

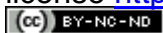
## Article (refereed) - postprint

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1 National scale evaluation of the InVEST nutrient retention model in the United Kingdom

2

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19 **Abstract**

20 A wide variety of tools aim to support decision making by modelling, mapping and quantifying  
21 ecosystem services. If decisions are to be properly informed, the accuracy and potential limitations  
22 of these tools must be well understood. However, dedicated studies evaluating ecosystem service  
23 models against empirical data are rare, especially over large areas. In this paper, we report on the  
24 national-scale assessment of a new ecosystem service model for nutrient delivery and retention, the  
25 InVEST Nutrient Delivery Ratio model. For 36 river catchments across the UK, we modelled total  
26 catchment export of phosphorus (P) and/or nitrogen (N) and compared model outputs to  
27 measurements derived from empirical water chemistry data.

28 The model performed well in terms of relative magnitude of nutrient export among catchments  
29 (best Spearman's rank correlation for N and P, respectively: 0.81 and 0.88). However, there was  
30 wide variation among catchments in the accuracy of the model, and absolute values of nutrient  
31 exports frequently showed high percentage differences between modelled and empirically-derived  
32 exports (best median absolute percentage difference for N and P, respectively:  $\pm 64\%$ ,  $\pm 44\%$ ). The  
33 model also showed a high degree of sensitivity to nutrient loads and hydrologic routing input  
34 parameters and these sensitivities varied among catchments.

35 These results suggest that the InVEST model can provide valuable information on nutrient fluxes to  
36 decision makers, especially in terms of relative differences among catchments. However, caution is  
37 needed if using the absolute modelled values for decision-making. Our study also suggests particular  
38 attention should be paid to researching input nutrient loadings and retentions, and the selection of  
39 appropriate input data resolutions and threshold flow accumulation values. Our results also  
40 highlight how availability of empirical data can improve model calibration and performance  
41 assessment and reinforce the need to include such data in ecosystem service modelling studies.

42 **Keywords**

43 Ecosystem services, nutrient delivery, runoff, eutrophication, river, land cover

44

45 **Abbreviations**

46 BRE - Beale ratio estimator, CEH-GEAR – centre for ecology and hydrology gridded estimates of areal rainfall,  
47 DEM - digital elevation model, IHDTM - integrated hydrological digital terrain model, InVEST - integrated  
48 valuation of ecosystem services and tradeoffs, LCM2007 - land cover map 2007, LULC - Land use/land cover,  
49 NDR - nutrient delivery ratio, NRFA - national river flow archive, TFA - threshold flow accumulation, UKCP09 -  
50 UK climate projections, WIMS - water information management system, WWTW - wastewater treatment  
51 works

## 52 1. Introduction

53 The ecosystem services concept is increasingly widely applied by decision makers seeking to assess  
54 the likely impacts of environmental change on human health and wellbeing (Braat and de Groot  
55 2012; Tallis et al. 2008). For ecosystem services to be useful in practice, they must be quantified and  
56 mapped to identify the risks, impacts and potential trade-offs associated with predicted or known  
57 environmental change, or among different change scenarios (Malinga et al. 2015). To achieve such  
58 assessments, a wide variety of methods and tools have been developed to map, quantify and value  
59 the provision of ecosystem services (Fisher et al. 2009; Malinga et al. 2015; Seppelt et al. 2011;  
60 Sharps et al. 2017).

61 In recent years, many ecosystem service modelling tools have become freely available to the global  
62 user community. This overcomes issues surrounding proprietary software and data formats, and  
63 enables model development and application to benefit from increased data and model sharing,  
64 cloud computing facilities and a larger user community (Feng et al. 2011). Critically, these tools  
65 model multiple services, allowing users to take a multi-criterion approach to decision-making (Keller  
66 et al. 2015). Whilst the free and open-source nature of such tools brings many advantages, it allows  
67 users to run a wide range of models, and obtain results, with little knowledge of the modelling  
68 process or expertise in the subject area. A potential pitfall is that users may not familiarise  
69 themselves with the intended use and limitations of the model before using it, and may be unaware  
70 of the uncertainty associated with results that they incorporate into decision making processes  
71 (Willcock et al. 2016). Whilst a body of literature has begun to emerge exploring the strengths and  
72 weaknesses of these models (Dennedy-Frank et al. 2016; Redhead et al. 2016; Sharps et al. 2017;  
73 Willcock et al. 2016) the number of studies seeking to validate and explore the sensitivities of  
74 ecosystem service models remains limited (Hamel et al. 2017; Maes et al. 2012; Malinga et al. 2015;  
75 Schulp et al. 2014; Seppelt et al. 2011), especially over the large (i.e. regional to national) spatial  
76 scales at which much resource management policy is formulated (e.g. Wilby et al. 2006). Such  
77 studies are vital in providing user communities with the information required to choose the tools  
78 that are most appropriate for their particular situation, to use them correctly, and to understand  
79 associated uncertainties (Willcock et al. 2016). They can also provide valuable information on  
80 potential data sources for parameterising models, and help to focus data acquisition by revealing  
81 which parameters have the most influence on model accuracy. As a result, recent reviews have  
82 identified that one of the key obstacles to successful ecosystem service mapping and  
83 implementation into decision making processes is the comparative scarcity of validation or  
84 measurements of uncertainty in many applications of ecosystem service models (Maes et al. 2012;  
85 Malinga et al. 2015; Schulp et al. 2014; Seppelt et al. 2011)

86

87 Freshwater ecosystem service models that assess how land management affects water quantity and  
88 quality have the advantage of using physical variables that are commonly used in hydrologic  
89 modelling, even though these contribute to a wide range of different final services, from recreation  
90 to human health (Keeler et al. 2012). One of the most frequently modelled services is nutrient  
91 retention, which represents the reduction in nutrient loads between sources and receiving  
92 watercourses, due to biogeochemical processes involved in nutrient transport. Models of nutrient  
93 retention (e.g. InVEST, ARIES, LUCI (Sharps et al. 2017; Vigerstol and Aukema 2011)), typically use a  
94 hydrologic module representing nutrient retention processes or, where available, direct outputs  
95 from more complex nutrient models (e.g. SWAT, RHESSys, see reviews in Breuer et al. (2008); and  
96 Shepherd et al. (1999)). When the modelling approach includes quantitative estimates of nutrient  
97 transport and retention, it becomes comparatively easier to validate models, because  
98 measurements of water chemistry are, in many countries, collected by environmental bodies and  
99 the water industry and these can be used to estimate watercourse loads for comparison with model  
100 outputs. Whilst this approach falls short of measuring a final ecosystem service (Keeler et al. 2012),  
101 it is an important step in providing the biophysical underpinning for any further assessments of  
102 ecosystem service value.

103 In this study, we use data from UK national monitoring to perform a thorough evaluation of the  
104 recently released nutrient retention tool of the Integrated Valuation of Ecosystem Services and  
105 Tradeoffs (InVEST, Sharp et al. 2016) ecosystem service modelling suite. InVEST is widely used for  
106 modelling multiple ecosystem services and considering trade-offs (e.g. Bai et al. 2013; Leh et al.  
107 2013; Nelson et al. 2009; Sánchez-Canales et al. 2012; Sharps et al. 2017) and is free and open-  
108 source. We used national scale, spatially distributed data (of the sort available to most potential  
109 users) for model inputs and performed validation against a long-term, empirically-measured dataset.  
110 Our objectives were 1) to examine the sensitivity of the model to variation in input parameter  
111 values, spatial resolution and data sources, and 2) to determine the accuracy of the model against  
112 empirical data when using the most informative combination of input parameter values, for both  
113 phosphorus (P) and nitrogen (N).

## 114 **2. Methods**

### 115 2.1. THE INVEST NUTRIENT DELIVERY RATIO MODEL

116 The InVEST (v.3.3.3) suite of tools has been developed to enable decision makers to assess trade-offs  
117 across ecosystem services and to compare the consequences of different future change scenarios,  
118 for example in land use or climate (Sharp et al. 2016). To this end, InVEST comprises a set of models

119 that cover a wide range of ecosystem services. Like many ecosystem service models, these models  
120 are based on comparatively simple production functions, enabling them to be run quickly on a  
121 standard desktop computer and to take advantage of readily available data (Sharp et al. 2016) and  
122 targeting a user community with potentially limited technical background.

123 The UK has a long history of issues arising from nutrient contamination of watercourses (Johnes et  
124 al. 1996; Withers and Lord 2002), as it is densely populated and has a large proportion of its land  
125 area under anthropogenic land uses (i.e. agricultural and urban land). This results in high levels of  
126 nutrient input to freshwater systems, and ensuing concerns over the contamination of drinking  
127 water and damage to aquatic ecosystems via eutrophication (Withers and Lord 2002). Validated  
128 nutrient export models, with clear estimates of their accuracy and uncertainty are therefore  
129 particularly valuable to compare nutrient exports under different scenarios of environmental change  
130 or management interventions over larger spatial scales (Johnes et al. 1996; Shepherd et al. 1999;  
131 Wilby et al. 2006).

132 The InVEST nutrient delivery ratio (NDR) model aims to quantify relative nutrient export and  
133 retention across different catchments or sub-catchments, and to reflect changes in nutrient  
134 export/retention under different change scenarios. The model maps the transport of nutrients from  
135 catchment sources to the stream network. It combines the advantages of nutrient transport models  
136 (e.g. SWAT (Arnold et al. 1998); RHESSys (Tague and Band 2004)), which often work at the scale of  
137 subwatersheds or hydrological units to provide quantitative estimates of nutrient flows, and index  
138 models (Drewry et al. 2011), which spatially map source risk and transport factors.

139 The model computes a nutrient mass balance that represents the long-term, steady-state flow of  
140 nutrients based on i) nutrient sources associated with different land use/land cover (LULC) in the  
141 landscape, and ii) the retention properties (e.g. LULC, slope) of pixels belonging to the same flow  
142 path (Parn et al. 2012; Sharp et al. 2016). Specifically, nutrient sources across the landscape are  
143 derived from LULC-specific nutrient application (loading) rates, which can be determined from  
144 empirical data. Nutrient sources can be divided into surface and subsurface sources (which  
145 conceptually represent sediment-bound and dissolved components, a distinction common to many  
146 nutrient transport models (Newham et al., 2004; Newham et al., 2008). The model only includes  
147 diffuse sources of nutrient; point sources are not included and need to be added in post-processing  
148 of model outputs. Next, the model uses topographic routing and an index, the NDR factor, to  
149 emulate the movement of nutrients across the landscape and into a watercourse. The NDR factor is  
150 calculated for each landscape pixel based on the properties (e.g. slope, retention coefficient) of  
151 pixels that belong to the same flow path. This empirical approach is in contrast to more complex,

152 process based models that incorporate detailed representations of nutrient cycling (see Breuer et al.  
153 2008 for a review). At the catchment outlet, the nutrient export to water is calculated as the sum of  
154 the pixel-level contributions. For further details on the model, see Supplementary Material,  
155 Appendix S1 and Sharp et al. (2016). Model source code is available in Hamel and Sharp (2017)  
156 Because of the qualitative nature of the NDR factor approach, calibration of the model is necessary  
157 to gain confidence in the quantitative outputs. The main calibration factor is the  $k_b$  parameter, which  
158 governs the relationship between the connectivity index, which is a function of topography, and the  
159 NDR factor. This relationship is further described in the user's guide (Sharp et al., 2016) and is akin to  
160 the structure of the InVEST sediment delivery ratio model (Hamel et al. 2015), which can be used  
161 independently to model this other facet of water quality.

