

1 **Modelling acoustic scattering by suspended flocculating sediments**

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Abstract

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30 The development of a theoretical description of how sound interacts with flocculating
31 sediments has been lacking and this deficiency has impeded sound being used to extract
32 quantitative suspended sediment parameters in suspensions containing flocs. As a step
33 towards theoretically examining this problem a relatively simple heuristic approach has been
34 adopted to provide a description of the interaction of sound with suspensions that undergo
35 flocculation. A model is presented for the interpretation of acoustic scattering from
36 suspensions of fine sediments as they transition from primary particles, through an
37 intermediate regime, to the case where low density flocs dominate the acoustic scattering.
38 The approach is based on modified spherical elastic solid and elastic fluid scatterers and a
39 combination of both. To evaluate the model the variation of density and compressional
40 velocity within the flocs as they form and grow in size is required. The density can be
41 estimated from previous studies; however, the velocity is unknown and is formulated here
42 using a fluid mixture approach. Uncertainties in these parameters can have a significant effect
43 on the predicted scattering characteristics and are therefore investigated in the present study.
44 Further, to assess the proposed model, outputs are compared with recently published
45 laboratory observations of acoustic scattering by flocculating cohesive suspensions.

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47 Key words: Acoustic scattering, suspended cohesive sediments, flocculation, modelling,
48 sediment transport.

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52 **List of main parameters and their units**

53

54 a. Particle radius. (m)

55 a_o . Mean radius based on $n(a)$. (m)

56 c_w . Sound velocity in water. (ms^{-1})

57 c_f . Sound velocity in a fluid scatterer. (ms^{-1})

58 c_s . Sound velocity in the primary particles. (ms^{-1})

59 C_f . Effective density flocculation constant. ($kgm^{(3-m)}$)

60 f . Intrinsic backscatter form function. (-)

61 f_{ss} . Intrinsic backscatter form function for a solid elastic sphere. (-)

62 f_{si} . Intrinsic backscatter form function for an irregularly shaped solid elastic particle. (-)

63 f_{fs} . Intrinsic backscatter form function for a fluid elastic sphere. (-)

64 f_{fi} . Intrinsic backscatter form function for an irregularly shaped fluid elastic scatterer. (-)

65 f_h . Intrinsic hybrid backscatter form function for a scatter of variable density. (-)

66 f_o . Ensemble backscatter form function. (-)

67 f_{ho} . Ensemble hybrid backscatter form function for a scatter of variable density. (-)

68 k . Acoustic wavenumber, $2\pi/\lambda$. (m^{-1})

69 K . Sediment backscattering property. ($kg^{-1/2}m$)

70 m . Exponent to which the particle size is raised to parameterise flocculation.

71 M . The suspended concentration. (kgm^{-3})

72 $n(a)$. Particle number radius probability density function. (-)

73 N . Number of particles per m^3 (m^{-3}).

74 r . Range from the transducer. (m)

75 \mathfrak{R} . The system constant. ($Vm^{3/2}$)

76 V . Root-mean-square backscattered signal. (V)

77 $x=ka$ (-), $x_o=ka_o$ (-)

78 α_w . Attenuation due to water absorption. (Nepers m^{-1})

79 α_s . Attenuation due to sediment scattering and viscous absorption. (Nepers m^{-1})

80 γ . Normalised density of the scatter relative to the density of water. (-)

81 γ_o . Minimum normalised density of the scatter relative to the density of water. (-)

82 δ . Normalised standard deviation σ/a_o of $n(a)$. (-)

83 ϵ . Fluid heuristic formulation coefficients (-)

- 84 ζ . Normalised sound velocity of the scatter relative to the sound velocity in water. (-)
- 85 ζ_0 . Minimum normalised sound velocity of the scatter relative to the sound velocity in water.
- 86 (-)
- 87 κ_w . Compressibility of water. (Pa)
- 88 κ_s . Compressibility of the solid primary particles. (Pa)
- 89 λ . Wavelength of sound. (m)
- 90 ν . Kinematic viscosity (m^2s^{-1})
- 91 ξ . Sediment attenuation constant. (kg^{-1}m^2)
- 92 ρ_w . Density of water. (kgm^{-3})
- 93 ρ . Density of the suspended scatterers. (kgm^{-3})
- 94 ρ_s . Density of the solid primary particles. (kgm^{-3})
- 95 ρ_f . Density of a fluid scatterer. (kgm^{-3})
- 96 ρ_o . Minimum density of the suspended scatterers. (kgm^{-3})
- 97 ρ_e . Effective density of the suspended scatterers. (kgm^{-3})
- 98 σ . Standard deviation of $n(a)$. (m)
- 99 ϕ . Porosity of the suspended scatterer.
- 100 χ . Intrinsic normalised total scattering cross-section. (-)
- 101 χ_{ss} . Intrinsic normalised total scattering cross-section for a solid elastic sphere. (-)
- 102 χ_{sv} . Intrinsic normalised total scattering cross-section for the viscous attenuation of a solid
- 103 elastic sphere. (-)
- 104 χ_{fs} . Intrinsic normalised total scattering cross-section for a fluid elastic sphere. (-)
- 105 χ_{si} . Intrinsic normalised total scattering cross-section for an irregularly shaped solid elastic
- 106 particle. (-)
- 107 χ_{fi} . Intrinsic normalised total scattering cross-section for an irregularly shaped fluid elastic
- 108 scatterer. (-)
- 109 χ_h . Intrinsic hybrid normalised total cross-section for a scatter of variable density. (-)
- 110 χ_o . Ensemble normalised total scattering cross-section. (-)
- 111 χ_{ho} . Ensemble hybrid normalised total cross-section for a scatter of variable density. (-)
- 112 ψ . Transducer nearfield correction term. (-)
- 113 ω . Angular acoustic frequency. (s^{-1})
- 114

115 **1. Introduction**

116 The transport of sediments in coastal and estuarine waters is important because of the impact
117 it has on aquatic habitats, water quality, turbidity, biogeochemistry and morphology
118 (Amoudry and Souza, 2011). Developing capabilities to monitor and model marine sediment
119 transport is therefore an essential component of coastal management (Davies and Thorne,
120 2008). To facilitate these developments new technologies are continually being investigated
121 and acoustics is one of the techniques being used to advance our measurement capabilities
122 (Thorne and Hay, 2012). Acoustics is being developed for sediment transport process studies
123 because it is recognised as having the capability to measure non-intrusively, co-located,
124 simultaneously and with high spatial-temporal resolution, suspended sediment (Pedocchi and
125 Garcia, 2012) and flow profiles (Hurther and Thorne 2011) and provide information on
126 bedforms (Hay, 2011).

127

128 The use of acoustics in non-cohesive inorganic sedimentary environments has been very
129 successful, with many studies utilising sound to examine sediment transport processes over
130 sandy beds (Hay et al, 2012; O’Hara Murray et al, 2012; Bolanos et al, 2012; Chassagneux
131 and Hurther, 2014). In particular the acoustic approach has been successfully applied to the
132 measurement of suspended sediments (Hay and Bowden, 1994; Thorne et al, 2009; O’Hara
133 Murray et al, 2011). Apart from the technology developments, the success of the use of sound
134 for suspension measurements has been due to an evolving description of the acoustic
135 scattering properties of irregularly shaped sandy particles (Hay, 1991; Thorne and Meral,
136 2008; Moate and Thorne, 2013) and the development of inversion methodologies to extract
137 suspension parameters from the backscattered sound (Crawford and Hay, 1993; Thosteson
138 and Hanes, 1998; Hurther et al 2011, Moore et al 2013; Thorne and Hurther 2014). This has
139 led to the development of multi-frequency acoustic backscatter systems for suspended
140 sediment studies becoming available as commercial products and these are being utilised by
141 the coastal and estuarine community.

142

143 Although acoustics has had success in measuring suspended sediments in regions
144 predominantly composed of non-cohesive sandy sediments, its application in the regime of
145 fine grained sediments, usually considered to be silts and clays, has been more problematic
146 (Gartner, 2004; Ha et al, 2009; Ha et al, 2011; Sahin et al, 2013). When acoustic systems are
147 used in studies on fine grained sediment transport, it is usually in combination with in-situ

148 samples to calibrate and quantify the acoustic measurements (Shi et al, 1999; Holdaway et al;
149 1999; Fugate and Friedrichs, 2002; Moore et al, 2012), however, it is generally
150 acknowledged that if the process of flocculation occurs during the measurement campaign,
151 interpretation of the acoustic observations are challenging and uncertain. The main reason for
152 this uncertainty arises because there has been neither measurements collected on the
153 interaction of sound with flocculating sediments under controlled conditions, nor the
154 development of a theoretical framework to describe such interactions. Therefore the use of
155 multi-frequency acoustic backscatter systems to study sediment transport processes in
156 cohesive fine grained environments is much less developed than that in the non-cohesive
157 sandy regime.

158

159 To expand the quantitative use of acoustics, from non-cohesive sediments, to fine grained
160 cohesive flocculating environments, a recent experimental study (MacDonald et al 2013) was
161 carried out. In a series of acoustics backscatter measurements on suspensions of fine grained
162 primary particles, of which flocs are composed, and, through the addition of a flocculating
163 agent, on flocs formed by the aggregation of the primary particles, controlled acoustic
164 observations were made on the interaction of sound with a suspension of flocculating
165 sediments. As a complementary study to the experimental work, developments to model the
166 observations have been in progress (Thorne et al, 2012a, b) and the result is reported here.

