Local inertial oscillations in the surface ocean generated by

time-varying winds

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Abstract

Following a review on the generation of inertial oscillations in the surface ocean, a new relationship describing the evolution of locally generated inertial oscillations, subject to time-varying wind stress, is presented. The inertial oscillation is expressed as the superposition of a previous oscillation and a newly generated oscillation, which depends upon the time-varying wind stress. This relationship is employed to investigate some idealized wind change events. For a wind series varying temporally with different rates, the induced inertial oscillation is dominated by the wind with the greatest variation. The resonant wind, which rotates anti-cyclonically at the local inertial frequency with time, produces maximal amplitude of inertial oscillations, which grows monotonically. For the wind rotating at non-inertial frequencies, the responses vary periodically, with wind injecting inertial energy when it is in phase with the currents, but removing inertial energy when it is out of phase. The wind rotating anti-cyclonically with time is much more favorable to generate inertial oscillations than the cyclonic rotating wind. The wind with a frequency closer to the inertial frequency generates stronger inertial oscillations. For a diurnal wind, the induced inertial oscillation is dependent on latitude and is most significant at 30 °. This relationship is also applied to examine idealized moving cyclones. The inertial oscillation is much stronger on the right hand side of the cyclone path than on the left hand side (in the northern hemisphere). This is due to the wind being anti-cyclonic with time on the right hand side, but cyclonic on the other side. The inertial oscillation varies with the cyclone translation speed. The optimal translation speed generating greatest inertial oscillations is 2 m/s at the latitude of 10 °, and gradually increases to 6 m/s at the latitude of 30 °.

Keywords: inertial oscillations, wind, cyclone

1. Introduction

Historic observations report energetic inertial oscillations being generated in the ocean during the passage of storms (e.g., Saelen 1963; Day and Webster 1965; Hunkins 1967; Webster 1968). A linear wind-driven model with a decay term can reproduce the amplitude, phase and intermittency of observed inertial oscillations in the mixed layer very well, suggesting that the inertial response is predominantly locally generated by sea surface winds (Pollard and Millard 1970).

The resonant wind, which rotates anti-cyclonically with the local inertial frequency at a fixed location, can generate very strong inertial oscillations (Crawford and Large 1996; Skyllingstad et al. 2000). In practice, however, the wind is usually non-resonant. A sudden wind change can also be effective at generating inertial oscillations (Pollard 1970), which has been frequently observed during the passage of atmospheric fronts and tropical cyclones (e.g., D’Asaro 1985; Shay and Elsberry 1987; Zheng et al. 2006; Sun et al. 2011). There are many other types of wind change events that result in inertial oscillations that have not been reported and discussed. For example, some wind change events, though dramatic, may only generate weak inertial oscillations. Thus a systematic review on different types of wind change events is necessary and helpful, and will be the main topic of this paper.

In our study, a direct relationship between inertial oscillations and changes of the wind stress is derived from a linear model (Section 2). The relationship is then employed to discuss the effect of several idealized types of wind events (Section 3), namely, the wind varying at different rates; the winds rotating anti-cyclonically or cyclonically at different frequencies with time; and the diurnal wind. We also apply this relationship to interpret effects of an idealized cyclone and the dependence on parameters of the cyclone (Section 4). The summary is presented in Section 5.

2. A Simple Linear Model of Inertial Oscillations

An inertial current in the mixed layer can be well simulated by a linear slab model (Pollard and Millard 1970):

 (1)

where the current (u, written in a complex form) and the wind stress (τ) are assumed uniform in the mixed layer (with a thickness of *H*). The inertial frequency is denoted by *f*, and the seawater density by *ρ*, which are both taken as constants. The damping coefficient *r* that is an inverse of the e-folding decay time parameterizes damping processes. Naturally this linear model does not fully represent inertial processes. For example without a pressure gradient term, it is a single-point model in which there is no interaction between points at nearby positions and only local processes are considered. Furthermore the slab nature assumes an instantaneous vertical propagation of information throughout the slab. Nevertheless, it can generally well reproduce amplitude and phase of inertial oscillations in the mixed layer (Pollard and Millard 1970; Kundu 1976; Pollard 1980). It has also been widely used to calculate the inertial energy flux from the wind (D’Asaro 1985; Alford 2001; Watanabe and Hibiya 2002; Alford 2003; Mickett et al. 2010).

The Eq. (1) can be written as:

 (2)

where

 (3)

The solution of Eq. (2) is

 (4)

where C is the value determined by the initial condition. Integration by parts gives

 (5)

On the right-hand side of Eq. (5), the second term is the instantaneous Ekman ‘steady’ transport. Since ω is the sum of *if* and *r*, the Ekman transport is not exactly at 90 degrees to the wind direction, as the friction term has a veering effect. The other two terms are both related to inertial oscillations. The first term represents the initial condition of the existing inertial oscillation and can be associated with a pre-existing inertial oscillation. The third term is associated with the inertial oscillation that is newly generated by the evolving wind stress. Note that the third term vanishes under the condition that no change in wind stress occurs, i.e., for steady wind stress, whereby pre-existing inertial oscillations are preserved.

For a sufficiently short time interval *∆t*, the wind stress can be approximated as piecewise linear, with a constant rate of change,

 (6)

where **A**nis a complex value. Substitution of An into Eq. (5) yields the velocity expression during the period (*t n ≤*  *t ≤ tn+1*)

 (7)

where Cnis the corresponding initial value. For convenience, the inertial terms are collected and denoted by In,

 (8a)

where

 (8b)

Similarly, the velocity during the previous interval, *tn-1 ≤ t ≤ tn*, is

 (9a)

where

 (9b)

Assuming the flow is piecewise continuous at the time *t*=*tn*, the velocity expressed in Eq. (8a) equals to that in Eq. (9a) when *t*=*tn*. Therefore,

 (10)

i.e.,

 (11)

which reveals that the inertial oscillation is composed of two parts. The first part depends on the forcing and solution of the previous interval (which decays at a rate given by the coefficient *r,* whilst turning anti-cyclonically by an angle of *f∆t*). The second part is due to the acceleration of wind stress. The relative size of these two parts varies with time, and the magnitude of the total inertial response depends on their relative magnitude and phase. As long as the time series of wind stress is known, Equation (11) can be easily employed to iteratively calculate the inertial response. This has been verified with real winds, reproducing the observed near-inertial motion well, especially during the period with relatively strong wind (Chen 2014).

