

## Article (refereed) - postprint

---

Hutchins, M.G.; Bowes, M.J. 2018. **Balancing water demand needs with protection of river water quality by minimising stream residence time: an example from the Thames, UK.**

© Springer Science+Business Media B.V., part of Springer Nature 2018

This version available <http://nora.nerc.ac.uk/519471/>

NERC has developed NORA to enable users to access research outputs wholly or partially funded by NERC. Copyright and other rights for material on this site are retained by the rights owners. Users should read the terms and conditions of use of this material at <http://nora.nerc.ac.uk/policies.html#access>

**This is a post-peer-review, pre-copyedit version of an article published in *Water Resources Management*, 32 (7). 2561-2568. The final authenticated version is available online at: <https://doi.org/10.1007/s11269-018-1946-0>.**

**There may be differences between this version and the publisher's version. You are advised to consult the publisher's version if you wish to cite from this article.**

Contact CEH NORA team at  
[noraceh@ceh.ac.uk](mailto:noraceh@ceh.ac.uk)

1 **Balancing water demand needs with protection of river water quality by minimising**  
2 **stream residence time: an example from the Thames, UK.**

3  
4 M. G. Hutchins\* and M. J. Bowes

5  
6 Centre for Ecology and Hydrology, Maclean Building, Benson Lane, Crowmarsh Gifford,  
7 Wallingford, Oxfordshire OX10 8BB, UK.

8 \*corresponding author, email: mihu@ceh.ac.uk  
9  
10

11 **Abstract**

12 Freshwater resources in the River Thames basin in southern UK are faced with combined  
13 pressures of future population growth and climate change. River basin managers are seeking  
14 increasingly innovative methods to meet water demand whilst at the same time maintaining  
15 ecological status. Using a river network hydrochemical model modified to account for  
16 possible future climate and population, the paper assesses the impact on downstream water  
17 quality of changing the location of a major point of abstraction serving the city of Oxford.  
18 The rationale behind the hypothetical change, although entailing an increase in energy costs  
19 and capital expenditure, was that flows would be maintained along a sensitive stretch of river.  
20 Model results at a location a further 23 km downstream suggested that better water quality  
21 would arise from this change. The predicted improvements included a decrease in the annual  
22 frequency of low DO concentrations ( $<6 \text{ mg L}^{-1}$ ) from 8-9 days to 2-3 days and a decrease in  
23 90<sup>th</sup> percentile (summer) temperatures of  $0.6 \text{ }^{\circ}\text{C}$ . It is believed these improvements would  
24 primarily be attributable to shortening of river residence time which curtails accelerated  
25 phytoplankton growth. The overall conclusion, of relevance both for the Thames basin and  
26 elsewhere, is that water quality in a river network can be surprisingly sensitive to the location  
27 of abstractions. Changing the location of abstractions should be considered as part of a suite  
28 of measures available to river basin managers when making plans to meet future water  
29 demand.  
30

31 **1. Introduction**

32 Across the globe, freshwater resources are increasingly being threatened due to population  
33 growth and changes in climate. Likely depletion of water resources will be exacerbated by  
34 increased pollution loads and treatment costs (Wen et al., 2017). As well as potentially failing  
35 to satisfy human needs, decreasing flows/river levels have adverse impacts on aquatic  
36 habitats and biodiversity (Laize et al., 2013). The principle of environmental flows is  
37 becoming increasingly embedded in management planning and acknowledges that water  
38 abstraction must be constrained where possible such that river ecosystems are not impaired  
39 (Acreman and Ferguson, 2010). Matching water availability under conditions of escalating  
40 demand is increasingly problematic. Identifying suitable combinations of investment  
41 strategies for addressing water scarcity in ways that protect ecosystems, in addition to  
42 providing sufficient supply, is a common challenge throughout the world (Vorosmarty et al.,  
43 2010). Meeting this challenge involves complex socio-economic considerations for which  
44 analysis using dynamic models can provide valuable insights (Dadson et al., 2017).  
45

46 The Thames river basin (southern UK) illustrates many contemporary issues, facing a likely  
47 increase in population (12% for England from 2017-2041: ONS 2017) alongside increasing  
48 climatic stress. An increase in flood frequency and magnitude brought about by climate  
49 drivers is very possible (Bell et al., 2012). At the other extreme, a future downward trend in

50 low flows is likely (Prudhomme et al., 2012). Projections suggest water resources will be  
51 threatened unless water is managed more efficiently and sustainably in domestic and  
52 industrial sectors (Hutchins et al., 2017). Allied to this it is expected that the increasing river  
53 residence time arising from lower baseflow will trigger longer and more severe  
54 eutrophication episodes (Bowes et al., 2012; Hutchins et al., 2016). Water companies are  
55 seeking concerted and innovative ways of balancing future water supply with environmental  
56 requirements. Thames Water (2016) are evaluating a suite of measures such as additional  
57 reservoir capacity, water transfers, waste-water re-use and desalinisation to meet the likely  
58 shortfall. Equally, regulators are working towards coherence in water quality and water  
59 resource planning around climate adaptation.

