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# <sup>1</sup> Organizing principles for vegetation dynamics

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# 49 Abstract

50 Understanding vegetation dynamics is very challenging because of the multitude of contributing processes at 51 widely different spatial and temporal scales. In this Perspective we propose that understanding of vegetation 52 dynamics can be improved, permitting better predictions, based on organizing principles that constrain plant 53 and ecosystem behaviour: natural selection, self-organization, and entropy maximization. Although these 54 ideas are increasingly used, a limited common understanding of their theoretical basis has prevented their full 55 potential to be realized. We explain the power of natural selection-based optimality to predict photosynthesis 56 and carbon allocation responses to multiple environmental drivers, and how individual plasticity leads to the 57 predictable self-organization of forest canopies. We show how models of natural selection acting on a few key 58 traits can generate realistic plant communities, and how entropy maximization can distinguish between 59 stochastic and deterministic drivers of vegetation patterns. We present directions for how these principles can 60 be combined to improve the capacity of vegetation models to explain and predict the complex responses to

61 environmental changes, resting on strengthened theoretical foundations.

# 62 Introduction – the challenge of vegetation complexity

63 Vegetation dynamics involves processes operating at widely different spatial and temporal scales, from 64 stomatal opening and closing (minutes to days, at leaf level) to biome shifts (decades to centuries, across 65 entire continents). Tremendous research efforts have been devoted to understanding and predicting how 66 plant processes and functional traits at the level of individuals combine to determine the structure, function 67 and dynamics of vegetation on larger scales. Because no single scientific discipline or theory deals with all 68 processes, dynamic vegetation models (DVMs) have been developed that combine elements from several 69 areas of research on plants and ecosystems – plant biogeography, biogeochemistry, plant physiology, forest 70 ecology and micrometeorology. The most well-known DVMs, dynamic global vegetation models (DGVMs), 71 have found a wide field of application including: assessments of land-atmosphere carbon, water and trace gas 72 exchanges; water resources; impacts of environmental change on plants and ecosystems; land management; 73 and feedbacks from vegetation changes to regional and global climates (Prentice and Cowling 2013, Fisher et 74 al. 2014). DVMs have also been applied on local scales for testing of ecological hypotheses, and to practical 75 questions in forest management and agriculture. All DVMs have in common that they are mechanistic, i.e. 76 based on the assumption of universally valid mechanisms (processes), which may enable them to make 77 predictions under conditions outside the range of observations.

78 Over time, DVMs became more complex as their developers strove to represent an ever-greater number of 79 processes. However, this additional complexity has rendered models dependent on the provision of values of 80 an ever-increasing number of parameters, many of which are poorly constrained by observations. This 81 tendency has created a "complexity trap", whereby apparent increases in realism are offset by decreases in 82 transparency, robustness and predictive power (Prentice et al. 2015). In the last decade some important 83 limitations of current DVMs have become apparent through strongly diverging predictions of C fluxes and 84 vegetation cover among state-of-the-art DGVMs that have stubbornly resisted resolution (Prentice et al. 2015, 85 Whitley et al. 2017, Pugh et al. 2018). Underlying reasons for these divergences include contrasting 86 representations of N uptake, water responses, and mortality (Walker et al. 2015, Huang et al. 2016, Thurner 87 et al. 2017). For example, DVMs have underestimated the ability of plants to enhance N uptake through 88 increased below-ground C allocation and at the same time overestimate changes in leaf N (Medlyn et al. 2015),

resulting in overly strong projected nutrient limitations of future C sequestration (Sulman et al. 2019). C
allocation is a key uncertainty in current DVMs (Montané et al. 2017, Xia et al. 2017) which is rooted in a lack
of consensus as to how plants and vegetation acclimate to combined water, C and N resource variations.

Plant diversity is another key challenge. The effects of diversity have recently been evaluated in DVMs using observed plant trait variation as an input (Fyllas et al. 2014, Sakschewski et al. 2016) and some have even addressed the generation and dynamics of plant diversity in some ecosystems (Langan et al. 2017, Gaillard et al. 2018). However, it remains a general challenge to predict how diversity is maintained and may change over time. Including diversity in DVMs without sufficient understanding of its mechanistic basis may further aggravate the complexity trap.

98 In summary, substantial progress has been made in understanding individual plant processes, which is used to 99 continuously enhance existing DVMs. While this improves predictions of current vegetation, the remaining 100 problem is to reliably predict dynamics in response to environmental changes. Among the wide range of 101 empirical and technical challenges linked to this problem here we focus on a particular but fundamental 102 aspect: controlling principles of the dynamics of plants and communities. We argue that general organizing 103 principles – based on natural selection and optimality, self-organization, and entropy maximization – can 104 facilitate the development of more reliable vegetation models. These ideas are not new but have been 105 explored primarily in small-scale and theoretical studies, and some are already in use in some prognostic 106 DVMs. However, their full potential for explaining vegetation dynamics has not yet been realized due to limited 107 common understanding of these concepts among empiricists, theoreticians and applied modellers. Here we 108 aim to clarify the theoretical basis, and the potential and limitations, of general organizing principles for 109 improving our understanding and ability to predict vegetation dynamics.

