# SEASIM-NEAM: A Spatially-Explicit Agent-based SIMulator of North East Atlantic Mackerel population dynamics 

Robin Boyd ${ }^{\text {d,* }}$, Nicola Walker ${ }^{\text {b }}$, Kieran Hyder ${ }^{\text {b,c }, ~ R o b e r t ~ T h o r p e ~}{ }^{\text {b }}$, Shovonlal Roy ${ }^{\text {d }}$, Richard Sibly ${ }^{\text {e }}$<br>${ }^{\text {a }}$ Centre for Ecology and Hydrology, Wallingford, United Kingdom<br>${ }^{\mathrm{b}}$ Centre for Environment, Fisheries and Aquaculture, Science, Lowestoft, United Kingdom<br>${ }^{\text {c }}$ School of Environmental Sciences, University of East Anglia, Norfolk, United Kingdom<br>${ }^{\text {d }}$ Department of Geography and Environmental Science, University of Reading, Reading, United Kingdom<br>${ }^{\mathrm{e}}$ School of Biological Sciences, University of Reading, Reading, United Kingdom


#### Abstract

In 2018 we published a spatially-explicit individual-based model (IBM) that uses satellite-derived maps of food availability and temperature to predict Northeast Atlantic mackerel (Scomber scombrus, NEAM) population dynamics. Since then, to address various ecological questions, we have extended the IBM to include additional processes and data. Throughout its development, technical documents have been provided in the form of e.g. supplementary information to published articles. However, we acknowledge that it would be difficult for potential users to collate information from separate supplementary documents and gain a full understanding of the current state of the IBM. Here, we provide a full technical specification of the latest version of our IBM. The technical specification is provided in the standard ODD (Overview, Design concepts and Details) format, and supplemented by a TRACE (TRAnsparent and Comprehensive model Evaludation) document. For the first time, we give our model the acronym SEASIM-NEAM: a Spatially-Explicit Agent-based SIMulator of North East Atlantic Mackerel population dynamics. This article supersedes previous documentation. Going forward we hope that this article will stimulate development of similar models.


- This article collates improvements that have been made to SEASIM-NEAM over time.

Crown Copyright © 2020 Published by Elsevier B.V.
This is an open access article under the CC BY license (http://creativecommons.org/licenses/by/4.0/)

## A R T I C L E I N F O

Method name: SEASIM-NEAM
Keywords: Atlantic mackerel, Individual-based model, Bioenergetics, Spatially-explicit, Approximate bayesian computation Article history: Received 3 July 2020; Accepted 24 August 2020; Available online 29 August 2020

[^0]| Specifications Table |  |
| :--- | :--- |
| Subject Area | Environmental Science |
| More specific subject area | Fisheries ecology |
| Method name | SEASIM-NEAM |
| Name and reference of original method | Boyd, R., S. Roy, R. Sibly, R. Thorpe, and K. Hyder. 2018. A general approach to |
|  | incorporating spatial and temporal variation in individual-based models of |
|  | fish populations with application to Atlantic mackerel. Ecological Modelling |
|  | $382: 9-17$. |
|  | Boyd, R., R. M. Sibly, K. Hyder, R. B. Thorpe, N. D. Walker, and S. Roy. 2020. |
|  | Simulating the summer feeding distribution of Northeast Atlantic mackerel |
|  | with a mechanistic individual-based model. Progress in Oceanography |
|  | $183: 102299$. |
|  | Boyd R, Thorpe R, Hyder K, Roy S, Walker N and Sibly R (2020) Potential |
|  | Consequences of Climate and Management Scenarios for the Northeast |
|  | Atlantic Mackerel Fishery. Front. Mar. Sci. 7:639. doi: |
|  | $10.3389 / f m a r s .2020 .00639$ |
|  |  |
|  |  |
|  | Model code - https://github.com/robboyd/SEASIM-NEAM/tree/master |
|  | R Markdown documents showing how to run and calibrate the model |
|  | provided in supplementary material. |
|  | Supporting "TRAnsparent and Comprehensive model Evaludation" (TRACE) |
|  | document provided in the supplementary material. |
|  | Input data for the model is very large. We are happy to provide this data to |
| anyone who can provide a means to transfer it. |  |

## Method details

## Model description

In this article, we provide a technical specification of SEASIM-NEAM in the standard ODD (Overview, Design Concepts and Details) format [26]. See [6,7] and [8] for earlier applications of the SEASIM-NEAM. We refer the reader to the supplementary TRACE (TRAnsparent and Comprehensive model Evaludation) document throughout, where full details of the IBM's calibration, validation, sensitivity analyses etc. can be found. SEASIM-NEAM was built in the open-source software NetLogo [83], where it comes with an easy-to-use GUI, but can also be run from the R statistical environment [59] using the RNetLogo package [73]. The Netlogo and R code can be found at https://github.com/ robboyd/SEASIM-NEAM/tree/master.

## Purpose and patterns

The primary goal of SEASIM-NEAM is prediction: it is designed to assess how the Northeast Atlantic mackerel (NEAM) stock may respond to various climate and management (fishing) scenarios. Specifically, the model predicts how e.g. NEAM Spawning Stock Biomass (SSB, biomass of mature individuals), average body weights-at-age and spatial distribution (density and presence/ absence) may respond to spatial and temporal variations in prey availability, temperature and exploitation.

## Model overview

The model seascape comprises dynamic maps of phytoplankton density, which is used as a proxy for baseline prey availability (Fig. 1), Sea Surface Temperature (SST), photoperiod and horizontal current velocities. The fish population represents the largest spawning unit of the NEAM stock, the western component, which has historically comprised $\sim 80 \%$ of the stock's total biomass $[32,33,35]$. It should be noted that there is evidence of straying between the western and the much smaller North Sea spawning component of NEAM [41], which is not accounted for in the IBM. Fish are grouped into super-individuals (SIs), which comprise a number of individuals with identical variables [63]. SIs are sometimes considered to represent schools of identical individuals in varying abundances [66], but the approach is mainly used for computational tractability. Each year, at fixed times, SIs


Fig. 1. SEASIM-NEAM's GUI. There are there are three types of NetLogo widgets shown: Grey buttons (used to initialise and run the model); green "sliders", used to select input values from a specified range; green "choosers" allowing users to select configuration options from drop down menus; and brown "plots and monitors" displaying e.g. predicted population dynamics. See TRACE section 5 for full details of the interface widgets. Grey SIs in the Nordic seas are adults, and the blue SIs to the west of the British Isles are juveniles. The red cells indicate "destination" patches towards which adults migrate. The southerly red cell is the destination for the spawning migration, and the northerly red cell is the destination for the feeding and return overwintering migrations (see text for details). The colour of the landscape corresponds to phytoplankton density: black indicates low density, through green and then white which indicates high density. The colour bins are arbitrary.
migrate between spawning, feeding and overwintering areas. After reaching the destination areas they then move locally until the next migration is triggered. Each SI has an energy budget which determines how its state variables (e.g. body length, body mass, energy stores) change in response to its local environment. Age-specific rates of fishing mortality from the NEAM stock assessment determine the number of individuals removed from the population due to harvesting [37]. A constant number of new SIs enter the model as eggs each year, but the abundance that they represent on entry reflects the amount of energy the spawning stock was able to accumulate for egg production prior to spawning. SIs' abundances are reduced as fishing and natural mortalities are applied each time-step. Population-level outputs are by summarising the characteristics of the SIs including their abundances. For example, biomass is the sum of individual body masses, and spatial distribution is a summary of the individuals' locations.

## State Variables and Scales

The IBM seascape comprises a two-dimensional grid of $60 \mathrm{~km}^{2}$ patches representing the sea surface (Fig. 1). The geographical extent spans from 47 to $77^{\circ} \mathrm{N}$, and from $-45^{\circ}$ to $20^{\circ} \mathrm{E}$. Each grid cell is characterised by prey density, SST, NEAM density, photoperiod (proportion of day length) and horizontal current velocities in x and y dimensions. The NEAM population is represented by a roughly constant number of SIs; as $\mathrm{n}_{\text {cohort }}$ new SIs enter the model as eggs each year, an equal number reach 15 years of age and are removed from the model. Slight variations in the number of SIs arise throughout simulations because 1 ) a SI is removed from the model if its abundance $<1$ (this is rare). Users can select the number of SIs in multiples of 1050 , which is equivalent to choosing $\mathrm{n}_{\text {cohort }}$ in multiples of 70 (as $70 *$ number of age groups $(15)=1050$ ). While the number of SIs remains approximately constant, the abundance that they represent differs: A SI's abundance is determined by the level of egg production in the year that it entered the model, and all subsequent mortality. Each SI is characterised by a number of state variables (see Table 1). The spawning area comprises patches on the continental shelf edge to the west of the British Isles ( $-550 \mathrm{~m}<$ depth $<-50 \mathrm{~m}$; fig. 1) on which $10^{\circ} \mathrm{C}<\mathrm{SST}<14^{\circ} \mathrm{C}$ [65]. The feeding area is a fully emergent feature of the IBM and is not constrained

Table 1
Key state variables charcterising SIs and patches. Here we define state variables as variables that cannot be immediately deduced from the state variables of the other entities [60]. As such this table does not include „rate" variables (e.g. growth, metabolic rate) which could be calculated from e.g. body size and temperature.