167

168 The methodology adopted for the flocculating scattering model is comparable to the
169 heuristics approaches used in the description of non-cohesive sediment scattering (Hay, 1991;
170 Schaafsma and Hay 1997; Thorne and Meral, 2008, Moate and Thorne, 2009) and
171 zooplankton scattering (Johnson, 1977; Stanton 1990, Wiebe et al, 1990; Stanton and Chu,
172 2000). The concept is to utilise the acoustic scattering characteristic of well understood
173 bodies with analytical solutions, such as spheres and cylinders, to form the basis of the
174 scattering description, and modify, and often simplify, the analytical expressions to obtain
175 formulae which can be usefully applied to more asymmetric irregularly shaped scattering
176 bodies. This approach is well developed and used successfully in acoustics (Stanton and Chu
177 2000; Lawson et al, 2006; Thorne and Meral, 2008, Moate and Thorne, 2012). For the present
178 study a modified solid elastic sphere is used to represent the scattering by primary particles
179 and this has been validated with published data (Thorne and Meral, 2008). To represent the
180 scattering characteristics of the somewhat nebulous collection of primary particles which

181 compose a large low density flocc, a single scattering body is proposed which has the
182 combined acoustic properties of the water and the primary particles. A modified fluid elastic
183 sphere model is used to characterise the scattering characteristics of the body using an
184 approach similar to Johnson (1977). This fluid model was chosen because large flocculated
185 scatterers have densities closer to that of water than the primary particles and would probably
186 not sustain shear wave propagation. To obtain a description which covers the whole range
187 from primary particles to low density floccs a hybrid model is proposed which provides
188 continuous scattering behaviour based on the variation of particle density as the flocculation
189 process occurs. To compare the scattering characteristics from such a hybrid model with
190 observations, measured parameters from the experimental study of MacDonald et al (2013)
191 are used to constrain the model output. Software to calculate flocc scattering responses is
192 given at <http://noc.ac.uk/using-science/products/software/csr-acoustic-inversions> Program
193 name (3) - model_floc_paper.m.
194

195 **2. Suspension scattering theory**

196 *2.1 Backscattered signal*

197 The root-mean-square backscattered voltage, V , from an aqueous suspension of particles
 198 insonified using a disc transceiver, under conditions of incoherent scattering and when
 199 multiple scattering can be ignored (Sheng and Hay, 1988; Crawford and Hay, 1993; Thorne
 200 et al, 1993; Thorne and Hanes, 2002; Hurther et al, 2011) can be expressed as

$$V = \left(\frac{K\mathfrak{R}}{r\psi} \right) M^{1/2} e^{-2r(\alpha_w + \alpha_s)} \quad (1)$$

201 K represents the sediment backscattering properties, r is the range from the transceiver, ψ
 202 accounts for the departure from spherical spreading within the transducer nearfield (Downing
 203 et al 1995) and \mathfrak{R} is the system constant (Betteridge et al 2008). The term α_w is the sound
 204 attenuation due to water absorption and α_s is the attenuation due to suspended particle
 205 absorption and scattering. M is the suspended concentration and is based on the
 206 approximation $M \approx \frac{4\pi\rho(a_o)N}{3} \int_0^\infty a^3 n(a) da$, where N the number of scatterers per unit volume,
 207 $\rho(a_o)$ is the density of the scatterer and a_o is the suspension mean particle radius. The
 208 dependency of scatterer density on particles size is used to introduce the process of
 209 flocculation into the suspension scattering characteristics.

210 The scattering and attenuation terms can be formulated as follows

$$K = \frac{f_o}{(a_o\rho(a_o))^{1/2}}, \quad \alpha_s = \frac{1}{r} \int_0^r \xi M dr, \quad \xi = \frac{3\chi_o}{4a_o\rho(a_o)}$$

211

$$f_o(a_o) = \left[\frac{\int_0^\infty an(a)da \int_0^\infty a^2 f^2 n(a)da}{\int_0^\infty a^3 n(a)da} \right]^{1/2} \quad (2a)$$

212

$$\chi_o(a_o) = \frac{\int_0^\infty an(a)da \int_0^\infty a^2 \chi n(a)da}{\int_0^\infty a^3 n(a)da} \quad (2b)$$

213

$$a_o = \int_0^\infty an(a)da \quad (2c)$$

214

215 f and χ are respectively the intrinsic form function and intrinsic normalised total scattering
216 cross-section for the particles in suspension. Here intrinsic refers to the scattering
217 characteristics measured using suspensions sieved into narrow size fractions. Physically, f
218 describes the backscattering characteristics of a particle relative to its geometrical size, whilst
219 χ quantifies the scattering from a particle over all angles, including viscous attenuation,
220 relative to its cross-sectional area, and is proportional to attenuation. f_0 and χ_0 represent the
221 ensemble mean scattering values obtained by integrating the intrinsic scattering
222 characteristics over the particle size probability density function, $n(a)$, of the particles in
223 suspension.

224 *2.2 Solid particle scattering characteristics*

225 In their primary unflocculated state the primary particles can be considered as being solid
226 elastic particles and represented using a modified sphere model. Such an approach has been
227 used in a number of studies (Moate and Thorne, 2013). The intrinsic expressions for the
228 backscatter form function and the normalised total scattering and viscous cross-section for a
229 solid elastic sphere are given by

$$f_{ss} = \left| \frac{2}{ix} \sum_{n=0}^{\infty} (-1)^n (2n+1) b_n \right| \quad (3a)$$

230

$$\chi_{ss} = \frac{2}{x^2} \sum_{n=0}^{\infty} (2n+1) |b_n| \quad (3b)$$

231

$$\chi_{sv} = \frac{2}{3} x (\gamma - 1)^2 \frac{\tau}{\tau^2 + (\gamma + \theta)^2} \quad (3c)$$

232

233 Where

$$\tau = \frac{9}{4\beta a} \left(1 + \frac{1}{\beta a} \right), \quad \theta = \frac{1}{2} \left(1 + \frac{9}{2\beta a} \right)$$

234

235 The subscript ‘ss’ refers to solid sphere. In equations (3a) and (3b) b_n is a function containing
 236 spherical Bessel and Hankel functions and their derivatives, $x=ka$, where $k=2\pi/\lambda$, λ is the
 237 wavelength of the sound in water and a is the radius of the spheres in suspension
 238 (Faran,1951; Gaunard and Uberall, 1983; Thorne et al 1993 appendix and MacDonald et al
 239 2013 Appendix A give b_n explicitly). The expression in equation (3c) (Urick 1948) accounts
 240 for viscous losses when for $x \ll 1$; $\gamma = \rho_s/\rho_w$ and $\beta = \sqrt{\omega/2\nu}$, where ω is the acoustic angular
 241 frequency, ν the kinematic viscosity for water, ρ_w is the density of water and ρ_s is the density
 242 of the solid particles. In the evaluation of ξ , $\chi = \chi_{ss} + \chi_{sv}$. Figures 1a and 1b show the form of
 243 the expressions given in equation (3) for solid elastic spheres with shear and compressional
 244 velocities of $c_{sh}=3545 \text{ ms}^{-1}$ and $c_s=5550 \text{ ms}^{-1}$, density of $\rho_s=2600 \text{ kgm}^{-3}$ and water properties
 245 of $c_w=1480 \text{ ms}^{-1}$, $\rho_w=1000 \text{ kgm}^{-3}$, $\nu=1.10^{-6} \text{ m}^2\text{s}^{-1}$.

246 Measurements (Hay, 1991; Schaafsma, and Hay, 1997; Moate and Thorne, 2009) have shown
 247 that for natural irregularly shaped sedimentary particles the detailed resonance structures
 248 associated with sharp dips in f_{ss} are not generally present due to the lack of symmetry in the
 249 shape of the particles and this allows simpler heuristic expressions to replace the relatively
 250 complex terms in equations (3a) and (3b). A number of similar intrinsic expressions have
 251 been published and the ones used here are based on a fit to a number of data sets (Thorne and
 252 Meral 2008) for suspensions of sands.

$$f_{si} = \frac{k_{sf}x^2(1 - 0.25e^{-((x-1.5)/0.5)^2})(1 + 0.35e^{-((x-2.0)/2.0)^2})}{1.13 + 0.8k_{sf}x^2} \quad (4a)$$

$$\chi_{si} = \frac{k_{s\alpha}x^4}{1 + x^2 + 0.9k_{s\alpha}x^4} \quad (4b)$$

253 The subscript ‘si’ refers to solid irregular. Generally k_{sf} and $k_{s\alpha}$ are given by (Morse and
 254 Ingard, 1986)

$$k_{sf} = \frac{2}{3} |\eta_k - \eta_p| \quad k_{s\alpha} = \frac{4}{3} \left(\frac{\eta_k^2 + \eta_p^2/3}{6} \right)$$

$$\eta_k = (\kappa_s - \kappa_w)/\kappa_w \quad \eta_p = 3(\rho_s - \rho_w)/(2\rho_s + \rho_w)$$

255 κ_s and κ_w are respectively the compressibility for the solid particles in suspension and the
 256 surrounding water. Values used are $\kappa_s=2.7.10^{-11} \text{ Pa}^{-1}$ and $\kappa_w=4.5.10^{-10} \text{ Pa}^{-1}$ (Kay and Laby,
 257 1986) which gives values of $k_{sf}=1.15$ and $k_{s\alpha}=0.24$. The expressions for f_{si} and χ_{si} reduce to

258 x^2k_{sf} and x^4k_{sa} for $x \ll 1$, the Rayleigh scattering regime, and to a constant value generally
 259 greater than unity in the geometrical regime $x \gg 1$. In figures 1a and 1b the heuristic
 260 equations (4a) and (4b) are compared with the exact solutions of equations (3a) and (3b)
 261 where it can be seen that the results are comparable, though with the heuristic expressions
 262 lacking the resonance oscillations when $x > 1$.

