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A CASE STUDY OF TURBULENCE IN THE

NOCTURNAL BOUNDARY LAYER DURING THE INDIAN SUMMER MONSOON

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Abstract Observations from the Cloud-Aerosol Interaction and Precipita tion Enhancement Experiment-Integrated Ground Observation Campaign

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¹² mospheric surface-layer processes and surface-layer turbulent characteristics ¹³ associated with the low-level jet (LLJ). Here, an observational case study of

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the nocturnal boundary layer is presented during the peak monsoon season 14 over Peninsular India using data collected over a single night representative 15 of the synoptic conditions of the Indian summer monsoon. Datasets based 16 on Doppler lidar and eddy-covariance are used for this purpose. The LLJ is 17 found to generate nocturnal turbulence by introducing mechanical shear at 18 higher levels within the boundary layer. Sporadic and intermittent turbulent 19 events observed during this period are closely associated with large eddies at 20 the scale of the height of the jet nose. Flux densities in the stable boundary 21 layer are observed to become non-local under the influence of the LLJ. Differ-22 ent turbulence regimes are identified, along with transitions between turbulent 23 periods and intermittency. Wavelet analysis is used to elucidate the presence 24 of large-scale eddies and associated intermittency during nocturnal periods in 25 the surface layer. Although the LLJ is a regional-scale phenomenon it has far 26 reaching consequences with regard to surface-atmosphere exchange processes. 27

Keywords Cospectral analysis · Intermittency · Low-level jet · Nocturnal
 boundary layer · Wavelet analysis

30 1 Introduction

The atmospheric boundary layer (ABL) over land becomes thinner, less 31 diffusive and stably stratified during typical nocturnal conditions due to the 32 absence of surface heating and convection, and is referred to as the nocturnal 33 boundary layer (NBL) (Stull, 1988). Generally, the NBL is considered to be 34 stable and several studies have shown that NBL turbulence is intermittent in 35 nature (Sun et al., 2002, 2004). The NBL has been traditionally classified into 36 three major regimes, namely: (i) weakly stable (Malhi, 1995; Mahrt, 1998), 37 (ii) very stable (Mahrt, 1985; Ohya et al., 1997), and (iii) intermittently 38 turbulent (Nappo, 1991; Howell and Sun, 1999; Mahrt, 1999). Turbulent 39 kinetic energy (TKE) in the NBL is generated solely through the action of 40 wind shear, in contrast to the daytime convective boundary layer (CBL) 41 where most of the TKE is associated with large-scale turbulent motions. 42 During the evening transition over land, enhanced stability extinguishes these 43 large-scale eddies and turbulence decays (Wyngaard, 2010). 44 The generation, maintenance, and decay of turbulence in the NBL is 45 a complex interplay between a range of atmospheric phenomena including 46

gravity waves (Fritts et al., 2003; Meillier et al., 2008; Viana et al., 2009; 47 Durden et al., 2013; Sorbjan and Czerwinska, 2013; Wang et al., 2013), frontal 48 activity (Mahrt, 2010; Hu et al., 2013), density currents (Blumen et al., 49 1999; Sun et al., 2002), shear-flow instabilities (Newsom and Banta, 2003), 50 wave-turbulence interaction (Finnigan, 1988; Einaudi et al., 1989; Nappo 51 et al., 2008; Román-Cascón et al., 2015) and large-scale coherent eddies (Sun, 52 2011; Sun et al., 2016). Such features have been investigated using theoretical 53 methods (Frisch et al., 1978; Xue et al., 1997; Wu and Zhang, 2008a,b) and 54 numerical simulations (Zilitinkevich et al., 2009; Zhou and Chow, 2014; Rorai 55 et al., 2014; He and Basu, 2015). Several authors have reported intermittency 56

⁵⁷ as an intrinsic feature of the NBL (Chimonas, 1993; Katul et al., 1994;
⁵⁸ Coulter and Doran, 2002; Sun et al., 2002; Acevedo and Fitzjarrald, 2003; Sun
⁵⁹ et al., 2004; Mahrt, 2014), although intermittency currently lacks a cohesive
⁶⁰ definition and is often identified from the vertical velocity field.

3

The wind field in the NBL often has a complex structure and can be 61 62 difficult to interpret. Local topography determines the wind direction in the lowest few metres, whereas the wind speed near the surface is a function 63 of friction, buoyancy, and entrainment. After sunset, the boundary layer 64 becomes more stably stratified, turbulence is reduced and a near-laminar layer 65 develops. The acceleration above this laminar layer drives a jet (Blackadar, 66 1957), resulting in detachment of the near-surface and overlying flows (Banta 67 et al., 2007; Banta, 2008). Turbulent eddies become smaller in the vertical 68 and momentum transfer takes place primarily through horizontal motion. In 69 many cases, a low-level jet (LLJ) develops during the evening and intensifies 70 over the course of night before dissipating rapidly with the onset of convection 71 after sunrise (Stull, 1988; Karipot et al., 2009), the existence of the LLJ often 72 leading to high wind shear during stable conditions. Several LLJ events over 73 south-eastern Kansas were experimentally validated during the CASES-99 74 (Cooperative Atmosphere-Surface Exchange Study 1999) field campaign, 75 which pioneered efforts to quantify the structure, evolution, and physical and 76 dynamical characteristics of the NBL (Poulos et al., 2002). 77

Processes that generate turbulence in the NBL have been investigated in 78 a number of previous studies; for example, Banta (2008) found that there 79 appears to be a strong link between turbulence within the near-surface layer 80 and the dynamics of the LLJ. He identified different turbulent regimes in 81 the NBL based on the atmospheric stability and the LLJ strength. However, 82 no previous studies have focused on nocturnal LLJs occuring during the 83 Indian summer monsoon. Several studies carried out at different locations 84 across the globe suggest that the LLJ generates and transports turbulence 85 downwards to the surface layer (Mahrt, 1999; Banta et al., 2003, 2006; Sun 86 et al., 2004; Karipot et al., 2006; Prabha et al., 2007; Bonin et al., 2015). 87 Banta et al. (2002) suggested that regions of high wind speeds within the 88 NBL are responsible for shear production of turbulence. In Prabha et al. 89 (2007, 2008), time—frequency characteristics of observed episodic bursts of 90 CO₂, TKE, and momentum when the LLJ was present indicated that eddies 91 on the scale of the height of the jet maximum were present in the surface 92 layer. Collectively, these studies indicate that the dynamics of surface-layer 93 turbulence are directly linked to the LLJ. 94

The LLJ over the Indian region is found to occur in association with 95 synoptic-scale monsoon circulations, especially during the south-west monsoon 96 season as a synoptic feature with local and regional components. However, 97 very few studies thus far have examined the LLJ in the context of the Indian 98 summer monsoon, despite the close association with larger-scale monsoon 99 dynamics. Bunker (1965) first reported the presence of large-scale LLJs during 100 the monsoon over Peninsular India on the basis of aircraft observations. 101 Subsequently, this jet was found to be predominantly westerly (Joseph and 102