3. Tests for Idealized Varying Wind Scenarios

In this section, Equation (11) is used to investigate the variation of inertial oscillations induced by some idealized types of wind change events. For convenience, Equation (11) is rewritten in the following form:

 (12a)

 (12b)

 (12c)

where Pn represents the pre-existing inertial oscillation, and Nn the newly wind-driven inertial oscillation. The damping coefficient (*r*) is set as a typical value of (4 day)-1 (D’Asaro 1985). The mixed layer depth is assumed to be 50 m. The inertial frequency (*f*) is 10-4 rad/s (corresponding to the latitude of 43.4 ºN). The time step is one hour. These values remain unchanged in all cases for this section.

3.1. Wind with Unchanged Direction

A simple case to consider is when wind only changes in magnitude. As seen in Fig. 1a, the wind examined is taken as eastward. For the first hour the speed increases from 0 to 5 m/s (corresponding to a wind stress of 0.04 N/m2, using the wind drag coefficient of Large and Pond (1981)), and increases from 5 m/s to 12 m/s (corresponding to 0.22 N/m2) for the second hour, and is then maintained at 12 m/s. The associated wind stress has the greatest rate of change during the second hour. Figures. 1b and 1c show the components of the resulting inertial oscillation.

For the first hour, an oscillation I1 is generated. At *t*=1hour, I1 has rotated clockwise by an angle of *f∆t* and decayed by a factor of *e-r∆t* to become P2 (Eq. (12b) and Fig. 1b). At the same time a change of the wind stress induced a new oscillation N2 of which the magnitude is proportional to the acceleration of wind stress (Eq. (12c)). Since the rate of wind change during the second hour is much greater than that of the first hour (i.e., *|*A2*|*>*|*A1*|*), the new oscillation N2 is mainly determined by A2. The oscillation at *t*=1 hour is the superposition of P2 and N2 (i.e., I2). At *t*=2 hour, I2 has rotated clockwise and decayed to be P3(Fig. 1c). The newly generated N3 is still quite strong, due to a greater rate of wind change A2. The superposition of P3 and N3 is I3. If the wind remains unchanged after *t=*3 hour, the new oscillation component, N4, will be zero. The remaining oscillation I3 will rotate freely and decay gradually. During this whole period, the resulting inertial oscillation is most strongly influenced by the period of steepest wind trend during the second hour. Therefore, for a general period with varying wind, the inertial oscillation generated is likely to be dominated by the period when the wind was most rapidly changing.

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Fig. 1. Variation of wind stress with time (a) and induced inertial oscillations plotted in the complex plane for the first two hours (b) and the third hour (c). The meaning of each abbreviation is as in Eq. (12).

3.2. Winds Rotating Anti-cyclonically

The resonant wind, i.e. rotating anti-cyclonically and at the local inertial frequency, has been reported to produce the maximum inertial energy (Crawford and Large 1996; Skyllingstad et al. 2000). Here we investigate how the inertial energy is built up by the resonant wind.

Figure 2a shows the time series of wind stress at hourly intervals. It rotates anti-cyclonically at the inertial frequency, with a constant wind speed of 18 m/s (i.e., 0.66 N/m2, this value is used in all cases of rotating wind in Sections 3.2 and 3.3). During the first hour an inertial oscillation I1 is produced. At *t*=1 hour (Fig. 2b), I1 has rotated by an angle of -*f∆t* to become P2, which combines with the newly generated oscillation N2to give I2. Since the angle between P2 and N2is acute, their combination I2 has a larger magnitude than either P2 or N2. The same situation occurs in the following time steps (Figs. 2c and 2d). In this way the inertial oscillation increases monotonically with time (Figs. 2e and 2f).

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Fig. 2. (a) Rotation of wind stress with time, starting eastward. The inertial oscillations plotted in the complex plane for the first two hours (b), the third hour (d) and the fourth hour (d). (e, f) Time-varying inertial oscillations. The meaning of each abbreviation is as in Eq. (12).

In practice, the wind will not usually rotate at the inertial frequency. Figure 3a illustrates cases where winds of constant amplitude rotate with other frequencies. Of all cases only the resonant wind maintains a persistently growing inertial oscillation. The response varies at the period of 2π/*|α*+*f|* (cf. Section 3.4 for a detailed discussion), where *α* and *f* are the wind frequency and the inertial frequency, respectively*.* The oscillation of the response arises as the wind adds, and then removes, energy from the mixed layer as the wind and mixed layer motion move in and out of phase with each other. The responses of higher frequency winds (|*α|*>*|f|*) are much greater than those of lower frequency winds (|*α|*<*|f|*) due to greater rates of wind change (as discussed in 3.1). Initially, the growth rate of the response to high frequency winds even exceeds the growth rate of the resonant wind. The case of *α*=-1.25*f* has stronger response than that of *α*=-1.5*f*, and the oscillation for *α*=-0.75*f* is stronger than that for *α*=-0.5*f*. This indicates that the winds with frequencies closer to the inertial frequency can generate more energetic inertial oscillations, consistent with intuition.

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Fig. 3. Inertial oscillations generated by anti-cyclonically rotating winds (a) and by cyclonically rotating winds (b). *α* is the wind frequency and *f*  is the inertial frequency.