## 162 2.2. MODEL INPUTS

163 Spatially explicit model inputs required for the NDR model are a digital elevation model (DEM), land  
164 use/land cover (LULC) raster data, nutrient runoff proxy raster data and a vector delineation of the  
165 watersheds. We used the Centre for Ecology & Hydrology's Integrated Hydrological Digital Terrain  
166 Model (CEH IHDTM, Morris and Flavin 1990) for the DEM. The IHDTM was resampled or aggregated  
167 to the required resolution (see below), filled to eliminate sinks and combined with a digital  
168 watercourse network (Moore et al. 1994) to ensure routing along known watercourses. These  
169 processes were performed in ArcMap (v10.3 © ESRI, Redlands, CA). The model also requires a  
170 threshold value for flow accumulation (TFA) to define streams, which is expressed as a number of  
171 upstream pixels. Within the model, watercourses are assumed not to retain or add to the nutrient  
172 load, and nutrients reaching a stream pixel will contribute directly to the total load from the  
173 catchment (Sharp et al. 2016). The TFA value was selected following sensitivity analyses and  
174 examination of watercourse maps (See below, section 2.3).

175 LULC data were obtained from the 25 m resolution raster version of the UK Land Cover Map 2007  
176 (LCM2007, Morton et al. 2011). The LCM2007 data are derived from satellite imagery, generalised  
177 digital cartography and image segmentation, and classify the UK land surface into 23 broad habitat  
178 classes (Jackson 2000; Morton et al. 2011). The InVEST model requires several parameter values for  
179 each distinct LULC class. These include the nutrient load applied to the land ( $\text{kg ha}^{-1}\text{y}^{-1}$ ), the  
180 proportional retention of that nutrient load, the length of flow path required to achieve that  
181 retention (in metres), and the proportion of the nutrient load that travels via subsurface flow. This  
182 last variable is set to zero by default, making the assumption that all nutrients travel via surface or  
183 shallow subsurface flow. However, if modified, the model then requires two further parameters –  
184 the subsurface nutrient retention efficiency and the flow length required to achieve this.

185 Nutrient loading and nutrient retention coefficients for each LULC class were obtained by performing  
186 an extensive literature search for values relevant to the UK and for habitats that most closely  
187 matched the broad habitats defined by the LCM2007 (Supplementary Material, Table S1). Where  
188 several possible values for a single LULC class were found, the median value was used. A wide variety  
189 of sources provided information on P (Dillon and Kirchner 1975; Fozzard et al. 1999; Johnes 1996;  
190 May et al. 2001; May et al. 1996; McGuckin et al. 1999; Smith et al. 2005) with rather fewer  
191 supplying suitable values for N (Johnes 1996; Shi et al. 2006). Because many of these publications  
192 report measured or estimated export coefficients from land to water, which are a function of the  
193 two required model inputs (load to land and retention), some loads were estimated from export  
194 coefficients according to the following formula (Sharp et al. 2016):

$$195 \quad \text{Load to land} = \frac{\text{Export from land}}{1 - \text{Retention}}$$

196 Critical flow length (i.e. the distance of travel required to achieve the nutrient retention coefficient)  
197 was set to the resolution of the input LULC raster across all LULC classes, catchments and nutrients,  
198 which is consistent with the relatively coarse resolution (25m at the minimum).

199 Previous studies have shown that choice of input data can have major impacts on the accuracy of  
200 InVEST ecosystem service models where these data relate to parameters to which the model is  
201 highly sensitive (Hamel and Guswa 2015; Pessacq et al. 2015; Redhead et al. 2016; Sánchez-Canales  
202 et al. 2012). We compared three sets of input data for the nutrient runoff proxy raster. These were,  
203 1) WorldClim precipitation data (Hijmans et al. 2005), which are readily available, widely used and  
204 have global coverage interpolated to approximately 1km resolution 2) UK Met Office UKCP09 data at  
205 5km resolution (Jenkins et al. 2008; Perry and Hollis 2005), which gave good estimates of total  
206 annual water yield when used in the relevant InVEST model (Redhead et al. 2016), and 3) CEH-GEAR  
207 data at 1km resolution (Tanguy et al. 2014), which has a higher spatial resolution. All datasets  
208 comprise gridded rainfall per raster cell at monthly or annual time steps, derived from interpolation  
209 and correction for geographic and topographic factors of measurements taken from a national  
210 network of meteorological stations. Data were derived from the mean of annual values between  
211 2000 and 2012 to match the period of the validation data. We also tested a randomised dataset  
212 using values drawn from the range of all three datasets to test the impact of large errors in the  
213 nutrient runoff proxy raster on model accuracy.

### 214 2.3. SENSITIVITY ANALYSIS

215 As well as varying input datasets for the nutrient runoff proxy raster we also tested the sensitivity of  
216 the model to changes in the values of the input parameters. This is key to understanding why the



217 model behaves as it does, setting appropriate ranges for calibration of parameter values and helping  
218 subsequent users to identifying those parameters for which it is most worthwhile investing in to  
219 obtain more accurate data. To do this, first we ran the model on “hypothetical” versions of our test  
220 catchments, with the UKCP09 precipitation data, default values for threshold flow accumulation and  
221  $k_b$  parameter (TFA = 1000 and  $k_b$  = 2, respectively), input LULC and DEM raster resolution of 25m and  
222 a single land cover class with a mean nutrient load to land ( $4.7 \text{ kg ha}^{-1}\text{y}^{-1}$ ) and retention (0.3)  
223 (because the model has the same structure, these analyses are valid for N and P). We then varied  
224 each of the precipitation data, nutrient load and nutrient retention by  $\pm 50\%$  and  $\pm 90\%$  and examined  
225 the percentage difference in modelled nutrient export to water. These values were chosen because  
226 the percentage difference between the median and maximum/minimum export coefficients was  
227 approximately 100%, so these variations explore the likely range of variation encountered when  
228 using literature derived coefficients.

229 For the single-value parameters (TFA and  $k_b$ ) we explored a range of values. We tested three TFA  
230 values (100, 1,000 and 10,000). We used these three values because preliminary analyses  
231 determined that more subtle variations in TFA made very little difference to the overall length of  
232 stream network, especially in larger catchments. Preliminary analyses also determined that values  
233 below 100 were very likely to overestimate the stream network density, whilst values above 10,000  
234 were not met in all catchments (i.e. no modelled watercourses were created). Because the ideal TFA  
235 value was catchment specific (see Results, section 3.1), we also used another approach, which  
236 involved setting the threshold either at default (1000) or high (10,000) but combining known  
237 watercourses into the LULC raster as a separate class with appropriately low retention. We used the  
238 same digital watercourse network to do this as was used to correct the flow paths generated from  
239 the DEM (Moore et al. 1994). For  $k_b$  we compared values of 0.5, 1, 2 (the default), 4, 8 and 16.  
240 Preliminary analyses determined that, whilst  $k_b$  is dimensionless and can in principle accept any  
241 value, values above this range made progressively less differences to the relationship between  
242 topography and nutrient delivery, whilst values below this range tend to collapse the function to the  
243 point where extreme changes in connectivity are required to impact on nutrient delivery. In all  
244 model runs we assumed a subsurface flow proportion of zero (i.e. all nutrient transported via  
245 surface flow).

246 Because the spatial scale and resolution of the input data can affect ecosystem service model  
247 outputs (Sharp et al. 2016), especially those with a dynamic flow component (Grafius et al. 2016), we  
248 also compared models run with versions of the LCM2007 and IHDTM at the highest resolution  
249 available (25m, the resolution of the raster LCM2007), and at lower resolutions that could easily be  
250 derived from these data (50m, the resolution of the IHDTM, 100, 200, 400 and 800 m.) Coarser

251 resolutions greatly speed up the modelling but potentially reduce accuracy. When changing the  
252 resolution of the input rasters, TFA was adjusted to keep the flow path length consistent across  
253 raster resolutions, following Hamel et al. (2017). Coarser inputs than 800m were not tested, as at  
254 values above this some smaller catchments begin to have flow paths of only 1 or 2 cells, making  
255 setting an appropriate TFA impossible.

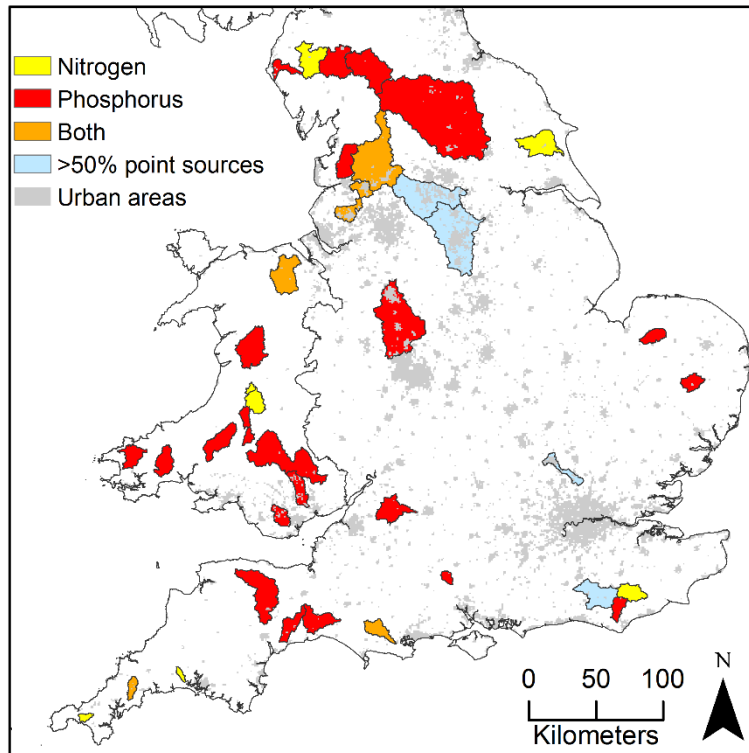
#### 256 2.4. VALIDATION DATA

257 The data used for validation were derived from the UK Environment Agency's Water Information  
258 Management System (WIMS), which provides records of total N and total P concentrations for a  
259 network of sampling points across England and Wales (Environment Agency 2017). Because these  
260 data represent instantaneous concentrations of nutrients, it was necessary to find sites with  
261 coincident records of river flow, and sufficiently frequent measurements of nutrient concentrations  
262 to enable the robust estimation of total annual nutrient load in the watercourse – comparable with  
263 the output of the NDR model – and to account for inter- and intra- annual variation. To achieve this,  
264 sites from WIMS were filtered to exclude sites with less than 5 years of available data over the years  
265 2000-2010, with each year containing at least one measurement per month of total N or P. These  
266 sites were then overlain with the locations of all flow gauging stations in the National River Flow  
267 Archive (NRFA). The NRFA collates, quality controls, archives and disseminates hydrometric data  
268 from gauging stations operated by government funded environmental bodies across the UK (Fry and  
269 Swain 2010 ). WIMS sites that were spatially coincident with NRFA gauging stations had the  
270 necessary daily flow data available to enable annual nutrient loads to be calculated and their  
271 catchments had been previously defined using the IHDTM. These temporal and spatial filters  
272 resulted in 33 catchments being identified as having sufficient data to act as a validation dataset for  
273 P. However, because total N is measured at a smaller proportion of sites (most measure NO<sub>x</sub>), only  
274 three catchments met all of the above criteria for N. Therefore, we reduced to three the required  
275 number of years with at least monthly measurements, giving 16 catchments with sufficient data for  
276 N.

