasing biomass production under very high flushing conditions. For  
25 example, the very shallow lakes (mean depth 1.1-1.2 m) of the Pampa Plain

1 (Argentina) were reported to have increased summer total chlorophyll and phosphorus  
2 (primarily from agriculture, i.e. diffuse sources) when the retention time decreased to  
3 < 15 days (Rennella & Quirós, 2006) and there have been similar responses observed  
4 in comparable systems that regularly experience such low retention times (Van den  
5 Brink et al., 1994; Walz & Welker, 1998). However, these systems are all considered  
6 hypertrophic, so nutrients are unlikely to be limiting, although there are other studies  
7 that show a similar response pattern and also nutrient limitation (Turner et al., 1983).  
8 Another study found an increase in in-lake phosphorus occurred with increasing  
9 discharge, but phytoplankton growth was curtailed by the raised turbidity caused by  
10 the flushing (Vanni et al., 2006). The influence on growth of other factors linked to  
11 changes in retention time again shows the limitations of a model as simple as equation  
12 2. Clearly, though, there is still a need for further research on this topic, particularly  
13 at the species level.

14

## 15 **Conclusions**

16 It would appear that variations in retention time, irrespective of discharge pattern, can  
17 have large influences on phytoplankton populations under several combined  
18 conditions. These are when the dominant source of phosphorus is point and the  
19 retention time is < 90-100 days, or simply when the retention time is < c.30 days.  
20 These results find further support in that it has been often found that retention times  
21 greater than 100 days are inconsequential in terms of their influence on growth rate  
22 (Søballe & Kimmel, 1987; Kimmel, Lind & Paulson, 1990; Reynolds, 2006) and,  
23 secondly, that lakes regularly experiencing retention days < 30 days struggle to  
24 support *Planktothrix* populations (Reynolds, 2006). Finally, both models show that if  
25 future climate change causes the predicted reduction in rainfall that could be seen in

1 mainly regions, the response of a lake to a change in its retention time will be greatly  
2 dependent on the nutrient source. Thus, if summer flows were low in a point source  
3 system limited by phosphorus, chlorophyll is likely to increase and conversely in a  
4 diffuse system, it would decrease.

5

## 6 **Acknowledgements**

7 We thank the British Atmospheric Data Centre and Mr B.C. Tebay for providing the  
8 meteorological data, the Environmental Agency for providing the flow data and for  
9 our colleagues in CEH for collecting the biological data. In this study, IDJ and TP  
10 were funded by NERC Research Grant NE/F011474/1.

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1 **Tables**

2 Table 1. The morphological and phylogenetic characteristics of the eight simulated  
3 species. The last three columns denote simple logic statements (TTrue/FFalse) which, if  
4 True, activate relevant functions in PROTECH.

5

<b>Species</b>	<b>Surface Area (<math>\mu\text{m}^2</math>)</b>	<b>Volume (<math>\mu\text{m}^3</math>)</b>	<b>Maximum dimension (<math>\mu\text{m}</math>)</b>	<b>Diatom ?</b>	<b>Grazed ?</b>	<b>Nitrogen fixer?</b>
<i>Chlorella</i>	50	33	4	F	T	F
<i>Cryptomonas</i>	1030	2710	21	F	T	F
<i>Aulacoseira</i>	4350	2970	240	T	F	F
<i>Asterionella</i>	6690	5160	130	T	T	F
<i>Fragilaria</i>	11950	8100	70	T	F	F
<i>Planktothrix</i>	7350	13970	300	F	F	F
<i>Anabaena</i>	6200	29000	75	F	F	T
<i>Aphanizomenon</i>	5200	15400	125	F	F	T

6

1 Table 2. Summary of PROTECH instructions governing vertical movements of  
 2 phytoplankton. In all cases of either moving up or down, if the top or bottom layer  
 3 (i.e. 0.1 m PROTECH layer) is encountered the movement is stopped; if it is the  
 4 bottom layer the phytoplankton is lost.

