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5 **Using a Bayesian framework and global sensitivity analysis to identify strengths and weaknesses**
6 **of two process-based models differing in representation of autotrophic respiration**

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24 **Introduction**

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28 During the last decades, forests have been experiencing fast changes in the environmental
29 conditions, to which forest management must adapt. Process-based models (PBMs), based on eco-
30 physiological principles, are invaluable tools for sustainable and adaptive forest management (Fontes et
31 al., 2010). PBMs allow for the estimation of site productivity and can simulate the effects of
32 management and environmental constraints on stand growth and the probable influence of climate
33 change on forest productivity. Furthermore PBMs enable analyses at different spatial and temporal
34 scales (Fontes et al., 2010). However, calibration of PBMs is often difficult because they tend to have
35 many parameters and outputs for which only few data are available. Moreover, because models are
36 simplifications of reality, we need to assess carefully how well their structure allows for simulation of
37 the phenomena of interest. Bayesian statistics, based on probability theory, offers an alternative to the
38 calibration problem and can provide parameter estimates with estimates of their uncertainty (van Oijen
39 et al., 2005). The Bayesian approach also allows for the evaluation of model structure by quantifying
40 the extent to which data support different models (Kass & Raftery, 1995; van Oijen et al., 2011). In
41 addition, the increasing availability of eddy-covariance measurements with high temporal resolution
42 (Pereira et al., 2007) provided by the Fluxnet and other regional networks, allows for calibration as
43 well as for model validation.
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49 In this work a Bayesian framework and a global sensitivity analysis were used in combination to
50 test an improvement of a process-based model (3PGN (Xenakis et al., 2008)) and to study model
51 behaviour. Two versions of 3PGN that differ in their representation of autotrophic respiration (R_{aut})
52 were calibrated and evaluated. 3PGN is based on a constant value of carbon-use efficiency (CUE),
53 defined as the ratio between net primary production (P_N) and gross primary production (P_G) (Gifford,
54 2003); therefore, R_{aut} is modeled as a fixed proportion of P_G . The understanding of the factors
55 regulating R_{aut} is one of the most challenging questions in ecological forest research. Many studies
56 argue that $P_N : P_G$ is constant (Dewar et al., 1998; Gifford, 1994, 2003). Waring et al. (1998) proposed
57 a universal value of 0.47 for most forests. More recently, van Oijen et al. (2010), using a mathematical
58 approach based on the law of conservation of mass, showed that $P_N : P_G$ is narrowly constrained.
59 However, owing to the difficulty in measuring carbon-use efficiency and in particular the P_G
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3 component, methodological problems can mask variation in $P_N : P_G$ (Medlyn & Dewar, 1999), casting
4 doubts about the existence of fixed values of the ratio between net and gross primary production.
5 DeLucia et al. (2007), conducting a literature review, found that CUE varied between 0.23 and 0.83
6 across 60 different forests, with an average of 0.53.
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9 A different approach is to model R_{aut} as the sum of two components: maintenance (R_{maint}) and
10 growth (R_{growth}) respiration, the first being proportional to the live biomass and its temperature, the
11 second being proportional to P_N . This theory was developed in the 1970s by McCree (1974), and many
12 authors followed this approach (e.g., Penning de Vries, 1974, 1975; Ryan & Waring, 1992). A detailed
13 review of the progress achieved in respiration modeling over the last decades can be found in Amthor
14 (2000). Warmer climates should have higher respiration costs, because the maintenance respiration
15 increases exponentially with temperature (Ryan, 1991). This kind of R_{aut} modeling ($R_{\text{maint}} + R_{\text{growth}}$)
16 has been used in many process-based models (e.g. CABALA (Battaglia et al., 2004); PIXGRO (Adiku
17 et al., 2006); MAESTRO (Wang & Jarvis, 1990)).
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21 In the present work the original version of 3PGN, based on a constant $P_N : P_G$ ratio, and a new
22 version (3PGN*), in which R_{aut} is modeled as the sum of maintenance and growth plant respiration,
23 were calibrated and evaluated under a Bayesian framework. As proposed by van Oijen *et al.* (2011), the
24 Bayesian framework consisted of model calibration, model comparison and analysis of model-data
25 mismatch. Sensitivity analyses of the two model versions were also carried out to have a better insight
26 of model behavior (Campolongo et al., 2007). For the first time a Bayesian framework and a global
27 sensitivity analysis, Morris method (Morris, 1991), were used in combination to highlight the strengths
28 and weaknesses of the two model versions and to evaluate their performances.
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33 **Materials and methods**

34 *Overview of the methodology*

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37 Our study used eddy-covariance data and forest measurements collected at two different sites: a
38 CarboEurope-IP site (Espirra forest) and a field experiment (Furadouro experiment). At a first stage
39 both models were calibrated using the full dataset (i.e., Espirra forest and Furadouro experiment). The
40 Bayesian framework proposed by van Oijen *et al.* (2011) and the Morris method were used in
41 combination to better understand the behaviour of the models.
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45 Subsequently, two Bayesian model comparisons were performed to evaluate the models. The
46 first BMC was carried out in light of the prior knowledge of the two models (*prior BMC*). Meanwhile,
47 for the second BMC part of the dataset was used for model calibration and the rest of the data were
48 used for model evaluation (*post BMC*). For the *prior BMC* 1000 parameter vectors were sampled from
49 the prior distributions of the two model versions. The models were run with the sampled parameter sets
50 and the distributions of model outputs were used in a Bayesian model comparison. For the *prior BMC*
51 the models were compared in light of the full dataset (i.e., Espirra forest and Furadouro experiment).
52 For the second Bayesian model comparison, the models were calibrated with the Furadouro experiment
53 data and then compared using the Espirra forest dataset.
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60 *3PGN Structure*

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3 3PGN was developed by Xenakis *et al.* (2008) coupling two models, 3-PG (Physiological
4 Principles in Predicting Growth) and ICBM (Introductory Carbon Balance Model). The resulting model
5 structure was comprehensively described by Xenakis *et al.* (2008) – only a brief outline is given here.
6

7
8 A detailed description of 3-PG was provided by Landsberg and Waring (1997) and by Sands
9 and Landsberg (2002). 3-PG is composed of five sub-models. One is used to calculate the productivity
10 of the stand and another is used for partitioning biomass between different organs (foliage, roots and
11 stem). The other three sub-models are used to determine the changes in stem number, soil water
12 balance and variables of interest to forest managers, such as stand timber volume (V , $\text{m}^3 \text{ha}^{-1}$), mean
13 diameter at breast height (D , cm) and stand basal area.
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16 3-PG is based on the principle that the net primary production of a stand is primarily determined
17 by radiation interception. P_G is calculated by multiplying the fraction of the photosynthetically active
18 radiation absorbed by the stand (Φ_{aPAR}) with canopy quantum efficiency (α_c). Φ_{aPAR} is calculated using
19 Beer's law. The canopy quantum efficiency is calculated by multiplying a theoretical maximum canopy
20 quantum efficiency (α) with an array of site and physiological modifiers that vary between 0 and 1
21 (functions of atmospheric vapor pressure deficit, air temperature, frost, water balance, age and fertility
22 rating (FR)). P_N is calculated as a constant fraction (Y) of P_G (Law *et al.*, 2000; Waring *et al.*, 1998).
23 The carbon allocation routine sub model is based on allometric equations, on a single-tree basis. A
24 fraction of P_N is allocated below-ground by a root allocation coefficient that is affected by soil fertility.
25 The remaining biomass is partitioned between the aboveground organs as a function of diameter at
26 breast height and foliage: stem ratio.
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31 The 3-PG model has been applied to many different species and sites and it is widely used in
32 research as well as by companies to assess forest growth and site productivity. Fontes *et al.* (2006)
33 parameterized 3-PG for Portuguese plantations of *Eucalyptus globulus*, Labill., demonstrating that
34 carbon allocation of *E. globulus* in Portugal differs strongly from allocation patterns in Australian
35 plantations.
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38 A complete description of ICBM is provided by Andr n and K tterer (1997) and K tterer and
39 Andr n (K tterer & Andr n, 1999, 2001). ICBM/2N considers three pools of C and three pools of N in
40 the soil, consisting of different forms of organic matter: the “young labile” pool, that includes small
41 tree detritus (such as litterfall and root turnover), a “young refractory” pool, that includes coarse woody
42 detritus (coarse root, branches and stems) and an “old” pool, that includes the recalcitrant organic
43 matter. Each pool has a different decomposition rate that varies along the year with environmental
44 conditions (i.e., temperature and soil water content), but does not change during stand development
45 (M kel  & Vanninen, 2000; Titus & Malcolm, 1999). Carbon decomposed from the young pools enters
46 the old pool at a constant relative rate of humification. The fraction from each young pool that is
47 decomposed but not humified is considered as respiratory loss. Similarly, decomposition losses take
48 place from the “old” pool. The sum of all the out-fluxes from the three pools gives the heterotrophic
49 respiration. The nitrogen balance is based on fixed C:N ratios and the size of the C fluxes and pools.
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53 In 3PGN, the biomass losses of the stand (litterfall, root turnover, death of trees, but excluding
54 tree harvesting), calculated by 3-PG, are the inputs for ICBM/2N. The latter model is used to calculate
55 the heterotrophic respiration, but not the site fertility parameter (FR) of 3-PG. As in the original version
56 of 3-PG (Landsberg and Waring, 1997), the FR parameter was site specific. In this work, five different
57 FRs were parameterised for each site by means of Bayesian calibration.
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61 *The two versions of 3PGN*
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3 In the two 3PGN versions used in this work, tree diameter D was calculated as a function of
4 total aboveground dry biomass (*i.e.*, leaves included).
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$$D = StCn * W_{abv}^{StPw} \quad (1)$$

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12 where W_{abv} is the aboveground biomass (kg per tree) and $StCn$ and $StPw$ are regression coefficients.