Raman, 1966) and linked to the land—ocean thermal gradient (Krishnamurti 103 et al., 1976). The existence of the jet has since been considered as a salient 104 feature of the Indian summer monsoon. Findlater (1969) demonstrated that 105 the jet stream originated to the north of the Mascarene anticyclone in the 106 southern Indian Ocean. Grossman and Durran (1984) studied the interaction 107 between low-level flow observed during the Indian summer monsoon and 108 the Western Ghats mountain range to examine the possible influence of 109 complex topography on the intensification of offshore convection. Analysis by 110 Sivaramakrishnan et al. (1992) showed the importance of downward transport 111 of momentum and sensible heat during the night-time under near-neutral 112 stability. It was also shown that momentum transfer occurs in bursts, under 113 the influence of large-scale circulations during monsoon conditions while the 114 diurnal and seasonal variation of the monsoon LLJ has been studied by, e.g., 115 Ardanuy (1979); Kalapureddy et al. (2007); Nair et al. (2014). 116

NBL turbulence associated with the Indian summer monsoon jet has 117 not yet been quantified over the Indian Peninsula. The presence of different 118 scales of eddies within the NBL during the Indian summer monsoon has also 119 not been examined in a systematic manner. Moreover, to the best of our 120 knowledge, very few, if any studies, have used time-frequency analysis of the 121 LLJ during the Indian summer monsoon. The exchange of various energy and 122 mass fluxes, including TKE and the fluxes of momentum, sensible heat, CO_2 123 and water vapour between the surface layer and the boundary layer above 124 remain unexplored during the monsoon period. Integrated observations made 125 during the recent Cloud-Aerosol Interaction and Precipitation Enhancement 126 Experiment (CAIPEEX) provide a unique opportunity for investigating these 127 associations and their temporal dynamics (Prabha et al., 2011; Kulkarni 128 et al., 2012). Our study addresses these uncertainties through the following 129 objectives: (i) to explore the characteristics of turbulence in the NBL during 130 the Indian summer monsoon; and (ii) to analyze the role of the LLJ in the 131 generation and propagation of turbulence within the NBL. 132 133

¹³⁴ 2 Observations and Data Processing

The datasets used herein are based on the Cloud-Aerosol Interaction and 135 Precipitation Enhancement Experiment-Integrated Ground Observational 136 Campaign (CAIPEEX-IGOC) conducted during 2011; this was an integrated 137 observational programme established at Mahbubnagar (78°45′E, 17°4′N), 138 approximately 85 km south-west of Hyderabad, Andhra Pradesh, India (Fig. 139 1). Mahbubnagar is a tropical semi-urban station located in a semi-arid 140 environment representative of a rain-shadow region, and is situated south-east 141 of the eastern range of the Deccan Plateau on the Indian Peninsula. The field 142 programme comprised airborne and ground-based experimental campaigns 143 conducted to investigate the interaction between aerosol and clouds during 144 pre-monsoon and monsoon conditions (Prabha et al., 2011). In the airborne 145

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| _ | - | | | ** | - | ~ | |
|---|--|--|----------------|--|----------|---------|---|
| | Instrument | Model and | Altitudes | Variable | Temporal | Spatial | Accuracy |
| | | manufac- | of mea- | | reso- | reso- | |
| | | turer | sure- | | lution | lution | |
| | | | ment | | (s) | (m) | |
| | | | (m) | | | | |
| | 3-D sonic anemometer- thermometer | Wind master Pro, Gill Instru- | 6 | $ \begin{array}{c} T (K), \\ T_s (K), \\ u (m s^{-1}). \end{array} $ | 0.1 | _ | < 1.5% r.m.s |
| | | ments, Lyming- ton, UK | | $v (m s^{-1}), w (m s^{-1})$ | | | |
| | CO ₂ and H ₂ O in- frared gas analyzers | IRGA Model: LI-7500A Open Path CO ₂ /H ₂ O analyzer, Li-COR Bio- sciences, Lincoln, USA | 6 | $c \; (\mu \text{mol m}^{-3}), \\ q \; (\text{g kg}^{-1})$ | 0.1 | _ | within 1% and 2% of readings for CO_2 and H_2O measurements, respectively |
| | Doppler li- dar | Windcube 200 (prod- uct no. WLS200- 1), LEO- SPHERE, France | 100 to 2000 | $u (m s^{-1}), v (m s^{-1}), w (m s^{-1})$ | 300 | 50 | $0.1 {\rm ~m~s^{-1}}$ |

 Table 1
 List of instruments and datasets used in the present work

campaign, an instrumented aircraft was employed to collect in-situ cloud 146 data, while the ground-based campaign consisted of tower-based observations 147 plus several other thermodynamic and aerosol measurements. The dataset 148 used encompasses a 12-h period from 1800 Indian Standard Time (IST) on 149 August 15 2011 to 0600 IST on the following day. As the duration is less than 150 a day, the timing of the events is reported without reference to the date of 151 the observation. Details of the instrumentation used herein are summarized 152 in Table 1. The period selected was chosen as a representative day during 153 which monsoon convection was active over the region. The analysis focuses 154 on NBL processes and intermittent events with fluxes and TKE derived from 155 a micrometeorological dataset. 156

157

158 2.1 Micrometeorological Tower

A 20-m micrometeorological tower was installed at the measurement site, 159 located on the southern slopes of a low-lying mountain range oriented in 160 the north-west to south-easterly direction, the maximum height of the 161 mountain range does not exceed 600 m. The site was characterized by 162 non-irrigated grassland with scattered patches of low-lying shrubs. Two 163 eddy-covariance systems were mounted at 6 m and 16 m above the soil 164 surface, although data from the eddy-covariance system at 16 m was not 165 available for the study period. These systems consisted of Windmaster 166 Pro 3-D sonic anemometers—thermometers (Gill Instruments, Lymington, 167 UK) and LI-7500A open-path CO_2/H_2O analyzers (LI-COR Biosciences, 168 Lincoln, USA). Only data obtained at 6 m were used and eddy-covariance 169 sensors were sampled at 10 Hz and logged using a CR-3000 Micrologger 170 (Campbell Scientific, Logan, Utah, USA). Ambient air temperature (T in 171 K), sonic temperature (T_s in K), the water-vapour mixing ratio (q in g 172 kg^{-1}), CO₂ concentration (c in μ mol m⁻³), and zonal, meridional and 173 vertical wind velocity components $(u, v \text{ and } w, \text{ respectively; in m s}^{-1})$ were 174 used in the analysis. Raw eddy-covariance data were despiked following 175 Vickers and Mahrt (1997) and linearly detrended following Kaimal and 176 Finnigan (1994). A two-dimensional coordinate rotation was used to align 177 the coordinate frames with the mean streamlines (Kaimal and Finnigan, 1994). 178 179

