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A systematic review of machine learning models for groundwater level prediction

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ABSTRACT

This study presents a comprehensive synthesis of machine learning (ML) techniques applied to groundwater level (GWL) prediction, focusing on model architectures, feature selection methods, hyperparameter tuning, optimization algorithms, and clustering techniques. A total of 223 peer-reviewed articles were systematically reviewed using the PRISMA framework to guide study identification, inclusion, and exclusion. Widely used models include artificial neural networks (ANN), support vector machines (SVM), long short-term memory networks (LSTM), and random forests (RF). More recent studies increasingly employ hybrid approaches that integrate wavelet transforms, signal decomposition, and optimization techniques such as particle swarm optimization (PSO), genetic algorithms (GA), and ant colony optimization (ACO). Transformer-based models have also begun to emerge as promising tools in this domain. A central focus of this review is feature selection, which remains one of the most underdeveloped areas in GWL modeling. Most studies rely on simple filter methods like autocorrelation and mutual information. While SHapley Additive exPlanations (SHAP) has gained some traction, more advanced techniques, such as recursive feature elimination (RFE), forward feature selection (FFS), factor analysis (FA), and self-organizing maps (SOM), are rarely used. Notably, no study systematically compared multiple feature selection strategies, limiting insights into their impact on model performance. Scientometric analysis shows that Iran, China, India, and the United States contribute the most impactful research. Despite strong predictive outcomes, trial-and-error remains the dominant approach to hyperparameter tuning. The review emphasizes the need for more systematic, interpretable, and generalizable ML approaches to support robust groundwater level (GWL) forecasting.

1. Introduction

Groundwater is a critical global resource that supplies clean water to more than two billion people (Famiglietti, 2014). However, increasing demand and unsustainable exploitation, particularly in developing regions, have strained aquifers, with projections indicating that nearly 20% are already overexploited and most could face the same fate by 2050 (Piesse, 2020). Groundwater levels (GWL), the depth from the surface to the saturated zone, are vital indicators of aquifer health and are measured through monitoring wells. Analyzing GWL fluctuations is

crucial for managing groundwater resources amidst growing demand and climate change impacts (Butler et al., 2013).

Traditional groundwater modeling often relies on conceptual or physically based models such as MODFLOW and HydroGeoSphere (Brunner and Simmons, 2012; Chakraborty et al., 2020; Dehghani et al., 2022). These physically based models require extensive data on aquifer properties like transmissivity, hydraulic conductivity, and recharge rates, datasets that are frequently unavailable in data-scarce or poorly instrumented regions. Machine learning (ML) has emerged as a robust alternative for modeling GWL dynamics due to its ability to learn

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complex, non-linear relationships directly from observed data (Nourani et al., 2011; Kalu et al., 2022; Maiti and Tiwari, 2014). A wide array of ML techniques, ranging from traditional methods like Support Vector Machines (SVMs) and Artificial Neural Networks (ANNs) to deep learning architectures such as Long Short-Term Memory (LSTM) and Deep Belief Networks (DBNs), have been deployed with promising results. For instance, Nourani et al. (2011) used a hybrid ANN model to predict GWLs in East Azerbaijan, Iran, while Kalu et al. (2022) applied a DBN to model groundwater fluctuations in southern Africa.

While our focus is on ML for GWL forecasting, ML has also been increasingly applied in related domains such as groundwater potential mapping and vulnerability assessment (e.g., delineating recharge zones using ML-MCDM models (Kanji and Das, 2025) and improving DRASTIC-based vulnerability indices (Dasgupta et al., 2024)). In parallel, non-ML statistical and GIS-based methods have also been employed for groundwater stress mapping, such as the GIS-statistical workflows presented by John and Das (2020) and John et al. (2023). Together, these applications highlight the breadth of data-driven approaches being explored in hydrogeology.

However, despite these advances, ML applications in GWL modeling still face critical limitations. Overfitting, underfitting, and poor generalization, particularly in deep learning frameworks, remain recurring issues, often exacerbated by the inclusion of noisy or irrelevant input features (Kuhn et al., 2013a; Sharghi et al., 2022). This highlights the vital role of feature selection: identifying a minimal yet informative subset of input variables that preserves predictive performance while reducing model complexity. Inadequate feature selection not only inflates computational costs, but can also obscure physical interpretability and worsen generalization in unseen conditions.

In other scientific fields such as genomics, remote sensing, and finance, systematic feature selection has been shown to substantially improve model performance and transparency (Pudjihartono et al., 2022; Dokeroglu et al., 2022; Iranzad and Liu, 2024). However, in GWL modeling, no prior review has comprehensively examined the methodologies and implications of feature selection despite its proven importance. Existing reviews in hydrology and groundwater modeling (Solomatine, 2006; Wu et al., 2014; Rajaee et al., 2019; Tao et al., 2022; Boo et al., 2024) tend to provide broad overviews of machine learning applications but often overlook critical methodological aspects. Specifically, they do not categorize or analyze feature selection methods, rarely discuss how time lags are determined, and do not distinguish between filter, wrapper, and embedded feature selection approaches.

To address this critical gap, this review provides a systematic and detailed assessment of ML-based groundwater level modeling, with a specific emphasis on the role of feature selection, model architecture, optimization strategies, and hyperparameter tuning. Using the PRISMA framework, we analyze recent peer-reviewed studies to identify trends, innovations, and research gaps.

This review is guided by the following core inquiries:

- What are the most commonly employed ML models in GWL modeling?
- 2. What strategies are used for feature selection, and how do they affect model performance?
- 3. How are model architectures structured and optimized in current research?
- 4. How are hyperparameters selected and tuned across different ML models?

By focusing on these aspects, our review not only synthesizes existing knowledge but also provides actionable insights into constructing more reliable, interpretable, and efficient models for GWL prediction. Unlike prior reviews that focus broadly on ML adoption in hydrology, our work uniquely foregrounds feature selection as a methodological pillar, setting a new benchmark for future research in this domain. We

do not delve into the mathematical derivations of the models; instead, we focus on their design principles, input structuring, optimization strategies, and performance implications, offering practical value to both researchers and practitioners.

2. Methodology

This systematic review adopts the PRISMA framework (Liberati et al., 2009; Page et al., 2021) to ensure a comprehensive, unbiased evaluation of the research literature. Following the PRISMA flow diagram, we minimized researcher bias and maintained a traceable review process.

The review aimed to identify the most common ML models used for GWL prediction, methods to determine optimal input variables, and techniques to fine-tune key hyperparameters to enhance model performance. Through this exploration, we sought to provide insights into factors influencing the accuracy of GWL predictions.

Key stages of the systematic review process included identification, screening, eligibility assessment, and full-text evaluation, as outlined in Fig. 1. By adhering to the PRISMA methodology, we ensured transparency, rigor, and replicability, enabling a thorough analysis of the existing literature and meaningful conclusions.

- 1. Identification: Following the PRISMA conceptual framework, our systematic review utilized a comprehensive search strategy to capture relevant articles from prominent electronic databases, including Scopus, Science Direct, and Google Scholar. The search was limited to English-language publications between 2010 and 2024, aiming to examine the contemporary applications of ML models in predicting groundwater levels and availability. The search strategy employed a carefully designed search string, incorporating specific terms such as ("groundwater level prediction" OR "water table prediction") AND ("machine learning" OR "artificial intelligence" OR "AI") AND (forecasting OR modeling). In total, our search yielded 426 articles in all selected databases, demonstrating the wide scope of literature available on this topic. The details of the search string can be found in Table 1.
- 2. **Screening**: Following the identification of relevant publications, key metadata, including title, keywords, abstract, DOI, publication year, and author names, was extracted and recorded in a Microsoft Excel spreadsheet. All articles were imported into Mendeley, a reference management software used to streamline literature organization and deduplication (Mendeley, 2022). After removing 68 duplicate records, 358 articles were retained for screening. These articles were evaluated against predefined inclusion and exclusion criteria, resulting in the exclusion of 62 papers whose titles or abstracts were determined to be out of scope. To ensure objectivity and consistency, two independent reviewers assessed the eligibility of the remaining articles. In cases of disagreement or ambiguity, article titles were discussed with external experts in groundwater or machine learning research. Final inclusion decisions were based on consensus between reviewers or expert resolution when needed.

3. Eligibility criteria

Studies were included if they:

- (a) Focused on the application of machine learning algorithms for simulating groundwater levels and availability.
- (b) Employed meteorological parameters as inputs in the models.
- (c) Reported original research (e.g., case studies, simulations, empirical analyses) with sufficient methodological detail and performance metrics.
- (d) Were published in peer-reviewed journals in English between 2010 and 2024.

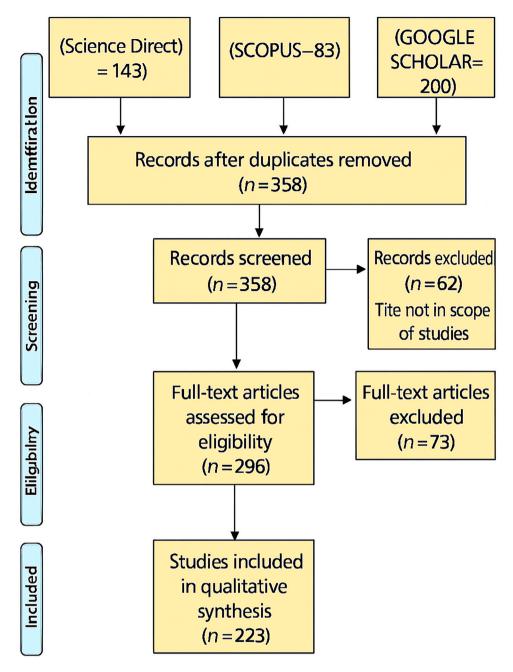


Fig. 1. The PRISMA workflow diagram.

Studies were excluded if they:

- (a) Relied solely on traditional statistical or physically based models without ML components.
- (b) Were secondary sources (reviews, editorials, opinions, conference abstracts, or book chapters).
- (c) Did not provide sufficient methodological or results information to assess model development and performance.

3. Results and discussion

3.1. Publication trends

As shown in Fig. 2, the application of ML for GWL prediction has seen a marked upward trend, particularly after 2019. Between 2010

and 2018, annual publication counts remained relatively modest, fluctuating between 2 and 13 papers per year and collectively accounting for less than 30% of the total reviewed studies. However, from 2020, research activity intensified significantly. In 2022 alone, 34 studies were published, representing approximately 15.1% of all 223 studies reviewed, while 2023 saw a comparable count of 39 papers (17.5%), and 2024 (year-to-date) currently leads with 43 publications (19.3%). This steady growth reflects a growing academic and practical interest in leveraging ML techniques to address groundwater-related challenges. These findings align with recent bibliometric reviews (Afrifa et al., 2022; Tao et al., 2022; Ahmadi et al., 2022; Boo et al., 2024), which also report a sharp increase after 2020 in data-driven groundwater modeling studies. Fig. 3 presents the distribution of total and average citations among the top academic publishers that contribute to the groundwater level (GWL) modeling literature. Elsevier emerged as the most influential publisher, with a total of 3191 citations, resulting in

Table 1 The detailed search query.

Search query

TITLE-ABS-KEY ("roundwater AND level AND prediction" OR "groundwater AND level AND forecasting" AND "machine AND learning") AND PUBYEAR > 2009 AND PUBYEAR ≤ 2024 AND (EXCLUDE (LANGUAGE, "Chinese") OR EXCLUDE (LANGUAGE, "Korean")) AND (LIMIT-TO (EXACTKEYWORD, "Forecasting") OR LIMIT-TO (EXACTKEYWORD, "Groundwater") OR LIMIT-TO (EXACTKEYWORD, "Machine Learning") OR LIMIT-TO (EXACTKEYWORD, "Groundwater Resources") OR LIMIT-TO (EXACTKEYWORD, "Artificial Neural Network") OR LIMIT-TO (EXACTKEYWORD, "Rain") OR LIMIT-TO (EXACTKEYWORD, "Hydrology") OR LIMIT-TO (EXACTKEYWORD, "Groundwater Level Fluctuation") OR LIMIT-TO (EXACTKEYWORD, "Aquifer") OR LIMIT-TO (EXACTKEYWORD, "Evaporation"))

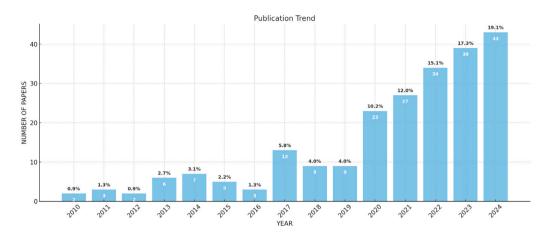


Fig. 2. Trends in publications within the reviewed articles from 2010 to 2024.

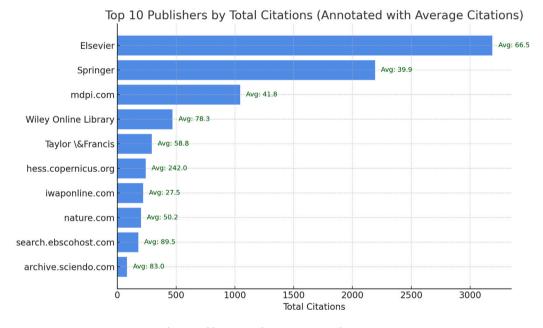


Fig. 3. Publication outlet average normal citations.

an average of approximately 66.5 citations per study. Springer accumulated 2192 citations with an average of 39.9 citations per article. MDPI followed with 1045 total citations (41.8 average citations per study). Wiley Online Library, while contributing fewer studies (6), achieved a higher average impact with 78.3 citations per article, indicating a strong influence relative to volume. Taylor & Francis, IWA Publishing (iwaponline.com), and Nature also demonstrated moderate to high average citation metrics. Notably, some specialized or lower-volume platforms such as Copernicus (hess.copernicus.org) and EBSCOhost showcased high average citations per article, although based on limited publication counts.

Our systematic review analyzed 223 articles, revealing distinct authorship patterns and geographic distribution. Iran led with 39% of

publications, followed by China (24%) and the United States (13%), as shown in Fig. 4. Many studies in Iran address its dependence on groundwater due to limited surface water resources, highlighting concerns about the depletion of aquifers (Sharafati et al., 2020; Motagh et al., 2017; Milan et al., 2023; Arabameri et al., 2019; Moravej et al., 2020). In general, Asia dominated the research landscape, contributing 81.24% of the studies. In contrast, the use of ML for groundwater modeling in Africa remains underrepresented, with little literature highlighting a significant research gap in applying ML techniques to groundwater dynamics on the continent. Fig. 4 summarizes the geographical distribution. Fig. 5 presents a country-level co-authorship and a normalized citation network derived from VOSviewer. The graph reveals clear regional and international collaboration clusters, with India,

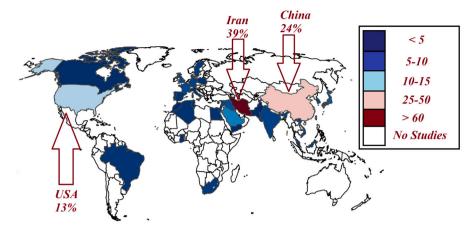


Fig. 4. Distribution of the reviewed papers based on the country of origin.

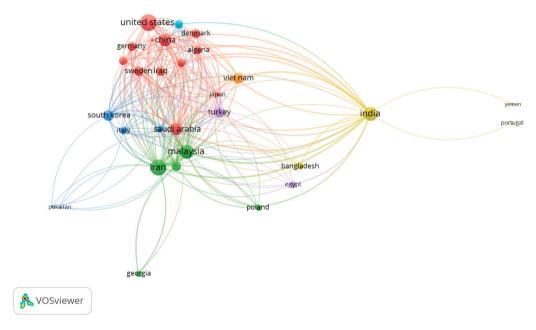


Fig. 5. Country-level co-authorship and normalized citation network for studies on machine learning-based groundwater level modeling, generated using VOSviewer.

Iran, and Malaysia serving as major hubs. In particular, India forms a distinct cluster of cooperation with countries such as Portugal, Yemen, and Bangladesh, while Iran exhibits strong ties within the Middle East and Central Asia. The United States and China are central to a western collaboration cluster, linking with Germany, Sweden, and Algeria. The size of the node reflects the strength of the citation, indicating that countries such as the United States, Iran, China, and India not only publish frequently, but also produce highly cited research in GWL modeling.