# 110 The concept of organizing principles

111 An organizing principle determines or constrains how components of a system, such as different plants in an 112 ecosystem or different organs of a plant, behave together. In mathematical terms, it is an additional equation 113 added to a system of equations, which allows one or more previously unknown variables in the system to be 114 determined, thus reducing the total uncertainty. Here we highlight three key principles that are valuable for 115 understanding the complexity of organisms and ecosystems and, we argue, will help vegetation models to 116 escape the complexity trap. The first is natural selection, operating primarily on individuals (genotypes) and 117 their traits but also on community composition. The second is self-organization, whereby the interactions of 118 system components (including individual plants) can lead to a predictable system structure. The third is 119 entropy maximization, a statistical selection principle which expresses the aggregated outcome of a large 120 number of underlying stochastic processes subject to a small number of system-level constraints.

# 121 Natural selection – the "missing law" for vegetation modelling

122 All persisting plant traits and behaviours must have passed the filter of natural selection. Acting on individuals 123 of a species, natural selection eliminates unfit or uncompetitive traits and trait combinations rapidly and 124 effectively. Natural selection is thus the reason why species do not possess arbitrary combinations of 125 important traits. Acting on differences between species, natural selection is a driver of population and 126 community dynamics. It generates strong relationships among traits, and correlations between traits and 127 environment, that are not mandated by physical laws alone. Therefore – and despite the underlying complex 128 interactions among organisms, communities, and ecosystems - natural selection is a key source of predictability in biological systems. This simple and powerful idea allows models to predict more and require 129 130 less input information (fewer uncertain parameters), which ultimately can improve both their predictive 131 power, and our scientific understanding of the patterns they describe. However, the operational application 132 of natural selection-based concepts to vegetation modelling is non-trivial, for several reasons.

# 133 Eco-evolutionary optimality shapes individual plants

Given that the evolution of traits and community composition are subject to natural selection for increasedfitness, the resulting trait combinations may be predictable as those maximising fitness. Optimality approaches

136 based on this principle can be seen as a shortcut to predicting evolved traits and how they vary with

environmental conditions (i.e. functional biogeography and phenotypic plasticity), without explicitly simulating the underlying evolutionary dynamics (Optimality here refers to eco-evolutionary optimality of the plants and not the *method* of optimization used to estimate model parameters). Optimality does not necessarily imply that there is an overall control mechanism (e.g. hormones) but may also result from bottom up effects, such as optimal allocation resulting from local sink and source dynamics in each organ (Thornley 1998) or coordination of processes (Chen and Reynolds 1997). Regardless of the underlying mechanisms, optimality hypotheses address the outcome of these mechanisms.

144 Optimality approaches often make use of economic concepts (Bloom 1986), expressing the fitness proxy and 145 the traits optimized in terms of costs and benefits in a common currency - usually carbon (C) (fig. 1, 146 Supplementary table 1). A key advantage of the optimality approach is that the fitness function integrates the 147 effect of all processes and does not have to be calibrated for different conditions or species. This makes it 148 suited to address complex and highly variable plant properties, such as C allocation and the pressing question 149 how plants will respond to continued increases in atmospheric CO<sub>2</sub> concentration in the presence of other 150 resource limitations. Based on the optimality hypothesis that plants minimize the combined C costs of 151 maintaining photosynthetic capacity and supporting water transport, a photosynthesis model explains a large 152 fraction of the global variation among biomes in leaf  $CO_2$  uptake properties in response to multiple 153 environmental factors using only two parameters that are common to all C<sub>3</sub> plants (Wang et al. 2017, 154 Bloomfield et al. 2019) (Fig. 2). An optimality hypothesis stating that trees maximize net biomass increment 155 and reproduction explains the interacting effects of elevated CO<sub>2</sub> and nitrogen (N) availability on tree growth 156 and allocation, as observed in Free Air Carbon Dioxide Enrichment (FACE) experiments (Franklin 2007, Franklin 157 et al. 2009) (Fig. 1). Maximization of a related fitness proxy also explained water use responses to elevated 158 CO<sub>2</sub> in FACE experiments (Schymanski et al. 2015).

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161 Figure 1. Optimality model of  $CO_2$  and N availability effects in free air  $CO_2$  enrichment (FACE) experiments. (a) The 162 hypothesis is that trees optimize canopy N (vertical dotted lines) by maximizing net C gain, G = GPP – Costs, where costs 163 are carbon costs for maintaining the canopy (respiration + leaf and root turnover). Elevated CO<sub>2</sub> increases GPP (subscript 164 e) compared to ambient CO<sub>2</sub> (subscript a), causing a potential large increase in optimal canopy N and net C gain (G<sub>eh</sub>), 165 which is not realized due to a simultaneous increase in C costs per N uptake (due to soil N limitation), resulting in smaller 166 net effect (G<sub>e</sub>). (b) Modelled versus measured CO<sub>2</sub> effects on productivity (GPP and NPP) and leaf area index (LAI) in forest 167 FACE experiments with sweetgum (ORNL), loblolly pine (Duke), poplar (Pop), and aspen. Adapted from (Franklin 2007) 168 and (Franklin et al. 2009).