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14 Because average stand height (H) is an important stand variable, a new equation for the calculation of
15 H was introduced.
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$$H = aH * W_{abv}^{bW} \quad (2)$$

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24 where aH and bW are regression coefficients.
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28 The two model versions used in this work calculate autotrophic respiration (R_{aut}) in different
29 ways. In the old version (3PGN), R_{aut} is proportional to photosynthesis. In the new version (3PGN*),
30 R_{aut} is the sum of respiration for maintenance (R_{maint}) and for growth (R_{growth}):
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$$R_{aut} = R_{growth} + R_{maint} \quad (3)$$

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39 Maintenance respiration is assumed to be a function of biomass and average temperature (T_{av})
40 and it follows different specific rates for the woody (r_w) and foliage (r_f) tissues. In the woody pool the
41 branches, stem and the root biomass were included.
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$$R_{maint} = \sum W_i r_i Q_{10}^{(T_{av}-20)/10} \quad (4)$$

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50 where W_i and r_i are dry weight and specific respiration rate, respectively, of the i th plant pool (woody
51 or foliage); Q_{10} determines the temperature responsiveness of respiration.
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53 Growth respiration is calculated as:
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$$R_{growth} = r_g * (P_G - R_{maint}) \quad (5)$$

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3 where r_g is the fraction of growth discarded as respiration (Penning de Vries 1975).
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5 Finally, P_N is calculated as:
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$$P_N = P_G - R_{\text{aut}} \quad (6)$$

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13 When the calculated $R_{\text{maint}} + R_{\text{growth}}$ exceed P_G total R_{aut} is set equal to P_G .
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15 The equations 4 and 5 were chosen because they required fewer parameters than other R_{maint} and
16 R_{growth} modeling approaches (Amthor, 2000; Ryan et al., 1996). With the insertion of the new
17 equations, just three additional parameters were entered into the model, maintaining model simplicity,
18 in agreement with the idea on which 3-PG was developed (Landsberg, 2003; Landsberg & Waring,
19 1997).
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24 *Experimental sites and data acquisition* 25

26 The data used for model calibration and evaluation were collected at two sites: Espirra and
27 Furadouro. The Espirra forest dataset consisted of measurements of net ecosystem production (P_E , Mg
28 C ha⁻¹ y⁻¹), mean stand height (H , m) and mean stand diameter at breast height (D , cm). The dataset
29 from the Furadouro experiment consisted of measurements of foliage (WF , Mg of dry mass (DM)
30 ha⁻¹), stems (WS , Mg DM ha⁻¹) and roots (WR , Mg DM ha⁻¹), stand volume, mean stand height and
31 mean diameter at breast height. The whole dataset consisted of 305 data points between the seven
32 output variables considered (i.e., P_E , D , H , V , WF , WR and WS).
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38 *Espirra forest* 39

40 The carbon fluxes, from which P_E was derived, were measured by eddy covariance (Aubinet et
41 al., 1999; Baldocchi, 2003) in Espirra (Pereira et al. 2007). This CarboEurope-IP site is a 300 ha
42 *Eucalyptus globulus* plantation (38°38'N, 8°36'W) tended as a coppice. Originally planted in 1986 at 3
43 x 3 m spacing, ca. 1100 trees ha⁻¹, was 11 years old (2nd rotation) in the end of the period analyzed,
44 and ca. 20 m height. The mean annual temperature for the site is 16°C whereas the mean annual
45 precipitation is 709 mm, more than 80% of which occurs from October to April.
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48 The flux data were collected between October 2002 and December 2005 at the half hourly
49 scale. Net ecosystem production data were aggregated at monthly time step and used for model
50 calibration and validation. Flux data quality control followed the CarboEurope-IP recommendations;
51 gap filling was performed according to Reichstein et al. (2005).
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56 *Furadouro experiment* 57

58 The mensurational data used for model calibrations were collected in a field experiment
59 installed from 1986 to 1992 at Quinta do Furadouro (Óbidos, Portugal, 39°29'N, 9°13'W, 30 m a.s.l.).
60 The mean annual temperature is 15.2 °C and the mean annual precipitation is 607 mm, but less than
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3 10% occurs between May and September. Three months old *E. globulus* seedlings were planted at 3 x 3
4 m spacing; each seedling was supplied at planting with 200g of a commercial fertilizer containing
5 14.0g of N, 18.3g of K and 11.6g of P. Before planting, the soil was ploughed at 80 cm depth and 1.5
6 Mg ha⁻¹ of dolomitic limestone (66.5% of CaCO₃, 32.5% of MgCO₃) was applied.
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8
9 The experimental design consisted of three treatments and a control. The treatments were daily
10 irrigation from April to October (I), application of a pelleted fertilizer in March and October of each
11 year (F) and daily irrigation as in I, combined with a liquid fertilizer solution once a week (IF). No
12 fertilization (except the initial amount at plantation) and irrigation were supplied to the control (C).
13

14 The differences in soil nitrogen concentration between C and I were due to some amount of N
15 contained into the irrigation water; while the different amounts of nutrient in F and IF resulted both
16 from the influence of irrigation water and from different application rates. For these reasons, the
17 fertility rate parameter of 3-PG was calibrated independently for each treatment. Different prior were
18 assigned to the FR of C, F, IF; Table 1b shows the minimum and maximum values and the distributions
19 of these parameters.
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22 23 24 *Sensitivity analyses* 25

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27 Sensitivity analyses can vary from the simplest class of the One Factor At the Time (OAT) to
28 global sensitivity. While OAT quantifies model output variation in relation to changes of one factor at
29 a time, global sensitivity analyses evaluate model's output sensitivity to simultaneous changes in
30 several factors. In this work the global sensitivity method proposed by Morris (1991) was adopted. This
31 method is a good compromise between efficiency and accuracy and it is particularly well-suited when a
32 high number of factors are considered and/or the model is costly to compute (Campolongo et al. 2007).
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34

35 The method consists of computing basic statistics, i.e., mean (μ) and standard deviation (σ),
36 from the distribution of a number of incremental ratios, called Elementary Effects. μ gives the overall
37 importance of an input factor, while σ describes non-linear effects and interactions between factors. For
38 a more detailed analysis of this methodology see Campolongo et al. (2007) and Morris (1991).
39
40

41 Campolongo et al. (2007) enhanced the Morris method improving the sampling strategy and
42 proposed to calculate the mean of the distribution of the absolute values of the elementary effects (μ^*).
43 μ^* is calculated to solve the problem of non-monotonic models, where the effects of opposite signs
44 could mask the importance of a factor.
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46

47 For the sensitivity analyses of 3PGN and 3PGN* we considered the following output: stem,
48 foliage and root biomasses, average stand diameter at breast height, average stand height, stand volume
49 and annual net ecosystem productivity (aP_E). Because output sensitivity to the factors could vary
50 across stand development, the sensitivity was computed at different stand ages (i.e., at four, eight and
51 twelve years). For the sensitivity analysis the environmental data (weather, soil, management) of the
52 Espirra forest were used as drivers for the models. The factors involved in the analysis consisted in the
53 parameters and the site variables reported in Table 1a-b. Factors ranged between the minimum and
54 maximum values used for the BC (Table 1).
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59 *Bayesian framework* 60 61 62 63 64 65

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3 Model calibration and comparison were carried out using a Bayesian approach. Bayesian
4 statistics is part of probability theory and it requires that beliefs about parameter values and models be
5 expressed as probability distributions. Our initial information about plausible parameter values, and
6 about which model is correct, is expressed in the *prior* distribution $P(\theta)$. Observed data (O) that are
7 used to update the prior distribution enter the analysis through the so-called *likelihood* function $L(\theta) =$
8 $P(O|\theta)$. An updated, *posterior* distribution is then found by application of Bayes' Theorem:
9

$$10 \quad P(\theta|O) = c P(O|\theta) P(\theta) \quad (7)$$

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17 where, $c = p(O)^{-1}$. The value c is fixed, and usually it is not necessary to compute it explicitly.
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21 *Likelihood function*

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23 The likelihood function (L) used was proposed by Sivia (2006) and it is described by the
24 equations (8) and (9):
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26

$$27 \quad P(O|\theta) = \prod_{i=1}^N \frac{1}{\sigma_i \sqrt{2\pi}} \frac{1 - \exp(-R_i^2/2)}{R_i^2} \quad (8)$$

$$28 \quad R = (\text{sim}(\theta) - O)/\sigma \quad (9)$$

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38 where, $\text{sim}(\theta)$ is the output from the model for parameter values θ , N is the number of data points and σ
39 is the uncertainty about the random error of the i th data point.
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42 This likelihood was chosen because it is heavy-tailed, so it puts less weight on the outliers that
43 can occur in eddy covariance measurements (Sivia 2006, Van Oijen et al. 2011).
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47 *Prior distribution for the parameters*

48
49 Table 1 shows the types of distribution and their bounds that were used for the prior marginal
50 distributions of the parameters. The prior was assigned using different sources of information:
51 literature, measurements and posteriors from previous Bayesian calibrations.
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53

54 For parameters for which knowledge is scarce the uniform distribution was chosen. The
55 truncated Gaussian distribution was assigned to many of the other parameters, using information
56 derived from literature. Those distributions were also quite uninformative (not too peaked).
57
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59 The prior distributions of the woody and foliage specific respiration rates (r_w and r_f ,
60 respectively) of eq. 5 were fitted with gamma distributions, on the basis of spot gas exchange
61 measurements collected at the Nicolaus site, close to the Espirra forest (Cerasoli et al., 2009).
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3 Since data were available to calibrate the allometric equations (eq. 1 and 2) and the 3PGN
4 equation to calculate the specific leaf area (*SLA*) as time function (eq. 10), Bayesian calibrations were
5 carried out independently for those equations.
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7

$$SLA(t) = SLAI + (SLAO - SLAI) * e^{-(\ln 2)(t / tSLA)^2} \quad (10)$$

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12
13 where *t* is the stand age, *SLAO* is the specific leaf area at age 0, *SLAI* is the specific leaf area for mature
14 leaves, *tSLA* is the age at which $SLA = (SLAO + SLAI)/2$.
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16

17 After Bayesian calibration (*BC*), the posterior distributions of the parameters of eq. 1, 2 and 10
18 were fitted with Weibull, normal and gamma distributions and then used as prior for the *BCs* of the
19 whole models.
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22 23 24 *Bayesian calibration (BC)*