263

264 A number of measurements have been collected on scattering by inorganic non-cohesive
 265 sediments and these data are compared with the predictions in figure 1a and 1b. The solid
 266 circles in the figures are the mean of a number of measurements (Thorne and Meral 2008)
 267 and the crosses are from a series of studies summarised in Richards et al 2003. The
 268 comparisons show that equations (3c), (4a) and (4b) provide a reasonable description of
 269 scattering by solid elastic irregularly shaped particles. Therefore the non-cohesive elastic
 270 model given by equations (3c) and (4a) and 4(b) should represent the scattering
 271 characteristics of the elemental particles reasonably well.

272

273 *2.3 Fluid particle scattering characteristics*

274 When particles undergo flocculation the primary particles become loosely bound to form
 275 large fragile floc structures of dimensions tens to hundreds of times larger than the primary
 276 particles. These flocs are predominately composed of the water itself and are therefore not
 277 solid scatterers, but have densities close to water and easily shear apart. They could therefore
 278 be considered to have scattering characteristics closer to that of a fluid sphere rather than that
 279 of a solid elastic sphere. Considering flocs with densities much closer to that of water than
 280 the primary particles as fluid spheres, their intrinsic scattering characteristics can be
 281 expressed as (Anderson, 1950)

$$f_{fs} = \frac{2}{x} \left| \sum_{n=0}^{\infty} \frac{(-1)^n (2n+1)}{1 + iC_n} \right| \quad (5a)$$

282

$$\chi_{fs} = \frac{2}{x^2} \sum_{n=0}^{\infty} \frac{(-1)^n (2n+1)}{1 + C_n^2} \quad (5b)$$

283

284 The subscript ‘fs’ refers to fluid sphere and C_n is composed of spherical Bessel and spherical
 285 Neumann functions (Anderson, 1950 equation (9) and MacDonald et al, 2013 Appendix A
 286 give C_n explicitly). Figure 1c and 1d show the form of the expressions given in equation (5)
 287 for fluid spheres having a compressional velocity of $c_f=1.02c_w$ and a density of $\rho_f=1.02\rho_w$.

288

289 As with the primary particles, modified sphere heuristic expressions exist for the
 290 backscattering characteristics of irregular fluid scatterers (Stanton and Chu, 2000). Here the
 291 intrinsic backscatter form function uses a heuristic expression for a fluid sphere (Johnson
 292 (1977) which in the present study is modified to retain a form similar to equation (4a), though
 293 without the bracketed terms associated with solid particle oscillations.

$$f_{fi} = \frac{k_{ff}x^2}{1 + \varepsilon_1 x^2} \quad (6a)$$

294 The subscript ‘fi’ refers to fluid irregular. For the total normalise scattering cross-section a
 295 modified version of equation (4b) is used

$$\chi_{fi} = \frac{k_{f\alpha}x^4}{1 - \varepsilon_2 x + \varepsilon_3 x^2 + k_{f\alpha}x^4} \quad (6b)$$

297 Values selected for the coefficients ε_1 , ε_2 and ε_3 were 1.2, 1.0 and 1.5 respectively. These
 298 values may well depend on floc structure and the degree of variability in the coefficients
 299 should be realised as experimental studies on floc scattering are carried out. This was the case
 300 for non-cohesive sediment acoustic scattering. Expressions for k_{ff} and $k_{f\alpha}$ (Clay and
 301 Medwin, 1997) are

$$k_{ff} = 2 \left(\frac{\gamma\zeta^2 - 1}{3\gamma\zeta^2} + \frac{\gamma - 1}{2\gamma + 1} \right), \quad k_{f\alpha} = 2 \left(\left(\frac{\gamma\zeta^2 - 1}{3\gamma\zeta^2} \right)^2 + \frac{1}{3} \left(\frac{\gamma - 1}{2\gamma + 1} \right)^2 \right)$$

302 The value for ζ is given by $\zeta=c_f/c_w$ and as before $\gamma=\rho_f/\rho_w$. The expressions for f_{fi} and χ_{fi}
 303 reduce to x^2k_{ff} and $x^4k_{f\alpha}$ in the Rayleigh scattering regime. In figures 1c and 1d equations (6a)
 304 and (6b) are compared with equations (5a) and (5b) where it can be seen that the results are
 305 comparable, and, as with the solid scatters, the higher resonance oscillations are not present
 306 in the heuristic expressions. Unlike the case for solid elastic scatterers there are few
 307 measurements on fluid spheres (Hartog and Knollman, 1963) due to the difficulty in
 308 obtaining such measurements and none on irregularly shaped fluid bodies, although fluid

309 sphere heuristic expressions have been applied successfully to acoustic scattering by
 310 zooplankton (Stanton 1989). The values selected for ε_1 , ε_2 and ε_3 were found to give similar
 311 comparisons to those shown in figures 1c and 1d for a range of values for ζ and γ between
 312 1.001-2.0.

313 *2.4 Hybrid particle scattering characteristics*

314 Equations (3c), (4a) and (4b) are considered to provide a description of the acoustic
 315 interaction with the solid primary particles and equations (6a) and (6b) have been suggested
 316 as expressions for scattering by low density fluid flocs. To link these two descriptions into a
 317 model that describes the scattering properties of the primary, transitional, and flocculated
 318 scatterers, the density and compressional velocity of sound in the scatterer are made a
 319 function of particle size. The term often used to indicate the degree of flocculation is the
 320 effective density, $\rho_e = \rho(a) - \rho_w$, where $\rho(a)$ is the floc density and ρ_e generally decreases as the
 321 floc size increases (Kranenburg, 1994; Fettweis, 2008; Manning et al 2007). The form for ρ_e
 322 with particle size is generally inverse linear on a log-log plot (Manning et al 2011) and can
 323 therefore be formulated as an inverse power of particle size (MacDonald et al, 2013)

$$\rho_e = \frac{C_f}{a^m} \quad (7)$$

324 The values of $C_f \text{ kgm}^{(3-m)}$ and m vary depending on the process of flocculation (Manning et al
 325 2011). As seen in the expressions above, equations (3c), (4) and (6), the density ratio between
 326 the scatterer and the fluid, $\gamma = \rho(a)/\rho_w$, is an important acoustic parameter for scattering and
 327 attenuation and using the expression for the effective density this can be written as

$$\gamma(a) = 1 + \frac{\rho_e}{\rho_w} \quad (8)$$

328 The other important ratio for scattering and attenuation is that of the sound velocity ratio in
 329 the scatterer to that in the fluid, $\zeta(a) = c(a)/c_w$. The velocity of sound within the flocs of a
 330 flocculating cohesive suspension has not been measured and is not known. To obtain an
 331 estimate for the compressional wave velocity in the flocs the approach adopted is based on
 332 the assumption that it has the same properties as that of a homogeneous fluid of the same
 333 mean density and compressibility. This approach was introduced by Wood (1930) for looking
 334 at fluid mixtures but it has also been applied to seabed porous sands (Hamilton, 1967). The
 335 water and solid components each contribute to the bulk compressibility and bulk density of

336 the floc proportionally through the porosity of the mixture (Urlick, 1947; Hamilton and
 337 Bachman, 1982; Buckingham, 1997). Using Wood's equation allows ζ to be expressed as

$$\zeta(a) = \frac{1}{c_w} (\{\phi\kappa_w + (1 - \phi)\kappa_s\} \{\phi\rho_w + (1 - \phi)\rho_s\})^{-1/2} \quad (9)$$

338 Here $\kappa_w=1/(\rho_w c_w^2)$, $\kappa_s=1/(\rho_s c_s^2)$ and ϕ is the porosity of the floc. Defining κ_s as equal to
 339 $1/(\rho_s c_s^2)$ is not strictly correct as $c_s^2 = (\kappa_s^{-1} + \frac{4}{3}G)/\rho_s$ for a solid, where G is the shear
 340 modulus, however, using $1/(\rho_s c_s^2)$ with the compressional velocity for the primary particles,
 341 provides the correct value for $\zeta(a)$ as $\phi \rightarrow 0$ and results in $k_{ff} \approx k_{sf}$ and $k_{fa} \approx k_{sa}$, thereby
 342 allowing equations 6(a) and 6(b) to also represent the primary particle scattering when $x \ll 1$.
 343 The porosity, ϕ , of the scatterer is given by

$$\phi = \frac{\rho_s - \rho(a)}{\rho_s - \rho_w} \quad (10)$$

344 Using equations (3c), (6a) and (6b) with equations (7-10) provides a description for the
 345 suspension backscattering and attenuation characteristics of flocculation which transitions
 346 from solid scatterers, the primary particles, in the Rayleigh regime, through the intermediate
 347 region as flocs are formed, towards fluid scatterers as large low density flocs become
 348 dominant. For the modelling an upper value is placed on ρ_e such that $\rho_e \leq \rho_s - \rho_w$ and a lower
 349 imposed value of $\rho_e = \rho_0$. The former value is a physical restriction dictated by the grain
 350 density of the primary particles, while the latter is chosen as a minimum effective density.