5	6	7	8
Phytoplankton	Light condition ( $\mu\text{mol photon m}^{-2} \text{s}^{-1}$ )	Movement ( $\text{m d}^{-1}$ )	
9			<b>1. Nearly neutrally-</b>
10			<b>buoyant, non-motile</b>
11			<b>life-forms</b>
12			<i>Chlorella</i>
13	all	sink 0.1	
14			<b>2. Non-buoyant non-</b>
15			<b>motile diatoms</b>
16			<i>Aulacoseira</i>
17	$\leq 500$	sink 0.8	
18	$> 500$	sink 1.0	
19			<i>Asterionella</i>
20	$\leq 500$	sink 0.2	
21	$> 500$	sink 1.0	
22			<i>Flagilaria</i>
23	$>600$	sink 1.0	
24	$\leq 600$	sink 0.3	
25			<b>3. Buoyancy-regulating</b>
26			<b>Cyanobacteria</b>
27			<i>Planktothrix</i>
28	$> 30$	sink 0.1	
29	$\leq 30$ but $> 10$	no move	
30	$\leq 10$	rise 0.1	
31			<i>Anabaena</i> , and
32	$> 100$	sink 0.3	
33	$\leq 100$ but $> 30$	sink 0.1	
34	$\leq 30$ but $> 10$	no move	
35	$\leq 10$	rise 0.1	
36			<b>4. Swimming flagellates</b>
			<i>Cryptomonas</i>
	$> 100$	rise 0.1	
	$\leq 100$	rise 2.0	

1 **Figure Legends**

2 Fig. 1. Illustration of the Equation 3 predicted response of annual mean total  
3 chlorophyll  $a$  ( $\text{mg m}^{-3}$ ) in Bassenthwaite Lake in 1996 to changing retention time  
4 (days) with a point (solid line) and diffuse (dashed line) source of phosphorus.

5

6 Fig. 2. Comparison between the observed (crosses) total chlorophyll  $a$  ( $\text{mg m}^{-3}$ ) in  
7 Bassenthwaite Lake in 1996 and that simulated by PROTECH (solid line).

8

9 Fig. 3. Response of the mean chlorophyll  $a$  ( $\text{mg m}^{-3}$ ) for the winter (long dashed  
10 lines), summer (short dashed lines) and whole year (solid line) to changing retention  
11 time (days) with (a) point and (b) diffuse sources of phosphorus.

12

13 Fig. 4. Response of the mean chlorophyll  $a$  ( $\text{mg m}^{-3}$ ) for (a) whole year and (b) the  
14 summer to changing retention time (days) with varying ratios of point-diffuse sources  
15 of phosphorus (e.g. 100\_0 = 100% point).

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17 Fig. 5. Variation in the timing (days from start of year) of the start (circles) and end of  
18 the bloom (crosses) with (a) point and (b) diffuse sources of phosphorus.

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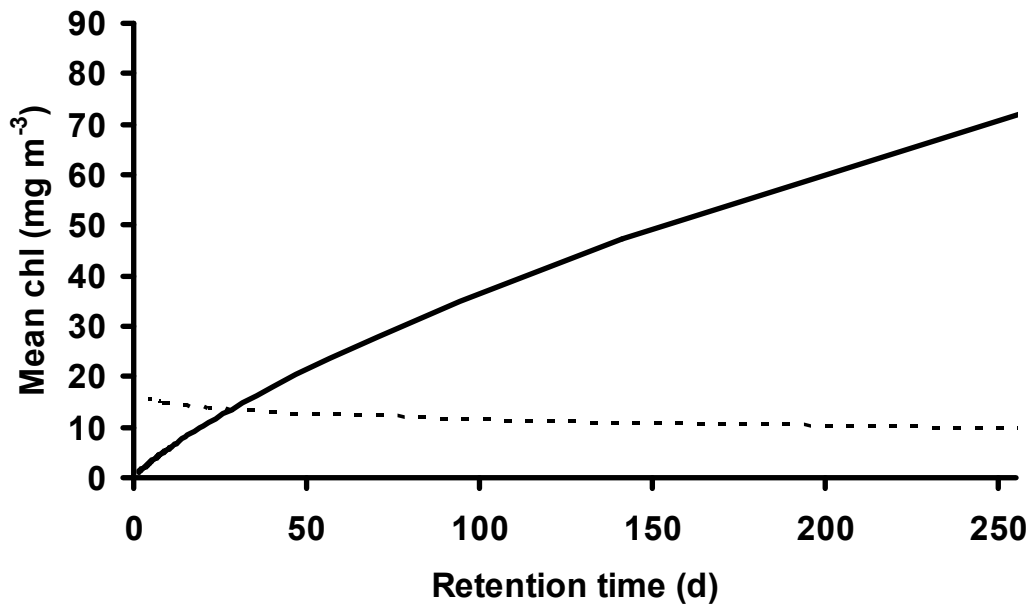
20 Fig. 6. Under the “stepped” average discharge pattern, the response of the mean  
21 chlorophyll  $a$  ( $\text{mg m}^{-3}$ ) for the winter (long dashed lines), summer (short dashed lines)  
22 and whole year (solid line) to changing retention time (days) with (a) point and (b)  
23 diffuse sources of phosphorus.