| State variable | Description | Details |
| :---: | :---: | :---: |
| Super-individuals |  |  |
| Abundance | Number of "actual" individuals represented by SI |  |
| Age |  | years/ days |
| $\mathrm{A}_{\text {mat }}$ | Age at which sexual maturity was reached | Years |
| Batches | Cumulative number of egg batches spawned in a season | Used to determine when spawning should cease (when >=5) |
| Breed | Life stage | Egg, yolk-sac larvae, larvae, juvenile or adult |
| Development | Number of days developed as an egg |  |
| Energy-reserve | Energy stored as lipid | kJ |
| F | Fishing mortality rate | Day ${ }^{-1}$ |
| Feeding | Whether or not the individual is feeding (only half of year for adults) | Boolean |
| Gender |  |  |
| L | Body length | Cm |
| $\mathrm{L}_{\text {mat }}$ | Length at which sexual maturity was reached | Cm |
| M | Total body mass | g |
| $\mathrm{Mgon}_{\text {gor }}$ | Gonad mass | g |
| Migrating | Whether or not individual is currently migrating | Boolean |
| $\mathrm{M}_{\text {standard }}$ | Standard body mass | g |
| $\mathrm{M}_{\text {struct }}$ | Structural body mass | g |
| Prey-choices | Potential prey (sufficiently small and on same patch as focal individual) | Netlogo ID numbers |
| $\mathrm{fr}_{\mathrm{r}}$ | Realised fecundity | Proportion of potential fecundity |
| $\mathrm{V}_{\mathrm{r}}$ | Realised swimming velocity | Minimum velocity plus random noise (km hour ${ }^{-1}$ ) |
| Spawning | Whether or not an individual is spawning | Boolean |
| $\mathrm{V}_{\text {min }}$ | Minimum swimming velocity | Km hour ${ }^{-1}$ |
| x | x coordinate | Floating point |
| y | y coordinate | Floating point |
| Patches |  |  |
| A4 | In ICES division 4a? | Boolean |
| A5 | In ICES division 5a? | Boolean |
| A6 | In ICES division 6a? | Boolean |
| Depth |  | m |
| Feed-dist | Distance from destination at the entrance to the feeding area | No. Patches |
| Latitude |  | Decimal degrees |
| Longitude |  | Decimal degrees |
| NArea | In nursery area? | Boolean |
| Ocean | In ocean? | Boolean |
| OWArea | In overwintering area? | Boolean |
| $\mathrm{p}_{\text {photo }}$ | Photoperiod | Proportion of 24 h |
| Rectangle | ICES rectangle |  |
| Ricker-spawnarea | Area designated as spawning grounds for Ricker model | Used as area over which to calculate mean SST for use in Ricker recruitment model (not the default recruitment configuration, see TRACE section 3) |
| SArea | In spawning area? | Boolean |
| Shelf-edge | On the European continental shelf edge? | -550 m < depth <-50 m |
| Spawn-dist | Distance from destination at end of spawning migration | No. Patches |
| SST | Sea Surface temperature | ${ }^{\circ} \mathrm{C}$ |
| True-north | Heading equal to true north on the Netlogo grid | Used to calculate effects of horizontal currents in the NetLogo grid |
| True-west | Heading approximately equal to true west on the Netlogo grid | Used to calculate effects of horizontal currents in the NetLogo grid |
| U | Zonal component of current velocity | km hour $^{-1}$ |
| V | Meridional component of current velocity | km hour ${ }^{-1}$ |
| X | Phytoplankton biomass | $\mathrm{g} \mathrm{m}^{-2}$ |



Fig. 2. Conceptual model showing the key bioenergetics processes that individuals of different life stages implement between time $t$ and $t+1$, and the conditions required for progression to the next life stage. Red boxes indicate an effect of SST, and grey boxes an effect of SST and food availability. L is body length.
geographically. The overwintering area is assumed to be ICES divisions 6a (west of Scotland) and 4a (northern North Sea, Fig. 5). The nursery area includes all patches that are $\leq 200 \mathrm{~m}$ deep [42] to the west of the British Isles ( $<4^{\circ} 00$ west). The temporal extent of the IBM depends on the choice of input data; where Earth System Model (ESM) derived inputs are used the model extent may span 1981 to 2050 (chosen by the user), but if satellite-derived inputs are used the temporal extent is fixed at 2005 to 2018. The IBM proceeds in discrete five-day time-steps.

## Processes, Overview and Scheduling

Full details of the model processes are given in the Submodels sections indicated in parentheses here. The order in which individuals or patches carry out a given process is random. State variables
are updated immediately after being calculated by a process. The order in which processes are implemented each time-step are as follows:

1. Phytoplankton and SST data are updated if appropriate (i.e. every tenth day)
2. If it is the first time-step in a month, then photoperiod, current velocities and the proportion of annual fishing mortality that should be applied in that month are updated
3. If it is the first time-step in a year, then annual rates of fishing mortality-at-age are updated
4. Fishing, starvation and background mortalities are applied to SIs (mortality)
5. SIs move to a new location (movement)
6. SIs update their energy budgets (with the exception of reproduction which comes later; energy budget Figure 2)
7. SIs progress to the next life stage if body size thresholds are met (it must also be February 1st for juveniles to reach sexual maturity)
8. If it is the start of the spawning period (March 1st), adults calculate their potential fecundity and the associated energy cost (energy budget)
9. If in the spawning period, adults implement a spawning module. This includes allocating energy to the production of egg batches, spawning those batches at specified intervals, and moving northward as suitably warm regions open up for egg development in the north
10. New SIs enter the model at the egg stage, and calculate their development
11. All SIs age by $\Delta t$ (days post-hatch)
12. SIs' state variables are recorded for analysis outside of the IBM

## Design Concepts

## Emergence

Movement and bioenergetics models describe the ways in which SIs' characteristics (e.g. body mass, energy reserves and location) respond to their local food availability and SST. By summarising the characteristics of all the SIs, population measures can be obtained. For example, SSB can be obtained by summing the individual body masses of all adults, and spatial distribution by summarising the locations of the individuals.

## Sensing

To direct movement individuals can sense the plankton biomass, SST, depth and area type of all patches, and the global variables that indicate when migrations and spawning should begin. To select prey, SIs can sense one another's body length and ID number. In order for density dependence to act an ingestion rates and perceptions of patch profitability (see Movement), SIs can sense the density of mackerel on all patches.

## Interaction

Larger individuals can feed on smaller ones, inflicting predation mortality on them and hence depleting fish prey. Individuals on the same patch also compete with each other for baseline prey (proxied by phytoplankton) according to a competition term in Eq. (2).

## Stochasticity

There are several stochatic elements to the IBM. If not migrating or actively foraging over summer, individuals move randomly to patches within their search radius (see Movement) and with suitable environmental conditions. Swimming velocity when feeding is given by a minimum swimming velocity plus some random noise (see Movement). In the gradient area search (GAS) foraging model, half of each day is spent moving in a random direction. If multiple potential mackerel prey SIs are available, one is selected randomly to be canniblised. At the end of the feeding migration, SIs stop migrating at a randomly selected distance from their target patch at the entrance to the feeding grounds (see Movement). In the spin-up period, recruits enter the model at the end of each year at body length $L_{1}$ (Table 4) minus some random noise.

Table 2
Population metrics obtained by summarising the characteristics of the individuals, and the dates on which they are extracted.

| Metric | Date extracted | Details |
| :---: | :---: | :---: |
| SSB in summer | August 1st | Sum of adult body masses |
| SSB at spawning time | May 1st | Sum of adult body masses |
| Egg production | June 1st | Number of eggs produced by the spawning stock |
| Recruitment | December 31st | Number of young-of-the-year surviving until December 31st |
| Maturity ogives | February 10th | Proportion mature-at-age |
| Adult summer age distribution | August 1st | Relative age distribution (years) of adults |
| Weight of 36 cm individuals | Mean each month | Mean body mass of individuals in the 36 cm length group. This length class was chosen as data are available for each month of the year |
| Quarter 1 juvenile length distribution | March 16th | Relative body length distribution of juveniles |
| Quarter 4 juvenile length distribution | November 23rd | Relative body length distribution of juveniles |
| Mean weight-at-age in summer | August 1st | Mean body mass in each age group |
| Mean weight-at-age at spawning time | May 1st | Mean body mass in each age group |
| Presence/ absence in summer | Mean over July/ August | Whether or not individuals were present on each patch |
| Density in summer | Mean over July/ August | Density of individuals present on each patch |

## Observation

During simulations the state variables of all, or a subset, of the SIs can be extracted and summarised to obtain measures of population dynamics and spatial distribution. Key model outputs are summarised in Table 2.

## Initialization

The IBM is initialised on January 1st of a chosen year (1981 onwards) using numbers-at-age in from the latest ICES stock assessment. This population is apportioned in to $n$ SIs assuming a gender ratio of $1: 1$. Body lengths are calculated from age using the standard von Bertalanffy equation (Eq. 12 here), and energy reserves are set at half maximum. From these all other state variables are calculated when the simulations begin. Adults and juveniles are distributed randomly in the overwintering and nursery areas, respectively (Fig. 5). After initialisation the model spins up for ten years with recruitment forced from the ICES stock assessment. Recruits are introduced at the end of each year, with body length set at the maximum length at the end of the first growing season (first winter), $\mathrm{L}_{1}$ $(\mathrm{cm})$, minus $\varepsilon 3$, where $\varepsilon$ is drawn randomly from uniform distribution between 0 and 1 .

## Input data

The IBM is forced with estimates of fishing mortality at age, chlorophyll concentration (from which we derive phytoplankton biomass with an empirical conversion factor), SST, zonal and meridional horizontal current velocities and photoperiod. See section TRACE section 3 for details of how these data were processed.