25 Bayesian calibration revises the state of knowledge about parameter values using new data.
26 Process based models are not analytically solvable and they need to be run to quantify the likelihood.
27 Therefore, to summarize the posterior distribution as a sample, from which we can calculate summary
28 statistics like the posterior mean, we used the version of Markov Chain Monte Carlo (*MCMC*), known
29 as the Metropolis-Hastings random walk (Robert & Casella, 2004). The *MCMC* method aims to
30 converge the sampling on the region of the parameter space with highest probability density. A
31 complete description of the Metropolis-Hastings algorithm is given in van Oijen et al. (2005).
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35 To optimise the *MCMC*-algorithm, some preliminary calibrations were carried out, varying the
36 chain length and the scale of the proposal distribution, in order to achieve efficient convergence of the
37 Markov chain. *BCs* were carried out with a chain length of 100,000 and 500,000 and the burn-in was
38 40% of the chain length. To assess convergence of iterative simulations, the Gelman-Rubin criterion
39 (Gelman & Rubin, 1992) was used. This method consists in comparing at least two independent
40 simulated sequences, checking if the variance within the chains is comparable with the variance
41 between the chains. To monitor convergence, the potential scale reduction (\hat{R}) is estimated; \hat{R} tends to 1
42 when we have a good inference about the target distribution. Gelman et al. (2004) stated that for the
43 majority of the cases a value of 1.1 for \hat{R} is acceptable, but in some cases a higher level of precision
44 may be more appropriate. Three chains were considered to evaluate convergence; after the *BCs*, all
45 chains, discarding the burn in, were joined and treated as a unique sample from the target distribution.
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51 52 *Bayesian model comparison (BMC)*

53 Bayesian model comparison is a powerful extension of *BC* that allows for the evaluation of
54 different model structures on the basis of their relative likelihoods (Kass & Raftery 1995; van Oijen et
55 al. 2011). In this case the Bayesian theorem is not applied over the parameter space of a single model
56 but over a set of models (*M*) (van Oijen et al. 2005).
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$$P(M_k|O) = P(O |M_k) P(M_k) / \sum P(O |M) P(M) \quad (11)$$

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5 where k varies between 1 and n models. In our application, with just two model versions being
6 compared, $n=2$.
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8 Assuming no initial preference for either of the models ($P(M_1) = \dots = P(M_n)$), equation 11
9 becomes:
10

$$11 \quad P(M_k|O) = P(O|M_k) / \sum P(O|M) \quad (12)$$

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18 $P(O|M)$ is the “integrated likelihood” (IL) which is defined over the whole parameter space of
19 M , i.e., $P(O|M) = \int P(O|\theta)P(\theta)d\theta$.
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23 *Analysis of model-data mismatch*

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25 The Bayesian model comparison treats models as black boxes, giving just indication about
26 which model is more plausible (van Oijen et al. 2011). The mismatch of simulated vs. observed data
27 can also be evaluated using more classical methods that allow identifying model weakness. For each of
28 the seven outputs considered, normalised root mean squared error (*NRMSE*) and squared correlation
29 coefficient (r^2) were calculated across the range of prior and posterior distributions.
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32 Moreover, for the modes of the prior and posterior distributions we calculated the mean squared
33 error (*MSE*) of each output. *MSE* was decomposed in three components as suggested by Kobayashi and
34 Salam (2000):
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$$39 \quad MSE = \overline{(S - O)^2} = (\bar{S} - \bar{O})^2 + (\sigma_S - \sigma_O)^2 + 2(\sigma_S\sigma_O)(1 - r) \quad (13)$$

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41
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43 where S are model predictions and O are the observed data, σ_S and σ_O are their respective
44 standard deviations, and r is the correlation between simulated and observed data.
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46

47 The first component of *MSE* is a measure of the average deviation of the simulations from the
48 data (i.e., bias error), the second element indicates if the model is able to catch the variability of the
49 data (i.e., variance error) and the third element expresses the ability of the model to reproduce the
50 pattern of the fluctuations among the data (i.e., phase shift error) (Kobayashi & Salam, 2000).
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54 **Results**

55 *Sensitivity analyses*

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57 The Morris method allowed for the identification of the key parameters for each of the model
58 output across the stand development. Note that the sensitivity analysis was contingent on the parameter
59 space considered for the Bayesian calibration, because parameters varied between the minimum and
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3 maximum values used in the BC. Part of the results about sensitivity analysis are reported in Figure 1a-
4 b, where μ^* and σ of the five factors at which model outputs are most sensitive (highest μ^*) are plotted
5 for each year considered (i.e., 4, 8, 12). More comprehensive results were difficult to report in graphs
6 and tables because of the high number of parameters, therefore general results were only discussed in
7 the text.
8

9
10 Below a general overview of the sensitivity analysis results is given. The fertility rate parameter
11 (*FR*) had a strong impact on all the outputs of both models. The parameters related to the autotrophic
12 respiration were also key factors; in particular, the $P_N : P_G$ ratio (*Y*) for 3PGN and the woody biomass
13 respiration rate for 3PGN* had a high influence on all the output variables. 3PGN* outputs resulted
14 also quite sensitive to Q_{10} and r_g , while less sensitive to r_f . Both models were highly sensitive to the
15 light use efficiency parameter (i.e., *alpha*), the optimum temperature for growth (i.e., *Topt*) and the
16 minimum available soil water (*minASW*). In the first part of stand development model outputs were
17 highly influenced by the age at which canopy close (i.e., *fullCanAge*) To a lesser extent, model outputs
18 were sensitive to parameters related to fertility (i.e., *fNO*), allometric parameters (i.e., *StemPower* and
19 *StemConst*), allocation parameters (i.e., *pRx*, *pRn*, *pFS2*, *pFS20*), parameters related to temperature
20 stress (i.e., *Tmin*, *Tmax*), parameters and variables related to water stress (i.e., *maxAWS*, *MaxCond*,
21 *CoeffCond*), soil parameters (i.e., *klmax*) and other parameters like the litterfall rate at maturity
22 (*gammaFI*). Low impact on model outputs was given by factors related to age stress (i.e., *nAge*,
23 *MaxAge*, *rAge*), root turnover, soil parameters and variables (i.e., *hc*, *komax*, *krmax*, *O_C_i*, *Yl_C_i*),
24 the initial biomass of stem and root (i.e., *WS*, *WR*), frost days.
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29 *Bayesian calibration*

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31 Bayesian calibration allowed for the updating of the joint probability distribution for the model
32 parameters in light of the data used (i.e., Furadouro experiment, Espirra forest). Using *MCMC*-
33 algorithms, convergence must be reached by all the parameters to obtain an accurate sample for the
34 posterior distribution. For *BCs* of 100,000 chain length, the \check{R} factor, calculated over three chains,
35 assumed values lower than 1.1 for all the parameters (data not showed). However, almost 20% of the
36 parameters did not assume the same marginal posterior distribution over the three chains. \check{R} was lower
37 or close to 1.03 for the *BCs* of 500,000 chain length. In this case all parameter marginal posterior
38 distributions were similar over the three chains (data not showed). The *BCs* with different chain lengths
39 showed that 500,000 chain length and \check{R} factors lower than 1.03 were proper to reach a good
40 convergence for parameter rich process-based models.
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44 The likelihood distributions of the two model versions, for each output, before and after *BC*, are
45 presented in Figure 2. Higher values of the likelihood correspond to better model performances, while
46 the variance of the likelihood distribution is a measure of model accuracy.
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48 *BC* significantly shifted the likelihood towards higher values for *D*, *H*, *WS* and *V*. This means
49 that, after calibration, the models better simulated those variables. Posterior likelihoods of 3PGN and
50 3PGN* were also higher for *P_E*, even though, for this output the likelihood improvements were less
51 pronounced. On the contrary, *WF* and *WR* likelihoods decreased after *BC*.
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54 Figure 3 shows prior and posterior marginal distributions of all the parameters.
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56 For the two model versions, in most of the cases, parameter posterior distributions were very
57 similar (Figure 3). There were differences between the posterior distributions of parameters linked with
58 water balance and water stress (i.e., *LAIgcx*, *Blcond*, *MaxIntcpntn*, *MinASW*) (Figure 3a), temperature
59 and frost stress (i.e., *Topt*, *kF*) (Figure 3a), soil parameters (i.e., *klmax*) (Figure 3b), fertility parameters
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3 (i.e., FR and $fN0$) (Figure 3b). Posterior distributions were also different for $alpha$, $tSLA$ and
4 $fullCanAge$ (Figure 3a).

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6 From marginal posterior distribution it is possible to understand parameter uncertainty in light
7 of the data used for BC ; if the posterior variance is lower than the prior variance the data were
8 informative for the parameter. The data used for BCs allowed for the reduction in the uncertainty of
9 about 70% of the parameters (Figure 3). The data were not informative for some parameters related to
10 temperature stress (i.e., $Tmax$) (Figure 3a), water stress (i.e., $SWpower$, $Blcond$, $LAI_{maxIntcptn}$) (Figure
11 3a), age effect on forest growth (i.e., $MaxAge$, $rAge$, $nAge$) (Figure 3b), litterfall parameters (i.e.,
12 $gammaF0$, $tgammaF$) (Figure 3a), stand volume (i.e., $fracBBI$, tBB) (Figure 3b), stand attributes (i.e.,
13 the initial root biomass (WR_i) and tree density at plantation ($StemNo$)) (Figure 3b). Uncertainty also
14 underpinned many parameters of the soil decomposition model (ICBM/2N): the decomposition rates of
15 the different soil pools (i.e., $krmax$, $komax$, hc) and the initial soil carbon contents (i.e., Yr_C_i , Yl_C_i ,
16 O_C_i) (Figure 3b). The data were extremely informative for the allocation and allometric parameters
17 (i.e., $pFS2$, $pFS20$, $StCn$, $StPw$, pRx , pRn , aH and cD) (Figure 3a), temperature parameters (i.e., $Tmin$,
18 $Topt$) (Figure 3a), fertility parameters (i.e., $m0$, FR) (Figure 3b), the litterfall rate at maturity
19 ($gammaFx$) (Figure 3a), water stress parameters (i.e., $MaxCond$, $CoeffCond$) (Figure 3a), light use
20 efficiency and light interception parameters (i.e., $alpha$, k , $SLA0$) (Figure 3a), the age at which canopy
21 close ($fullCanAge$) (Figure 3a) and initial biomass (i.e., WF_i , WS_i) (Figure 3b).

22
23 Upon examination of the posterior distribution of the parameters related to the autotrophic
24 respiration, it is shown that the data were highly informative to Y (in 3PGN) and r_w (in 3PGN*),
25 moderately informative to Q_{10} and r_f and uninformative to r_g (Figure 3a).

26 27 28 29 30 31 32 33 *Analysis of model-data mismatch*

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35 For each output, MSE were calculated using the mode of the prior and posterior distributions
36 (Figure 4). BC allowed for the reduction, to a varying extent, of the phase, variance and bias error of
37 D , V and WS . Bias error for H was also strongly reduced, while phase and variance error slightly
38 increased. WF $MSEs$ increased after calibration, especially for 3PGN*; the highest component of WF
39 MSE was the phase error. WR MSE slightly decreased for 3PGN, because BC reduced the variance
40 error but increased the phase error. Instead, after BC , all WR MSE components significantly increased
41 in 3PGN*. BC decreased the MSE of net ecosystem production, but the phase error remained quite
42 high.