24

1 Fig. 7. Under the “stepped” average discharge pattern, the response of the mean  
2 summer chlorophyll *a* ( $\text{mg m}^{-3}$ ) to changing retention time (days) and inflow  
3 phosphorous concentration (from no change (1.0) to 80% reduction (0.2)) with (a)  
4 point and (b) diffuse sources of phosphorus.  
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1 **Figures**

2 **Fig. 1**



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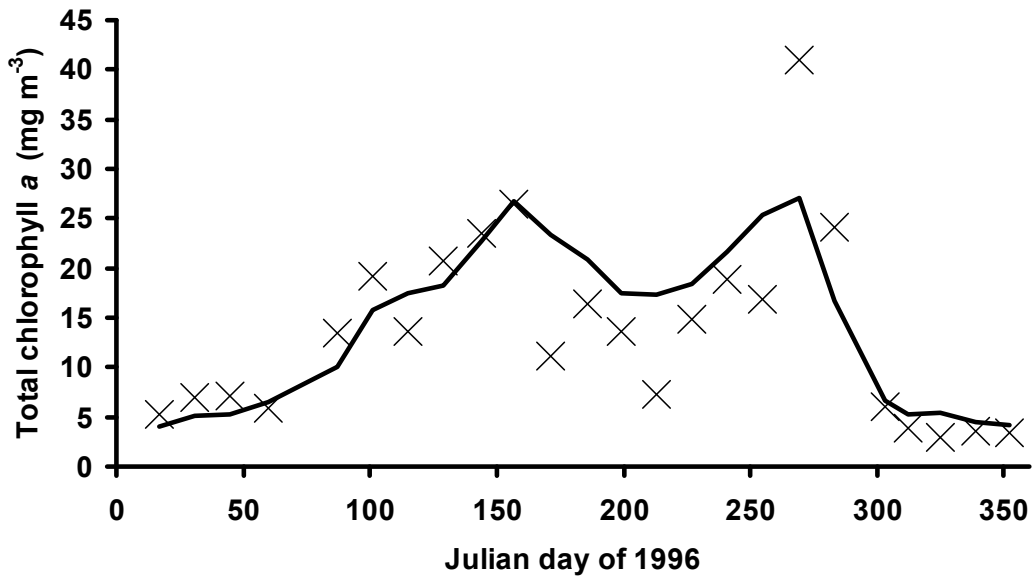
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1 Fig. 2