3.2. Algorithms used in groundwater level prediction

This review explores techniques for predicting GWL, with a focus on the most widely applied machine learning algorithms. As illustrated in Fig. 6, five dominant models: ANN (51%), SVM (13%), LSTM (12%), tree-based ensembles (8%) and ANFIS (5%) collectively account for 89% of the models reviewed. These approaches have been used independently and in hybrid configurations in diverse case studies. The

following sections critically examine methodological elements including feature selection, model design, data pre-processing, and parameter tuning.

3.3. ANN (Standalone and hybrid) models

3.3.1. Bibliographic review

Experts worldwide have conducted numerous studies on groundwater level prediction across various geographical regions using ANNs, and these studies have consistently reported the efficacy of these models. For example, Dash et al. (2010) developed a hybrid ANN-GA (Genetic Algorithm) model to predict GWLs in the Mahanadi River Basin, India, outperforming standalone ANN models trained with Levenberg–Marquardt (LM), gradient descent, and Bayesian Regularization (BR) algorithms. Hyperparameters and activation functions were optimized via trial and error, with the hybrid model demonstrating superior predictive performance. Chen et al. (2010) employed self-organizing maps (SOM) to predict GWLs in the Zhuoshuixi River Basin, Taiwan, using single-site and multisite models. ACF and PACF determined input

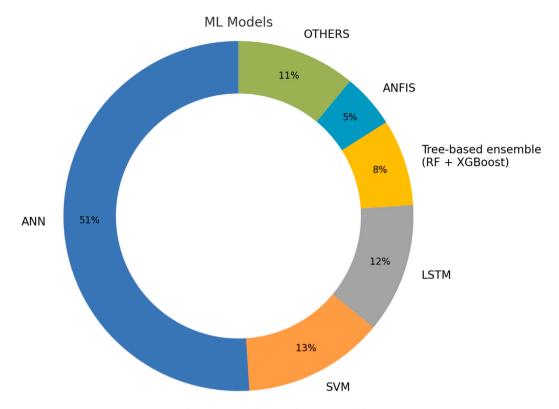


Fig. 6. ML models utilized in GWL modeling.

features, and the multisite model outperformed single-site configurations. Building on this, Chen et al. (2011) combined SOM with backpropagation networks (BPN), developing six models. The improved multisite SOM-BPN model outperformed ARIMA and single-site ANN models. Rakhshandehroo et al. (2012) compared FFNN, Radial Basis Function (RBF), Elman (ELNN), and generalized regression neural networks (GRNN) for monthly GWL prediction in the Shiraz plain, Iran. All models performed effectively, with FFNN achieving the best results. Adamowski and Chan (2011) integrated ANN with discrete wavelet transform (DWT) for GWL forecasting in the Chateauguay watershed, Quebec. DWT decomposed time series data, and the WA-ANN model, trained with the LM algorithm, outperformed standalone ANN and ARIMA models.

Nourani et al. (2011) integrated ANN and geostatistics to predict GWL in eastern Azerbaijan, Iran. Sensitivity analysis guided input selection, and FFNNs with optimized hidden neurons, trained using the LM algorithm, achieved superior performance. Taormina et al. (2012) applied FFNNs for hourly GWL simulations in the Lagoon of Venice, Italy, utilizing AutoRegressive with eXogenous inputs (ARX) models and the Akaike Information Criterion for input selection. Optimized via trial and error, the models effectively simulated GWL over extended periods.

A few years after Chen et al. (2010) used SOM for determining hidden layer neurons in RBFN models, Nourani et al. (2015) combined SOM-based clustering and wavelet transform (WT) to model one- and multi-step-ahead GWLs in the Aradabil plain, Iran. SOM identified homogeneous clusters, and WT extracted multi-scale features from non-stationary GWL, runoff, and rainfall time series. The FFNN model, trained via backpropagation with feature selection and lagged values guided by mutual information (MI), demonstrated improved accuracy and reduced model complexity. Bahaa et al. (2015) compared MLR, ANN, wavelet MLR, wavelet ANN, and a wavelet ensemble ANN for GWL forecasting in Quebec, Canada. The "a Trous" wavelet transform was used for de-noising, and MI guided feature selection. The wavelet ensemble ANN consistently outperformed other models across all lead

times. Chang et al. (2015) developed ANN models to simulate suprapermafrost GWLs in the Qinghai-Tibet Plateau, China, using two and three input variable configurations. A three-layer feedforward network trained with the LM algorithm showed higher accuracy with three inputs, while the two-input model performed reasonably well without field GWL data.

Gholami et al. (2015) used a multilayer perceptron (MLP) network with dendrochronology and precipitation data to simulate GWLs in the Caspian Sea's alluvial aquifer (1912–2013). A standard three-layer feedforward neural network, trained using LM backpropagation, showed that the sigmoid transfer function provided the best results during the growing season.

Sun et al. (2016) employed a standard FFNN with a quasi-Newton training algorithm to predict GWLs in a swamp forest in Singapore. Inputs included reservoir levels and rainfall. Using logistic and threshold activation functions, the ANN achieved accurate forecasts up to 7 days ahead, though performance decreased with longer lead times.

Choubin and Malekian (2017) compared ANN and ARIMA models for simulating GWLs in Iran's Shiraz basin using precipitation, streamflow, temperature, evaporation, and GWL data. The LM algorithm trained the ANN with logistic-sigmoid and purelinear activation functions. ARIMA outperformed ANN based on the evaluation metrics. Wen et al. (2017) also compared a wavelet analysis-based ANN (WA-ANN) with a traditional ANN model for forecasting GWLs in an arid inland river basin in northwestern China. Input variables included GWLs, total precipitation, evaporation, and average temperature. Both models used a three-layer architecture with a single-neuron output layer, sigmoid activation for hidden layers, and a linear activation for the output layer. The WA-ANN consistently outperformed the traditional ANN model across all evaluation metrics.

Sahoo et al. (2017) developed a hybrid artificial neural network (HANN) model for GWL prediction, incorporating innovative covariate processing methods. Singular spectrum analysis decomposed time series data, while mutual information and genetic algorithms identified key components. The model used logistic sigmoid and linear activation

functions in a single hidden layer, optimized through trial and error, and trained with the LM algorithm. HANN outperformed hybrid linear and nonlinear regression models. Similarly, El Ibrahimi et al. (2017) integrated DWT with ANN-PMC for GWL prediction in Morocco, using a three-layer architecture with precipitation, temperature, and GWLs as covariates. Systematic parameter optimization showed the DWT-ANN-PMC model exceeded standalone ANN-PMC and MLR models in accuracy.

Guzman et al. (2017) used the Nonlinear autoregressive exogenous model (NARX) network to predict daily groundwater levels (GWLs) in the Mississippi River Valley Alluvial (MRVA) aquifer in the southeastern United States. The model, trained with both LM and BR algorithms, used precipitation and GWL as covariates. Sensitivity analysis identified historical GWL and precipitation as key variables. The optimal network consisted of two hidden nodes with sigmoid transfer functions and one output node with a linear function. The NARX-BR model achieved the highest predictive accuracy among the tested models. Wunsch et al. (2018) employed the NARX model for GWL prediction in southwest Germany, identifying influential time lags using STL decomposition and auto/cross-correlation. The study demonstrated NARX's accuracy and adaptability for GWL modeling. Similarly, Kouziokas et al. (2018) implemented multilayer FFNN models with varying architectures to forecast GWLs in Montgomery County, Pennsylvania. Using the LM algorithm with Tanh-Sigmoid transfer functions in hidden layers, the models achieved optimal predictive performance compared to other training algorithms and transfer functions.

A year later, Lee et al. (2019) developed FFNN models to predict GWLs in South Korea's Yangpyeong riverside area. Correlation analysis identified surface water level as the most influential covariate. The models used logistic-sigmoid and linear activation functions in the hidden and output layers, respectively, and were trained using backpropagation, achieving strong predictive performance. Chen et al. (2020) compared MLP, RBF, MODFLOW, and SVM models for GWL prediction in the Heihe River Basin. The MLP employed a single hidden layer with optimized neurons, using backpropagation and gradient descent. Results showed that SVM and RBF outperformed MODFLOW in accuracy. Banadkooki et al. (2020) assessed RBF neural networks with Whale Algorithm (WA), MLP-WA, and GP models for GWL prediction in Yazd-Ardakan, Iran. Cross-correlation and partial autocorrelation guided feature selection, with MLP-WA demonstrating superior predictive performance. Similarly, Yadav et al. (2020) combined singular spectrum analysis (SSA), MI, GA, ANN, and SVM models to analyze groundwater fluctuations in India, considering climatic and non-climatic factors. Hybrid models (SSA-MI-GA-ANN and SSA-MI-GA-SVM) consistently outperformed standalone models.

Müller et al. (2021) compared LSTM, MLP, RNN, and CNN models for GWL prediction in Butte County, California, using surrogatebased algorithms and random sampling for hyperparameter tuning. MLP, optimized with ADAM and ReLU activation, outperformed the other models, emphasizing the importance of precise hyperparameter tuning. Sharghi et al. (2022) evaluated FFNN, ANFIS, LSTM, and GMDH models for multi-step GWL forecasting in Iran. Pre- and postprocessing techniques like COMUSA and NAE improved accuracy, with GMDH outperforming others, highlighting the benefits of clustering and ensemble approaches. Yin et al. (2021) introduced a Bayesian ensemble model integrating ANN, SVM, and Response Surface Regression (RSR) to predict groundwater storage fluctuations. The ANN model, trained with the LM algorithm, demonstrated low uncertainty, particularly at sub-regional scales. Bayesian model averaging provided the most accurate predictions. Kalu et al. (2022) utilized a Deep Belief Network (DBN) to simulate monthly GWLs in southern Africa, using hydrological variables and global climate indices. Variable selection employed correlation analysis, and the architecture was optimized through trial and error. Results highlighted DBN's efficacy in GWL prediction. Collados-Lara et al. (2023) applied NAR, NARX, and Elman Neural Networks for short-term GWL prediction in Spain. Effective

precipitation emerged as a key predictor, with NARX and Elman Neural Networks outperforming others. Van Thieu et al. (2023) proposed the Augmented Artificial Ecosystem Optimization-based Multi-Layer Perceptron (AAEO-MLP) model for monthly GWL prediction in India, using ELU activation and mutual information for input selection. The AAEO-MLP consistently outperformed other MLP models. Panahi et al. (2023) compared Radial Basis Function Neural Network (RBF), ANFIS, SVM, and MLP for GWL prediction under future climate conditions in Iran. RBFNN exhibited superior performance, proving reliable for climate-related GWL forecasts. Wei et al. (2023a) proposed a hybrid WT-PSR-ANN model for GWL forecasting by combining wavelet decomposition, phase space reconstruction (PSR), and ANN. GWL time series were decomposed using three types of mother wavelets, and PSR was applied to select relevant sub-series as input. Lyapunov exponent analysis confirmed chaotic behavior in the data. The WT-ANN outperformed standard ANN, while WT-PSR-ANN yielded the best results overall. The study highlighted PSR as a valuable enhancement to wavelet-based preprocessing for improving model accuracy. Ghafoor et al. (2024) applied autoregressive moving average (ARIMA) and ANN models to predict GWLs across four wells in Cheyenne and Delta counties, Colorado. USA. Monthly GWL data were preprocessed via interpolation and up-sampling to enhance model training. The ANN employed a feedforward architecture with rectified linear unit (ReLU) and linear activation functions. Model evaluation revealed that ANN consistently outperformed ARIMA in accuracy across all sites. This result was attributed to ANN's robustness against nonlinearity and noise, making it more adaptable to the irregular GWL fluctuations observed. Fahim et al. (2024) evaluated MLR, SVM, Gaussian process regression (GPR), regression trees, bagged and boosted ensembles, and ANN models for GWL prediction in Bangladesh. Weekly GWL observations, with missing values addressed using cubic spline interpolation. Inputs included Global Land Data Assimilation System (GLDAS) groundwater storage, rainfall, temperature, elevation, irrigation, population, and GRACE-based water storage variability. ANN performed best, effectively modeling spatial groundwater variability. Seifi et al. (2024) proposed a hybrid BFSA-MVMD-GRU-RVM model for GWL prediction in Iran's Bastam Plain. Boruta was used for feature selection, multivariate variational mode decomposition (MVMD) for decomposition, gated recurrent unit (GRU) for sequence learning, and relevance vector machine (RVM) for prediction. Inputs included lagged rainfall, temperature, pumping, irrigation return flow, and humidity. The model outperformed other MVMDbased models and showed reduced prediction uncertainty across shortto long-term forecasts. Moradi et al. (2023) compared a numerical model (GMS) with AI models including GA-ANN, ICA-ANN, Extreme Learning Machine (ELM), Outlier Robust ELM (ORELM), and Group Method of Data Handling (GMDH) for predicting GWL in the Lur Plain, Iran. Initial inputs were GWL, rainfall, temperature, and evaporation, but only GWL was retained due to stronger correlations. ORELM outperformed all other models and the numerical approach. Model evaluation used RMSE, NRMSE, NASH, R, and a Taylor diagram. Abdi et al. (2024) applied CNN and DNN models for GWL prediction in Iran, using 34 wells. Missing data were handled via interpolation (Kriging, SVM, M5P), with M5P proving most accurate. Inputs included spatial coordinates and groundwater levels. CNN outperformed DNN across scenarios, especially when interpolated data were used to expand input coverage. Ghafoor et al. (2024) applied ARIMA and ANN models to forecast GWL at four wells in Colorado, USA. Auto-ARIMA identified optimal parameters for ARIMA. A feedforward ANN with one hidden layer used Adam optimizer and ReLU activation. ANN consistently outperformed ARIMA across all wells. Despite data limitations and a small number of wells, both models showed effectiveness for GWL prediction. Seidu et al. (2023) evaluated four ANN models (BPNN, RBFNN, GRNN, GMDH) for groundwater level prediction using data from 13 boreholes in Ghana. Input features included rainfall, evaporation, and temperature. Min-Max normalization was applied, and model performance was assessed across five train-test splits (90-10

to 50-50). The 70-30 and 80-20 splits produced the most accurate predictions. RBFNN performed best in six out of thirteen boreholes. Akbari Majd et al. (2024) developed ANN-based models hybridized with three metaheuristic algorithms (Particle Swarm Optimization (PSO), Genetic Algorithm (GA), Ant Colony Optimization (ACO)) to predict GWL in Iran's Ardabil Plain. Unlike most studies, historical GWL was not used. Inputs included rainfall, temperature, runoff, and discharges. Three preprocessing stages were tested, with Stage 3 involving time series decomposition (trend, seasonality removal) showing the best performance. ANN-GA performed best for some wells, ANN-PSO for others. Overall, Stage 3 improved prediction accuracy by 76%, making the method suitable for data-scarce basins. Feng et al. (2024) evaluated decision tree (DT), RF, SVM, convolutional neural network (CNN), recurrent neural network (RNN), and generative adversarial network (GAN) models for GWL prediction in Izeh City, Iran. The study used extraction rate, rainfall, and river flow as inputs. Feature importance was assessed using Pearson and Spearman correlation, revealing that river flow and extraction had stronger associations with GWL than rainfall. CNN outperformed other models, demonstrating robustness and high accuracy in capturing groundwater fluctuations.

Refer to supplementary information for a detailed description of ANN.

3.3.2. Results

Based on the reviewed papers, we found that

- 1. The Levenberg–Marquardt (LM) algorithm emerged as the primary optimization method for training ANN models, often enhanced with Bayesian Regularization to improve generalization. The Backpropagation algorithm was utilized to compute gradients for weight updates. The LM algorithm is recognized for its computational efficiency, balancing Newton's method, which converges rapidly near minima but risks divergence, with gradient descent, which ensures convergence but at a slower rate if step sizes are chosen carefully (Tyagi et al., 2022). Researchers have highlighted the LM method's computational advantages and its reduced likelihood of becoming trapped in local minima, making it a robust and effective choice for training ANN models (Daliakopoulos et al., 2005).
- 2. A typical ANN structure consists of three layers, incorporating the sigmoid activation function in the hidden layer and a linear activation function in the output layer. Some studies also employed ReLU and ELU. Notably, in most of the reviewed papers, the determination of the ANN structure, the number of hidden neurons, and hyper-parameter tuning were achieved using a trial-and-error approach. However, genetic programming (GP) was used for hyperparameter optimization in specific cases. The reported learning rates mainly ranged between 0.001 and 0.009, with the highest recorded as 0.01 (Emamgholizadeh et al., 2014).