351

352 3. Modelled flocculation scattering characteristics

353 3.1 Intrinsic floc scattering characteristic

354 To provide an illustration of the output from the scattering model for flocculating sediments
355 an example is given in figure 2. The frequency used for the calculation was 3.0 MHz, this
356 was chosen as it is a common acoustic frequency used in sediment process studies. The
357 particle size varied from $a=0.01-1000 \mu\text{m}$, $c_s=5550 \text{ ms}^{-1}$, $\rho_s=2600 \text{ kgm}^{-3}$, $c_w=1480 \text{ ms}^{-1}$, ρ_w
358 $=1000 \text{ kgm}^{-3}$, $\kappa_w=1/(\rho_w c_w^2)$, $\nu=1.10^{-6} \text{ m}^2 \text{ s}^{-1}$, $C_f=0.001 \text{ kgm}^{-2}$ and $m=1$ (Manning et al 2011).
359 For the solid irregular elastic scatter given by equation (4) $\kappa_s=2.7.10^{-11}$, while in equation (9)
360 $\kappa_s=1/(\rho_s c_s^2)$. The elastic and acoustic properties of clay and silt sediments can be quite
361 variable (Wang et al, 2001; Vanorio, 2003; Mondol et al, 2008) and the values used above are
362 therefore indicative. In figure 2a the form for the effective density, $\rho_e(x)$ normalised by $\rho_s-\rho_w$
363 is presented. Below $0.6 \mu\text{m}$ ($x\approx 0.008$) the effective density derived from equation (7) became
364 greater than $\rho_s-\rho_w$ and therefore the normalised value was set to unity. A minimum effective
365 density of $\rho_e=20 \text{ kgm}^{-3}$ was applied, thereby yielding a minimum value for γ_o of 1.02. For the
366 modelling an equivalent minimum value of 1.02 was also applied to ζ_o . This led to the forms
367 for $\gamma(x)$ and $\zeta(x)$ shown in figure 2a. It is the trends in $\gamma(x)$ and $\zeta(x)$ with particle size that
368 represents the process of flocculation in the scattering model.

369

370 In figure 2b is shown what would happen to the backscatter form function, f_{si} , calculated
371 using equation (4a), if the irregular solid primary particles increased in diameter. This shows
372 f_{si} increasing with x until around $x\approx 2$ where above this value f_{si} tends to a constant magnitude
373 somewhat greater than unity. Also shown is the backscatter characteristics, calculated using
374 equation (6a), f_{fi} , for an irregular fluid sphere with $\gamma(x)=\gamma_o$ and $\zeta(x)=\zeta_o$. This shows a similar
375 trend to the primary particles although with reduced values due to the much lower acoustic
376 scattering characteristics. The solid line in figure 2b is the modelled hybrid intrinsic hybrid
377 backscatter form function, f_h , as the scatterer transitions from a irregular solid elastic primary
378 particle through a transition region to an irregular elastic fluid particle. This curve was
379 calculated using equations (6a-10). The plot for f_h shows agreement with the f_{si} for the
380 primary particles when $x\leq 0.01$ ($a\leq 0.8 \mu\text{m}$), f_h then progressively transitions from the primary
381 scattering characteristics toward that of fluid scatterer, becoming essential fluid at $x\approx 1$ ($a\approx 80$
382 μm) and above this value f_h follows that of a fluid scatterer, f_{fi} , with scattering characteristics
383 based on γ_o and ζ_o having a value of 1.02. In figure 2c results are shown for the normalised
384 total scattering cross-section calculated using equations (3c, 4b, 6b-10). Similar trends are

385 observed for χ_{si} and χ_{fi} below $x \approx 1$, although with χ_{fi} smaller in magnitude due to the lower
386 scattering characteristics. Above $x \approx 1$ χ_{si} tends to level off towards a value close to unity,
387 while χ_{fi} tends to increase, though at a somewhat reduced rate. The further term in the
388 normalised scattering cross-section is the viscous attenuation which begins to dominate
389 attenuation when $x \lesssim 0.2$ for the fluid sphere and $x \lesssim 0.1$ for the solid sphere. A peak value
390 in χ_{vi} is seen to occur at $x \approx 0.01$. As with figure 2b the solid line is the modelled hybrid
391 intrinsic normalised total backscatter cross-section, χ_h , for a particle transitioning from a solid
392 elastic primary particle, χ_{si} , through a transition region to an elastic fluid particle, χ_{fi} . As
393 mentioned above χ_{sv} dominates below $x \lesssim 0.2$ and in this regime χ_h follows the trend of χ_{sv} ,
394 above this value the attenuation due scattering begins to dominate and because the scattering
395 characteristics have transitioned from solid to mainly fluid particle scattering by $x \approx 0.2$, χ_h is
396 dominated by that of a fluid scatterer.

397

398 *3.2 Ensemble floc scattering characteristics*

399 The results presented in figure 2 are the intrinsic scattering characteristics and therefore
400 represent scattering by a suspension with a very narrow particle size distribution. However, in
401 practice marine suspensions typically have relatively broad size distribution. Therefore to
402 obtain the ensemble scattering characteristics the intrinsic values need to be integrated over a
403 size distribution, $n(a)$, as defined in equations (2a) and (2b). The lognormal distribution is
404 often used to describe the size probability density function of marine sediments (Soulsby,
405 1997) and is therefore used here with $n(a)$ given by

406

$$407 \quad n(a) = \frac{1}{a\mu_1\sqrt{2\pi}} e^{-(\log_e(a)-\mu_2)^2/2\mu_1^2} \quad (11)$$

$$408 \quad \mu_1 = \sqrt{\log_e[\delta^2 + 1]}, \quad \mu_2 = \log_e(a_0/\sqrt{1 + \delta^2})$$

409

410 Where $\delta = \sigma/a_0$ is the normalised standard deviation and σ and a_0 are respectively the standard
411 deviation and mean of $n(a)$. Figure 3 shows the impact on f_{ho} and χ_{ho} as the value for δ
412 increased from 0.0 to 1.0. To obtain the plots equations (3c), (6a) and 6(b) were evaluated
413 using equations (7-10) and integrating over $n(a)$, given in equation (11), using equations (2a)
414 and (2b) with a_0 varying between 0.001-1000 μm . The parameters used to calculate the

415 scattering characteristic were the same as those used in figure 2. The solid line, $\delta=0$,
416 represents the intrinsic scattering characteristics and is identical to the solid line given in
417 figure 2. Figure 3a shows the impact of increasing δ on f_{ho} , where it is observed that for $x_o < 1$
418 the trend for f_{ho} is to increase with δ relative to f_h and with the increase being greater the
419 smaller the value of x_o . For $x_o > 1$, the trend is for f_{ho} to moderately reduce with δ relative to f_h
420 with the reduction remaining nominally constant as x_o increases. Figure 3b shows the impact
421 of increasing δ on χ . As can be seen in the figure the departure of χ_{ho} from χ_h increases with δ
422 and this departure varies with x_o depending on the dominate attenuation term. These results
423 clearly illustrate the impact δ can have on the ensemble scattering characteristics.

424

425 3.3 Model sensitivities

426 As mentioned above values for C_f and m in equation (7) are not unique and separate studies
427 give different values depending on the sediment mineralogy and flocculation processes. To
428 assess the impact variations in these two parameters had on the modelling of f_{ho} and χ_{ho} their
429 values were changed and the results are shown in figure 4. In figure 4a the change in $\gamma(x)$ is
430 shown for 20 different cases. The main impact is that as C_f and m increase the region over
431 which the flocculation transition occur decreases, with the lower limit in x at which the
432 scatterers reach the density of the primary particles increasing from $x=8 \cdot 10^{-4}$ ($a=0.06 \mu m$) to
433 $x=0.04$ ($a=3.0 \mu m$) for $C_f=0.0005$, $m=0.9$ and for $C_f=0.0015$, $m=1.1$ respectively. To assess
434 the impact the changes in C_f and m had on the suspension scattering characteristics, f_{ho} and
435 χ_{ho} were calculated using values identical with those used to obtain the plots in figures 2 and
436 3 with $\delta=0.5$. Taking $C_f=0.001$ and $m=1$ as a reference, the thick solid line in figures 4b and
437 4c, the plots show that in the transition region, $0.005 \leq x_o \leq 1$, as C_f and m increases, the dashed
438 lines, the values for f_{ho} and χ_{ho} increase, while if C_f and m decreases, the dotted lines, the
439 values for f_{ho} and χ_{ho} decrease. These scattering changes are not marginal and lead to
440 important differences in the modelled values for f_{ho} and χ_{ho} in the transition region.

441 In figure 5 comparisons are made of the modelled scattering characteristic as γ_o and ζ_o were
442 varied between 1.005-1.3. All other parameters were the same as used to calculate the plots in
443 figures 2 and 3 with $\delta=0.5$. In figure 5a the results for f_{ho} are shown. For values of $x_o \leq 0.01$
444 the impact of changes in γ_o and ζ_o on f_{ho} is negligible, between $x_o=0.01-1$ there is increasing
445 divergence between the 20 curves and above $x_o \approx 1$ the values for f_{ho} remain nominally
446 uniform, although for the $\gamma_o = \zeta_o=1.005$ case there is a slight reduction in values. The

447 difference in the values for f_{ho} at $x_o=10$, between cases $\gamma_o = \zeta_o=1.005$ and $\gamma_o = \zeta_o=1.3$, is a
448 factor of 40, indicating the impact γ_o and ζ_o have on the backscattering characteristic. The
449 results for χ_{ho} are presented in figure 5b. In this case we can see that for $x \lesssim 0.05$ the
450 variations in γ_o and ζ_o have little impact on χ_{ho} , above this value the 20 curves diverge with
451 χ_{ho} taking on values of between 0.007- 0.6, at $x_o=10$, for γ_o and ζ_o having magnitudes over the
452 range 1.005-1.3. As with the variation of the suspension scattering characteristic with C_f and
453 m , changes in γ_o and ζ_o can lead to significant difference in the modelled values for f_{ho} and χ_{ho}
454 as the larger flocs begin to dominate the scattering. The results presented in figures 3, 4 and
455 5 indicate that the modelled acoustics scattering characteristics of flocculating sediments are
456 quite sensitive to the physical parameterisation of the flocculation process.

457

458

4. Comparison of the floc scattering model with measurements

The measurement of acoustic scattering by flocculating sediments is a difficult experiment to conduct and only recently has quantitative data been published (MacDonald et al, 2013). The objective of the study was to perform measurements on the scattering properties of the primary particles and by adding a flocculant to the primary suspension control the process of flocculation and measure the acoustic backscattered response. Details of the experimental study are given in MacDonald et al (2013) and only the salient features are outlined here for model comparison.