60  
61 The present paper seeks to show how an alternative configuration of water infrastructure  
62 (abstraction and effluent locations) can, in the right circumstances, help protect river water  
63 quality whilst minimising energy usage and capital expenditure. Specifically the alternative  
64 scenario we consider maintains river flows in a stretch of the Thames passing through Oxford  
65 where rapid increases in chlorophyll concentrations are observed in most years (Bowes et al.,  
66 2012). To do this we use QUESTOR, a water flow and quality model developed for the upper  
67 Thames (Hutchins et al., 2016).

68

## 69 **2. Method**

### 70 **2.1. Study area**

71 The Thames, a river of total length 354 km has the largest catchment area wholly in England  
72 (Figure 1). In the basin, 40% of water supply comes from groundwater (predominantly  
73 Oolitic Limestone and Cretaceous Chalk aquifers). In terms of the water quality of  
74 groundwater bodies, 47% and 38% have poor quantitative and chemical status respectively  
75 (Environment Agency 2016). Whilst the majority of surface water bodies have good chemical  
76 status, only a small minority (<10%) meet good ecological status.

77

78 The upper Thames (catchment area at the town of Wallingford 3445 km<sup>2</sup>) is the focus of the  
79 present study. The upper basin receives mean annual rainfall of 744 mm (Marsh and  
80 Hannaford, 2008). It is predominantly rural despite being highly populous (the dominant land  
81 classification being arable 45%, with only 6% urban/suburban). Surface water supply is  
82 primarily from Farmoor Reservoir (with an abstraction from the river 2.9 km upstream of Site  
83 2 on Figure 1), which supplies Swindon and Oxford amongst other population centres. The  
84 Farmoor abstraction of 1.62 m<sup>3</sup>s<sup>-1</sup> effectively reduces mean flow at Wallingford (51 km  
85 downstream) by about 5%. In return, the Sewage Treatment Works (STW) effluent  
86 downstream of Oxford contributes 0.47 m<sup>3</sup>s<sup>-1</sup>. At Wallingford, ample nutrient loads sustain  
87 phytoplankton; nitrate-N and total phosphorus in recent years always exceeding 1.4 and 0.09  
88 mgL<sup>-1</sup> respectively (Bowes et al., 2012).

89

### 90 **2.2. Model description**

91 The QUESTOR model application (Hutchins et al., 2016) focuses on a stretch representing  
92 126.4 km of river channel network (comprising the River Cherwell and River Thame  
93 tributaries and the main Thames) split into 41 reaches. The model is fed by 23 tributaries and  
94 7 major STWs, and accounts for 2 abstractions and 22 weirs. The main determinands  
95 simulated are chlorophyll-a (a proxy for phytoplankton biomass), biochemical oxygen  
96 demand (BOD), dissolved oxygen (DO), inorganic phosphorus (equating to SRP, the Soluble  
97 Reactive Phosphorus fraction), organic phosphorus, nitrate, particulate organic nitrogen,  
98 ammonium, pH, temperature, flow and photosynthetically-active radiation in the water

99 column. The processes represented are aeration, BOD decay, deamination, nitrification,  
 100 denitrification, benthic oxygen demand, BOD sedimentation, phosphorus mineralisation, in  
 101 conjunction with a biological sub-model of phytoplankton (comprising growth, respiration  
 102 and death), which includes nutrient uptake and release. A mixed phytoplankton population is  
 103 assumed. The equations describing DO, BOD, temperature and chlorophyll-a are given  
 104 (Online Resource 1). Values of the Nash-Sutcliffe efficiency goodness-of-fit statistic for  
 105 model performance at Wallingford (Site 4) for a two-year period of testing against weekly  
 106 data were 0.81, 0.77, 0.13 and 0.22 for temperature, nitrate, SRP and chlorophyll-a  
 107 respectively. Further model performance statistics are shown below (Table 1) and discussed  
 108 in detail by Hutchins et al. (2016). Overestimation in SRP is predominantly attributed to  
 109 especially low flows in the Thames tributary, conditions known to promote attenuation of  
 110 phosphorus in bed sediments, which is not represented in the model. Mismatches of  
 111 chlorophyll time series are primarily arise through assuming a constant grazing rate for  
 112 phytoplankton loss. Data are insufficient to represent grazing in the model in more detail.  
 113

114 Table 1: Paired values under calibration (2009-10) and corroboration (2011-12) conditions (separated  
 115 by “;”) of NSE for daily flow, and % error in mean for temperature, DO, nitrate (NO<sub>3</sub>), soluble  
 116 reactive phosphorus (SRP) and chlorophyll-a. Values in bold are based on observed data availability  
 117 at a resolution of weekly or better. a) locations of monitoring sites 1-4 on Figure 1; b) data for  
 118 Abingdon only available in 2009