277 Total annual nutrient load for each year was calculated from the WIMS and NRFA data for each  
278 catchment using the Beale Ratio Estimator (BRE, Beale 1962) which relates the ratio of average load  
279 to average flow, at times when concentrations are measured, to the ratio of average true load to  
280 average true flow over the entire period of interest (Dunn et al. 2014). Whilst there are a wide  
281 variety of methods available with which to extrapolate loads from intermittent data, ratio estimators  
282 have been used in previous validation studies (Terrado et al. 2014) and the BRE has been shown to  
283 produce robust results, especially when the measurement frequency of the concentration data is  
284 lower than that for discharge (Dolan et al. 1981; Dunn et al. 2014; Meals et al. 2013; Quilbé et al.

285 2006; Richards and Holloway 1987), as was the case here. The median BRE nutrient load across  
286 years for each catchment was then calculated.

287 Because the NDR model only accounts for nutrients from diffuse sources, it was necessary to adjust  
288 the modelled output of total load by an estimated load for point sources, to enable comparison with  
289 the validation data. In the UK, point sources can contribute the majority of P and a substantial  
290 proportion of N to waterways (Edwards and Withers 2008), although this varies across space and  
291 time (Arheimer and Lidén 2000). The estimated load from point sources was obtained using a GIS  
292 layer of wastewater treatment works (WWTWs) provided from UK Water Companies through the  
293 Environment Agency (see Williams et al. 2009). Although there is a wide variety of other point  
294 sources of N and P releases (Edwards and Withers 2008), WWTWs are likely to be the largest  
295 contributor at a whole-catchment scale in the UK (Bowes et al. 2005; Edwards and Withers 2008).  
296 For each WWTW, data were available describing the maximum human population served and the  
297 treatment type employed (i.e. primary, secondary or tertiary). These data were combined with a  
298 mean annual per capita export of P and N in untreated sewage of 0.52 kg P and 4.5 kg N and nutrient  
299 retention efficiencies for the different treatment types, both derived from a recent UK-wide review  
300 (Naden et al. 2016), to give an estimated annual N and P output for each WWTW. N and P outputs  
301 from individual WWTWs were then summed to give an annual load from WWTWs per catchment.  
302 This value was then subtracted from the per-catchment BRE to give a total export from diffuse  
303 sources only for comparison with the output of the InVEST NDR model. We removed catchments for  
304 which the estimated nutrient export from point sources contributed to more than 50% of the total  
305 estimated export (mostly relatively heavily urbanised catchments, Fig. 1), as these were unlikely to  
306 be well represented by the model (which focuses on diffuse sources) and would be highly influenced  
307 by any errors in our estimation of point source nutrient exports, giving final sample sizes of 28 for P  
308 and 14 for N (Figure 1 and Supplementary Material, Table S1).



309

310 **Fig. 1.** Map of southern UK showing catchments providing validation data for nitrogen (yellow),  
 311 phosphorus (red) or both (orange). Blue catchments indicate those which had sufficient nutrient  
 312 and flow measurements, but were estimated to have over 50% of total nutrient runoff due to point  
 313 sources and so were excluded from further analyses. Urban areas are also shown in grey (from  
 314 LCM2007). Note that none of these catchments overlap.

315 2.5. STATISTICAL ANALYSIS

316 Comparisons between the modelled and measured data were made by performing linear regressions  
 317 implemented in R (R Core Team 2014), as well as comparing the percentage differences between  
 318 modelled and measured. Many stakeholders require models simply to predict accurately the rank  
 319 order of locations in terms of ecosystem services, rather than absolute values (Willcock et al. 2016)  
 320 and the InVEST model does not necessarily aim for accurate prediction of values (Sharp et al. 2016).  
 321 Therefore, we also tested the accuracy of the InVEST NDR model in predicting relative export values  
 322 using rank correlation (Spearman's rho).

323

324 **3. Results**

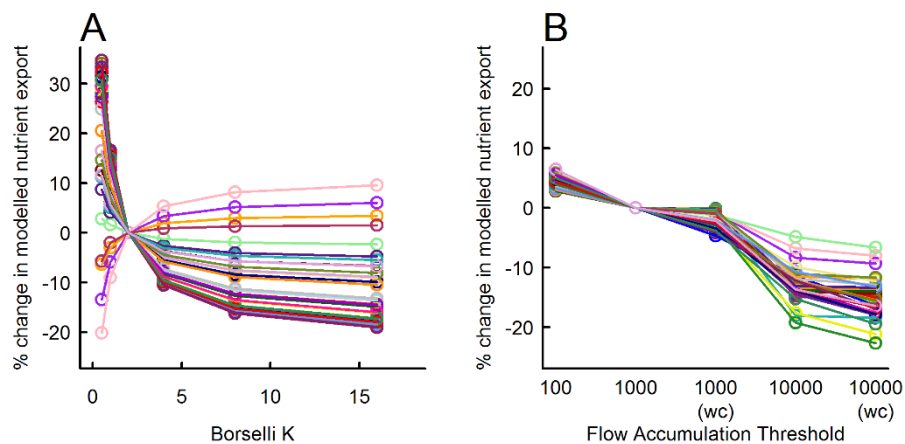
325 3.1. SENSITIVITY ANALYSIS

326 Modelled nutrient export from the NDR model was insensitive to variation in precipitation  
 327 (Supplementary Material Fig S1A). This was expected since these variations were applied as

328 consistent percentage change across the entire spatial extent. Because the role of this input is to  
329 represent relative runoff between pixels, the model is still likely to be sensitive to different inputs  
330 where they show different spatial patterns, as opposed to different magnitudes. This was addressed  
331 by comparing the three different input datasets (see below, Section 3.2).

332 The model was sensitive to variation in the nutrient loading and retention values (Supplementary  
333 Material Fig S1B and S1C) although sensitivity was linear. Because land cover was held constant for  
334 these analyses, sensitivity to these parameters did not show any catchment specificity.

335 In contrast, sensitivity to the two calibration parameters was highly catchment specific. Figure 3  
336 illustrates the percentage change in modelled nutrient export compared to the values obtained  
337 when using the default parameter values of 2 for  $k_b$  and 1000 for TFA. The effect of  $k_b$  on the  
338 magnitude and direction of change in nutrient export was catchment specific (Fig 2A). Overall,  
339 decreasing  $k_b$  to 0.5 produced the most extreme changes (-20% to +35%), whilst increasing  $k_b$  to 4  
340 resulted in changes of  $\pm 10\%$ . Further increases in  $k_b$  resulted in changes that remained within this  
341 range for the majority of catchments (Fig 2A). Catchment sensitivity appeared driven by topography,  
342 with more topographically varied catchments in the uplands showing decreases in nutrient export in  
343 response to increased  $k_b$  values and less varied, lowland catchments showing the opposite response  
344 (Pearson's  $r$  against % change at  $k_b = 0.5$ ; Mean catchment altitude  $n = 35$ ,  $r = 0.704$ ,  $p < 0.001$ ;  
345 Standard deviation in catchment altitude  $n = 35$ ,  $r = 0.709$ ,  $p < 0.001$ ).



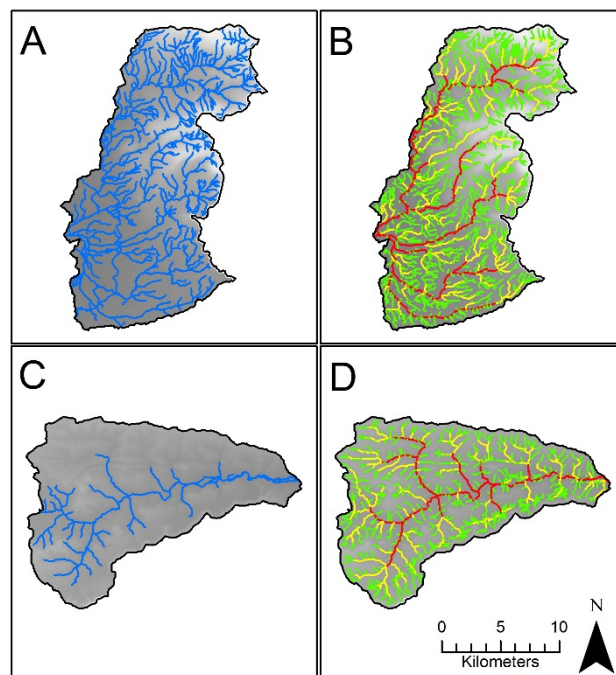
346

347 **Fig. 2** Sensitivity of the NDR model output to variation in the values of A) Borselli  $k_b$  parameter and  
348 B) Flow accumulation threshold, TFA (with wc indicating where the threshold was applied along with  
349 known watercourses from the digital watercourse network being added to the LULC raster). Each  
350 colour represents a different catchment.

351 Sensitivity to variation in the flow accumulation threshold TFA was also catchment specific (Fig 2B).

352 This was unsurprising as the degree to which a given TFA value accurately represents actual

353 watercourses will vary among catchments depending on their hydrogeology and topography. As can  
 354 be seen in Figure 4, the default value of 1000 overestimated the stream density in some catchments  
 355 whilst underestimating it in others. Thus, either reducing or increasing the threshold improved  
 356 representation of the routing of nutrients in some catchments but made it less accurate in others –  
 357 values of 100 captured most watercourses in some catchments (Fig. 3A and 3B) whilst in others  
 358 actual watercourses were best represented by TFA of 10,000 (Fig. 3C and 3D). Addition of mapped  
 359 watercourses to the LULC input with a TFA of 1000 resulted in comparatively minor changes to the  
 360 nutrient export (Fig 2B), but ensured that no catchment had known watercourses which were not  
 361 modelled as such. Using the same approach with a TFA of 10,000 had a large effect on the modelled  
 362 nutrient export (Fig 2B), reducing nutrient export by up to 20%, by restricting in-stream transport to  
 363 mapped watercourses only. Which of these latter results is the more accurate is likely to depend on  
 364 the accuracy of the mapped watercourse network (Baker et al. 2007), many of which, for example  
 365 ditches and field drains, have not been mapped into a hydrologically consistent network for the UK.  
 366 Because small, unmapped watercourses are known to have a potentially high impact on nutrient flux  
 367 (Edwards and Withers 2008; Foster et al. 2003; Heathwaite et al. 2006) we chose to use a TFA value  
 368 of 1000 with watercourses from Moore et al. (1994) added to the LULC raster for further analyses.



369  
 370 **Fig. 3** Examples of two catchments showing the catchment specific effects of variation in the flow  
 371 accumulation threshold, TFA, on modelled watercourse location. Panels A and C show the known  
 372 watercourse network (in blue) overlain onto the hydrologically corrected digital elevation model.  
 373 Panels B and D show streams as determined by three flow accumulation thresholds (100 = green;

1000 = green + yellow; 10,000 = green + yellow + red). The catchments are shaded according to altitude from dark (low, minimum = sea level) to pale (high, maximum = 600 m.a.s.l) grey.

### 3.2. MODEL VALIDATION AND COMPARISON OF INPUT DATASETS

Whilst the slope of the relationship remained similar for both nutrients, both N and P showed increasing percentage differences at resolutions coarser than 100m (Table 1 and Figure 4A and D). When reporting percentage differences we use median absolute percentage difference to avoid an apparent approach towards zero resulting from an increased range of under- and overestimates. At coarser (>100m) resolutions, although absolute values became increasingly erroneous for both nutrients, modelled N tended to preserve relative magnitudes of differences between catchments (shown by slightly increased Spearman’s  $\rho$ ). Indeed, the relatively stable values for  $r_{LR}^2$  for N suggest that coarser resolutions gave increasingly severe underestimates, but that the relationship between modelled and measured data remained relatively consistent across catchments. In contrast, at coarser resolutions than 100m, modelled P became increasingly inaccurate in terms of both absolute and relative export, and the relationship between modelled and measured data became increasingly inconsistent (table 1).