Activation function plays a crucial role in the successful training of deep neural networks. It introduces non-linearity into the neural network model, enabling the network to learn more effectively by capturing and understanding the intricate non-linear patterns present in input datasets. Table 2 summarizes the general output range, along with some advantages and disadvantages of the various activation functions used in GWL modeling. Further details on these functions can be in the works of LeCun et al. (2015), Banerjee et al. (2019), Ramachandran et al. (2017), Jamel and Khammas (2012), Narayan (1997), Kalaiselvi et al. (2022), Ding et al. (2018), Nwankpa et al. (2018) and Rasamoelina et al. (2020)

 The selection of optimal input variables primarily relied on correlation analyses, including Partial Auto-correlation, Autocorrelation, and Cross-Correlation function. In some cases, MI

Table 2
Comparison of activation functions (LeCun et al., 2015; Banerjee et al., 2019; Ramachandran et al., 2017; Jamel and Khammas, 2012; Narayan, 1997; Kalaiselvi et al., 2022; Ding et al., 2018; Nwankpa et al., 2018; Rasamoelina et al., 2020).

Activation function	Sigmoid	Tanh	ReLU	ELU
Output range	(0, 1)	(-1, 1)	[0, ∞)	[−1, ∞)
Smooth gradient	Yes	Yes	No	No
Vanishing gradient issue	Yes	Yes	Yes (for negative inputs)	Reduced
Zero-centered output	No	Yes	No	Yes
Computational efficiency	Yes	No	Yes	No
Dying neurons problem	No	No	Yes	Reduced

was used to improve model performance through enhanced feature selection.

Auto-correlation gauges how similar a time series is to a lagged version of itself, helping spot repeating patterns or trends at different time points in the same series. Partial Auto-correlation is similar but removes the influence of intermediate lagged values.

Cross-correlation compares two different time series at the same time points, identifying relationships and potential lead–lag patterns between them.

MI quantifies the mutual information shared between two variables, offering an indirect means to identify pertinent time lags by evaluating information content across various temporal shifts (Van Thieu et al., 2023). Table 3 provides a summary of the formulas, advantages, and disadvantages of the feature selection methods employed. Further details on these methods can be found in the works (Kraskov et al., 2004; Veyrat-Charvillon and Standaert, 2009; Batina et al., 2011; Latham and Roudi, 2009; Bourke, 1996; Yoo and Han, 2009; Ramsey, 1974)

 Among the hybrid models, the combinations consistently yield optimal performance involving ANN coupled with WT.

3.4. ANFIS (Standalone and hybrid) models

3.4.1. Bibliographic review

When it comes to GWL modeling with Adaptive Neural Networks Fuzzy Inference Systems (ANFIS), Jalalkamali et al. (2011) evaluated the predictive performance of ANFIS and ANN models for groundwater level (GWL) prediction in two neighboring wells in Kerman Plain, Iran. Input variables included rainfall, air temperature, and GWLs. Hyperparameters for both models were optimized through trial and error, with the ANFIS model utilizing the Gaussian membership function (gaussmf). Performance evaluations indicated that ANFIS outperformed ANN in accuracy. Emamgholizadeh et al. (2014) compared ANFIS and ANN for GWL prediction in Bastam Plain, Iran, concluding that ANFIS, with trapezoidal input membership functions and a hybrid learning algorithm, consistently outperformed ANN. Similarly, Maiti and Tiwari (2014) evaluated ANN, Bayesian Neural Network (BNN), and ANFIS for modeling GWL fluctuations in Dindigul, Southern India. The study found ANFIS excelled with noise-free data, while BNN was more effective for noisy hydrological series. The following year, Mirzavand et al. (2015) evaluated the ANFIS model against the support vector regression (SVR) model for predicting monthly GWL fluctuations in the Kashan plain, Iran, concluding that ANFIS with a Bell-shaped MF outperformed SVR. Similarly, Gong et al. (2016) compared ANFIS to ANN and support vector machine (SVM) for forecasting GWLs near Lake Okeechobee, Florida. Input factors were selected using partial and autocorrelation coefficients, and models were tuned via trial-and-error. Results indicated that ANFIS and SVM consistently outperformed ANN.

Seifi et al. (2020) combined six meta-heuristic methods (e.g., grasshopper optimization algorithm (GOA), cat swarm optimization

Table 3
Comparison of feature selection methods employed for ANN (Kraskov et al., 2004; Veyrat-Charvillon and Standaert, 2009; Batina et al., 2011; Latham and Roudi, 2009; Bourke, 1996; Yoo and Han, 2009; Ramsey, 1974).

Method	Formula	Advantages	Disadvantages
Partial Autocorrelation (PACF)	$PACF(k) = \phi_{kk}$	 Measures the direct effect of a lagged variable Helps determine appropriate lag in time series models 	- Assumes linearity - Sensitive to noise and outliers
Autocorrelation (ACF)	$\rho_k = \frac{\text{Cov}(X_t, X_{t+k})}{\text{Var}(X_t)}$	- Detects repeating patterns and serial correlation - Easy to compute and interpret	Only captures linear dependence Can be misleading for non-stationary or non-linear data
Cross-Correlation (CCF)	$CCF(k) = \frac{Cov(X_t, Y_{t+k})}{\sigma_X \sigma_Y}$	- Identifies lead–lag relationships across variables - Useful in multivariate time series	- Does not account for indirect effects - Assumes stationarity and linearity
Mutual Information (MI)	$I(X;Y) = \sum_{x,y} p(x,y) \log \left(\frac{p(x,y)}{p(x)p(y)} \right)$	- Captures non-linear dependencies - More general than correlation - Model-agnostic	- Computationally expensive - Hard to interpret for high-dimensional data

Notes

 X_t , Y_t represent time series variables at time t; k is the lag; $Cov(\cdot)$ is covariance; $Var(\cdot)$ is variance; σ_X , σ_Y are standard deviations of X and Y; ϕ_{kk} is the kth lag partial autocorrelation coefficient.

p(x) and p(y) are marginal probabilities; p(x, y) is the joint probability distribution.

(CSO), and genetic algorithm (GA)) with ANN, ANFIS, and SVM for monthly GWL predictions. Principal component analysis (PCA) reduced time series data, and the Taguchi model optimized parameters. ANFIS-GOA achieved the best accuracy, while SVM was less effective. Kayhomayoon et al. (2022) applied ANFIS with meta-heuristic algorithms (e.g., Genetic Algorithm (GA) and Ant Colony Optimization (ACO)) to predict GWLs in the Urmia aquifer. Using a Sugeno-type function with Gaussian membership functions, ANFIS-ACOR outperformed the base model and other hybrids. Roy et al. (2023) developed a Bayesian model averaging (BMA)-based ensemble model for GWL forecasting in Bangladesh, combining seven ML models including ANFIS, RF, GPR, Bi-LSTM, and SVR. Past GWL values were used as inputs, with Minimum Redundancy Maximum Relevance (MRMR) applied for lag selection. Lag-1 was most predictive. MARS and RF handled feature selection internally. The ensemble consistently outperformed standalone models across all wells and forecast horizons.

Refer to supplementary information for a detailed description of ANFIS.

3.4.2. Results

Based on the reviewed papers, we found that

- 1. Gaussian Membership Functions (MF) were the most frequently employed, followed by Trapezoidal MF. Membership functions are a fundamental component of fuzzy logic systems, and they define how each input variable's value is associated with different fuzzy sets. These functions are essential to ANFIS's fuzzy inference procedure. In a study by Talpur et al. (2017), the influence of four common membership function shapes on the effectiveness of ANFIS in tackling diverse classification tasks was investigated. Their findings indicated that the Gaussian membership function, due to its superior accuracy and lower computational demands, emerged as the most promising choice. It is worth noting that several reviewed papers did not specify the MF utilized.
- 2. Hyperparameter tuning was performed primarily using a trial-and-error approach. However, in select cases, algorithms such as ACOR, GOA, CSO, WA, GA, KA, and PSO were employed, producing favorable results. Section 5.1, provides more information about these algorithms.
- Partial Autocorrelation and Autocorrelation analyses were the prevalent methods for selecting optimal features for model inputs.
- 4. Both standalone ANFIS models and hybrid ANFIS models consistently outperformed ANN models. This superior performance can likely be attributed to ANFIS models integrating both neural networks and fuzzy logic, making them more adept at handling non-stationary time series data.

3.5. SVM/SVR (Standalone and hybrid) models

3.5.1. Bibliographic review

Behzad et al. (2010) compared SVM and ANN for simulating and forecasting GWLs in the Towaco aquifer, Morris County, N.J., across multiple timeframes (daily to bimonthly). The study employed the radial basis function kernel for SVM and concluded that SVM outperformed ANN in both training and testing phases, showcasing its reliability for GWL prediction. In a similar study, Yoon et al. (2011) evaluated the performance of SVM and ANN models in predicting GWL fluctuations in a coastal aquifer in Korea. The study employed the cross-correlation analysis to identify the most influential features. The SVM model was trained using the Sequential Minimal Optimization (SMO) algorithm, and parameters were fine-tuned through trial and error. Results showed that the SVM model outperformed the ANN model in forecasting GWL fluctuations. Suryanarayana et al. (2014) introduced an integrated wavelet-SVR (WA-SVR) model with an RBF kernel for predicting monthly GWL fluctuations in Visakhapatnam, India. Optimized through trial and error, the WA-SVR outperformed SVR, ANN, and ARIMA models. Zhou et al. (2017) combined discrete wavelet transform (DWT) with SVM (WSVM) for GWL forecasting in the Huai River Basin, China. Using PSO-based hyperparameter tuning and lag optimization via Partial Autocorrelation Function, WSVM achieved superior performance over standard ANN, SVM, and Wavelet Preprocessed ANN (WANN) models. In the same year, Ebrahimi and Rajaee (2017) evaluated the impact of wavelet analysis on SVR, MLR, and ANN models for one-month-ahead GWL predictions in the Qom Plain, Iran. Using auto-correlation analysis for feature selection, wavelet-enhanced models (WNN, WLR, WSVR) outperformed standalone counterparts. The RBF kernel was used for SVR with trial-and-error optimization. Nie et al. (2017) applied SVM and RBF-ANN models to forecast monthly GWL in Jilin province, China, concluding that SVM effectively predicts GWL while analyzing uncertainties through confidence intervals. Huang et al. (2017) employed chaos theory for variable selection, bypassing linear correlation analyses. They developed SVM and BP-ANN models for predicting GWLs in China's Three Gorges Reservoir Area. The chaotic PSO-SVM model, optimized with RBF kernel and PSO, achieved superior accuracy over its linear counterpart and chaotic BP-ANN models. Mukherjee and Ramachandran (2018) explored the relationship between terrestrial water changes from GRACE data (\(\Delta TWS \)) and GWLs in India using SVR, ANN, and linear regression models. SVR outperformed the others, highlighting ΔTWS as a valuable input for modeling irregular GWL time series. Hussein et al. (2020) compared SVR with MLR, MLP, RF, and XGB for GWL prediction, with XGB also used for feature selection. Feature engineering was performed using the Gaussian Mixture Model on GRACE data. SVR consistently outperformed all other models. Yadav et al. (2020) integrated MI

theory, SSA, and GA with SVM and ANN models to analyze climatic and non-climatic impacts on GWL fluctuations in India. Using the Kernel Basis Function, hybrid models (SSA-MI-GA-ANN and SSA-MI-GA-SVM) outperformed standalone models after hyperparameter fine-tuning. Yin et al. (2021) developed a Bayesian ensemble modeling approach using SVM, ANN, and Response Surface Regression to predict groundwater storage fluctuations. The SVM model, employing a Gaussian kernel, demonstrated low uncertainty and strong regional-scale predictions. Yu et al. (2021) combined Grey Relational Analysis (GRA) and Factor Analysis (FA) with SVM to predict GWL in Mingin County, China. The GRA-FA-SVM, utilizing an RBF kernel, outperformed standalone SVM, BPNN, and RBFNN models. Liu et al. (2021) compared standalone SVM and SVM with data assimilation (SVM-DA) for predicting short- to medium-term GWL changes (1-3 months) in the northeastern United States. Using correlation analysis for feature selection and the RBF kernel with fine-tuned hyperparameters, SVM-DA achieved higher accuracy than standalone SVM. Dehghani et al. (2022) evaluated hybrid models (BWO-SVR, WSVR, and AIG-SVR) for predicting GWL changes under the RCP8.5 scenario in Iran's Khorramabad plain. Parameter tuning employed black widow and rifile algorithms, with WSVR consistently outperforming other models. Kajewska-Szkudlarek et al. (2022) compared SVR and MLP for monthly GWL prediction in northern Poland, using the Hellwig method for predictor selection. The RBF kernel in SVR slightly outperformed MLP. Sarkar et al. (2024) evaluated five nonlinear ML models: Polynomial Regression, Random Forest, XGBoost, KNN, and SVM-RBF for GWL prediction at a well in IIT Roorkee, India. Cross-validation was used for hyperparameter tuning. XGBoost achieved the highest accuracy and was best suited for capturing GWL changes linked to gravity variations. Niu et al. (2023) used a SVM model to predict GWL in the North China Plain, focusing on regions with varying human activity. Cross-correlation analysis and SHapley Additive exPlanations (SHAP) analysis were used to select input variables (e.g., precipitation, temperature, population, GDP) and determine time lags. Bayesian optimization tuned SVM parameters. The model had a commendable overall performance. Kayhomayoon et al. (2023) evaluated GWL prediction in Iran's Dehgolan aquifer using MODFLOW and machine learning models-SVR, least-square SVR (LSSVR), and a hybrid SVR-WOA. Inputs included past GWL and monthly recharge/withdrawal. LSSVR outperformed other ML models, and the combined LSSVR-MODFLOW model gave the best results. Wu et al. (2023) compared SVM, Long-Short Term Memory (LSTM), MLP, and Gated Recurrent Units (GRU) models for GWL prediction in China's Hebei Plain using data from six monitoring stations (2018-2020). RBF kernel function selected for SVM. GRU showed the highest accuracy, especially for fluctuating or increasing trends. SVM had the weakest performance.

Refer to supplementary information for a detailed description of SVM/SVR

3.5.2. Results

Based on the reviewed papers, we found that

1. The RBF that is the Radial Basis Function kernel was the most frequently employed, followed by the Polynomial and Linear kernels. The RBF kernel formulated by Broomhead and Lowe (1988) in 1988 is a mathematical function commonly used in machine learning, particularly in SVM and other kernel-based algorithms. It is a type of kernel function that helps transform data into a higher-dimensional space, making it easier to classify or separate non-linear data. it is important to note that there is no one-size-fits-all kernel function. The choice of kernel relies on the particular problem, dataset, and its inherent characteristics. In some cases, other kernels like linear, polynomial, or sigmoid kernels may perform better. Table 4 provides a comparison between these kernels.

- Hyper-parameters were predominantly fine-tuned through a trial-and-error approach. However, in specific instances, alternative methods such as the Creative Rifle and Black Widow (Dehghani et al., 2022), and the Taguchi Model (Seifi et al., 2020) were utilized to optimize the tuning process.
- 3. In addition to correlation analysis, Principal Component Analysis (PCA), Chaos theory, Grey Relational Analysis (GRA), Factor Analysis (FA), and the Hellwig method were utilized to facilitate optimal feature selection. Table 5 provides a general overview as well as some advantages and disadvantages.
- SVMs, when tuned to optimal hyperparameters, consistently outperformed ANN and ANFIS models.