3.3. Winds Rotating Cyclonically

For a wind that rotates cyclonically at the inertial frequency, the evolution of the induced inertial oscillation is shown in Fig. 4. At the first hour, an oscillation I1 is generated (Fig. 4b). When *t*=1 hour, I1 has rotated clockwise by an angle of *f∆t* to become P2, and a new oscillation N2 is produced. Since the angle between P2and N2is greater than 90 degree and they have comparable magnitudes, their superposition is smaller than the previous oscillation, i.e., |I2|<|I1|. It is the same case at *t*=2 hour (Fig. 4c). In this way the inertial energy is gradually removed by the wind. Overall the amplitude varies at a period of π/*f* (Fig. 4d) while its phase change does not exhibit a gradual rotation like that induced by resonant wind. The inertial oscillation in this case is much weaker than that generated by the resonant wind.

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Fig. 4. (a) Rotation of wind stress with time, starting eastward. The inertial oscillations plotted in the complex plane for the first two hours (b) and the third hour (c). (d) The variation of the inertial oscillation with time. The meaning of each abbreviation is denoted as in Eq. (12).

Also examined are the cyclonic winds at other frequencies (Fig.3b). All the responses vary periodically (*T*=2π/*|α*+*f|*) and decay gradually. The wind with higher frequency can produce stronger inertial oscillations. However, compared with the cases of anti-cyclonic winds (Fig.3a), the responses are much smaller. Evidently, therefore, the rotation direction of the wind plays a key role during the transfer of wind energy into inertial oscillations.

3.4. Mathematical Interpretation of the Response of Rotating Winds

The inertial oscillation associated with rotating wind can also be explored mathematically. A wind rotating with a constant amplitude (*B*) and at a constant frequency (*α*)takes a form as:

 (13)

Substitution in Eq. (5) gives

 (14)

Assume the current moves from rest, i.e. when *t*=0, u=0, which is applied to Eq. (14), yielding

 (15)

The first two terms (with square brackets) in Eq. (15) are associated with inertial oscillations. The magnitude of the first term depends upon the wind magnitude. The second term is the product of three parts (with round brackets). The first part is the same as the first term. The other two parts (named Cα and Ct) take the forms as follows:

 (16)

 (17)

It shows Ct varies at a period of 2π/*|α*+*f|*, which explains the periodic tendency mentioned in Sections 3.2 and 3.3. Assuming *f* is fixed (10-4 rad/s), the magnitude of Cα is shown as a function of *f/α* in Fig. 5. Cα is symmetric along *f/α*=-1, where the major peak occurs and corresponds to the resonant wind case. The closer *f/α* tend to negative unity, the greater the magnitude becomes. This explains why the wind with a frequency closer to the inertial frequency can generate stronger inertial oscillations. Also it is evident that anti-cyclonic winds (*f/α*<0) have much larger values of Cα than cyclonic winds (*f/α*>0) and, therefore, produce much more energetic inertial oscillation.