180 2.2 Doppler Wind Lidar

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A Windcube 200 scanning Doppler wind lidar (LEOSPHERE, model WLS200-181 1) was installed at the experimental site, operating in the near-infrared range 182 $(1.54 \ \mu m)$ with a pulse energy of 100 μ J, a scanning cone angle of 15° and 183 speed, and a detection accuracy of 0.5 m s^{-1} and 1.5° , respectively. The 184 backscattered lidar signal is stored in an array of range gates having fixed 185 time delay, with the typical beam accumulation time being 11.8 s for all direc-186 tions. At each direction step, the lidar combines the four most recent radial 187 speeds at each height to calculate the zonal, meridional and vertical wind ve-188 locity components (u, v and w in m s⁻¹, respectively). The default threshold 189 for the carrier-to-noise ratio (CNR) is -30 dB, and the effect of the instrument 190 range on CNR measurement is filtered. The components u, v and w are mea-191 sured at 119 different levels between 100 m and 6000 m, while the horizontal 192 wind speed $(v_h \text{ in m s}^{-1})$ was calculated at each level using 193

$$v_h = \sqrt{u^2 + v^2}.\tag{1}$$

For all scan angles, u, v and w are measured along the four cardinal directions. As the full-beam rotation takes between 40 to 50 s, the time resolution of the data is irregular and ranges between 10.5 to 12.1 s, with a

 $[\]mathbf{6}$

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mean of 11.5 s; average values are stored as 5-min means. A high frequency 198 of missing values represents a key limitation of the Windcube 200 system. 199 Here, vertical velocities up to an altitude of 2000 m were used. Raw lidar 200 data were only used to examine time—height contours of the vertical velocity 201 (w). Wavelet analysis was performed on the averaged data, since a continuous 202 record of fixed temporal resolution is a requirement for frequency domain 203 decomposition. More details on the Windcube 200 lidar system, including 204 an intercomparison against radiosonde observations are reported in Ruchith 205 et al. (2014). 206

207

208 2.3 Synoptic Conditions

Synoptic conditions prevailing at the time of this experiment were inferred 209 from the ERA-Interim (European Centre for Medium-Range Weather Fore-210 casts Re-analysis) product (http://apps.ecmwf.int/datasets/data/interim-full-211 daily/). The zonal and meridional velocity components at the 850-hPa level 212 at 1200 UTC (1730 IST) on 15 August 2011 were used from this product. 213 Grid size for the wind data is $0.25^{\circ} \times 0.25^{\circ}$, while more details about the 214 ERA-Interim data can be found in Dee et al. (2011). Data visualization and 215 analysis were carried out using the Ferret software developed by the National 216 Oceanic and Atmospheric Administration — Pacific Marine Environmental 217 Laboratory. 218

219 2.4 Wavelet Analysis

Wavelet analysis has widespread applications in the Earth sciences, reflecting 220 its ability to examine the non-linear and non-stationary components of time 221 series (Lau and Weng, 1995; Torrence and Compo, 1998). A time series can 222 be simultaneously decomposed in a two-dimensional time-frequency domain 223 by this method, providing unique advantages over other time-series analysis 224 techniques, such as the frequency spectrum (Farge, 1992) or Fourier trans-225 form (Thomas and Foken, 2005). Wavelet analysis has been used previously to 226 examine ABL turbulence and associated scalar mixing (Hudgins et al., 1993; 227 Salmond, 2005; Terradellas et al., 2005; Woods and Smith, 2010; Zeri and Sá, 228 2011), and is used herein to separate the energies contained in the frequency 229 bands of a set of turbulent time series to analyze energetic interaction among 230 different scales of turbulent motion. Continuous wavelet analysis in the time-231 frequency domain (Torrence and Compo, 1998) was employed on w and v_h 232 measured by the lidar at different altitudes, as well as for fluxes obtained us-233 ing the eddy-covariance technique. 234

²³⁵ Wavelets $(\psi_0(\eta))$ are analysis functions localized in space, with the func-²³⁶ tions dilated or contracted before convolving with the signal. Continuous ²³⁷ wavelet transform of a regularly spaced time series, \mathbf{x}_n , with a timestep of $_{238}$ δt can be expressed using

$$W_n(s) = \sum_{n'=0}^{n-1} x_{n'} \psi^* [\frac{(n'-n)\delta t}{s}],$$
(2)

where, $\psi^*[(n'-n)\delta t/s]$ is the normalized complex conjugate of a scaled and translated version of $\psi_0(\eta)$. The wavelet power is defined as $|W_n(s)|^2$, and can be rewritten as $W_n(s).W_n^*(s)$, where $W_n^*(s)$ is the complex conjugate of $W_n(s)$. The Morlet wave function was used since it has found extensive application in dealing with the stable ABL (Everson et al., 1990; Qiu et al., 1995; Thomas and Foken, 2005; Prabha et al., 2007, 2008); this wave function with an angular frequency ω_0 is defined as

$$\psi_0(\eta) = \pi^{-\frac{1}{4}} \exp(i\omega_0 \eta) \exp(-\frac{\eta^2}{2}).$$
 (3)

Scales analyzed are written as fractional powers of two and are derived from the following relations (Farge, 1992; Torrence and Compo, 1998),

$$s_j = s_0 2^{j\delta j}, j = 0, 1, 2, 3....J,$$
(4)

$$J = \frac{1}{\delta j} \log_2 \frac{N \delta t}{s_0},\tag{5}$$

248 249

where s_0 and J determine the smallest and the largest resolvable temporal scales, respectively. A value of 0.5 has been used here for δj as it is the maximum value that still allows the maximum sampling rate. White noise was used as the background spectrum to check the significance of any peak appearing in $|W_n(s)|^2$.

Scale-averaged wavelet power is defined as the weighted sum of the wavelet power spectrum over the time periods in a specific band. Here, eddies have been classified into multiple scales according to their time periods and scaleaveraged wavelet power for these bands was calculated and plotted in order to compare their relative contributions to the total power.

260 2.5 Cospectral Analysis

²⁶¹ Cospectral analysis has particular utility for identifying the sources and sinks ²⁶² of scalars within the ABL (Zeri and Sá, 2011), the propagation of gravity waves

²⁶³ (Viana et al., 2009; Sorbjan and Czerwinska, 2013) and large coherent eddies

²⁶⁴ (Sun et al., 2016), as well as other coherent structures. We have investigated

²⁶⁵ the genesis and transport of turbulence through different heights within the

²⁶⁶ NBL using this technique.