3.6. LSTM (Standalone and hybrid) models

3.6.1. Bibliographic review

Zhang et al. (2018) assessed the LSTM model's performance in five sub-areas of the Hetao Irrigation District in arid northwestern China, comparing it with a traditional FFNN and a double-layered LSTM model. Monthly data on evaporation, temperature, precipitation, water diversion, and time were used as inputs. Key hyperparameters were fine-tuned through trial and error. The results indicated that the LSTM model outperformed both the FFNN and the double-layered LSTM model. A few years later, Solgi et al. (2021) employed the LSTM-NN model to predict GWLs using historical GWL data as the only input. The study compared its performance with a basic neural network (NN) for predicting short- and long-term GWLs in the Edwards aquifer, Texas. The LSTM-NN model was trained with the Adam optimizer, and input variable selection was refined through trial and error. Results consistently demonstrated that the LSTM-NN outperformed the basic NN across all evaluation scenarios. In that same year, Hag et al. (2021) applied LSTM networks for real-time tracking and prediction of Terrestrial Water Storage Change (TWSC) and Groundwater Storage Change (GWSC) across five Saudi Arabian basins using GRACE datasets from 2003 to 2025. Correlation analysis was employed to evaluate the influence of input variables. The LSTM model, trained with the ADAM optimizer, outperformed the autoregression model in accuracy and computational efficiency. Wu et al. (2021a) proposed the WT-multivariate LSTM (WT-MLSTM) method for simulating and predicting GWLs, tested in the Liangshui River Basin, China, and the Cibola National Wildlife Refuge, USA. The model, trained using the Adam optimizer, demonstrated superior prediction accuracy compared to standard LSTM, MLSTM, and WT-LSTM models. Ao et al. (2021) compared the LSTM model, the kernel-based nonlinear extension of the Arps decline model (KNEA), and the GRU model for estimating GWL in the Hetao Irrigation District, China. Hyperparameters were optimized using grid search, and the study concluded that the LSTM model outperformed the other methods.

In some of the more recent studies, Vu et al. (2023) utilized the Bidirectional LSTM (BiLSTM) model to predict GWL dynamics in a Normandy karst massif in eastern France. Feature relevance was determined through correlation analysis, and the ADAM optimizer was used for training. The study concluded that the BiLSTM model outperformed the standard LSTM model, Manna and Anitha (2023) developed the Double-Edge Bi-Directed Long Short-Term Memory (DEBi-LSTM) model, a deep ensemble learning approach for simulating and forecasting groundwater levels in India. The model was enhanced using the Randomized Low-Ranked Approximation (RLRA) algorithm, with feature selection guided by the Variance Inflation Factor (VIF) and Multi-Collinearity Test. The study concluded that the DEBi-LSTM model outperformed existing models, including LSTM, bagging ensemble, and general ensemble models. Foroumandi et al. (2023) employed ConvLSTM, FFNN, and RF models to downscale monthly GRACE-derived Terrestrial Water Storage Anomaly (TWSA) to a 10 km resolution over Iran using remote sensing images. The Growing Neural Gas (GNG)

Table 4
Comparison of the SVM kernels (Rahmadani and Lee, 2020; Scholkopf et al., 1997; Panja et al., 2019; Patle and Chouhan, 2013).

Kernel	Description	Formula	Advantages	Disadvantages
RBF (Gaussian)	The RBF kernel maps input vectors into an infinite-dimensional space and is effective for capturing complex non-linear relationships.	$K(x, x') = \exp(-\gamma x - x' ^2)$	- Handles non-linear relationships well - Effective in high-dimensional spaces - Few parameters to tune	- Requires careful tuning of γ - May overfit with high γ - Computationally demanding for large datasets
Polynomial kernel	Captures interactions of features by computing polynomial combinations of inputs. Useful when prior knowledge suggests polynomial relationships.	$K(x, x') = (a \cdot x \cdot x' + b)^d$	 Models non-linear patterns Adjustable via degree d Performs well when data is polynomially separable 	- Computationally expensive for large d - Prone to overfitting - Requires parameter tuning (a, b, d)
Sigmoid kernel	Inspired by neural networks, this kernel simulates the behavior of an activation function.	$K(x, x') = \tanh(a \cdot x \cdot x' + b)$	- Mimics neural network behavior - Useful for binary classification - Captures certain non-linearities	- Sensitive to parameter choices - Less robust than RBF - Not always positive semi-definite
Linear kernel	Assumes linear separability. Best suited for high-dimensional data with a clear linear margin.	$K(x, x') = x \cdot x'$	- Fast and simple - Fewer hyperparameters - Works well with linearly separable data - Less prone to overfitting	- Ineffective for non-linear problems - Limited flexibility - May underfit complex patterns

Notes: x, x' are input feature vectors; $x \cdot x'$ denotes their dot product; $||x - x'||^2$ is the squared Euclidean distance.

 γ is a kernel parameter controlling the spread in the RBF kernel; a is a scale factor; b is a bias term; d is the degree of the polynomial. tanh is the hyperbolic tangent function used in the sigmoid kernel. Proper tuning of these parameters is essential for optimal model performance.

Table 5
Comparison of feature selection methods (King and Jackson, 1999; Tang et al., 2014; Omiotek et al., 2019; Huang et al., 2017).

Method	Description	Advantages	Disadvantages
PCA	PCA is a dimensionality reduction technique that transforms features into a set of linearly uncorrelated components, ordered by variance.	- Reduces dimensionality - Highlights key features - Simplifies data visualization	- May lose interpretability - Assumes linear relationships - Not ideal for non-linear data
Chaos theory	Chaos theory examines complex systems that appear disordered but are deterministic. In ML, it identifies chaotic patterns in data.	- Identifies hidden patterns - Useful for complex systems - Captures dynamic behaviors	Requires complex calculations Interpretation can be difficult Sensitive to initial conditions
GRA	Evaluates the relationship between multiple criteria using grey relational grades to rank and select important features.	Handles uncertainty and complex multi-criteria problems well Requires fewer data points compared to some methods Provides a clear ranking of features based on relational grades	Can be complex to implement and interpret Sensitive to the selection of reference series May require normalization of data for accurate analysis
FA	A statistical method that identifies underlying factors that explain the relationships between variables, reducing dimensionality.	Reduces dimensionality by identifying latent factors Helps in understanding the underlying structure of data Simplifies the feature space by focusing on significant factors	Assumes linear relationships among variables Can be sensitive to outliers and data noise Interpretation of factors can be subjective and complex
Hellwig method	The Hellwig method evaluates the importance of features by considering their correlation with the target variable and redundancy among themselves.	Considers both relevance and redundancy Facilitates selection of non-redundant features Provides a clear ranking of features	- May require large datasets - Can be computationally intensive - Relies on accurate correlation measures

algorithm clustered TWSA data to identify similar pixels for model inputs and outputs. ConvLSTM utilized the ReLU activation function, with layer optimization performed through trial-and-error. The results indicated that ConvLSTM outperformed RF and FFNN, effectively downscaling GRACE data and producing groundwater storage maps for Iran. Ehteram et al. (2023) developed a hybrid SATCN-LSTM model integrating self-attention and temporal convolution with LSTM to improve GWL prediction accuracy. The model was tested using meteorological inputs and outperformed baseline SATCN, TCN, and standalone LSTM models. It achieved the lowest MAE (0.06) and RMSE (0.08), addressing limitations of vanishing gradients and redundant inputs in sequence forecasting. Heudorfer et al. (2023) used global LSTM models to predict GWL from 108 wells in Germany. Dynamic inputs included precipitation and temperature, while static features (e.g., land cover, hydrogeology) were selected via correlation and spatial relevance analysis. Feature importance was assessed using permutation feature importance (PFI). Models with static features performed no better than random ones in-sample. Out-of-sample, the dynamic-only model gave the best results, highlighting the stronger role of climatic inputs. Jing

et al. (2023) applied six models (RF, XGBoost (XGB), GBR, Light-GBM, Vanilla-LSTM, EnDe-LSTM) to simulate GWL in China's North China Plain. Feature engineering created GWSAFE and Human_activity from GRACE and GLDAS datasets. Feature importance was assessed using GINI and Permutation Feature Importance (PFI). Human_activity emerged as the dominant predictor. Deep learning models, especially EnDe-LSTM, outperformed tree-based models in capturing groundwater variation across aguifer types. Zheng et al. (2024) developed a VMDiTransformer model to predict GWL in China's Kubuqi Desert using data from nine monitoring stations. Variational Mode Decomposition (VMD) was used as a preprocessing step to decompose non-stationary time series into intrinsic components. The VMD-iTransformer model outperformed both classic Transformer and LSTM models. Elzain et al. (2024) used CBR, XGB, LGBM and LSTM, GRU, Transformer to forecast water table rise (WTR) in Oman. SHAP was used for feature selection. Data preprocessing involved lag creation, differencing, and seasonal aggregation. Stacked models outperformed individual ones, with GRU leading in one-week ahead forecasts. Sun et al. (2023) assessed GWL

prediction in Beijing's Yongding River fan using Long Short-Term Memory (LSTM) models and a physics-based (PB) model (PGMS). Input variables included water supply, precipitation, and runoff, with lag times identified via correlation analysis. Improved LSTM models consistently outperformed the PB model in short-term forecasts. The PB model remained better for long-term trends.

Refer to supplementary information for a detailed description of LSTM.

3.6.2. Results

- 1. The Adam optimizer, introduced by Kingma and Ba (2014), was predominantly utilized for training the LSTM model. Renowned for its efficiency and adaptability, Adam combines the strengths of RMSprop and Momentum optimizers, resulting in faster and more reliable convergence compared to traditional algorithms. Its ability to dynamically adjust learning rates for each parameter during training proves particularly advantageous for complex models like LSTMs, where varying learning rates enhance convergence. The widespread adoption of Adam is evidenced by its over 100,000 citations within eight years of publication. In comparative studies, LSTM consistently outperformed ANN models, likely due to its robust architecture, which effectively mitigates issues like local minima that often impede convergence during training.
- 2. The ReLU activation function was commonly utilized as the activation function for the LSTM model. The ReLU activation function was created by Nair and Hinton (2010) and it is well known for its ability to handle the gradient vanishing problem. Using the ReLU function as the activation in a neural network, as opposed to the sigmoid function, results in partial derivatives of the loss function having values of either 0 or 1. This property effectively mitigates the issue of gradient vanishing, making ReLU an effective choice for preventing gradient-related problems.
- 3. Hyperparameters were mostly adjusted through trial and error. However, in some cases, like in the study by Ao et al. (2021), the grid search method was used. The grid search approach is a systematic method used in machine learning to find the optimal hyperparameters for a model. it involves defining a grid of possible values for each hyperparameter and then evaluating the model's performance for every possible combination of these values.
- 4. The selection of optimal input variables primarily relied on correlation analyses. However, in some select cases, methods such as Cross-wavelet analysis and the Granger causality (Kim et al., 2023), Multi Collinearity Test, and Variance Inflation Factor (VIF) (Manna and Anitha, 2023) were employed to improve model performance through enhanced feature selection. Also, it is worth mentioning that one of the primary advantages of the LSTM model compared to other AI models like FFNN is that, while important features of the input dataset typically need to be identified through mathematical measures such as Cross-correlation (CC) or MI, the LSTM model can automatically achieve this through its hidden layers (Sharghi et al., 2022). Table 6 provides an overview of these methods as well as some strengths and limitations.
- In terms of performance, LSTM consistently outperformed ANN models, possibly due to its inherent capability to overcome the limitations associated with local minima, which can hinder convergence in the training process.

3.7. RF (Standalone and hybrid) models

3.7.1. Bibliographic review

In the scope of GWL simulation and modeling with RF, Lendzioch et al. (2021) assessed the RF model's ability to predict peat bog GWL

and soil moisture in the Rokytka Peat Bog using ultrahigh-resolution UAV maps. Predictor selection, hyperparameter tuning, and performance evaluation were conducted using a leave-location-out (LLO) spatial cross-validation strategy combined with forward feature selection (FFS) to mitigate overfitting and enhance predictions for untested locations. The study concluded that the RF model demonstrated strong predictive performance. Mosavi et al. (2021) utilized ensemble models, including GamBoost, AdaBoost, and Bagged CART, to simulate and predict GWLs in the Dezekord-Kamfiruz watershed, Iran. Variable selection was optimized using Recursive Feature Elimination (RFE) and multicollinearity assessment via the Variance Inflation Factor (VIF). The study concluded that Bagging methods, particularly Random Forest and Bagged CART, outperformed Boosting models like AdaBoost and GamBoost, with Random Forest achieving the highest performance.

Zhou et al. (2022) explored the use of GRACE satellite data, GLEAM, and GLDAS datasets, combined with meteorological variables, to predict GWL using RF, SVR, and ELM models. For the RF model, hyperparameters such as Ntree (100-500) and Mtry (1-3) were fine-tuned. The study concluded that RF demonstrated the best predictive performance, followed by SVR and ELM. Liu et al. (2022) developed multiple models, including RF, SVM, GRNN, DT, CNN, LSTM, and GRU, to simulate GWLs in the lower Tarim River basin. The SHAP method was employed to evaluate the impact of covariates on model performance. Results indicated that the RF model consistently outperformed the other models. Pham et al. (2022) tested the validity of the RF model in simulating and forecasting GWL fluctuations in two wells in northwest Bangladesh. The study compared the RF model with six other models: Random Tree (RT), Decision Stump, M5P, SVM, Locally Weighted Linear Regression (LWLR), and Reduced Error Pruning Tree (REP Tree). They concluded that the Bagging RF and Bagging RT models outperformed the others. Rafik et al. (2023) evaluated Random Forest (RF), SVM, and k-Nearest Neighbors (k-NN) for GWL prediction in the Saïs basin, Morocco. Input data included precipitation, soil moisture, runoff, and evapotranspiration from ERA5-Land, along with NDVI and land surface temperature (LST). A correlation matrix was used for feature selection. Among the models, RF showed the most satisfactory performance, making it the preferred choice for regional GWL prediction. Zowam and Milewski (2024) applied RF and SVR for statewide GWL anomaly prediction in Arizona, integrating geostatistical interpolation (EBK) to estimate GWL and using it as a predictor in the RF model. Final features were selected using permutation feature importance after training. The integrated RF+EBK model showed high accuracy in unconsolidated aquifers, emphasizing the role of geology and data quality. May-Lagunes et al. (2023) assessed several ML and deep learning models including ARIMA, XGBoost, RF, LSTM, and TFT for GWL prediction in California's Sacramento River Basin. Inputs included historical GWLs, well characteristics (e.g., depth, usage, location), SWE, ET, and seasonal features from Fourier decomposition. Feature selection involved experimenting with lagged variables and measuring importance in XGBoost, where well-specific features ranked highest. XGBoost outperformed all models, especially for 3-month forecasts, highlighting the value of well-level information over climate predictors. Hikouei et al. (2023) applied MLR, RF, and XGBoost to predict GWL in Indonesia's Mawas peat dome. Inputs included elevation, precipitation, ET, and distance from canals. Tree-based models provided feature importance, with elevation ranked highest. XGBoost outperformed RF and MLR, showing superior accuracy and lower residuals. Yi et al. (2024) predicted GWL near South Korea's Baekje weir using five ML models: RF, ANN, SVR, GB, and XGBoost. Feature selection was done via permutation-based importance. XGBoost consistently outperformed all others across evaluation metrics. Gupta et al. (2024) applied three Bagging-based models, Random Forest (RF), Bagging-REPTree, and Bagging-DSTree, to forecast groundwater levels in Punjab, India, using long-term GWL data from 14 wells. Feature importance was derived using the RF model. RF

Table 6
Analytical methods for feature selection in GWL using LSTM (Thompson et al., 2017; Maraun and Kurths, 2004; Akinwande et al., 2015; Torrence and Compo, 1998; Attanasio et al., 2013; Stokes and Purdon, 2017).