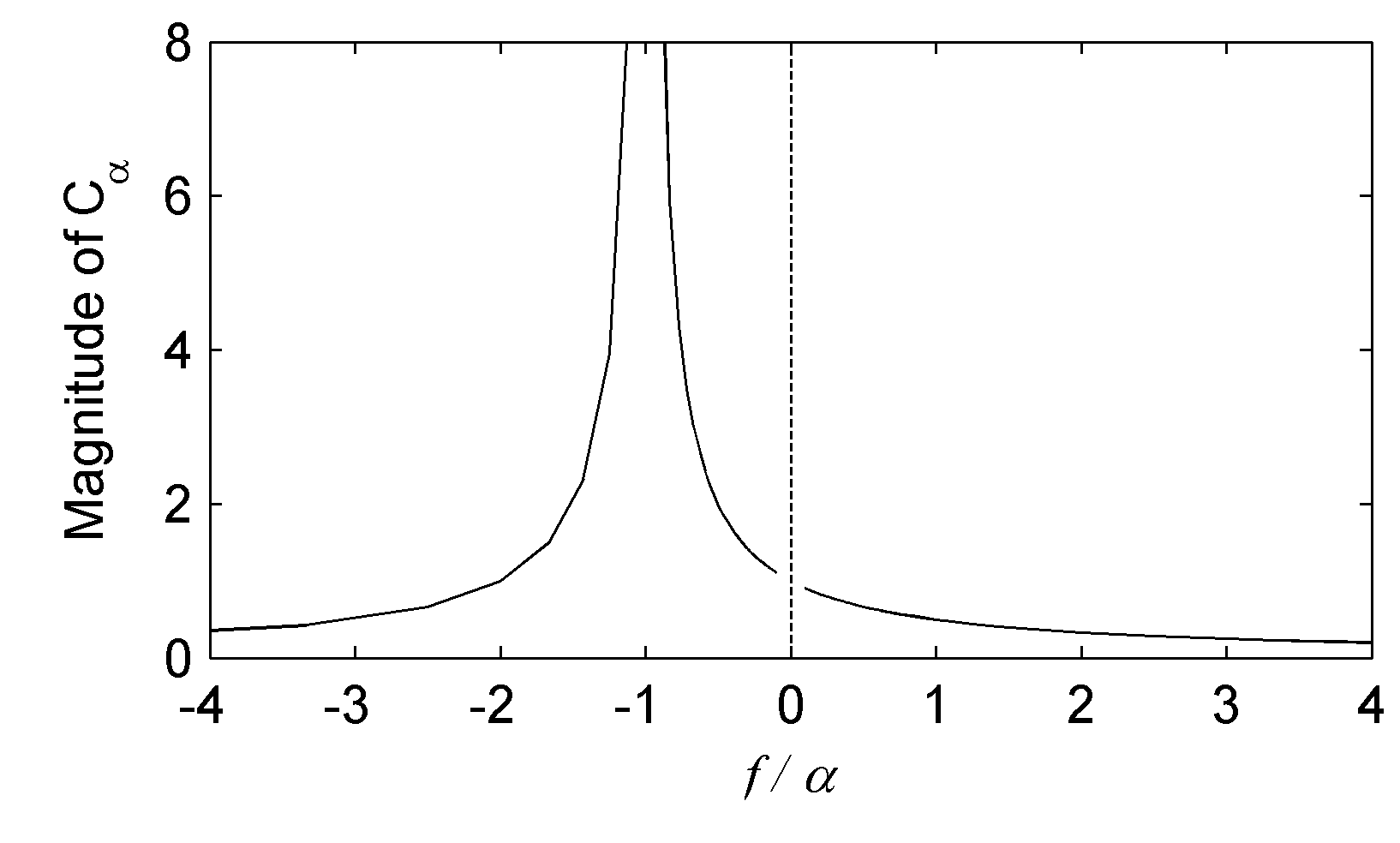


Fig. 5. The magnitude of Cα as a function of *f/*α. The inertial frequency *f* is a constant of 10-4 rad/s. Positive values of *f/*α correspond to cyclonic winds, and negative values are for anti-cyclonic winds.

3.5. Diurnal Winds

In coastal regions, the across-shore temperature gradient changes its sign over the course of the day and commonly drives a diurnal wind - the sea breeze (Simpson 1994). Theoretically, the diurnal wind could generate significant inertial oscillations (Craig 1989; Ingel 2015), which have been reported in both ocean (e.g., Simpson et al. 2002; Zhang et al. 2009; Hyder et al. 2011; Dippe et al. 2015) and atmosphere (Stockwell et al. 2004; Shibuya et al. 2014). Here the inertial oscillation in the surface ocean produced by diurnal winds is investigated.

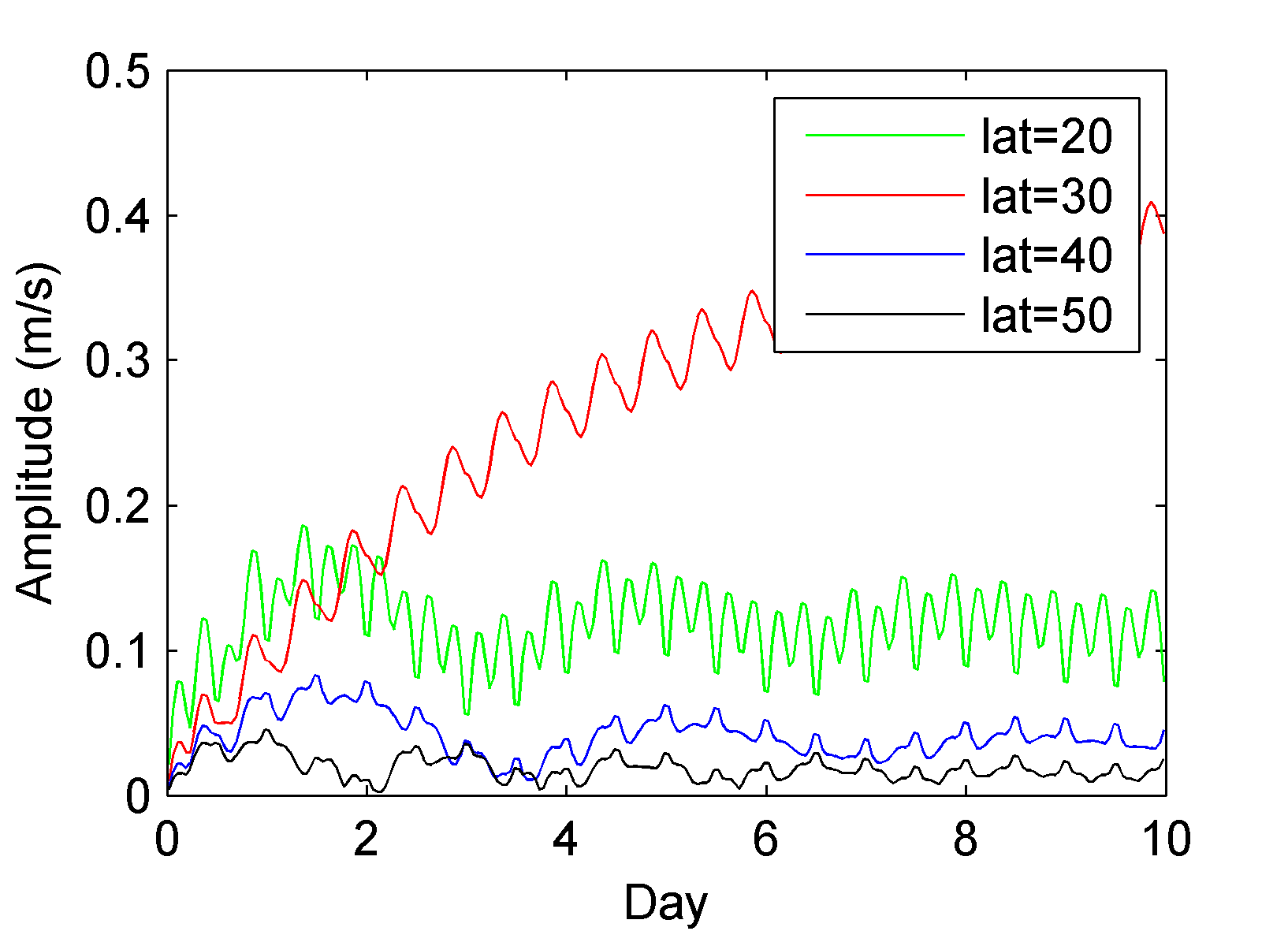


Fig. 6. The amplitude of inertial oscillations generated by diurnal winds at different latitudes.