Acoustic backscatter measurements were carried out on suspensions of kaolin (Specwhite™ SiO₂ (47%), Al₂O₃ (38%), density 2600 kgm⁻³) in a well-mixed re-circulation tank which generated a homogeneous suspension. Flocculation in the tank was controlled through the incremental addition of a commercial flocculent (MAGNAFLOC®). Mass concentrations between 0.2-3.2 kg m⁻³ were used and repeated measurements showed the kaolin was uniformly distributed to ±5% within the measurement region of the tank. Acoustic backscatter was measured using an Aquatec Aquascat-1000™ with transducers operating at frequencies of 3.0, 4.0 and 5.0 MHz over a range of 0.7 m at 0.01 m sampling intervals. The size distribution of the primary particles was determined using a Malvern MasterSizer 2000™. The floc size and settling velocity distributions for the flocculated suspension were determined using an optical FLOCView system. Figures 6a and 6b show measurements of the primary particles, and a representative floc size distribution, compared with lognormal probability density functions having $a_0=0.43 \mu\text{m}$, $\delta=0.85$ and $a_0=80 \mu\text{m}$, $\delta=0.5$ respectively. Over the size range of the flocs $\bar{\delta}=0.5\pm 0.2$. Using the settling velocity and floc size with Stokes law allowed $\rho_e(a)$ to be estimated. The results were expressed in the form of equation (7) with $C_f = 5.83 \cdot 10^{-4}$ and $m=1.12$. To obtain f_{ho} and χ_{ho} the approach of Thorne and Buckingham (2004) was adopted based on the assumption of a homogeneous concentration in the measurement tank and taking the natural logarithm of equation (1). It is the published values of f_{ho} and χ_{ho} with which the present model is compared.

486

To calculate the modelled scattering values for f_{ho} and χ_{ho} the following central parameters were used; $\rho_s=2650 \text{ kg m}^{-3}$, $\rho_w=1000 \text{ kg m}^{-3}$, $c_s=2060 \text{ ms}^{-1}$, $c_w=1480 \text{ ms}^{-1}$, $\nu=1 \cdot 10^{-6} \text{ m}^2\text{s}^{-1}$, $C_f = 6 \cdot 10^{-4}$, $m=1.1$, (MacDonald et al, 2013), $\varepsilon_1=1.4$, $\varepsilon_2=1.5$, $\varepsilon_3=1.0$ and $\gamma_0 = \zeta_0=1.05$. The selection of $c_s=2060 \text{ ms}^{-1}$ is relatively low compared with some reported values (Wang et al,

491 2001; Vanorio, 2003; Mondol et al, 2008), however, the study of MacDonald et al (2013)
 492 indicated $c_s=2060 \text{ ms}^{-1}$ was the appropriate value to use for the comparison with their
 493 experimental data. As mentioned previously the ε coefficients will have a degree of
 494 uncertainty at this stage in the development of laboratory floc measurements and modelling,
 495 and were therefore selected pragmatically. Using equations (3c, 6-10) and integrating over
 496 $n(a)$ using equation (2) with the lognormal distribution of equation (11) having $\delta(x)$ varying
 497 linearly from 0.85 for the primary particles to 0.5 for the low density flocs, f_{ho} and χ_{ho} were
 498 evaluated at 3.0, 4.0 and 5.0 MHz for $a_o=0.001-1000 \mu\text{m}$. To allow for uncertainties in the
 499 floc parameters the calculations were repeated at 4 MHz with $C_f = 3.10^{-4}$, $m=1.05$, $\gamma_o=$
 500 $\zeta_o=1.025$ and $C_f = 12.10^{-4}$, $m=1.2$, and $\gamma_o= \zeta_o=1.1$. These were not considered unreasonable
 501 uncertainties given the spread in the data used to estimate the floc parameters. The results of
 502 the modelling and the measured values for f_{ho} and χ_{ho} are shown in figure 7.

503
504

505 In figure 7a is shown the modelled values for f_{ho} at the three different frequencies using the
 506 central parameters and with the grey area indicating the region of uncertainty. The model
 507 shows steadily increasing values of f_{ho} with x_o for $x_o \lesssim 2$, with nominally uniform values of
 508 approximately 0.1 for $x_o > 2$. Comparison of the model output with the primary particle
 509 observations, $x_o < 0.01$, shows good agreement with the data with the model capturing the
 510 absolute level and trend of the solid primary particle scattering. The model marginally
 511 underestimates the measured values, however, the estimated region of uncertainty
 512 encompasses the data. For the floc measurements, $x_o = 0.5-3$, a regime where fluid scattering
 513 becomes dominant in the model, the model captures the level of the measured values for f_{ho}
 514 and the increasing trend with x_o , although the data indicates f_{ho} increasing somewhat more
 515 steeply than modelled. This difference in steepness could be due to a number of factors
 516 including C_f and m not being invariant with a_o , $n(a)$ having a somewhat different trend with
 517 a_o than that applied and the selected values for the ε coefficients in equation (6) may not be
 518 invariant with a_o . In figure 7b is shown the modelled values for χ_{ho} which show a somewhat
 519 different form with x_o to that of f_{ho} . For values of $x_o \lesssim 0.1$ the dominant component of χ_{ho} is
 520 associated with viscous attenuation, this is seen to steadily increase initially with x_o peaking
 521 at a value of $\chi_{ho} \approx 5.10^{-4}$ at $x_o \approx 0.01$ and thereafter declining due to the reducing particle
 522 density. Above $x_o \approx 0.1$, the fluid scattering component of χ_{ho} begins to prevail and steadily
 523 increases with x_o . Comparing the model with the observations for the solid primary particle
 524 regime, the modelled values for χ_{ho} are comparable in level and form with the data. The

525 measurements of χ_{ho} shown in figure 7b for the primary particles have relatively large error
526 bars due to experimental difficulties in obtaining accurate values for χ_{ho} when attenuation due
527 to water absorption is comparable with the suspension attenuation (Moate and Thorne 2009).
528 In the regime of floc scattering, $x_o=0.5-3$, the model is dominated by the fluid particle
529 scattering characteristics and is seen to follow the data reasonably well both in terms of
530 magnitude and trend. There is some underestimate of the absolute level and this could be
531 associated with the factors noted above in the difference in steepness for f_{ho} , although,
532 generally, the data lie within the region of estimated uncertainty. The model therefore
533 captures in broad terms the general behaviour of the observed primary and flocculated
534 scattering characteristics.

535

536 **5. Conclusions**

537

538 The use of acoustics to study suspended sediment transport processes, in environments of
539 non-cohesive inorganic sandy sediments, has developed significantly over the past two to
540 three decades. Underpinning the use of the acoustic technology has been the development of
541 a comprehensive theory on the interaction of sound with suspensions of irregularly shaped
542 scatterers. These theoretical developments have been assessed using data from a number of
543 experimental studies. With the veracity of the scattering theory established for non-cohesive
544 sediments, it has been possible to develop inversion methodologies, to extract suspension
545 parameters, using the signal backscattered from suspended sediments in the marine
546 environment. It has been this combination of technology advancement, theoretical
547 developments and inversion methodologies, which has led to the increasing application of
548 acoustics in the study of non-cohesive sediment transport processes (Thorne and Hay 2012).

549

550 Although acoustics has had success in its application over non-cohesive sandy beds, its utility
551 in cohesive silt and clay environments, where flocculation can occur, has been much more
552 challenging. The primary reason for this difficulty has been the lack of experimental data and
553 a theoretical framework for the interpretation of the backscattered signal from flocculating
554 suspensions. This has resulted in the analysis of acoustic measurements of cohesive
555 suspension processes being much more problematic than that of non-cohesive. To investigate
556 the scattering characteristics of primary particles and flocculating cohesive sediments a
557 laboratory study was conducted and the results recently published (MacDonald et al, 2013).
558 In complementary studies (Thorne et al, 2012a,b), aimed at developing a model of the
559 acoustic scattering characteristics of suspended cohesive sediments, an approach using
560 heuristic formulations based on spherical scatterers was proposed. Such a heuristic approach
561 has often been used in underwater acoustics to study complex shaped scattering bodies
562 (Stanton and Chu, 2000; Thorne and Meral; 2008). In the present study a modified solid
563 elastic sphere has been used to describe the scattering of the primary particles and a modified
564 fluid elastic scatterer to characterise the scattering of large low density flocs. To link these two
565 descriptions together a hybrid model has been proposed based on variable particle density to
566 represent the processes of flocculation. This variable density has been used with Woods
567 equation to obtain the compressional sound velocity in the flocs and thereby their acoustic
568 scattering characteristics. The aim of the model was to describe the scattering characteristics
569 of the primary micron size sediments through the transition process of flocculation, to large

570 low density flocs. To examine the model comparisons were made with recently published
571 data (MacDonald et al, 2013). The output from the model captured the observations
572 reasonably well, considering the lack of detailed internal floc structure incorporated into the
573 heuristic hybrid model. To accommodate the internal structure of flocs into a description of
574 their scattering characteristics, theories such as those of Biot 1956a, 1956b, 1962 and the
575 more recent works of Buckingham 1997, 1998, 2000, 2005 and 2007 could be considered.
576 These provide a more detailed description of the interaction of sound with an aqueous porous
577 body composed of marine sediments and may therefore have application to floc scattering.

578

579 The model presented here compared reasonably well with the measurements from the
580 laboratory study, where conditions were well prescribed and parameters carefully measured.
581 However, the results in figures 3-5 show that scattering characteristic can have significantly
582 different values depending on the input values to the model. Changes in C_f , m , ζ , γ , ρ_s , c_s , $n(a)$
583 and the coefficients in equation (6) all impact on the modelled acoustic scattering of
584 flocculating sediments. Therefore the application of the model to field studies has to be
585 carried out judiciously, with as many supporting measurements as practicable to constrain the
586 input parameters and with outputs calculated using reasonable variability on the inputs to
587 establish the veracity of the model output.

