Forecasting the Gulf Stream Path using Buoyancy and Wind Forcing over the North Atlantic

Submitted: May 27, 2021; Revised: July 19, 2021; Accepted: July 26, 2021

Adrienne Silver¹, Avijit Gangopadhyay¹, Glen Gawarkiewicz², Arnold Taylor³ and Alejandra Sanchez-Franks⁴

¹School for Marine Science and Technology, University of Massachusetts Dartmouth, MA, 02747, USA ²Woods Hole Oceanographic Institution, Woods Hole, MA, 02543, USA ³Plymouth Marine Laboratory, Prospect Place, West Hoe, Plymouth, PL1 3DH, England, UK ⁴National Oceanography Centre, Southampton SO14 3ZH, UK

Key Points:

3

4

5

10

11	•	The Parsons-Veronis hypothesis on the separation of the Gulf Stream appears to
12		hold true for at least the last 40 years (1980-2019).
13	•	The forecasting model of the Gulf Stream path (75-65°W) uses the previous year's
14		path, space-time integrated winds and Icelandic low location.
15	•	The model shows a correlation of 0.65 for its one-year forecast compared to the
16		actual path for the years 1994-2020.

Corresponding author: Adrienne Silver, asilver@umassd.edu

17 Abstract

Fluctuations in the path of the Gulf Stream (GS) have been previously studied by 18 primarily connecting to either the wind-driven subtropical gyre circulation or buoyancy 19 forcing via the subpolar gyre. Here we present a statistical model for one year predic-20 tions of the GS path (represented by the GS northern wall - GSNW) between 75°W and 21 $65^{\circ}W$ incorporating both mechanisms in a combined framework. An existing model with 22 multiple parameters including the previous year's GSNW index, center location and am-23 plitude of the Icelandic Low and the Southern Oscillation Index was augmented with basin-24 25 wide Ekman drift over the Azores High. Addition of the wind is supported by a validation of the simpler two-layer Parsons-Veronis model of GS separation over the last forty 26 years. A multivariate analysis was carried out to compare one-year-in-advance forecast 27 correlations from four different models. The optimal predictors of the best performing 28 model include: (i) the GSNW index from the previous year, (ii) gyre-scale integrated Ek-29 man Drift over past two years, and (iii) longitude of the Icelandic Low center lagged by 30 three years. The forecast correlation over the 27-years (1994-2020) is 0.65, an improve-31 ment from the previous multi-parameter model's forecast correlation of 0.52. The im-32 provement is attributed to the addition of the wind-drift component. Sensitivity of fore-33 casting the GS path after extreme atmospheric years are quantified. Results indicate pos-34 sibility of better understanding and enhanced predictability of the dominant wind-driven 35 variability of the Atlantic Meridional Overturning Circulation and of fisheries manage-36 ment models that use the GS path as a metric. 37

³⁸ Plain Language Summary

The position of the Gulf Stream, the western boundary current in the North At-39 lantic, after it detaches from the coast can affect processes from fisheries to atmospheric 40 events and is an indicator of climate change. In this paper we were able to create a fore-41 casting model predicting the position of the northern wall of the Gulf Stream one year 42 in advance. This model incorporated integrated winds generated from the Azores High 43 and the Icelandic low, the two major atmospheric pressure centers over the North At-44 lantic. The correlation between the predicted latitude from the model with the observed 45 Gulf Stream North Wall index for over twenty-seven years is 0.65. The ability to cor-46 rectly predict the Gulf Stream path has important implications for improving the man-47 agement of Living Marine Resources. 48

49 **1** Introduction

In the North Atlantic subtropical gyre, the Gulf Stream (GS) is the northward flow-50 ing geostrophic current that is topographically bound until it reaches the latitude of Cape 51 Hatteras, where it separates from the coast and becomes a 'free-wheeling' jet. The lat-52 itudinal excursion of the GS meanders from its mean path are on the order of 100-200 53 km after it departs from the coast (Cornillon, 1986). This path variability has been linked 54 to multiple processes spanning from fisheries (Nye et al., 2011) to atmospheric events 55 (Joyce et al., 2009) and is often interpreted as an indicator of climate change (Zhang et 56 al., 2019; Caesar et al., 2018). In particular recent rapid changes in the northwest At-57 lantic water properties and ecosystem responses have been linked to the variations of the 58 GS path and its instabilities (Pershing et al., 2015; Mills et al., 2013; Gawarkiewicz et 59 al., 2012, 2018, 2019; Andres, 2016; Brickman et al., 2018; Gangopadhyay et al., 2019; 60 Silver et al., 2021) 61

The path of the GS from the separation point up to 65°W and beyond has often been quantified with one single metric – called the Gulf Stream North Wall (GSNW) Index. The GSNW at the surface is defined by the sharp temperature gradient that occurs where warm waters at the northern edge of the GS meet the cooler waters from the Slope Sea. A recent review of different metrics and their inter-relationship with respect
to the GS axis is given by Chi et al. (2019).

The meandering of the GS path is also linked with its separation near Cape Hat-68 teras $(75^{\circ}W, 35^{\circ}N)$. The separation of the GS from the coast at Hatteras is governed 69 by multiple factors such as inertial control (Fofonoff, 1954), basin-wide wind stress (Parsons, 70 1969; Veronis, 1973; Gill, 1982; Gangopadhyay et al., 1992; Dengg, 1996) and bathymet-71 ric control (Zhang & Vallis, 2007; Schoonover et al., 2017). The TSI (Taylor-Stephens 72 Index; see Data for details), an index of the GSNW (Taylor et al., 1998) has been shown 73 74 previously to correlate well with the separation point inter-annually (Taylor & Gangopadhyay, 2001). 75

Previous studies have focused on two distinctly separate but somewhat linked force-76 response mechanisms between the GS path and the overlying wind system. First, the 77 Parsons-Veronis hypothesis is built on the concept of separation by detachment. This 78 theory, within a two layer ocean model, implies that the GS detaches from the coast when 79 it reaches a latitude in which the boundary between the two layers extends to the sur-80 face, essentially at an outcropping of isopycnals (Parsons, 1969; Veronis, 1973; Huang 81 & Flierl, 1987). This hypothesis was tested by Gangopadhyay et al. (1992) (GCW92, here-82 after), who found evidence that the observed separation latitude of the GS was corre-83 lated with the predicted outcropping latitude of the two-layer model if one integrates the 84 wind-stress over the subtropical Atlantic basin (dominated by Azores High) for three years. 85 This three year time-period was attributed to the integrating effect of long-planetary Baro-86 clinic Rossby Waves (BRW) to cross the Atlantic and affect the western boundary (Gill, 87 1982). 88

Furthermore, the path of the GS after separation is dependent on the separation point itself. It is well known that the GS has a standing meander pattern between 75°W and 70°W (Cornillon, 1986; Lee & Cornillon, 1996; Tracey & Watts, 1986). Thus the latitude and angle of the GS at separation dictates the path of the GS at least up to 70°W; indicting that the choice of TSI as a metric of separation as well as a GSNW index (at least for the western half of the GS between 75 and 65°W) is reasonable.

A number of studies have proposed that the path of the GS is influenced by the 95 southward flow of Labrador Seawater (Rossby, 1999), dictated by the strength and lo-96 cation of one of the NAO's center of action, the Icelandic low-pressure center (Hameed 97 & Piontkovski, 2004; Sanchez-Franks et al., 2016). Sanchez-Franks et al. (2016) (SHW16 98 hereafter) created a regression prediction method of forecasting the GSNW position one-99 year ahead using Icelandic low center pressure and longitude paired with the Southern 100 Oscillation Index (SOI). SHW16 found that the forecasted GSNW values accounted for 101 36% of the variance and did not consider other mechanisms e.g. the latitude of separa-102 tion, that could influence the GS location. 103

The variability of the path and transport (of heat and mass) of the GS is also linked 104 to the variability of the Atlantic Meridional Overturning Circulation (AMOC). Under-105 standing the GS path variability, a component of the AMOC, might lead to better un-106 derstanding and prediction of the variability of the overall AMOC (Lozier, 2010; Cae-107 sar et al., 2021). A number of studies have recently suggested that the impacts of buoy-108 ancy and wind forcing on the AMOC transport are different over different time-scales; 109 wind-forcing dominating the seasonal, interannual and decadal variability while the buoy-110 ancy forcing dominates over the longer, centennial time-scales (Biastoch et al., 2008; Zhao 111 & Johns, 2014a, 2014b; Mielke et al., 2013). Using data (2004-2010) and model simu-112 lations, both Zhao and Johns (2014a, 2014b) and (Mielke et al., 2013) concluded that 113 although it is a relatively smaller constituent of the total AMOC transport, most of the 114 AMOC variability results from the Ekman transport component. 115

¹¹⁶ Mooring array programs at both 26°N (Smeed et al., 2016, RAPID) and 53°N (Lozier ¹¹⁷ et al., 2017, OSNAP) show that the variability of the Ekman transport is about ± 1.5 – ¹¹⁸ 2 Sv, while the amplitude and seasonal range is about 3–4 Sv. Thus, it makes a case ¹¹⁹ for understanding the variability of the Ekman transport which is restricted to the up-¹²⁰ per layer of the AMOC. In turn, in a simple 2-layer Parsons-Veronis model sense, this ¹²¹ Ekman drift is related to the separation and path of the Gulf Stream at the western bound-¹²² ary between 26°N and 41°N.