The wind is set to vary as a sine function with a period of 24 hours and an amplitude of 10 m/s. The induced inertial oscillation is evidently dependent on latitude (Fig. 6). When the latitude is 30 °, such that the inertial frequency (*f*) equals the diurnal frequency, the inertial oscillation grows unboundedly. At a lower latitude of 20 °, the response is comparable with the case of 30 ° in the first two days, but becomes smaller later on. The responses at higher latitudes (40 °and 50 °) are small, even much weaker than the case of 20 °. This is because the wind frequency is greater than the inertial frequency at lower latitude, however, smaller than the inertial frequency at higher latitude. In reality, inertial oscillations in the shelf region are usually damped by friction. For the seas near the latitude of 30 ° where this suppressing effect is weak, the inertial oscillation generated by diurnal wind could be significant.

4. Application to Idealized Cyclones

It is well known that the passage of a cyclone can generate intense inertial oscillations (e.g., Price 1981; Zheng et al. 2006; Sun et al. 2011). In this section, we first investigate the structure of cyclone-induced inertial oscillations. Then the dependence on cyclone parameters (translation speed, occurring latitude, maximum wind radius) is discussed.

Assume the cyclone moves eastward along the middle line of a rectangle region (1200 km × 600 km). The wind field used is idealized (Chang and Anthes 1978). The wind stress varies linearly with distance and does not contain asymmetry. The radial () and tangential () stresses are:

 (18a)

 (18b)

where *r* is the distance away from the cyclone centre, *R1* the radius of maximum wind and *R2* the radius to the cyclone edge. and are the maximum radial and tangential wind stress, respectively. The time series of wind stress for each position is used to compute inertial oscillations by Eq. (11), where the damping coefficient (*r*) and the mixed layer depth (*H*) are set as (4 day)-1 and 50 m, respectively.

4.1 An Initial Case

In this case, the cyclone moves at a speed of 5 m/s. Other wind parameters are set as: *R1*=50 km, *R2*=300 km, =1.0 N/m2, =3.0 N/m2. The inertial frequency is uniform (5×10-5 rad∙s-1, corresponding to a latitude of 20 ºN).

As seen in Fig. 7, the induced inertial oscillation is intense near the cyclone centre. It is much greater on the right hand side of cyclone’s path (y<0) than on the left hand side (y>0). The highest value occurs near the radius of maximum wind. A similar right-bias temperature cooling after a cyclone passage is a well-known phenomenon (e.g., Chang and Anthes 1978). Price (1981) attributes it to the asymmetry of near-inertial motions, which can induce enhanced mixing.

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Fig. 7. The horizontal distribution of the inertial oscillation amplitude (m/s) when the cyclone centre (the white circle) is located at x=*R2*. The pink lines are the radius of maximum wind (y=±50 km). The coordinates are scaled by the cyclone radius (300 km).

The asymmetry in the inertial response is due to different rotation directions of the wind, as has already been shown by Price (1981) for the case of a hurricane. Here the winds at different positions are investigated in detail (Fig. 8). The wind on the right hand side (y<0, Figs. 8c and 8d) along the cyclone’s path rotates anti-cyclonically with time, whereas the wind on the left hand side (y>0, Figs. 8a and 8b) is cyclonic. It has been shown in Section 3 how the anti-cyclonic wind produces much larger inertial oscillation than the cyclonic wind. Note that the wind rotates at a varying frequency, which increases with proximity to the cyclone centre. This suggests the wind induced by a cyclone will rarely exactly match the resonant frequency of inertial oscillations, though it could possibly be near resonant for a period. The wind magnitude is also time dependent. For the positions outside the radius of maximum wind (Figs. 8a and 8d), the wind reaches its maximum amplitude when the cyclone centre is closest. For the positions inside the radius of maximum wind (Figs. 8b and 8c), local wind maxima are attained twice.

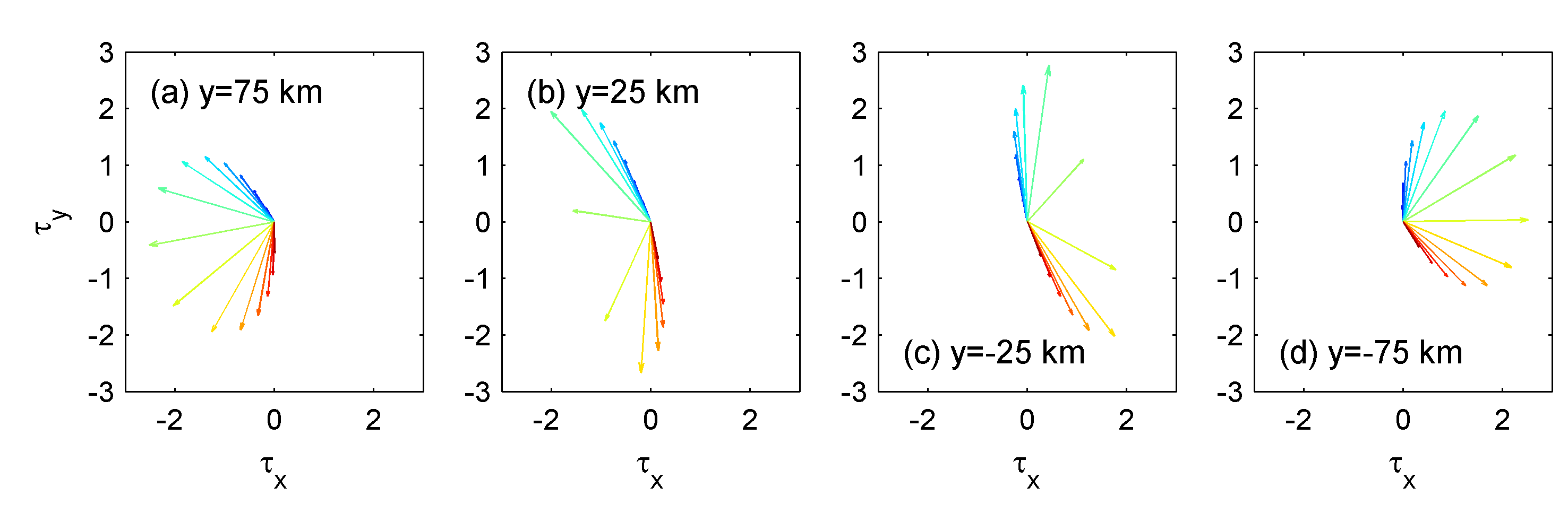


Fig. 8. The wind stress (N/m2) rotating with time at different y positions along the section of x=300 km. Stress vectors are plotted with an interval of 2 hours (shown from blue to red).