<sup>a</sup> Monitoring Site	Flow	Temp	DO	NO <sub>3</sub>	SRP	Chl-a
Newbridge (1)		<b>0.5, 5.9</b>	3.6, 13.1	<b>0.82, -5.0</b>	<b>-9.3, 6.8</b>	<b>-25.5, -9.1</b>
Eynsham (2)	<b>0.92, 0.91</b>	<b>2.2, 8.6</b>		<b>-1.3, -5.4</b>	<b>2.0, 12.7</b>	<b>-27.9, 31.4</b>
<sup>b</sup> Abingdon (3)		<b>13.4, n/a</b>	<b>-3.6, n/a</b>			<b>7.3, n/a</b>
Wallingford (4)		<b>6.1, 7.9</b>	-1.4, 3.6	<b>-4.3, -3.0</b>	<b>12.3, 24.6</b>	<b>-29.4, 1.0</b>

119

### 120 2.3. Model applications

121 The model was run for a 4 year period, based on 2009-12 weather patterns, but with  
 122 modifications made to account for changes which may occur under future climate and  
 123 population growth. Input conditions in tributaries and other influences (e.g. for N and P  
 124 concentrations) were defined by taking present day monthly mean concentrations. Thereby it  
 125 was assumed that agricultural nutrient management practice and levels of sewage treatment  
 126 would remain unchanged. Daily radiation data were provided from Little Rissington near the  
 127 River Windrush in Gloucestershire (NGR 4299 2107) by the British Atmospheric Data  
 128 Centre (MIDAS Landsat Data). To account for effects of riparian shading, direct radiation  
 129 reaching the water surface was reduced by 19% under conditions of full leaf, this reduction  
 130 equates to riparian canopy occupancy of 27%. Waylett et al. (2013) provide further details of  
 131 the procedure for quantifying shading. Representations of effects of future climate on river  
 132 flows and water temperature were guided by modelling of hydroclimatology (Prudhomme et  
 133 al., 2012) as summarised for the Thames by Hutchins et al. (2016). Focus was made on best  
 134 capturing summer conditions when river water quality is most vulnerable to deterioration. To  
 135 represent population growth, the UK Office for National Statistics previously estimated a  
 136 16% growth from the period covered by QUESTOR model testing up to 2035. To allow for  
 137 these projections the following modifications to all present-day daily values of model input  
 138 were made:

- 139 • Flow: scalar multiplier x0.8
- 140 • Water temperature: change factor +3<sup>0</sup>C
- 141 • Urbanisation: scalar multiplier x1.16 (this represents a combination of population  
 142 growth and changes in water use efficiency)

143 To meet the objectives of the paper a pair of model applications was undertaken to represent  
 144 the following scenarios (Figure 2):

- 145 1. A system with the same configuration for abstraction as occurs presently (i.e.  
 146 abstraction from the River Thames upstream of Farmoor Reservoir). “Present  
 147 Configuration (PC)”  
 148 2. A scenario whereby the volume of water currently abstracted upstream of Farmoor is  
 149 abstracted from the river further downstream near the town of Abingdon instead (Site  
 150 3) and piped back to Farmoor for storage and distribution. “Alternative Configuration  
 151 (AC)”, This Alternative Configuration (AC) scenario would avoid the reduced flows  
 152 for the 20 km stretch through Oxford, thereby reducing residence times.

153

154 **3. Results and Discussion**

155 Whilst simulated flows will differ between the scenarios from reach to reach between Sites 2  
 156 and 3, at Wallingford (Site 4) they are identical for the two configurations. In contrast, a set  
 157 of water quality indicators, representative of summer low flow periods when conditions are  
 158 most vulnerable, (Table 2) are substantially better under the alternative configuration. These  
 159 indicators are assessed in the context of regulatory standards. UKTAG (2008) cite the  
 160 Freshwater Fish Directive values for (i) 98<sup>th</sup> percentile water temperature of 21.5 C for salmonids and  
 161 28 C for cyprinids, (ii) 10<sup>th</sup> percentile DO set at 6 mg L<sup>-1</sup> (iii) a 90<sup>th</sup> percentile BOD value of 4 mg L<sup>-1</sup>  
 162 is cited as a good status target for salmonid rivers. Standards related to phytoplankton biomass are  
 163 absent in the UK. However in the USA, Dodds et al. (1998) cite summer median chlorophyll-a  
 164 concentrations above 0.03 mg L<sup>-1</sup> as being indicative of eutrophic conditions.