In summary, the wind-driven GS, resulting from integrated effects of basin-scale 123 wind gyres (Gangopadhyay et al., 1992, 2016) flowing around the two atmospheric Cen-124 ters of Action (i.e. the Icelandic Low and the Azores High) of the NAO, is sensitive to 125 both atmospheric pressure cells. A schematic in Figure 1 captures this synergistic force-126 response system of the GS path to both the components of the NAO via their respec-127 tive forcing parameters. The GS is situated at the boundary between the subtropical and 128 subpolar gyres. The variability of the GS path is thus partly due to (a) the basin-scale 129 wind-driven through long baroclinic Rossby waves (BRW) and the latitude of separa-130 tion as per GCW92 associated with the Azores High and (b) the buoyancy advection of 131 Labrador Current and Labrador Sea Water from the Labrador Sea region (Joyce et al., 132 2009), associated with the Icelandic Low as per SHW16. 133

In this paper for the first time we present a statistical model whose parameters rep-134 resent the effects of buoyancy and wind-forcing in a combined response system for pre-135 dicting the variability of the GS path using 40 (1980-2019) years of observed wind and 136 41 years (1980-2020) of GS index data. Specifically, we will be first exploring the hypoth-137 esis proposed by Parsons (1969) and Veronis (1973) and building upon the work done 138 by Gangopadhyay et al. (1992), reanalyzing the hypothesis over a longer time (40 years). 139 We then combine the Parsons-Veronis hypothesis (wind-forcing) with influences of the 140 Icelandic Low (bringing in the buoyancy-forcing by extending the previous work by SHW16) 141 to develop a new forecasting model for the path of the GS. 142

The organization of this paper is as follows. Section 2 outlines the different data 143 sets used in this study. Section 3 presents the validation of the Parsons-Veronis mech-144 anism of predicting the outcropping latitude for the 40-year period (1980-2019). A hi-145 erarchical forecast model development is presented in Section 4 starting from the SHW16 146 model and ending with a model that incorporates both the effects of integrated wind stress 147 over subtropical Atlantic and the longitudinal movement of the Icelandic Low. Additional 148 parameters such as the Southern Oscillation Index (SOI) and the Icelandic Low Pres-149 sure (ILP) amplitude are included in intermediate steps to test the sensitivity of the GS 150 response to extreme conditions of the El Niño Southern Oscillation (ENSO) and NAO 151 variability. Section 4 also discusses these sensitivities and Section 5 summarizes the re-152 sults with implications to the presently active AMOC. 153



Figure 1. This synergistic schematic shows the different aspects of atmospheric forcing and their influence on the Gulf Stream which are incorporated into the forecasting model. (a) The two components of the NAO (AH and IL) are presented with wind vector arrows while the dashed line on the right edge shows the typical latitudinal variation of the zonal wind stress, τ_x . (b) The surface circulation with the red arrows represent the GS and the North Atlantic Current; the blue arrows represent the Labrador current and other currents around Greenland. The small black arrows show the southward Ekman drift (T_E) under the Azores High. The dashed line shows the location of the Outcropping latitude (OCL) along which the vertical depth structure is depicted in the bottom panel. (c) The depth structure of the two-layer ocean model with the OCL marked on the western side is shown here. The geostrophic flow is marked by the red arrow and the interface between the two boundaries on the eastern side is marked by h_e . BRW represents the baroclinic Rossby waves. Image was generated using Inkscape (Inkscape Project, 2020) and MATLAB's mapping toolbox (The MathWorks, 2020).

154 **2 Data**

In this section, we briefly describe the different data sets used in this study: (i) the GS path and (ii) multiple parameters from the atmospheric system.

157 Gulf Stream Path

The Taylor-Stephens index (TSI) was calculated by applying principal components analysis to the time series of monthly latitudes of the north wall at [79, 75, 72, 70, 67, and 65°W], and found to be significantly linked to the North Atlantic Oscillation (NAO) (Taylor et al., 1998; Taylor & Gangopadhyay, 2001).

The TSI in addition to being used as a measurement of the GSNW is also used here 162 as an estimation of the GS separation latitude. We validated this by comparing the TSI 163 with the Atlantic Zone Mapping Program's (AZMP) (Fisheries and Oceans Canada, 2021) 164 GS location at 74° W and with the location of the 50cm contour line from AVISO sea 165 surface height fields at 74°W (Global Monitoring and Forecasting Center, 2021). Both 166 comparisons, AZMP and AVISO, showed high correlations with the TSI (r = 0.74 and 167 0.66 respectively for the period 1993 to 2016) as seen in Figure 2 justifying our usage 168 of TSI as a proxy for the separation latitude. 169



Figure 2. Validating the TSI with two different metrics of the GS separation latitude at 74°W. The Atlantic Zone Mapping Program (AZMP) uses sea surface temperature and the AVISO quantification uses the 50cm contour from sea surface height fields. The correlation between the AVISO separation and with the TSI and the AZMP with the TSI are r = 0.66 (red text in figure) and r = 0.74 (blue text in figure) respectively for the period 1993 to 2016.

170 Atmospheric Forcing Related Data

The wind stress data was obtained from JRA-55 yearly wind fields which are avail-171 able from 1958 to 2019 at a 1.25° grid (Japan Meteorological Agency, 2013). This is higher 172 resolution than the 2.5° wind used in GCW92. The JRA-55 wind data is available from 173 https://rda.ucar.edu/datasets/ds628.1/. The SOI data is available from https://climatedataguide 174 .ucar.edu/climate-data/southern-oscillation-indices-signal-noise-and-tahitidarwin-slp-soi 175 (Trenberth, 1984). The atmospheric centers of action indices (for Azores High and Ice-176 landic Low) are available from https://you.stonybrook.edu/coaindices/ (Hameed & Pi-177 178 ontkovski, 2004; Hameed & Riemer, 2012). The NAO winter index is available from https:// climatedataguide.ucar.edu/climate-data/hurrell-north-atlantic-oscillation-nao-index-station 179 -based (Hurrell et al., 2003). 180

Finally, the analysis time-period for the Parsons-Veronis model focusing on validating the linkage between the GS path and the Azores High winds (in an integrated sense) was the forty-year period (1980-2019). The forecasting model was fit over the 14-year period 1980-1993, and the one-year forecast comparisons were carried out over the next 27-year period (1994-2020). Extreme years for SOI, ILL and NAO were identified as those years when the parameters were beyond ± 0.8 standard deviation from their mean value over 1980-2019 period.

