International Geomagnetic Reference Field:

² The Eleventh Generation

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SUMMARY 5

The eleventh generation of the International Geomagnetic Reference Field (IGRF) was 6 adopted in December 2009 by the International Association of Geomagnetism and Aeron-7 omy (IAGA) Working Group V-MOD. It updates the previous IGRF generation with a 8 definitive main field model DGRF 2005.0, for 2005.0, a main field model IGRF 2010.0, 9 for 2010.0, and a linear predictive secular variation model for 2010.0-2015.0. In this note 10 the equations defining the IGRF model are provided together with the spherical harmonic 11 coefficients for the eleventh generation. Maps of the magnetic Declination, Inclination 12 and Total Intensity for epoch 2010.0 and their predicted rate of change for 2010.0 - 2015.0 13 are presented and the recent evolution of the South Atlantic Anomaly and magnetic pole 14 positions are examined. 15

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Key words: Geomagnetism – Main Field – Secular Variation – Reference Field – IGRF

INTRODUCTION 1 17

The International Geomagnetic Reference Field (IGRF) is an established numerical model used to 18 calculate the large scale, internal, part of the Earth's magnetic field at times between 1900.0 A.D. 19 and present, at locations on or above Earth's surface. It is produced and maintained by a team of 20 geomagnetic field modellers under the auspices of the International Association of Geomagnetism and 21 Aeronomy (IAGA) Working Group V-MOD and is derived from observations collected by satellites, at 22 magnetic observatories, and during magnetic surveys. It is used by scientists (for example in studies of 23 space weather or in investigations of local magnetic anomalies) and also by commercial organizations 24 and private individuals who often use the geomagnetic field as a source of orientation information. 25

The internal part of the geomagnetic field, which is almost entirely core-generated, undergoes 26 slow, but noticeable, changes over years to decades. Consequently the IGRF must be revised, typically 27 every five years, in order to remain up to date and as accurate as possible; Table 1 summarizes details 28 of previous generations of the IGRF. Each generation of the IGRF consists of a series of constituent 29 models at five-year intervals, each one of which is designated definitive or non-definitive. Once a con-30 stituent model is designated definitive it is called a Definitive Geomagnetic Reference Field (DGRF) 31 and it is not revised in subsequent generations of the IGRF. The non-definitive constituent models 32 are referred to as IGRFs. Note that DGRFs have been produced only for epochs from 1945.0 on-33 wards. For further details concerning the history of the IGRF readers should consult Barton (1997), 34

Full name	Short name	Valid for	Definitive for	Reference
IGRF 11th generation	IGRF-11	1900.0-2015.0	1945.0-2005.0	Finlay et al. (2010) - this article
IGRF 10th generation	IGRF-10	1900.0-2010.0	1945.0-2000.0	Maus et al. (2005a)
IGRF 9th generation	IGRF-9	1900.0-2005.0	1945.0-2000.0	Macmillan et al. (2003)
IGRF 8th generation	IGRF-8	1900.0-2005.0	1945.0-1990.0	Mandea & Macmillan (2000)
IGRF 7th generation	IGRF-7	1900.0-2000.0	1945.0-1990.0	Barton (1997)
IGRF 6th generation	IGRF-6	1945.0-1995.0	1945.0-1985.0	Langel (1992)
IGRF 5th generation	IGRF-5	1945.0-1990.0	1945.0-1980.0	Langel et al. (1988)
IGRF 4th generation	IGRF-4	1945.0-1990.0	1965.0-1980.0	Barraclough (1987)
IGRF 3rd generation	IGRF-3	1965.0-1985.0	1965.0-1975.0	Peddie (1982)
IGRF 2nd generation	IGRF-2	1955.0-1980.0	_	IAGA (1975)
IGRF 1st generation	IGRF-1	1955.0-1975.0	_	Zmuda (1971)

Table 1. Summary of IGRF generations, their intervals of validity and related references.

Maus et al. (2005a) or Macmillan & Finlay (2010); here attention will focus on the latest (11th gen-

eration) revision. Legacy versions of the IGRF are now available from the online archive located at

³⁷ http://www.ngdc.noaa.gov/IAGA/vmod/igrf_old_models.html. These may be useful, for ex-

³⁸ ample, to workers who know that a previous generation IGRF had been subtracted from their data and

³⁹ who wish to recover the original data or re-correct it with a more recent IGRF revision.