In practical terms, finer resolutions substantially increased the model run time, from around 30 seconds at 800m resolution, through 5 minutes at 100m resolution to around 4 hours at 25m resolution. The size of the input and output files was also substantially greater at finer resolutions, with output export maps for a single nutrient of 1.5 gigabytes, 100 megabytes and 2 megabytes for resolutions of 25, 100 and 800 metres, respectively. Given the observed drop off in  $r_{LR}^2$  and Spearman’s  $\rho$  for P and the increased percentage difference between modelled and measured data for both nutrients at resolutions coarser than 100m (Table 1 and Figure 4) we selected a resolution of 100m for further model testing and validation.

**Table 1** Comparisons of total P and N export from the InVEST NDR model with exports estimated from measured flows and nutrient concentrations, for varying resolutions of input data. Estimated exports were adjusted to remove point sources. Results are: median absolute percentage difference; Spearman’s  $\rho$  and the intercept, slope and  $r^2$  ( $r_{LR}^2$ ) of a linear regression; between the two datasets.

Nutrient	Resolution (m)	Median absolute % difference	Spearman’s rho ( $\rho$ )	Linear regression		
				Intercept	Slope ( $\pm$ 95% CI)	$r_{LR}^2$
Phosphorus	25	54.51	0.77	0.31	0.49 ( $\pm$ 0.12)	0.72
	50	56.43	0.78	0.34	0.49 ( $\pm$ 0.12)	0.71
	100	55.73	0.79	0.34	0.49 ( $\pm$ 0.12)	0.73

	200	56.30	0.79	0.31	0.48 ( $\pm 0.13$ )	0.69
	400	67.91	0.75	0.15	0.47 ( $\pm 0.14$ )	0.62
	800	88.96	0.56	-0.28	0.44 ( $\pm 0.23$ )	0.36
Nitrogen	25	72.57	0.75	0.31	0.67 ( $\pm 0.27$ )	0.71
	50	70.37	0.78	0.33	0.67 ( $\pm 0.27$ )	0.72
	100	72.58	0.81	0.28	0.69 ( $\pm 0.25$ )	0.76
	200	76.56	0.83	0.15	0.71 ( $\pm 0.23$ )	0.80
	400	84.11	0.87	-0.25	0.79 ( $\pm 0.23$ )	0.81
	800	95.51	0.88	-1.28	0.98 ( $\pm 0.37$ )	0.73

402

403 Because the sensitivity of the model to  $k_b$  appeared relatively high (Fig. 3A), and because there was  
404 no clear way to assess which value was most appropriate from our sensitivity analysis alone, we ran  
405 the model and compared to validation data for values of  $k_b$  of 0.5, 1, 1.5, 2, 2.5, 3, 3.5 and 4. We did  
406 not explore values of  $k_b$  beyond the range 0.5 - 4 here because sensitivity analysis demonstrates that  
407 at values much over 4 the impact of  $k_b$  on the model levels off, whilst at values approaching zero,  
408 the results diverge towards extreme values (Figure 2A). Overall, the effect of varying  $k_b$  on the fit to  
409 the validation data was not large, with near identical  $r_{LR}^2$ , slope and Spearman's correlation  
410 coefficient (Table 2). From Figure 4B and 4E, it can be seen that lower  $k_b$  values resulted in median  
411 percentage differences closer to zero, but this appears due to an increased number of outliers with  
412 substantial overestimates rather than a general improvement across catchments. This is perhaps  
413 unsurprising, given the widely varying catchment responses to changes in  $k_b$  seen in Figure 3A. There  
414 was thus no clear evidence to support altering the value of  $k_b$  from the default of 2 for our modelling  
415 across multiple catchments.

416 **Table 2** Comparisons of P and N export from the InVEST NDR model with exports estimated from  
417 measured flows and nutrient concentrations (adjusted to remove point sources), for eight values of  
418  $k_b$ .

Nutrient	$k_b$	Median absolute % difference	Spearman's rho ( $\rho$ )	Linear regression		
				Intercept	Slope ( $\pm 95\%$ CI)	$r_{LR}^2$
Phosphorus	0.5	41.16	0.77	0.41	0.49 ( $\pm 0.12$ )	0.71
	1	53.97	0.76	0.37	0.49 ( $\pm 0.12$ )	0.71
	1.5	58.43	0.77	0.33	0.49 ( $\pm 0.12$ )	0.71
	2	55.73	0.79	0.34	0.49 ( $\pm 0.12$ )	0.73
	2.5	56.99	0.79	0.32	0.49 ( $\pm 0.12$ )	0.72
	3	55.41	0.79	0.31	0.49 ( $\pm 0.12$ )	0.72
	3.5	53.59	0.79	0.30	0.49 ( $\pm 0.12$ )	0.72



Nitrogen	4	54.54	0.79	0.29	0.49 ( $\pm 0.12$ )	0.72
	0.5	64.00	0.78	0.38	0.68 ( $\pm 0.24$ )	0.75
	1	72.99	0.78	0.32	0.68 ( $\pm 0.24$ )	0.75
	1.5	75.49	0.80	0.27	0.68 ( $\pm 0.24$ )	0.76
	2	72.58	0.81	0.28	0.69 ( $\pm 0.25$ )	0.76
	2.5	73.72	0.81	0.25	0.69 ( $\pm 0.25$ )	0.76
	3	74.52	0.81	0.22	0.70 ( $\pm 0.25$ )	0.76
	3.5	75.11	0.81	0.21	0.70 ( $\pm 0.25$ )	0.76
	4	75.56	0.81	0.19	0.70 ( $\pm 0.24$ )	0.77

419

420 Having explored the effect of  $k_b$  and the input data resolution, we then compared the three input  
 421 precipitation data sources. The choice of precipitation data again made comparatively little  
 422 difference to either N or P export (Table 3 and Figure 4C and 4F). The randomised precipitation  
 423 dataset did show reductions in  $\rho$  and  $r_{LR}^2$  but actually decreased median percentage difference.

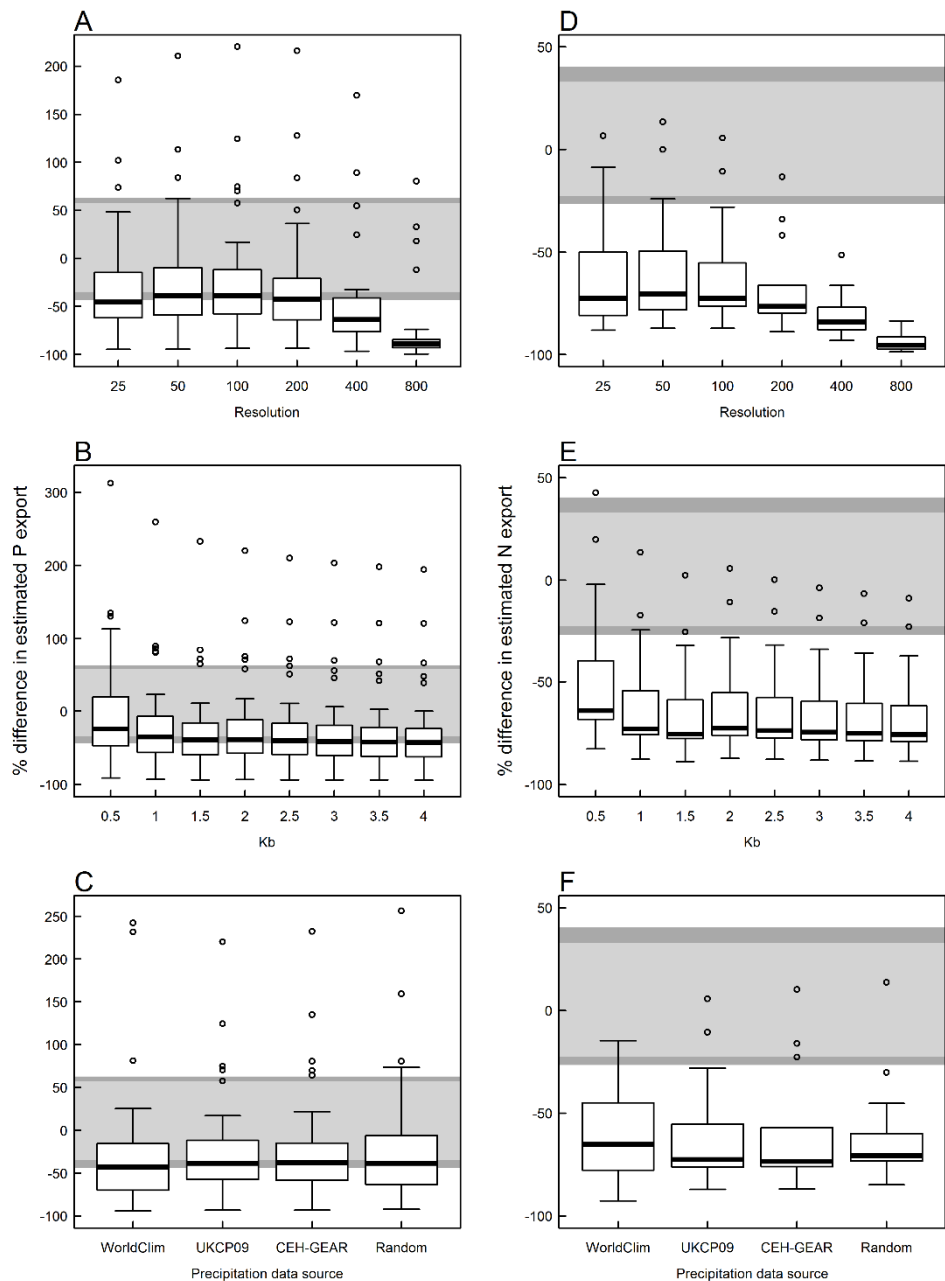
424 **Table 3** Comparisons of total P and N export from the InVEST NDR model with exports estimated  
 425 from measured flows and nutrient concentrations (adjusted to remove point sources), for three  
 426 difference sources of precipitation data (WorldClim, Met Office UKCP09 and CEH-GEAR).