¹⁸⁸ 3 The Variability of the Gulf Stream Separation Latitude (1980-2019)

189

3.1 The Parsons-Veronis Model (Wind-forcing)

Following GCW92's methodology, we considered a two-layer ocean forced by steady wind stress with the bottom layer at rest. Using a balance between Ekman transport and the northward geostrophic flow, the outcropping latitude was predicted. The model was constructed using the equations from GCW92 with the final form being:

$$\frac{g'}{2f}h_w^2 = \frac{g'}{2f}h_e^2 - T_E$$
(1)

The term $\frac{g'}{2f}h_e^2$ represents the geostrophic transport and $g' = \frac{g(\rho_2 - \rho_1)}{\rho_2}$ is the reduced gravity of the 2-layer model with ρ_1 and ρ_2 being the densities of the upper and 194 195 lower layers and f being the Coriolis parameter. Depths of the interface between the two 196 layers at the eastern and western boundaries are represented by h_e and h_w respectively. 197 The outcropping latitude is obtained by setting $h_w = 0$, so that the isopycnal reaches 198 the surface at the western boundary. This eliminates the left hand side of Equation 1 199 and establishes a balance between the northward geostrophic flow and the Ekman trans-200 port. Ekman transport increases as one moves further North, so in order to maintain this 201 balance the GS has to detach from the coast and move eastward. In this way we can use 202 this equation to predict the separation latitude (as the outcropping latitude) of the GS. 203 The h_e and ρ values were based on the GCW92 work which designed a data-based two-204 layer system of the subtropical north Atlantic using CTD casts (conductivity, temper-205 ature, and depth) from the National Oceanographic Data Center database. Specifically, 206 $\rho_1 = 1026.4 \, kgm^{-3}$ and $\rho_2 = 1027.61 \, kgm^{-3}$, which yielded a $g' = 0.0115 \, ms^{-2}$. The 207 values of h_e were adapted from the CTD-based two-layer model presented by GCW92 208 and are interpolated to higher resolution grid for this study. The original values of h_e 209 were 375m, 300m, 230m and 125m at 31°N, 33°N, 37°N and 41°N respectively. 210

The Ekman Transport was computed by integrating the zonal wind stress (τ_x) from 20°W to 75°W, excluding regions over land. GCW92 used a constant 110 km per degree longitude and a constant f value, equivalent to f at 35°N, for all latitudes. This was updated here by allowing for both longitudinal distance variation over spherical earth and for f to vary with latitude. The Ekman transport T_E in Sv was then calculated us-

ing the equation

$$T_E = \frac{\int_{x_E}^{x_W} \tau_x dx}{\rho_1 f} \tag{2}$$

Where ρ_1 is the density of the surface layer (1026.4 kgm⁻³) and τ_x is integrated from 75°W (x_W) to 20°W (x_E).

Note that, Zhao and Johns (2014a, 2014b) set up a simple two layer model to un-213 derstand the seasonal and interannual variability of the AMOC and found credence to 214 the dominance of wind-driving in explaining its observed variability in both time-scales. 215 The present data-based model set up for validating the Parsons-Veronis hypothesis is 216 very similar to that of Zhao and Johns (2014a, 2014b) 2-layer numerical model set with 217 wind forcing. It is thus reasonable to test and validate the variability of the path of the 218 GS based on a simpler Parsons-Veronis hypothesis with a 2-layer model in the presence 219 of a robust and active AMOC. 220

Wind stress acting on a thermocline generates planetary waves that propagate to 221 the west (Anderson & Corry, 1985). Given that the time scale for planetary waves mov-222 ing across the North Atlantic (with speeds of ≈ 3.7 km day⁻¹) is on the order of 3-5 years 223 (Halliwell Jr & Cornillon, 1990; Gill, 1982), it is not expected that a significant corre-224 lation between prediction and observation will be obtained when the annual wind is used 225 to predict the outcropping latitude. A correlation was expected once this time integra-226 tion scale is accounted for as was the case in GCW92. For this reason, running averages 227 of three, four, and five years were conducted on T_E values which were then used to cal-228 culate the predicted outcropping latitude. For example, for a three-year running aver-229 age, an average of T_E values from 1991, 1992 and 1993 would be used to predict the out-230 cropping latitude for 1993 and be compared to the observed north wall position (TSI) 231 in 1993. 232

All reported p-values were calculated with an adjusted sample size to account for autocorrelation. This was done using the equation from Quenouille (1951) given below and following the methodology of Taylor (1995) and SHW16:

$$N' = N/(1 + 2r_1r_1' + 2r_2r_2' + \dots)$$
(3)

where N is the unadjusted number of points in each time series and r_1 and r'_1 are the lag one autocorrelations of the respective time series, and r_2 and r'_2 are the two year lag autocorrelations. While investigating the outcropping latitude, this calculation included terms up to r_4 , because the addition of higher-order autocorrelations had a negligible effect on the p-values.

238

3.2 Predicted Outcropping Latitude Versus Observed GSNW Index

The outcropping latitudes predicted on the basis of Parsons-Veronis hypothesis are 239 correlated with the GSNW position given by the TSI over the years 1980 to 2019 when 240 averaged over a three-year period. Figure 3 shows the comparisons between the predicted 241 outcropping latitude and the TSI for the years 1980-2019 with annual and three, four, 242 and five-year running averages. Similar to GCW92 results, the annual averages showed 243 insignificant correlation between the predicted outcropping latitude and observed sep-244 aration locations (TSI) (r = -0.04, p = 0.84). When a three-year running average was 245 applied to T_E , a strong correlation emerges for the year-to-year comparison between TSI 246 and Parsons-Veronis prediction, with r = 0.55 p = 0.012. The four- and five-year run-247 ning averages also show similar correlations with the observed TSI; however the corre-248 lation coefficients slightly decrease, and the p-values increase with increased averaging 249 period after 3 years, matching what was observed in GCW92. The three year integrated 250 wind-based predictions of the outcropping separation latitude from Equation 1 also showed 251 significant correlations with the AZMP and AVISO with r = 0.44 (p = 0.023) and r =252 0.44 p = 0.105) respectively. 253



Figure 3. Correlation (r) between predicted separation latitudes using JRA-55 winds averaged annually, and with 3, 4, and 5 year running averages against the observed GSNW (TSI). The 3-, 4-, and 5-year averaged correlations are significant.

This increased correlation with 3-year averaging is also shown in Figure 4(a-b). Figure 4a shows the annual average with an apparent lag between the outcropping latitude and the observed one. Figure 4b then shows the outcropping latitudes with 3-year averaging, closing this gap between outcropping and observed latitudes due to the delayed integrated effect of the generated planetary waves.

It is worth pointing out the connection between the 'lost fluid' in the upper layer of the original 2-layer Parsons-Veronis equations (see equation 9 of GCW92) and the uncertainties in AMOC transports. The AMOC has a mean flow around 18 Sv at 26°N and around 13 Sv at 41°N, in comparison the Ekman transport variations of around 2-4 Sv might seem insignificant (Mielke et al., 2013). As mentioned before, the majority of the interannual variability is driven by fluctuations in the wind stress (Frajka-Williams et al., 2019; Zhao & Johns, 2014b).

Using the latitudinal difference between the known separation latitude from AZMP and our predictions a yearly estimate of the loss of fluid in the two layer model was obtained with a mean of 0.8Sv and a range of 0.04–1.6Sv. These numbers match well with the 0.7-4.9 Sv found to be lost in the observed range of AMOC-Ekman transport between 26°N and 41°N (Mielke et al., 2013).



Figure 4. Comparison of TSI (red solid line) with Normalized predicted outcropping latitudes (black dashed line) based on (a) annual averaged winds and (b) three year running average winds from 1980 to 2019.

4 A Forecast Model for the Path of the Gulf Stream

4.1 Icelandic Low Model (Buoyancy Forcing)

272

The strength of the NAO directly influences the North Atlantic circulation (Walker 273 & Bliss, 1932; Hurrell et al., 2000, 2001). Many recent studies (Rossby, 1999; Rossby & 274 Benway, 2000; Drinkwater et al., 2003; Drinkwater, 2004; Hameed & Piontkovski, 2004, 275 SHW16) have focused their attention on the lag time scale between the advection from 276 the Labrador Sea and the latitudinal variation of the GS path. Mechanisms such as forc-277 ing by the Deep Western Boundary Current (Thompson & Jr, 1989; Spall, 1996) con-278 nected with the Labrador convection region and the movement of the Icelandic low (Hameed 279 & Piontkovski, 2004) have been suggested. 280

SHW16 developed a regression-based forecasting model incorporating the hypothesis of the Icelandic low forcing the Labrador Sea water into the Slope Sea from Hameed and Piontkovski (2004) and the influence of the Southern Oscillation Index (SOI) from Taylor et al. (1998). For a one-year forecasting model, SHW16 obtained the best regression equation for the 'i'th year prediction as follows,

$$GSNW_i = a GSNW_{i-1} + b ILP_{i-2} + c ILL_{i-3} + d SOI_{i-2} + e \quad \text{Model A}$$
(4)

where GSNW is the GS north wall position from the TSI, ILP and ILL are the aver-286 age Icelandic Low pressure and longitude from December through February respectively, 287 and SOI is the average SOI from September through February for the subscript year. 288 The multipliers a, b, c, and d are the regression coefficients, while e is the residual. We 289 were able to reproduce the results from SHW16 as well as extend the model prediction 290 through 2020 (Table 1 and 2 and Figure 5; for data sources, see Section 2).