The 11th generation of the IGRF (hereafter IGRF-11) was agreed in December 2009 by a task

⁴¹ force of IAGA Working Group V-MOD. The purpose of this note is to document the release of IGRF⁴² 11, to act as a permanent published record of model coefficients, and to briefly describe the large scale

features of the present geomagnetic field at Earth's surface as revealed by the updated model.

44 2 MATHEMATICAL FORMULATION OF THE IGRF MODEL

On and above the Earth's surface. the IGRF model represents the geomagnetic field $\mathbf{B}(r, \theta, \phi, t)$ produced by internal sources in terms of a scalar potential $V(r, \theta, \phi, t)$. We then have $\mathbf{B} = -\nabla V$ where V is a finite series having the numerical Gauss coefficients g_n^m , h_n^m (conventionally given in units of nanotesla, hereafter nT):

$${}_{49} \quad V(r,\theta,\phi,t) = a \sum_{n=1}^{N} \sum_{m=0}^{n} \left(\frac{a}{r}\right)^{n+1} \left[g_n^m(t)\cos m\phi + h_n^m(t)\sin m\phi\right] P_n^m(\cos\theta). \tag{1}$$

Here r denotes the radial distance from the centre of the Earth in units of km, a = 6371.2 km is the magnetic reference spherical radius which is close to the mean Earth radius, θ denotes geocentric ⁵² co-latitude (i.e. 90° - latitude), and ϕ denotes east longitude. When converting between geocentric and ⁵³ geodetic co-ordinates, it is recommended to use the World Geodetic System 1984 datum and spheroid ⁵⁴ (major axis A of 6378.137 km and a reciprocal flattening 1/f of 298.257223563). $P_n^m(\cos \theta)$ are the ⁵⁵ Schmidt semi- (or quasi-) normalized associated Legendre functions of degree n and order m (see, for

example, Winch et al., 2005). The maximum spherical harmonic degree of the expansion is N.

In the IGRF model, Gauss coefficients g_n^m and h_n^m are provided for the main field (MF) at epochs separated by 5 year intervals between 1900.0 and 2010.0 A.D. The time-dependence of the Gauss coefficients is then specified using the following linear expression,

$$g_n^m(t) = g_n^m(T_0) + g_n^m(T_0) \cdot (t - T_0), \tag{2}$$

and similarly for h_n^m . Here t is the time of interest (in units of years) and T_0 is the epoch preceeding twhich is an exact multiple of 5 years, such that $T_0 \le t < (T_0 + 5.0)$. The coefficients $g_n^{in}(T_0)$, given in units of nT/yr, denote the average first time derivative of $g_n^m(t)$ during the interval T_0 to $T_0 + 5.0$, i.e. the linear secular variation (SV) during this interval. When MF models exist for both T_0 and $T_0 + 5.0$ then $g_n^{in}(T_0)$ is simply calculated using linear interpolation as $[g_n^m(T_0 + 5.0) - g_n^m(T_0)]/5.0$. For the final 5 years of the model validity (between 2010.0 and 2015.0 for IGRF-11) coefficients of predictive average SV $g_n^{in}(t)$ and $h_n^{in}(t)$ are explicitly provided.

The geocentric components of the geomagnetic field in the northward, eastward and radially inwards directions (X', Y' and Z') are obtained from the model coefficients using equation (1) and by taking appropriate components of the gradient of V in spherical polar co-ordinates,

$$_{71}$$
 $X' = \frac{1}{r} \frac{\partial V}{\partial \theta}, \quad Y' = -\frac{1}{r \sin \theta} \frac{\partial V}{\partial \phi}, \quad Z' = \frac{\partial V}{\partial r}.$ (3)

It is often necessary to work in geodetic co-ordinates and to use the World Geodetic System 1984 datum defined above. Transformations from geocentric to geodetic coordinates and from the geocentric field components (X', Y', Z') into the geodetic field components (X, Y, Z) are described by eqns 1 - 4 of Hulot et al. (2007). Often the Declination *D*, Inclination *I*, the horizontal intensity *H* and the total intensity *F* are required for applications; these are obtained from *X*, *Y* and *Z* using the relations,

⁷⁸
$$H = \sqrt{X^2 + Y^2}, \quad F = \sqrt{X^2 + Y^2 + Z^2}, \quad D = \arctan(Y/X), \quad I = \arctan(Z/H).$$
 (4)

The computation of field components from the model coefficients can be performed using the software
available at http://www.ngdc.noaa.gov/IAGA/vmod/igrf.html or using the online calculators
listed in section 5.