Method	Description	Advantages	Disadvantages
Cross-wavelet analysis	Analyses the relationship between two time series in the time-frequency domain, providing insights into their co-movement at different frequencies and times.	Provides detailed time–frequency information Useful for analyzing non-stationary time series Can identify phase relationships	Computationally intensive Requires careful interpretation Sensitivity to noise and boundary effects
Granger causality	Determines whether one time series can predict another, indicating a directional influence between the variables.	Helps identify potential causal relationships	Assumes linear relationships May not capture complex dynamics Sensitive to the choice of lag length
Multi Collinearity Test	Assesses the degree of correlation among independent variables in a regression model, indicating potential multicollinearity issues.	Identifies problematic correlations Helps in improving model stability Simple and easy to apply	Does not quantify the impact on the model May miss subtle collinearity issues Assumes linear relationships
Variance Inflation Factor (VIF)	Quantifies the degree of multicollinearity by measuring how much the variance of an estimated regression coefficient increases if the predictors are correlated.	Provides a clear numerical measure of multicollinearity Easy to interpret and use Helps in model refinement	Only applicable to linear models Does not indicate causality May not detect non-linear relationships

consistently outperformed the other models in both pre- and postmonsoon seasons across multiple evaluation metrics. Chi et al. (2024) used Tree Ensemble models (DT, RF, XGBoost) with rolling means and lagged features to predict GWL. Inputs included groundwater depth, temperature, rainfall, and drainage volumes. SHAP analysis highlighted lagged GWL and moving averages as most important.

Refer to supplementary information for a detailed description of RF.

3.7.2. Results

- In the extensive body of research we have examined, it is clear that both standalone RF models and their hybrid counterparts consistently outperform traditional models like ANN and SVM in various fields. RF's strength lies primarily in its exceptional predictive accuracy, which makes it a valuable tool across many applications.
- 2. In conjunction with correlation analysis, the SHAP (SHapley Additive exPlanations), the Recursive Feature Elimination (RFE) (Mosavi et al., 2021), and forward feature selection (FFS) (Lendzioch et al., 2021) methods were occasionally employed to select optimal input variables for the models. Table 7 provides an overview of these methods as well as some strengths and limitations.
- 3. A noteworthy observation is that many papers did not explicitly specify the hyperparameter values for 'ntree' and 'mtry'. The optimal values for 'ntree' and 'mtry' in RF models are recognized to be problem-dependent (Martínez-Muñoz and Suárez, 2010). While specific values may vary based on the nature of the problem, it is commonly acknowledged that RF often performs reasonably well with default hyperparameter values. For instance, the default value for 'ntree' is typically set at 500 trees, and 'mtry' is defaulted to one-third of the total number of variables (Mutanga et al., 2012). This suggests that researchers may rely on these default values without explicit specification. However, the significance of choosing appropriate hyperparameter values, particularly in the context of groundwater recharge studies, should not be overlooked.

4. Trends and gaps in feature selection for GWL modeling

Across the reviewed studies, a diverse array of feature selection techniques have been employed, ranging from classical statistical tools to modern hybrid and model-driven approaches. Broadly, these methods fall into three categories: filter-based, wrapper, and embedded approaches. Filter methods evaluate features based on statistical metrics independent of the model, wrapper methods iteratively assess feature subsets using the learning algorithm itself, and embedded methods perform selection as part of the model training process. Each

comes with trade-offs in interpretability, computational demand, and robustness. A close inspection reveals that while performance-centric motivations drive most feature selection choices, methodological inconsistencies and reporting gaps persist, limiting comparability and reproducibility across studies.

4.1. Filter-based approaches

Filter methods are independent of the machine learning model and select features based on general characteristics of the data, such as statistical relevance or correlation. These techniques are computationally efficient and easy to implement. However, they may overlook feature interactions and dependencies that are only revealed during model training.

Filter techniques were extensively applied across early ANN, ANFIS, and SVM studies. ACF, PACF, cross-correlation, and Mutual Information (MI) were commonly used for lag selection. For instance, Nourani et al. (2015) and Bahaa et al. (2015) used MI to identify relevant time lags and improve model accuracy by capturing nonlinear dependencies. Yu et al. (2021) implemented Gray Relational Analysis (GRA) and Factor Analysis (FA) in the SVM frameworks, observing better precision than conventional methods. The Hellwig method was adopted in SVR (Kajewska-Szkudlarek et al., 2022) to assess feature weights using a synthetic capacity index. LSTM-based studies often employed correlation matrices to select relevant features (Sun et al., 2023), while PCA was used in hybrid ANN-ANFIS frameworks (Seifi et al., 2020) to reduce dimensionality. VIF and multicollinearity tests were also used (Manna and Anitha, 2023). Additional studies supporting filter-based selection include Wei et al. (2023a), who applied wavelet decomposition and phase space reconstruction (PSR) to preprocess inputs before feeding them into ANN models. Lyapunov exponent analysis supported the relevance of PSR in chaotic systems. In Ghafoor et al. (2024), ANN models using interpolated and upsampled GWL time series outperformed ARIMA, reinforcing ANN's capability to learn from preprocessed, irregular data. Correlation and standard preprocessing approaches (e.g., normalization, cubic spline interpolation) were also applied in studies by Fahim et al. (2024), Seidu et al. (2023), Feng et al. (2024). Zheng et al. (2024) used Variational Mode Decomposition (VMD) as a preprocessing tool to decompose non-stationary time series before feeding data into the iTransformer model.

4.2. Wrapper approaches

Wrapper methods evaluate subsets of features by training and testing a specific model. These approaches often yield better performance as they consider interaction effects and model dynamics. However, they

Table 7
Feature selection methods applied with RF models in GWL prediction studies (Strobl et al., 2007; Chen and Jeong, 2007; Kuhn et al., 2013b; Lundberg and Lee, 2017; Jović et al., 2015; Kamalov et al., 2024; Takefuji, 2025).

Method	Description	Advantages Disadvantages	
SHAP (SHapley Additive exPlanations)	Game-theory-based approach that assigns each feature an importance value by quantifying its marginal contribution to predictions.	Provides consistent, interpretable attributions; captures nonlinear interactions.	Computationally expensive for large datasets; results can be sensitive to background data selection.
Recursive Feature Elimination (RFE)	Iteratively fits the model, removes the least important feature(s), and repeats until the optimal subset is identified.	Efficiently identifies strong predictors; helps reduce dimensionality.	Greedy elimination may discard interacting features too early; requires repeated model training.
Forward Feature Selection (FFS)	Begins with no features, adds predictors sequentially based on performance improvement until no significant gain is observed.	Computationally less intensive than exhaustive search; yields parsimonious models; avoids inclusion of irrelevant predictors.	Greedy nature may miss optimal subsets; struggles with correlated predictors; can overfit without proper validation.
RF Inherent Feature Importance	RF naturally provides importance measures based on mean decrease in impurity (MDI) or mean decrease in accuracy (MDA).	Embedded in the model; efficient and scalable; offers direct ranking of features.	Importance may be biased toward variables with more categories or higher variance; does not always reflect causal relevance.

are computationally expensive and prone to overfitting, especially on small datasets.

Wrappers were increasingly adopted in more recent studies. Forward Feature Selection (FFS) was used by Lendzioch et al. (2021) to select UAV-based predictors for RF models under a leave-location-out strategy, showing strong performance in untested locations. Recursive Feature Elimination (RFE) was used in ensemble studies (Mosavi et al., 2021), leading to the selection of non-redundant inputs and improved accuracy for RF and Bagged CART. The Taguchi method was used to select the optimal combinations of characteristics and parameters for ANFIS in Seifi et al. (2020), producing the best performing hybrid (ANFIS-GOA). Metaheuristic wrappers such as Genetic Algorithms (GA), Particle Swarm Optimization (PSO), and Ant Colony Optimization (ACO) were used to tune the inputs and parameters of SVM and ANFIS (Kayhomayoon et al., 2022; Zhou et al., 2017), improving the generalization of the model. Akbari Majd et al. (2024) applied multiple preprocessing stages involving decomposition and metaheuristic optimization (GA, PSO, ACO) in ANN frameworks, with wrapper-based improvements delivering up to 76% accuracy gain. In Seifi et al. (2024), Boruta was used as a wrapper for feature importance before applying decomposition and GRU-RVM sequence models. Moradi et al. (2023) evaluated different sets of characteristics using internal validation performance, choosing only GWL for the final training after evaluating the correlation patterns.

4.3. Embedded approaches

Embedded methods integrate feature selection directly into the model training process. These include regularization techniques and importance measures derived from model parameters. Embedded methods are more efficient than wrappers and often yield robust and interpretable outcomes.

In studies based on RF and XGBoost, the importance of permutation characteristics and GINI was frequently applied after training to rank predictors (Yi et al., 2024; Jing et al., 2023). These techniques revealed the dominant role of well-level inputs and GRACE-derived groundwater storage indicators. SHAP values were used in the RF, SVM and LSTM studies (Elzain et al., 2024; Niu et al., 2023), providing interpretable information on variable contributions. MARS and RF were used as embedded selectors in ensemble pipelines (Roy et al., 2023), while permutation importance was used to refine features in ConvL-STM and GRU models trained on remote sensing inputs (Foroumandi et al., 2023). GNG clustering, while not a direct selection method, helped identify spatially coherent input structures prior to model training (Heudorfer et al., 2023). Chi et al. (2024) used SHAP to analyze lagged inputs in tree ensemble models, confirming the dominance of moving averages and historical GWLs. Abdi et al. (2024) used CNN

and DNN models in which the relevance of input characteristics was indirectly derived from the learned filters. Their preprocessing relied on model-based interpolation techniques (e.g., M5P) to reconstruct missing inputs. Feng et al. (2024) further evaluated model-specific importance rankings using Pearson and Spearman correlations to interpret dominant drivers. Jing et al. (2023) used GINI and Permutation Feature Importance (PFI) to assess the relevance of engineered features like GWSAFE and Human_activity, with deep learning models (especially EnDe-LSTM) outperforming tree-based alternatives.

Despite methodological innovations, a recurring limitation across all studies is the lack of standardization in reporting. Feature selection procedures were often vaguely described or entirely omitted, complicating reproducibility and interpretation. Only a handful of works explicitly distinguished between filter, wrapper, and embedded selection techniques. To date, only one study by Saroughi et al. (2024) has come close to systematically evaluating the impact of input processing strategies on groundwater level modeling. Their work tested 126 data preprocessing methods across multiple AI models (SVR, ANN, LSTM, and POA-ANN), focusing on how statistical, wavelet, and decomposition-based transformations influenced predictive accuracy. However, even this comprehensive effort emphasized data pre-processing rather than a formal comparison of feature selection methods.

This signals a methodological gap where future research could systematically evaluate and benchmark feature selection techniques, especially under varying hydrogeological and data availability scenarios, to establish standardized best practices for ML-based GWL forecasting. Table 9 provides a summary of all the feature selection approaches reviewed.

5. General overview and discussion

This section will highlight key findings from the analysis of the 223 reviewed articles. These findings encompass various aspects, including optimization algorithms, the treatment of time steps, selection of input variables, validation metrics, etc.

5.1. Optimization algorithms

In recent decades, several bio-inspired optimization techniques have been created. According to Tang and Wu (2009), these algorithms can be broadly categorized into three primary types: swarm intelligence, bacterial foraging algorithms, and evolutionary algorithms. Swarm intelligence algorithms were the most popular optimization techniques used in groundwater studies, according to the articles reviewed. Table 10 provides some advantages and disadvantages of the optimization algorithms mentioned above. Refer to the Supplementary Information for a detailed description of the workflow of all the optimization algorithms discussed.

Table 8
Summary of the reviewed paper used in the bibliographic sections.

Paper Ref	AI used	Prediction horizon	Input variables	Time steps	Data division (%)	Length of total data
Dash et al. (2010)	ANN	Short-term (1-week ahead)	GWL,R	Weekly	70/30	1993-2002 (2340 samples
Mohanty et al. (2010)	FFNN	Short-term (1,2,3,4-weeks ahead)	R, E, RS, water level in the drain, pumping rate, GWL	Weekly	70/30	Feb 2004–June 2007 (174 samples)
Chen et al. (2010)	RBFN	Short-term (1-month ahead)	GWL	Monthly	79/21	1997–2003 (63 samples)
Chen et al. (2011)	BPN	Short-term (1-month ahead)	GWL	Monthly	79/21	Jul 1998–Nov 2004 (76 samples)
Trichakis et al. (2011)	ANN	Short-term (1-day ahead)	GWL, wet days, R, pumping rate	Daily	80/20	- (7109 samples)
Rakhshandehroo et al. (2012)	FFNN, RBNN, ELNN, GRNN	Short-term (1-month ahead)	GWL, Temp, Runoff, R	Monthly	77/23	1993 to 2003 (4524 samples)
Adamowski and Chan (2011)	ANN, ARIMA	Short-term (1-month ahead)	GWL, Temp, R	Monthly	80/20	Nov 2002–Oct 2009 (84 samples)
Nourani et al. (2011)	ANN, Geostatistics	Short-term (1-month ahead)	GWL, Temp, R, discharge, lake level	Monthly	80/20	Apr 1994–Mar 2006 (144 samples)
Γaormina et al. (2012)	FFNN, ARX	Short-term (1-h ahead)	GWL, Evapotranspiration, R	Hourly	83/17	Oct 2006–June 2008 (23 850 samples)
Sahoo and Jha (2013)	ANN, MLR	Short-term (1-month ahead)	GWL, Evapotranspiration, R, Temp, river stage, SDV	Monthly	73/27	1999–2004 (72 samples)
Nourani et al. (2015)	FFNN, ARIMAX	Short-term (1-month ahead)	GWL, Runoff, R	Monthly	72/28	1988–2012 (298 samples)
Guzman et al. 2015)	ANN, SVR	Short-term (1-day ahead)	GWL, R	Daily	55/45	Jun 1984–Sep 1994 (267 samples)
Bahaa et al. (2015)	ANN, MLR, ENN	Short-term(1- day,week,month ahead)	Tailing Recharge, R, Air temp	Daily	90/10	May 2009–Oct 2011 (900 samples)
Chang et al. (2015)	ANN	Short-term (10-days ahead)	GWL, Temp, R	Daily	56/44	Jul 2009–Dec 2012 (653 samples)
Gholami et al. (2015)	ANN	Monthly (dendrochronology)	Tree-ring diameter, R	Monthly	70/30	1970–2013 (44 samples)
Sun et al. (2016)	FFNN	Short-term (1,3,7 days ahead)	GWL, R	Daily	50/50	Jan 2012–Dec 2013 (731 samples)
Choubin and Malekian (2017)	ANN, ARIMA	Short-term (1 months ahead)	R, SF, Temp, Evaporation, GWL	Monthly	83/17	1993–2010 (216 samples)
Wen et al. (2017)	ANN	Short-term (1,2,3 months ahead)	R, Temp, Evaporation, GWL, R	Monthly	74/26	Jun 2003–Dec 2010. (91 samples)
Sahoo et al. (2017)	ANN, MLR, MNLR	Seasonal-annual ($\tilde{1}$ year ahead)	R, Temp, ENSO, NAO, SF, ID	Monthly	70/30	1980–2012 (148 368 samples)
Ebrahimi and Rajaee (2017)	ANN	Short-term (1-month ahead)	R, Temp, GWL	Monthly	70/30	Apr 2002–Mar 2013 (132 samples)
Guzman et al. (2017)	NARX	Short-term (3-months ahead)	R, GWL	Daily	70/30	1987–1994 (2922 sample
Vunsch et al. 2018)	NARX	short-mid-term(1 week-6 months ahead)	R, Temp	Daily	90/10	1948–2015 (13676 samples)
leong and Park 2019)	NARX, LSTM, GRU	Short-term (1-day ahead, continuous)	R, Temp, Humidity, GWL, CSH, AAP	Daily	50/50	2005-2014 (7284 sample
Lee et al. (2019)	FFNN	Short-term (1-h ahead)	SWL, GA, GHPU	Hourly	60/40	Feb 2016– Apr 2017 (87 samples)
Kouziokas et al. 2018)	FFNN	Short-term (1-day ahead)	Humidity, Temp, R, GWL	Daily	70/30	Jan 2014–Dec 2014 (365 samples)
Ghose et al.	RNN	Short-mid-term (monthly	Humidity, Temp, R,	Monthly	70/30	1988–2007 (120 samples

5.2. Validation metrics

Machine learning models are prone to limitations that can hinder their predictive performance, one of the most notable being overfitting. Overfitting occurs when a model learns patterns and noise specific to the training dataset, resulting in high training accuracy but poor performance on unseen test data. Detecting overfitting therefore requires evaluating model performance on both training and test datasets, and comparing the results. The role of validation metrics is to quantify prediction accuracy and reliability, enabling meaningful comparison of results across datasets and studies.