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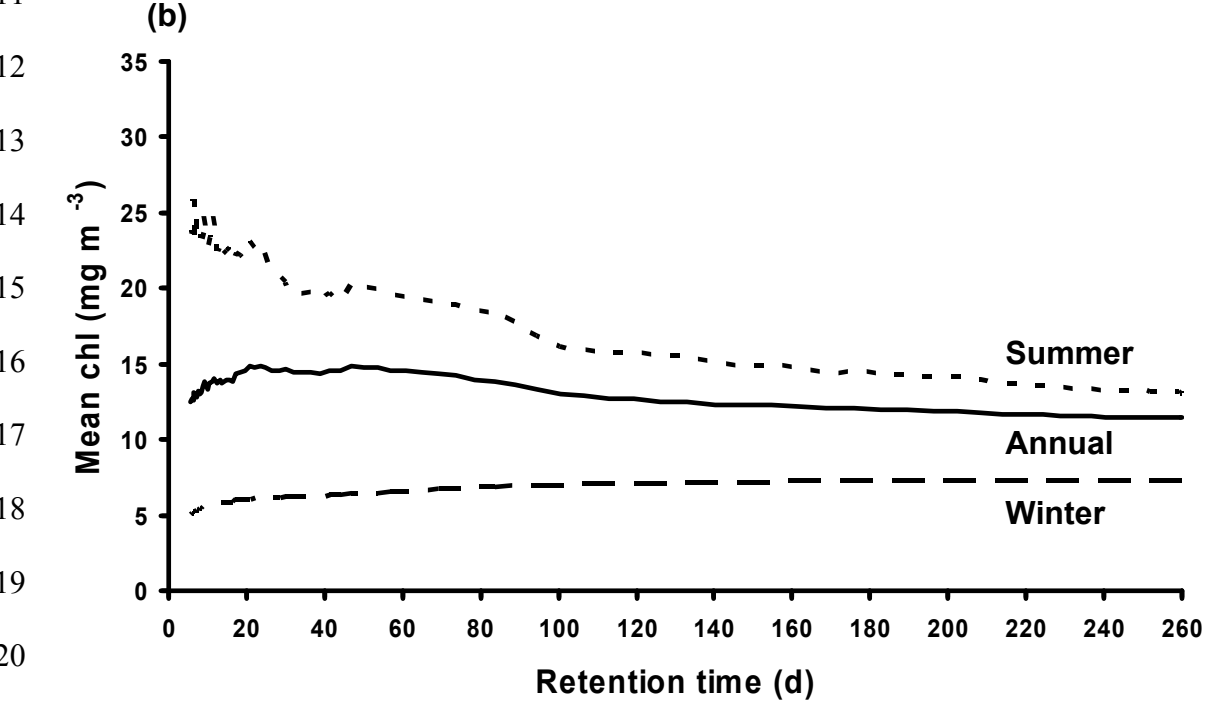