82 **3** THE 11TH GENERATION IGRF

In May 2009 the IGRF-11 task force (as appointed by IAGA Division V-MOD) issued a call for can-83 didate models. Candidates for the Definitive Geomagnetic Reference Field (DGRF) for epoch 2005, 84 for a provisional IGRF model for epoch 2010, and for a predictive SV model for the interval 2010-85 2015 were requested. Candidates were received in early October 2009. Seven candidates were sub-86 mitted for the DGRF epoch 2005.0 and IGRF epoch 2010.0 MF models. Team A was led by DTU 87 Space, Denmark along with workers from IPGP, France and GSFC-NASA, U.S.A.; Team B was led 88 by NGDC/NOAA, U.S.A. together with colleagues from GFZ, Germany; Team C was from BGS, 89 U.K.; Team D was from IZMIRAN, Russia; Team E was led by EOST, France with assistance from 90 colleagues at LPGN, IPGP and LATMOS, France; Team F was led by IPGP, France with input from 91 workers in NGDC/NOAA, U.SA. and LPGN, EOST and LATMOS, France; Team G was from GFZ, 92 Germany. The same teams also contributed candidate SV models and there was one additional SV 93 candidate from a team led by GSFC-NASA, U.S.A. in collaboration with UMBC, U.S.A. and Univ. 94 Liverpool, U.K.; in all, eight SV candidates were received. 95

The MF candidate models had a maximum spherical harmonic degree N = 13, while the task force voted to retain a maximum degree of N = 8 for the predictive SV models. The candidate models together with brief descriptions provided by the authors may be obtained from the web page http://www.ngdc.noaa.gov/IAGA/vmod/candidatemodels.html. Papers providing fuller details on the candidate models and describing the evaluations carried out by the task force (similar to the analysis of the candidates contributing to IGRF-10 carried out by Maus et al., 2005b) will appear in a forthcoming special issue of Earth, Planets and Space.

The final IGRF-11 MF models for epochs 2005.0 and 2010.0 as well as the predictive SV model for 2010.0-2015.0 were calculated using weighted means of the candidates. The weights were agreed by a vote of the IGRF-11 task force based on information gleaned from various evaluations, fuller details of which are given in Finlay et al. (2010).

High quality, globally distributed, observations of the geomagnetic field are essential to the production of an accurate IGRF revision. The collection of the required comprehensive set of observations
involves a significant international collaborative effort. The availability of satellite measurements,
from the CHAMP (Reigber et al., 2002), Ørsted (Neubert et al., 2001) and SAC-C missions, and
observatory measurements (see Table 4 in the Appendix) was of fundamental importance to IGRF-11.

IGRF-11 remains unchanged from IGRF-10 for epoch 2000 and earlier. The model MF coefficients are rounded to 1 nT for epochs between 1900.0 and 1995.0; to 0.1 nT for epochs 2000.0 and 2010.0, and to 0.01 nT for DGRF 2005.0 reflecting the increasing consistency of the candidate models (Finlay et al., 2010). The predictive SV coefficients are rounded to the nearest 0.1 nT/yr. Note that

although the formal root mean square (rms) error in DGRF 2005.0, based on the internal consistency 116 of the contributing candidates, was only 1.0 nT, the true error (due to errors of commission rather 117 than unmodelled sources in the Earth's crust and magnetosphere) is probably closer to 5 nT. The error 118 in IGRF-2010 is expected to be slightly larger (approximately10 nT) because extrapolation of mod-119 els from submission in October 2009 forward to 2010 was necessary (Lowes, 2000). Regarding the 120 predictive SV model, retrospective analysis of previous predictions has shown that errors of up to 20 121 nT/yr are likely (Maus et al., 2005b; Finlay et al., 2010). For further details on the limitations of the 122 IGRF and difficulties in estimating its accuracy readers should consult the IGRF health warning found 123 at http://www.ngdc.noaa.gov/IAGA/vmod/igrfhw.html. 124

125 4 IGRF-11 MODEL COEFFICIENTS AND MAPS

In Table 2 the Schmidt semi-normalized spherical harmonic coefficients comprising IGRF-11 are reproduced. Units are nT for the MF models and nT/yr for the predictive SV model. The coefficients are also available in various file formats at http://www.ngdc.noaa.gov/IAGA/vmod/igrf.html, together with software to compute the various components of the magnetic field values. IGRF-11 is also available from the world data centres listed at the end of this paper.