## Fishing mortality

Historical annual rates of fishing mortality F at age are taken from the 2019 NEAM stock assessment [37]. Unless stated otherwise, F is applied uniformly to all individuals in an age group regardless of their location. We incorporate monthly variation in F by setting the fractional of annual $F$ taken in each month as proportional to the mean historical (2001 to 2018) fraction of the annual NEAM catch taken in each month (Fig. 3).

The default future fishing scenario comprises a constant F-at-age at the historical mean level (Fig. 3). Alternatively, users can select one of three multipliers which are used to convert the historical mean F over the most important age groups to the fishery (for NEAM 4-8 years) to one of three rates: $\mathrm{F}=0 ; \mathrm{F}_{\mathrm{MSY}}\left(0.23\right.$ year $\left.^{-1}\right)$, i.e. the level of harvesting that is likely to result in maximum sustainable

Table 3
Parameters and their values used in the model. All normalizing and rate constants are shown in units of $1 /$ day and are adjusted for the time-step in the IBM.

| Parameter | Symbol | Value | Units | Reference | Details |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Taxon-specific normalization constant (AMR) | $\mathrm{a}_{\text {AMR }}$ | $8.86 \times 10^{7}$ |  | [16] | See TRACE section 2.3 |
| Assimilation efficiency | $\mathrm{A}_{\text {e }}$ | 0.95 | Proportion of ingested energy | [46] | Proportion of ingested energy made available to the energy budget |
| Normalizing constant for fecundity | $\mathrm{a}_{\mathrm{f}}$ | 8.80 |  | [48] | Normalizing constant for fecundity-length relationship |
| Caudal fin aspect ratio | $\mathrm{A}_{\mathrm{r}}$ | 4.01 |  | FishBase |  |
| Taxon-specific normalization constant (SMR) | $\mathrm{a}_{\text {SMR }}$ | $0.45 \times 10^{8}$ |  | [29] | See TRACE section 2.3 |
| Swimming speed normalizing constant | $\mathrm{a}_{\mathrm{v}}$ | 0.15 |  | [62] | Normalizing constant for speed-length relationship |
| Exponent for the scaling of AMR with body mass | $\mathrm{b}_{\text {AMR }}$ | 0.75 |  | [29] | See TRACE section 2.3 |
| Scaling exponent for fecundity | $\mathrm{b}_{\mathrm{f}}$ | 3.02 |  | [48] | Exponent in fecundity-length relationship |
| Exponent for the scaling of SMR with body mass | $\mathrm{b}_{\text {SMR }}$ | 0.75 |  | [16] | See TRACE section 2.3 |
| Exponent for scaling of swimming velocity with body length | $\mathrm{b}_{\mathrm{v}}$ | 0.62 |  | [62] |  |
| Strength of the predator density dependence | C | $9.71 \times 10^{-11}$ |  | This study | Estimated with ABC (see TRACE section 2.3) |
| Exponent for the scaling of AMR with swimming speed | $\mathrm{c}_{\text {AMR }}$ | 1 |  | [16] | See TRACE section 2.3 |
| Maximum consumption rate | $\mathrm{C}_{\text {max }}$ | 0.69 | $\mathrm{g} \mathrm{g}^{-1}$ day $^{-1}$ | [28] | See TRACE section 2.3 |
| Exponent for scaling of swimming velocity with caudal fin aspect ratio | $\mathrm{c}_{\mathrm{V}}$ | 0.35 |  | [62] |  |
| Activation energy | $\mathrm{E}_{\text {a }}$ | 0.5 | eV | [22] | Minimum energy required for physiological chemical reactions |
| Energy content of flesh | Eflesh | 7.00 | kJ g ${ }^{-1}$ | [53] |  |
| Energy content of lipid | $\mathrm{E}_{\text {lipid }}$ | 39.3 | $\mathrm{kJ} \mathrm{g}{ }^{-1}$ | [64] |  |
| Maximum energy reserves | $\mathrm{E}_{\text {max }}$ | 0.78 | Proportion of structural mass | [24] | See TRACE section 2.3 |

Table 3 (continued)

| Parameter | Symbol | Value | Units | Reference | Details |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Energy density of phytoplankton | $\mathrm{E}_{\text {phyto }}$ | 6.02 | kJ g ${ }^{-1}$ | [2] |  |
| Energy costs of synthesizing flesh | $\mathrm{E}_{\text {sf }}$ | 3.60 | kJ g ${ }^{-1}$ | [67, 68] |  |
| Energy costs of synthesizing lipid | $\mathrm{E}_{\text {sl }}$ | 14.7 | $\mathrm{kJ} \mathrm{g}{ }^{-1}$ | [58] | See TRACE section 2.3 |
| Half saturation constant | h | 1.26 | $\mathrm{g} \mathrm{m}{ }^{-2}$ | This study | Estimated with ABC (see section 2.3). The food density at which ingestion is half maximum at a given temperature |
| Rate of cannibalism | $\mathrm{IR}_{\text {cannibalism }}$ | 0.064 | Proportion of ingestion rate | [56] | Only relavent where suitable prey are available. Proportion of ingestion rate comprising mackerel prey. |
| Growth constant | k | $8.6 \times 10^{-4}$ | day $^{-1}$ | FishBase | See TRACE section 2.3 |
| Boltzmann's constant | K | $8.62 \times 10^{-5}$ | $\mathrm{eV} \mathrm{K}{ }^{-1}$ |  |  |
| Maximum growth rate | $\mathrm{k}_{1}$ | 0.025 | $\mathrm{day}^{-1}$ | [79] | See TRACE section 2.3 |
| Maximum length after first growing season | $\mathrm{L}_{1}$ | 20 | cm | [79] |  |
| Asymptotic length | $\mathrm{L}_{\infty}$ | 42.4 | cm | FishBase | See TRACE section 2.3 |
| Length at hatching | $\mathrm{L}_{\text {hatch }}$ | 0.3 | cm | [79] |  |
| Threshold length for maturity | $\mathrm{L}_{\text {mat }}$ | 26.2 | cm | FishBase | See TRACE section 2.3 |
| Background adult mortality | $\mathrm{M}_{\mathrm{a}}$ | 0.00041 | day $^{-1}$ | [36] | Constant for all ages, based on tagging studies in 1980's and used in the stock assessment |
| Background early mortality | $\mathrm{M}_{\text {e }}$ | 0.287 | day ${ }^{-1}$ | This study | Estimated with ABC (see TRACE section 2.3). Applied to eggs, yolk-sac larvae and larvae |
| Number of egg batches spawned | $\mathrm{n}_{\mathrm{b}}$ | 5 | season ${ }^{1}$ | This study | For simplicity, the actual number is around 20 |
| Lower temperature limit | $\mathrm{SST}_{\text {lim }}$ | 7 | ${ }^{\circ} \mathrm{C}$ | [52] | In summer the threshold SST below which SIs avoid |
| Age at maximum growth | $\mathrm{t}_{\text {max }}$ | 55 | days | [79] |  |



Fig. 3. Left panel: Mean historical $F$ at age ( 2001 to 2018 , black line) from which $F_{M S Y}$ is calculated with a multiplier of 0.83 (grey line) and $\mathrm{F}_{\text {lim }}$ with a multiplier of 1.66 (red line). Right panel: Proportion of annual catch in each month over the historical period which is used to apportion $F$ over each year in SEASIM-NEAM.


Fig. 4. Conceptual movement algorithm. Local movement differs between different areas and at different times (e.g. spawning period and overwintering, see text for full details).
yield in the long-term; and $\mathrm{F}_{\text {lim }}\left(0.46\right.$ year $\left.^{-1}\right)$, i.e. high mortality used as an upper reference point [31,38] (see Fig. 3). Monthly variation in F is implemented as in the historical period.

## Environmental inputs

Environmental inputs to SEASIM-NEAM include maps of chlorophyll concentration, from which we derive phytoplankton density (with an empirical conversion factor), SST, bathymetry, photoperiod and horizontal current velocities. Users can select chlorophyll and SST estimates derived from satellite remote-sensing, or from the earth system model GFDL-ESM-2M [18]. The satellite-derived inputs comprise ten-day composites and are updated accordingly. It should be noted that when using the satellite-derived inputs the temporal extent of SEASIM-NEAM is fixed at 2005 to 2018. The ESM outputs represent monthly averages. The data required processing for use in SEASIM-NEAM (e.g. regridding), the details of which can be found in TRACE section 3. When using the ESM inputs users must choose from one of representative concentration pathways (RCPs) 2.6 or 8.5 , representing high and low levels of climate change mitigation action, respectively. Forecasts of the environmental inputs are available out to 2050 for each RCP scenario.


Fig. 5. Left panel: Broad summary of adults locations throughout a year. White segments indicate migrations which begin at the start of a month but do not necessarily last the whole month. Right panel: Locations of the spawning (orange cells), overwintering (red boxes) and nursery areas (white cells, yellow cells are both spawning and nursery areas). The adult feeding distribution is not constrained geographically; it is a fully-emergent feature of the IBM.

Near surface (average over 0 to -30 m ) horizontal current velocities were taken from the $1 / 3^{0}$ OSCAR dataset [20]. Currents influence the movements of adults over summer (Eq. 4), so we obtained data for the months May through September. Outside of this period current velocities have no effect in SEASIM-NEAM. It would not be appropriate to include the effects of near surface current velocities on individuals outside of the summer period, when mackerel may inhabit deeper waters (e.g. -50 to 220 m over winter) [39]. Over summer NEAM are found in the upper water layer (average of $\sim-20 \mathrm{~m}$ ) [50]. As data are not available for the selected months prior to 2012, we generated mean climatologies for each month over 2012 to 2018. As such we do not account for inter-annual variability in current velocities.