Table 8 (continued).

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Van Thieu et al. (2023)	MLP	Short-term (1-month ahead)	R, Temp, Tidal height, GWL	Monthly	-	1989–2012 (552 samples)
Aderemi et al. (2023)	NARX	Short-term (No. specified)	R, Temp	Monthly	70/30	1996-2021 (6240 samples
Panahi et al. (2023)	RBFNN, ANFIS, SVM, MLP	Long-term (Years ahead)	R, Max Temp, Min Temp, Evaporation	Daily	-	2022–2064 (10 950 samples)
Jalalkamali et al. (2011)	ANFIS, ANN	Short-term (1-month ahead)	R, Temp, GWL	Monthly	80/20	1988–2009 (264 samples)
Shirmohammadi et al. (2013)	ANFIS, ARIMA, ARMA, ARX, ARMAX, SARIMA	Short-term (1,2,3-months ahead)	Discharge, R, Evaporation	Monthly		1992–2007 (180 samples)
Emamgholizadeh et al. (2014)	ANFIS, ANN	Long-term (2-Years ahead)	Recharge, Pumping Rates, IRF	Monthly	80/20	2002–2011 (108 samples)
Maiti and Tiwari (2014)	ANFIS, ANN, BNN	Short-term (1-month ahead)	Temp, R	Monthly	75/25	Sep 1972–Oct 2001 (350 samples)
Mirzavand et al. (2015)	ANFIS, SVR	Long-term (No. Specified)	Streamflow, Evaporation, SD, AD, R	Monthly	70/30	Jan 1990–Jan 2010 (240 samples)
Gong et al. (2016)	ANFIS, ANN, SVM	Short-term (1,2,3-months ahead)	GWL, Temp, Lake levels, AD, R	Monthly	80/20	1998–2009 (144 samples)
Seifi et al. (2020)	ANFIS, ANN	Short-term (1-month ahead)	GWL	Monthly	80/20	Jan 2000–Sep 2012 (140 samples)
Kayhomayoon et al. (2022)	ANFIS	Short-term (1-month ahead)	GWL, R, Temp, GW	Monthly	70/30	2001–2017 (204 samples)
Behzad et al. (2010)	SVM, ANN	Daily, Weekly, Monthly	Pump Rates, R, Temp, GWL	Daily, Weekly, Biweekly, Monthly, Bimonthly	-	2002–2002 (63,93,109,116,122 samples)
Yoon et al. (2011)	SVM, ANN	Short-term (multiple-hours ahead)	Tide level, R, GWL	Hourly	-	Jun 2004–Nov 2006 (321 samples)
Suryanarayana et al. (2014)	SVR, ANN, ARIMA	Short-term (1-month ahead)	GW Depth, Max Temp, Mean Temp, R	Monthly	-	May 2001–Feb 2012 (130 samples)
Yoon et al. (2016)	SVR, ANN	Long-term (1-day ahead)	GWL, R	Daily	70/30	2003–2008 (10 229 samples)
Zhou et al. (2017)	SVM, ANN	Short-term (1-month ahead)	GWL, R	Monthly	75/25	Jan 1974–Dec 2010 (444 samples)
Nie et al. (2017)	SVM, RBF-ANN, MLR	Short-term (1-month ahead)	R, Evaporation, Temp	Monthly	83/17	Jan 2003 to Dec 2014 (144 samples)
Huang et al. (2017)	SVM, BPNN	Short-term (1-day,week,month ahead)	GWL	daily, weekly, monthly	50/50	2006–2014 (171, 90, 24 samples)
Mukherjee and Ramachandran (2018)	SVM, ANN, LRM	Short-term (No. Specified)	△TWS, R, Temp, Humidity	monthly	80/20	Jan 2005–Dec 2013 (35, 67 samples)
Hosseini et al. (2016)	ANN	Short-term (1-month ahead)	R, Average Discharge, Temp, Evaporation	Monthly	-	Oct 2000 80/20 Sep 2009 (108 samples)
Yadav et al. 2020)	SVM, ANN	Short-term (1,2-months ahead)	GWL, R, Temp, Population, GR, SOI, NOI, NINO3	Monthly	70/30	2010–2017 (96 samples)
iu et al. (2022)	RF, SVM, GRNN, DT, CNN, LSTM, GRU	Long-term (Month-years-ahead)	Temperature, Humidity	Monthly	75/25	Jan 2000–Dec 2020 (Ĩ8 648 samples)
Guzman et al. 2019)	SVR, NARX	Short-term (days-ahead)	GWL R, Evapotranspiration	Daily	70/30	Jun 1985–Sep 1994 (259) samples)
Chen et al. (2020)	MLP, RBF, MODFLOW, SVM	Long-term (1 month-ahead)	SF, GWL	Daily	80/20	Jan 1986–Dec 2010 (300 samples)
						(continued on next po

In groundwater level (GWL) modeling, a wide variety of evaluation metrics have been employed. Fig. 7 shows the frequency of performance metrics reported in the reviewed literature. Among these, RMSE is the most frequently adopted, appearing in nearly 160 instances,

followed by R², correlation coefficient (Corr), and NSE. Metrics such as

MAE, MSE, and MASE are also widely used, reflecting a strong preference for error-based evaluations. In contrast, less common metrics like ME, RE, and NRMSE appear less frequently but still contribute to the assessment landscape. The "Others" category includes less standardized or study-specific measures.

Table 8 (continued)

Table 8 (continued).						
Kajewska- Szkudlarek et al. (2022)	SVR, MLP	Long-term (Monthly)	R, Temp, GWL	Monthly	75/25	1975–2014 (414, 411, 476 samples)
Zhang et al. (2018)	LSTM, FFNN	Long-term (1-month ahead)	R, Temp, Evaporation, Water Division, Time	Monthly	85/15	2000–2013 (168 samples)
Solgi et al. (2021)	LSTM-NN	Short&Long-term (days,months-ahead)	GWL	Monthly	80/20	Nov 1932–Jul 2020 (31 239, 1043 samples)
Haq et al. (2021)	LSTM-NN, ARIMA	Long-term (65 months ahead)	GRACE	Monthly	85/15	Jan 2003–Jun 2020 (185 samples)
Wu et al. (2021a)	LSTM	Short&Long-term (months-ahead)	River Stage, GWL	Monthly	70/30	Nov 2003-Dec 2019 (194, 10176, samples)
Ao et al. (2021)	LSTM, KNEA, GRU	Long-term (1-month ahead)	Temp, GWL, R, GSR, Irrigation Quantity	Monthly	70/30	1990–2015 (312 samples)
Gaffoor et al. (2022)	LSTM, GBDT	Long-term (1-month ahead)	Temp, GWL Anomaly, R, runoff, Evapotranspiration	Monthly	70/30, 80/20, 65/36	2009–2019 (42, 88 samples)
Kim et al. (2023)	LSTM	Short-term (2-weeks head)	Sun Hours, GWL Anomaly, R, runoff, Min Temp, Mean Wind Speed, Evaporation, R	Daily	90/10	2012–2021 (3653 samples)
Vu et al. (2023)	BiLSTM	Long-term (7,4,30-days ahead)	River Level, River Flux, Sea Level, R, Temp, Seinen River Data	Daily, Hourly	65/35	1971–2021 (5479 samples)
Manna and Anitha (2023)	DEBi-LSTM	Long-term (Multiple days ahead)	GW Recharge, Natural GW Discharge, R	Daily	60/40	2000 to 2021 (12 000 samples)
Patra et al. (2023)	LSTM	Short-term (Daily)	GWL	Daily	-	2013 83/17 Jun 2021 (139653 samples)
Foroumandi et al. (2023)	ConvLSTM, FFNN, RF	-	LST, NDVI, R, DEM, ET, SM, SWE	Monthly	70/30	Apr 2002–Dec 2016 (297 samples)
Lendzioch et al. (2021)	RF	-	GWL, NDVI, SM	Monthly	-	Aug 2018–Nov 2019 (630 samples)
Gonzalez and Arsanjani (2021)	RF, ANN, SVM	Long-term (years-ahead)	Max Temp, Min Temp, R, Mean Temperature, Topography	Monthly	80/20	1990–2018 (over 10 000 samples)
Zhou et al. (2022)	RF, SVR, ELM	Short-term (1,2,3-months ahead)	R, Temp, Actual Evapotranspiration, GLEAM, GLDAS	Monthly	80/20	Apr 2002–Jun 2017(183 samples)
Kalu et al. (2022)	DBN	Short-term (5-months ahead)	GWL, ENSO, NAO, AMO, IOD, PDO	Monthly	70/30	Nov 2007–Oct 2012 (1620 samples)
Hussein et al. (2020)	MLR, MLP, RF, XGB	Short-term (1-month ahead)	GRACE	Monthly	90/10	Mar 2002-May 2019 (161 samples)
Liu et al. (2021)	SVM	Short-term (3-months ahead)	GRACE, Temp, R, Solar Radiation, IST	Monthly	50/50	Jan 2007–Dec 2016 (5520 samples)
Yu et al. (2021)	SVM, BPNN, RBFNN	Short-term (Months ahead)	Meteorological, Socio-economic factors	Monthly	86/14	2004–2010 (168 samples)
Derbela and Nouiri (2020)	ANN	Medium-term (months-ahead)	R, GWL, Evapotranspiration	Monthly	80/20	2000–2018 (1944 samples)
Chenjia et al. (2024)	LSTM, GRU, MLP, 1DCNN, TR	Short-term (12,24,36-days ahead)	GWL, Extraction, ET	Daily	70/30	2017–2022 (2190 samples)
Akbari Majd et al. (2024)	ANN	Short-term (Months ahead)	Climate Variables	Monthly	70/30	2001–2019 (7068 samples)
Mohapatra et al. (2021)	DNN, ANFIS, SVM	Long-term (seasons ahead)	GWL, R, Temp,	Monthly	70/30	1996–2016 (835 044 samples) (continued on next page)

RMSE and R^2 are especially prominent choices because they provide complementary insights: RMSE quantifies the average magnitude of prediction error in the same units as the observed data, while R^2 measures the proportion of variance in the observations explained by the model. The choice of metric should be informed by the study's objectives, the characteristics of the dataset, and the model's intended application, ensuring that the evaluation process captures both accuracy and explanatory power.

5.3. Covariates used

ML models offer a unique advantage by learning patterns in data, whether simple or complex, to predict specific outcomes. In the context of this systematic review, we examine the use of different types of data for groundwater modeling, including climate variables, hydrogeological parameters, and aquifer characteristics, albeit the latter being

Table 8 (continued).

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Müller et al. (2021)	LSTM, MLP, RNN, CNN	Short-term (1-day ahead)	Streamflow, Temp, R	Daily	67/33	2010–2018 (2191 samples)
Sharghi et al. (2022)	FFNN, ANFIS, LSTM, GMDH	Long-term (1,2,3 - months ahead)	GWL, R, Runoff	Monthly	70/30	1989–2018 (17 640 samples)
Yin et al. (2021)	ANN, SVM, RSR, BMA	Short-term (1-month ahead)	ASR, GP, SWD	Monthly	80/20	Oct 1973–Sept 2015 (2016 samples)
Maheswaran and Khosa (2013)	ANN, LR, DAR	Long-term (multiple months ahead)	GWL	Monthly	90/10	1975–2002 (648 samples)
Dehghani et al. (2022)	SVR	Long-term (Months & Years ahead)	R, Temp, GWL, Water Withdrawal	Monthly	70/30	2000–2020 and 2021–2040 (960 samples)
Pham et al. (2022)	RT, Decision Stump, M5P, SVM, LWLR, REP, Tree	Long-term (months ahead)	GWL, Mean Temp, R, Humidity	Monthly	80/20	Jan 1981–Dec 2017 (888 samples)
Collados-Lara et al. (2023)	NARX, NAR, ELNN	Short-term (1–6 months ahead)	R, Min Temp, Max Temp	Monthly	70/30	Jan 2000–Jan 2020 (12852 samples)
Chang et al. (2016)	NARX	Short-term (1-month ahead)	GWL, SF, R	Monthly	80/20	2000–2013 (168 samples)
Banadkooki et al. (2020)	RBFNN, MLP	Short-term (months-ahead)	R, Temp	Monthly	70/30	2000–2012 (156 samples)
Guo et al. (2021)	ConvLSTM	Short-term (5-days intervals)	GWL, R, GSD, HPD	Monthly	70/30	Jan 2012-Dec 2012 (3456 samples)
Rafik et al. (2023)	RF, SVM	Short-term (Months-ahead)	TWS, R, ET, Q, SM, NDVI, and LST	Monthly	-	Apr 2002–2022 (264 samples)
Elmotawakkil et al. (2024)	GBR, SVR, RF, and DT	Short-term (Months-ahead)	ET, R, NDVI, and LST	Daily	70/30	Feb 2000–Feb 2023 (42 000 samples)
Bonkoungou et al. (2024)	NeuralProphet, LSTM, XGBoost	Short-term (multiple days ahead)	GWLs, R, and EVI	Daily	85/15	2010–2021 (26 298 samples)
Singh et al. (2024)	AutoML, RF, Boosting EL, BDT, GAM, GRNN, LR, ANN, SVR, RBNN, KR, LSTM	Long-term (quarterly seasons)	GWLs, EVAP, Temp, R, RH, Soil type	Monthly	70/30	1997–2018 (8310 samples)
Fahim et al. (2024)	MLR, Tree models, SVM, GPR, and ANN	Spatial prediction	GLDAS GWS data, ED, Temp, R, PD, ID, GRACE	Monthly	80/20	2003–2019 (183 samples)
Osman et al. (2024)	ANN, SVR, XGBoost, and LSTM	Short-term (1-day ahead)	R, Temp, EVAP, GWLs	Daily	70/30	Jan 2030–Dec 2039 (1390 samples)
Wei et al. (2023a)	ANN	Short-term (m \times 10-days ahead)	GWLs	Daily	80/20	1991–2015 (576 samples)
Seifi et al. (2024)	RVM, ANN, MLP	Short-term (1-month ahead)	R, Average Temp, RH, IRF	Daily	80/20	1995–2015 (252 samples)
Ali et al. (2024)	TFT, LSTM	Short-term (7,30,60 days ahead)	R, GWL	Daily	70/30	2001–2023 (8400 samples)
LaBianca et al. (2024)	CatBoost, GBDT, PB	Spatial prediction	DEM, LandUse, TS, GWLs	Monthly	67/33	2006–2022 (280 samples)
Moradi et al. (2023)	ANN, ELM, ORELM, and GMDH	Short-term (1-month ahead)	GWL, R, Temp, and EVAP	Monthly	80/20	2010–2016 (198 samples)
Heudorfer et al. (2023)	LSTM	Short-term (weeks ahead)	R, Temp, RH, Tsin	Weekly	50/50	Jan 2000–Dec 2015 (205 343 samples)
Roy et al. (2023)	ANFIS, Bagged RF, Boosted RF, GPR, LSTM MARS, SVR	Short-term (1–3 weeks ahead)	GWLs	Weekly	70/30	Feb 1984–Sep 2018 (7228 samples)
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non-mandatory compared to conventional models. The choice of these covariates is critical, significantly affecting model performance.

Groundwater levels are closely tied to climate conditions, and the ever-growing concerns of climate change, marked by events like droughts, floods, and shifting precipitation patterns, emphasize the urgency of groundwater management. Fig. 8 shows that historical GWL data is the most employed covariate for ML models predicting groundwater levels.