165

166 Table 2: Summary water quality outcomes for a set of indicators.

<b>Water quality indicator</b>	<b>1. Present Configuration</b>	<b>2. Alternative Configuration</b>
5 <sup>th</sup> percentile DO (mg/L)	6.76	7.69
1 <sup>st</sup> percentile DO (mg/L)	5.32	6.21
Days in the 4 year period with DO < 6 mg/L	33	10
90 <sup>th</sup> percentile chlorophyll-a (mg/L)	0.093	0.081
90 <sup>th</sup> percentile water temperature (°C)	25.1	24.5
90 <sup>th</sup> percentile BOD (mg/L)	3.65	2.86

167

168 Fluctuating and periodically low DO occurs throughout the summer when river flows are low  
 169 (Figure 3). These did not occur in the wet summer conditions of 2012. The number of days  
 170 with low DO are more frequent under PC than AC. The key difference for DO and other  
 171 indicators of water quality is that in the “present configuration”, when conditions become  
 172 drier in the summer, the flow rate becomes low in the 20 km stretch of the Thames passing  
 173 through Oxford (between Farmoor and Sandford where Oxford sewage effluent returns to the  
 174 Thames). These low flows provide potentially longer residence times and therefore viable  
 175 conditions for phytoplankton blooms to develop and then crash due to nutrient limitation.  
 176 Crashes generate BOD and remove DO. Lower flows and longer residence times also lead to  
 177 higher water temperatures which in turn can further lower the DO. In the “alternative  
 178 configuration” flow levels are maintained through the stretch between Farmoor and Sandford.  
 179 Consequently accelerated eutrophication and its impacts are less likely to occur, and the river  
 180 will warm up to a lesser extent.

181

182 It is apparent that the differences in DO between the two configurations by no means wholly  
 183 arise from differences in water temperature. (Figure 4). Especially in early-midsummer these  
 184 differences are driven by eutrophication impacts, corresponding more strongly to differences  
 185 in chlorophyll-a and BOD.

186

#### 187 **4. Wider Implications**

188 Abstracting from Abingdon instead of upstream of Farmoor Reservoir (for water supply to  
189 urban areas such as Oxford) may not initially seem rational from the perspective of economic  
190 and energy costs, yet the water quality downstream is predicted to be substantially better. Of  
191 particular note is the protected reduction in the incidence of DO falling below the ecological  
192 threshold of 6 mg L<sup>-1</sup>. The incidence of poor water quality is attributable to periods where  
193 flows are low in part of the river network, in this case through Oxford. The finding, that flow  
194 levels can have direct water quality and ecological implications, is of direct relevance for the  
195 pinpointing of environmental flow requirements.

196

197 Our results, identifying considerable implications arising from moving a major abstraction  
198 point, merit further discussion. Water supply in the Thames has some inherent vulnerability  
199 to climate pressures, as the storage space quoted by Thames Water (2016) is only of the order  
200 of 100 days. Of the options available to meet future shortfall, raw water transfers from wetter  
201 regions of the country have been put forward. Whilst those water transfers deemed plausible  
202 (Thames Water, 2016) have a deployable output of approximately 3 m<sup>3</sup>s<sup>-1</sup> and could greatly  
203 improve water quality as well as meeting shortfalls, adverse effects are likely. Canal or  
204 pipeline construction is complex. Transfers may introduce invasive species and will impair  
205 the natural flow regime in the upper Thames. In addition, impacts on the source water body  
206 may be detrimental.

207

208 An analysis of the differences in capital expenditure and operating costs between raw water  
209 transfer options and a re-configuration of reservoir storage outlined above is out of the scope  
210 of this paper. Nevertheless, some broad differences are noteworthy. Piping and treating  
211 Thames river water from Abingdon, which is more polluted than river water at Farmoor,  
212 would clearly incur greater overall costs than that entailed presently. In comparison however,  
213 a potential transfer from the adjacent River Severn basin would potentially be much more  
214 costly, needing to cover a far longer distance (approximately 4 times as far) and much hillier  
215 terrain (approximately 10 times the increase in altitude).

216

217 It seems that the option addressed here should be considered alongside other major water  
218 supply options when making plans to meet future water demand. We argue that such  
219 considerations should be built into strategic appraisals by river basin managers of the various  
220 options available. This is important both in basins such as the Thames, but not least in those  
221 regions throughout the world where urbanisation is predicted to proceed much more rapidly  
222 and where infrastructure is currently minimal or absent.

223

#### 224 **Acknowledgements**

225 We acknowledge support from NERC-CEH Pollution & Environmental Risk and Water  
226 Resources Science Areas. The model was supplied with and tested against hydrological data  
227 from the National River Flow Archive. Solar radiation data were accessed from British  
228 Atmospheric Data Centre.

229

#### 230 **References**

231 Acreman MC & Ferguson AJD (2010). Environmental flows and the European Water  
232 Framework Directive. *Freshwater Biology* 55, 32-48

233 Bell VA, Kay AL, Cole SJ, Jones RG, Moore RJ & Reynard NS (2012). How might climate  
234 change affect river flows across the Thames Basin? An area-wide analysis using the  
235 UKCP09 Regional Climate Model ensemble. *Journal of Hydrology* 442-443, 89-104.