Data on photoperiod (as a proportion of 24 h ) at all latitudes in the IBM grid was extracted for each month using the daylength() function in the R package geosphere [30]. Values correspond to the 15th day of each month, and are updated at the start of each month in SEASIM-NEAM.

Sub-models

Most parameters were derived from the literature as shown in Table 4. Mass is in units of wet weight throughout.

## Movement

The following sub-models describe the ways in which SIs are directed around the landscape. In broad terms, SIs migrate between different areas (e.g. spawning, nursery, feeding), and otherwise move locally within an area. Migrations are date-triggered. Localised movement differs between area, e.g. local movement when spawning in spring differs from local movement when feeding over summer. At most times of year movement is represented in discrete space, i.e. on a patch-by-patch basis. However, we spent considerable time improving the way in which movement is modelled for adults in the summer period [7], which now operates in continuous space (details below). We hope that in time SEASIM-NEAM will be further developed such that all movement is described in a Lagrangian framework.

## Migrations

Adults cycle between overwintering, spawning and feeding areas [75] (see state variables and scales). Migration departure dates were approximated from Uriarte et al. [75] and Petitgas et al. [55] and imposed at: October 1st for the overwintering migration; February 1st for spawning; and May 1st for the feeding migration (Fig. 5). While this scheme captures the general pattern of NEAM migration, it should be noted that in reality migration timings can vary between years [40].

Once a migration is triggered, adults move from their current area towards the relevant destination. For each migration there is a destination patch corresponding to the entrance to the
relevant area. The destination for the feeding and return overwintering migrations are at the entrance to the feeding area in the Faroe Shetland channel (northernmost red patch on Fig. 1). For the spawning migration the destination patch is located in the southern region of the spawning area (southernmost red patch on Fig. 1). We give each patch that is not on land an index R corresponding to its distance from the destination patch, while accounting for the fact that individuals cannot move over land. Once a migration is triggered (see Fig. 5 for dates), individuals move towards the appropriate destination to a patch with the lowest R within their possible search area. A SIs‘ search area is calculated from its minimum swimming velocity $\mathrm{V}_{\text {min }}\left(\mathrm{km} \mathrm{hr}^{-1}\right)$ [62]:

$$
\begin{equation*}
V_{\min }=a_{v} L^{b_{v}} A_{r}{ }^{c_{v}} \tag{1}
\end{equation*}
$$

where $a_{V}$ is a normalizing constant, $L$ is body length, $A_{r}$ is the caudal fin aspect ratio, and $b_{V}$ and $c_{v}$ are scaling exponents (see Table 2 for a full list of parameters and TRACE section 8 for a local sensitivity analysis). Eq. 1 allows larger SIs to arrive earliest in destination areas, which has been noted for NEAM [40].

The spawning and feeding migrations are slightly more complicated than the overwintering migration, as they occur primarily along the European shelf edge to the west of the British Isles $[10,81]$. We represent the shelf edge with a corridor around the British Isles in which 550 m < depth <-50 m (Fig. 1). For the spawning and feeding migrations we then add the constraint that individuals must remain on the shelf edge while moving to minimise $R$.

## Local movement

There are three types of local (non-migratory) movement in SEASIM-NEAM: 1 ) adult foraging in the summer months; 2) random movement constrained to a particular area type (e.g. juveniles in the nursery area, adults in overwintering area in deep winter months); and 3) gradual northward movement on the spawning grounds as suitably warm regions open up for egg development in spring. The details of each type of local movement are given below.

## Adult foraging

At the end of their feeding migration (Fig. 5), adults begin to move in search of the most profitable locations at which to feed. Each patch is characterised by a profitability cue $\mathrm{c}_{\mathrm{dd}}$ which is proportional to potential ingestion rate (Eq. 6) in that location. $c_{\text {dd }}$ represents the bottom-up effect of phytoplankton density as a proxy for food availability, a density-dependent effect of intraspecific competition, an effect of photoperiod (as NEAM are primarily visual feeders), and an effect of SST (Kelvins), in the form of a Beddington-DeAngelis functional response [4,15]:

$$
\begin{equation*}
\mathrm{c}_{\mathrm{dd}}=\mathrm{A}(\mathrm{SST}) \mathrm{p}_{\text {photo }} \frac{\mathrm{X}}{\mathrm{X}+\mathrm{h}+\mathrm{cD}} \tag{2}
\end{equation*}
$$

where X is phytoplankton density $\left(\mathrm{g} \mathrm{m}^{-2}\right)$, h is a half saturation constant, $\mathrm{p}_{\text {photo }}$ is photoperiod (as a proportion of 24 h ) at the SI's location, D is local mackerel density ( $\mathrm{g} \mathrm{patch}^{-1}$ ), c determines the strength of the density dependence, and $\mathrm{A}(\mathrm{SST})$ is an Arrhenius function giving the effect of SST. $\mathrm{A}(\mathrm{SST})$ is given as:

$$
\begin{equation*}
\mathrm{A}(\mathrm{SST})=\mathrm{e}^{\frac{-\mathrm{E}_{a}}{\mathrm{~K}}\left(\left(\frac{1}{\left.\left(\frac{1}{s S T}\right)-\left(\frac{1}{T_{\text {ref }}}\right)\right)}\right.\right.} \tag{3}
\end{equation*}
$$

where $E_{a}$ is an activation energy, $K$ is Boltzmann's constant and $T_{\text {ref }}$ is an arbitrary reference temperature.

SIs move in search of the most profitable locations (Eq. 2) at which to feed following a gradient area search (GAS). The GAS algorithm is based on those of Politikos et al. [57], Tu et al. [74] and Boyd et al. [7]. SIs can detect the profitability of the four patches neighbouring their current location. Positions are updated five times per time step (i.e. once per day) to ensure that SIs cannot overshoot the neighbouring patch. Positions in x and y dimensions are updated by:

$$
\begin{align*}
& x_{t+1}=x_{t}+\left(D_{x}+R_{x}+C_{x}\right) \\
& y_{t+1}=y_{t}+\left(D_{y}+R_{y}+C_{y}\right) \tag{4}
\end{align*}
$$

where $D_{x}$ and $D_{y}$ denote orientated movements towards the most profitable patches, $R_{x}$ and $R_{y}$ denote random movements, and $C_{x}$ and $C_{y}$ are displacements caused by zonal and meridional horizontal currents, respectively.

In the orientated component of Eq. (4) $\mathrm{D}_{\mathrm{x}}$ and $\mathrm{D}_{\mathrm{y}}$, SIs make a comparison between the environment at their current location and that of the day before. If it their current location is more profitable, then they maintain the heading of the orientated component of their movement the day before. If their current location is less profitable than the day prior, SIs undertake a gradient search towards what is perceived to be the most profitable neighbouring patch, given by:

$$
\begin{align*}
& D_{x}=V_{r} \frac{g_{x}}{\sqrt{g_{x}^{2}+g_{y}{ }^{2}}} \\
& D_{y}=V_{r} \frac{g_{y}}{\sqrt{g_{x}^{2}+g_{y}{ }^{2}}} \tag{5}
\end{align*}
$$

where $g_{x}$ and $g_{y}$ are the gradients of the profitability cue (Eqn 2) in $x$ and $y$ dimensions, and $\mathrm{V}_{\mathrm{r}}$ is realized swimming velocity. $\mathrm{V}_{\mathrm{r}}$ is equivalent to $\mathrm{V}_{\text {min }}$ (Eq. 2) plus some random noise, as $\mathrm{V}_{\mathrm{r}}=\mathrm{V}_{\text {min }}+\left(\mathrm{V}_{\text {min }} \varepsilon\right)$, where $\varepsilon$ is drawn randomly from a uniform distribution ranging from zero to one.

Following Politikos et al. [57] we assume that SIs spend half of each day moving in search of the best feeding opportunities ( $\mathrm{D}_{\mathrm{x}}, \mathrm{D}_{\mathrm{y}}$ ) and half moving in a random direction that is not southward ( $\mathrm{R}_{\mathrm{x}}, \mathrm{R}_{\mathrm{y}}$ ). Random southward movement is not permitted because acoustic studies have shown that NEAM infrequently swim southwards over summer [50]. However, SIs may still move southward during the oriented component of the GAS algorithm (i.e. if feeding conditions are best on a more southerly patch), or due to currents. $\mathrm{R}_{\mathrm{x}}$ and $\mathrm{R}_{\mathrm{y}}$ introduce stochasticity into the GAS models and prevent unrealistic overcrowding on optimal patches.

The effects of horizontal currents on SIs' locations, $\mathrm{C}_{\mathrm{x}}, \mathrm{C}_{\mathrm{y}}$, are given as zonal ( u ) and meridional ( v ) current velocities ( $\mathrm{km}_{\mathrm{h}}^{\mathrm{h}} \mathrm{Sor}^{-1}$ ), respectively, multiplied by the time step (here 24 h as the GAS model operates five times per 5 day time-step).

NEAM avoid areas in which temperature is below $7^{0} \mathrm{C}$ [52]. To reflect this, SIs are deterred from moving to patches on which SST is below this threshold. In the directed component of Eq. 4, we repel individuals from patches with SST $<7^{\circ} \mathrm{C}$ by setting their profitability at zero. For the random component of Eq. 4, if a SI orientates towards a patch on which SST < $7^{\circ}$, its heading is reversed. If currents displace individuals on to an intolerably cold patch (or land) then this movement is abandoned and the SI instead moves to the centroid of the nearest suitable patch.