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44 For each model, 1000 parameter vectors were sampled from the prior and posterior distributions
45 to calculate the coefficient of correlation, the slopes and the normalized root mean squared error for the
46 comparisons between the predicted and the observed data. Table 3 shows the mean r^2 , slopes and
47 $NRMSE$ for both prior and posterior of the seven outputs.

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49 The coefficient of correlation was high for all the output apart for P_E . Even if r^2 , the slope and
50 $NRMSE$ of P_E improved after the calibration, the models were not able to reproduce the net ecosystem
51 productivity pattern over the months. BC significantly improved all the statistics (i.e., r^2 , slopes and
52 $NRMSE$) for D , WS and V . This being said, model performances worsened for WF and WR .

53 54 55 56 57 58 59 *Bayesian model comparison*

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3 Results regarding the Bayesian model comparison are summarised in Table 2 where the log-
4 transformed integrated likelihood values are presented for the *prior BMC* and *post BMC*. The highest
5 integrated likelihood indicates the most plausible model. The percentage probability of a model of
6 being correct is obtained dividing the integrated likelihood of each model by the sum of the integrated
7 likelihoods. In the *prior BMC* the integrated likelihood showed that the 3PGN* model had a probability
8 of 84% of being the superior model. Also results from the *post BMC* supported the new model version,
9 in this case 3PGN* had a 99% probability of being the superior model.
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14 Discussion

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16 For the first time in this work we showed how the Bayesian framework proposed by van Oijen
17 et al. (2011) can be used to improve the structure of a process-based model. Furthermore the
18 framework was strengthened with a global sensitivity analysis, to better explore strengths and
19 weaknesses of the model. These techniques can be applied to any kind of model, simpler or more
20 complicated than 3PGN. However, the use of the Bayesian framework for model of higher complexity
21 can be hampered by computational limitations. In particular future works should search to increase the
22 efficiency of the Bayesian calibration to reduce the computational costs. The BC efficiency can be
23 increased reducing the number of parameters involved in the calibration by means of parameter
24 screening or using more effective MCMC algorithms such as the delayed rejection adaptive Metropolis
25 (Haario et al., 2006) and the differential evolution Markov chain (ter Braak & Vrugt, 2008).
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32 *Uncertainty and sensitivity.*

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34 Uncertainty and sensitivity analyses are fundamental processes that help to understand model
35 behavior. Even though previous works (Esprey et al. 2004; Xenakis et al., 2008) already performed
36 sensitivity analyses of 3-PG and 3PGN, using the simplest method of the One Factor At a Time (OAT)
37 screening techniques, this was the first attempt to study 3PGN sensitivity using a global method. In this
38 work the Morris sensitivity analysis was performed within the parameter space defined by the prior,
39 instead of varying the parameters values of a certain fix percentage (Esprey et al. 2004; Xenakis et al.
40 2008). The minimum and the maximum values of the prior are ranges within which the parameters are
41 meaningful. The prior represents the state of knowledge about the parameters before the calibration and
42 it contains information coming from different sources such as literature, experimental data or previous
43 Bayesian calibrations. In this way sensitivity analysis permits to focus the attention of the modelers on
44 the parameter space that is meaningful and supported by previous evidence.
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48 The sensitivity-analysis carried out at different ages helped to understand how the impact of the
49 factors on model outputs varies across the rotation. Some of the parameters are more influential on the
50 outputs at the beginning of the rotation (i.e., *fullCan Age*, *Topt*), while others, like the parameters
51 related to water stress (i.e., *minASW*, *MaxCond*, *Swconst*), had a higher impact on the outputs at the end
52 of the rotation. These results imply that having a dataset that spans across the stand development is
53 crucial to achieving a good calibration of the models. For all 3PGN* output variables, the sensitivity to
54 the wood respiration rate increased at the end of the rotation and this parameter became the most
55 influential one, because r_w is related to the biomass that increases with age. For this reason, particular
56 attention must be given to the parameterization of r_w . Furthermore, we are not considering in the
57 autotrophic respiration model the percentage of the wood that do not contribute to R_{aut} (i.e.,
58 heartwood), because *E. globulus* plantations are usually managed with a 13 year rotation and the trees
59 do not present heartwood at this stage or it is negligible. If the new version of 3PGN is applied to
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3 different species and to different Eucalyptus management, the percentage of heartwood must be taken
4 into account.
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6 The uncertainty in both parameters and model predictions was significantly reduced by the
7 calibration. The degree of parameter uncertainty varied across the parameters but was similar between
8 the two models. P_E measurements were particularly useful for model calibration because they reflected
9 the seasonal variability of stand growth and for this reason they were more informative for the
10 physiological parameters. Eddy-covariance data reduced the uncertainty of parameters related to the
11 photosynthetic activity like water stress, light use efficiency and temperature stress parameters, while
12 the biometric data (i.e., D , H , V , WF , WR , and WS) were mainly informative for parameters related to
13 the allometry and the carbon allocation routine.
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17 In the future, to reduce the uncertainty of parameters that remained less certain, modelers can
18 work on the prior of those parameters or can use, in a future calibration, output variables that are highly
19 sensitive to the uncertain parameters. Model simplification can also be considered if the parameters do
20 not affect any of the output variables of interest.
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23 The 3PGN and 3PGN* outputs characterized by the highest uncertainty a posteriori were
24 foliage and root biomasses. These were the variables with fewest measurements, so the biomass
25 datasets should be enriched correspondingly to decrease the degree of uncertainty.
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28 29 *Bayesian calibration and model-data mismatch:* 30

31 In *BC* the bottom-up and the top-down approaches can be used in combination to improve the
32 knowledge about parameters (Hartig et al., 2012). The bottom-up approach can be used in determining
33 the prior, as we did for the respiration rates (i.e., r_w and r_f) and the parameters of the allometric
34 equations. This approach allows for the integration of different data sources in the calibration process
35 and it has the merit of redressing the parameters towards realistic values. In contrast, using a top-down
36 approach, stand variables like D , H or V can be used, by means of the likelihood, to inform parameters
37 that are highly variable or difficult to measure.
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41 Bayesian calibration of the two model versions significantly reduced uncertainty in the outputs
42 and parameters. Calibration improved the probability distributions of P_E , D , H , V and WS , i.e. the
43 posterior likelihood distribution means were shifted towards higher values and the standard deviations
44 were strongly reduced (Figure 2). The analyses on *MSE* confirmed the effectiveness of the calibration,
45 with the posterior *MSE* being much lower than the prior *MSE*, for the majority of outputs. On the one
46 hand, the highest reductions in *MSE* were achieved for the data that were more certain (i.e., D , H , stand
47 volume and stem biomass) and with a high number of measurements. On the other hand, *MSE* just
48 slightly decreased for the net ecosystem productivity and increased for foliage and root biomasses.
49 Other works already demonstrated the weakness of 3-PG in predicting foliage biomass and LAI (Sands
50 & Landsberg 2002). In our case, model failure could be explained by the fact that WR and WF were the
51 data characterised by the highest uncertainty and the lowest number of measurements, therefore WF
52 and WR had smaller weight on the likelihood than the other data. *BC* results suggested that foliage and
53 root biomass dataset should be improved to better test if the models are able to reliably reproduce those
54 data, otherwise model structure should be improved.
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59 The decomposition of *MSE* provided additional useful information about model performances
60 and structure in light of the data used. The models were not able to reliably reproduce P_E
61 measurements. In fact, even if the models had really low bias and variance error, i.e. the models were
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3 able to capture the mean and the magnitude of the fluctuation among the measurements, they failed to
4 simulate the pattern of the fluctuation (phase shift error), because r was low. In other words, the models
5 are not able to reproduce the seasonal pattern of net ecosystem production. Model failure in predicting
6 P_E can be explained by systematic and/or random errors in the measurements, a problem in the model
7 structure or wrong settings of some parameter bounds in the prior. We expect the error to be mainly in
8 model structure, as 3PGN was probably too simple to respond to all environmental changes that affect
9 net ecosystem production, as shown by Minunno *et al.* (2010). Furthermore, the P_E dataset was
10 characterized by one year of intensive drought (year 2005-2006) and simple models like 3PGN and
11 3PGN* are ill designed to capture forest responses to extreme events.
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15 16 17 *Bayesian model comparison* 18

19 In ecological modelling there is a lively discussion about model complexity. Simple models are
20 not able to reproduce the intricacies of the ecological mechanisms, while complicated models are
21 theoretically closer to real processes. Nevertheless, it is difficult to calibrate parameter rich models,
22 because of lack of data or the difficulty in measuring variables related to the parameters. This is not a
23 negligible aspect as simple models with well-known parameters might perform better than complicated
24 ones. There is a need to find a compromise between model complexity and parameter uncertainty, in
25 accordance with the amount of data that are available. Therefore, model implementation should always
26 take into account these two aspects. *BMC* is such a method that allows for the evaluation of model
27 performances across their whole parameter distribution, in light of the data used. Even if this method
28 has already been applied in ecological sciences, this application to parameter rich forest process-based
29 models is still a novelty. As far as we are aware, only van Oijen *et al.* (2011) already implemented
30 *BMC* for the evaluation of four biogeochemical models in a Norway spruce forest, while this work
31 uses, for the first time, Bayesian model comparison to evaluate improvements in model structure.
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36 The Bayesian model comparison of 3PGN and 3PGN* showed that the new version of the
37 model performed better, even though it increased model complexity, adding three new parameters.
38 Although 3PGN* autotrophic respiration model is slightly more complicated than the $P_N : P_G$ ratio used
39 in 3PGN, 3PGN* parameter uncertainty is not necessarily higher. In fact, wood and foliage respiration
40 rates might be easier to measure than the $P_N : P_G$ ratio, because of the difficulty to reliably measure P_G .
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43 The marginal posterior distributions of the parameters that are common to the two models gave
44 additional information about model structure. Posterior distributions (Figure 3) are not significantly
45 different for the majority of the parameters, however the parameters that assumed significantly
46 different marginal posterior distribution between the two model versions were the parameters at which
47 the output variables are most sensitive (i.e., *alpha*, *MinASW*, *Topt*, *fullCanAge* and *FR*). Therefore, the
48 new autotrophic model produced strong changes to the 3PGN structure, because the autotrophic
49 respiration parameters, in particular Y for 3PGN and r_w for 3PGN*, have strong influence on the model
50 output variables.
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53 In conclusion, our results supported the new version of 3PGN. It should be noted, however, that
54 models are always incorrect because they are a simplification of real processes and model
55 performances cannot be discussed in an absolute manner (Oreskes et al., 1994). Thus, our analyses and
56 probabilities of correctness must be considered as indicative information towards plausible model
57 structures (van Oijen et al. 2011).
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Conclusions

In this work, different methods (i.e., *BC*, *BMC*, *MSE*-decomposition and the Morris method) were used in combination for the first time to evaluate improvements in the structure of a process-based model. Our results showed that the new version of the 3PGN model, with the new algorithm for autotrophic respiration based on maintenance and growth respiration, has a higher conditional probability of being correct. Overall, the three operations of the Bayesian framework (Bayesian calibration, Bayesian model comparison and the analysis of model-data mismatch) in combination with the Morris method, allowed us to reduce uncertainties in parameters and outputs, and identify the weaknesses of the two 3PGN versions. Furthermore, the Bayesian approach allowed to identify the weaknesses and strengths of the dataset used, making possible the improvement and optimization of future data collection.