One-year model forecasts from Model A and D compared to TSI. The r_f values Figure 5. in the figures represent correlations between the TSI and the one year predictions from both forecast models. Note that the time-axis spans the forecast period (1994-2020).

291

292

293

4.2 Combined Icelandic Low - Azores High Model (Buoyancy and Wind Forcing)

Motivated by the validation of the Parsons-Veronis mechanism for over the last forty 294 years as shown in Section 3, a new model that incorporates both the Icelandic Low and 295 the basin-wide, time-integrated wind-driven predicted outcropping latitude information 296 is proposed. This is the novelty of this work. It connects the two pressure cells of the 297 Atlantic wind system: (i) Icelandic Low Center longitude's east-west excursion with a 298 lag of multiple years, and (ii) Azores High component contributing through the basin-299 wide time-integrated Ekman wind drift as modeled by the Parsons-Veronis hypothesis. 300 A series of experiments were carried out with different combinations of the longitudinal 301 variation of the Icelandic Low, basin-wide wind stress integrated over 2-3 years and the 302 SOI. We present the results in Table 1 and Table 2 and discuss them below. 303

While the three-year integration timescale works well for validating the Parsons-304 Veronis mechanism, a forecast model for year 'i' does not have the wind information for 305

the forecast year. Given the need for one year in advance prediction without knowing next year's winds, predicted outcropping latitudes based on two years of wind-integration were used with a one-year lag. The addition of the two-year integrated wind-derived outcropping latitude (*OCL2*) into Model A created a new model, Model B which can be given as follows

$$GSNW_{i} = a GSNW_{i-1} + b OCL2_{i-1} + c ILP_{i-2} + d ILL_{i-3} + e SOI_{i-2} + f \qquad \text{Model B}$$
(5)

Following the methodology from SHW16, the model fit was assessed by making con-311 tinual one-year predictions for 1994 through 2020 and then comparing the correlation 312 and mean absolute error (MAE) between forecast locations and the observed GSNW po-313 sitions. Following SHW16, $MAE = \frac{1}{n} \sum_{i=1}^{n} |f_i - y_i|$ where f_i is the model's predic-314 tion and y_i is the observed GSNW position (TSI for the i-th year). Both f_i and y_i time-315 series were standardized to compute the MAE. For each one-year prediction the model 316 was fit from 1980 through one year prior to the prediction year. For example, the years 317 1980-1993 were used to fit the model and forecast for 1994. Similarly, the years from 1980-318 1994 were used to fit the model and forecast for 1995. This process was continued for 319 all one-year predictions from 1994 to 2020. The model is evaluated by calculating the 320 correlation between its predictions with observations. To avoid confusion with other r 321 values used in this paper, this correlation coefficient between model predictions and ob-322 servations will be called the 'forecast correlation' r_f from here on. Years 1980-1993 were 323 not predicted as the model would not have enough data to robustly fit all variables (see 324 SHW16) for one-year advance prediction for those years. Table 1 presents the resulting 325 r_f values and their corresponding p-values. The sample size was adjusted with autocor-326 relations up to four years in equation (3) with the addition of further lagged autocor-327 relations having a negligible effect on the p-values. 328

Table 1. Standardized beta coefficients of model variables for Models A, B, C, and D fit from 1980-2020. Coefficient values with asterisk indicate significance at 95% level. The r_f is the correlation coefficient between one year model predictions and the TSI; the corresponding p-value is listed in the last column.

Model	$GSNW_{i-1}$	$OCL2_{i-1}$	ILP_{i-2}	ILL_{i-3}	SOI_{i-2}	r_{f}	p-value
A	0.42^{*}	NA	-0.10	-0.24^{*}	0.04	0.52	0.029
В	0.33^{*}	0.31^{*}	-0.04	-0.17^{*}	0.04	0.65	0.007
\mathbf{C}	NA	0.36^{*}	-0.12	-0.11	0.04	0.61	0.007
D	0.33^{*}	0.32^{*}	NA	-0.16^{*}	NA	0.65	0.016

The one-year model prediction for Model B using the integrated outcropping latitude shows a strong correlation with TSI with an $r_f = 0.65$ and MAE = 0.54 over the forecast period (1994-2020). In comparison Model A has a $r_f = 0.52$ and MAE = 0.64. The correlation is increased and the MAE is decreased with the addition of the windintegrated prediction of outcropping latitude.

To compare the relative contribution of each predictor variable to the outcome variable (GSNW) in the forecasting model, standardized beta coefficients are used. Beta coefficients show the degree of change in the outcome variable given one unit change of the predictor variable. So, beta coefficients with larger absolute values indicate larger influences on the outcome variable. Given that all our variables are normalized before

Table 2. Model fit parameters with r_f being the correlation between the one-year predictions and observed TSI from 1994-2020, MAE being the mean absolute error of one year predictions, RV being the residual variance between predictions and TSI, AICc being the Akaike information criterion adjusted for small sample sizes for each model fit to the whole time series.

Model	r_{f}	MAE	RV	AICc
А	0.52	0.64	0.70	68.3
В	0.65	0.54	0.53	59.3
\mathbf{C}	0.61	0.53	0.54	63.1
D	0.65	0.50	0.40	57.0

going in to the model these are standardized beta coefficients with units of standard deviations. The final model can thus be selected using the beta coefficients from the different individual model experiments.

Both the $GSNW_{i-1}$ and $OCL2_{i-1}$ explain roughly the same amount of variance in Model B with beta coefficients of 0.33 and 0.31 respectively (Table 1). When the $GSNW_{i-1}$ variable was removed from Model B, creating Model C, the r_f value dropped to 0.61.

$$GSNW_i = a GSNW_{i-1} + b OCL2_{i-1} + c ILL_{i-3} + d SOI_{i-2} + e$$
 Model C (6)

When both $GSNW_{i-1}$ and $OCL2_{i-1}$ were removed from Model B, the correlation between one year predictions and observed locations dropped to $r_f = 0.42$, showing the large contribution of the wind-integrated outcropping latitude in the model.

The Icelandic low pressure and *SOI* explain relatively less variance compared to other variables and are not significant in Model A or B. For this reason we built a new model with only the significant contributors, which is,

$$GSNW_i = a GSNW_{i-1} + b OCL2_{i-1} + c ILL_{i-3} + d$$
 Model D (7)

This model resulted in an r_f value of 0.65 for the whole forecast period of 1994-351 2020 (Figure 5). The reason that ILP and SOI were found to be significant in the SHW16 352 paper but not in any of the models in our study, is because of the difference in the time 353 periods used to fit the model. SHW16 used data beginning in 1966 whereas we use data 354 beginning in 1980 to fit the models. We restricted our analysis to the 40-year period af-355 ter 1980 for two reasons. First, it is well known that there were relatively poor spatial 356 coverage of the atmospheric data in the years before satellite observations started in 1979. 357 This led to the poorer quality of wind products (due to coarser resolution of available 358 data and spatial-temporal gaps), which have been well recognized by many studies re-359 cently (Kistler et al., 2001; Sturaro, 2003; Huesmann & Hitchman, 2003). Second, prior 360 to the 1970s the data used to calculate the GS indices was much more scarce, leading 361 to potentially less accurate estimates of the GS north wall location (McCarthy et al., 2018). 362 Furthermore, while testing the models for the period used in SHW16 paper we found that 363 even though the ILP and SOI are significant in Models A-C; Model D still performed 364 best with a $r_f = 0.66$, compared to a $r_f = 0.57$ for Model A. The fidelity of Model D 365 is attributed to the inclusion of both buoyancy forcing (ILL) and wind driving (OCL) 366 effects to forecast the GS path. 367

In addition to evaluating the forecast correlation, two other tests were carried out to assess model fit, residual variance and AICc (see Table 2). Residual variance is the sum of squares of the difference between the observation and the model predicted value (Weisberg, 2005). Model D showed a drop in residual variance compared to Model A, both when comparing the one year predictions to the observed TSI (0.40 and 0.70 respectively) and when comparing the model when fit with all available years to the TSI (0.27 and 0.34 respectively).