4.2 Varying Cyclone Parameters

Previous research suggests that sea surface cooling is enhanced for slow-moving cyclones (e.g., Price 1981; Mei and Pasquero 2013). Firstly we investigate the cyclones with varying translation speeds, ranging from 1 m/s to 12 m/s (12 cases in total). All other parameters are the same as the case in Section 4.1.

When the cyclone moves as slowly as 2 m/s, the induced inertial oscillation is very weak (Fig. 9a). With an increasing translation speed, the amplitude of the inertial oscillation increases (Fig. 9b). This is because a cyclone moving faster generates winds with a higher local rotation frequency. However, when a cyclone moves faster, it also passes the region more quickly, with a less time to influence it, as seen in the case of 8 m/s (Fig. 9c). Thus an optimal translation speed that produces the highest inertial energy levels should be the best match of wind intensity and influence duration. As shown in Fig. 10, for these parameters, the optimal translation speed is found to be around 4 m/s.

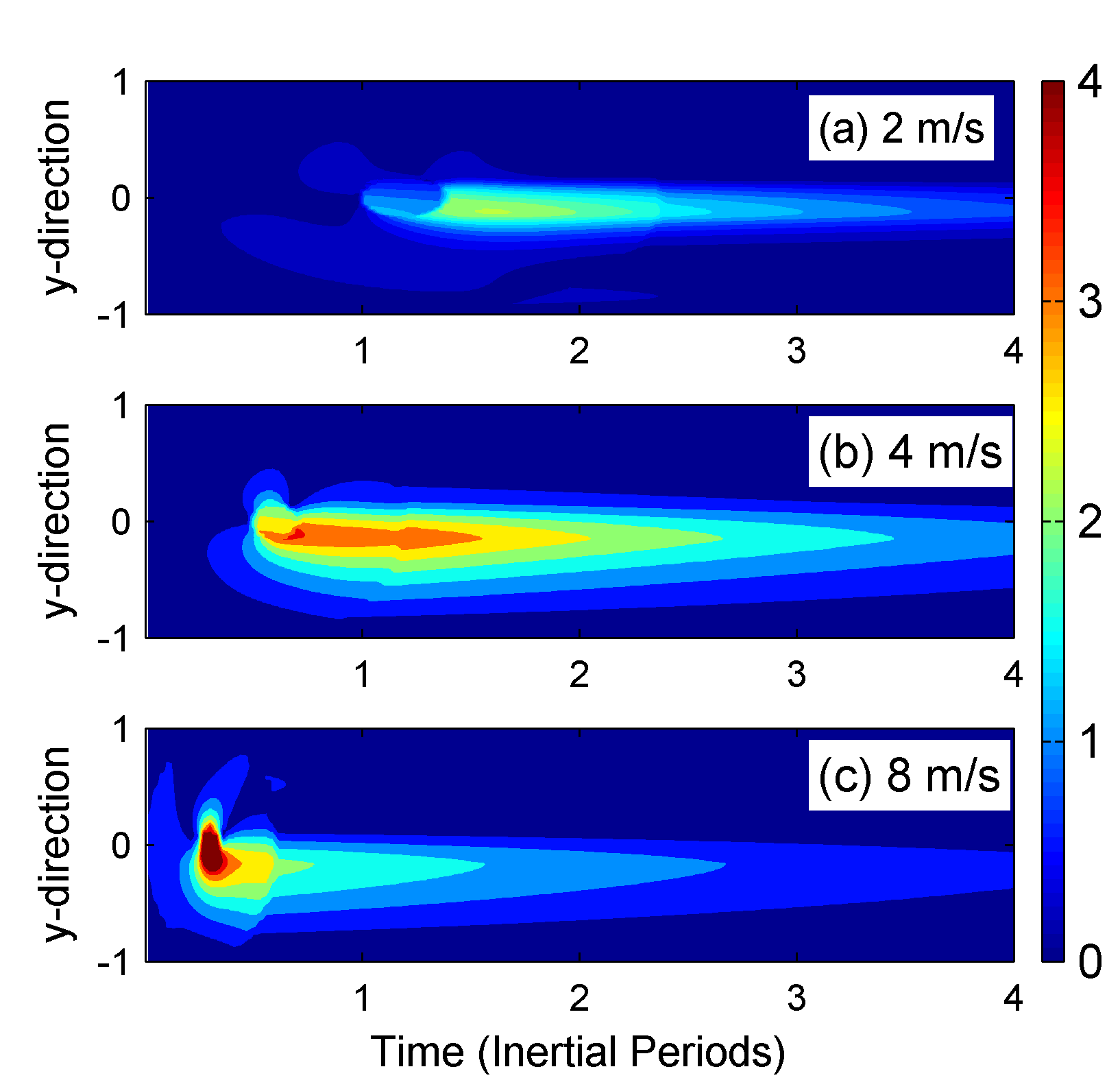


Fig. 9. Time-space (y) distribution of the inertial oscillation (m/s) at the section of x=300 km associated with different translation speeds. The time is scaled by the inertial period and the y space by the cyclone radius (300 km).