The analyses on model-data mismatch showed that both versions of the model are able to reliably predict average stand diameter at breast height, average stand height, stand volume and stem biomass. However, the models were unable to accurately predict foliage and root biomass, probably because the dataset was small and characterized by high uncertainty. Net ecosystem production was also not well predicted, because of uncertainty in the data but also due to model structural errors.

The efficiency of the *MCMC* algorithm should be enhanced to reduce the chain length and make the process less time consuming. In our study with process-based models rich in parameters, good convergence of all parameters is reached when the potential scale reduction (\hat{R}) assumes values close to 1.03.

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Table 1a. Symbols, units, minimum and maximum values and prior distributions for the 3PGN and 3PGN* parameters calibrated for *Eucalyptus globulus* in Portugal.

Parameter description	Symbols	Units	Min	Max	Prior distr.
Constant in the aboveground biomass vs. height relationship	<i>aH</i>	—	1.9	2.8	Normal*
Canopy quantum efficiency	<i>alpha</i>	mol C * MJ ⁻¹	0.04	0.08	Normal
Canopy boundary layer conductance	<i>BLcond</i>	m*s ⁻¹	0.16	0.24	Uniform
Power in the aboveground biomass vs. height relationship	<i>bW</i>	—	0	0.3	Weibull*
Defines stomatal response to VPD	<i>CoeffCond</i>	Mbar ⁻¹	0.04	0.06	Uniform
Basic density	<i>Density</i>	Mg*m ³	0.36	0.54	Normal
Conversion of fresh biomass to dry biomass	<i>dmC</i>	—	0.45	0.55	Normal
Value of fNutr when FR = 0	<i>fN0</i>	—	0	0.5	Uniform
Branch and bark fraction at age 0	<i>fracBB0</i>	—	0.6	0.9	Normal
Branch and bark fraction for mature stands	<i>fracBB1</i>	—	0.12	0.18	Normal
Age at canopy cover	<i>fullCanAge</i>	years	2	5	Normal
Litterfall rate at t = 0	<i>gammaF0</i>	month ⁻¹	0.0008	0.0012	Normal
Maximum litterfall rate	<i>gammaFx</i>	month ⁻¹	0.0216	0.0324	Normal
Humification coefficient	<i>hc</i>	—	0.1	0.15	Uniform
Extinction coefficient for absorption of PAR by canopy	<i>k</i>	—	0.4	0.6	Normal
Days of production lost per frost day	<i>kF</i>	days	0	3	Normal
Decomposition rate constant for the “young and labile” pool per month	<i>klmax</i>	month ⁻¹	0.006	0.01	Uniform
Decomposition rate constant for the “old” pool	<i>komax</i>	month ⁻¹	0.0004	0.0006	Uniform
Decomposition rate constant for the “young and refractory” pool per month	<i>krmax</i>	month ⁻¹	0.03	0.05	Uniform
LAI for maximum canopy conductance	<i>LAIgcx</i>	—	2.664	3.996	Uniform
LAI for maximum rainfall interception	<i>LAImaxIntcptn</i>	—	0	0.05	Uniform
Value of m when FR = 0	<i>m0</i>	—	0	0.2	Uniform
Maximum stand age used in age modifier	<i>MaxAge</i>	years	80	200	Uniform
Maximum canopy conductance	<i>MaxCond</i>	m*s ⁻¹	0.016	0.024	Uniform
Maximum proportion of rainfall evaporated from canopy	<i>MaxIntcptn</i>	—	0.12	0.18	Uniform
Power of relative age in function for fAge	<i>nAge</i>	—	2	5	Uniform
Foliage–stem partitioning ratio @ D = 2 cm	<i>pFS2</i>	—	0.8	1.2	Uniform
Foliage–stem partitioning ratio @ D = 20 cm	<i>pFS20</i>	—	0.12	0.18	Uniform
Maximum fraction of NPP to roots	<i>pRn</i>	—	0.2	0.3	Uniform
Minimum fraction of NPP to roots	<i>pRx</i>	—	0.64	0.96	Uniform
Q10	<i>Q10**</i>	—	1	3.5	Normal
Relative age to give fAge = 0.5	<i>rAge</i>	—	0.76	1	Uniform
Foliage biomass respiration rate	<i>rf**</i>		0.0005	0.02	Gamma
Growth respiration rate	<i>rg**</i>		0.2	0.3	Normal
Average monthly root turnover rate	<i>Rttover</i>	month ⁻¹	0.012	0.018	Gamma

Table 1a. (Concluded)

Parameter description	Symbols	Units	Min	Max	Prior distr.
Woody biomass respiration rate	rw^{**}		0.001	0.06	Gamma
Woody biomass respiration rate	rw^{**}		0.001	0.06	Gamma
Specific leaf area at age 0	$SLA0$	m^2*kg^{-1}	10.5	14	normal*
Specific leaf area for mature leaves	$SLA1$	m^2*kg^{-1}	3.7	4.4	normal*
Constant in the aboveground biomass vs. diameter relationship	$StemConst$	—	1.15	1.4	gamma*
Power in the aboveground biomass vs. diameter relationship	$StemPower$	—	0.5	0.55	gamma*
Moisture ratio deficit for $f_q = 0.5$	$SWconst$	—	0.63	0.77	normal
Power of moisture ratio deficit	$SWpower$	—	8.1	9.9	normal
Age at which $fracBB = (fracBB0 + fracBB1)/2$	tBB	years	1.6	2.4	normal
Age at which litterfall rate has median value	$tgammaF$	years	9.6	14.4	normal
Maximum temperature for growth	$Tmax$	°C	32	48	normal
Minimum temperature for growth	$Tmin$	°C	6.8	10.2	normal
Optimum temperature for growth	$Topt$	°C	12.8	19.2	normal
Age at which specific leaf area = $(SLA0 + SLA1)/2$	$tSLA$	years	1.2	2	normal*
Ratio NPP/GPP	Y^{***}	—	0.376	0.564	normal

* distributions fitted over posterior distributions

** only 3PGN* parameters

*** only 3PGN parameters

Table 1b. Symbols, units, minimum and maximum values and prior distributions for the 3PGN site variables used in this work.

Site variable description	Symbols	Units	min	max	prior distr.
Fertility rating for the Espirra site	<i>FR_espirra</i>	—	0.4	0.7	normal
Fertility rating for the ferc site	<i>FR_ferc</i>	—	0.4	0.7	normal
Fertility rating for the ferf site	<i>FR_ferf</i>	—	0.6	1	normal
Fertility rating for the feri site	<i>FR_feri</i>	—	0.4	0.7	normal
Fertility rating for the ferif site	<i>FR_ferif</i>	—	0.6	1	normal
Maximum available soil water for the Espirra forest	<i>MaxASW_espirra</i>	mm*ha ⁻¹	120	180	uniform
Maximum available soil water for the Furadouro experiment	<i>MaxASW_fer</i>	mm*ha ⁻¹	120	180	normal
Minimum available soil water for the Espirra forest	<i>MinASW_espirra</i>	mm*ha ⁻¹	0	60	uniform
Minimum available soil water for the Furadouro experiment	<i>MinASW_fer</i>	mm*ha ⁻¹	0	40	normal
Initial carbon in the old pool	<i>O_C_i</i>	kg*ha ⁻¹	30	50	normal
Tree density at the Espirra site	<i>StemNo_espirra</i>	trees*ha ⁻¹	1650	1750	normal
Tree density at the ferc site	<i>StemNo_ferc</i>	trees*ha ⁻¹	1060	1120	normal
Tree density at the ferf site	<i>StemNo_ferf</i>	trees*ha ⁻¹	1060	1120	normal
Tree density at the feri site	<i>StemNo_feri</i>	trees*ha ⁻¹	1060	1120	normal
Tree density at the ferif site	<i>StemNo_ferif</i>	trees*ha ⁻¹	1060	1120	normal
Initial foliage biomass	<i>WF_i</i>	kg*ha ⁻¹	0.01	0.2	uniform
Initial root biomass	<i>WR_i</i>	kg*ha ⁻¹	0.001	0.1	uniform
Initial stem and branches biomass	<i>WS_i</i>	kg*ha ⁻¹	0.001	0.05	uniform
Initial carbon in the young labile pool	<i>Yl_C_i</i>	kg*ha ⁻¹	8	12	normal
Initial carbon in the young refractory pool	<i>Yr_C_i</i>	kg*ha ⁻¹	0	10	uniform

Table 2. Results of the Bayesian model comparison of 3PGN and 3PGN*. The table shows the log-transformed integrated likelihood values for the *prior BMC* and *post BMC*.

	3PGN	3PGN*
<i>prior BMC</i>	-640.6	-638.94
<i>post BMC</i>	-71.58	-65.71

Table 3. Comparison of data with model outputs: squared correlation coefficient (r^2) and normalized root mean square error (NRMSE). The table shows the distribution means of statistics induced by prior and posterior parameter distributions. In bold: posterior values that are improvements over the prior (r increased, NRMSE reduced).