Since there were a varying degree of parameters in different models (A-D), we used 375 376 the Akaike information criterion (AIC) to test model fit. AIC is an estimate of model prediction error taking into account both the goodness of fit and the simplicity of the 377 model. AIC accounts for the amount of information lost while penalizing for the addi-378 tion of parameters to account for over-fitting. In this study, we used AICc, which adds 379 a modified correction for smaller sample sizes (Hurvich & Tsai, 1989). The smaller the 380 AICc, the better the model fit. Model D yields an AICc of 57.0 (least among all four mod-381 els) whereas Model A had an AICc of 68.31. 382

383

4.3 Forecast Model Sensitivity to Extreme Events

Observational studies have shown that the GS has experienced climate-scale changes 384 in its path variability and instability processes (Andres, 2016; Gangopadhyay et al., 2019; 385 Silver et al., 2021; Caesar et al., 2021), over the past forty years. These changes include 386 long-term shifts of the path, regime-shift of annual ring formations and the westward move-387 ment of the destabilization point of the GS. Looking ahead, one of the projected impacts 388 of the current rate of global warming is possible future increases in the frequency and 389 amplitude of extreme events (e.g. hurricanes), which are related to atmospheric indices 390 such as the SOI and NAO (Brickman et al., 2018; Wang et al., 2020). The elements of 391 forecast models presented herein (Models A-D) allow us the opportunity to test the sen-392 sitivity of the GS forecasts to such extreme atmospheric conditions. We thus repeated 393 the forecast correlation exercise on a number of subsets of previously identified extreme 394 SOI and NAO years during the forecasting period of 1994-2020. Results and interpre-395 tations from this sensitivity experiments are presented next. 396

Table 3. Extreme years (outside ± 0.8 standard deviation from the mean) for different atmospheric indices used in the sensitivity testing. Also see Figure 6.

NAO	SOI	ILL
1994	1994	1994
1995	1997	1995
1996	1998	1996
2000	1999	1998
2001	2000	1999
2006	2004	2003
2007	2007	2005
2010	2008	2006
2011	2009	2011
2012	2010	2014
2013	2011	2015
2014	2015	2017
2015	_	_

Model sensitivity to predicting the GSNW for years of different atmospheric extreme events was tested by selecting one year predictions from respective years of extreme

SOI in one subset of extreme events and of NAO in the other subset. We chose NAO ex-399 treme years as it is a more recognized index than either ILL or ILP or its Azores High 400 components. The NAO winter index has a positive correlation of 0.49 with ILL and a 401 negative correlation of 0.78 with ILP. In our models, the impact of buoyancy forcing comes from the ILP/ILL variables and that of the wind-forcing comes from the OCL factor, 403 which is the integrated wind-stress over the basin and over time. The selected set of ex-404 treme years (chosen as those falling outside ± 0.8 standard deviations) are shown in Fig-405 ure 6 and are listed in Table 3. The cut off of 0.8 standard deviations was used to al-406 low for a large enough sample size for analysis. All indices were normalized with respect 407 to the mean over the 1980-2019 period before extreme years where selected. This resulted 408 in 12 SOI years, 13 NAO years, and 12 ILL years (Table 3). 409

For the extreme SOI year subset, one year predictions showed the strongest correlation for Model D with $r_f = 0.83$. Models A, B, C showed values of r_f as 0.50, 0.70, and 0.62 respectively. Model A, the only model without OCL, had the lowest r_f value, which might indicate that OCL is an important predictor for extreme SOI years.

For the extreme NAO year subset, Model C had the highest r_f value with $r_f =$ 0.62. Model B had the second highest with $r_f = 0.57$. Model D had similar correlation as Model B ($r_f = 0.54$). Models B and C are the only two models that include OCL, ILP, and ILL indicating that all three variables associated with the NAO might play an important role in predicting extreme NAO years. Interestingly, all of the models outperformed the extreme NAO subsets when compared against the extreme ILL years (third row of Table 4).

The fact that Model D still preformed well when predicting the GS path for ex-421 treme NAO, SOI, and ILL years (r_f from 0.54-0.83) highlights the robustness of the model. 422 However, the model could be further improved for predicting the extreme excursions of 423 the GS by including other important forcings. A challenge for the future is accurately 424 predicting extreme events of different types such as extreme conditions of NAO and SOI, 425 more frequent ring formation, marine heatwaves, more frequent and stronger atmospheric 426 storms. Extreme events may lead to disruption of ecosystems and multiple extreme events 427 may affect the long term structure of an ecosystem (Gupta et al., 2020). This is an area 428 that is worthy of concentrated research in the future. 429

In addition to testing the models' ability to predict the GSNW during extreme events, 430 the models' sensitivity to forecasting from an extreme event was also tested. This was 431 done to understand the lasting impact of both buoyancy and wind forcing after an ex-432 treme event year. Considering the same extreme event years described above, correla-433 tions between the model forecast and TSI were computed for 2 years after an extreme 434 SOI year because the models (A, B and C) incorporated a 2-year lagged SOI variable. 435 Model A had the lowest correlation ($r_f = 0.22$) with models B, C, and D showing bet-436 ter forecasting performance ($r_f = 0.51, 0.49, 0.47$ respectively). In contrast, for 2 and 437 3 years after extreme NAO events (some of the models incorporated 2-year lagged ILP 438 and 3-year lagged ILL) there was less difference in forecast correlations between mod-439 els. Two years after an extreme NAO, Models A, B, C, and D had r_f values of 0.56, 0.55, 440 0.52 and 0.53, respectively; whereas three years after an extreme NAO year, the values 441 of r_f were 0.52, 0.59, 0.53, and 0.72, respectively. Table 4 summarizes the forecast cor-442 relation for all these cases. Again, for the 3-year lagged extreme ILL years, all of the mod-443 els except model A, outperformed the other extreme NAO and SOI subsets (bottom row 444 of Table 4). 445

Figure 7 shows the τ_x fields for the years with the pressure center being furthest west and furthest east. When the ILL is farthest west, as shown in Figure 7(a), the τ_x anomaly over the Labrador region is negative. This negative τ_x anomaly reduces the southward Ekman drift in the region and results in reduced amount of cold Labrador surface water entering the Slope Sea. This allows for a northward shift of the GSNW in later



Figure 6. Time series of atmospheric indices SOI, NAO, with extreme years (outside ± 0.8 standard deviation) highlighted with vertical stripes and shown with shaded dark red or dark blue regions. All indices are normalized. The SOI is averaged over September through February and NAO is averaged over December through February. The TSI is the annual Taylor-Stephens Index, the OCL is the three year integrated predicted outcropping latitude, and Model D is the one year forecast from the final model.

years. SHW16 found that when the ILL was anomalously west, the sea surface temper ature over the Labrador Sea and east and south of Greenland was reduced resulting in

Table 4. Sensitivity testing results for years concurrent and following to the extreme events of different atmospheric forcing. The top half of the table with row labels NAO, SOI and ILL, shows the correlation coefficient between model forecasts and the TSI for *concurrent* extreme years listed in Table 3. The bottom half of the table with row labels NAO₂, NAO₃, SOI₂, and ILL₃ shows the correlation coefficients between model forecasts and the TSI for years either 2 or 3 years *following* an extreme event indicated by the subscript number.

Index	Model A	Model B	Model C	Model D
	Forecast of	of Extreme	Event Years	s
NAO	0.43	0.57	0.62	0.54
SOI	0.50	0.70	0.62	0.83
ILL	0.71	0.84	0.82	0.79
Fe	orecast Follo	owing Extre	eme Event Y	lears
NAO ₂	0.56	0.55	0.52	0.53
NAO_3	0.52	0.59	0.53	0.72
SOI_2	0.22	0.51	0.49	0.47
ILL_3	0.48	0.66	0.56	0.65

enhanced deep water convection, decreased amounts of cold water entering the Slope Sea, and a northward shift in the GSNW. In contrast, when the ILL is to the east as shown in Figure 7(b), a positive τ_x anomaly appears in this region, increasing southward advection of Labrador water into the Slope Sea and less deep water convection resulting in a more southward GSNW.