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**Figure 2. CO**<sub>2</sub> **uptake parameters predicted by optimality principle.** Using uniform parameters in conjunction with a costminimizing optimality hypothesis, a theoretical model predicts the ratio of leaf-internal to ambient CO<sub>2</sub> ( $c_i/c_a$ ) – a key index of leaf-level C and water exchange – across the world's biomes (Wang et al. 2017). The inputs are growing-season temperature, vapour pressure deficit and elevation. Observations (based on leaf  $\delta^{13}$ C data) are compared with model predictions. Means and standard deviations are indicated for each biome, showing that although there is considerable unexplained variation among individual plants (grey points, r<sup>2</sup>=0.26), biome means are well predicted by the model (r<sup>2</sup>=0.73). The continuous line is the regression line (constrained through the origin); the dashed line is the 1:1 line.

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179 Despite the power of eco-evolutionary optimality approaches to explain a wide range of observed phenomena 180 (Supplementary table 1), only a few have been applied in prognostic DVMs (e.g. DGVMs), notably optimal 181 stomatal conductance (De Kauwe et al. 2015, Xu et al. 2016, Eller et al. 2018, Kennedy et al. 2019) and also 182 optimal leaf level N allocation (Xu et al. 2012). Optimal C allocation has also been addressed in a prognostic 183 DVM, however not in terms of optimal acclimation (as in Fig. 1) but as an outcome of competition between 184 different plant types, each with a fixed allocation (Weng et al. 2015). It is not straight forward to introduce 185 optimal allocation in existing DGVMs because it requires a rethinking of the structure, from a typically 186 sequential C flux from one compartment to the next to an inter-linked regulation of leaves, stem, and roots 187 based on the costs and benefits of all limiting resources. However, in addition to this real technical challenge 188 some conceptual confusion may have hampered the application of optimality in prognostic DVMs.

189 A potential argument against the optimality approach is that in a variable and fluctuating environment 190 optimality may never be reached (Fisher et al. 2015). This however rather calls for a careful analysis of the 191 appropriate temporal and spatial scale of the fitness proxies and the environmental variables and vegetation 192 responses analysed (Schymanski et al. 2015). At the leaf scale, the cost efficiency of leaf photosynthesis in 193 terms of water and C use has been used as a fitness proxy to predict regulation of stomatal conductance 194 (Medlyn et al. 2011, Manzoni et al. 2013, Dewar et al. 2018). At the whole plant scale, maximization of fitness 195 proxies related to whole plant production has been used to predict CO<sub>2</sub> uptake, root distributions (Schymanski 196 et al. 2009, Guswa 2010, Yang et al. 2016), C allocation (Franklin et al. 2012), and tree height (King 1990). By 197 also including survival in the fitness proxy, an optimality model explained broad patterns in such whole-life 198 dependent strategies and traits, such as observed spectra of growth rate, mortality, wood density, and drought 199 response in trees (Franklin et al. 2014b). Hypothetically, and in contrast to previous attempts to separate 200 ontogeny and "true" plasticity (McConnaughay and Coleman 1999), a whole plant fitness proxy could also be 201 used to model ontogeny of traits as a form of plasticity, based on the effects of increasing size on fitness costs 202 and benefits.

203 Another source of confusion is a perceived conflict between optimality and the evolutionary stable strategy 204 (ESS, the strategy, or trait values, emerging from competition among alternative strategies) (Hikosaka and 205 Anten 2012, Fisher et al. 2015). Based on game theory, it may be argued that evolution does not result in 206 optimal solutions, because the winning strategy in competition with others (the ESS) is not the same as the 207 optimal strategy in the absence of competitors. However, the conflict disappears once it is recognized that, (i) 208 optimality is defined at the individual level, and (ii) if competition plays a role for the trait in question, then its 209 impact has to be included in the definition of the environment, which otherwise would be incompletely 210 defined. Effects of competition can be included in the fitness proxy, e.g. by maximizing height growth as the 211 winning strategy under competition for light (Valentine and Mäkelä 2012), or by explicitly modelling the 212 competition for light and nutrients (King 1990, Franklin et al. 2012), water (Farrior et al. 2013), or mycorrhizal 213 N supply (Franklin et al. 2014a). Competition can have large effects on optimal behaviour. For example, 214 competition for water reduces the benefits of saving water and leads to different optimal stomatal behaviour 215 than non-competitive optimality (Wolf et al. 2016).

An important - yet still largely ignored - question is to what extent trait variation along environmental 216 217 gradients is due to phenotypic plasticity (individual acclimation) or genotypic differentiation. Traits differ in 218 this respect (Meng et al. 2015, Dong et al. 2017, Yang et al. 2018) and the difference is critical for the time 219 scale of changes, as plastic acclimation of traits is fast compared to mean-trait changes due to shifts in 220 community composition. Further, although often clumped together in empirical studies, plasticity is not 221 equivalent to intraspecific variation, because the latter may also include non-plastic variation. While plastic 222 traits acclimate to the current environment, non-plastic variation has been shaped by the whole evolutionary 223 history, which is significantly more challenging to represent and makes it precarious to predict non-plastic 224 traits from the plant's current environment. However, some inter-relationships between different traits 225 (rather than trait versus environment) may be more predictable across variable environments, as indicated by 226 trait economics spectra (Wright et al. 2004, Reich 2014, Díaz et al. 2016). These relationships can not only be 227 used to reduce the number of independent traits (degrees of freedom) in models, but also to test optimality 228 hypotheses, which can explain the mechanisms underlying the trait relationships (McMurtrie and Dewar 2011, 229 Maire et al. 2013) - and thus be used to predict how the trait relationships may vary across environments, in 230 time as well as in space.