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Chi et al. (2024)	WT-Model	Short-term (7-days ahead)	Temp and R	Daily	80/20	Jan 2009–Jun 2020 (5223, 609 samples)
Abdi et al. (2024)	CNN, DNN	Short-term (1-month ahead)	GWS	Monthly	70/30	2018–2021 (1632 samples)
Zowam and Milewski (2024)	SVR, RF	Long-term (1-month ahead)	R, SM, ET, LST, VI, CN, SHC, and GSA	Monthly	60/40 and 85/15	Jan 2010–Dec 2019 (7080 samples)
Zhu et al. (2024)	GBDT	Short-mid-term (days,month-ahead)	GWL, R, Q, CWD	Monthly	70/30	Jan 1997 to Dec 2011 (163155 samples)
Feng et al. (2024)	CNN, RNN, SVM, DT, RF, and GAN	-	GRE, R, and RFR	Monthly	70/30	2018–2022 (2136 samples)
May-Lagunes et al. (2023)	XGBoost, RF, TFT, GDR, LR	Short-term (3-months ahead)	SWE, ET, WSE	Monthly	-	2010–2020 (3960 samples)
Jing et al. (2023)	RF, XGBoost, GBR, LightGBM, LSTM	-	R, ET, RD, GWL	Daily	-	2003–2014 (1584 samples)
Zheng et al. (2024)	iTransformer, LSTM	Short-term (4-months ahead)	Agricultural irrigation, climatic component, basin factor, and human factor	Hourly	-	Jul 2021-Sep 2022 (24678 samples)
Hikouei et al. (2023)	RF, XGBoost, MLR	-	GWL ET ET, R, Z, DFC	Monthly	80/20	2010–2012 (11 641 samples)
Seidu et al. (2023)	ANN, BPNN, RBFNN, GMDH, GRNN	-	R, EVAP, Temp	Monthly	50/50, 60/40, 70/30, 80/20, 90/10	2013–2018 (676 samples)
Yi et al. (2024)	RF, ANN, SVR, GB, XGBoost	Short-term (1-day ahead)	DWL, R	Daily	80/20	2011–2021 (17 350 samples)
Chidepudi et al. (2023)	LSTM, BiLSTM, GRU	Short-term (Daily)	TEMP, R	Daily	80/20	1970–2020 (600)
Sriram et al. (2023)	RF, ML, MD, KNN	-	-	-	-	- (4044 samples)
Sun et al. (2023)	LSTM, PB	Short-term (3-months ahead)	R, WS, GWL, Q	Daily	80/20	Jan 2018–Sep 30 (68 958 samples)
Elzain et al. (2024)	CBR, XGB, LGBM, LSTM, GRU	Short-term (1,2,3-weeks ahead)	WTR	Daily	90/10	Dec 2017–Jan 2019 (19 465 samples)
Chen et al. (2023)	CBR, XGB, LGBM, LSTM, GRU	Short-term (1–10 days ahead)	GWL, R	Daily	70/30	2002–2021 (7305 samples)
Sarkar et al. (2024)	KNN, SVM-RBF, PR, XGB, RF	-	GRACE	Daily	83/13	Jan 2022–Oct 2022 (177 samples)
Ehteram et al. (2023)	SATCN, LSTM	Short-term (1-month ahead)	Temp, R, Elevation, WS, RH, GWL	Monthly	75/25	1995–2010 (192 samples)
Niu et al. (2023)	SVM	Short-term (1-month ahead)	R, wind speed WS, Temp, POP,GDP, EIA	Monthly	60/40	Jan 1991–Dec 2019 (240 samples)
Kayhomayoon et al. (2023)	SVR, Least-Square SVR (LSSVR), MODFLOW	Long-term (Years ahead)	GWL, Recharge, Withdrawal	Monthly	75/25	Oct 2010–Sep 2013 (150 samples)
Bai and Tahmasebi (2023)	GWN, GWN-adaptive, LSTM, GRU	Long-term (Multiple weeks ahead)	Temp, R, VP, SR, day	Weekly (GWL), Daily (Climate)	60/40	2010–2020 (23 452 samples)
Nan et al. (2023)	Attention-GRU, LSTM, RNN, CNN	Short-mid-term (6-months ahead)	GWL, R, Temp, ELEV, SM	Monthly	75/25	2017–2022 (24120 samples)
Li et al. (2023)	MLR, MARS, ANN, RFR, GBR	-	ELEV, soil type, Climate Data, NDVI	Seasonal	84/16	Oct 2005–Sep 2007 (75 samples)
Nand et al. (2024)	MLP-GA, MODFLOW	Long-term (Annual/Seasons ahead)	ETC, R, GR, GD	Annual	67/33	2000–2015 (880 samples)
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Bhadani et al. (2024)	F-IWO-GWL, RF, BoosteL, BDT, LSTM, SVR, GAM, ANN, RBNN, GRNN, hybrids	Short-mid-term (Annual/Seasons ahead)	R, Temp, ET, RH, GWL	Daily	70/30	1997–2018 (8310 samples)
Sun et al. (2024)	Transformer, MLP, LSTM, CNN	Short-term (10, 20 days ahead)	R, Flow, GWL	Daily	60/40	2000–2019 (725 samples)
Zhang et al. (2023)	TCN, LSTM	Short-term (1,3,7,15-days ahead)	Tidal-level, R, GWL	Hourly	80/20	Oct 2011–Oct 2012 (28 836 samples)
Xie and Zhang (2024)	STA-GRU, LSTM, GRU, CNN+GRU, CNN+BiLSTM+ Attention	Short-term (1-month ahead)	Climate, hydrogeological, Topographic	Monthly	70/30	2017–2117 (7272 samples)
Zhou et al. (2024)	LSTM	Short-term (1-month ahead)	GWL	Monthly	81/19	2018–2022 (20 340 samples)
Wei et al. (2023b)	M5, RF, GRBFN, MLP, Ensemble methods	Spatial (No time-series)	Remote sensing Data	-	80/20	2018 (436 samples)
Wang et al. (2024)	LSTM, RR-LSTM, Geo-RR-LSTM, ARIMA, ARIMAX, MLR	Long-term (1-year ahead)	R, geographical features	Monthly	78/22	2009–2013 (3816 samples)
Su et al. (2024)	MLR, SVR, LSTM	Long-term (20-months ahead)	GWL, Extraction	Daily	89/11	2007–2021 (964 260 samples)
Wu et al. (2023)	SVM, LSTM, MLP, GRU	Short-term (1-h ahead)	GWL	Hourly	70/30	2018–2020 (32880 samples)
Eghrari et al. (2023)	LSTM, GRU	Long-term (Monthly)	Climate Data	Monthly	80/20	Nov 2002–Jun 2022 (1652 samples)
Fronzi et al. (2024)	Prophet, ARIMA, MARS, ETS	Short-term (2-weeks ahead)	GWL, Hydrological, Exogenous, Atmospheric	Daily	87/13	Mar 2023–Apr 2023 (485 samples)
Gupta et al. (2024)	RF, Bagging- REPTree, Bagging-DSTree	Seasonal	variables GWL	Seasonal	70/30	1997–2018 (616 samples)
Ghazi et al. (2021)	ANN, LSSVM, NARX	Long-term (Years ahead)	R, Temp, Time Delay	Monthly	70/30	1966–2019 (6840 samples)
Idrizovic et al. (2020)	ANN	Long-term (Years ahead)	R, Temp, PET, GWL	Daily and monthly	70/30	1988–2016 (342 samples)
Karthikeyan et al. (2013)	FFNN, RNN	Short-term (1-week ahead)	R, Temp, EVAPO, GWL	weekly	70/30	May 2004–May 2006 (109 samples)
Yan and Ma (2016)	ARIMA, RBFN	Short-term (1-month ahead)	GWL	monthly	83/17	Jan 1998–Dec 2010 (144 samples)
Secci et al. (2023)	NARX, LSTM, CNN	Long-term (years ahead)	R, Temp	monthly	90/10	Mar 2005–Dec 2020 (190 samples)
Fallah-Mehdipour et al. (2013)	ANFIS, GP	Medium-term (months)	EVAPO, R, GWL	monthly	86/14	7-year (84-month) (252 samples)

Abbreviations: R, Precipitation; SM, Soil moisture; E, efficiency coefficient; LWLR; locally weighted linear regression, REP Tree; reduce error pruning tree; TWI, Topographic wetness index; TPI, Topographic position index; TRI, Topographic roughness index, Dd; Drainage density; Dff, Distance from fault; NDVI, Normalized Difference Vegetation Index; DEM: Digital Elevation Map; GSR; Global Solar Radiation, IST; Infrared Surface Temperature, Streamflow; SF, Seasonal Dummy Variables, SDV; Streamflow Discharge, SD; Aquifer Discharge, AD; Linear Regression, LR; Dynamic Auto-Regressive, DAR; Nash sutcliffe criteria, NSC; Geological Structure Data, GSD; Hydrogeological Parameter Data; HPD, Terrestrial Water Storage; TWS, evaportanspiration; ET, Soil Moisture; SM, Gradient Boosting Regression; GBR, Enhanced Vegetation Index; EVI, Runoff; Q, Fuzzy Inference Systems; FIS, Teaching-Learning Based Optimization; TLBO, Ant Colony Optimization; ACO, Harmony Search; HS, Evaporation; EVAP, Relative Humidity; RH, Self-Normalizing Neural Network; SNN, Standardized Bathymetry Data; SBA, Population Data; PD, ID; irrigation data, elevation data; ED, phase space reconstruction; PSR, Relevance Vector Machine; RVM, multivariate variational mode decomposition; MVMD, Boruta feature selection algorithm; BFSA; Irrigation Flow; IRF, Temporal Fusion Transformer; TFT, Bayesian optimization; BO, Terrain slope; TS, Group Method of Data Handling; GMDH, Annual sinusoidal curve fitted to temperature; Tsin, drainage_volumes; V, drainage_volumes; V, groundwater surfaces; GWS, Empirical Bayesian kriging; EBK, Land Surface Temperature; LST, Generative adversarial network; GAN, Groundwater extraction rate; GRE, River flow rate; RFR, crop water demands; CWD, Temporal Fusion Transformer; TFT, Gradient Descent Regressor; GDR, Snow water equivalent; SWE, Water Surface Elevation; WSE, River Discharge; RD, Elevation; Z, and Distance from canal; DFC, Daily weir level; DWL, Transformer; TR, LightGBM; LGBM,CatBoost Regressor; CBR, Water Table Rise; WTR, Polynomi

Out of 223 papers, 187 incorporate groundwater level data as an input, with 77 using it as the sole input without additional factors. Precipitation data is also frequently used, appearing in 161 instances.

Other hydrological data, such as temperature, river discharge, evapotranspiration, and surface water levels, have been employed as inputs. Some papers have explored additional variables like irrigation patterns,

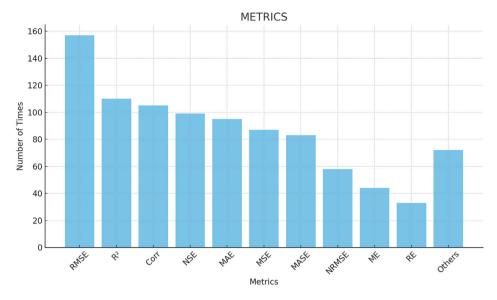


Fig. 7. Various metrics used in validation reviewed ML models' performance.

Table 9Feature selection methods identified in groundwater level (GWL) modeling studies, organized by general category. This taxonomy reflects common practice but is not absolute, as some methods overlap across categories.

, 1	
Feature selection method	Type
Autocorrelation Function (ACF)/Partial ACF (PACF)	Filter
Mutual Information (MI)	Filter
Cross-correlation analysis	Filter
Correlation matrix/Pearson/Spearman correlations	Filter
Principal Component Analysis (PCA)	Filter
Grey Relational Analysis (GRA)	Filter
Factor Analysis (FA)	Filter
Hellwig method	Filter
Variance Inflation Factor (VIF)	Filter
Multicollinearity test	Filter
Lyapunov exponent + Phase Space Reconstruction (PSR)	Filter
Wavelet decomposition/Variational Mode Decomposition (VMD)	Filter
Recursive Feature Elimination (RFE)	Wrapper
Forward Feature Selection (FFS)	Wrapper
Taguchi design method	Wrapper
Genetic Algorithm (GA)	Wrapper
Particle Swarm Optimization (PSO)	Wrapper
Ant Colony Optimization (ACO)	Wrapper
Boruta algorithm	Wrapper
Internal validation performance-based selection	Wrapper
SHAP (SHapley Additive exPlanations)	Embedded
GINI importance (from decision trees)	Embedded
Permutation Feature Importance (PFI)	Embedded
Model-derived importance (RF, XGBoost, MARS, etc.)	Embedded
Growing Neural Gas (GNG) clustering	Embedded
Model-based interpolation (e.g., M5P)	Embedded

Note: Some methods fall at the boundary of categories. For example, Boruta leverages Random Forest importance measures but is generally treated as a wrapper due to its iterative retraining process. Permutation Feature Importance (PFI) is technically post-hoc but grouped under embedded methods here because it is tied directly to fitted models. Wavelet and variational mode decomposition (VMD) are primarily preprocessing/feature extraction steps but are treated as filter techniques in this context.

population figures, seasonal factors, and more, though to a lesser extent. These variables may present challenges during the input selection process.

5.4. Programming languages utilized

In the review, we realized that most of the research papers used MATLAB, PYTHON, and R to build the various ML algorithms used. Researchers predominantly utilizing these programs for developing

machine learning algorithms in their studies can be attributed to the fact that these programming languages offer extensive libraries and frameworks specifically tailored for machine learning, simplifying algorithm development and implementation. Python, in particular, boasts a vast machine-learning ecosystem, including popular libraries like Scikit-Learn and TensorFlow, making it highly versatile and ideal for a wide variety of ML tasks.

R is favored for its exceptional statistical capabilities and visualization tools, providing researchers with robust data analysis and model interpretation capabilities alongside machine learning functionalities. These languages are open-source, facilitating collaboration and accessibility for researchers globally, while also significantly reducing research costs. Their active and supportive communities continuously contribute to the development and improvement of machine learning tools and resources, ensuring researchers have access to the latest advancements in the field. Information regarding these software programs is available online, and we do not delve into their specifics here. Nevertheless, it is noteworthy that MATLAB is commonly favored in the development of AI models, although several papers have not explicitly mentioned the software used.

5.5. Time steps and forecast horizons

Fig. 9 shows the time steps used in the reviewed GWL modeling studies. Most studies (187 papers) employed monthly data, followed by daily (19) and hourly (8) intervals. Weekly, biweekly, and bimonthly resolutions appeared only rarely. The dominance of monthly data can be partly attributed to its wider availability from monitoring networks and its suitability for capturing the delayed recharge response of precipitation, which must travel through the vadose zone before reaching the water table. In inland aquifers, groundwater levels often vary slowly, making coarse temporal resolution sufficient. In contrast, coastal aquifers (Yoon et al., 2011; Taormina et al., 2012) and areas near large reservoirs (Rajaee et al., 2019) require finer time steps to represent rapid tidal or reservoir-driven fluctuations.

A notable trend shown in Table 8 is the strong emphasis on short-term forecasts (3rd column), typically ranging from days to a few months, in the majority of studies. This focus reflects the strengths of machine learning models, which are effective at capturing recent patterns and correlations directly from data. However, the predictive accuracy of ML models tends to decline as the forecasting lead time increases (Shirmohammadi et al., 2013; Sun et al., 2016; Yu et al., 2018; Wu et al., 2021b; Momeneh and Nourani, 2022; Roy et al., 2023).

Table 10
Comparison of optimization algorithms (Gandomi and Alavi, 2012; Mehrabian and Lucas, 2006; Saremi et al., 2017; Mafarja et al., 2019; Wang et al., 2018; Asgari et al., 2016; Chandirasekaran and Jayabarathi, 2019; Puente et al., 2009).