Nutrient	Precipitation data source	Median absolute % difference	Spearman's rho ( $\rho$ )	Linear regression		
				Intercept	Slope ( $\pm 95\%$ CI)	$r_{LR}^2$
Phosphorus	WorldClim	56.40	0.81	0.33	0.51 ( $\pm 0.12$ )	0.73
	UKCP09	55.73	0.79	0.34	0.49 ( $\pm 0.12$ )	0.73
	CEH-GEAR	57.07	0.77	0.35	0.49 ( $\pm 0.12$ )	0.71
	Random	55.13	0.69	0.37	0.46 ( $\pm 0.17$ )	0.53
Nitrogen	WorldClim	70.70	0.88	0.17	0.74 ( $\pm 0.21$ )	0.83
	UKCP09	72.58	0.81	0.28	0.69 ( $\pm 0.25$ )	0.76
	CEH-GEAR	73.59	0.84	0.28	0.69 ( $\pm 0.25$ )	0.75
	Random	65.27	0.74	0.28	0.68 ( $\pm 0.27$ )	0.71

427

428

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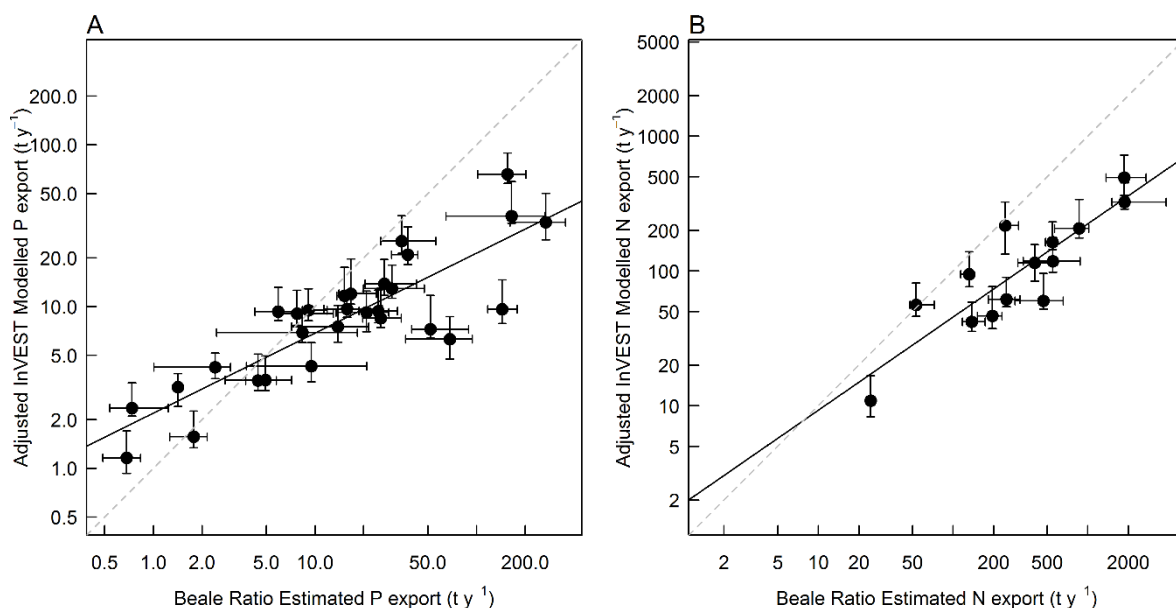


430

431 **Fig. 4** Boxplots showing the effect of spatial resolution (i.e. dimensions of raster cells in metres)  
 432 (A,D), Borselli  $k_b$  (B,E) and precipitation data source (C,F) on percentage differences between  
 433 estimated total nutrient export per catchment from the InVEST NDR model and corresponding  
 434 exports estimated from gauged flow and measured nutrient concentration data (adjusted to remove  
 435 point sources), for phosphorus (A,B,C) and nitrogen (D,E,F). Grey shaded areas indicate the range of  
 436 variation in estimated nutrient export values resulting from interannual variation in estimated  
 437 exports (quartiles, light grey) and the maximum and minimum values for average per capita nutrient  
 438 outflow from point sources (dark grey)

439 Modelled total nutrient export showed a better fit to the empirical data than did modelled load  
 440 alone ( $P$ :  $r_{LR}^2 = 0.73, 0.56$ , Spearman's  $\rho = 0.79, 0.69$ ,  $N$ :  $r_{LR}^2 = 0.76, 0.72$ , Spearman's  $\rho = 0.80, 0.75$ ,  
 441 for load and export, respectively, with 100m resolution inputs,  $K_b = 2$  and UKCP09 precipitation  
 442 data). The NDR factor component of the model thus results in substantial increases in model  
 443 performance over a simple summation of loads, especially for P.

444 Because the results at all values of  $k_b$  and the different precipitation datasets resulted in good  
 445 predictions of the relative magnitude of nutrient export ( $\rho = 0.77 - 0.81$  and  $0.75 - 0.88$ , for  
 446 phosphorous and nitrogen, respectively) but relatively large underestimates of absolute values  
 447 (range of absolute median estimates  $\pm 44.4\% - \pm 58.4\%$  and  $\pm 65.3\% - \pm 76.6\%$  for phosphorous and  
 448 nitrogen, respectively), we ran a final model with reduced retention coefficients for both nutrients.  
 449 Whilst this deviates from parameter values reported from empirical studies (see section 2.2), we  
 450 were interested to see if a large improvement in accuracy could be made by performing a simple,  
 451 uniformly applied adjustment to retention values. We therefore divided retention values by two and  
 452 re-ran the model (with 100m resolution inputs,  $K_b = 2$  and UKCP09 precipitation data). Although this  
 453 resulted in slightly reduced absolute median percentage differences (by 8.5% and 9.2% for  
 454 phosphorous and nitrogen, respectively), the Spearman's  $\rho$  and the slope and  $r_{LR}^2$  from linear  
 455 regression were also reduced (4-10% reduction Spearman's  $\rho$ , 4-13% reduction in  $r_{LR}^2$ , 8%-12%  
 456 reduction in slope). This suggests that modifying the retention coefficients away from literature  
 457 values helps to reduce the median level of underestimates, but reduces the ability of the model to  
 458 predict relative magnitude of nutrient export between catchments, probably by worsening  
 459 overestimation in low exporting catchments whilst improving underestimation in high yielding ones  
 460 (Figure 5).



461

462 **Fig. 5.** Nutrient export per catchment from the InVEST NDR model plotted against exports estimated  
463 from measured flows and nutrient concentrations (adjusted to remove point sources), for P (panel  
464 A) and N (panel B). Points represent InVEST results (input resolution = 100m,  $k_b = 2$ , precipitation  
465 data = UKCP09) against Beale Ratio Estimated nutrient export from measurements. Horizontal bars  
466 span the range given by 25<sup>th</sup> to 75<sup>th</sup> percentile of interannual variation in the Beale ratio estimated  
467 nutrient export  $\pm$  the maximum and minimum values for average *per capita* nutrient outflow from  
468 point sources. Vertical bars indicate the range in modelled export resulting from running the model  
469 with values of  $k_b$  between 0.5 and 4, input raster resolution of 25, 50, 100 and 200 metres and the  
470 three different precipitation datasets. A 1:1 relationship is indicated by the dotted line. Note axes  
471 are on a log<sub>10</sub> scale.

## 472 **4. Discussion**

### 473 4.1. PERFORMANCE OF THE INVEST NDR MODEL

474 Our results suggest that the InVEST NDR model can give good results in terms of the relative  
475 magnitude of N and P export across a wide variety of UK river catchments, with  $\rho$  between 0.7 and  
476 0.83 depending on the scale of input data and parameter values used. However, accuracy in terms  
477 of estimating actual nutrient export was comparatively low with the majority of catchments showing  
478 over or underestimates of up to 44% for P and 65% for N. It should be noted that attempting to gain  
479 good model performance over a large number of widely varying catchments is a challenging test for  
480 the model. Performance is expected to be higher with calibration at the regional level with  
481 catchments having similar hydrogeological properties. Whilst some studies perform such model  
482 performance assessment (e.g. Bai et al. 2013; Terrado et al. 2014), many ecosystem service models  
483 are applied at regional or national scales without validation (Martínez-Harms and Balvanera 2012). A  
484 survey across sub-Saharan Africa demonstrated that many stakeholders wish to run ecosystem  
485 service models at national scales (Willcock et al. 2016). Furthermore, ecosystem service models are  
486 often perceived as being of great use in data-scarce parts of the world (Pandeya et al. 2016; Villa et  
487 al. 2014) where there are few opportunities to calibrate or validate. Therefore, it is important for  
488 studies such as ours to demonstrate some of the possible pitfalls of applying ecosystem service  
489 models without extensive validation and sensitivity testing.

### 490 4.2. UNDERSTANDING MODEL SENSITIVITIES

491 Sensitivity to variation in the input parameter values is unsurprising and, of course, desirable if a  
492 model is to be used to assess change over time or among future change scenarios. However, it is  
493 also important to understand that such sensitivities can determine how appropriate a model is to a  
494 particular study region, where to focus most effort on data acquisition (Boithias et al. 2014; Sánchez-

495 Canales et al. 2012), or to aid in assessing the uncertainty associated with model outcomes. In brief,  
496 the model appeared most sensitive to the nutrient loading and retention values, the threshold flow  
497 accumulation and the resolution of the input raster data (beyond a certain range). We discuss each  
498 of the parameters in turn.

#### 499 4.2.1. *Nutrient load and retention*

500 The linear response between nutrient export and nutrient load and nutrient retention coefficients is  
501 to be expected, given that nutrient export is calculated as the product of nutrient load on a pixel and  
502 the NDR factor, which is proportional to nutrient retention parameters from downslope pixels.  
503 These parameters are thus the major drivers by which the spatial configuration of land use/land  
504 cover affects nutrient runoff. Importantly, nutrient loads and retention efficiencies will vary greatly  
505 in time and space. In our test catchments, most of which are dominated by arable land or  
506 agriculturally-improved grassland, such variation will be driven by crop type, stocking density,  
507 fertiliser application rates and timings, and other farm management practices. It is, therefore,  
508 essential to research these values sufficiently to ensure that they are robust for the land cover types  
509 that are dominant in the study region and those that are of most interest in relation to any change  
510 scenarios that are being explored.

#### 511 4.2.2. *$k_b$ parameter*

512 The Borselli  $k_b$  parameter determines the relationship between hydrologic connectivity (the degree  
513 of connection from patches of land to the stream) and the NDR. Higher values mean that the  
514 relationship between the connectivity index and the NDR factor becomes linear, whereas lower  
515 values mean that this relationship becomes a step function. This relationship is site-specific, as  
516 demonstrated by the very different responses to varying  $k_b$  shown by different catchments in our  
517 sensitivity analysis. This is also likely to be the reason that, from our results, calibration to produce  
518 the best cross-catchment absolute accuracy may not result in the most accurate predictions of  
519 relative magnitude between catchments and *vice versa*. Therefore, although this parameter is in  
520 practice the main parameter used for calibration (Sharp et al. 2016), where possible  $k_b$  should be  
521 determined regionally, across catchments with similar hydrogeological properties.

#### 522 4.2.3. *Threshold flow accumulation*

523 Varying the flow accumulation threshold TFA had a substantial effect on model output. This effect is  
524 partly explained by the model structure, which assumes that stream pixels do not export any  
525 nutrient. Therefore, changing the density of the stream network also changes the number of pixels  
526 that actually contribute to nutrient loading and retention (e.g. 66%, 92%, 98%, 99% at TFAs of 10,  
527 100, 1000 and 10000, respectively, at 25m DEM resolution). Our results show that, as with  $k_b$ ,

528 selecting a single value that is equally applicable across a number of catchments is difficult, because  
529 catchment topography and hydrogeological attributes (e.g. groundwater flow) can change the  
530 threshold that needs to be set to capture actual watercourses. Comparing the derived stream  
531 network to a known watercourse network is a key first step to selecting an appropriate value, and  
532 our results also suggest that modifying the DEM and LULC map to capture known watercourse  
533 networks may provide a robust approach to overcoming this issue when conducting cross-catchment  
534 analyses.

#### 535 4.2.4. DEM and LULC raster resolution

536 Changing the resolution of the input DEM and LULC spatial data had comparatively little effect on  
537 the accuracy of the model output for both P and N at resolutions less than or equal to 100m. Whilst  
538 this is in contrast to other studies which have concluded that increased data resolution usually  
539 results in increased model accuracy (Brazier et al. 2005), decreased sensitivity to input raster  
540 resolution is a stated aim of the design of the NDR model (Sharp et al. 2016), hence the inclusion of  
541 TFA and critical flow length parameters which the user can modify. It appears that resolutions finer  
542 than 100m gain little in absolute accuracy to justify the very substantial increases in file size (making  
543 data harder to store, manage and disseminate) and running time which result from running the  
544 model with finer resolution inputs.