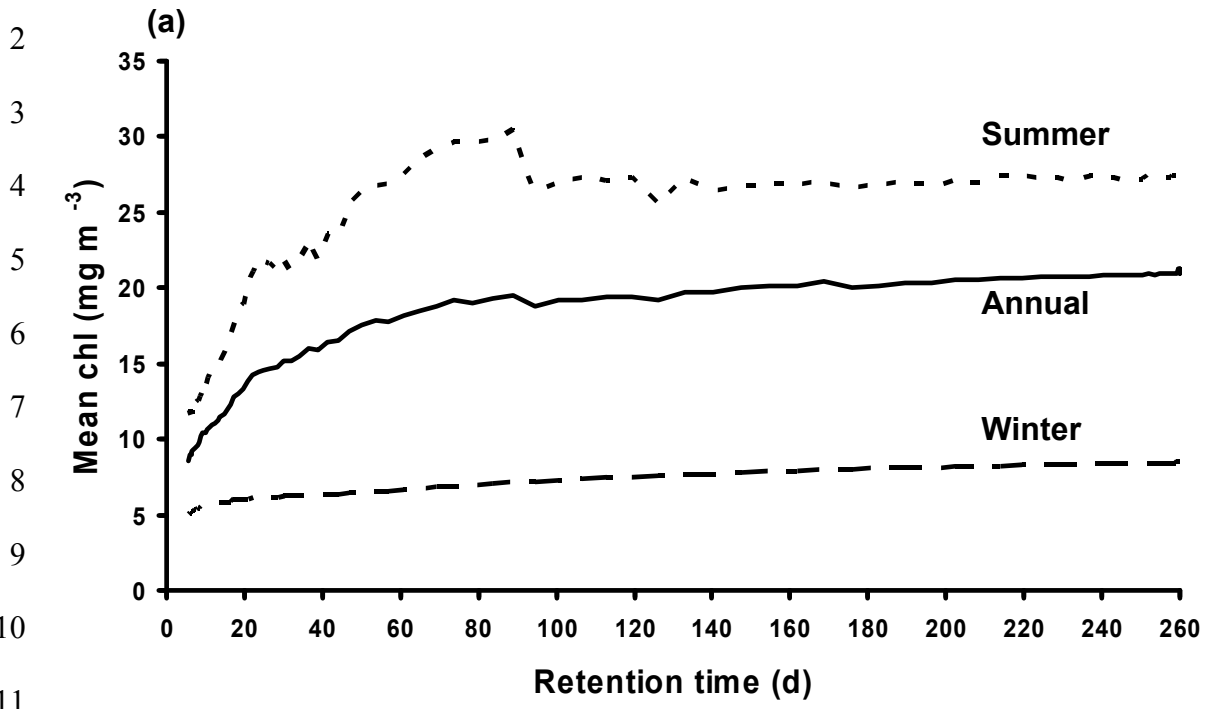
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1 **Fig. 3**