This process is also evident in Figure 8(a), which shows the integrated T_E for the 3 years following each extreme ILL event. For years after an extreme westward (eastward) ILL the integrated T_E is weaker (stronger) resulting in the intersection with T_g occurring at a higher (lower) latitude. This confirms the workings of the Parsons-Veronis hypothesis as presented earlier (Section 3.1) for the years following extreme ILL years as well. This also validates the best performance of Model D, which captures both of the effects of buoyancy and wind forcing within a single framework.

The relationship between the SOI and GSNW is less understood and needs further investigation. Figure 8(b) shows a negative relationship between SOI and OCL for years selected after two years of an extreme SOI event. For years with a low (high) SOI the integrated T_E is weaker (stronger) and the OCL is further north (south). This matches with the Parsons-Veronis idea again as discussed for ILL. However, how exactly the SOI influences the subtropical winds is beyond the scope of this study.

We note in passing that the SOI beta coefficient in all models fitted from 1980 to 471 2020 was very slightly positive. This is in contradiction to the consistent negative beta 472 coefficients found by SHW16 while analyzing the period from 1966 to 2014. The result 473 presented in Figure 8(b) was for years mostly before 2014, with 2017 (from the 2015 ex-474 treme) being the only years after 2014 (see Table 3) and matches with the negative cor-475 relation idea. The changeover of beta coefficients from negative to slightly positive could 476 be in part due to observed changes in the SOI variation in recent years. Power and Smith 477 (2007) found that the mean state of the SOI has decreased in recent years due to climate 478 change. Additionally Wang et al. (2020) projected that the number of concurrent extreme 479 warm and convective El Nino events will increase under greenhouse warming. 480



Figure 7. Example of zonal wind stress (τ_x) anomaly for extreme years of ILL with (a) showing the westernmost center for the ILL in 2010, (b) showing easternmost ILL for 1983. (c) shows the mean τ_x field from 1980-2019.

481 5 Summary and Conclusion

To summarize, we presented a new model (Model D) for forecasting the GS path which includes: (i) the GSNW index from the previous year, (ii) gyre-scale integrated Ekman Drift over past two years, and (iii) the longitude of Icelandic Low center lagged by three years. The forecast correlation over the 27-year period (1994-2020) was 0.65, which is a reasonable improvement from the previous model's (Model A) correlation value of 0.52. This improvement was attributed to the addition of the effect of time-integrated basin-scale wind drift to allow for the baroclinic Rossby waves to cross the Atlantic to



Figure 8. Impact of extreme events on GS path forecasting. The meridional distributions of the total Ekman transport (T_E) integrated zonally for 3 years following each occurrence of an extreme ILL to the east (red) or west (blue) are shown in (a). Similar to (a) but for two years after an extreme SOI high (red) or low (blue) is shown in (b). Dotted lines show individual years whereas solid lines show the mean. The black line represent the T_g line whose intersection points with T_E represents the OCL. Both T_E and T_g are in Sverdrups. (The predicted OCL being further north than the observed separation point is due to the loss of fluid not accounted for in the model discussed at the end of section 3.2).

489 490	affect the separation of the GS. This also highlights the importance of both North At- lantic pressure cells, Icelandic Low and Azores High in dictating the path of the GS.
491	The major results from this study can be detailed as follows:
492	• The observed separation of the GS path is significantly correlated $(r=0.55)$ with
493	the basin-wide Ekman drift over the subtropical Atlantic integrated over three years
494	for over forty years.
495	• The integrated wind effect was incorporated as an outcropping latitude for the sep-
496	aration point of the GS to improve the forecasting model created earlier in SHW16.
497	• The model yielding the best results was Model D using the $GSNW_{i-1}$, $OCL2_{i-1}$,
498	and ILL_{i-3} with a forecast correlation of 0.65.
499	SHW16's model was able to predict the TSI with a correlation coefficient of $r_f =$
500	0.52. We believe that part of this model's success was due to the $GSNW_{i-1}$ variable in-
501	corporating the influence of the integrated outcropping latitude into the model (see Ta-
502	ble 1). When both $GSNW_{i-1}$ and OCL_{i-1} are removed the accuracy of the model drops

⁵⁰³ substantially, showing the large role that wind stress is playing on the separation loca-

tion. The model with the most explained variance for the TSI prediction used only $GSNW_{i-1}$, OCL2_{i-1}, and ILL_{i-3} , with a $r_f = 0.65$.

Using both the Azores high and the Icelandic Low parameters in Model D has sub-506 stantially improved the explained variance to 50% from 36% (with just Icelandic Low 507 as in Model A) for the variability of the GS path between 75 and 65W. Extreme years 508 of SOI or NAO were similarly predictable (Models B and C), which indicate that Model 509 D is able to capture most of the forcing influences from the wind gyres in the North At-510 lantic and their connection to the equatorial Pacific. However, there is a substantial amount 511 512 of unexplained variance (40-45%) which requires future investigation. Some of the factors that may influence the path of the Stream and can be explored in the future are: 513 (i) wind stress curl integrated over basin and time; (ii) position of the zero and the max-514 imum of the wind stress curl in the subtropical north Atlantic; (iii) strength, intermit-515 tency and spatial variability of the DWBC linked with ice melting and convection in the 516 Labrador region; (iv) atmospheric forcing strengthening recirculation gyres to the north 517 and south of the Stream. The results presented here open up new research pathways which 518 could utilize long-term data sets now available and advanced numerical models to test 519 similar hypotheses. 520

Furthermore, the four different models allowed us to carry out a sensitivity study to understand the impacts of extreme events (represented by SOI and NAO indices) on forecasting the GS path. Based on the analysis of a selected subset of years strategically following extreme events during the period 1994-2019, our recommendation is to use Model B (with OCL, SOI and ILP and ILL indices) in addition to Model D (with OCL and ILL only) and reevaluate the forecast correlations and adapt in the coming 5-10 years.

Finally, the implication of this simple study to understand climatic variability of 527 the AMOC needs further attention. As presented here, the Parsons-Veronis two-layer 528 idea of Ekman wind drift affecting the GS path is working for four decades in the back-529 ground of an active AMOC. Given that most of the AMOC variability is in fact dom-530 inated by this Ekman Drift (Lozier, 2012; Mielke et al., 2013; Caesar et al., 2021; Frajka-531 Williams et al., 2019), it is possible that one could use this simpler variability predic-532 tion model within the context of a time-varying AMOC predictability scheme when more 533 observations for AMOC would be available. 534

535 Acknowledgments

We are grateful for financial supports from NSF (OCE-1851242), SMAST and UMass 536 Dartmouth. GG was supported by NSF under grants OCE-1657853 and OCE-1558521. 537 We gratefully acknowledge the efforts of UCAR, Stoney Brook, and the Japan Meteo-538 rological Agency for generating the data that made this paper possible. All data is freely 539 available, and sources are listed in the Data section of the paper. Our thanks to Andre 540 Schmidt for helping with the Matlab and system software while working remotely dur-541 ing COVID-19 for completion of this work and the analysis of multiple years of data. Mul-542 tiple discussions with Sultan Hameed on Gulf Stream and NAO, and with Chris Wolfe 543 of Stony Brook on winds are appreciated. 544

The Taylor-Stephens index (TSI) data can be accessed at http://www.pml-gulfstream 545 .org.uk/. The AZMP data is available from https://www.dfo-mpo.gc.ca/science/data 546 -donnees/azmp-pmza/index-eng.html. The AVISO SSH data is available from https:// 547 marine.copernicus.eu/. The JRA-55 wind data is available from https://rda.ucar.edu/ 548 datasets/ds628.1/. The SOI data is available from https://climatedataguide.ucar.edu/ 549 climate-data/southern-oscillation-indices-signal-noise-and-tahitidarwin-slp-soi (Trenberth, 550 1984). The atmospheric centers of action indices (for Azores High and Icelandic Low) 551 are available from https://you.stonybrook.edu/coaindices/ (Hameed & Piontkovski, 2004; 552 Hameed & Riemer, 2012). The NAO winter index is available from https://climatedataguide 553

- .ucar.edu/climate-data/hurrell-north-atlantic-oscillation-nao-index-station-based (Hurrell
 et al., 2003).
- The authors would like to dedicate this manuscript to the fond memories of many discussions with Professor Geroge Veronis (1926-2019).