The cross spectrum between two time series, $x_n(A)$ and $x_n(B)$ is defined as $G_{AB} = W_n^A(s).W_n^{B*}(s)$ where the cospectrum (*Co*) is obtained after separating the real and imaginary parts. Alternatively,

$$G_{AB} = Co - iQ, \tag{6}$$

where Q is the quadrature spectrum and Co is an alternate representation of the covariance between $x_n(A)$ and $x_n(B)$. Here, Co was calculated and plotted using different variables to explore the mutual effects of these on each other.

²⁷³ The phase difference between these two time series is defined as

$$\phi_{AB} = \tan^{-1} \frac{Q}{Co},\tag{7}$$

and used to differentiate the relative contributions of different phenomena
(e.g. gravity waves, non-linear waves, etc.) to total boundary-layer turbulence.

277 **3 Results and Discussions**

Figure 1 shows wind vectors at the 850-hPa level at 1730 IST on 15 August 278 2011, with a strong westerly flow prevalent over the measurement site on this 279 date. This is a synoptic feature of the Indian summer monsoon, and the pres-280 ence of this westerly flow indicates an active Indian summer monsoon over the 281 central Indian region during the study period. In the first part of this analysis 282 is mostly based on the data from the Windcube 200; vertical profile analyses 283 from this instrument form the context for the later analysis where microme-284 teorological tower data have been used. 285

Wave-like oscillations were observed in the horizontal wind speed at dif-286 ferent altitudes during the study period, and an LLJ was also present. These 287 oscillations become more prominent with the strengthening of the LLJ at 288 around 0000 IST. 30-min averages of u and v calculated from the lidar data 289 are plotted as functions of altitude in Figs. 2a and 2b, respectively, where a 290 zone of maximum wind speed or the 'jet nose' can be seen in the wind pro-291 file (Fig. 2a). The wind speed clearly decreases both above and below this 292 nose; such a wind profile is typical of the classic LLJ structure (Pichugina and 293 Banta, 2010). The maximum wind speed was observed at an altitude of 400 294 m from 0300 to 0330 IST, representing the nose or jet core; it can be seen 295 that the meridional velocity component was smaller than the zonal compo-296 nent (Fig. 2). The maximum value of $v = 4 \pm 1$ m s⁻¹ (Fig. 2b), and the 297 maximum value of $u = 11 \pm 1 \text{ m s}^{-1}$ (Fig. 2a) during the same time interval. 298 Wind direction remained predominantly westerly, with the wind speed at the 299 jet core remaining at 11.8 ± 1.3 m s⁻¹ during the period of observation. 300

Pichugina and Banta (2010) show that for the stable boundary layer with 301 a traditional LLJ structure having a prominent nose, as seen in our case from 302 Fig. 2, the height of the boundary layer (h) is most accurately given by the 303 height of the first significant minimum in the vertical profile of the variance of 304 the horizontal wind speed (σ_{Vh}^2 in m² s⁻²). Following this, the vertical profile of σ_{Vh}^2 was calculated from the lidar data at 10-min intervals, with several 305 306 representative profiles plotted in Fig. 3 for estimating h. The first significant 307 minimum in σ_{Vh}^2 occurs at 500 m at 1900, 0100, 0200 and 0500 IST; however, 308 minima were observed at 350 m at 2000 and 0300 IST. These two heights 309

are marked as h_A and h_B in Fig. 3. Finally, h has been approximated as the average of h_A and h_B with an error bar of half of the difference between h_A and h_B i.e. $h \approx 425 \pm 75$ m.

Such a high horizontal wind speed at the jet core, as seen from Fig. 2, introduces strong vertical shear in the atmosphere. Vertical shear in horizontal wind speed can be obtained from the lidar data (Fig. 4), using

$$S_V = \frac{dv_h}{dz},\tag{8}$$

where the maximum magnitude of this shear as shown in Fig. 4 is $\approx 0.05 \text{ s}^{-1}$. 316 Observations of u, v and w were obtained every 5 min from the lidar at all 317 measurement heights, with analyses of lidar data confined to 2000 m. Hence 318 'all heights' are representative of all available heights up to 2000 m, unless 319 stated otherwise. Note that v_h is calculated for all heights using Eq. 1, and 320 standard deviations for u and v (σ_u and σ_v , respectively) are calculated from 321 the lidar data at all heights at 30-min intervals. As the time resolution of 322 the wind lidar data is 5 min, each 30-min record contains six measurements 323 of u and v. The temporal mean of v_h ($\overline{v_h}$) was also calculated for each of 324 these 30-min periods. Finally, σ_u and σ_v are normalized by $\overline{v_h}$ (σ_{uN} and σ_{vN} , 325 respectively) at all heights for each 30-min period. These parameters ($\sigma_u/\overline{v_h}$ 326 and $\sigma_v/\overline{v_h}$ are dimensionless and indicative of the turbulence intensity, with 327 vertical profiles of these parameters plotted in Figs. 2c and 2d, respectively. 328

Mean vertical velocity (\overline{w} in m s⁻¹) during the period of our study has 329 been calculated at all vertical levels from the lidar data, with fluctuations in w330 (w') during this period calculated by subtracting \overline{w} from w. The time-height 331 contour plot of w' from the lidar is shown in Fig. 5, where Updrafts and 332 downdrafts are seen to occur in an alternating fashion. However, two strong 333 updraft events take place at 1915 and 0100 IST that are annotated by the 334 black vertical dashed lines. The occurrence of these events coincides with the 335 appearance of strong velocity shear (Fig. 4), whose presence is highlighted 336 using vertical black dashed lines in Fig. 4. 337

339 3.1 Scale-averaged Variance

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Five different periodicities were considered to represent large (128-256 min), coherent (64-128 min) and small (10-16 min) scales. Each of these scale-averaged variances acts as a measure of the energy associated with the eddies having time periods within each respective band (Fig. 6).

The appearance of a sharp peak was not observed for eddies in the frequency band at 128-256 min (Fig. 6), however, the maximum amount of scale-averaged variance was observed for the same eddies at around 0100 IST at the time when the LLJ is strengthening. Statistically significant peaks were simultaneously observed for eddies in the 64-128 min band, and an increase in power was also observed around 0300 IST for this band. For the 32-64 min band, peaks appeared later at around 0145 IST. Subsequent to this, eddies
in the 16-32 min and 10-16 min bands record peaks at 0215 and 0330 IST,
respectively. In general, peaks were observed at later times for smaller-scale
events.

The maximum magnitude of the scale-averaged variance increases with decreasing time scale, and for the 128-256 min eddies it is $0.01 \text{ m}^2 \text{ s}^{-2}$, compared to $0.06 \text{ m}^2 \text{ s}^{-2}$ for 10-16 min eddies. A six-fold increase in the magnitude of scale averaged variance was observed between the smallest and largest scales considered; for 64-128, 32-64 and 16-32 min frequency bands, maximum values were 0.02, 0.015 and $0.05 \text{ m}^2 \text{ s}^{-2}$, correspondingly.