231 Fitness-based optimality is well-defined only at individual or genotype level and predict a single strategy or 232 plant type for a given environment. However, although real communities usually consist of many coexisting 233 types, the single optimal strategy may be a good first-order approximation of the dominant plant type in a 234 given environment. For example, a model that postulates that plants optimize the proportions of leaf, stem 235 and root growth to compete with neighbours for N and C (resulting in an ESS) successfully reproduces observed 236 global distributions of primary production and the allocation of N and C to leaves, stems and roots (McNickle 237 et al. 2016). This finding suggests that maximization of individual competitiveness for resources, is a useful 238 optimality principle to explain the dominant vegetation type and traits in a given environment. Moreover, it

- may be possible to use an optimality approach to address diversity by generating a range of equally or similarly optimal strategies (Marks 2007). A key advantage of the optimality compared to alternative empirical community-mean-traits approaches, e.g. (van Bodegom et al. 2014), is that the fitness function integrates and
- thereby accounts for covariation among traits (Laughlin and Messier 2015, Clark 2016).

In summary, the theory of eco-evolutionary optimality is a powerful approach to predict plant traits as a function of environmental conditions, especially for plastic phenomena such as C and N allocation, which is a weak spot in predictive DVMs (Achat et al. 2016). There is also a considerable potential to use optimality hypotheses to better understand how and why different plant traits co-vary, and to apply them in both DVMs and empirically based frameworks to improve predictions of how traits and species distributions respond to environmental changes.

# 249 Emerging communities and functional diversity

250 Optimality concepts help in predicting a single (or dominant) strategy or plant type in a given environment, 251 but they do not predict biodiversity within a site ( $\alpha$ -diversity). For understanding vegetation dynamics, 252 functional diversity – variation in functional traits among the plants in a community – is the most relevant 253 aspect of biodiversity (Tilman et al. 1997). Natural selection drives the evolution of traits and community 254 dynamics precisely by operating on functional diversity; so the concept is fundamental for understanding 255 community dynamics in the long term. The inability of many current DVMs to realistically account for 256 functional diversity has been shown to cause underestimation of local acclimation and adaption (de Almeida 257 Castanho et al. 2016), artificial threshold behaviour (Kleidon et al. 2007, Lavorel et al. 2007), and 258 underestimation of the resilience of vegetation to environmental change (Sakschewski et al. 2016). Functional 259 trait diversity has been included as an input in a tropical forest model to improve its predictions of ecosystem 260 processes (Fyllas et al. 2014, Sakschewski et al. 2016). This approach however does not address the generation and maintenance of diversity over time. Diversity-generating approaches were pioneered in a simulation of 261 262 the large-scale biogeography of marine phytoplankton (Follows et al. 2007) and have been applied to 263 theoretical analysis of vegetation dynamics (Scheiter et al. 2013, Falster et al. 2017) and even to the prognostic 264 modeling of tropical ecosystems (aDGVM2 (Langan et al. 2017, Gaillard et al. 2018)). How best to represent 265 functional diversity in DVMs nonetheless remains an open question.

266 Functional diversity can be viewed as the outcome of two interacting effects: environmental filtering by the 267 abiotic environment determines where a plant can potentially survive (the fundamental niche), while biotic 268 interactions determine which plants can persist together (the realized niche). Environmental filtering is 269 relatively straightforward to model (Pavlick et al. 2013) but coexistence is much more difficult. One approach 270 is to more-or-less explicitly model the process of natural selection to derive trait combinations (genotypes or 271 species) corresponding to evolutionary stable strategies (ESS), i.e. an ESS-community that cannot be invaded 272 by other strategies (Hofbauer and Sigmund 1988, Falster et al. 2017). By embedding the process of natural 273 selection within models, functional diversity becomes an emergent property of ecosystems, thereby avoiding 274 the need to pre-specify trait combinations or the number of types or species within a model. This approach 275 may also provide a framework for addressing evolutionary adaptation to a changing climate (Jump and 276 Peñuelas 2005, Franks et al. 2007).

The community ESS concept provides a way to generate and test hypotheses on co-existence (mechanisms that prevent one species from out-competing another) that can be applied in predictive models. In such a model, successional processes involving size-structured competition for light and disturbance can maintain functional diversity in a plant community (Falster et al. 2017). By allowing species to differentiate along two functional trade-offs, functional diversity could be recovered despite the absence of any imposed environmental heterogeneity (Fig. 3). However, without disturbance and the process of growing from seed, diversity in this model disappears. It follows that successional processes and individual dynamics need to be included in order to maintain diversity in vegetation models; processes that are represented in recent demography-enabled DVMs (Medvigy et al. 2009, Weng et al. 2015, Fisher et al. 2018), which therefore possibly could be further developed into diversity-enabled prognostic DVMs.