The energy cost associated with the GAS algorithm is subsumed in to a SI's active metabolic rate (see Maintenance for details).

## Random movement constrained to particular area types

Movement for adults in the overwintering area, and juveniles in the nursery area, follows a true random walk: They each move to a randomly-selected patch within their possible search area and the same area type each time-step (see migrations and Eq. 1).

## Spawning movement

Spawning begins on March 1st and lasts for 60 days [19,43,82]. This period covers peak spawning in 2007 and 2010 as observed in the triennial mackerel egg survey (MEGS) [34]. Throughout spring NEAM gradually progress northwards towards the feeding area as warming opens up suitable spawning habitat at higher latitudes [14,19]. To reflect this, after spawning a batch of eggs, SIs move to the nearest patch north of their current location on which $10^{\circ} \mathrm{C}<\mathrm{SST}<14^{0} \mathrm{C}$ (preferred spawning temperature). If there are no patches northwards in which $10^{\circ} \mathrm{C}<$ SST $<14^{\circ} \mathrm{C}$, SIs move to a random neighboring patch within that temperature range.

## Bioenergetics

The following sub-models describe the energy budgets of larvae, juveniles and adults in terms of individual physiology. We assume eggs and yolk-sac larvae have sufficient energy to satisfy maintenance and maximal growth/ development.

## Prey availability

SIs can cannibalise other individuals which are: 1) located on the same patch at the same time; $2) \geq 3.5$ times smaller (as in [66]); and 3 ) $<0.33 \mathrm{~cm}$ [3]. If multiple SIs satisfy these conditions, then one is chosen at random to be preyed upon. The energy content of prey depends its fat content (as a proportion of its total mass). Lipid has an energy content $\mathrm{E}_{\text {lipid }}\left(\mathrm{kJ} \mathrm{g}^{-1}\right)$ which is higher than the energy content of structural mass (1- lipid content, $\mathrm{E}_{\text {flesh }}$ ). At most times individuals do not overlap with potential mackerel prey and instead eat phytoplankton, which we use as a proxy for baseline food availability, with energy content $\mathrm{E}_{\mathrm{p}}\left(\mathrm{kJ} \mathrm{g}^{-1}\right)$.

## Ingestion and energy uptake

Adults fast from November until after spawning the following year. Otherwise, ingestion rate IR is given as a function of both predator and prey density. This is described by a Beddington-DeAngelis functional response [4,15], relating IR to body surface area $\left(\mathrm{M}^{2 / 3}\right)[45]$ and SST (kelvin), as:

$$
\begin{equation*}
\mathrm{IR}=\mathrm{A}(\mathrm{SST}) \mathrm{C}_{\max } \frac{\mathrm{X}}{\mathrm{X}+\mathrm{h}+\mathrm{cD}} \mathrm{M}^{2 / 3} \tag{6}
\end{equation*}
$$

where IR is in g time-step ${ }^{-1}, \mathrm{C}_{\text {max }}$ is the maximum ingestion rate ( g time-step ${ }^{-1} \mathrm{~g}^{-1}$ mackerel), h a the half saturation constant $\left(\mathrm{g} \mathrm{m}^{-2}\right), \mathrm{X}$ is phytoplankton density $\left(\mathrm{g} \mathrm{m}^{-2}\right), \mathrm{D}$ is local mackerel density ( g patch ${ }^{-1}$ ) including the density of the focal individual, c determines the strength of predator density dependence and $\mathrm{A}(\mathrm{SST}$ ) is an Arrhenius function giving the effect of SST (Eq. 3). If potential mackerel prey are available (see conditions above), then a proportion of $I \mathbb{R}, \mathrm{IR}_{\text {cannibalism }}$, comprises mackerel prey (see mortality later in this section for the associated predation mortality). A justification for $\mathrm{IR}_{\text {cannibalism }}$ is provided in TRACE section 3. The remainder of ingested prey, total IR multiplied by ( $1-\mathrm{IR}_{\text {cannibalism }}$ ), comprises baseline prey availability as proxied by phytoplankton. Ingestion rate is converted from g time-step ${ }^{-1}$ to kJ time-step ${ }^{-1}$ using the energy content of the relevant prey type $(\mathrm{kJ}$ $\mathrm{g}^{-1}$ ). A proportion of ingested energy, an assimilation efficiency $\mathrm{A}_{\mathrm{e}}$, becomes available for allocation to the following vital processes.

## Maintenance

Standard metabolic rate, SMR, the level below which an individual cannot survive [21], is used as a baseline measure of maintenance. SMR scales with body mass and temperature, according to:

$$
\begin{equation*}
S M R=a_{S M R} M^{b_{S M R}} e^{-E_{a} / K S S T} \tag{7}
\end{equation*}
$$

where SMR is measured in kJ time-step ${ }^{-1}$, $\mathrm{a}_{\text {SMR }}$ is a normalizing constant and $\mathrm{M}^{\mathrm{b} \text { SMR }}$ is body mass ( g ) raised to a scaling exponent $\mathrm{b}_{\text {SMR }}$ (see TRACE section 2.3). SMR is increased to active metabolic rate (AMR, kJ time-step ${ }^{-1}$ ) when migrating or actively foraging, given by:

$$
\begin{equation*}
\mathrm{AMR}=\mathrm{a}_{\mathrm{AMR}} \mathrm{M}^{\mathrm{b}_{\mathrm{AMR}} V^{\mathrm{c}_{\mathrm{AMR}}} \mathrm{e}^{-\mathrm{E}_{\mathrm{a}} / \mathrm{KSST}}, ~} \tag{8}
\end{equation*}
$$

where $\mathrm{a}_{\text {AMR }}$ is another normalizing constant and V is swimming velocity $\left(\mathrm{km} \mathrm{hr}^{-1}\right)$. For this case study we calculated that AMR scales linearly with V , i.e. an exponent of 1 (see TRACE section 2.3).

## Growth

S. scombrus growth has a different form and rate in the first growing season than in later life [71,84]. Body length $L(\mathrm{~cm})$ at age $t$ (days) in the first growing season is well described by the Gompertz function:

$$
\begin{equation*}
\mathrm{L}_{\mathrm{t}}=\mathrm{L}_{1} \mathrm{e}^{-\mathrm{e}^{-\mathrm{k}_{1}\left(\mathrm{t}-\mathrm{t}_{\max }\right)}} \tag{9}
\end{equation*}
$$

[13,23,69,79] where $L_{1}$ is the maximum length at the end of the first growing season (cm), $\mathrm{k}_{1}$ is the maximum growth rate in the first season, and $t_{\max }$ is $t$ (days) at which growth is maximum. $\mathrm{k}_{1}$ is adjusted for the SST at which it was recorded using the Arrhenius function. For older individuals the von Bertalanffy equation [5] is generally used:

$$
\begin{equation*}
\mathrm{L}_{\mathrm{t}}=\mathrm{L}_{\infty}\left(1-\mathrm{e}^{-\mathrm{k}\left(\mathrm{t}-\mathrm{t}_{0}\right)}\right) \tag{10}
\end{equation*}
$$

[78] where k is the Bertalanffy growth constant (time-step ${ }^{-1}$ ), $\mathrm{L}_{\infty}$ is the asymptotic length (cm) and $\mathrm{t}_{0}$ is an adjustment parameter. k is adjusted for the SST at which it was recorded using the

Arrhenius function. Taking the end of the first growth phase to be at $\mathrm{t}=240$ (days, see TRACE section 2.3), from Eqs. 9 and 10 the maximum growth rate $\Delta \mathrm{L}\left(\mathrm{cm}\right.$ time-step $\left.{ }^{-1}\right)$ is given by:

$$
\Delta L=\left\{\begin{array}{cl}
k_{1} e^{\frac{-E_{a}}{K}\left(\left(\frac{1}{\text { sST }}\right)-\left(\frac{1}{T_{\text {ref }}}\right)\right)} L \ln \left(\frac{L_{1}}{L}\right), & t<240  \tag{11}\\
k e^{\frac{-E_{a}}{K}\left(\left(\frac{1}{\text { ssT }}\right)-\left(\frac{1}{T_{\text {ref }}}\right)\right)}\left(L_{\infty}-L\right), & t \geq 240
\end{array}\right.
$$

We assume that adults grow only when feeding [55], i.e. for half of the year. To reflect this, their value of k obtained from Eq. 10 is doubled. $\Delta \mathrm{L}$ ( cm time-step ${ }^{-1}$ ) is converted to the difference in structural mass $\Delta \mathrm{M}$ ( g time-step ${ }^{-1}$ ) assuming an allometric relationship between L and structural body mass $\mathrm{M}_{\text {struct }}$ :

$$
\begin{equation*}
M_{\text {struct }}=a_{w} L^{b_{w}} \tag{12}
\end{equation*}
$$

where $a_{w}$ is a normalizing constant and $b_{w}$ is a scaling exponent. We define structural mass as total body mass minus lipid stores and gonads. Growth costs are calculated using $\Delta M\left(E_{c}+E_{s}\right)$, where $E_{c}$ is
 energy is available to support maximum growth, the growth rate is reduced accordingly.