588

589 If acoustics is to be used quantitatively in flocculating marine sediment process studies, then
590 a description of the acoustic scattering processes is required, coupled with an inversion
591 algorithm to extract suspension parameters. The model presented here is considered to be a
592 step towards this goal. To-date only one controlled experiment on the acoustic interaction
593 with flocculating sediment has been reported, with a flocculation region between $x_0=0.5-3.0$.
594 There is a broad region, roughly between $x_0=0.01-0.5$ which was not covered in the
595 experimental study. Therefore there is a definite requirement for further well controlled
596 laboratory studies on acoustic scattering with suspension of flocculating sediments. This will
597 enable the present and any other developing theoretical models to be assessed and advanced.
598 It is anticipated that such measurements and modelling will broaden the application of the
599 quantitative application of acoustic into the complex regime of flocculating sediments.

600

601

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603

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884 **FIGURE CAPTIONS**

885 Figure 1. Theoretical comparisons of sphere and heuristic intrinsic form function, f , and
886 intrinsic normalised total scattering cross-section, χ . Equations used are given by the numbers
887 in the brackets in the legend, see text for the equations. Measurements are presented from
888 Thorne and Meral, 2008 (●) and Richards et al, 2003 (x) for solid scatters. a) and b) are for a
889 solid scatterer and c) and d) are for a fluid scatterer.

890

891 Figure 2. Calculations for a) the normalised effective density, $\rho_e/(\rho_s-\rho_w)$, density ratio, γ , and
892 velocity ratio, ζ , b) the intrinsic form function, f , and c) the intrinsic normalised total
893 scattering cross-section, χ , for a solid, fluid and hybrid scatterer. Equation numbers are given
894 in brackets in the legend, see text for the equations.

895

896 Figure 3. Calculations for a) the hybrid ensemble form function, f_{ho} , and b) the hybrid
897 ensemble normalised total scattering cross-section, χ_{ho} , with increasing normalised standard
898 deviation, δ , for a lognormal particle size probability density function, $n(a)$.

899

900 Figure 4. Variation of a) the normalised density of the scatterer, γ , with C_f and m and the
901 impact this has on b) the hybrid ensemble form function, f_{ho} , and c) the hybrid ensemble
902 normalised total scattering cross-section, χ_{ho} . The lines represent $C_f > 0.001$ and $m > 1.0$ (— —),
903 $C_f < 0.001$ and $m < 1.0$ (· · ·) and $C_f = 0.001$ and $m = 1.0$ (—).

904

905 Figure 5. Variation of a) the hybrid ensemble form function, f_{ho} , and b) the hybrid ensemble
906 normalised total scattering cross-section, χ_{ho} , with the lower limit of the density, γ_o , and
907 velocity ratios set equal to $\zeta_o = \gamma_o = 1.005-1.3$.

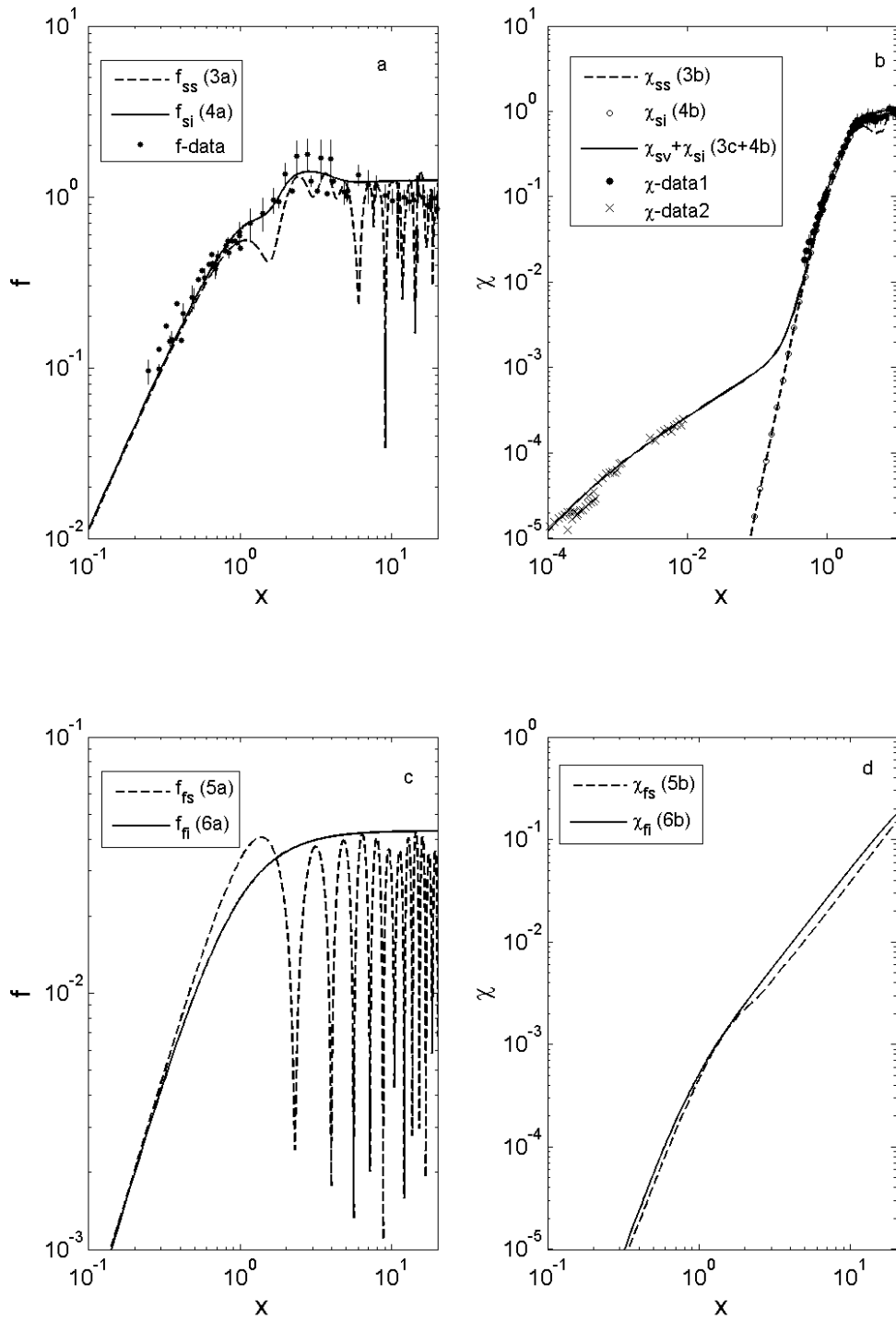
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909 Figure 6. Lognormal particle size probability density function fits (—) to measurements (●)
910 for; a) the primary particles and b) an example for the flocs.

911

912 Figure 7. Comparison of the model output with the measurements. In the legend for the
913 measurements P refers to primary particles, F to flocs and the subscript is the acoustic
914 frequency in megahertz. The three lines are the modelled scattering characteristics at 3.0
915 MHz (— —), 4.0 MHz (—) and 5.0 MHz (— • —) using the central parameters, see text, with
916 the grey region associated with uncertainties in the floc parameters, see text.

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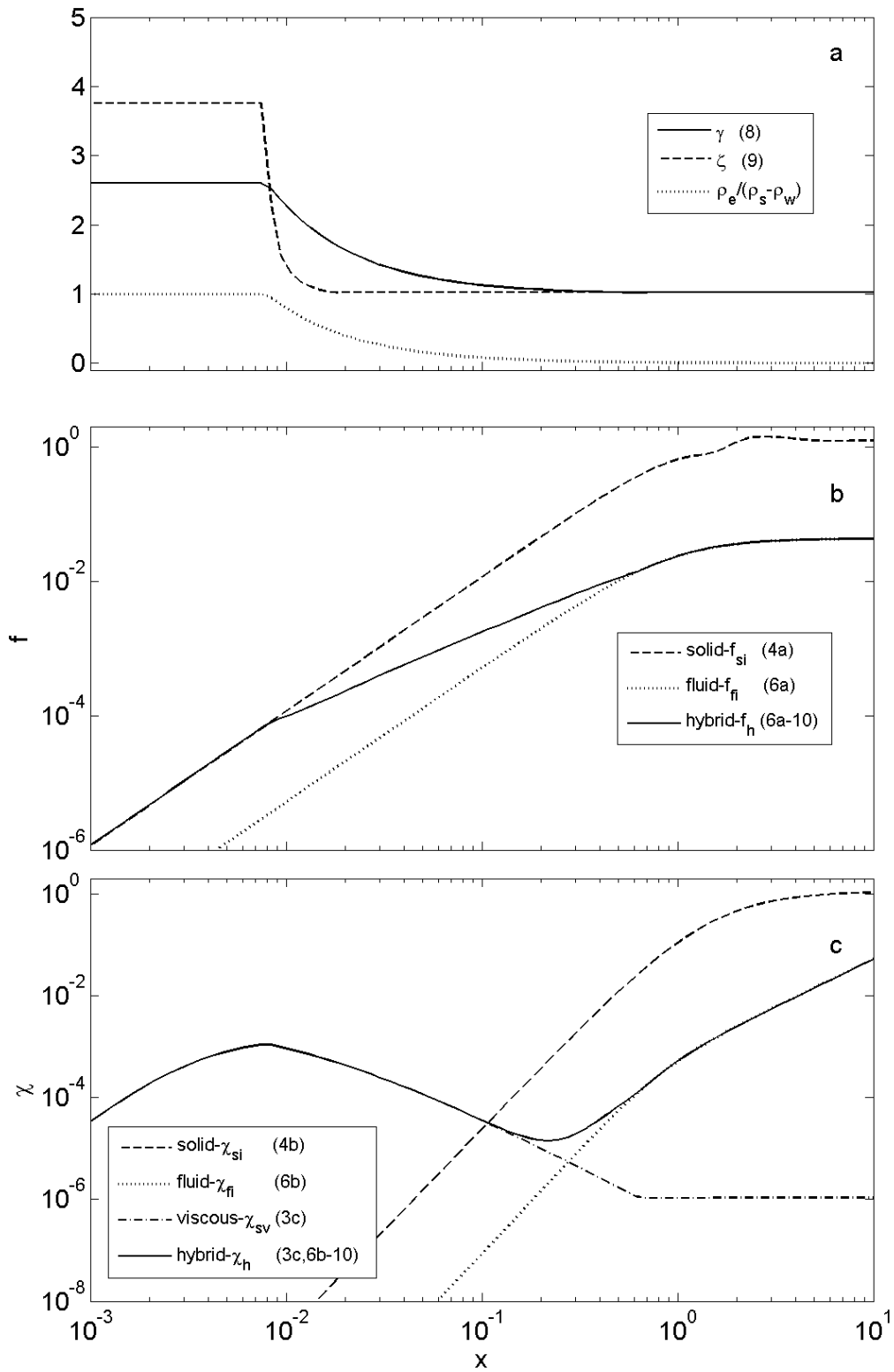