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в C D A Height at maturation (m) 50 Fitness 10 2 10 0.01 0.1 10 0.01 0.1 10 0.01 0.1 10 0.01 0.1 1 1 1 1



Leaf mass per unit leaf area (kg  $m^{-2}$  )

290 Figure 3. Modelling diverse communities based on evolutionary stable strategies. By modelling reproductive success in 291 competition with existing types (white dots), ESS models estimate the fitness of potential invaders (coloured shading) 292 and use this to guide community assembly. Here species are allowed to vary in two traits, underpinned by physiological 293 trade-offs. A) Initially, a wide variety of trait combinations have positive fitness and could establish. B) Through directional 294 selection, any single species is driven towards a local evolutionary attractor. However, this single species cannot prevent 295 the invasion of other types, if regions of positive fitness occur elsewhere in trait space. C) Through repeated rounds of 296 mutation and selection, an ESS mix may be established, i.e. existing residents all have positive abundance while fitness is 297 zero or negative elsewhere. The ESS trait mixture represents a prediction for the system diversity. D) In traditional models 298 with pre-specified trait combinations, species may coexist, but are not evolutionarily stable - i.e. they could be invaded 299 if new plant types were allowed into the system. In each panel, the solid white line delimits trait combinations that are 300 not viable even in the absence of any competition (pure environmental filtering, as indicated in Panel A). In panel B, the 301 dashed white line shows the evolutionary attractors for each trait when allowed to evolve in isolation (Falster et al. 2017).

302 However, while the diversity-enabled models are advancing the science of vegetation dynamics, developing 303 them into prognostic tools pose additional challenges compared to traditional DVMs, such as the testing and 304 calibration of diversity maintaining mechanisms. In particular, the predictive ability of diversity-enabled 305 models is potentially limited by the set of traits and coexistence mechanisms that are accounted for. In 306 addition to trade-offs between costs and benefits of traits linked to resource (light) competition discussed 307 above (Falster et al. 2017) there are many mechanisms of coexistence, involving resources, natural enemies, 308 spatial heterogeneity, and temporal variability (Loreau 2010, Adler et al. 2013), making species coexistence a 309 high-dimensional problem (Clark et al. 2007). For example, complementarity – more species can use the total 310 resources more completely – has been shown to reduce competition and promote coexistence in theoretical 311 and empirical studies (Loreau 2010, Cardinale et al. 2012, Craven et al. 2018, Isbell et al. 2018) and therefore 312 deserves more attention in future applied DVMs. While explaining the basis and roles of biodiversity has long 313 been at the centre of interest among theoretical and empirical ecologists (García-Palacios et al. 2018), it is 314 now also becoming critical for DVMs.

# 315 Self-organization at the ecosystem level

While plant processes and behaviours originate at the level of individuals that are subject to natural selection and environmental constraints, the collective actions of individuals also drive patterns and processes that can provide organizing principles at the ecosystem level. For example, the collective spatial behaviour of plants gives rise to remarkable patterns in vegetation structure that provide both scientific insights, and possible ways to reduce model complexity.

#### Self-organization simplifies forest structure 321

322 In forests, the individual acclimation (plasticity) of stem angles, leading to the collective organization of crown 323 layers, is an example of self-organization at the ecosystem level. The most computationally intensive aspect 324 of many forest dynamics models is the calculation of plant light availability based on all individuals' locations 325 heights, and shapes (Moorcroft et al. 2001, Weiner et al. 2001). Despite their detail, however, these individualbased models often do not produce realistic-looking forest stands. There are too many gaps, and the emergent 326 327 "jig-saw puzzle" canopy pattern is missing. The Perfect Plasticity Approximation (PPA) was developed to 328 correct the problems of both computational intensity and unrealistic canopy. The PPA is based on the 329 observation that individuals can move their crowns horizontally towards sunlight (phototropism), which leads 330 to a simple pattern (Fig. 4): Canopy trees fill the horizontal space and there is approximately one height above 331 which individual crowns are sunlit and below which individuals are in the shade of those canopy trees (Strigul et al. 2008). There will be a single height of canopy closure, and information on the locations of stems is no 332 longer needed to calculate access to light. A rule defined at the level of individual trees (the search for sunlight) 333 334 thus leads to a simple, emergent pattern that greatly simplifies the modelling of forest stand dynamics (Purves 335 et al. 2008).

336 The PPA has also made possible the analytical ESS analysis of allocation strategies and predictions of their 337 variation across environmental gradients in temperate forests (Dybzinski et al. 2011, Farrior et al. 2013, Farrior 338 et al. 2015). Although many tropical forests exhibit a different size structure, the same individual rule of 339 phototropism, though with different growth rates for canopy trees and frequency of stand-level disturbance, 340 predicts the emergent structure of tropical stands (Farrior et al. 2016).