## Reproduction

The maximum number of eggs that a female can produce, potential fecundity $f_{p}$, is calculated at the beginning of the spawning period (Fig. 5) as a function of body length L , as:

$$
\begin{equation*}
f_{p}=a_{f} L^{b_{f}} \tag{13}
\end{equation*}
$$

where $a_{f}$ is a normalizing constant and $b_{f}$ is a scaling exponent. The energy cost of producing $a$ maximum-sized batch of eggs $b_{\max }\left(\mathrm{kJ}\right.$ time-step ${ }^{-1}$ ) is then given as a function of $f_{p}$, as:

$$
\begin{equation*}
\mathrm{b}_{\max }=\frac{\mathrm{f}_{\mathrm{p}} \mathrm{M}_{0}\left(\mathrm{E}_{\mathrm{c}}+\mathrm{E}_{\mathrm{s}}\right)}{\mathrm{n}_{\mathrm{b}}} \tag{14}
\end{equation*}
$$

where $M_{0}$ is egg mass, $E_{c}$ is the energy content of flesh, $E_{s}$ is the cost of synthesising tissue and $n_{b}$ is the number of batches produced. NEAM are batch spawners, so energy is allocated to each batch over the inter-batch intervals $\mathrm{b}_{\text {int }}$. Hence, the duration of the spawning period is given by $\mathrm{n}_{\mathrm{b}}$ multiplied by $b_{\text {int }}$. If less energy than $b_{\text {max }}$ is available, batch size is reduced accordingly. We define gonad mass as equal to the mass of the eggs produced in a batch. This increases as energy is allocated to a batch over $\mathrm{b}_{\text {int }}$, then is reset to zero when that batch is spawned. The egg production of all females is divided equally among $\mathrm{n}_{\text {cohort }}$ new individuals (eggs) each year. We assume that male and female investment in reproduction is equal.

## Energy reserves

Larval mackerel prioritse growth [54] over energy storage. Juveniles and adults store energy as lipid $[24,80]$ in preparation for maturation, spawning and, for adults, the winter fast. Individuals can store energy up to their maximum possible energy reserve $\mathrm{E}_{\max }$ (see TRACE section 2.3). The energy cost of synthesising lipid $\mathrm{L}_{\mathrm{s}}$ is accounted for when assimilated energy is converted to energy stores. The mass of stored lipid and, for adults, the gonads are added to structural mass to get total mass M .

## Egg development

While embryo duration in S. scombrus decreases with temperature, background mortality rate $M_{\text {back }}$ increases. Hence, the cumulative proportion of eggs that die from $M_{\text {back }}$ varies little except at extreme temperatures [49] (see TRACE section 2.4) not encountered in the model (see TRACE section 2.4). We therefore assume for simplicity that the egg development period is five days and $\mathrm{M}_{\text {back }}$ is constant at rate $\mathrm{M}_{\mathrm{e}}$ (see Mortality).


Fig. 6. Predicted vs observed (stock assessment, red dots) SSB. The black line denotes the single best-fitting simulation from the ABC, and the grey shaded area delimits the $95 \%$ credible intervals from the accepted $1 \%$ of 2000 simulations (i.e. the posterior parameter uncertainty).

## Ontogenetic transformation

Eggs transform into yolk-sac larvae at length $\mathrm{L}_{\text {hatch }}$ once reaching the end of their development period. Thereafter individuals transform into larvae (cease to be nourished by the yolk sac) when they reach 0.61 cm [72]; into juveniles when they reach 3 cm (at which point S.scombrus have been observed to exhibit active taxis and schooling behaviour; Sette [65]); and can sexually mature as adults after reaching 26.2 cm ( $\mathrm{L}_{\mathrm{mat}}$ ). For simplicity juveniles with a sufficient length all reach maturity on the same day each year, February 1st. At this point they join the adult migration towards the spawning area.

## Mortality

The ways in which the abundance n of of an individual can decrease are outlined below.
Starvation: If a SIs total mass reduces to its structural mass it is removed from the model.
Predation: If a SI is selected as prey for a larger SI, its abundance is reduced by $M_{\text {pred }}$. $M_{\text {pred }}$ is given as ingestion rate IR of the predator ( g time-step $^{-1}$ ) / prey body mass ( g ), after adjusting the predator's $I R$ by $\mathrm{IR}_{\text {cannibalism }}$. Hence, $\mathrm{M}_{\text {pred }}$ depends on the number of predators and SST.

Background mortality: Eggs and larvae are susceptible to background mortality at rate $\mathrm{M}_{\mathrm{e}}$. Juvenile susceptibility to $\mathrm{M}_{\text {back }}$ at length L is given by:

$$
\begin{equation*}
\mathrm{M}_{\mathrm{back}}=\mathrm{M}_{\mathrm{a}} \frac{\mathrm{~L}_{\mathrm{mat}}}{\mathrm{~L}} \tag{15}
\end{equation*}
$$

where $\mathrm{M}_{\mathrm{a}}$ is a constant equal to adult mortality susceptibility (time-step ${ }^{-1}$ ), $\mathrm{L}_{\mathrm{mat}}$ is the threshold length above which juveniles can sexually mature and L is length (cm) [9]. Because background mortality rates decrease with life stage or body length, cumulative mortality depends on growth.

Fishing mortality: Annual rates of fishing mortality rates F (time-step ${ }^{-1}$ ) are taken from the stock assessment (stockassessment.org). These rates are applied each day, such that the proportion being applied in each month is proportional to the historical proportion of annual catch in that month (Fig. 3).
$\mathrm{M}_{\text {back }}$ and F are converted to a proportion of a Sl's abundance dying in a time-step as 1 -$\mathrm{e}^{-\left(\mathrm{M}_{\text {back }}+\mathrm{F}\right)}$. Sls with abundance $<1$ are removed from the model.

## Recruitment

Recruitment is defined as the number of young-of-the-year that survive to December 31st each year. This depends on the total number of eggs spawned, and the fraction of those eggs that survive. The number of eggs spawned is determined by the amount of energy that the spawning stock is able to accumulate prior to spawning, which reflects the feeding opportunities available over the previous summer. The fraction of eggs that survive to the end of their first year depends largely on the previling


Fig. 7. Predicted (SEASIM-NEAM, black line) and observed (red dots) weight at ages three to twelve at spawning time (extracted May 1st). The grey shaded region represents the $95 \%$ credible intervals of the posterior distributions as estimated by $A B C$.
environmental conditions on the spawning grounds. Mortality rate is inversely related to body size meaning that, if conditions favour quick growth (e.g. high prey availability and temperature), then cumulative mortality in that cohort is reduced and more SIs recruit. Users can choose to substitute this 'emergent" recruitment scheme for a more traditional Ricker-type stock-recruitment relationship that has been fitted to data from the stock assessment. Doing so removes the egg and larval stages from the IBM; instead, recruits enter the model on December 31st. See TRACE section 2 for details of the Ricker model.

## Model calibration and validation

In the following we outline how SEASIM-NEAM was calibrated and evaluated following the principles of "pattern oriented modelling" (see e.g. [12,25,27,44,61]), i.e. by assessing its ability to match spatial and temporal patterns at the individual and population level.

## Model calibration

Values for three of SEASIM-NEAM's parameters cannot be justifiably extracted from the literature. These parameters are the half saturation constant (h) and strength of the competition effect (c) in the functional feeding response, and the background early mortality rate for eggs and larvae (excluding explicit cannibaism, $\mathrm{M}_{\mathrm{e}}$ ). Although alternative algorithms are available (e.g. [17,70,77]), we estimate these parameters by fitting SEASIM-NEAM to available data using rejection Approximate Bayesian Computation (ABC). Generally following van der Vaart et al. [76], the ABC comprises: 1) selecting data to which the model should be fitted; 2) generating prior distributions for the three parameters; 3) running a number of simulations while randomly sampling values of the parameters from their prior distributions; 4) accepting the parameters that resulted in the best fits to the data; and 5) examining the accepted parameters (i.e. the posterior distributions).


Fig. 8. Predicted and observed presence/ absence of NEAM over July/ August. Predictions were obtained after optimising a threshold mackerel density above which a patch is classed as a presence, and below which it is classed as an absence (see text). The numbers on each panel represent the total proportion of data points for which SEASIM-NEAM correctly predicted whether or not NEAM were present.

We suggest that SEASIM-NEAM should be fitted to estimates of SSB from the latest NEAM stock assessment, and data on weight-at-age (spawning time). For both variables data are freely available at www.stockassessment.org, where they are updated annually. Note that, if new SSB data from the stock assessment is used for calibration, then fishing mortality from the same stock assessment must be used as input to the IBM. If SEASIM-NEAM can simultaneously match data SSB and weight-at-age, then competition for food at a given SSB can be considered realistic, as reflected by the individual body weights of the fish. In addition, the model's ability to match data at both the individual (body weights) and population level (biomass) gives credibility to its underlying structure. For $\mathrm{M}_{\mathrm{e}}, \mathrm{c}$ and h we use uninformative uniform prior distributions spanning intentionally wide bounds, but users can define their own priors based on e.g. expert knowledge. In previous applications we have run 1000-4500 simulations, but again users can decide on how many simulations are sufficient for their purposes. We use the sum of the squared deviations of the model outputs from the data as a cost function, but normalise the deviations to account for differences in units between the datasets. Full details of the most recent ABC can be found in TRACE section 3. We also provide an annotated R script in the supplementary material which can be used to conduct future calibrations. Figs. 6 and 7 show the fits of SEASIM-NEAM to the data on SSB and weight-at-age, respectively.