Var.	Statistic	3PGN		3PGN*	
		Prior	Post.	Prior	Post.
P_E	r^2	0.11	0.25	0.15	0.26
	<i>slope</i>	0.27	0.47	0.33	0.52
	<i>NRMSE</i>	118.4	101.8	121.3	109.3
D	r^2	0.89	0.98	0.91	0.98
	<i>Slope</i>	1.51	0.88	1.24	0.9
	<i>NRMSE</i>	124.7	20.4	91.6	14.8
H	r^2	0.96	0.93	0.92	0.93
	<i>slope</i>	1.65	1.25	1.38	1.29
	<i>NRMSE</i>	78.9	33.2	44.7	31.2
WF	r^2	0.92	0.71	0.83	0.68
	<i>slope</i>	1.36	0.89	1.03	0.88
	<i>NRMSE</i>	52	55.4	33.1	57.2
WR	r^2	0.99	0.95	0.96	0.93
	<i>slope</i>	1.5	0.83	1.06	0.94
	<i>NRMSE</i>	28	38.4	17.3	31.3
WS	r^2	0.94	0.97	0.91	0.96
	<i>slope</i>	3.53	1.09	2.15	1.15
	<i>NRMSE</i>	86.2	19.5	63.4	21.5
V	r^2	0.94	0.98	0.95	0.98
	<i>slope</i>	3.74	1.06	2.14	1.1
	<i>NRMSE</i>	89.3	14	63.9	17.1

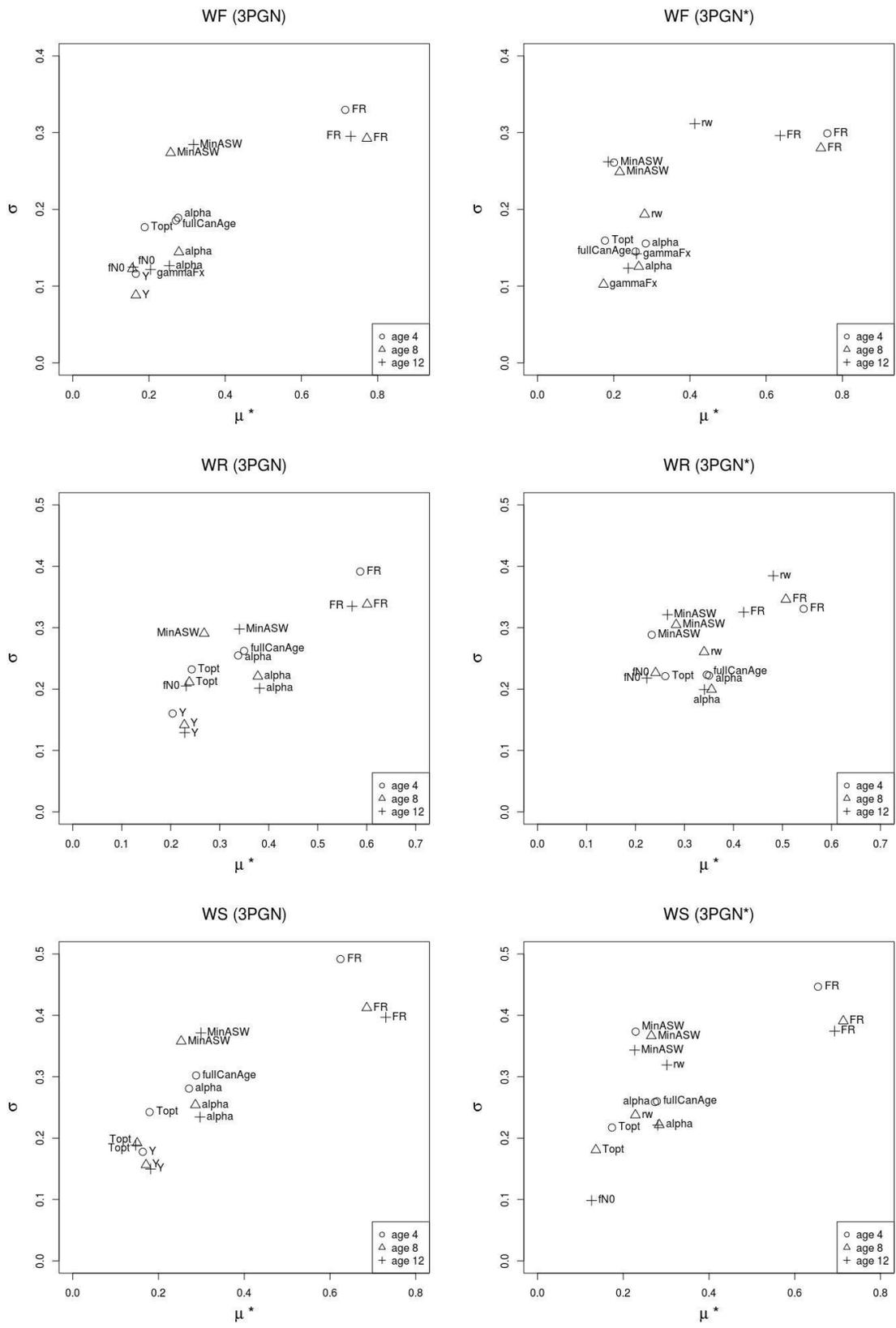


Figure 1a. Plots of σ vs. μ^* of the five highest sensitive parameters for foliage (WF), root (WR) and stem (WS) biomasses for 3PGN and 3PGN* outputs at age 4 (circles), 8 (triangles) and 12 (cruces).

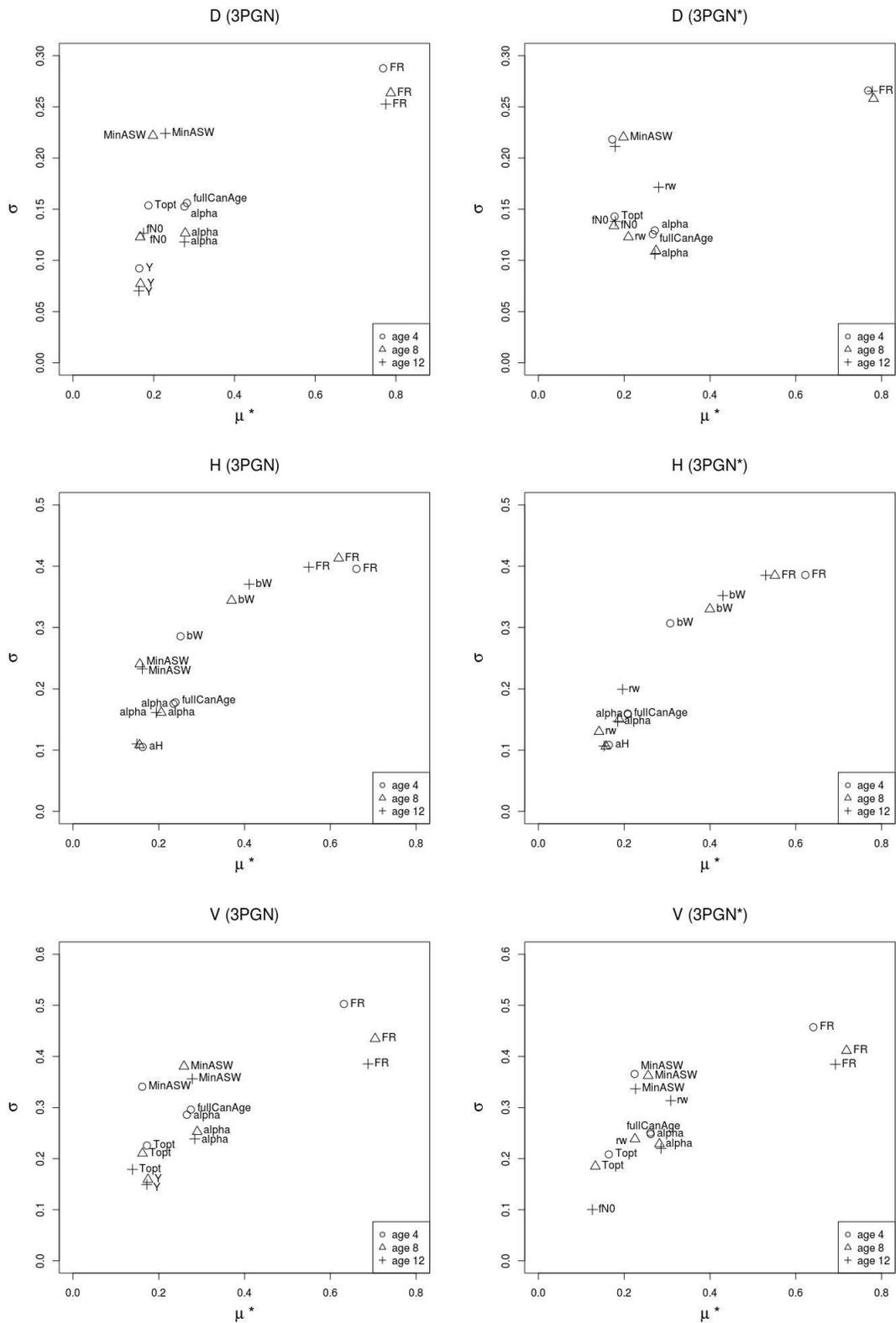


Figure 1b. Plots of σ vs. μ^* of the five highest sensitive parameters for diameter at breast height (D), average stand height (H) and stand volume (V) for 3PGN and 3PGN* outputs at age 4 (circles), 8 (triangles) and 12 (crosses).

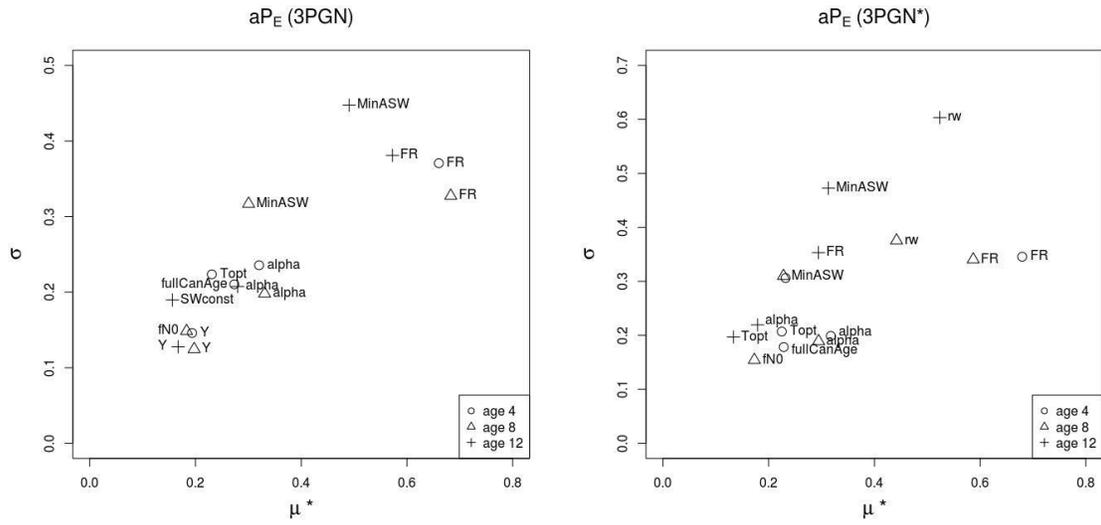


Figure 1c. Plots of σ vs. μ^* of the five highest sensitive parameters for the annual net ecosystem production (aP_E) for 3PGN and 3PGN* outputs at age 4 (circles), 8 (triangles) and 12 (cruces).