As scale-averaged variance represents the amount of energy contained 360 in a particular band of frequencies (Torrence and Compo, 1998), this can 361 be interpreted as an example of an energy cascade from larger to smaller 362 turbulent scales (Wyngaard, 2010). Energy in the form of large-scale turbulent 363 eddies is introduced into the atmosphere by the LLJ at levels beneath the 364 jet nose. This energy is in turn transferred to smaller eddies in a process 365 analogous to the redistribution of TKE within layers between the LLJ and 366 land surface (Smedman et al., 1993). 367

Peaks appear in the 32-64 min eddies at all levels around 1830 IST (Fig. 368 6), with peaks occurring later (1930 IST) for the 16-32 min and 10-16 min 369 eddies (Fig. 6). Increases in scale-averaged variance were observed at 2030, 370 2300, 0030 and 0215 IST for the 16-32 min eddies (Fig. 6) and multiple peaks 371 were also observed for 10-16 min eddies at 2030, 2330, 0200 and 0330 IST 372 (Fig. 6). Smaller peaks were observed for 32-64 min eddies around 0000 and 373 0345 IST (Fig. 6). Such small peaks were also seen to appear in 16-32 min 374 eddies around 0030 and 0215 IST (Fig. 6). For 10-16 min eddies, peaks were 375 observed at around 0000, 0200 and 0330 IST (Fig. 6). 376

The appearance of peaks containing significant energy coincides with 377 the temporal evolution of the LLJ (Figs. 2 and 5). Strong mechanical shear 378 produced by the LLJ was present in the atmosphere during the time of 379 large-scale oscillations, i.e. when the 128-256 min and 64-128 min eddies were 380 present (Fig. 5). These large eddies are generated by several means, including 381 gentle gravity waves and/or non-linear waves, as well as passing disturbances, 382 and subsequently decay into smaller eddies at levels below the jet core. This 383 is illustrated by the cospectral plot for w at different levels below the jet core 384 (Figs. 7 and 8); w at 500 m was taken as a reference for this purpose and 385 cospectra with w at other levels are calculated. The height of this reference 386 level was chosen to be 500 m as the LLJ maximum was close to this height 387 during the observational period. Only two cospectra plots are presented, 388 namely those with w at 100 m and 450 m (Figs. 7 and 8, respectively). 389 These correspond to the levels that are closest and most distant to the 500-m 390 reference level. 391

The LLJ was observed to facilitate the downward propagation of the large-scale eddies that are present in the upper level of the boundary layer. Maximum correlation was observed for the 128-256 min and 64-128 min eddies (Fig. 7). The timing of correlation for 128-256 min eddies occurred ³⁹⁶ between 0030 - 0330 IST. For 64-128 min eddies the maximum correlation
³⁹⁷ was observed between 2330 - 0200 IST at the time when the wind shear was
³⁹⁸ strongest due to the presence of the LLJ (Fig. 4). Correlation values increase
³⁹⁹ for all time scales at 450 m. For 128-256 and 64-128 min eddies, the maximum
⁴⁰⁰ correlation occurred between 2130 - 0330 and 2330 - 0100 IST.

Wind shear is responsible for generating small scale turbulent events 401 observed at all levels. Another, weaker, wind shear event that was not related 402 to the LLJ was observed between 1930 and 2100 IST (Fig. 4), with the 403 maximum correlation observed for 16-32 min eddies around this time at both 404 100 m and 450 m (Figs. 7 and 8 respectively). This implies that smaller-scale 405 temporal events at all levels coincide with the periods of increased wind 406 shear. As outlined above, wind shear transports large-scale eddies from upper 407 levels downwards, and in turn, these large-scale eddies generate smaller-scale 408 processes in the surface layer. This also implies the presence of large-scale as 409 well as small-scale features in the lower atmosphere. 410

411

⁴¹² 3.2 Surface Fluxes and TKE

The vertical velocity w measured by the sonic anemometer at 6 m is shown 413 in Fig. 9a. Vertical kinematic fluxes of TKE ($\overline{w'e'}$ in m³ s⁻³ where e is 414 TKE) and sensible heat H ($\overline{\theta' w'}$ in K m s⁻¹) are presented in Fig. 9b, 415 with the magnitude of H fluctuating around zero during this period. This 416 is characteristic of the lack of buoyant production of turbulence during the 417 nocturnal period. Radiative cooling of the surface takes place, together with 418 the cooling of the atmospheric surface layer, which is supported by the 419 observed negative values of H (Karipot et al., 2008). 420

Turbulence was not completely absent in the surface layer as is evident 421 from the non-zero values of $\overline{w'e'}$. During most of the time, $\overline{w'e'}$ remained 422 of negligible magnitude and negative. Several occurrences of large negative 423 peaks in $\overline{w'e'}$ were observed over the study period; the first of these was 424 observed around 1900 IST when $\overline{w'e'} = -0.02 \text{ m}^3 \text{ s}^{-3}$; additionally, $\overline{w'e'}$ 425 $= -0.06 \text{ m}^3 \text{ s}^{-3}$ around 2030 IST, with $\overline{w'e'}$ remaining close to zero until 426 2200 IST. A sharp fall in its value was observed at 0000 IST when it became 427 slightly lower than $-0.07 \text{ m}^3 \text{ s}^{-3}$ before remaining close to zero for the 428 remainder of the night. The sensible heat flux was lowest at 1900 IST. The 429 magnitude of this negative peak is -0.003 K m s⁻¹, coinciding with the 430 negative peak in $\overline{w'e'}$. Another broad negative peak in H is observed during 431 2000 to 2030 IST, and closely coincides with the negative peak in $\overline{w'e'}$ at 2030 432 IST. Non-exact coincidence of the sensible heat and TKE fluxes in time may 433 occur if counter-gradient fluxes are present (Lee et al., 1996; Prabha et al., 434 2007). 435

Vertical kinematic fluxes of u and v ($\overline{u'w'}$ and $\overline{v'w'}$, respectively, in m² s⁻²) were also calculated for each 30 min from the eddy-covariance data at 6 m (Fig. 10a). The sum of both these zonal and meridional momentum

fluxes $(\overline{u'w'} + \overline{v'w'})$ is also shown. Both of these momentum fluxes showed 439 a significant increase in magnitude around 1930 IST, with absolute values 440 for both of these fluxes comparable and close to $0.10 \text{ m}^2 \text{ s}^{-2}$. Additionally, 441 another peak was observed in zonal momentum flux around 2030 IST, with 442 peaks also observed around 2300, 0000, and 0010 IST. The sum of the zonal 443 and meridional momentum fluxes registers positive peaks at 2030, 2300, 0000 444 and 0100 IST. The maximum magnitude for these peaks was $0.10 \text{ m}^2 \text{ s}^{-2}$ at 445 2030 IST followed by $\approx 0.08 \text{ m}^2 \text{ s}^{-2}$ at 0000 IST. 446