1 Fig. 4 (In colour)

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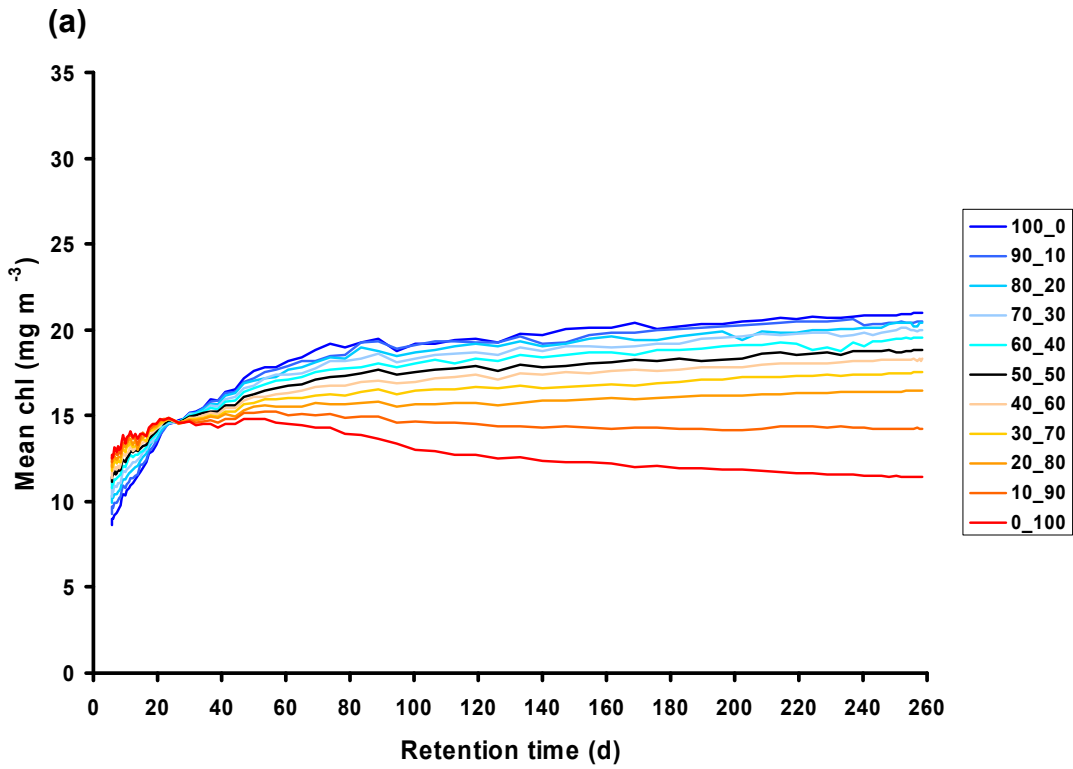
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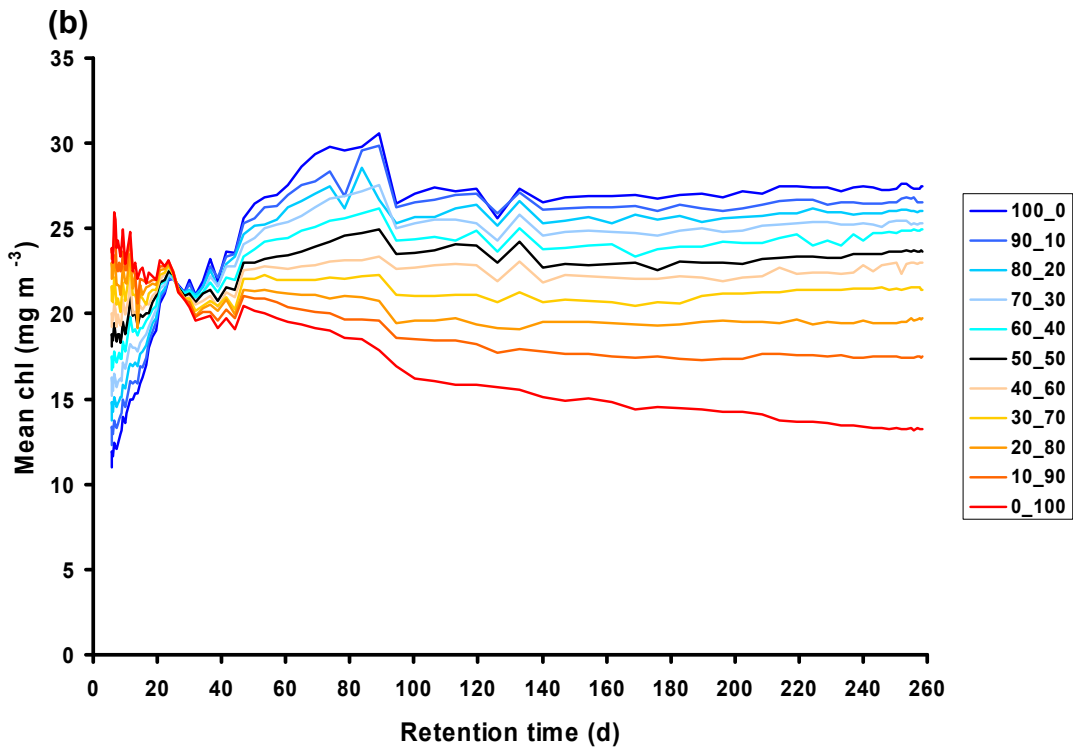
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1 Fig. 5