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#### 343

increasing precipitation

344 Figure 4. Spatial self-organization in ecosystems. A-C) Individual level phototropism leads to emergent regularity in 345 forest crown height and size. Model and forest images from above. A) A forest dynamics model without phototropism 346 (Strigul et al. 2008). B) The same forest dynamics model with individual phototropism (individuals allowed a maximum of

347 5° lean in their trunks). Brightness indicates the height of the canopy. Note with phototropism, canopy height and crown size are more regular. C) Image of a near-natural forest in the Hainich National Park, Germany. A and B redrawn from
 (Strigul et al. 2008) Figure 7, and C from (Getzin et al. 2012), Figure S1. D) Spatial self-organization in dry lands. Typical
 sequence of vegetation patterns along a rainfall gradient. Modeled (upper panels) and observed (lower panels), redrawn
 from (Meron 2016).

352

#### 353 Spatial self-organization at the landscape scale

354 Spatial self-organization is driven by feedbacks between vegetation and the environment. For example, when 355 trees establish in grasslands, they shade and suppress light-demanding grasses, competitively favoring other 356 trees and eventually stabilizing patches of forests (Favier et al. 2004). Dryland landscapes provide another 357 striking example of vegetation self-organization into regular spatial patterns (Fig. 4b) caused by positive 358 feedbacks between local vegetation growth and water transport towards the growth location, by laterally 359 extended roots, overland water flow, or soil-water diffusion (Meron 2012). That is, water transport helps 360 vegetation growth, and that growth, in turn, enhances the water transport. The emergence of these patterns 361 can be modeled in spatially continuous models, which reveal that the underlying positive feedback loop is a 362 common organizing principle for spatial patterns across different locations and systems. The spatial self-363 reorganization in response to reduced rainfall slows desertification and results in successive state transitions 364 to patterns of lower productivity (Fig. 4b), rather than in abrupt, direct collapse to bare soil (Rietkerk et al. 365 2004, Meron 2016). Vegetation patterning can also promote species coexistence and help mitigate 366 biodiversity loss (Gilad et al. 2007, Meron 2016). However, the process is missing in general prognostic DVMs, 367 perhaps due to the difficulty of representing spatial feedbacks in these spatially discrete (cell or gap-based) 368 models. This problem may be addressed in future DVMs when enhanced computational power allows 369 sufficiently high spatial resolution for explicit modeling of spatial feedbacks. Alternatively, the regularity of the 370 patterns across rainfall gradients suggests that it may be possible to find universal approximations of their 371 impacts, such as scaling relationships between fraction of vegetation cover and NPP or biomass (Glenn et al. 372 2008). Such a relationship could readily be incorporated in large-scale DGVMs or land-surface models to 373 account for the larger scale impacts of fine scale spatial feedbacks without modeling these explicitly. The idea 374 of simplification by upscaling, or aggregation is also central to another simplifying organizing principle, entropy 375 maximization- as discussed next.

# 376 Entropy maximization – making order from chaos

Ecosystems are complex systems with myriads of interacting organisms and processes, yet there are obvious 377 378 patterns in their macroscopic features. This fact echoes the situation in physics where, for example, 379 reproducible relationships among the pressure, temperature and volume of a large assembly of molecules 380 emerge from the chaos of the underlying molecular collisions. The principle of Maximum Entropy (MaxEnt (Jaynes 2003)) has proved successful in predicting those relationships from a statistical perspective, as the 381 382 most likely outcome of the underlying microscopic variables treated as random noise within the imposed 383 experimental constraints (e.g. fixed volume and temperature). MaxEnt can be applied at many scales but the 384 most interesting from the point of view of vegetation dynamics is the ecosystem scale where the aggregated 385 behaviour of large numbers of interacting individuals may to an extent be treated stochastically within the 386 limits imposed by community-level environmental constraints (e.g. community resource use = resource 387 availability). The stochasticity means that many ecosystem states (e.g. vegetation cover in a grid cell) can 388 correspond to the same resource use (constraint) and MaxEnt predicts the probability of each state based on 389 the number of ways it can be realized. Thus, in contrast to both purely mechanistic models and climate-based 390 species distribution models MaxEnt does not *ignore* stochastic factors but *accounts* for their effects.

391

#### 392 Identifying the stochastic and deterministic drivers of community assembly

MaxEnt is not a purely stochastic principle because the description of community resource use (e.g. of water or nitrogen) within the resource constraints requires some underlying biology to be modelled deterministically. MaxEnt enables us to test the assumed division between stochastic drivers (treated as random noise) and deterministic drivers, or mechanisms (treated as constraints): agreement between MaxEnt predictions and observations indicates that the correct distinction has been identified; disagreement signals
 missing constraints or mechanisms. In MaxEnt, extension to more than one resource constraint is
 straightforward.

400 An illustrative example is the use of MaxEnt to predict statistical patterns of tree-grass distribution over large 401 areas of tropical savannas across a gradient in water availability (Bertram and Dewar 2013). The key constraint 402 was assumed to be the mean annual community-scale water balance (evapotranspiration = water availability), 403 with a simple hierarchy in the water use of trees versus grasses versus bare ground. The broad agreement 404 between predictions and satellite-based data (Fig. 5) suggests that, indeed, the main deterministic driver of 405 global patterns in tree-grass distribution is mean annual water availability, and the essential biology that needs 406 to be modelled deterministically is the higher water demand of trees compared to grasses and bare ground. 407 Other processes, which include disturbances by fire and herbivory, contribute to the statistical spread of the 408 data in Fig. 5 at any given water availability, and can be treated as random noise that has no systematic effect 409 on the mean trends.