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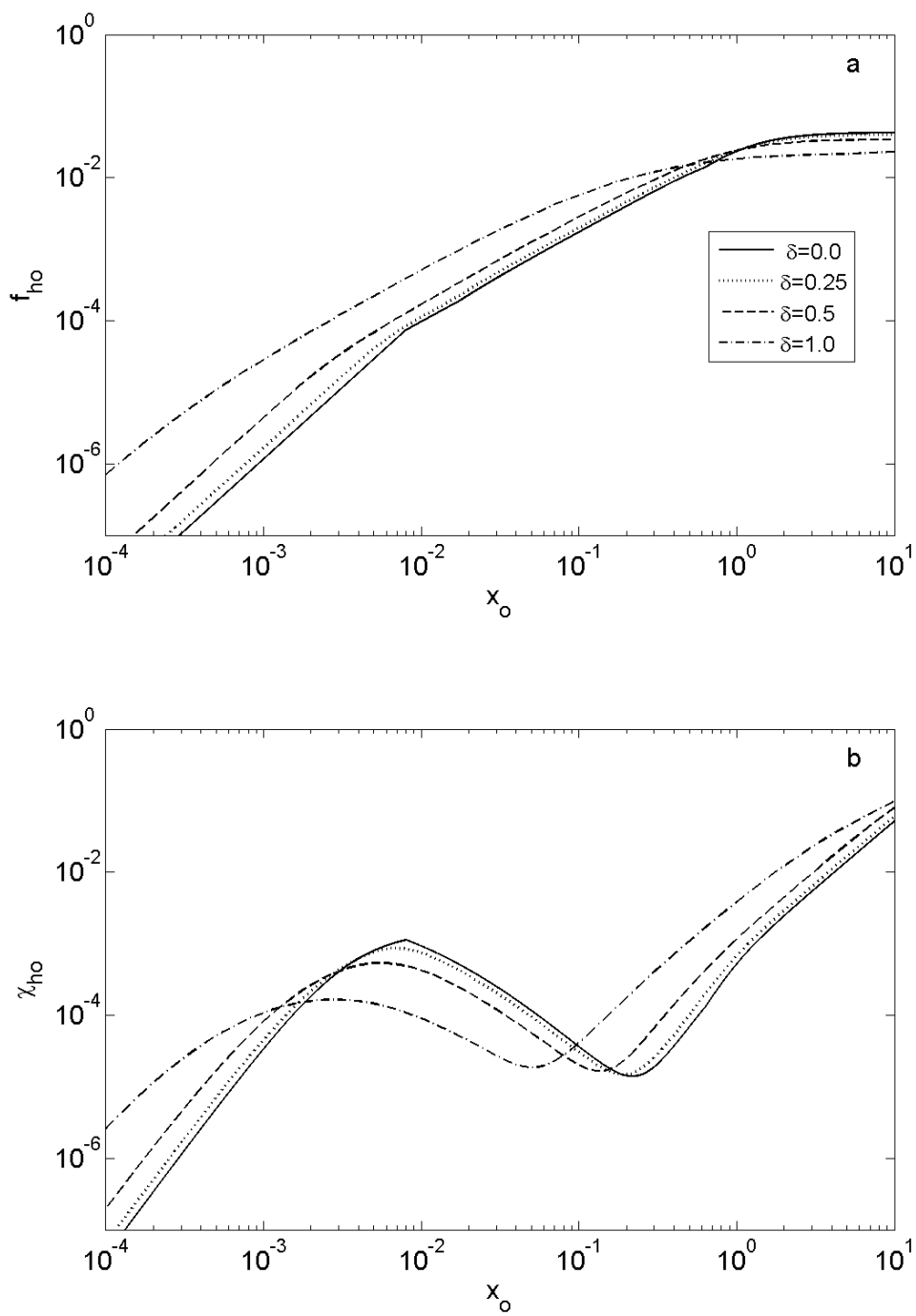
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927 Fig 2.