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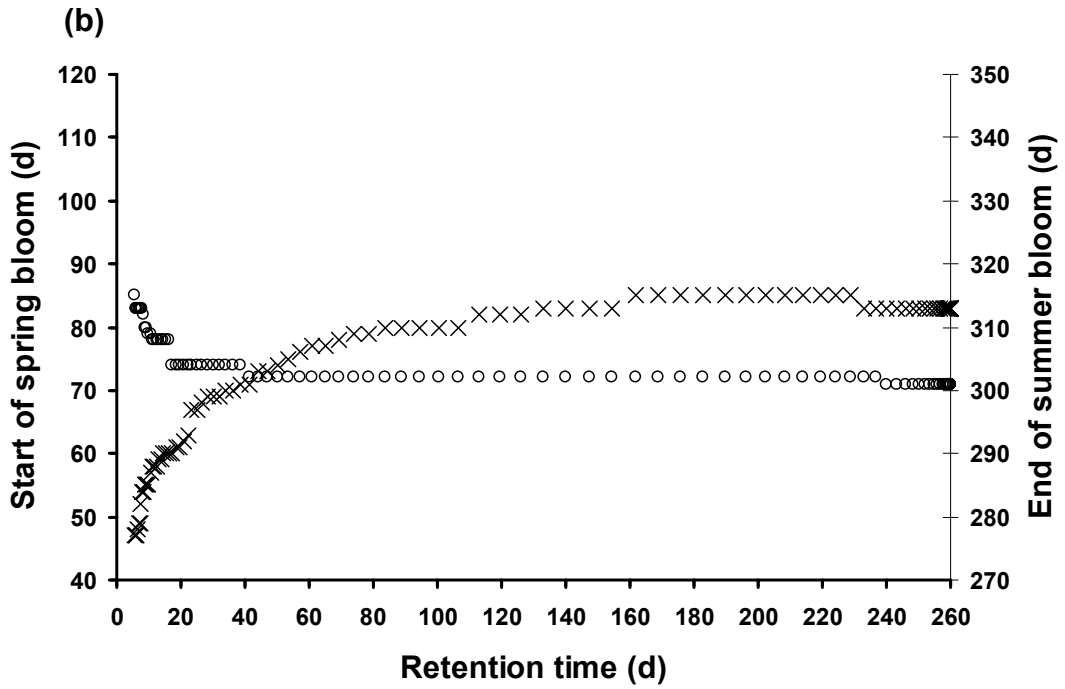
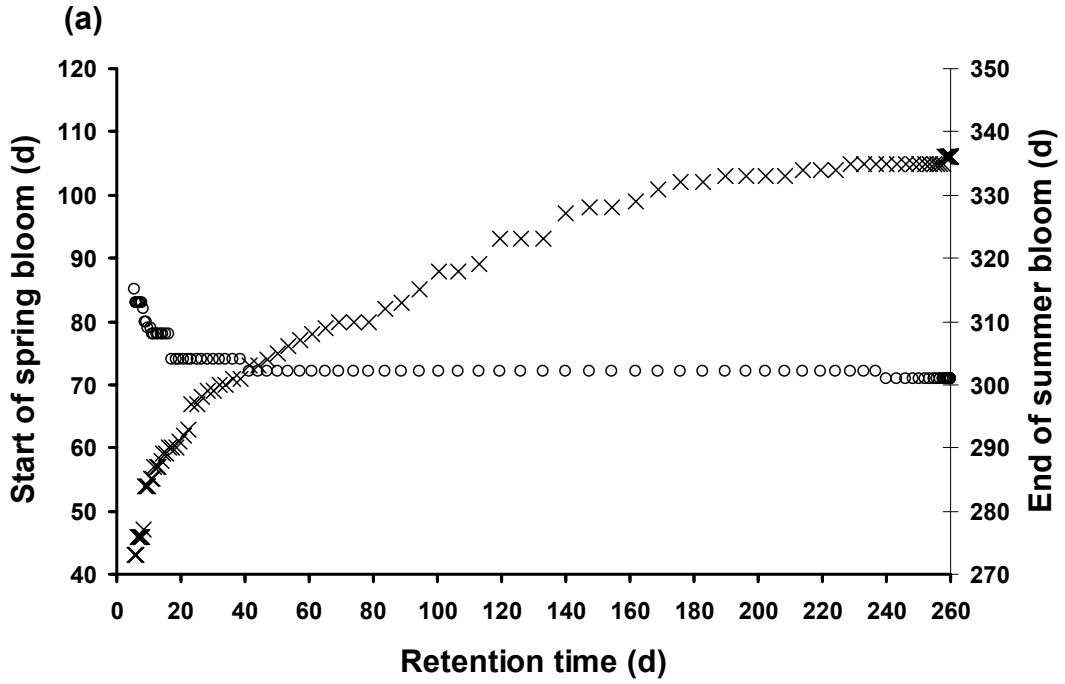
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1 **Fig. 6**