545 However, resolutions coarser than 100m resulted in decreasing accuracy, especially for P. This is  
546 likely to be a result of coarser resolution cells losing spatial detail, with values being generalised to  
547 average (DEM) or dominant (LULC) values per cell. The most likely mechanism for the effects we  
548 observed are loss of detail from the LULC raster. If the key LULC classes governing nutrient export  
549 are relatively small in area, they may be lost from aggregated inputs. For example, in UK upland  
550 catchments which are largely semi-natural, small areas of agricultural land close to watercourses  
551 would have a disproportionate effect on total nutrient export, but may not form the majority cover  
552 of any non-watercourse pixels in a coarse resolution LULC map, removing their potential to influence  
553 modelled nutrient export. The two nutrients differed somewhat in their responses to resolution  
554 (with N retaining accurate relative magnitude and a consistent relationship between modelled and  
555 measured data, even though underestimation became more severe). This is probably because of  
556 their different loadings and export pathways. Phosphorus is more associated with high releases from  
557 proportionally small areas with high hydrologic connectivity whilst nitrogen is more evenly spread  
558 across land cover classes and less directly linked to the degree of hydrologic connectivity (Edwards  
559 and Withers 2008; Withers and Lord 2002), such that the loss of spatial detail at coarser resolutions  
560 affects the ability of the model to reflect actual export to different degrees.

561 4.2.5 Precipitation data source

562 Unlike the InVEST water yield model (Redhead et al. 2016), the NDR model appeared relatively  
563 insensitive to the source of input precipitation data. All three datasets produced similar results, and  
564 even the randomised data only reduced accuracy slightly. To some extent this is unsurprising. The  
565 effect of precipitation data is to modify the per pixel load to account for runoff potential by relating  
566 the precipitation per cell to the average across the raster (see Supplementary Material, Appendix  
567 S1). Therefore, providing that general spatial patterns are preserved between input datasets, this  
568 should be sufficient to obtain similar results. The lack of effect of using randomised data is perhaps  
569 more surprising, as here the spatial pattern of relative runoff has been removed. However, by using  
570 long term average data at 1km to 5km scales, the range of values is not high within many  
571 catchments, so even when randomising the data the distribution of runoff potential across the  
572 landscape does not vary hugely (Supplementary Material, Table S2). Of course, for those catchments  
573 with a higher range in precipitation (in our analysis this was limited to larger catchments spanning  
574 upland and lowland), randomisation will have a greater effect, so in locations where rainfall is more  
575 variable within catchments (e.g. Boithias et al. 2014; Terrado et al. 2014), or over timescales where  
576 temporal variation becomes an issue, this parameter may become of much greater importance.

577 4.3. LIMITATIONS OF THE MODEL

578 The InVEST NDR model includes only a relatively limited number of the wide range of complex, and  
579 spatially and temporally variable processes that influence nutrient transport from land to  
580 watercourses (see reviews in Arheimer and Lidén 2000; Edwards and Withers 2008; Parn et al.  
581 2012). Whilst this is clearly stated in the InVEST documentation, it is important to explore some of  
582 these limitations to remind potential users of the sensible use of the model and to explain the  
583 relatively large and variable underestimates of nutrient delivery that our results show.

584 One of the most obvious limitations of applying this model within the UK is that it focuses on diffuse  
585 (i.e. non-point) sources of nutrient only, while most UK catchments, especially those in more  
586 populated areas, are also affected by nutrient discharges from WWTWs. This is not a limitation of  
587 the model as such, but it is a problem that needs to be addressed when comparing modelled output  
588 with measured values. This is discussed below under limitations of our validation approach (Section  
589 4.3).

590 A limitation of the model that is harder to compensate for is the presence of catchment specific  
591 processes that may affect nutrient transport and export in ways that are hard to predict or capture  
592 within model frameworks that are based on an average load per area of land use/land cover class.  
593 These include nutrient releases from so-called intermediate sources (because they are neither

594 diffuse nor a predictable point source) such as field drains, septic tanks, farmyard and/or road/track  
595 runoff (Edwards and Withers 2008). Such features are difficult to include as a LULC class because  
596 they are rarely well mapped and nutrient releases from them are often difficult to predict because of  
597 high spatial and temporal variation (Edwards and Withers 2008; Withers et al. 2014). For example,  
598 field drains can release large amounts of P into watercourses from agricultural land during storm  
599 events, bypassing surface flow and normal retention capabilities (Foster et al. 2003; Heathwaite et  
600 al. 2006; Hooda et al. 1999). Such features may be especially important in rural catchments where  
601 most other sources are diffuse (Jarvie et al. 2003). In addition, it has been shown that interpolation  
602 of infrequent data is unlikely to give reliable estimates of in-stream P loads where temporal changes  
603 in stream flow and P concentrations happen very quickly in response to rainfall and surface runoff  
604 (Defew et al. 2013).

605 The model can be set to apportion a set amount of nutrient transport to subsurface flow for each  
606 LULC class; this is then subject to a simple exponential decay function driven by distance to stream.  
607 A value can be defined by the user across all LULC classes (Sharp et al. 2016), but in reality  
608 subsurface flow and nutrient retention varies considerably within LULC classes. There are also many  
609 features that, whilst contributing to nutrient retention and export, lie below the spatial resolution of  
610 most input LULC maps. These include riparian buffer strips or riparian vegetation that can retard or  
611 reduce the level of nutrients entering the watercourse (Aguar Jr et al. 2015; Darch et al. 2015; Lena  
612 et al. 1994; Parn et al. 2012). Once nutrient enters a watercourse it may be subject to further  
613 retention by aquatic vegetation or uptake by riverine sediments (Jarvie et al. 2005). However, on an  
614 annual scale, most of these in stream nutrient sinks are temporary and much of the nutrient  
615 delivered to a watercourse from land eventually leaves the catchment in one form or another  
616 (Bowes and House 2001).

617 Although the two nutrients are modelled in identical ways by the InVEST model, the extent to which  
618 the model is able to reflect the real world flow of the two nutrients is likely to differ, hence our  
619 observed differing accuracies for N and P. This is because of differences in anthropogenic sources,  
620 temporal and spatial variation in levels of output, and the chemical properties of the two elements  
621 and the various forms in which they are usually transported through soil-water systems. One key  
622 difference is that N can be removed from the hydrological system by denitrification to atmospheric  
623 N<sub>2</sub> and, in some cases, very high retention can be achieved within a watercourse by riverine or  
624 wetland vegetation that promotes such processes (Parn et al. 2012; Saunders and Kalff 2001). No  
625 equivalent process exists for P (Parn et al. 2012), so at times of high P runoff, the normal retention  
626 capacity of any particular land cover class may be more likely to become saturated, leading to higher  
627 than expected exports (Koerselman et al. 1990). Phosphorus flows are often dominated by point



628 source releases and temporal factors such as surface runoff during and after storm events. In  
629 contrast, N transport is more often associated with broader land cover patterns, subsurface flow and  
630 soil chemistry (Edwards and Withers 2008; Nedwell et al. 2002; Parn et al. 2012; Withers and Lord  
631 2002).

632 The issues outlined above may be part of the reason why a simple, universally applied reduction of  
633 retention coefficients did not substantially improve model accuracy. However, it is also worth noting  
634 that the ability of the model to obtain good predictions in terms of the relative magnitude of  
635 nutrient export, despite these limitations, suggests that the model and its results are useful if  
636 interpreted with caution, especially in order to identify spatial patterns of N or P delivery across  
637 catchments or to examine relative change under potential scenarios, which is the intended use for  
638 most InVEST models (Sharp et al. 2016). However, the relative export or retention of nutrients alone  
639 may not be sufficiently informative for decision makers, who may need to know whether export is  
640 sufficient to meet a threshold (e.g. a legal maximum for drinking water or a level known to cause  
641 certain ecological impacts) or to place an economic value the service of nutrient retention in terms  
642 of avoided water treatment costs. In this case, an understanding of the absolute accuracy of  
643 modelled nutrient export figures, and how to best improve this, is key. Of note, the model is open-  
644 source and its code is regularly updated by the development team or external contributors so that  
645 such limitations may be addressed in the future. For example, the NDR model used here was already  
646 an improvement over a previous version (Water Quality model, InVEST v3.2).

#### 647 4.4. LIMITATIONS OF THE VALIDATION APPROACH

648 Validation of the model using the approach detailed in this paper has its limitations. Without actual  
649 measurements of nutrient export to water, estimations of average annual export will always be  
650 subject to a degree of error arising from a variety of factors whatever the method of calculation  
651 used.

652 Firstly, whilst the Beale ratio approach to calculating nutrient has been shown to provide better  
653 results than other methods (Dolan et al. 1981; Dunn et al. 2014; Meals et al. 2013; Quilbé et al.  
654 2006; Richards and Holloway 1987), it has the potential to underestimate in-stream nutrient load if  
655 nutrient sampling does not coincide with periods of peak flow (Quilbé et al. 2006) or peak runoff, as  
656 may occur during short duration, extreme weather events. During such events, P transport is very  
657 difficult to measure accurately unless sampled at very high frequencies, which is rarely the case for  
658 routine monitoring data (Defew et al. 2013). Also, the peak flows recorded by gauging stations may  
659 themselves be underestimates where these events affect the accurate measurement of flow (e.g.  
660 bypassing of the gauging station by groundwater or flooding, water transfer, etc.). However, our

661 results suggested that BRE derived values were mostly larger than the modelled N and P values,  
662 even when compared to the interquartile range of BRE values across years or the inter-annual  
663 ranges per catchment, so this is unlikely to be a major driver of this apparent error in model  
664 predictions.

665 Because the model only accounts for nutrients derived from surface runoff, it was necessary to  
666 adjust the validation data to estimate the total that would be derived from diffuse sources, only.  
667 Using WWTW locations and average per capita nutrient export values is common practice, but  
668 potential per capita figures show wide variation between studies, catchments and over time  
669 (Edwards and Withers 2008; Johnes 1996; Naden et al. 2016). However, this variation is unlikely to  
670 show a systematic bias towards over- or under-estimation across catchments and so our results  
671 should provide a fair reflection of model performance in terms of the slope of the linear regression  
672 line, even if individual catchments over- or under-estimate the proportion of nutrient export that is  
673 derived from point sources. We also quantified the likely extent of this potential error by examining  
674 the variation in estimated diffuse source nutrient export imparted by varying the maximum and  
675 minimum per capita values for nutrient export from point sources. Even so, there remains a  
676 potential for unquantified error in terms of unmapped point sources and variation in per capita  
677 values among catchments. Because we excluded catchments where point source nutrient exports  
678 appeared to contribute over 50% to the total in-stream nutrient load, we also excluded heavily  
679 urbanised catchments. So, our validation cannot inform on the ability of the model to predict diffuse  
680 pollution in these types of catchment.

#### 681 4.5. CONCLUSIONS

682 Whilst the InVEST NDR model gives good estimates of the relative magnitude of nutrient exports  
683 across catchments, absolute values are frequently underestimated even after calibration of input  
684 parameter values. This is to be expected given the simple nature of the InVEST model and the aims  
685 of using it to compare the outcomes of change scenarios across a wide range of ecosystem services  
686 (Sharp et al. 2015). Key model sensitivities were to nutrient loading and retention factors and the  
687 threshold flow accumulation. Input raster resolution had major impacts on model performance only  
688 at resolutions coarser than 100m. For resolutions finer than this, there was little in the way of  
689 increased accuracy to offset the increased model run time and output data volume.

690 Collating the data sources for input and validation of the model, even in such a well-studied region  
691 such as the UK, was time consuming and complex. Similar difficulties are likely to be encountered in  
692 regions that have less frequent monitoring schemes for nutrients and water flow. Since one of the  
693 stated aims of the InVEST model is to allow meaningful analyses to take place in data-poor regions,

694 we recommend the following uncertainty assessment analyses: exploration of alternative input  
695 datasets for the study region, sensitivity analyses on loads and retention efficiencies for dominant  
696 LULC types, TFA, and  $k_b$ , and a thorough exploration of the model outputs before using them to  
697 inform decisions. This reflects the recommendations of the designers of the InVEST NDR model  
698 (Hamel et al. 2015; Sharp et al. 2016) and the findings of previous studies across a number of  
699 ecosystem services (Boithias et al. 2014; Pessacg et al. 2015; Redhead et al. 2016; Sánchez-Canales  
700 et al. 2012).