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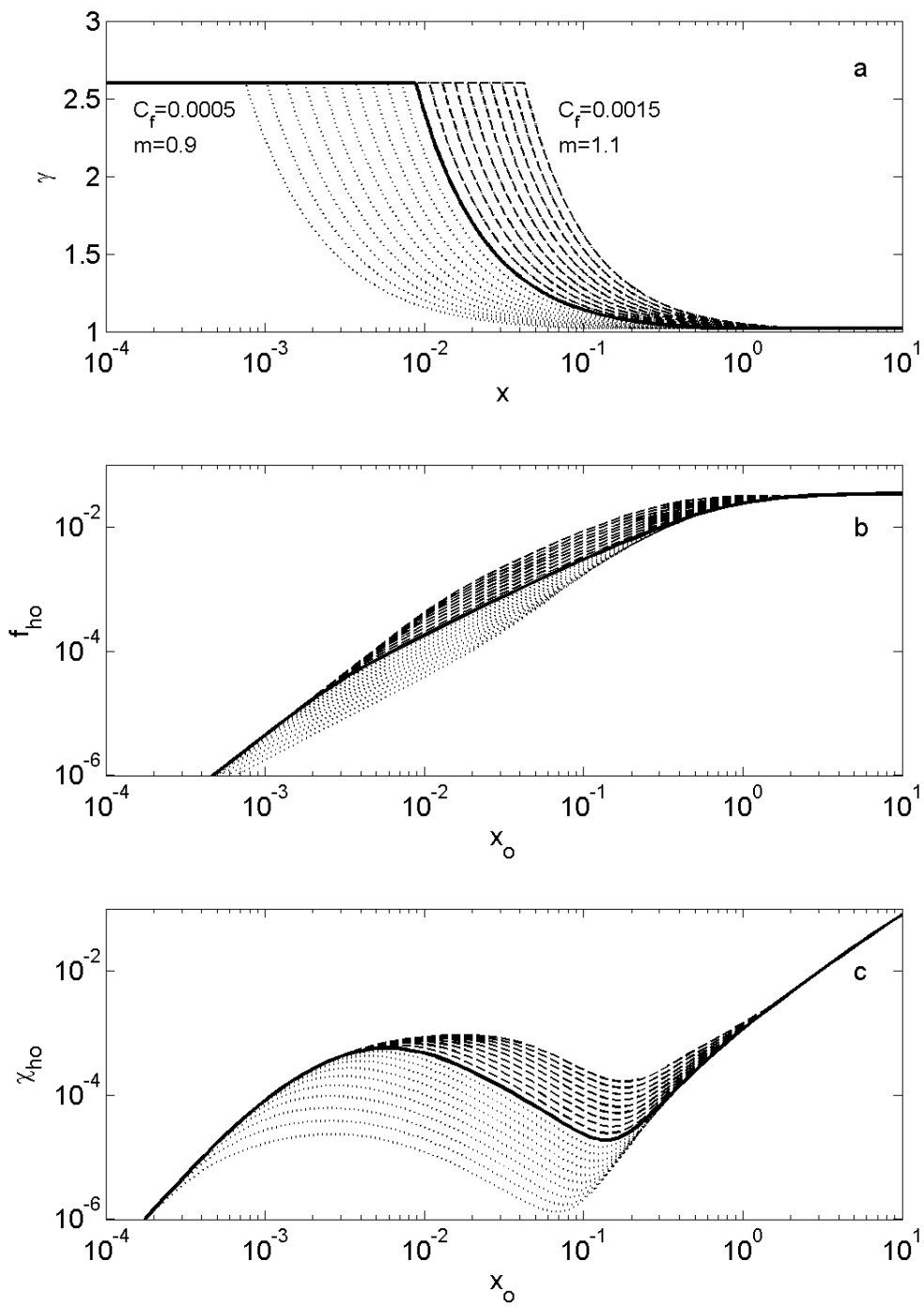
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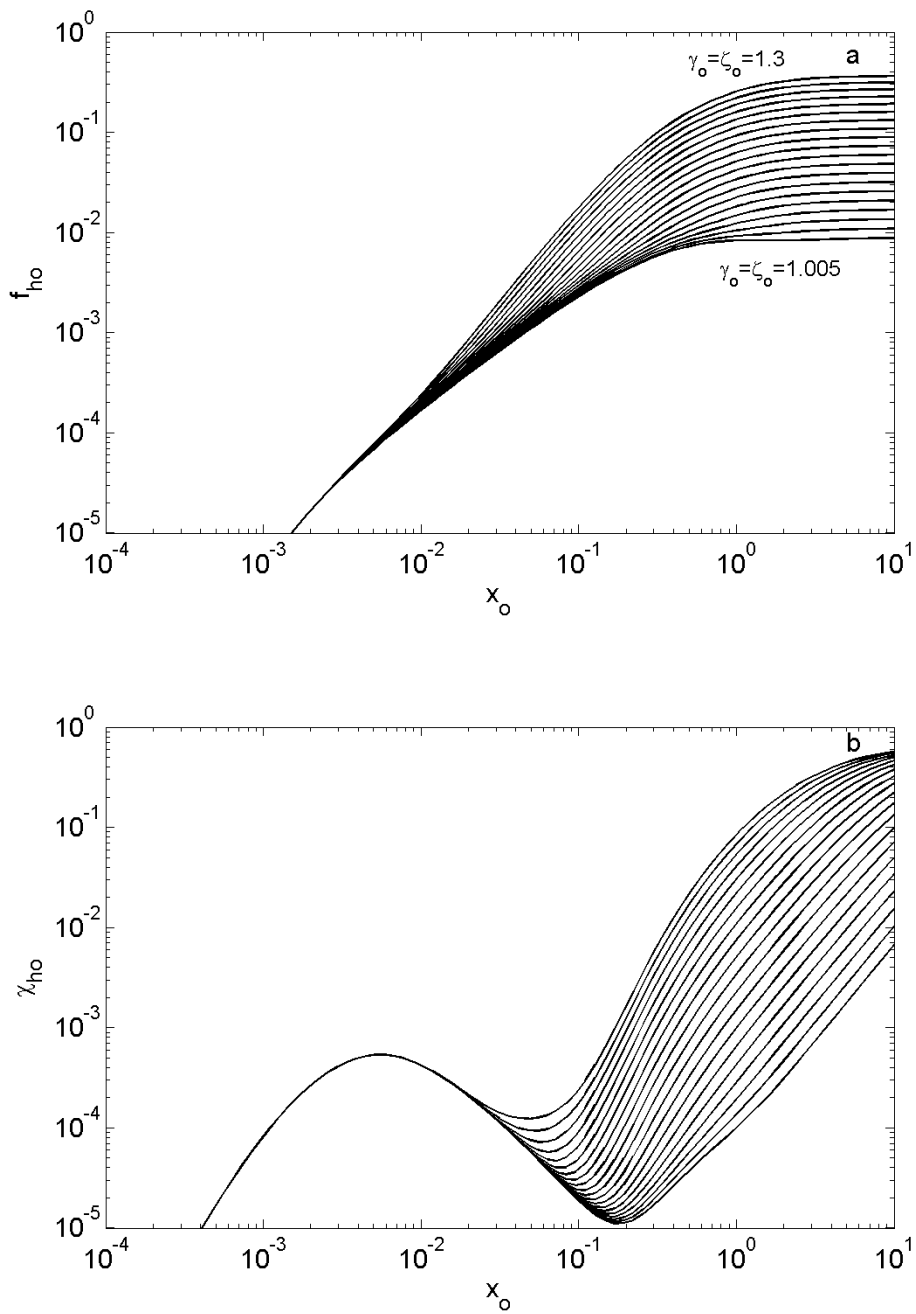
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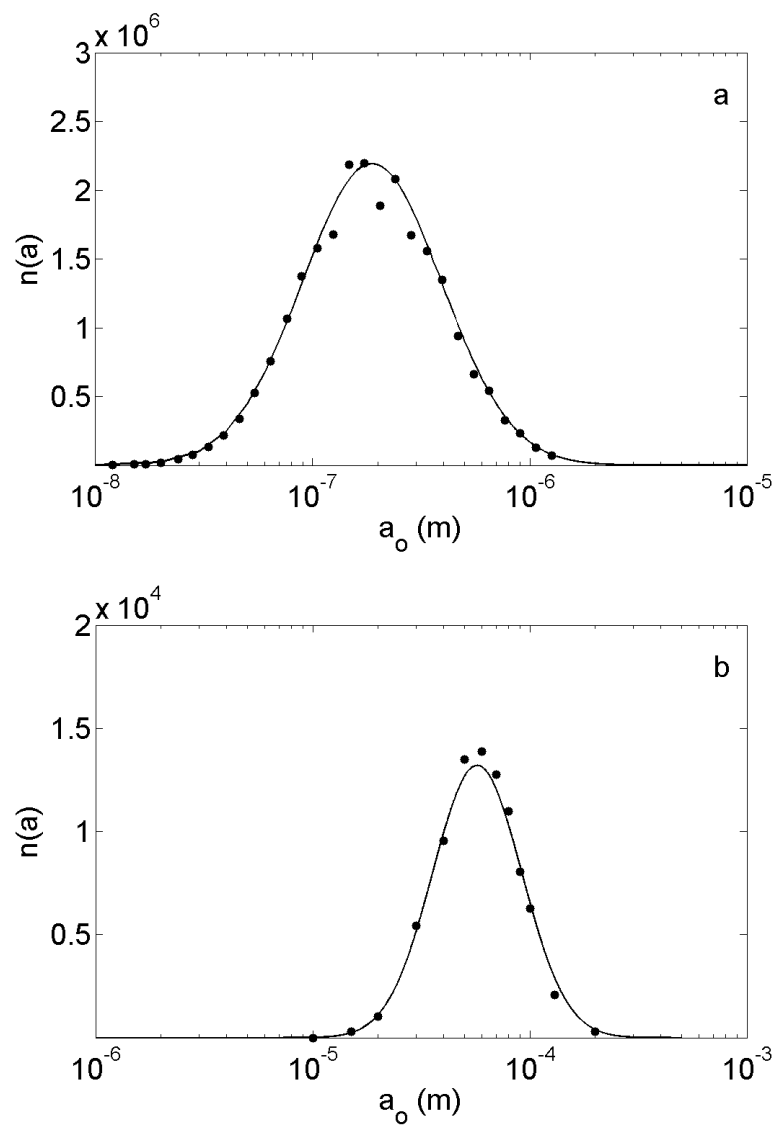
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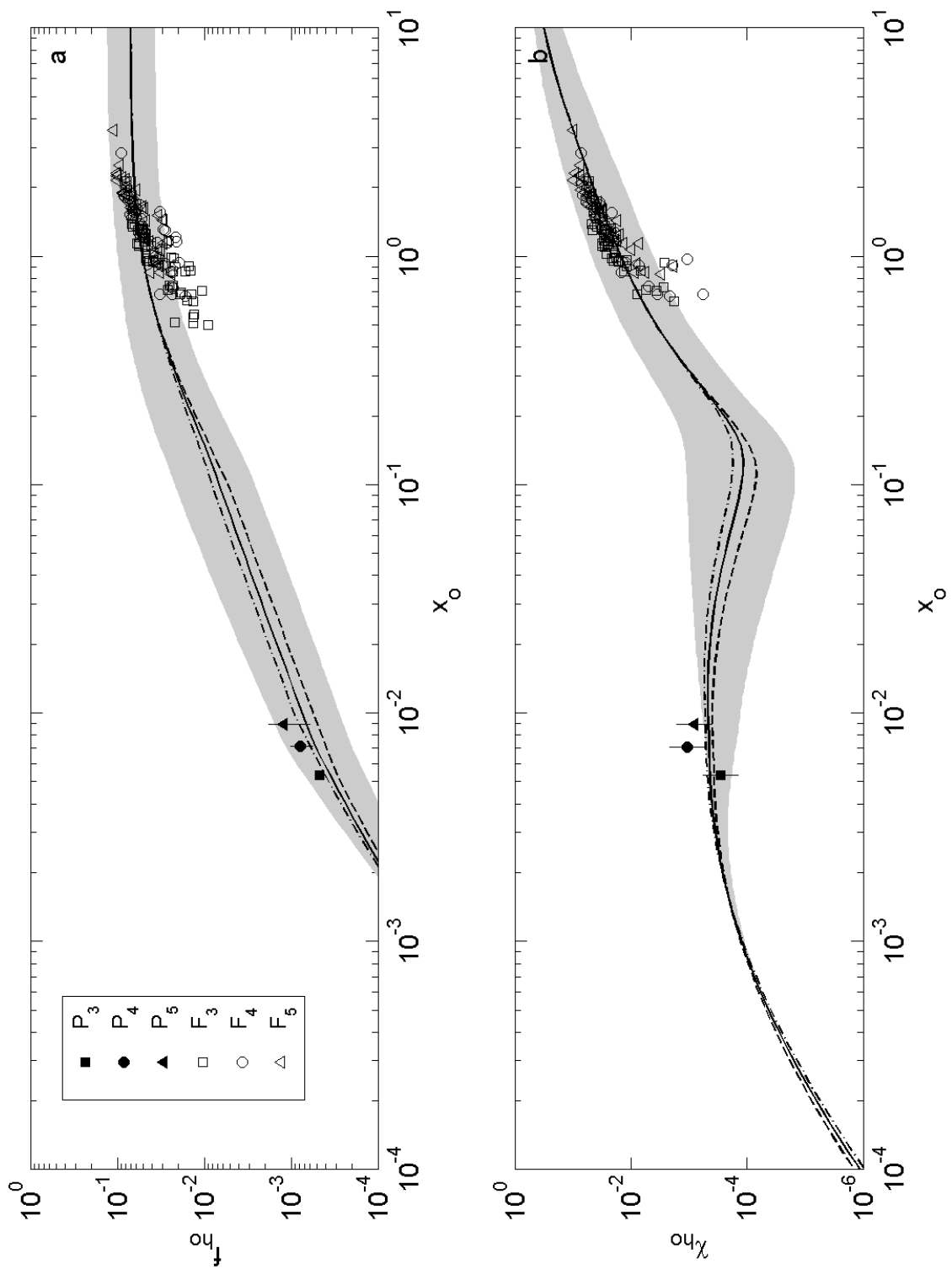
948 Fig 6.

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953 Fig 7