## Model validation using data on the summer distribution

To assess SEASIM-NEAM's ability to match data that was not used in the ABC, we compare its predictions of presence/ absence over July/ August to observations from the Internation Ecosystem Survey in the Noridc Seas (IESSNS, Fig. 8). See Nøttestad et al. [51] for details of these data, which we
approximated from Olafsdottir et al. (2018) using Java's PlotDigitizer (http://plotdigitizer.sourceforge. net/). To assess model fits we used two standard statistics for binary data, sensitivity and specificity, i.e. the proportion of presences and absences correctly classified, respectively. As is standard, we first optimised a threshold mackerel density (patch ${ }^{-1}$ ) above which that patch is classed as a presence, and below which it is classed as an absence (see TRACE section 7 for full details) [11,47]. After optimising this threshold, sensitivty and specificity values of 0.73 and 0.68 were obtained, respectively. Note that we pooled the predictions and data across all (surveyed) years over 2007 to 2015. This gives extra weight to years in which sampling effort was higher, which we consider appropriate. See Fig. 8 for a comparison of predicted and observed presence/ absence over the summer months.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Acknowledgements

We would like to thank Richard Nash for his helpful comments on this manuscript.

## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:10. 1016/j.mex.2020.101044.

## References

[2] E.R. Annis, E.D. Houde, L.W. Harding, M.E. Mallonee, M.J. Wilberg, Calibration of a bioenergetics model linking primary production to Atlantic menhaden Brevoortia tyrannus growth in Chesapeake Bay, Mar. Ecol. Prog. Ser. 437 (2011) 253-267.
[3] E. Bachiller, X. Irigoien, Marine Science, ICES J. Mar. Sci. 70 (2013) 352-361.
[4] J.R. Beddington, Mutual interference between parasites or predators and its effect on searching efficiency, J. Anim. Ecol. 44 (1975) 331-340.
[5] L. von Bertalanffy, A quantitative theory of organic growth, Hum. Biol. 10 (1938) 181-213.
[6] R. Boyd, S. Roy, R. Sibly, R. Thorpe, K. Hyder, A general approach to incorporating spatial and temporal variation in individual-based models of fish populations with application to Atlantic mackerel, Ecol. Modell. 382 (2018) 9-17.
[7] R. Boyd, R.M. Sibly, K. Hyder, R.B. Thorpe, N.D. Walker, S. Roy, Simulating the summer feeding distribution of Northeast Atlantic mackerel with a mechanistic individual-based model, Prog. Oceanogr. 183 (2020) 102299.
[8] Boyd, R., R. Thorpe, K. Hyder, S. Roy, and N. Walker. 2020 b. Potential consequences of climate and management scenarios for the Northeast Atlantic Mackerel Fishery.
[9] J. Brodziak, J. Ianelli, K. Lorenzen, R.D. Methot, Estimating Natural Mortality in Stock Assessment Applications, U.S. Dep. Commer., NOAA Tech. Memo. NMFS-F/SPO-119, 201138 p.:38.
[10] T. Brunel, C.J.G. van Damme, M. Samson, M. Dickey-Collas, Quantifying the influence of geography and environment on the northeast Atlantic mackerel spawning distribution, Fish. Oceanogr. (2017) 1-15.
[11] S.B. Cantor, C.C. Sun, G. Tortolero-Luna, R. Richards-Kortum, M. Follen, A comparison of C/B ratios from studies using receiver operating characteristic curve analysis, J. Clin. Epidemiol. 52 (1999) 885-892.
[12] N.H. Carter, S.A. Levin, V. Grimm, Effects of human-induced prey depletion on large carnivores in protected areas: Lessons from modeling tiger populations in stylized spatial scenarios, Ecol. Evol. 9 (2019) 11298-11313.
[13] U. Cotano, P. Alvarez, Growth of young-of-the-year mackerel in the Bay of Biscay, J. Fish. Biol. 62 (2003) 1010-1020.
[14] W.A. Dawson, S.J. Lockwood, Changes in western mackerel (Scomber scombrus) spawning stock composition during the spawning season, J. Mar. Biol. Assoc. U.K. (1986) 367-383.
[15] D.L. DeAngelis, R.a. Goldstein, R.V. O'Neill, A model for tropic interaction, Ecology 56 (1975) 881-892.
[16] K.a Dickson, J.M. Donley, C. Sepulveda, L. Bhoopat, Effects of temperature on sustained swimming performance and swimming kinematics of the chub mackerel Scomber japonicus, J. Exp. Biol. 205 (2002) 969-980.
[17] C. Dietzel, K.C. Clarke, Toward optimal calibration of the SLEUTH land use change model, Trans. GIS 11 (2007) 29-45.
[18] J.P. Dunne, J.G. John, S. Shevliakova, R.J. Stouffer, J.P. Krasting, S.L. Malyshev, P.C.D. Milly, L.T. Sentman, A.J. Adcroft, W. Cooke, K.A. Dunne, S.M. Griffies, R.W. Hallberg, M.J. Harrison, H. Levy, A.T. Wittenberg, P.J. Phillips, N. Zadeh, GFDL's ESM2 global coupled climate-carbon earth system models. Part II: Carbon system formulation and baseline simulation characteristics, J. Clim. 26 (2013) 2247-2267.
[19] a.T.G.W. Eltink, Changes in age - size distribution and sex ratio during spawning and migration of Western mackerel (Scomber scombrus L.), J. Cons. int. Explor. Mer. 44 (1987) 10-22.
[20] ESR. 2009. OSCAR third degree resolution ocean surface currents. Ver. 1. PO.DAAC, CA, USA, accessed February 2020.
[21] F.E.J. Fry, Effect of environmental factors on the physiology of fishes, Yale J. Biol. Med. 30 (1971) 152-153.
[22] J.F. Gillooly, A. Allen, V. Savage, E. Charnov, G. West, J. Brown, Response to Clarke and Fraser : effects of temperature, Funct. Ecol. 20 (2006) 400-404.
[23] M.G. Gluyas-Millan, M. Castonguay, C. Quinonez-Velazouez, Growth of juvenile Pacific mackerel, Scomber japonicus in the Gulf of California, Sci. Mar. 62 (1998) 225-231.
[24] Grégoire, F., H. Dionne, C. Lévesque, M. Lamontagne, P. O. Box, and D. Mer. 1992. Fat content of Atlantic mackerel (Scomber scombrus L.) in 1991 and 1992 Canadian Industry Report of Fisheries and Aquatic Sciences 220.
[25] V. Grimm, S.F. Railsback, Pattern-oriented modelling: a "multi-scope" for predictive systems ecology, Philoso. Trans. R. Soc. B: Biol. Sci. 367 (2012) 298-310.
[26] V. Grimm, S.F. Railsback, C.E. Vincenot, U. Berger, C. Gallagher, D.L. Deangelis, B. Edmonds, J. Ge, J. Giske, J. Groeneveld, A.S.A. Johnston, A. Milles, J. Nabe-Nielsen, J.G. Polhill, V. Radchuk, M.S. Rohwäder, R.A. Stillman, J.C. Thiele, D. Ayllón, The ODD protocol for describing agent-based and other simulation models: A second update to improve clarity, replication, and structural realism, Jasss (2020) 23.
[27] V. Grimm, E. Revilla, U. Berger, F. Jeltsch, W.M. Mooij, F. Steven, H. Thulke, J. Weiner, T. Wiegand, D.L. Deangelis, S.F. Railsback, Pattern-Oriented Modeling of Agent Based Complex Systems: Lessons from Ecology, Am. Assoc. Adv. Sci. 310 (2005) 987-991.
[28] M. Hatanaka, K. Sekino, M. Takahashi, T. Ichimura, Growth and food consumption in young mackerel, Pneumatophorus japiconus, J. Agric. Res. (1957) VII.
[29] J.P. Herrmann, E.C. Enders, Effect of body size on the standard metabolism of horse mackerel, J. Fish Biol. 57 (2000) 746-760.
[30] R.J. Hijmans, Geosphere: Spherical Trigonometry, R. Package Version 1.5-10 (2019).
[31] ICES. 2012. 1.7 Acronyms and terminology.
[32] ICES, Report of the benchmark workshop on pelagic stocks (WKPELA), ICES Cm Acom. 43 (2014) 7-125.
[33] ICES. 2014 b. Report of the Report of the Working Group on Widely Distributed Stocks (WGWIDE) report 2014:37-192.
[34] ICES, Manual for the mackerel and horse mackerel egg surveys (MEGS): sampling at sea, Page Ser. ICES Surv. Protoc. (2014).
[35] ICES, ICES WGWIDE Rep. 2017 (2017) 356-503.
[36] ICES. 2017 b. ICES WGWIDE REPORT 2014 Report of the Report of the Working Group on Widely Distributed Stocks (WGWIDE) International Council for the Exploration of the Sea.
[37] ICES. 2019 b. Mackerel (Scomber scombrus) in subareas 1-8 and 14, and in Division 9.a (the Northeast Atlantic and adjacent waters). ICES Advice on fishing opportunities, catch, and effort.
[38] ICES. 2019 a. Norway special request for revised 2019 advice on mackerel (Scomber scombrus) in subareas 1-8 and 14, and in Division 9. a (the Northeast Atlantic and adjacent waters):1-17.
[39] T. Jansen, A. Campbell, C. Kelly, H. Hátún, M.R. Payne, Migration and Fisheries of North East Atlantic Mackerel (Scomber scombrus) in Autumn and Winter, PLoS One (2012) 7.