410 An important caveat here is that just as the laws of probability only predict the most likely frequency 411 distribution of heads and tails in a long run of coin tosses, and not the outcome of an individual toss, MaxEnt 412 only predicts the most likely frequency distribution of tree-grass cover fractions across many sites, and not the

- 413 tree-grass cover fractions at a given site (an individual data point in Fig. 5). The latter would require explicit
- 414 representation of, and site-specific information about, other processes such as fire history and herbivory.
- 415





Figure 5. Vegetation distributions predicted by the principle of maximum entropy (MaxEnt). Observed and modelled frequency distributions of tree, grass and bare ground cover fractions vs. mean annual water availability (*E*) in tropical savannas at a 1 km<sup>2</sup> resolution. Points: frequency histogram of satellite-based (MODIS) fractional cover estimates

- sampled from Africa, South America and Australia. Black curves (from bottom to top): 5th percentile, mean, and 95<sup>th</sup>
   percentile of the observed sample frequency histogram *vs. E.* Blue curves (from bottom to top): 5th percentile, mean,
   and 95th percentile of the modelled frequency distributions *vs. E.* Adapted from (Bertram and Dewar 2013).
- 423 In this simple example, the link between MaxEnt and the underlying biology occurs through the assumed water 424 use rates  $e_i$  of each cover type i (trees, grass, bare ground), which determine the community water use that 425 appears in the water balance constraint. MaxEnt then predicts that the cover type with the highest (lowest) 426 value of  $e_i$  dominates at high (low) water availability (Fig. 5). A natural generalisation of this approach would 427 be to replace assigned values of  $e_i$  by an eco-physiological optimality model,  $e(FT, FT_o)$ , for the dependence of 428 plant resource use on plastic acclimating traits ( $FT_o$ ) and other plant functional traits (FT). Then, at high (low) 429 resource availability MaxEnt would predict a relative abundance distribution in trait space that follows the 430 peaks (troughs) of e(FT, FT<sub>o</sub>), thus establishing a link between diversity in FT and FT<sub>o</sub> at the community level 431 and optimality at the individual level ( $FT_o$ ). Effects of climate change could also be incorporated through the 432 additional dependence of e on environmental conditions.
- MaxEnt based approaches could potentially be developed to incorporate stochastic effects on coexistence and
   in DVMs, and to identify the key deterministic drivers that generate and maintain diversity an important
   challenge for understanding long-term vegetation dynamics, as discussed below.

# 436 A roadmap for the use of organizing principles in vegetation modeling

We have demonstrated the nature and utility of three types of organizing principles in explaining and predicting different aspects of vegetation dynamics. We propose that the principles can be combined in a hierarchically structured framework for vegetation modeling, from functional traits (FTs), to species (or plant functional types), to stand structure and community composition (Fig. 6). We do not attempt to provide a complete blueprint for the development of next-generation DVMs. Instead we highlight some fundamental challenges that the organizing principles can help address, with focus on dynamics at individual to community scales.



#### 444

**Figure 6. Framework for the use of organizing principles in vegetation modelling.** Each organizing principle (circles, white text) helps predict (arrows) different vegetation properties (boxes). Natural selection drives the evolution of heritable functional traits (FTs). Phenotypic plasticity is predictable through fitness-proxy maximization (optimality). Collective selforganization among many plants results in predictable patterns of spatial structure at the stand level (e.g. due to plasticity of stems, the Perfect Plasticity Approximation -PPA). Natural selection controls community dynamics together with stochastic factors. Many different community compositions may be possible and the most likely may be predicted by entropy maximization (MaxEnt). The external environment includes abiotic factors and all other external drivers such asdisturbances.

453

#### 454 Which functional traits are most relevant?

455 In DVMs, plant species (or functional types) are defined in terms of a number of FTs, for which measured 456 values are available, and which have been observed to vary among plants and to be important for plant 457 function. Our perspective implies more precise criteria for how to select and use FTs. First, the observation 458 that only two underlying dimensions of variation explains 75% of the global variation in key FTs (Díaz et al. 459 2016) suggest a potential to reduce the number of FTs used to define species compared to most current DVMs. 460 Furthermore, we propose a shift from the traditional approach of using measurements (e.g. mean values per 461 PFT) of traits directly in models towards using traits measurements to test optimality principles and quantify 462 interrelationships that constrain trait values (Fisher et al. 2015). Plastic traits which vary with environmental 463 conditions, such as leaf:stem:root ratios, relative growth rate, and height, should not be used to define species. 464 Instead they can be predicted based on optimality approaches (as described in the section on Eco-evolutionary 465 optimality and Supplementary table 1). An efficient representation of species should be based on a few 466 functionally important FTs that are as non-plastic (heritable) as possible (Fig. 6). To establish such FTs, 467 observed trait variation and function can be analysed in new ways that separate plasticity from other sources 468 of trait variation (Niinemets et al. 2015). For example, SLA is commonly used to define species in terms of a 469 mean value although it varies strongly with environmental conditions, even within individuals (Scheepens et 470 al. 2010). To resolve this problem, SLA could be separated into a non-plastic maximal SLA and a plastic 471 component.