Vertical kinematic fluxes of the zonal and the meridional wind velocity 447 components ($\overline{u'w'}$ and $\overline{v'w'}$, respectively) registered large positive peaks at 448 around 1930 IST, and coincide with the occurrence of a local but strong 449 velocity shear. Subsequently, at around 0000 IST, positive and negative 450 peaks were observed in $\overline{u'w'}$ and $\overline{v'w'}$, correspondingly, appearing at around 451 the same time when very strong vertical velocity shear is generated by the 452 development of the LLJ (Fig. 4). These peaks imply a significant amount 453 of momentum exchange between the surface and the levels above. Hicks 454 et al. (2015) recently illustrated downwards transfer of momentum associated 455 with a downburst resulting in a periodic increase in wind speed at ground 456 level, attributing this to the synoptic-scale events rather than to surface 457 characteristics. In our study, however, both upwards and downwards transfer 458 of momentum occur simultaneously with strong updrafts, strengthening 459 the proposition that momentum transfer takes place in association with 460 the velocity shear in the atmosphere. Moreover, the LLJ appears to drive 461 the transfer process, as is evident from the cospectral analyses presented 462 previously (Figs. 7 and 8; Sec 3.1). This represents a classic example of the 463 top-down nature of the turbulence that exists in the presence of vertical shear 464 and in the absence of convection (Banta et al., 2003; Mahrt, 2014). 465

⁴⁶⁷ 3.3 CO₂ and Water Vapour Fluxes

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Vertical kinematic fluxes $\overline{q'w'}$ (in g m kg⁻¹ s⁻¹) and $\overline{c'w'}$ (in μ mol m⁻² s⁻¹) 468 were calculated from the eddy-covariance data at 6 m (Fig. 10b); $\overline{c'w'}$ remains 469 positive for the entire duration of the observation period, except at 2200 IST 470 when it decreased to zero. Positive peaks appear in $\overline{c'w'}$ at 1900 and 0000 471 IST (Fig. 10b) with magnitudes of 0.28 μ mol m⁻² s⁻¹ and 0.18 μ mol m⁻² 472 s^{-1} , respectively. Similarly, $\overline{q'w'}$ remained positive during the entire period 473 with positive peaks at 1930 (0.025 g m kg⁻¹ s⁻¹) and 0000 IST (0.015 g m 474 $kg^{-1} s^{-1}$). It is evident that the peaks in fluxes of momentum, sensible heat 475 and TKE, as well as CO_2 and water vapour, appear around the time when 476 non-zero vertical shear was observed in association with the LLJ (Fig. 4). 477

Peaks appearing in the vertical kinematic fluxes of CO₂ and moisture
around 1930 IST (Fig. 10b) coincide with local shear. Another set of peaks
appear simultaneously in both these fluxes around 0000 IST (Fig. 10b), again
coinciding with velocity shear related to the LLJ. Hence, mechanical shear

is seen to play an important role in vertical exchanges of moisture as well 482 as CO_2 between the surface and atmospheric levels above, enhancing the 483 upward transport of water vapour and CO_2 . During the nocturnal period, 484 production of these two variables is considered to be dominated by the 485 respiration processes of plants and the soil, while, turbulent fluxes are thought 486 to be closely correlated with the friction velocity (u_*) (Aubinet et al., 2012). 487 Hence, fluxes appearing at nighttime during low u_* conditions are commonly 488 treated as errors and filtered out. However, several authors have pointed out 489 the limitations of this approach as it seriously underestimates the pollutant 490 and water vapour fluxes at night-time that arise as a result of shear-induced 491 turbulence (Salmond et al., 2005; Prabha et al., 2008). A slightly different 492 mechanism associated with the passage of a cold front simulated by Hu et al. 493 (2013), also illustrates the importance of strong mechanical shear, resulting 494 in intermittent bursts of turbulence and the negative counter-gradient fluxes 495 of sensible heat as reported in the present study. A gravity wave event was 496 seen to generate significant amount of CO_2 and sensible heat fluxes under low 497 u_* conditions (Zeri and Sá, 2011), although, in their study, the CO₂ flux was 498 negative since the gravity wave carried CO₂-rich air downwards, in contrast to 499 the results presented here. The present study clearly indicates that mechanical 500 shear acts as a driving mechanism for fluxes in the NBL, which is otherwise 501 treated as stably stratified and weak in terms of turbulent mixing. It also 502 emphasizes the importance of understanding the dynamics of night-time fluxes 503 in order to improve currently accepted nocturnal data-filtering techniques 504 (Gu et al., 2005). 505



⁵⁰⁷ 3.4 Intermittency

The data presented for TKE and other fluxes suggest a downward transfer 508 of TKE with associated changes in the surface fluxes (Fig. 10), that coincide 509 with the occurrence of the LLJ. The presence of the intermittency is evident in 510 vertical velocity measured using the eddy-covariance technique (Fig. 9a), with 511 two clear events at 1915 and 2300 IST (Fig. 11). The scale-averaged variance 512 for 128-256 min eddies was very low and insignificant, being lower than the 513 white-noise threshold. Two broader insignificant peaks were observed for 64 514 to 128 min eddies at around 2100 and 0100 IST, while three broader and sig-515 nificant peaks were observed for 32-64 min eddies. These were of comparable 516 magnitude to one another (around $1 \times 10^{-4} \text{ m}^2 \text{ s}^{-2}$), appearing at around 517 2045, 0015 and 0245 IST. For 16-32 min eddies, multiple, sharper peaks evolved 518 at 1945, 2045, 0000, 0030, 0215 and 0315 IST, with the largest peak observed 519 at 2045 IST, with a magnitude of approximately $6 \times 10^{-4} \text{ m}^2 \text{ s}^{-2}$. In this 520 case, the magnitude of the scale-averaged variance was proportional to the 521 decreasing time scale of the eddies. There was a six-fold increase in absolute 522 values of the scale-averaged variance between the largest (64-128 min) and 523 smallest (10-16 min) eddies considered. 524

Velocity shear in the atmosphere introduces turbulent eddies in the surface layer (monitored at 6 m). As seen from observations discussed above, local velocity shear around 1900 IST resulted in an increase in the power contained within the 64-128, 32-64 and 16-32 min eddies in *w*. However, the increase in power for 64-128 min eddies was not statistically significant, suggesting that generation aloft and the downward propagation of turbulence is responsible for the genesis of these high-frequency events.

The cross-spectrum between T and w at 6 m was calculated from eddycovariance data. The phase difference (ϕ_{wT}) of 90° between w and T (Fig. 12) can be attributed to gravity waves (Stull, 1988; Lee et al., 1996; Nappo, 2012), whereas for events having larger time scales a phase difference of 180° between w and T is possibly due to non-linear waves. Additionally, for turbulent events, a phase difference of 180° between w and T is expected at smaller time scales (Barthlott et al., 2007; Prabha et al., 2007).