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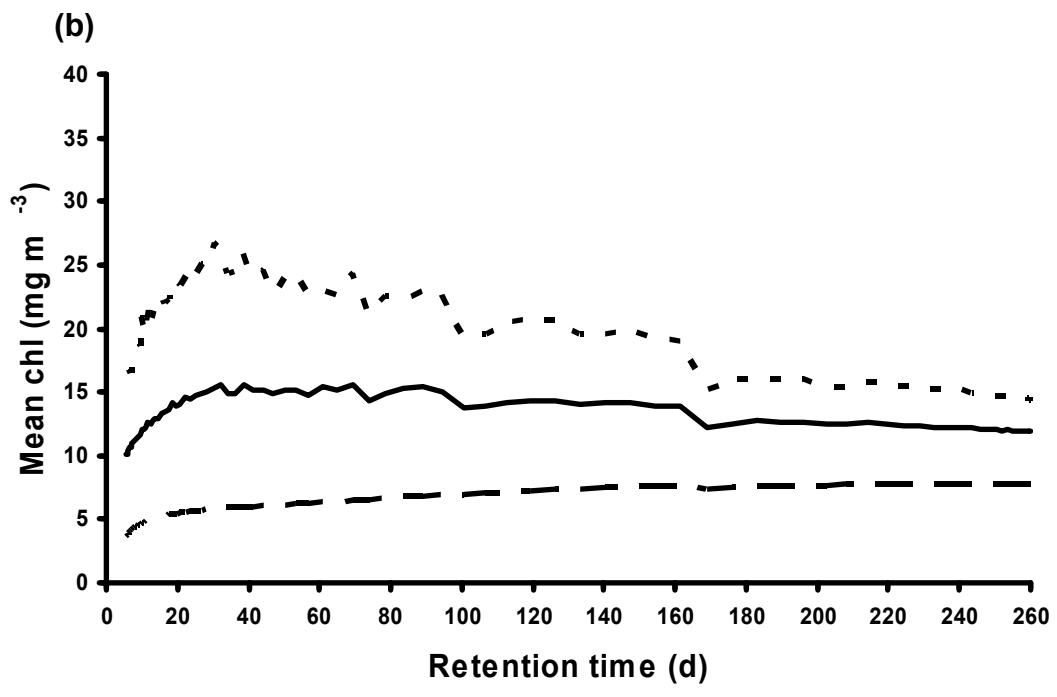
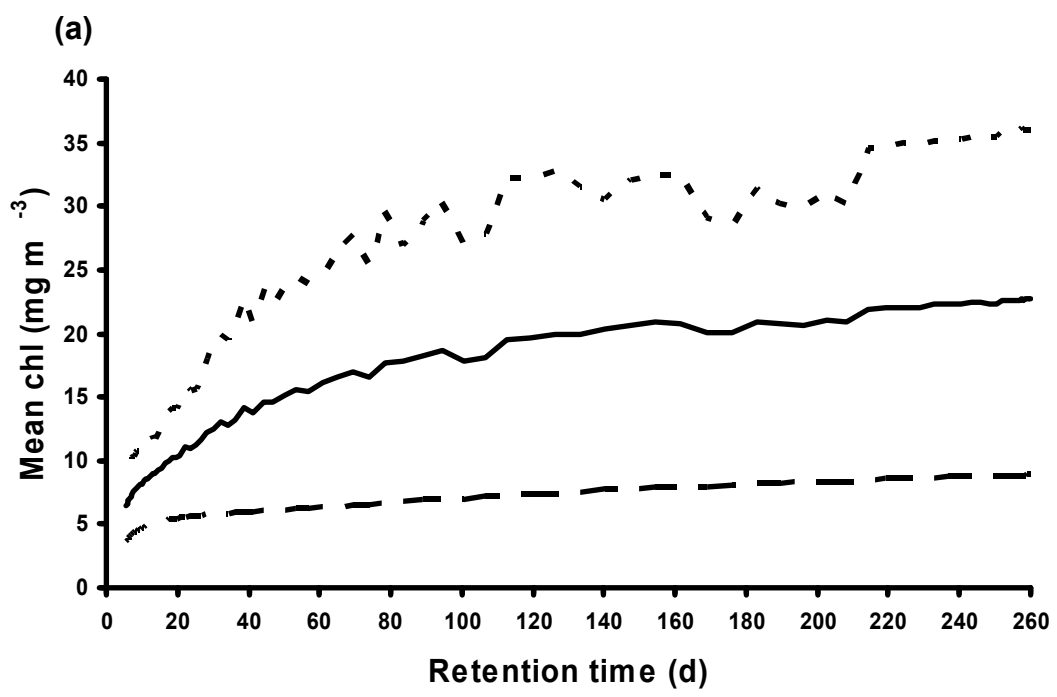
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1 Fig. 7 (In colour)

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