[40] T. Jansen, H. Gislason, Temperature affects the timing of spawning and migration of North Sea mackerel, Cont. Shelf Res. 31 (2011) 64-72.
[41] T. Jansen, H. Gislason, Population Structure of Atlantic Mackerel (Scomber scombrus), PLoS One (2013) 8.
[42] T. Jansen, K. Kristensen, J. Van Der Kooij, S. Post, A. Campbell, K.R. Utne, P. Carrera, J.A. Jacobsen, A. Gudmundssdottir, B.A. Roel, E.M.C. Hatfield, Nursery areas and recruitment variation of Northeast Atlantic mackerel (Scomber scombrus), ICES J. Mar. Sci. (2014).
[43] P.O. Johnson, A review of spawning in the north Atlantic Mackerel, Scomber Scombrus L (1977).
[44] J.Y. Kang, J. Aldstadt, Using multiple scale spatio-temporal patterns for validating spatially explicit agent-based models, Int. J. Geogr. Inform. Sci. 33 (2019) 193-213.
[45] S.A.L.M. Kooijman, J.A.J. Metz, On the dynamics of chemically stressed populations: the deduction of population consequences from effects on individuals, Hydrobiol. Bull. 17 (1983) 88-89.
[46] T.C. Lambert, Gastric emptying time and assimilation efficiency in Atlantic mackerel (Scomber scombrus), Can. J. Zool. 63 (1985) 817-820.
[47] Liu, C., P. M. Berry, T. P. Dawson, and R. G. Pearson. 2005. Thresholds of occurrence in the prediction of species distributions 28:385-393.
[48] S.J. Lockwood, J.H. Nichols, W.A. Dawson, The estimation of a mackerel (Scomber scombrus L.) spawning stock size by plankton survey, J. Plankton Res. 3 (1981) 217-233.
[49] D. Mendiola, P. Alvarez, U. Cotano, E. Etxebeste, a., M. de Murguia, Effects of temperature on development and mortality of Atlantic mackerel fish eggs, Fish. Res. 80 (2006) 158-168.
[50] L. Nøttestad, J. Diaz, H. Peña, H. Søiland, G. Huse, A. Fernö, Feeding strategy of mackerel in the Norwegian Sea relative to currents, temperature, and prey, ICES J. Mar. Sci. 73 (2016) 1127-1137.
[51] L. Nøttestad, S. p. Jo, J.A. Jacobsen, K.R. Utne, J.O. Guðmundur, Ø. Tangen, V. Anthonypillai, S. Aanes, J.H. Vølstad, M. Bernasconi, J.C. Holst, T. Jansen, A. Slotte, H. Debes, L. Smith, S. Sveinbjo, Quantifying changes in abundance, biomass and spatial distribution of Northeast Atlantic mackerel in the Nordic seas from 2007 to 2014, ICES J. Mar. Sci. 73 (2015) 359-373.
[52] A.H. Ólafsdóttir, K.R. Utne, J.A. Jacobsen, T. Jansen, G.J. Óskarsson, L. Nøttestad, B. P. Elvarsson, C. Broms, A. Slotte, Geographical expansion of Northeast Atlantic mackerel (Scomber scombrus) in Nordic Seas from 2007-2016 was primarily driven by stock size and constrained by low temperatures, Deep-Sea Res. Part II: Top. Stud. Oceanogr. (2018) 0-1.
[53] R. Peters, Ecological implications of body size, Cambridge University Press, New York, 1983.
[54] W. Peterson, S. Ausubel, Diets and selective feeding by larvae of Atlantic mackerel Scomber scombrus on zooplankton, Mar. Ecol. Prog. Ser. 17 (1984) 65-75.
[55] P. Petitgas, A. Uriarte, E. Nogueira, J. Massé, U. Cotano, Life-cycle spatial patterns of small pelagic fish in the Northeast Atlantic, ICES Cooperative Res. Rep. 306 (2010) 40-44.
[56] J.K. Pinnegar, DAPSTOM - An integrated database \& portal for fish stomach records, Page Cefas Contr. Rep. (2014).
[57] D. Politikos, M. Huret, P. Petitgas, A coupled movement and bioenergetics model to explore the spawning migration of anchovy in the Bay of Biscay, Ecol. Modell. 313 (2015) 212-222.
[58] J. Pullar, A. Webster, The energy cost of fat and protein deposition in the rat, Br. J. Nutr. 37 (1977) 355-363.
[59] R Core Team, R: A language and environment for statistical computing, R Foundation for Statistical Computing, Vienna, Austria, 2019.
[60] S.F. Railsback, V. Grimm, Models, agent-based models, and the modeling Cycle 1.1, Agent-Based Individ.-Based Model.: Pract. Introd. (2010) 3-13.
[61] S.F. Railsback, M.D. Johnson, Pattern-oriented modeling of bird foraging and pest control in coffee farms, Ecol. Modell. 222 (2011) 3305-3319.
[62] Sambilay Jr, V. 1990. Interrelationships between swimming speed, caudal fin aspect ratio and body length of fishes.
[63] M. Scheffer, J.M. Baveco, D.L. Deangelis, K.a Rose, E.H. Vannes, Super-Individuals A Simple Solution For Modeling Large Populations On An Individual Basis, Ecol. Modell. 80 (1995) 161-170.
[64] K. Schmidt-Nielsen, Animal physiology: Adaption and environment, Fifth edition, Cambridge University Press, 2013.
[65] O. Sette, Part I. Biology of the atlantic mackerel (Scomber scombrus) of North America, Fish. Bull. (1943) 50.
[66] Y.J. Shin, P. Cury, Exploring fish community dynamics through size-dependent trophic interactions using a spatialized individual-based model, Aquat. Living Resour. 14 (2001) 65-80.
[67] R.M. Sibly, P. Calow, Physiological ecology of animals: an evolutionary approach, Blackwell, 1986.
[68] R.M. Sibly, V. Grimm, B.T. Martin, A.S. a Johnston, K. Kulakowska, C.J. Topping, P. Calow, J. Nabe-Nielsen, P. Thorbek, D.L. Deangelis, Representing the acquisition and use of energy by individuals in agent-based models of animal populations, Methods Ecol. Evol. 4 (2013) 151-161.
[69] P. Sirnard, M. Castonguay, D.D. Arnours, P. Magnan, Growth comparison between juvenile Atlantic mackerel from the two pawning groups of the Northwest Atlantic, Can. J. Fish. Aquat.Sci. (1992) 49.
[70] S.A. Sisson, Y. Fan, M.A. Beaumont, Handbook of Approximate Bayesian Computation, CRC Press, Boca Raton, Florida, 2019.
[71] G. Steven, Contributions to the biology of the mackerel, Scomber scombrus L. III. Age and growth, J. Mar. Biol. Assoc. U. K. (1952) 30.
[72] Studholme, a. L., D. B. Packer, P. L. Berrien, D. L. Johnson, C. a. Zetlin, and W. W. Morse. 1999. Atlantic Mackerel, Scomber scombrus, Life history and Habitat Characteristics. NOAA Technical report NMFS-NE-141:44.
[73] Jan C. Thiele, Winfried Kurth, and Volker Grimm (2012). RNetLogo: An R Package for Running and Exploring IndividualBased Models Implemented in NetLogo. Methods in Ecology and Evolution 3 (3), 480-483. URL http://onlinelibrary.wiley. com/doi/10.1111/j.2041-210X.2011.00180.x/abstract/
[74] C.Y. Tu, Y.H. Tseng, T.S. Chiu, M.L. Shen, C.H. Hsieh, Using coupled fish behavior-hydrodynamic model to investigate spawning migration of Japanese anchovy, Engraulis japonicus, from the East China Sea to Taiwan, Fish. Oceanogr. 21 (2012) 255-268.
[75] Uriarte, A., P. Alvarez, S. Iversen, J. Molloy, B. Villamor, M. M. Martins, and S. Myklevoll. 2001. Spatial pattern of migration and recruitment of North East Atlantic Mackerel.
[76] E. van der Vaart, M. a. Beaumont, A.S. a. Johnston, R.M. Sibly, Calibration and evaluation of individual-based models using Approximate Bayesian ccomputation, Ecol. Modell. 312 (2015) 182-190.
[77] E. Van Der Vaart, D. Prangle, R.M. Sibly, Taking error into account when fitting models using Approximate Bayesian Computation, Ecol. Appl. 28 (2018) 267-274.
[78] Villamor, B., P. Abaunza, and C. Farina. 2001. Age and growth of Northeast Atlantic mackerel in waters off the north and northwest of Spain.
[79] B. Villamor, M. Bernal, C. Hernandez, Models describing mackerel (Scomber scombrus) early life growth in the North and Northwest of the Iberian Peninsula in $2000^{*}$, Sci. Mar. 68 (2004) 571-583.
[80] P.D. Wallace, Seasonal variation in fat content of mackerel (Scomber scombrus L.) caught in the western English Channel, Fish. Res. Tech. Rep., MAFF Direct. Fish Res., Lowestoft (91) (1991) 8 pp:8.
[81] M. Walsh, D.G. Reid, W.R. Turrell, Understanding mackerel migration off Scotland: Tracking with echosounders and commercial data, and including environmental correlates and behaviour, ICES J. Mar. Sci. 52 (1995) 925-939.
[82] J.J. Watson, I.G. Priede, P.R. Witthames, A. Owori-Wadunde, Batch fecundity of Atlantic mackerel, Scomber scombrus L, J. Fish. Biol. (1992) 591-598.
[83] Wilensky, U.1999. NetLogo. http://ccl.northwestern.edu/netlogo/.
[84] T.M. Yohannan, The growth pattern of Indian mackerel, Ind. Jo. Fish. (1979) 26.


[^0]:    * Corresponding author.

    E-mail address: robboy@ceh.ac.uk (R. Boyd).