236 Bowes MJ, Gozzard E, Johnson AC, Scarlett PM, Roberts C, Read DS, Armstrong LK,  
237 Harman SA & Wickham HD (2012). Spatial and temporal changes in chlorophyll-a  
238 concentrations in the River Thames basin, UK: are phosphorus concentrations  
239 beginning to limit phytoplankton biomass? *Science of the Total Environment* 426,  
240 45–55.

241 Dadson S, Hall JW, Garrick D, Sadoff C, Whittington D & Grey D (2017). Water security,  
242 risk and economic growth: insights from a dynamical systems model. *Water*  
243 *Resources Research* 53, 6425-6438.

244 Dodds WK, Jones JR & Welch EB (1998). Suggested classification of stream trophic state:  
245 distributions of temperate stream types by chlorophyll, total nitrogen and phosphorus.  
246 *Water Research* 32, 1455-1462.

247 Environment Agency (2016). Thames river basin district River Basin Management Plan. Part  
248 1.

249 Hutchins MG, Williams RJ, Prudhomme C, Bowes MJ, Brown HE, Waylett AJ &  
250 Loewenthal M (2016). Projections of future deterioration in UK river quality are  
251 hampered by climatic uncertainty under extreme conditions. *Hydrological Sciences*  
252 *Journal* 61, 2818-2833.

253 Hutchins MG, Abesser C, Prudhomme C, Elliott JA, Bloomfield JP, Mansour MM, Hitt OE,  
254 (2017). Combined impacts of future land-use and climate stressors on water resources  
255 and quality in groundwater and surface waterbodies of the upper Thames river basin,  
256 UK, *Science of the Total Environment* (submitted)

257 Laize CLR, Acreman MC, Schneider C, Dunbar MJ, Houghton-Carr HA, Florke M &  
258 Hannah DM (2013). Projected flow alteration and ecological risk for pan-European  
259 rivers. *River Research and Applications* 30, 299-314.

260 Marsh TJ, Hannaford J (2008). UK Hydrometric Register. Hydrological data UK series.,  
261 Centre for Ecology and Hydrology.

262 ONS (2017). National Population Projections: 2016-based statistical bulletin. Office for  
263 National Statistics. 26 Oct 2017.

264 Prudhomme C, Haxton T, Crooks S, Jackson C, Barkwith A, Williamson J, Kelvin J, Mackay  
265 J, Wang L, Young A & Watts G (2012). Future Flows Hydrology: an ensemble of  
266 daily river flow and monthly groundwater levels for use for climate change impact  
267 assessment across Great Britain. *Eart System Science Data Discussions* 5, 1159-1178.

268 Thames Water (2016). Draft Drought Plan October 2016 Accessed at  
269 [https://corporate.thameswater.co.uk/About-us/Our-strategies-and-plans/Our-drought-](https://corporate.thameswater.co.uk/About-us/Our-strategies-and-plans/Our-drought-plan/Drought-plan-update-2017)  
270 [plan/Drought-plan-update-2017](https://corporate.thameswater.co.uk/About-us/Our-strategies-and-plans/Our-drought-plan/Drought-plan-update-2017). Accessed on 3<sup>rd</sup> December 2017.

271 UKTAG (2008). Environmental Standards and Conditions (Phase 1). UK Technical Advisory  
272 Group of the Water Framework Directive. Final report April 2008.

273 Vörösmarty CJ, McIntyre PB, Gessner MO, Dudgeon D, Prusevich A, Green P, Glidden S,  
274 Bunn SE, Sullivan CA, Liermann CR & Davies PM (2010). Global threats to human  
275 water security and river biodiversity. *Nature*, 467, 555–561.

276 Waylett AJ, Hutchins MG, Johnson AC, Bowes MJ, Loewenthal M (2013). Physico-chemical  
277 factors alone cannot simulate phytoplankton behaviour in a lowland river. *Journal of*  
278 *Hydrology* 497: 223-233.

279 Wen Y, Schoups G, van de Giesen N (2017). Organic pollution of rivers: Combined threats  
280 of urbanization, livestock farming and global climate change. *Scientific Reports*. 7:  
281 43289.

282

283 **List of Figures**

284 **Figure 1:** Map of River Thames catchment (key locations mentioned in text: 2. Farmoor, 3.  
285 Abingdon, 4. Wallingford)

286 **Figure 2:** Schematic map (not to scale) of River Thames near Oxford indicating main  
287 locations mentioned in text and configuration of present day (PC) and alternative (AC) water  
288 abstraction scenarios

289 **Figure 3:** Flow and Dissolved Oxygen time-series representing the two scenarios at  
290 Wallingford (site 4) in the surrogate 2009-12 period