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## 707 **References**

- 708 Aguiar Jr, T.R., Rasesa, K., Parron, L.M., Brito, A.G., Ferreira, M.T., 2015. Nutrient removal  
709 effectiveness by riparian buffer zones in rural temperate watersheds: The impact of no-till crops  
710 practices. *Agricultural Water Management* 149, 74-80.
- 711 Arheimer, B., Lidén, R., 2000. Nitrogen and phosphorus concentrations from agricultural  
712 catchments—influence of spatial and temporal variables. *Journal of Hydrology* 227, 140-159.
- 713 Arnold, J.G., Srinivasan, R., Muttiah, R.S., Williams, J.R., 1998. Large area hydrologic modeling and  
714 assessment part i: model development. *JAWRA Journal of the American Water Resources  
715 Association* 34, 73-89.
- 716 Bai, Y., Zheng, H., Ouyang, Z., Zhuang, C., Jiang, B., 2013. Modeling hydrological ecosystem services  
717 and tradeoffs: a case study in Baiyangdian watershed, China. *Environmental Earth Sciences* 70, 709-  
718 718.
- 719 Baker, M.E., Weller, D.E., Jordan, T.E., 2007. Effects of stream map resolution on measures of  
720 riparian buffer distribution and nutrient retention potential. *Landscape Ecology* 22, 973-992.
- 721 Beale, E.M.L., 1962. Some uses of computers in operational research. *Industrielle Organisation* 2, 51-  
722 52.
- 723 Boithias, L., Acuña, V., Vergoñós, L., Ziv, G., Marcé, R., Sabater, S., 2014. Assessment of the water  
724 supply:demand ratios in a Mediterranean basin under different global change scenarios and  
725 mitigation alternatives. *Science of the total environment* 470–471, 567-577.
- 726 Bowes, M., House, W., 2001. Phosphorus and dissolved silicon dynamics in the River Swale  
727 catchment, UK: a mass-balance approach. *Hydrological Processes* 15, 261-280.
- 728 Bowes, M.J., Hilton, J., Irons, G.P., Hornby, D.D., 2005. The relative contribution of sewage and  
729 diffuse phosphorus sources in the River Avon catchment, southern England: Implications for nutrient  
730 management. *Science of the total environment* 344, 67-81.
- 731 Braat, L.C., de Groot, R., 2012. The ecosystem services agenda:bridging the worlds of natural science  
732 and economics, conservation and development, and public and private policy. *Ecosystem Services* 1,  
733 4-15.
- 734 Brazier, R.E., Heathwaite, A.L., Liu, S., 2005. Scaling issues relating to phosphorus transfer from land  
735 to water in agricultural catchments. *Journal of Hydrology* 304, 330-342.

736 Breuer, L., Vache, K., Julich, S., Frede, H.-G., 2008. Current concepts in nitrogen dynamics for  
737 mesoscale catchments. *Hydrological Sciences Journal* 53, 1059-1074.

738 Darch, T., Carswell, A., Blackwell, M.S.A., Hawkins, J.M.B., Haygarth, P.M., Chadwick, D., 2015.  
739 Dissolved Phosphorus Retention in Buffer Strips: Influence of Slope and Soil Type. *Journal of*  
740 *Environmental Quality* 44, 1216-1224.

741 Defew, L.H., May, L., Heal, K.V., 2013. Uncertainties in estimated phosphorus loads as a function of  
742 different sampling frequencies and common calculation methods. *Marine and Freshwater Research*  
743 64, 373-386.

744 Denedy-Frank, P.J., Muenich, R.L., Chaubey, I., Ziv, G., 2016. Comparing two tools for ecosystem  
745 service assessments regarding water resources decisions. *Journal of Environmental Management*  
746 177, 331-340.

747 Dillon, P.J., Kirchner, W.B., 1975. The effects of geology and land use on the export of phosphorus  
748 from watersheds. *Water Research* 9, 135-148.

749 Dolan, D.M., Yui, A.K., Geist, R.D., 1981. Evaluation of River Load Estimation Methods for Total  
750 Phosphorus. *Journal of Great Lakes Research* 7, 207-214.

751 Drewry, J.J., Newham, L.T.H., Greene, R.S.B., 2011. Index models to evaluate the risk of phosphorus  
752 and nitrogen loss at catchment scales. *Journal of Environmental Management* 92, 639-649.

753 Dunn, S.M., Sample, J., Potts, J., Abel, C., Cook, Y., Taylor, C., Vinten, A.J.A., 2014. Recent trends in  
754 water quality in an agricultural catchment in Eastern Scotland: elucidating the roles of hydrology and  
755 land use. *Environmental Science: Processes & Impacts* 16, 1659-1675.

756 Edwards, A.C., Withers, P.J.A., 2008. Transport and delivery of suspended solids, nitrogen and  
757 phosphorus from various sources to freshwaters in the UK. *Journal of Hydrology* 350, 144-153.

758 Environment Agency, 2017. Water quality data archive.

759 Feng, M., Liu, S., Euliss Jr, N.H., Young, C., Mushet, D.M., 2011. Prototyping an online wetland  
760 ecosystem services model using open model sharing standards. *Environmental Modelling &*  
761 *Software* 26, 458-468.

762 Fisher, B., Turner, R.K., Morling, P., 2009. Defining and classifying ecosystem services for decision  
763 making. *Ecological economics* 68, 643-653.

764 Foster, I.D., Chapman, A., Hodgkinson, R., Jones, A., Lees, J., Turner, S., Scott, M., 2003. Changing  
765 suspended sediment and particulate phosphorus loads and pathways in underdrained lowland  
766 agricultural catchments; Herefordshire and Worcestershire, UK, In *The Interactions between*  
767 *Sediments and Water*. pp. 119-126. Springer.

768 Fozzard, I., Doughty, R., Ferrier, R.C., Leatherland, T., Owen, R., 1999. A quality classification for  
769 management of Scottish standing waters. *Hydrobiologia* 395, 433-454.

770 Fry, M.J., Swain, O., 2010 Hydrological data management systems within a national river flow  
771 archive, In *Role of Hydrology in Managing Consequences of a Changing Global Environment*. ed. C.  
772 Kirby, pp. 808-815. British Hydrological Society.

773 Grafius, D.R., Corstanje, R., Warren, P.H., Evans, K.L., Hancock, S., Harris, J.A., 2016. The impact of  
774 land use/land cover scale on modelling urban ecosystem services. *Landscape Ecology* 31, 1509-1522.

775 Hamel, P., Chaplin-Kramer, R., Sim, S., Mueller, C., 2015. A new approach to modeling the sediment  
776 retention service (InVEST 3.0): Case study of the Cape Fear catchment, North Carolina, USA. *Science*  
777 *of the total environment* 524, 166-177.

778 Hamel, P., Falinski, K., Sharp, R., Auerbach, D.A., Sánchez-Canales, M., Denedy-Frank, P.J., 2017.  
779 Sediment delivery modeling in practice: Comparing the effects of watershed characteristics and data  
780 resolution across hydroclimatic regions. *Science of the total environment* 580, 1381-1388.

781 Hamel, P., Guswa, A.J., 2015. Uncertainty analysis of a spatially explicit annual water-balance model:  
782 case study of the Cape Fear basin, North Carolina. *Hydrological Earth System Science* 19, 839-853.

783 Hamel, P., Sharp, R., 2017. InVEST 3.3.3 Nutrient Delivery Ratio Model, Zenodo.

784 Heathwaite, A.L., Burke, S.P., Bolton, L., 2006. Field drains as a route of rapid nutrient export from  
785 agricultural land receiving biosolids. *Science of the total environment* 365, 33-46.

786 Hijmans, R.J., Cameron, S.E., Parra, J.L., Jones, P.G., Jarvis, A., 2005. Very high resolution interpolated  
787 climate surfaces for global land areas. *International Journal of Climatology* 25, 1965-1978.

788 Hooda, P.S., Moynagh, M., Svoboda, I.F., Edwards, A.C., Anderson, H.A., Sym, G., 1999. Phosphorus  
789 Loss in Drainflow from Intensively Managed Grassland Soils. *Journal of Environmental Quality* 28,  
790 1235-1242.

791 Jackson, D.L., 2000. Guidance on the interpretation of the Biodiversity Broad Habitat Classification  
792 (terrestrial and freshwater types): Definitions and the relationship with other classifications.

793 Jarvie, H.P., Jürgens, M.D., Williams, R.J., Neal, C., Davies, J.J., Barrett, C., White, J., 2005. Role of  
794 river bed sediments as sources and sinks of phosphorus across two major eutrophic UK river basins:  
795 the Hampshire Avon and Herefordshire Wye. *Journal of Hydrology* 304, 51-74.

796 Jarvie, H.P., Neal, C., Withers, P.J.A., Robinson, A., Salter, N., 2003. Nutrient water quality of the Wye  
797 catchment, UK: exploring patterns and fluxes using the Environment Agency data archives. *Hydrol.*  
798 *Earth Syst. Sci.* 7, 722-743.

799 Jenkins, G.J., Perry, M.C., Prior, M.J., 2008. The climate of the United Kingdom and recent trends.  
800 Hadley Centre, Exeter, UK.

801 Johnes, P., Moss, B., Phillips, G., 1996. The determination of total nitrogen and total phosphorus  
802 concentrations in freshwaters from land use, stock headage and population data: testing of a model  
803 for use in conservation and water quality management. *Freshwater Biology* 36, 451-473.

804 Johnes, P.J., 1996. Evaluation and management of the impact of land use change on the nitrogen  
805 and phosphorus load delivered to surface waters: the export coefficient modelling approach. *Journal*  
806 *of Hydrology* 183, 323-349.

807 Keeler, B.L., Polasky, S., Brauman, K.A., Johnson, K.A., Finlay, J.C., O'Neill, A., Kovacs, K., Dalzell, B.,  
808 2012. Linking water quality and well-being for improved assessment and valuation of ecosystem  
809 services. *Proceedings of the National Academy of Sciences* 109, 18619-18624.

810 Keller, A.A., Fournier, E., Fox, J., 2015. Minimizing impacts of land use change on ecosystem services  
811 using multi-criteria heuristic analysis. *Journal of Environmental Management* 156, 23-30.

812 Koerselman, W., Bakker, S.A., Blom, M., 1990. Nitrogen, Phosphorus and Potassium Budgets for Two  
813 Small Fens Surrounded by Heavily Fertilized Pastures. *Journal of Ecology* 78, 428-442.

814 Leh, M.D.K., Matlock, M.D., Cummings, E.C., Nalley, L.L., 2013. Quantifying and mapping multiple  
815 ecosystem services change in West Africa. *Agriculture, Ecosystems & Environment* 165, 6-18.

816 Lena, B.M.V., Dahl, J., Carsten Lauge, P., Jean, O.L., xe, re, 1994. Nutrient Retention in Riparian  
817 Ecotones. *Ambio* 23, 342-348.

818 Maes, J., Egoh, B., Willemen, L., Liqueste, C., Vihervaara, P., Schägner, J.P., Grizzetti, B., Drakou, E.G.,  
819 Notte, A.L., Zulian, G., Bouraoui, F., Luisa Paracchini, M., Braat, L., Bidoglio, G., 2012. Mapping  
820 ecosystem services for policy support and decision making in the European Union. *Ecosystem*  
821 *Services* 1, 31-39.