558 References

564

565

566

578

579

580

581

582

587

588

589

595

596

597

605

- Anderson, D., & Corry, R. (1985). Ocean response to low frequency wind forcing
 with application to the seasonal variation in the Florida Straits—Gulf Stream
 transport. Progress in Oceanography, 14, 7–40.
- Andres, M. (2016). On the recent destabilization of the Gulf Stream path downstream of Cape Hatteras. *Geophysical Research Letters*, 43(18), 9836–9842.
 - Biastoch, A., Böning, C. W., & Lutjeharms, J. (2008). Agulhas leakage dynamics affects decadal variability in Atlantic Overturning Circulation. Nature, 456(7221), 489–492.
- Brickman, D., Hebert, D., & Wang, Z. (2018). Mechanism for the recent ocean
 warming events on the Scotian Shelf of eastern Canada. Continental Shelf Research, 156, 11–22.
- ⁵⁷⁰ Caesar, L., McCarthy, G., Thornalley, D., Cahill, N., & Rahmstorf, S. (2021). Current Atlantic Meridional Overturning Circulation weakest in last millennium.
 ⁵⁷² Nature Geoscience, 1–3.
- ⁵⁷³ Caesar, L., Rahmstorf, S., Robinson, A., Feulner, G., & Saba, V. (2018). Observed
 ⁵⁷⁴ fingerprint of a weakening Atlantic ocean overturning circulation. Nature,
 ⁵⁷⁵ 556 (7700), 191–196.
- ⁵⁷⁶ Chi, L., Wolfe, C. L., & Hameed, S. (2019). The distinction between the Gulf ⁵⁷⁷ Stream and its north wall. *Geophysical Research Letters*, 46(15), 8943–8951.
 - Cornillon, P. (1986). The effect of the New England Seamounts on Gulf Stream meandering as observed from satellite ir imagery. *Journal of Physical Oceanography*, 16(2), 386–389.
 - Dengg, J. (1996). The Gulf Stream separation problem. The Warmwatersphere of the North Atlantic Ocean, 254–290.
- Drinkwater, K. F. (2004). Atmospheric and sea-ice conditions in the northwest
 Atlantic during the decade, 1991–2000. Journal of Northwest Atlantic Fishery
 Science, 34.
- Drinkwater, K. F., Belgrano, A., Borja, A., Conversi, A., Edwards, M., Greene,
 - C. H., ... Walker, H. (2003). The response of marine ecosystems to climate variability associated with the North Atlantic Oscillation. *Geophysical Monograph-American Geophysical Union*, 134, 211–234.
- Fisheries and Oceans Canada. (2021). Atlantic Zone Monitoring Program website.
 (Retrieved 5 January 2021 from Fisheries and Oceans Canada.)
- Fofonoff, N. (1954). Steady flow in a frictionless homogeneous ocean. J. mar. Res, 13, 254–262.
- ⁵⁹⁴ Frajka-Williams, E., Ansorge, I. J., Baehr, J., Bryden, H. L., Chidichimo, M. P.,
 - Cunningham, S. A., ... others (2019). Atlantic Meridional Overturning Circulation: Observed transport and variability. *Frontiers in Marine Science*, 6, 260.
- Gangopadhyay, A., Chaudhuri, A. H., & Taylor, A. H. (2016). On the nature of
 temporal variability of the Gulf Stream path from 75° to 55° w. Earth Interac *tions*, 20(9), 1–17.
- Gangopadhyay, A., Cornillon, P., & Watts, D. R. (1992). A test of the Parsons–
 Veronis hypothesis on the separation of the Gulf Stream. Journal of Physical
 Oceanography, 22(11), 1286–1301.
- Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., Monim, M., & Clark, J.
 - (2019). An observed regime shift in the formation of warm core rings from

606	the Gulf Stream. Scientific reports, $9(1)$, 1–9.
607	Gawarkiewicz, G., Chen, K., Forsyth, J., Bahr, F., Mercer, A. M., Ellertson, A.,
608	Han, L. (2019). Characteristics of an advective marine heatwave in the Middle
609	Atlantic Bight in early 2017. Frontiers in Marine Science, 6, 712.
610	Gawarkiewicz, G., Todd, R. E., Plueddemann, A. J., Andres, M., & Manning, J. P.
611	(2012). Direct interaction between the Gulf Stream and the shelfbreak south of
612	New England. Scientific reports, $2(1)$, 1–6.
613	Gawarkiewicz, G., Todd, R. E., Zhang, W., Partida, J., Gangopadhyay, A., Monim,
614	MUH., Dent, M. (2018). The changing nature of shelf-break exchange
615	revealed by the OOI Pioneer Array. Oceanography, 31(1), 60–70.
616	Gill, A. E. (1982). Atmosphere-ocean dynamics. Int. Geophys. Ser., 30, 662p.
617	Global Monitoring and Forecasting Center. (2021). Global ocean gridded 14 sea sur-
618	face heights and derived variables nrt product, E.U. Copernicus Marine Service
619	Information. ((Accessed: 5th January 2021))
620	Gupta, A. S., Thomsen, M., Benthuysen, J. A., Hobday, A. J., Oliver, E., Alexander,
621	L. V., others (2020). Drivers and impacts of the most extreme marine
622	heatwave events. Scientific reports, $10(1)$, 1–15.
623	Halliwell Jr, G. R., & Cornillon, P. (1990). Large-scale sst variability in the west-
624	ern North Atlantic Subtropical Convergence Zone during FASINEX. Part II:
625	Upper ocean heat balance and frontogenesis. Journal of physical oceanography,
626	20(2), 223-234.
627	Hameed, S., & Piontkovski, S. (2004). The dominant influence of the Icelandic
628	Low on the position of the Gulf Stream northwall. <i>Geophysical research letters</i> ,
629	31(9).
630	Hameed, S., & Riemer, N. (2012). Relationship of sahel precipitation and atmo-
631	spheric centers of action. Advances in Meteorology, 2012.
632	Huang, R., & Flierl, G. (1987). Two-layer models for the thermocline and cur-
633	rent structure in subtropical/subpolar gyres. Journal of physical oceanography,
634	17(7), 872-884.
635	Huesmann, A. S., & Hitchman, M. H. (2003). The 1978 shift in the NCEP reanalysis
636	stratospheric quasi-biennial oscillation. Geophysical research letters, $30(2)$.
637	Hurrell, J. W., Brown, S. J., Trenberth, K. E., & Christy, J. R. (2000). Comparison
638	of tropospheric temperatures from radiosondes and satellites: 1979–98. Bulletin
639	of the American Meteorological Society, 81(9), 2165–2178.
640	Hurrell, J. W., Kushnir, Y., Ottersen, G., & Visbeck, M. (2003). An overview of
641	the North Atlantic Oscillation. Geophysical Monograph-American Geophysical
642	Union, 134, 1–36.
643	Hurrell, J. W., Kushnir, Y., & Visbeck, M. (2001). The North Atlantic Oscillation.
644	Science, 291 (5504), 603–605.
645	Hurvich, C. M., & Tsai, CL. (1989). Regression and time series model selection in
646	small samples. Biometrika, $76(2)$, 297–307.
647	Inkscape Project. (2020). Inkscape 1.0.1. Retrieved from https://inkscape.org
648	Japan Meteorological Agency. (2013). Jra-55: Japanese 55-year reanalysis, monthly
649	means and variances. research data archive at the national center for atmo-
650	spheric research jra-55: Japanese 55-year reanalysis, monthly means and vari-
651	ances research data archive at the national center for atmospheric research.
652	Retrieved 02 Aug, 2019, from https://doi.org/10.5065/D60G3H5B
653	Joyce, T. M., Kwon, YO., & Yu, L. (2009). On the relationship between synoptic
654	wintertime atmospheric variability and path shifts in the Gulf Stream and the
655	Kuroshio extension. Journal of Climate, 22(12), 3177–3192.
656	Kistler, R., Kalnay, E., Collins, W., Saha, S., White, G., Woollen, J., others
657	(2001). The NCEP–NCAR 50-year reanalysis: monthly means cd-rom and doc-
658	umentation. Bulletin of the American Meteorological society, 82(2), 247–268.
659	Lee, T., & Cornillon, P. (1996). Propagation and growth of Gulf Stream meanders
660	between 75 and 45 w. Journal of physical oceanography, $26(2)$, $225-241$.