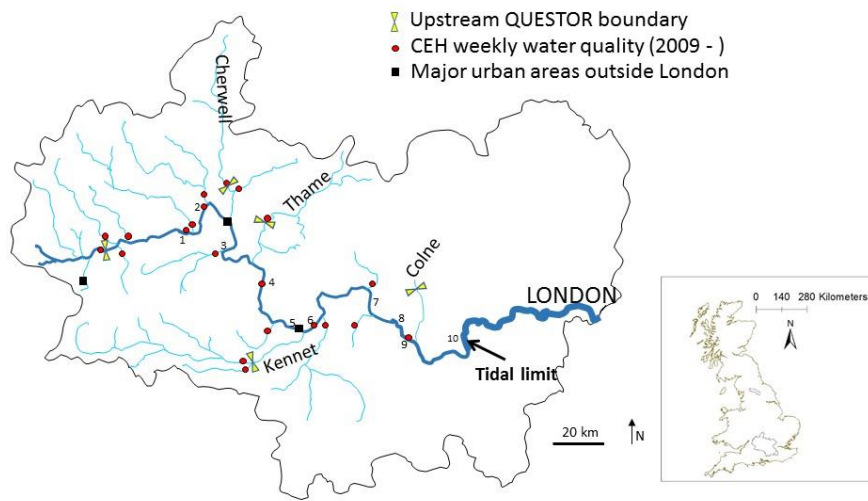
291 **Figure 4:** Time series of differences in the Alternative Configuration (AC) relative to the  
292 Present Configuration (PC); these are displayed for DO (mg/L) and Water Temperature (°C)