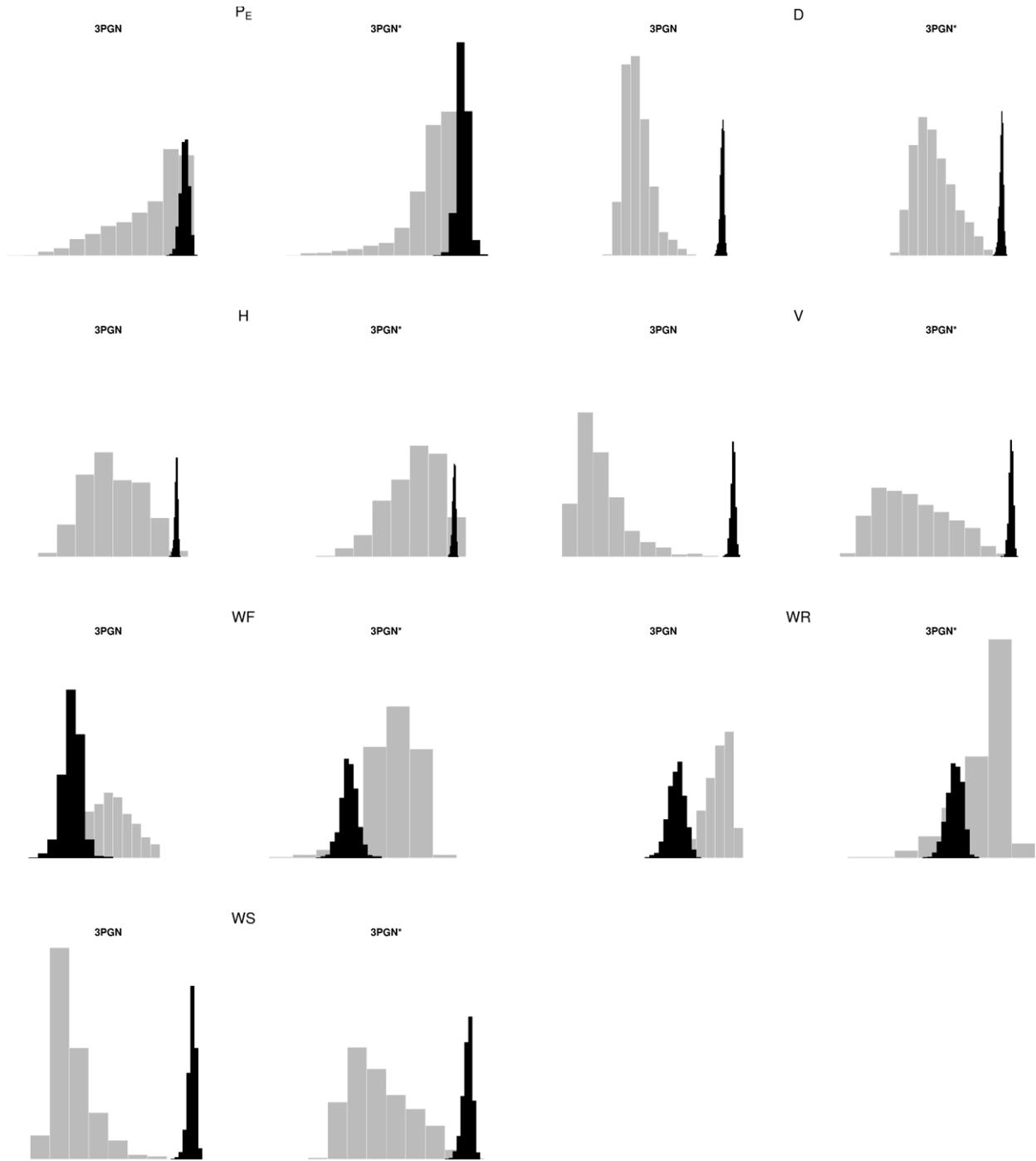


Figure 2. Prior (grey histograms) and posterior (black histograms) distributions of log-likelihoods for the two model versions, for the seven categories of output variables.

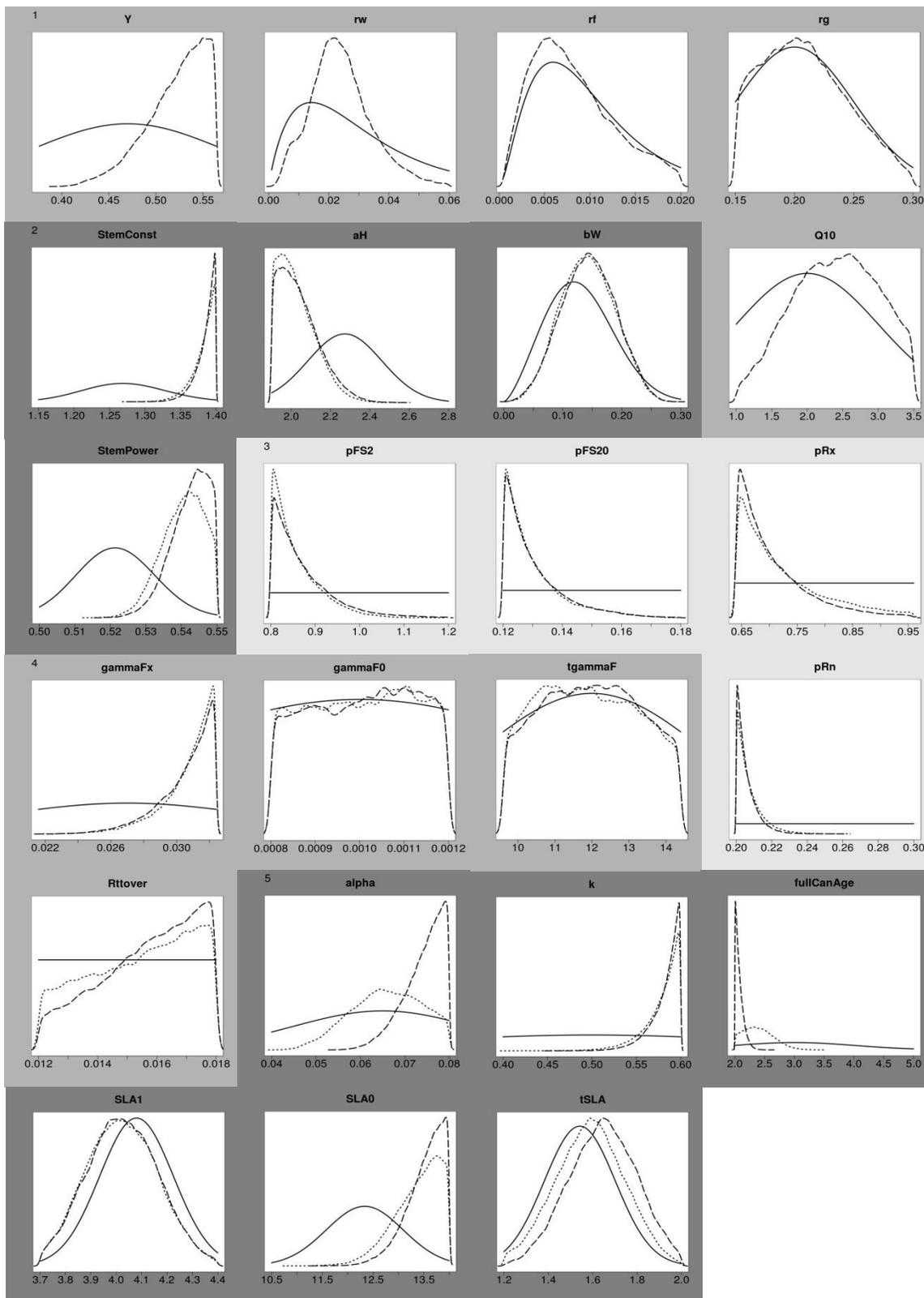


Figure 3a. Marginal prior distributions (continuous line) and marginal posterior distributions of 3PGN (dashed line) and 3PGN* (dotted line). Parameters are grouped as respiration parameters (group 1), allometric parameters (group 2), allocation parameters (group 3), turnover parameters (group 4), light use efficiency and light interception parameters (group 5).