661	Lozier, M. S. (2010). Deconstructing the conveyor belt. <i>science</i> , 328 (5985), 1507–
662	1511.
663	Lozier, M. S. (2012). Overturning in the North Atlantic. Annual review of marine
664	science, 4, 291–315.
665	Lozier, M. S., Bacon, S., Bower, A. S., Cunningham, S. A., De Jong, M. F.,
666	De Steur, L., others (2017). Overturning in the subpolar North At-
667	lantic program: A new international ocean observing system. Bulletin of the
668	American Meteorological Society, $98(4)$, $737-752$.
669	McCarthy, G. D., Joyce, T. M., & Josey, S. A. (2018). Gulf Stream variability
670	in the context of quasi-decadal and multidecadal Atlantic climate variability.
671	Geophysical Research Letters, $45(20)$, 11–257.
672	Mielke, C., Frajka-Williams, E., & Baehr, J. (2013). Observed and simulated vari-
673	ability of the AMOC at 26 n and 41 n. Geophysical Research Letters, $40(6)$,
674	1159 - 1164.
675	Mills, K. E., Pershing, A. J., Brown, C. J., Chen, Y., Chiang, FS., Holland, D. S.,
676	others (2013). Fisheries management in a changing climate: lessons from
677	the 2012 ocean heat wave in the northwest Atlantic. $Oceanography, 26(2),$
678	191–195.
679	Nye, J. A., Joyce, T. M., Kwon, YO., & Link, J. S. (2011). Silver hake tracks
680	changes in northwest Atlantic circulation. Nature communications, $2(1)$, 1–6.
681	Parsons, A. (1969). A two-layer model of Gulf Stream separation. Journal of Fluid
682	Mechanics, 39(3), 511–528.
683	Pershing, A. J., Alexander, M. A., Hernandez, C. M., Kerr, L. A., Le Bris, A., Mills,
684	K. E., others (2015). Slow adaptation in the face of rapid warming leads to
685	collapse of the Gulf of Maine cod fishery. Science, $350(6262)$, $809-812$.
686	Power, S. B., & Smith, I. N. (2007). Weakening of the walker circulation and ap-
687	parent dominance of El Niño both reach record levels, but has ENSO really
688	changed? Geophysical Research Letters, 34 (18).
689	
689 690	Quenouille, M. (1951). The variate-difference method in theory and practice. Revue
690	Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129.
690 691	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies
690 691 692	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164.
690 691 692 693	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream
690 691 692 693 694	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120.
690 691 692 693 694 695	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a
690 691 692 693 694 695 696	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanog-
690 691 692 693 694 695 696 697	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826.
690 691 692 693 694 695 696 697 698	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitiv-
690 691 692 693 694 695 696 697 698 699	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2),
690 691 692 693 694 695 695 696 697 698 699 700	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373.
690 691 692 693 694 695 695 696 697 698 699 700 701	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021).
690 691 692 693 694 695 696 697 698 699 700 701 701	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from
690 691 692 693 694 695 696 697 698 699 700 701 702 703	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7.
690 691 692 693 694 695 696 697 698 699 700 701 702 703 703	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., &
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 706 707	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council.
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary cur-
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 709	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary current crossover. Part II: Low-frequency internal oscillations. Journal of Physical
690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary current crossover. Part II: Low-frequency internal oscillations. Journal of Physical Oceanography, 26(10), 2169–2182.
 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711 712 	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary current crossover. Part II: Low-frequency internal oscillations. Journal of Physical Oceanography, 26(10), 2169–2182. Sturaro, G. (2003). A closer look at the climatological discontinuities present in the
 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711 712 713 	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary current crossover. Part II: Low-frequency internal oscillations. Journal of Physical Oceanography, 26(10), 2169–2182. Sturaro, G. (2003). A closer look at the climatological discontinuities present in the NCEP/NCAR reanalysis temperature due to the introduction of satellite data.
 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711 712 	 Quenouille, M. (1951). The variate-difference method in theory and practice. Revue de l'Institut International de Statistique, 121–129. Rossby, T. (1999). On gyre interactions. Deep Sea Research Part II: Topical Studies in Oceanography, 46(1-2), 139–164. Rossby, T., & Benway, R. (2000). Slow variations in mean path of the Gulf Stream east of Cape Hatteras. Geophysical Research Letters, 27(1), 117–120. Sanchez-Franks, A., Hameed, S., & Wilson, R. E. (2016). The Icelandic Low as a predictor of the Gulf Stream north wall position. Journal of Physical Oceanography, 46(3), 817–826. Schoonover, J., Dewar, W. K., Wienders, N., & Deremble, B. (2017). Local sensitivities of the Gulf Stream separation. Journal of Physical Oceanography, 47(2), 353–373. Silver, A., Gangopadhyay, A., Gawarkiewicz, G., Silva, E. N. S., & Clark, J. (2021). Interannual and seasonal asymmetries in Gulf Stream ring formations from 1980 to 2019. Scientific Reports, 11(1), 1–7. Smeed, D., McCarthy, G., Rayner, D., Moat, B., Johns, W., Baringer, M., & Meinen, C. (2016). Atlantic Meridional Overturning Circulation observed by the rapid-mocha-wbts (rapid-meridional overturning circulation and heatflux array-western boundary time series) array at 26n from 2004 to 2015. British Oceanographic Data Centre/Natural Environment Research Council. Spall, M. A. (1996). Dynamics of the Gulf Stream/deep western boundary current crossover. Part II: Low-frequency internal oscillations. Journal of Physical Oceanography, 26(10), 2169–2182. Sturaro, G. (2003). A closer look at the climatological discontinuities present in the

nection with the abundance of zooplankton in the uk and its surrounding seas. *ICES Journal of marine Science*, 52(3-4), 711–721.
Taylor, A. H., & Gangopadhyay, A. (2001). A simple model of interannual displacements of the Gulf Stream. *Journal of Geophysical Research: Oceans*, 106(C7), 13849–13860.
Taylor, A. H., Jordan, M. B., & Stephens, J. A. (1998). Gulf Stream shifts following ENSO events. *Nature*, 393(6686), 638–638.

726

727

728

- The MathWorks, I. (2020). Mapping toolbox [Computer software manual]. Natick,
 Massachusetts, United State. Retrieved from https://www.mathworks.com/
 help/map/index.html
 - Thompson, J. D., & Jr, W. S. (1989). A limited-area model of the Gulf Stream: Design, initial experiments, and model-data intercomparison. *Journal of Physical Oceanography*, 19(6), 791-814.
- Tracey, K. L., & Watts, D. R. (1986). On Gulf Stream meander characteristics near
 Cape Hatteras. Journal of Geophysical Research: Oceans, 91(C6), 7587–7602.
- Trenberth, K. E. (1984). Signal versus noise in the Southern Oscillation. Monthly
 Weather Review, 112(2), 326–332.
- Veronis, G. (1973). Model of world ocean circulation. 1. wind-driven, 2-layer. Jour nal of Marine Research, 31(3), 228–288.
- Walker, G., & Bliss, E. (1932). Memoirs of the royal meteorological society. QJR
 Meteorol.Soc., 4 (36), 53.
- Wang, G., Cai, W., & Santoso, A. (2020). Stronger increase in the frequency
 of extreme convective than extreme warm El Niño events under greenhouse
 warming. Journal of Climate, 33(2), 675–690.
- ⁷⁴⁰ Weisberg, S. (2005). Applied linear regression (Vol. 528). John Wiley & Sons.
- Zhang, R., Sutton, R., Danabasoglu, G., Kwon, Y.-O., Marsh, R., Yeager, S. G., ...
 Little, C. M. (2019). A review of the role of the Atlantic Meridional Overturning Circulation in Atlantic multidecadal variability and associated climate impacts. *Reviews of Geophysics*, 57(2), 316–375.
- Zhang, R., & Vallis, G. K. (2007). The role of bottom vortex stretching on the
 path of the North Atlantic western boundary current and on the northern
 recirculation gyre. Journal of Physical Oceanography, 37(8), 2053–2080.
- Zhao, J., & Johns, W. (2014a). Wind-driven seasonal cycle of the Atlantic Meridional Overturning Circulation. Journal of physical oceanography, 44(6), 1541– 1562.
- Zhao, J., & Johns, W. (2014b). Wind-forced interannual variability of the At lantic Meridional Overturning Circulation at 26.5 n. Journal of Geophysical
 Research: Oceans, 119(4), 2403–2419.