293

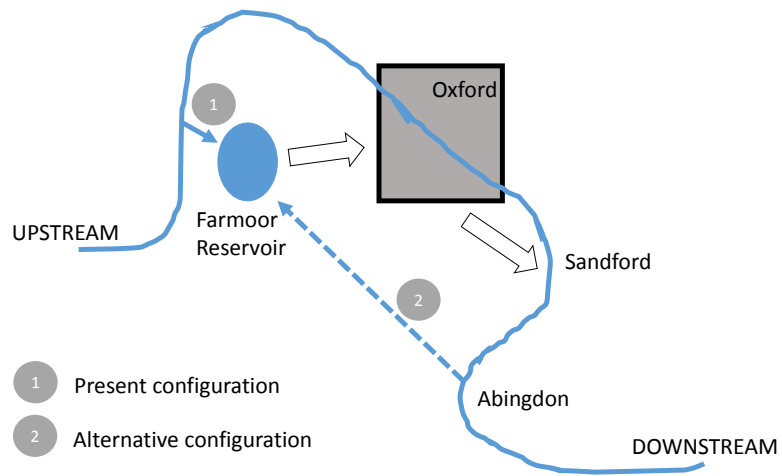
294

295

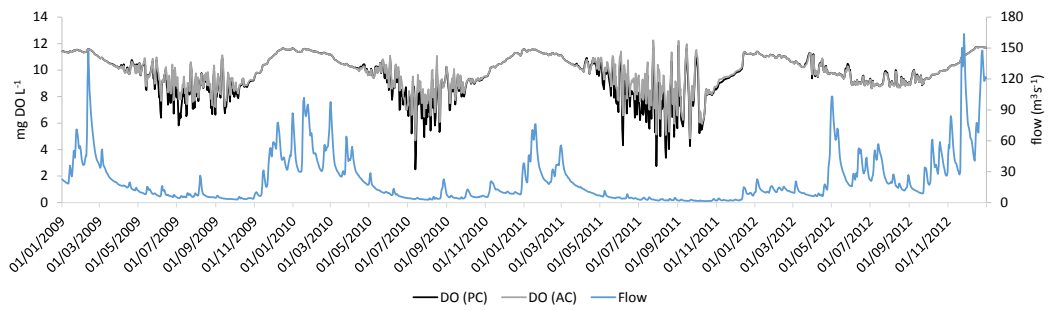




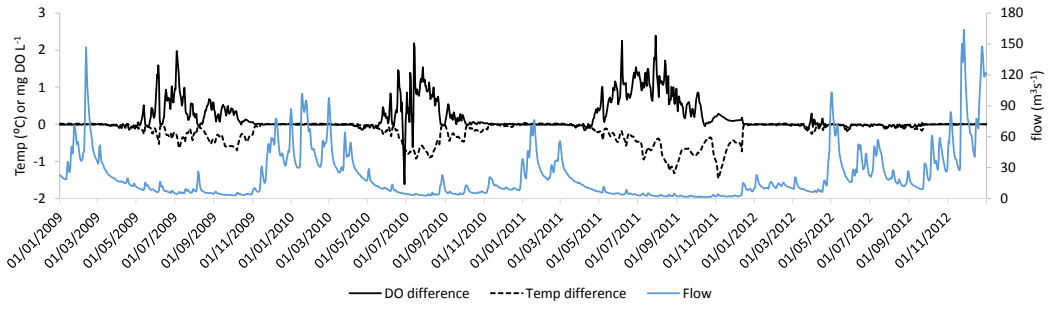
296  
 297 Figure 1  
 298



299  
300 Figure 2  
301



302  
303 Figure 3  
304



305  
306 Figure 4  
307

## 308 **Online Resource 1. Theoretical basis to QUESTOR**

309

310 QUESTOR simulates Chlorophyll-a (Phytoplankton), Biochemical Oxygen Demand (BOD),  
311 Dissolved Oxygen (DO), Inorganic (P-in, equating to soluble reactive fraction) and Organic  
312 Phosphorus, Nitrate, Particulate Organic Nitrogen, Ammonium, pH, Temperature, Flow and  
313 Photosynthetically-Active Radiation in the water column. Processes that the QUESTOR model  
314 represents are aeration, BOD Decay, Deamination, Nitrification, Denitrification, Benthic  
315 Oxygen Demand, BOD Sedimentation, P Mineralisation, in conjunction with a biological sub-  
316 model of Phytoplankton (comprising Growth, Respiration and Death), which includes nutrient  
317 uptake and release. To simulate the hydrological and chemical variables the configuration of  
318 QUESTOR as described by Boorman (2003) was used. The full sets of equations used are given  
319 elsewhere (Boorman, 2003) so only those equations directly impinging on phytoplankton and  
320 DO concentrations are given here.

321

### 322 **1. Phytoplankton model**

323

324 The growth of a mixed population of phytoplankton is modelled as described by Hutchins et  
325 al. (2010) using a fixed stoichiometry model whereby the ratio chl-a:C:N:P was 1:50:10:1.

326

327 **Equation A1:** Shows the photosynthetic rate with respect to biomass and temperature. For the  
328 Mixed Population model the calculation based on the Arrhenius equation.

329

$$330 \quad k^{pho} = Phy \cdot k_{ref}^{pho} \cdot \theta^{(T-T_{ref})} \cdot f(N) \cdot f(L) \quad [A1]$$

331

332  $k^{pho}$  = Photosynthetic rate ( $\text{day}^{-1}$ ),

333  $Phy$  = Concentration of Chl-a ( $\text{mg L}^{-1}$ )

334  $T$  = Temperature ( $^{\circ}\text{C}$ ),

335  $T_{ref}$  = 20  $^{\circ}\text{C}$

336  $f(N)$  and  $f(L)$  = limitation factors for nutrients and light, each holding values between 0 and 1

337  $\theta$  = Arrhenius factor for temperature dependencies ( $\theta = 1.08$ )

338  $k_{ref}^{pho}$  = Maximum phytoplankton growth rate ( $\text{day}^{-1}$ ) at  $T_{ref}$ .

339

340 **Equation A2:** Calculates the maximum photosynthetic rate and the limitations by nutrients,  
341 this has been taken from Michaelis Menten kinetics

342

$$343 \quad f(N) = \min\left(\frac{N}{N+k_N}, \frac{P}{P+k_P}\right) \quad [A2]$$

344

345  $N$  = Nitrate-N plus Ammonium-N ( $\text{mg L}^{-1}$ )

346  $P$  = Inorganic-P (equivalent to SRP) plus Organic-P ( $\text{mg L}^{-1}$ )

347 Where  $k_N = 0.1$  and  $k_P = 0.01 \text{ mg L}^{-1}$

348

349 **Equation A3:** Light limitation, attenuation with depth is described by the Beer-Lambert Law

350

$$351 \quad \gamma = \gamma_{base} + L_{SS} \cdot SS + L_{phy} \cdot Phy \quad [A3]$$

352

353  $\gamma_{base}$  = light extinction coefficient in clean water ( $0.01 \text{ m}^{-1}$ )

354  $SS$  = concentration of suspended sediment ( $\text{mg L}^{-1}$ )

355  $L_{SS}$  = Light attenuation with depth due to suspended sediment ( $\text{m}^{-1} \text{ mg}^{-1} \text{ L}$ )

356  $L_{phy}$  = Light attenuation with depth due to phytoplankton ( $\text{m}^{-1} \text{ mg}^{-1} \text{ L}$ )

357

358 **Equation A4:** Photolimitation with respect to phytoplankton-specific optimum intensities  
359 (Steele, 1962)

360

$$361 \quad f(L) = \frac{2.718}{\gamma d} \left[ \exp\left(\frac{R_s L_1 L_2}{L_{opt}} \cdot \exp(-\gamma d)\right) - \exp\left(\frac{R_s L_1 L_2}{L_{opt}}\right) \right] \quad [A4]$$

362

363  $\gamma d$  = Water column depth (m),

364  $R_s$  = Radiation at the surface not reflected ( $\text{W m}^{-2}$ ) (i.e. input solar radiation x 0.6)

365  $L_1$  = Fraction of incoming radiation that is visible light (0.5)

366  $L_2$  = Fraction of visible light used for phytoplankton (0.5)

367  $L_{opt}$  = Optimum light intensity for phytoplankton ( $60 \text{ W m}^{-2}$ )