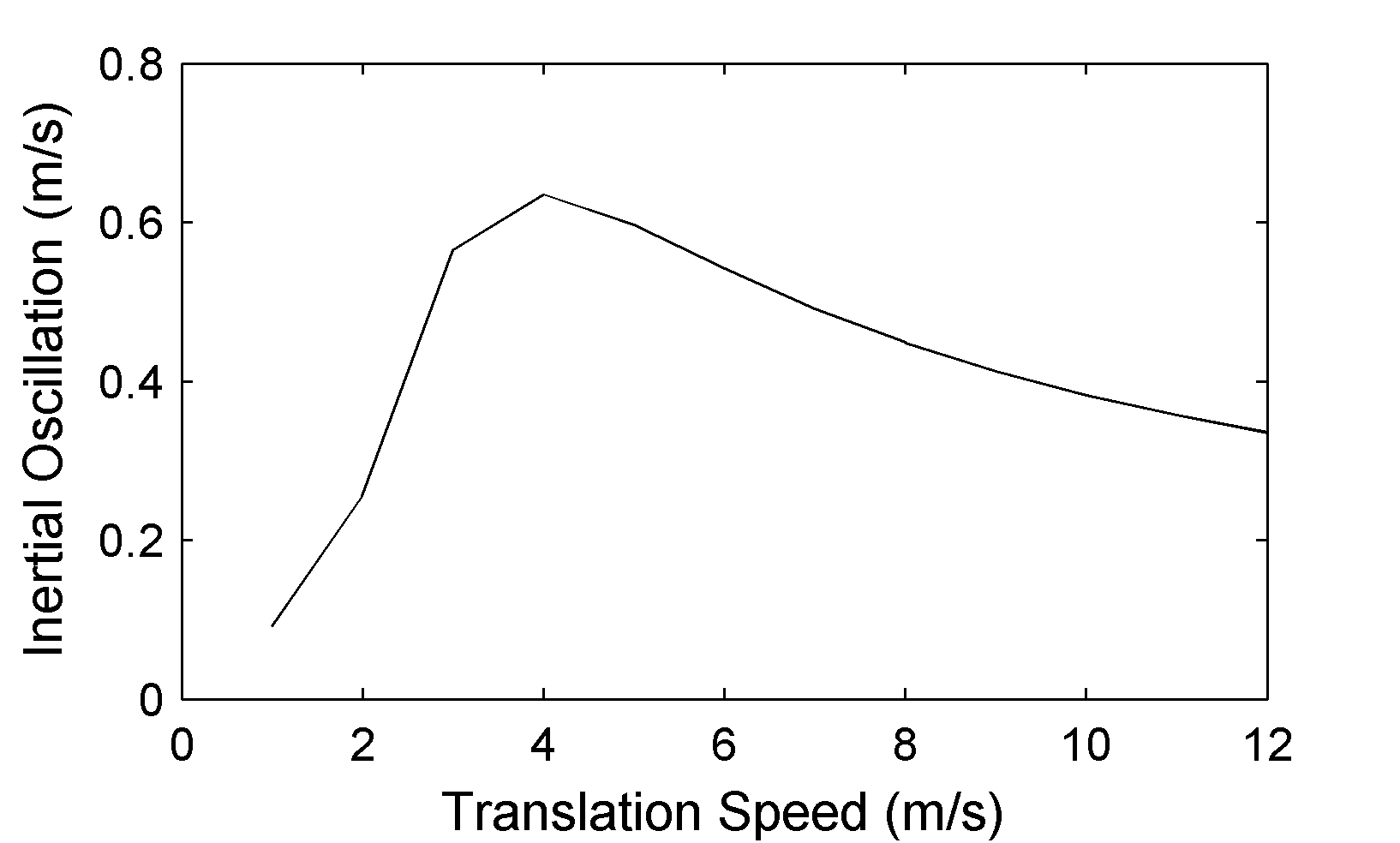


Fig. 10. The mean amplitude of inertial oscillations induced by cyclones with different translation speeds. For each cyclone case with a specific translation speed, a value is obtained by averaging the inertial oscillation at the section x=300 km over the first five inertial periods.

The optimal translation speed is also dependent on the latitude (Fig. 11a). At 10 ºN, the optimal speed is around 2 m/s. With increasing latitude this speed increases gradually and reaches 6 m/s at 30 ºN. The speed increases with latitude as a function of the inertial frequency, since at high latitudes with greater inertial frequencies, a faster translating cyclone is required to generate winds that rotate at a faster rate. However when the radius of maximum wind, *R1*, is changed, the optimal translation speed remains constant at 4 m/s, though the amplitude of the inertial response does increase with the radius of maximum wind, *R1* (Fig. 11b).