822 Malinga, R., Gordon, L.J., Jewitt, G., Lindborg, R., 2015. Mapping ecosystem services across scales  
823 and continents – A review. *Ecosystem Services* 13, 57-63.

824 Martínez-Harms, M.J., Balvanera, P., 2012. Methods for mapping ecosystem service supply: a review.  
825 *International Journal of Biodiversity Science, Ecosystem Services & Management* 8, 17-25.

826 May, L., House, W.A., Bowes, M., McEvoy, J., 2001. Seasonal export of phosphorus from a lowland  
827 catchment: upper River Cherwell in Oxfordshire, England. *Science of the total environment* 269, 117-  
828 130.

829 May, L., Place, C.J., George, D.G., McEvoy, J., 1996. An Assessment of the Nutrient Loadings from the  
830 Catchment to Bassenthwaite Lake, In Report to the Environment Agency. p. 54 pp, North West  
831 Region.

832 McGuckin, S.O., Jordan, C., Smith, R.V., 1999. Deriving phosphorus export coefficients for corine land  
833 cover types. *Water Science and Technology* 39, 47-53.

834 Meals, D.W., Richards, R.P., Dressing, S.A., 2013. Pollutant load estimation for water quality  
835 monitoring projects., In Tech Notes. Developed for U.S. Environmental Protection Agency by Tetra  
836 Tech, Inc., Fairfax, VA.

837 Moore, R., Morris, D., Flavin, R., 1994. Sub-set of UK digital 1: 50,000 scale river centre-line network.  
838 NERC, Institute of Hydrology, Wallingford.

839 Morris, D.G., Flavin, R.W., 1990. A Digital Terrain Model for Hydrology, In Proc 4th Int. Symposium  
840 on Spatial Data Handling. pp. 250-262, Zurich.

841 Morton, D., Rowland, C., Wood, C., Meek, L., Marston, C., Smith, G., Simpson, I.C., 2011. Final report  
842 for LCM2007 - the new UK land cover map. , p. 112pp. NERC/Centre for Ecology and Hydrology.

843 Naden, P., Bell, V., Carnell, E., Tomlinson, S., Dragosits, U., Chaplow, J., May, L., Tipping, E., 2016.  
844 Nutrient fluxes from domestic wastewater: a national-scale historical perspective for the UK 1800–  
845 2010. *Science of the total environment*.

846 Nedwell, D.B., Dong, L.F., Sage, A., Underwood, G.J.C., 2002. Variations of the Nutrients Loads to the  
847 Mainland U.K. Estuaries: Correlation with Catchment Areas, Urbanization and Coastal  
848 Eutrophication. *Estuarine, Coastal and Shelf Science* 54, 951-970.

849 Nelson, E., Mendoza, G., Regetz, J., Polasky, S., Tallis, H., Cameron, D., Chan, K.M.A., Daily, G.C.,  
850 Goldstein, J., Kareiva, P.M., Lonsdorf, E., Naidoo, R., Ricketts, T.H., Shaw, M., 2009. Modeling  
851 multiple ecosystem services, biodiversity conservation, commodity production, and tradeoffs at  
852 landscape scales. *Frontiers in Ecology and the Environment* 7, 4-11.

853 Pandeya, B., Buytaert, W., Zulkafli, Z., Karpouzoglou, T., Mao, F., Hannah, D., 2016. A comparative  
854 analysis of ecosystem services valuation approaches for application at the local scale and in data  
855 scarce regions. *Ecosystem Services* 22, 250-259.

856 Parn, J., Pinay, G., Mander, U., 2012. Indicators of nutrients transport from agricultural catchments  
857 under temperate climate: A review. *Ecological Indicators* 22, 4-15.

858 Perry, M., Hollis, D., 2005. The generation of monthly gridded datasets for a range of climatic  
859 variables over the UK. *International Journal of Climatology* 25, 1041-1054.

860 Pessacg, N., Flaherty, S., Brandizi, L., Solman, S., Pascual, M., 2015. Getting water right: A case study  
861 in water yield modelling based on precipitation data. *Science of the total environment* 537, 225-234.

862 Quilbé, R., Rousseau, A.N., Duchemin, M., Poulin, A., Gangbazo, G., Villeneuve, J.-P., 2006. Selecting  
863 a calculation method to estimate sediment and nutrient loads in streams: Application to the  
864 Beaurivage River (Québec, Canada). *Journal of Hydrology* 326, 295-310.

865 R Core Team, 2014. R: A language and environment for statistical computing. R Foundation for  
866 Statistical Computing, Vienna, Austria.

867 Redhead, J., Stratford, C., Sharps, K., Jones, L., Ziv, G., Clarke, D., Oliver, T., Bullock, J., 2016. Empirical  
868 validation of the InVEST water yield ecosystem service model at a national scale. *Science of the total  
869 environment* 569, 1418-1426.

870 Richards, R.P., Holloway, J., 1987. Monte Carlo studies of sampling strategies for estimating tributary  
871 loads. *Water Resources Research* 23, 1939-1948.

872 Sánchez-Canales, M., López Benito, A., Passuello, A., Terrado, M., Ziv, G., Acuña, V., Schuhmacher,  
873 M., Elorza, F.J., 2012. Sensitivity analysis of ecosystem service valuation in a Mediterranean  
874 watershed. *Science of the total environment* 440, 140-153.

875 Saunders, D.L., Kalff, J., 2001. Nitrogen retention in wetlands, lakes and rivers. *Hydrobiologia* 443,  
876 205-212.

877 Schulp, C.J.E., Burkhard, B., Maes, J., Van Vliet, J., Verburg, P.H., 2014. Uncertainties in Ecosystem  
878 Service Maps: A Comparison on the European Scale. *PLoS ONE* 9, e109643.

879 Seppelt, R., Dormann, C.F., Eppink, F.V., Lautenbach, S., Schmidt, S., 2011. A quantitative review of  
880 ecosystem service studies: approaches, shortcomings and the road ahead. *Journal of Applied  
881 Ecology* 48, 630-636.

882 Sharp, R., Tallis, H.T., Ricketts, T., Guerry, A.D., Wood, S.A., Chaplin-Kramer, R., Nelson, E., Ennaanay,  
883 D., Wolny, S., Olwero, N., Vigerstol, K., Pennington, D., Mendoza, G., Aukema, J., Foster, J., Forrest,  
884 J., Cameron, D., Arkema, K., Lonsdorf, E., Kennedy, C., Verutes, G., Kim, C.K., Guannel, G., Papefnus,  
885 M., Toft, J., Marsik, M., Bernhardt, J., Griffin, R., Glowinski, K., Chaumont, N., Perelman, A., Lacayo,  
886 M., Mandle, L., Hamel, P., Vogl, A.L., Rogers, L., Bierbower, W., 2015. InVEST 3.2.0 User's Guide. The  
887 Natural Capital Project, Stanford.

888 Sharp, R., Tallis, H.T., Ricketts, T., Guerry, A.D., Wood, S.A., Chaplin-Kramer, R., Nelson, E., Ennaanay,  
889 D., Wolny, S., Olwero, N., Vigerstol, K., Pennington, D., Mendoza, G., Aukema, J., Foster, J., Forrest,  
890 J., Cameron, D., Arkema, K., Lonsdorf, E., Kennedy, C., Verutes, G., Kim, C.K., Guannel, G., Papenfus,  
891 M., Toft, J., Marsik, M., Bernhardt, J., Griffin, R., Glowinski, K., Chaumont, N., Perelman, A., Lacayo,  
892 M., Mandle, L., Hamel, P., Vogl, A.L., Rogers, L., Bierbower, W., 2016. InVEST 3.3.0 User's Guide. The  
893 Natural Capital Project, Stanford University, University of Minnesota, The Nature Conservancy and  
894 World Wildlife Fund, Stanford.

895 Sharps, K., Masante, D., Thomas, A., Jackson, B., Redhead, J., May, L., Prosser, H., Cosby, B., Emmett,  
896 B., Jones, L., 2017. Comparing strengths and weaknesses of three ecosystem services modelling tools  
897 in a diverse UK river catchment. *Science of the total environment* 584–585, 118-130.

898 Shepherd, B., Harper, D., Millington, A., 1999. Modelling catchment-scale nutrient transport to  
899 watercourses in the U.K. *Hydrobiologia* 395, 227-238.

900 Shi, J., Davis, R., Densham, J., 2006. Better Land for Better Water: Modelling land-use change to  
901 improve water quality in England. RSPB/ WWF/ Water UK.

902 Smith, R.V., Jordan, C., Annett, J.A., 2005. A phosphorus budget for Northern Ireland: inputs to  
903 inland and coastal waters. *Journal of Hydrology* 304, 193-202.

904 Tague, C.L., Band, L.E., 2004. RHESSys: Regional Hydro-Ecologic Simulation System—An Object-  
905 Oriented Approach to Spatially Distributed Modeling of Carbon, Water, and Nutrient Cycling. *Earth*  
906 *Interactions* 8, 1-42.

907 Tallis, H., Kareiva, P., Marvier, M., Chang, A., 2008. An ecosystem services framework to support  
908 both practical conservation and economic development. *Proceedings of the National Academy of*  
909 *Sciences* 105, 9457-9464.

910 Tanguy, M., Dixon, H., Prosdociimi, I., Morris, D., Keller, V., 2014. Gridded estimates of daily and  
911 monthly areal rainfall for the United Kingdom (1890–2012)[CEH-GEAR]. NERC Environmental  
912 Information Data Centre.

913 Terrado, M., Acuña, V., Ennaanay, D., Tallis, H., Sabater, S., 2014. Impact of climate extremes on  
914 hydrological ecosystem services in a heavily humanized Mediterranean basin. *Ecological Indicators*  
915 37, 199-209.

916 Vigerstol, K.L., Aukema, J.E., 2011. A comparison of tools for modeling freshwater ecosystem  
917 services. *Journal of Environmental Management* 92, 2403-2409.

918 Villa, F., Voigt, B., Erickson, J.D., 2014. New perspectives in ecosystem services science as  
919 instruments to understand environmental securities. *Philosophical Transactions of the Royal Society*  
920 *of London B: Biological Sciences* 369, 20120286.

921 Wilby, R.L., Orr, H.G., Hedger, M., Forrow, D., Blackmore, M., 2006. Risks posed by climate change to  
922 the delivery of Water Framework Directive objectives in the UK. *Environment International* 32, 1043-  
923 1055.

924 Willcock, S., Hooftman, D., Sitas, N., O'Farrell, P., Hudson, M.D., Reyers, B., Eigenbrod, F., Bullock,  
925 J.M., 2016. Do ecosystem service maps and models meet stakeholders' needs? A preliminary survey  
926 across sub-Saharan Africa. *Ecosystem Services* 18, 110-117.

927 Williams, R.J., Keller, V.D.J., Johnson, A.C., Young, A.R., Holmes, M.G.R., Wells, C., Gross-Sorokin, M.,  
928 Benstead, R., 2009. A national risk assessment for intersex in fish arising from steroid estrogens.  
929 *Environmental Toxicology and Chemistry* 28, 220-230.

930 Withers, P.J., Jordan, P., May, L., Jarvie, H.P., Deal, N.E., 2014. Do septic tank systems pose a hidden  
931 threat to water quality? *Frontiers in Ecology and the Environment* 12, 123-130.

932 Withers, P.J.A., Lord, E.I., 2002. Agricultural nutrient inputs to rivers and groundwaters in the UK:  
933 policy, environmental management and research needs. *Science of the total environment* 282, 9-24.

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