472 Once a set of non-plastic FTs have been identified, observed inter-relationships between them (trait 473 spectrums) can be used in two ways: (i) to constrain potential species in terms of possible (or more or less 474 probable) trait combinations to generate candidate species in model of community or (ii), they could be used 475 to calibrate and evaluate ESS approaches such as (Falster et al. 2017)) which predict such inter-trait 476 relationships.

# 477 How should vegetation structure and competition be modelled?

478 As discussed in section Self-organization at the ecosystem level, self-generating spatial structures have strong 479 effects on vegetation dynamics by both generating and reducing heterogeneity. The latter effect is used in the 480 PPA to simplify models of light competition in forest canopies, but the question is: can the PPA be applied for 481 all forest or what are its limitations? Intuitively, PPA appears well suited to low diversity canopies whereas its 482 binary light availability may lead to artificial exclusion of species with low shade tolerance in more diverse 483 communities. Or could such problems be resolved by a sufficiently high spatial resolution in the critical canopy 484 height? Similarly, while competition below ground can be readily modelled by assuming common pools of soil 485 resources for all plants in a stand, the actual spatial extent of competition for nutrients and water is not well understood despite potentially large impacts on key processes, such as root growth (Farrior 2019) water use 486 487 (Wolf et al. 2016) and whole plant growth (Franklin et al. 2012). Thus, although the representation of 488 vegetation structure and competition has been improved in recent DGVMs (Weng et al. 2015, Fisher et al. 489 2018), quantitative evaluations of the accuracy and efficiency of different approximations of vegetation 490 structure and competition are urgently needed.

# 491 How can we handle the complexity of communities?

492 As discussed in the section Emerging communities and functional diversity, DVMs have emerged recently that 493 generate communities by modeling the natural selection process (diversity-enabled DVMs, (Scheiter et al. 494 2013, Falster et al. 2017)). While the prognostic use of these innovative approaches is yet limited (Langan et 495 al. 2017, Gaillard et al. 2018), compared to traditional DGVMs they have a fundamentally improved capacity 496 to predict long-term ecosystem dynamics under climate change. This includes biome shifts and the role of 497 biodiversity for ecosystem resilience. Adding individual plasticity in addition to diversity in these models (as 498 described above) could lead to novel insights in how plasticity and community dynamics interact and influence 499 the rate of adaptation of vegetation to climate change, which is critical for projections of future vegetation

processes and carbon balance (Chevin et al. 2010, Walker et al. 2015). The need to model both individual
plasticity and community dynamics further highlighted by the observation that they sometimes drive mean
values for FTs in opposite directions along environmental gradients (Kichenin et al. 2013).

503 A critical question for the further development of community ESS approaches is if the relevant coexistence 504 mechanisms are included. An important, but often neglected, factor in this context is demographic and 505 environmental stochasticity. The MaxEnt approach has been used to account for randomness in predicting 506 community composition, i.e. the abundance of each species, using mean trait values as site level constraints 507 (Shipley et al. 2006). Potentially, a similar approach may also be applied with a (deterministic) diversity-508 enabled DVM that represents the hypothesized coexistence mechanisms and with resource availabilities as 509 additional constraints. For given resource availabilities there is stochastic variation in environmental variables 510 and plant demography (e.g. recruitment and mortality) and the DVM generates many communities with 511 different species compositions. The mechanisms incorporated in the DVM and the resource availabilities 512 influence the probability (or frequency) that a given community is generated. Based on the generated accumulated distribution of community compositions, MaxEnt is used to find the most likely community 513 514 composition. The MaxEnt model's ability to explain observed community compositions is then a measure of 515 the relevance of the hypothesized (deterministic) coexistence mechanisms, as described in the section 516 "Identifying the stochastic and deterministic drivers of community assembly".

517 In conclusion, the principles and approaches put forward here all address the same underlying key challenge 518 in the science of vegetation dynamics – how to make sense of complexity. During the initial development of 519 DVMs (1980s), very few ecologists were looking for general patterns in nature. The phrase "despairing 520 empiricism" (Prentice 1998) was coined to describe the view (still held in some circles) that such patterns do 521 not exist – implying that models will always require large numbers of parameters to be measured directly, 522 rather than predicted from underlying principles. Since then many promising but sometimes diverging 523 approaches have emerged. With the perspectives on organizing principles presented here we hope to 524 contribute to a coherent theoretical basis for explaining and predicting interactions among plants and the 525 environment. While many other strands of vegetation research not discussed here are also needed for this, 526 organizing principles are necessary for putting progress on different processes and traits into a consistent 527 framework and avoiding the "complexity trap", which is essential for a better understanding of vegetation 528 dynamics under climate change.

529

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#### 547 Competing Interests

548 The authors declare that they have no competing financial interests.

#### 549 Authors' Contributions

OF, SPH, ÅB, UD, SPH, HW, WC, ER, and ICP contributed to the outline of the paper, OF led the writing process,
RD, CEF, DF, ML, HW, ICP, KTR, ÅB and OF contributed display items or specific sections, and all authors
contributed to the final version of the paper.

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