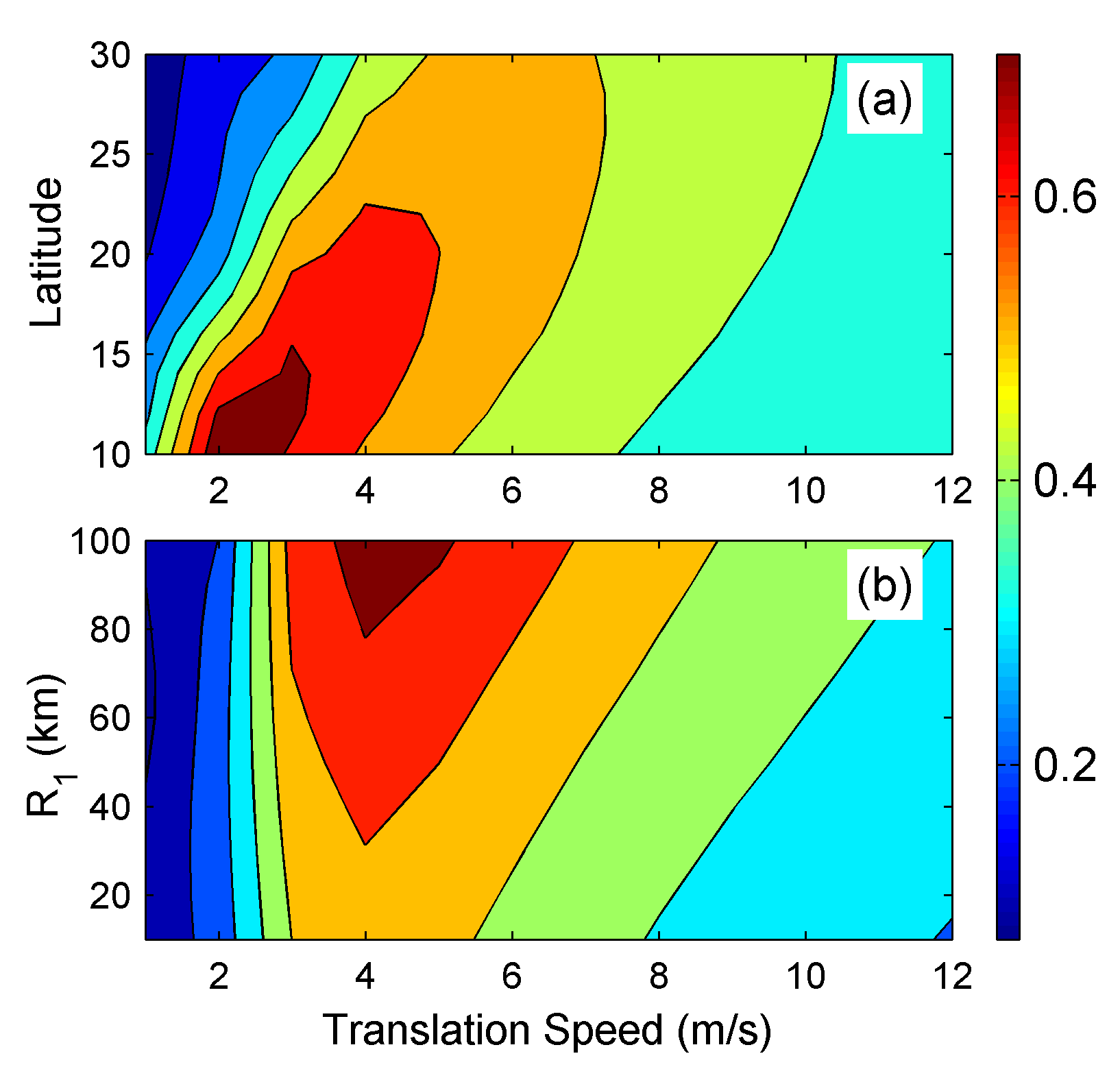


Fig. 11. (a) The mean amplitude of inertial currents (m/s) induced by cyclones with different translation speeds and occurring at different latitudes. For each cyclone case with a specific translation speed and at a specific latitude, a value is obtained by averaging the inertial oscillation at the section x=300 km over the first five inertial periods. (b) The mean amplitude of inertial currents (m/s) induced by cyclones with different translation speeds and different radius of maximum wind. For each cyclone case with a specific translation speed and a specific radius of maximum wind, a value is obtained by averaging the inertial oscillation at the section x=300 km over the first five inertial periods.

5. Summary and Discussion

A new relationship between the amplitude of inertial oscillations and the wind stress is derived from a set of linear momentum equations. The relationship shows that inertial oscillations are determined by the superposition of two parts (Eq. (11)): one is associated with previous inertial motion; the other is newly generated and depends upon the time-varying wind stress.

Using this relationship, the variation of inertial oscillations can be easily calculated from a time-series of wind stress. This relationship is employed to investigate the inertial response to some idealized wind change events. When the wind direction does not change, but the wind magnitude varies at different rates, the resulting inertial oscillation is dominated by the wind from the period with greatest variation.

When the wind is resonant (rotating anti-cyclonically at the inertial frequency with time), the phase difference between the previous oscillation and the new oscillation is always acute. Thus their superposition has greater magnitude than either component. Consequently, a strong inertial oscillation grows monotonically. When the anti-cyclonic wind rotates at other frequencies, a weaker inertial oscillation is generated. The amplitude of inertial oscillation varies at a period of 2π/*|α*+*f|* (where *α* and *f* are the wind frequency and the inertial frequency, respectively), which increases for the first half period, but declines at the second half period. The wind with a frequency closer to inertial frequency can induce stronger inertial oscillations. When the wind rotates cyclonically with time, the inertial oscillation also varies at the period of 2π/*|α*+*f|*, but is much smaller in amplitude compared with that generated by anti-cyclonic winds.

When the wind is diurnal (i.e., sea breeze), the inertial oscillation can also be significant, and is maximal at the latitude of 30 °. However diurnal wind mostly occurs in a coastal region where the dissipation heavily suppress the growth of inertial oscillations. In regions where the dissipation is small, the diurnal wind will probably generate significant inertial oscillations.

The relationship between the time-varying wind stress and its inertial response is also applied to study idealized cyclones. Intense inertial oscillations are located on the right hand side of the cyclone path (in the northern hemisphere). This is because the wind at a fixed point, on this side of the cyclone, rotates anti-cyclonically with time and can phase-lock with the inertial oscillation. However, the wind on the left hand side of the path is cyclonic and can therefore never phase-lock with the inertial oscillation.

Cyclones moving at a speed ranging from 1 m/s to 12 m/s are compared. If the translation speed is reduced, then the amplitude of inertial oscillations is also reduced, though the cyclone can force the ocean for a longer duration. Alternatively, if the translation speed is increased, then the amplitude of inertial oscillations is increased, though the cyclone forces the ocean for a shorter duration. When the translation speed is around 4 m/s, the time average amplitude of inertial oscillation is maximal. This optimal translation speed is dependent on latitude, which is 2 m/s at 10 º, and gradually increases to 6 m/s at 30 º. This is because at higher latitude the inertial frequency is greater, which requires a match of higher wind frequency, and thus a quicker translation speed. If the radius of maximum wind is also variable, then the optimal translation speed is not found to change. However cyclones with a larger radius generates larger amplitudes of inertial oscillations.

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