368

369 **Equation A5:** Respiration

370

$$371 \quad k^{res} = P_{hy} \cdot k_{ref}^{res} \cdot k_{ref}^{pho} \cdot \theta^{(T-T_{ref})} \quad [A5]$$

372

373  $k_{ref}^{res}$  = reference respiration rate for phytoplankton ( $\text{day}^{-1}$ )

374

375 **Equation A6:** Death

376

$$377 \quad k^{death} = P_{hy} \cdot k_{ref}^{death} \cdot k_{ref}^{pho} \cdot [1 - (f(N) \cdot f(L))] \cdot \theta^{(T-T_{ref})} \quad [A6]$$

378

379  $k_{ref}^{death}$  = reference death rate for phytoplankton ( $\text{day}^{-1}$ )

380

381 Death is a combination of grazing and non-predatory mortality.

382

## 383 2. Dissolved Oxygen model

384

385 **Equation A7:** Change in Dissolved Oxygen.

386

$$387 \quad \frac{dDO}{dt} = \frac{1}{T} (DO_i - DO + W) + (P - R)$$

388

$$389 \quad - (k_{ben} DO / dep) + k_{rea} (OCS - DO) - 4.57 k_{nit} NH_4 - k_{bod} BOD \quad [A7]$$

390

391 Where:

392  $T$  = a time constant representing the average retention time in the reach. This is defined by  
393  $L/(bQ^c)$  in which  $L$  is length of reach (m),  $Q$  is flow out of reach ( $\text{m}^3\text{s}^{-1}$ ) and  $b$  and  $c$  are reach  
394 specific constants.

395  $DO$  = DO concentration leaving the reach ( $\text{mgL}^{-1}$ )

396  $DO_i$  = input DO concentration ( $\text{mgL}^{-1}$ )

397  $W$  = aerating effect of a weir as calculated from an empirical relationship based on weir type  
398 and height

399  $P = k^{pho}(133.3Phy) = \text{DO increase due to photosynthesis}$

400  $R = k^{res}(133.3Phy) = \text{DO decrease due to respiration}$

401  $k_{ben}$  = benthic respiration rate ( $\text{day}^{-1}$ )

402  $dep$  = mean water depth of reach (m)

403  $k_{bod}$  = rate of loss of DO as BOD decays ( $\text{day}^{-1}$ )

404  $k_{nit}$  = rate coefficient for complete nitrification ( $\text{day}^{-1}$ )  
 405  $NH_4$  = concentration of ammonium in water column ( $\text{mg L}^{-1}$ )  
 406  $k_{rea}$  = aeration coefficient at the water surface ( $\text{day}^{-1}$ ) (dependent on velocity, depth and  
 407 temperature)  
 408  $OCS$  = DO concentration at saturation ( $\text{mg L}^{-1}$ )  
 409

410 The amount of oxygen produced in photosynthesis (P) or consumed in respiration (R) per unit  
 411 mass of algae. For each 1 mg of chlorophyll-a 133.3 mg of oxygen are produced. This same  
 412 ratio applies for oxygen consumption in respiration, and in additions to BOD on  
 413 phytoplankton death.  
 414

### 415 **3. Biochemical oxygen demand model**

416 **Equation A8:** Change in biochemical oxygen demand:

$$417 \quad \frac{dBOD}{dt} = \frac{1}{\tau} (BOD_i - BOD) - k_{bod} BOD - \frac{(v_{sed} BOD)}{dep} + k^{death} (133.3 Phy) \quad [A8]$$

418 Where:

419  $BOD$  = BOD concentration leaving the reach ( $\text{mgL}^{-1}$ )  
 420  $BOD_i$  = input DO concentration ( $\text{mgL}^{-1}$ ) (mean from all sources)  
 421  $v_{sed}$  = settling velocity of BOD. A value of  $0.25 \text{ ms}^{-1}$  was used.  
 422

### 423 **4. River water temperature model**

424 **Equation A9:** Change in water temperature is defined as follows:

$$425 \quad \frac{dT}{dt} = \frac{1}{\tau} (T_i - T) - \frac{H(R_s - R_o)}{dep} \quad [A9]$$

427

428 Where:

429  $T_i$  = mean temperature ( $^{\circ}\text{C}$ ) from all sources  
 430  $T$  = temperature in water leaving the reach ( $^{\circ}\text{C}$ )  
 431  $R_o$  = outgoing long-wave radiation ( $\text{Wm}^{-2}$ )  
 432  $H$  = heat flux coefficient ( $0.005 \text{ m}^{-1}$ )

433 The largest component for the outgoing radiation is the long wave back radiation which is given  
 434 by

435  $R_o = 0.97 \sigma T^4$  (in which 0.97 is the emissivity constant of a water surface and  $\sigma$  is the Stefan-  
 436 Boltzman constant ( $5.67051 \cdot 10^{-8} \text{ Wm}^{-2} \text{ k}^{-4}$ ) and T is the temperature in  $^{\circ}\text{K}$ )  
 437  
 438  
 439