 ϕ_{wT} has a wide range of variation between 0° and 160° for events with 539 time scales of 256-512 min (Fig. 12), and for these events ϕ_{wT} remained close 540 to 20° between 1830 - 2300 IST, and close to 90° between 0400 to 0600 IST. 541 ϕ_{wT} fluctuated randomly between 0° to 160° for 128-256 min events, and there 542 are several instances when it attained a value close to 90°. Similarly, ϕ_{wT} is 543 equal to 90° at multiple times for the 64-128 min events, for example, ϕ_{wT} 544 approaches a value of 90° during 2000 - 2300 IST and 0130 - 0330 IST for both 545 64-128 and 32-64 min events, and alternated rapidly between 20° and 180° for 546 events with time-periods of less than 32 min. Hence, certain contributions from 547 gravity waves and non-linear waves are seen in large-scale eddies, i.e. 128-256, 548 64-128 and 32-64 min oscillations. At small scales, these waves are dominated 549 by turbulence. 550

Scale-averaged variances were also calculated for the horizontal velocity 551 component from sonic anemometer data (Fig. 13). Figure 13 shows that 128-552 256 min eddies do not show any significant peaks throughout the observation 553 period, although, significant peaks were observed for 64-128, 32-64 and 16-32 554 min eddies. For 64-128 min eddies, multiple peaks of a broader nature were 555 observed, with one such peak observed around 0030 IST, with a magnitude 556 of $\approx 5 \times 10^{-4} \text{ m}^2 \text{ s}^{-2}$. Multiple peaks were observed in 32-64 min eddies 557 at approximately at 2345, 0115 and 0400 IST; the first of these peaks had a 558 maximum value of approximately $0.01 \text{ m}^2 \text{ s}^{-2}$. For 16-32 min eddies, three 559 broader peaks were observed at approximately at 0000, 0045 and 0415 IST. 560 The first of these had a maximum value of $0.05 \text{ m}^2 \text{ s}^{-2}$. As observed for earlier 561 cases, the variance increases with the decreasing time scale of eddies (Fig. 6). 562 However, the increment in absolute values of scale-averaged variance between 563 the largest (64-128 min) and smallest (10-16 min) eddies was more than two 564 orders of magnitude (400) larger. This increment is much larger compared to 565 that of w (Fig. 11). 566

Scale-averaged variances were calculated for a 30-min time series of wmeasured at 6 m with the eddy-covariance sensors from 1930 IST onwards. Two separate time were considered in order to differentiate contributions from smaller and larger scales of eddies to the total turbulence. Eddies with time



Fig. 1 Geographical distributions of 850-hPa wind vectors (m s⁻¹) over the Indian region at 1730 IST on 15 August 2011. The arrow on top of the figure denotes the scale of the vector. The location of the measurement site is marked by a black star. Data are from the ERA-Interim dataset.

periods in the range from 0.0033 to 15 min and 15 to 30 min are clustered
together as 'turbulent' and as 'non-turbulent', respectively (Fig. 14).

574 4 Discussion

Turbulence in the atmosphere during our study period can largely be 575 attributed to mechanical shear since the thermal production of turbulence 576 is absent. Negative peaks in $\overline{w'e'}$ are observed frequently implying the 577 downward transport of turbulence (Mahrt, 1999; Banta et al., 2002). This 578 process has been suggested by Mahrt and Vickers (2002) as one of the 579 criteria for detecting cases when turbulence generated at the upper levels is 580 transported downwards. The occurrence of each of these peaks coincides with 581 the generation of strong vertical shear in the horizontal velocity. During the 582 period 1915 - 2100 IST a local velocity shear is observed up to an altitude 583



Fig. 2 Vertical variation of 30-min averages of (a) zonal velocity component (u) and (b) meridional wind component (v); and the vertical distributions of (c) standard deviation of zonal velocity component (σ_{uN} ; dimensionless) and (d) standard deviation of meridional velocity component (σ_{vN} ; dimensionless) calculated for 30-min period at hourly interval and normalized by mean horizontal wind speed. The legend shows the corresponding times in IST. Data are from the Windcube 200 lidar up to 2000 m.

of 300 m, resulting in a highly negative $\overline{w'e'}$. The appearance of the second 584 peak coincides with the development of the LLJ that starts strengthening 585 around 0000 IST and results in strong velocity shear at all levels below the jet 586 nose. At around this time, a second negative peak was observed in $\overline{w'e'}$, and 587 interestingly, this peak was more negative than the first. It can be thought of 588 as an outcome of the stronger shear induced by the LLJ. These results support 589 those of Duarte et al. (2015), where turbulence in the NBL was found out to 590 be more prominent on days with the occurrence of the LLJ, since higher wind 591 speeds lead to more intense turbulence in the NBL. Mechanical production 592 of TKE possibly occurs below the jet core (Smedman et al., 1993). The 593 maximum wind speed is observed at this height, and as a result maximum 594 shear is observed between this level and adjacent levels. TKE is transported 595 away by pressure transport to the layers above and below the LLJ (Smedman 596 et al., 1993; Berström and Smedman, 1995; Cuxart et al., 2002). However, 597 transport of TKE above the level of the LLJ remains restricted to within a 598 thin atmospheric layer (Smedman et al., 1993). The results of the cospectral 599 analysis also support this hypothesis, as significant power was observed to 600



Fig. 3 Vertical profiles of the variance of horizontal wind speed (σ_{Vh}^2) calculated for 10-min periods. Figure legend represents the corresponding times in IST. The horizontal dashed lines in black, A and B mark the heights h_A and h_B respectively. These are the heights at which the first significant minimum values in σ_{Vh}^2 are observed at different times. The average height of the boundary layer (h) during the period of our study is approximated to be the average of h_A and h_B and marked by the horizontal black dashed line C. h_A , h_B and h are marked by the vertical arrows. Data are from the Windcube 200 lidar up to 1000 m.

⁶⁰¹ be concentrated in 128-256 min and 64-128 min eddies around these times. ⁶⁰² The LLJ starts weakening after around 0400 IST, and this is reflected in the ⁶⁰³ cospectral analysis as powers concentrated in these eddies start reducing.