Algorithm	Type of optimization	Advantages	Disadvantages
GA	Evolutionary	-Good for global optimization -Flexible and adaptable -Handles complex spaces	-Requires careful parameter tuning -Can be computationally intensive -May converge to local optima
CSO	Swarm intelligence	-Balances exploration and exploitation -Good for dynamic problems -Simple implementation	-Sensitivity to parameters -Requires parameter tuning -Can be slow in convergence
PSO	Swarm intelligence	-Simple implementation -Few parameters to adjust -Efficient global search	-May get stuck in local minima -Sensitivity to initial settings -Can require many iterations
GOA	Swarm intelligence	-Balances exploration and exploitation -Effective for continuous problems -Adaptable to various problems	-Computationally expensive -Sensitive to parameter settings -May require many iterations
WOA	Bio-inspired	-Good for dynamic environments -Mimics natural adaptability -Simple concept to understand	-Can be computationally demanding -Requires careful tuning -Sensitivity to initial population
КНА	Swarm intelligence	Effective in multi-modal problems Adaptive to problem complexity Good convergence properties	Computationally intensive Sensitive to parameters Requires many iterations
ACO	Swarm intelligence	-Good for combinatorial problems -Utilizes collective intelligence -Finds good paths through search space	-Can be slow to converge -Parameter sensitive -May require large computational resources
BWO	Bio-inspired	-Early convergence due to cannibalism -Maintains diversity -Simple implementation	-Risk of losing good solutions -Sensitive to cannibalism and mutation rates -Requires careful tuning

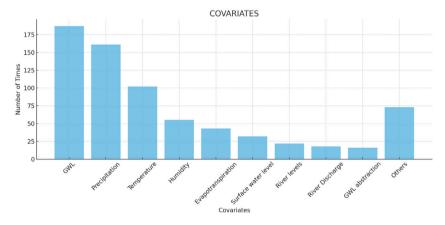


Fig. 8. Various covariates employed in reviewed articles.

Over longer horizons, these models may experience error accumulation and reduced generalization, especially when future conditions differ from those present in the training data.

Time step choice is closely linked to the intended forecast horizon. Short-term predictions often employ daily or hourly steps to capture high-frequency variations (Wu et al., 2023; Zhang et al., 2023; Sun et al., 2024), while long-term studies generally adopt monthly intervals to reflect slower groundwater responses (Ghazi et al., 2021; Eghrari et al., 2023; Zowam and Milewski, 2024). Selecting an appropriate combination of time step and forecast horizon should be guided by the dynamics of the aquifer system and the overall purpose of the prediction, balancing the short-term skill of ML methods with the need for robustness in longer-term projections.

6. Implications and future directions

This review identifies several key methodological patterns and research gaps that can inform future GWL modeling efforts and guide the development of more robust, interpretable, and operational models.

First, the lack of comparative studies on feature selection methods represents a major limitation. Although various techniques such

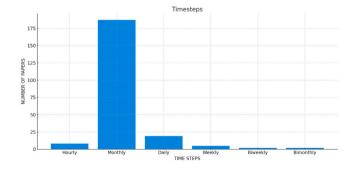


Fig. 9. Different time steps used in GWL modeling.

as mutual information, cross-correlation, importance of permutation, SHAP, and elimination of recursive features have been used in studies, very few have systematically evaluated their impact within a consistent modeling framework. Given the strong influence of input features on

model performance, future research should prioritize controlled comparisons of feature selection strategies, especially in cases involving high-dimensional or multi-source inputs.

Second, the consistent superiority of hybrid models over standalone approaches highlights a promising direction. Many hybrid frameworks, such as LSTM-CNN or RF-GA, combined different model components or algorithms to address specific limitations. For instance, decomposition methods like EMD and VMD (Wu et al., 2021b) helped isolate signal components with clearer temporal patterns, making them easier to model. Optimization algorithms such as GA and PSO were often used to fine-tune hyperparameters, reducing manual trial-and-error. Ensemble techniques also improved prediction by combining outputs from multiple learners (Yin et al., 2021), reducing variance and enhancing robustness. These strategies allowed hybrid and ensemble models to better capture the complex, nonlinear, and multi-scale dynamics of groundwater systems. Future studies should explore their broader integration, particularly in conjunction with hybrid model architectures.

Third, recent developments in deep learning point to new opportunities. Transformer-based architectures, though used in only a few studies, demonstrated strong predictive capabilities and the ability to handle long sequences and complex dependencies. Their limited use in groundwater applications suggests a valuable area for further exploration, especially for multi-step forecasting or spatially distributed predictions.

Fourth, this review finds that remotely sensed data, particularly from GRACE satellites, offer great promise for groundwater modeling in data-scarce regions. GRACE-derived storage changes, while only used in a few studies, enhanced prediction accuracy and captured large-scale dynamics that in-situ measurements could not. There is a strong case for integrating remote sensing into machine learning workflows, especially in regions with sparse monitoring networks.

Additionally, long-term prediction horizons (beyond one year) remain a significant gap, with very few studies attempting extended forecasts due to data limitations, non-stationarity, and issues like model drift. This is particularly relevant for water planning and early warning systems. Addressing this will require robust temporal validation strategies and possibly the integration of seasonal climate forecasts.

Also, despite limited datasets, most ML-based GWL studies achieved strong short-term predictive accuracy. A majority of the reviewed models were developed using relatively small datasets, often fewer than 500 samples, yet still demonstrated high performance, particularly for short-term forecasts. This confirms the flexibility of ML models in data-scarce settings, especially when supported by decomposition, optimization, and appropriate input selection. However, the predictive accuracy of ML models tends to decline as the forecasting lead time increases, as shown by Shirmohammadi et al. (2013), Sun et al. (2016), Yu et al. (2018), Wu et al. (2021b), Momeneh and Nourani (2022) and Roy et al. (2023).

A notable mention in the reviewed literature is the consistent commendation of Long Short-Term Memory (LSTM) networks for their strong performance in long-term groundwater level forecasting (Kajewska-Szkudlarek et al., 2022; Zhang et al., 2018; Solgi et al., 2021; Haq et al., 2021; Wu et al., 2021a; Ao et al., 2021). These studies highlighted LSTM's ability to capture complex temporal dependencies and delayed hydrological responses, even under extended lead times. Ao et al. (2021), in particular, compared LSTM with Kernel-based Nonlinear Extreme Learning Algorithm (KNEA) and Gated Recurrent Unit (GRU) models across multiple districts, and found that LSTM not only achieved a good accuracy but also demonstrated better generalization across spatially distinct sites. This is likely due to LSTM's internal memory and gated structure, which allow it to retain relevant information over long sequences, making it especially suitable for modeling persistent and gradual groundwater dynamics.

While few studies directly compared ML with conceptual models, Chen et al. (2020) found that physically based models like MOD-FLOW offered better generalization under varying conditions because

of the inclusion of physical mechanisms, although not higher short-term accuracy. Based on these findings, future studies could explore combining both approaches. For example, a physically based model could simulate the overall groundwater system, while a machine learning model could improve predictions by learning from the errors or gaps in the physical model. Sun et al. (2023) demonstrated the value of this approach by integrating LSTM with a PB model, achieving prediction accuracy improvements for over 67% of wells when PB model performance was moderate or better, and over 77% when PB performance was poor. Similarly, Kayhomayoon et al. (2023) combined MODFLOW with support vector regression variants, showing that the MODFLOW-LSSVR configuration achieved near-perfect accuracy (NSE = 0.998) in forecasting groundwater levels under climate change scenarios. These examples illustrate how physically consistent PB outputs can provide a robust baseline, while ML components refine predictions by capturing nonlinear and site-specific dynamics. This kind of setup could help improve forecast accuracy across both short- and long-term timeframes.

Finally, the near absence of socio-economic and anthropogenic factors in GWL modeling remains a critical oversight. Land use change, irrigation practices, and population pressures play a significant role in groundwater dynamics, yet are rarely modeled. Future work should consider coupling physical and socio-economic data to capture humanwater interactions more effectively.

7. Limitations

Although we employed a broad and comprehensive set of keywords to capture a wide range of relevant studies, systematic reviews are inherently challenged by the diversity of terminology used in the literature. For example, some studies may refer to "groundwater level" as "water table" or use "forecasting" instead of "prediction". Similarly, certain papers highlight specific algorithms without explicitly mentioning "machine learning" or "AI". While our expanded keyword strategy mitigated much of this risk, it remains possible that a small number of relevant studies were omitted.

Another limitation is the tendency of the reviewed literature to predominantly report positive results of machine learning applications. Few studies explicitly discussed the failures or shortcomings of the models they employed. This publication bias may have led to an overrepresentation of successful applications, thereby limiting the scope for a balanced evaluation of machine learning performance.

Finally, our review focused exclusively on peer-reviewed journal articles. This decision was intended to ensure methodological rigor and comparability, but it also excluded potentially valuable insights from grey literature, such as conference papers, theses, or technical reports. While including these sources might have broadened the perspective, it would also have increased heterogeneity and made systematic analysis more challenging.

8. Conclusion

ML models have shown significant promise in hydrology and groundwater modeling. This review examines 223 research articles, published from 2010 to 2024, focusing on ML applications in groundwater level (GWL) modeling across diverse geographical settings. These models excel at identifying complex patterns in groundwater datasets, enabling accurate GWL simulations and predictions. Key findings emphasize the critical roles of variable selection, hyperparameter tuning, model architecture, and data preprocessing in achieving optimal model performance. Selecting relevant variables and employing effective preprocessing and optimization techniques can significantly enhance model accuracy and reliability. This review offers practical guidance for researchers adopting ML models for GWL studies, highlighting best practices in variable selection, architecture design, and optimization strategies to improve the accuracy and interpretability of ML-based groundwater predictions

- 1. During the review, feature selection methods such as correlation analysis and SHapley Additive exPlanations (SHAP) were identified, but no single optimal method emerged. The choice depends on data characteristics, model needs, and research objectives, encouraging researchers to test multiple techniques for relevance. Linear correlation, widely used, assumes proportional relationships between variables. However, groundwater systems involve complex, non-linear interactions like precipitation and aquifer properties, which linear methods often overlook, affecting model performance (Huang et al., 2017). Advanced methods, including mutual information, recursive feature elimination, and model-based approaches, are recommended for identifying features in non-linear contexts.
- 2. Most studies relied on trial-and-error for hyperparameter tuning, but combining machine learning models with optimization algorithms consistently improved performance. particle swarm optimization (PSO), known for strong global search capabilities, was particularly effective for SVM (Lin et al., 2008; Fei et al., 2009; Huang et al., 2017). Other algorithms, such as Genetic Algorithm (GA), Ant Colony Optimization (ACO), and Grasshopper Optimization Algorithm (GOA), offered robustness and adaptability. However, research on newer techniques like Weed Optimization Algorithm (WOA) and Black Widow Optimization (BWO) remains limited in GW Level modeling studies using ML. Further exploration of these methods is recommended to enhance model performance and optimization.
- 3. Our review of hybrid models, particularly those integrating wavelet transforms with machine learning, highlights their value for improving groundwater level simulations (e.g., Adamowski and Chan, 2011; Nourani et al., 2015; Ebrahimi and Rajaee, 2017; Wei et al., 2023a; Saroughi et al., 2024). Daubechies wavelets, especially db2 and db4, were widely used. Their popularity may be due to their short support and strong time localization, which help capture sudden fluctuations in groundwater signals. However, because they rely on downsampling, they may distort temporal alignment. To address this, some studies used the à trous wavelet transform, which maintains the original signal length and better preserves structure in seasonal or noisy data. The à trous method has been described as well suited for forecasting applications (Mallat, 1989; Bahaa et al., 2015).
- 4. It is not possible to recommend a single best ML model for simulating groundwater levels, but the review shows that hybrid models consistently performed better than individual models. This advantage often results from improved handling of signal complexity, more effective parameter tuning, and reduced overfitting. Some studies (Yin et al., 2021) also applied ensemble techniques like Bayesian model averaging, where combining predictions from multiple models produced more stable and accurate results than any standalone model. By testing and combining different models, it is possible to achieve optimal performance in groundwater level simulations.
- 5. Our review identified Self-Organizing Maps (SOM), Growing Neural Gas (GNG), Fuzzy C-Means (FCM), and K-means as common clustering techniques, particularly in studies utilizing GRACE-derived Terrestrial Water Storage Anomaly (TWSA) data for downscaling to finer resolutions. These algorithms effectively clustered TWSA data to identify similar pixels for inputs and outputs, enhancing GWL understanding in areas with limited observations. SOM was also applied to optimize the number of hidden layer neurons, improving standalone model accuracy. However, most studies relied on trial and error for model structure, highlighting a gap in systematic research.

- 6. Among the 223 articles reviewed, the data splits for training and testing varied from 50%–50%, 56%–44% (Chang et al., 2015; Seidu et al., 2023; Heudorfer et al., 2023) to 90%–10% (Maheswaran and Khosa, 2013; Bahaa et al., 2015; Secci et al., 2023), with an 80/20 split being the most common. Most studies used monthly datasets spanning over 10 years, with sample sizes ranging from 35 (Mukherjee and Ramachandran, 2018), 48 (Guo et al., 2021), 23,850 (Taormina et al., 2012), 445,104 (Sahoo et al., 2017) 835,044 (Mohapatra et al., 2021) to 964,260 (Su et al., 2024). Larger datasets, particularly for training, generally improved model performance.
- 7. We recommend further exploration of modeled meteorological variables from IPCC climate change scenarios, such as Shared Socioeconomic Pathways (SSPs) and Representative Concentration Pathways (RCPs), as inputs for GWL models. Assessing how well these models simulate future conditions under climate change is crucial but currently underexplored. Only a hand full of studies explored this in detail (e.g. Javadinejad et al. (2020), Secci et al. (2023) and Osman et al. (2024)). Expanding this research could deepen our understanding of climate impacts on groundwater resources and improve future resource management strategies.
- 8. Finally, future work should explore combining physically based models with machine learning to benefit from the process representation of conceptual models and the pattern-learning strengths of ML. Recent work by Sun et al. (2023) demonstrated that integrating LSTM with physically based models can substantially improve prediction accuracy, especially when the physical model's performance is moderate or poor. Given the strong long-term forecasting performance of LSTM under datascarce conditions (Gaffoor et al., 2022), it is a strong candidate for inclusion in such hybrid frameworks. This integration could enhance forecast robustness across varying time horizons, and model development should also move beyond trial-and-error by adopting more systematic optimization techniques.

List of abbreviations

AI	Artificial Intelligence
ANN	Artificial Neural Network
ANFIS	Adaptive Neuro-Fuzzy Inference System
ACF	Autocorrelation Function
PACF	Partial Autocorrelation Function
MI	Mutual Information
SHAP	SHapley Additive exPlanations
RFE	Recursive Feature Elimination
PSO	Particle Swarm Optimization
GA	Genetic Algorithm
ACO	Ant Colony Optimization
CNN	Convolutional Neural Network
LSTM	Long Short-Term Memory
RF	Random Forest
SVM	Support Vector Machine
MLP	Multilayer Perceptron
GWL	Groundwater Level
\mathbb{R}^2	Coefficient of Determination
RMSE	Root Mean Square Error
MAE	Mean Absolute Error
MSE	Mean Squared Error
ME	Mean Error
RE	Relative Error
GCM	Global Climate Model
GRACE	Gravity Recovery and Climate Experiment
DA	Data Assimilation
WOA	Weed Optimization Algorithm

BWO	Black Widow Optimization
LM	Levenberg-Marquardt
BR	Bayesian Regularization
ARX	AutoRegressive with eXogenous inputs
FCM	Fuzzy C-Means
SOM	Self-Organizing Maps
GNG	Growing Neural Gas
SSPs	Shared Socioeconomic Pathways (SSPs)
RCPs	Representative Concentration Pathways
GOA	Grasshopper Optimization Algorithm
CSO	Cat Swarm Optimization
KHA	Krill Herd Algorithm

CRediT authorship contribution statement

Gilbert Jesse: Writing – review & editing, Writing – original draft, Visualization, Validation, Software, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. Cyril D. Boateng: Writing – review & editing, Validation, Supervision, Resources, Project administration, Methodology, Investigation, Funding acquisition, Conceptualization. Jeffrey N.A. Aryee: Writing – review & editing, Validation, Supervision. Marian A. Osei: Writing – review & editing, Validation, Supervision. David D. Wemegah: Writing – review & editing, Validation, Supervision. Solomon S.R. Gidigasu: Writing – review & editing, Validation, Supervision. Akyana Britwum: Writing – review & editing, Validation, Data curation. Haoulata Touré: Writing – review & editing, Validation. Vera Mensah: Writing – review & editing, Validation. Prinsca Owusu-Afriyie: Writing – review & editing, Validation, Data curation.

Computer code availability

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Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Appendix A. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.acags.2025.100303.

Data availability

No data was used for the research described in the article.

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