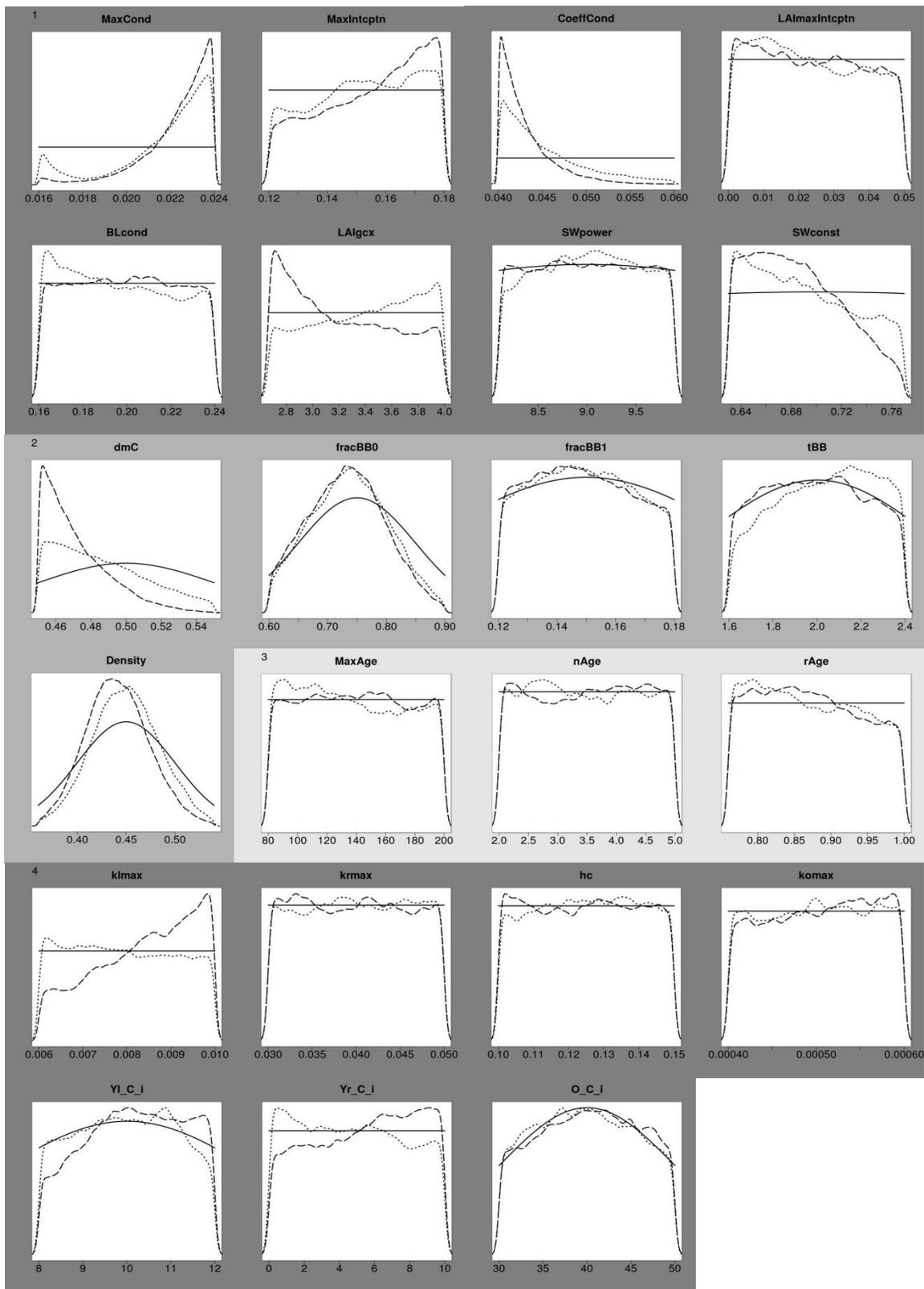


Figure 3b. Marginal prior distributions (continuous line) and marginal posterior distributions of 3PGN (dashed line) and 3PGN* (dotted line). Parameters are grouped as water stress parameters (group 1), volume and density parameters (group 2), age stress parameters (group 3) and soil parameters (group 4).

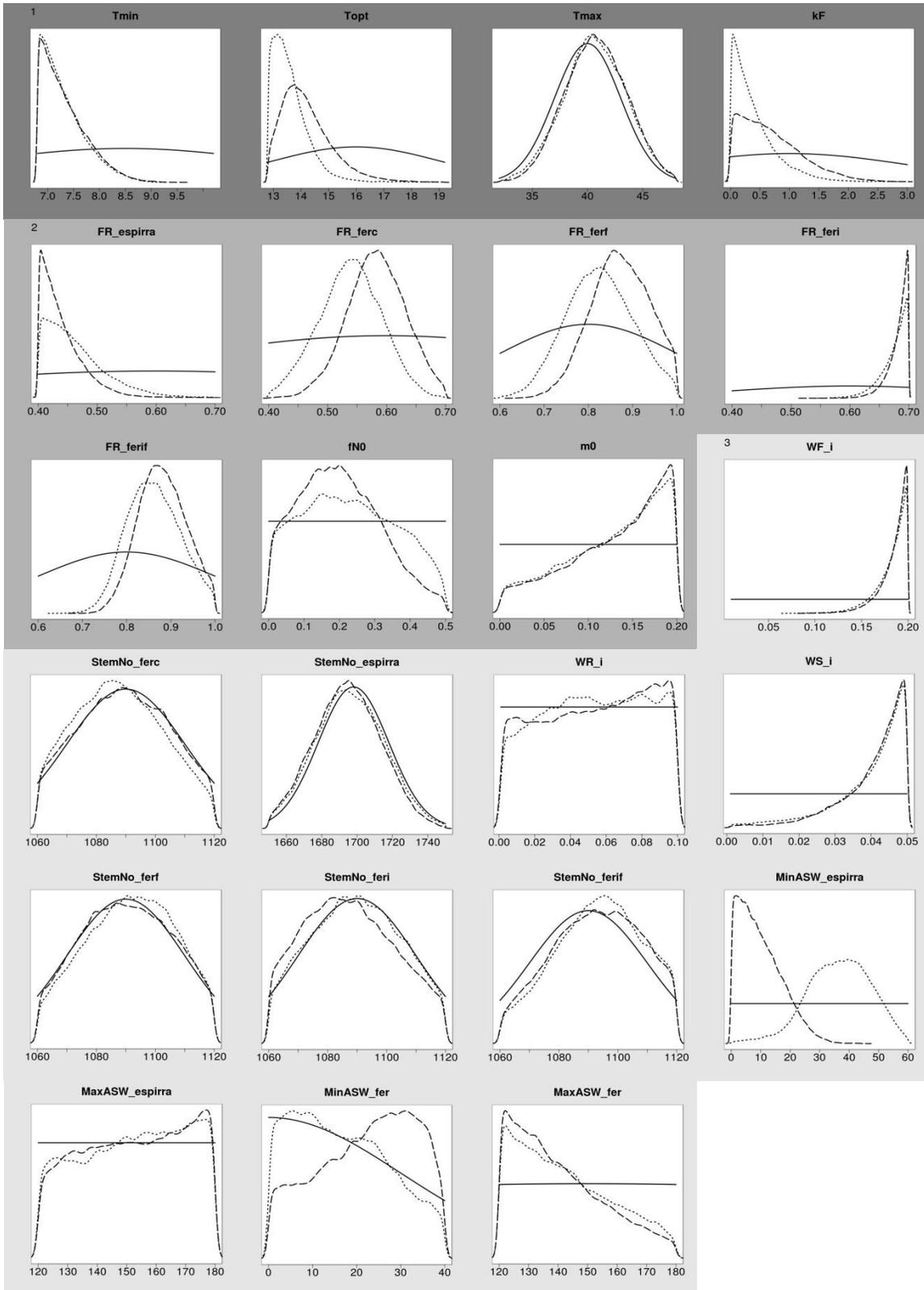


Figure 3c. Marginal prior distributions (continuous line) and marginal posterior distributions of 3PGN (dashed line) and 3PGN* (dotted line). Parameters are grouped as temperature and frost stress parameters (group 1), fertility parameters (group 2), site parameters (group 3).

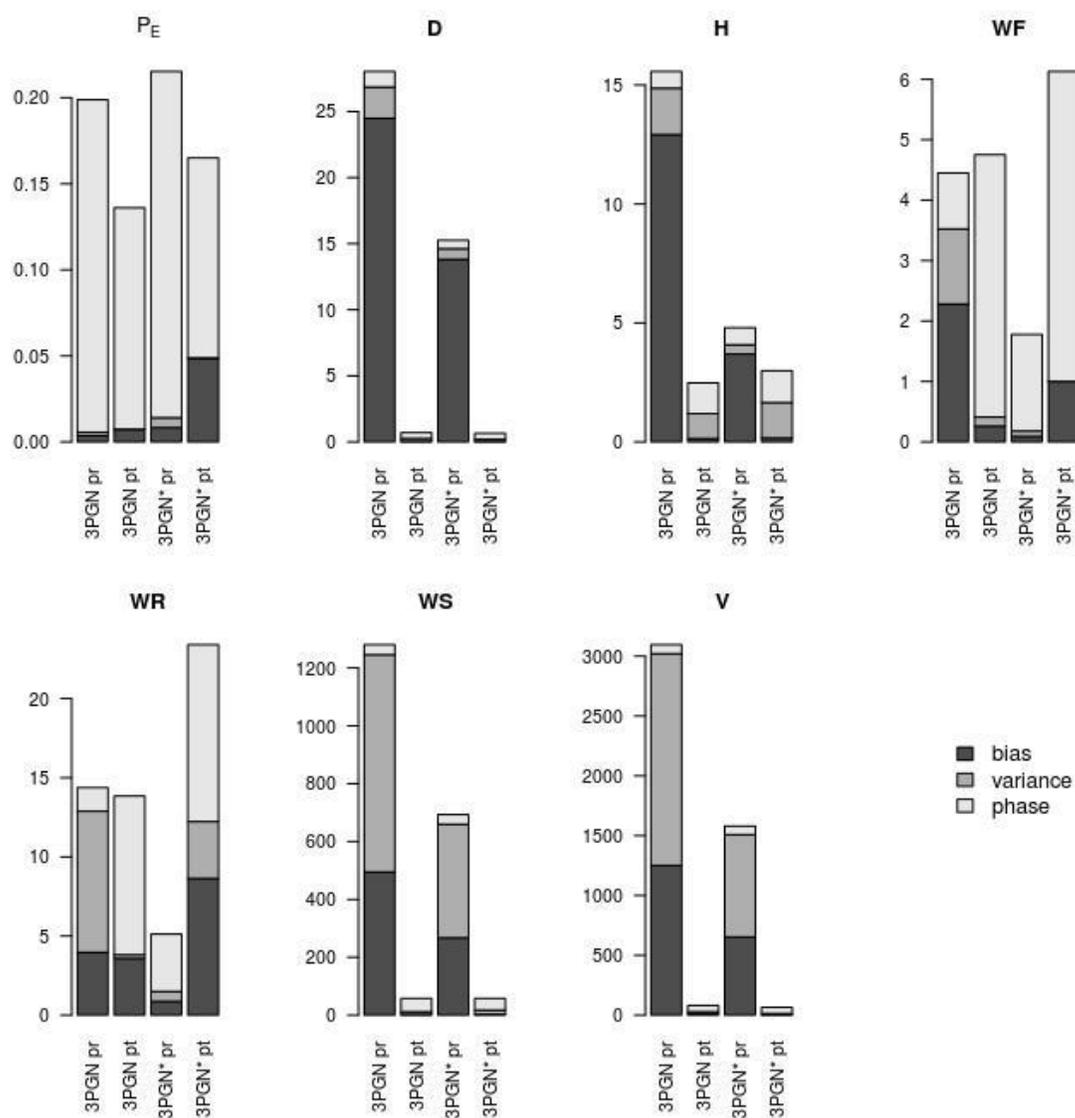


Figure 4. Decomposition of the mean squared error associated with the modes of the prior (pr) and posterior (pt) parameter distributions, for 3PGN and 3PGN*. In squared brackets are reported the number of data for each variable.