Variances of the zonal and the meridional velocity components normalized 604 by the mean horizontal wind speed provide qualitative estimates of the 605 mechanical turbulence (Prabha et al., 2007). Normalizing the variance in this 606 way neutralizes any effect that might significantly change the mean value, 607 making it more suitable for inter-comparisons. Figures 2c and 2d show that 608 this parameter for u and v has significant variations in the lowest 500 m of 609 the ABL under the influence of the LLJ. At upper levels, different profiles 610 calculated in the same way merge with each other and are characterized 611 by very small values. Fluctuations observed around this value are also 612 significantly lower compared to the lowest 500 m of the boundary layer. These 613 observations suggest the presence of two distinct turbulent zones above and 614



Fig. 4 Time-height contour plot of the vertical shear in the horizontal wind speed (S_V in s^{-1}) below the low-level jet. The arrows are indicative of wind speed (length of arrows) and direction. The colour bar shows the scale in s^{-1} . Two strong occurrences of the shear are marked by the vertical black dashed lines A and B which are seen to take place around 1915 IST and 0100 IST, respectively. Data are from the Windcube 200 lidar up to 500 m.



Fig. 5 Time-height contour plot of the fluctuations in vertical velocity $(w' \text{ in m s}^{-1})$ below the low-level jet. w' is calculated by subtracting the mean $w(\overline{w})$ during the 12-h period from 1800 IST on August 15 2011 to 0600 IST on the following day from w at each vertical level. The colour bar shows the scale in m s⁻¹. Two strong updrafts are seen around 1915 IST and 0100 IST which are marked by the vertical black dashed lines A and B which, respectively. Data are from the Windcube 200 lidar.

below the LLJ. Layers above the LLJ are less turbulent whereas those layers 615 below the jet are more turbulent and better-mixed. This is supported by 616 the results of Smedman et al. (1993) who concluded that the confinement 617 of mechanically-generated turbulence to within a thin layer above the LLJ 618 resulted in a well-defined maximum. It also suggests that turbulence is carried 619 downwards from the level of production to enhance the turbulence in the 620 layers below. Beyond an altitude of 1500 m, normalized velocity variances 621 show significant fluctuations at specific times; however, detailed analysis of 622



Fig. 6 Scale-averaged variances of vertical velocity (w) contained in different frequencybands at multiple heights above the land surface. Different colours in each panel correspond to different heights. The y-axis scale differs from panel to panel. Data are from the Windcube 200 lidar up to 500 m.



Fig. 7 Cospectrum (*Co*) between vertical velocity (*w*) at 100 m and 500 m. The *x* and *y* axes show the time of occurrence (IST) and the time period (T_P in min) of the oscillations, respectively. The scale on the *y*-axis is in reverse order. The colour bar shows the scale in m² s⁻². Data are from the Windcube 200 lidar.

these fluctuations remains beyond the scope and objectives of the present study.

Based on the arguments presented above, the genesis of nocturnal turbulence can be attributed principally to mechanical shear. The turbulence is generated aloft, and subsequently transported downwards. It can also be thought of in terms of as being introduced in the form of the larger turbulent motions, which gradually decay into smaller eddies. Thus, the turbulent energy is transferred from the height of the jet height to smaller turbulent scales.



Fig. 8 Cospectrum (Co) between vertical wind velocity (w) at 450 m and 500 m. The x and y axes show the time of occurrence (IST) and the time period (T_P in min) of the oscillations, respectively. The scale on the y-axis is in reverse order. The colour bar shows the scale in m² s⁻². Data are from the Windcube 200 lidar.



Fig. 9 Temporal variations of (a) fluctuation in vertical wind velocity (w) and (b) vertical kinematic fluxes of TKE $(\overline{w'e'})$ and sensible heat (H) calculated using the eddy-covariance data at a measurement height of 6 m above the surface.



Fig. 10 Temporal variations of vertical kinematic fluxes of, (a) zonal and meridional momentum, and (b) water vapour and CO_2 calculated using the eddy-covariance data at a measurement height of 6 m above the surface.



Fig. 11 Scale-averaged variances of vertical velocity (w) in different frequency bands. Time scales for the frequency bands are shown in the text boxes. Broken lines represent white noises for the corresponding frequency bands. The *y*-axis scale differs from panel to panel. Data are from the eddy-covariance measurement at 6 m.

The magnitude of the scale-averaged variance for the 'non-turbulent' eddies is statistically significant throughout the period of study (Fig. 14). It is higher than the corresponding white noise which is treated as the baseline for the comparison. However, the absolute value of the scale-averaged variance is three orders of magnitude smaller than the same for the 'turbulent' events.



Fig. 12 Phase spectrum between vertical wind (w) and ambient air temperature (T) (ϕ_{wT} in °) at 6 m. The x and y axes show the time of occurrence and the time period $(T_P \text{ in min})$ of the oscillations, respectively. The scale on the y-axis is in reverse order. The colour bar shows the scale in degrees. Data are from the eddy-covariance measurement.



Fig. 13 Scale-averaged variances of horizontal wind speed (v_h) in different frequency bands. Time scales for the frequency bands are shown in the text boxes. Broken lines represent white noises for the corresponding frequency bands. The *y*-axis scale differs from panel to panel. Data are from the eddy-covariance measurement at 6 m.

Scale-averaged variance for the turbulent eddies becomes significant around 1930 IST and reaches a value of around 0.55 m² s⁻². The findings discussed earlier support the fact that the small-scale eddies become dominant during periods of intermittent turbulence. The evolution of the intermittency can be seen to happen around this time at the surface level. This observation suggests the intermittency of turbulence at the surface results from non-turbulent waves and instabilities that were present below the core of the LLJ.

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Fig. 14 Scale-averaged variances for turbulent and non-turbulent processes for one 30minute period of vertical velocity (w) from the eddy-covariance data at 6 m above the surface.

645 5 Conclusions

We analyzed features of the nocturnal boundary layer during monsoon conditions over Peninsular India from collocated eddy-covariance, lidar and radiometer observations using wavelet and cospectral analysis. Such an analysis relating turbulence intermittency to the monsoon LLJ has not been conducted previously. Nocturnal, regional-scale jets were observed over the region and occurred in association with the large-scale monsoon flow. The genesis and propagation of turbulence in the presence of the LLJ were

⁶⁵³ investigated, with the following key findings.

Large-scale oscillations of the wind velocity are present in the NBL as
 evidenced by the results of wavelet analysis.

2. The LLJ generates mechanical shear within the layers below the jet
 height, and is responsible for the genesis of sporadic turbulence within the
 stably-stratified surface layer.

⁶⁵⁹ 3. The LLJ is associated with strong vertical shear in the horizontal velocity

and strong updrafts and downdrafts occurred below the LLJ. These events introduce smaller periodic and turbulent fluctuations into the surface layer.

4. The large eddies contained below the jet transport a significant amount of

⁶⁶³ TKE, analogous to the upside-down boundary layer described by Banta et al.

25

664 (2003).

- ⁶⁶⁶ larger eddies generated by the LLJ. These events result in the enhancement
- $_{667}$ of fluxes of heat, moisture, and CO_2 between the land surface and atmosphere.
- 668

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679 paper (http://ferret.pmel.noaa.gov/Ferret/).

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^{5.} Intermittent events observed at the surface occurred in association with the

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