Table 2: 11th Generation International Geomagnetic Reference Field. Here Schmidt semi-normalized spherical harmonic coefficients are provided. Coefficients for degrees n=1,13 in units nanotesla are listed for IGRF and definitive DGRF main-field models. Coefficients for degrees n=1,8 in units of nanotesla/year are listed for the predictive secular variation. Undefined coefficients are marked with '-'; these should be set to

0.0 in numerical calculations as is the case in the coefficient files available online.

	Degree	Order	IGRF	IGRF	IGRF	IGRF	IGRF	IGRF	IGRF	IGRF	IGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	IGRF	sv
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
g	1	0	-31543	-31464	-31354	-31212	-31060	-30926	-30805	-30715	-30654	-30594	-30554	-30500	-30421	-30334	-30220	-30100	-29992	-29873	-29775	-29692	-29619.4	-29554.63	-29496.5	11.4
g	1	1	-2298	-2298	-2297	-2306	-2317	-2318	-2316	-2306	-2292	-2285	-2250	-2215	-2169	-2119	-2068	-2013	-1956	-1905	-1848	-1784	-1728.2	-1669.05	-1585.9	16.7
h	1	1	5922	5909	5898	5875	5845	5817	5808	5812	5821	5810	5815	5820	5791	5776	5737	5675	5604	5500	5406	5306	5186.1	5077.99	4945.1	-28.8
g	2	0	-677	-728	-769	-802	-839	-893	-951	-1018	-1106	-1244	-1341	-1440	-1555	-1662	-1781	-1902	-1997	-2072	-2131	-2200	-2267.7	-2337.24	-2396.6	-11.3
g	2	1	2905	2928	2948	2956	2959	2969	2980	2984	2981	2990	2998	3003	3002	2997	3000	3010	3027	3044	3059	3070	3068.4	3047.69	3026.0	-3.9
h	2	1	-1061	-1086	-1128	-1191	-1259	-1334	-1424	-1520	-1614	-1702	-1810	-1898	-1967	-2016	-2047	-2067	-2129	-2197	-2279	-2366	-2481.6	-2594.50	-2707.7	-23.0
g	2	2	924	1041	1176	1309	1407	1471	1517	1550	1566	1578	1576	1581	1590	1594	1611	1632	1663	1687	1686	1681	1670.9	1657.76	1668.6	2.7
h	2	2	1121	1065	1000	917	823	728	644	586	528	477	381	291	206	114	25	-68	-200	-306	-373	-413	-458.0	-515.43	-575.4	-12.9
g	3	0	1022	1037	1058	1084	1111	1140	1172	1206	1240	1282	1297	1302	1302	1297	1287	1276	1281	1296	1314	1335	1339.6	1336.30	1339.7	1.3
g	3	1	-1469	-1494	-1524	-1559	-1600	-1645	-1692	-1740	-1790	-1834	-1889	-1944	-1992	-2038	-2091	-2144	-2180	-2208	-2239	-2267	-2288.0	-2305.83	-2326.3	-3.9
h	3	1	-330	-357	-389	-421	-445	-462	-480	-494	-499	-499	-476	-462	-414	-404	-366	-333	-336	-310	-284	-262	-227.6	-198.86	-160.5	8.6
g	3	2	1256	1239	1223	1212	1205	1202	1205	1215	1232	1255	1274	1288	1289	1292	1278	1260	1251	1247	1248	1249	1252.1	1246.39	1231.7	-2.9
h	3	2	3	34	62	84	103	119	133	146	163	186	206	216	224	240	251	262	271	284	293	302	293.4	269.72	251.7	-2.9
g	3	3	572	635	705	778	839	881	907	918	916	913	896	882	878	856	838	830	833	829	802	759	714.5	672.51	634.2	-8.1
h	3	3	523	480	425	360	293	229	166	101	43	-11	-46	-83	-130	-165	-196	-223	-252	-297	-352	-427	-491.1	-524.72	-536.8	-2.1
g	4	0	876	880	884	887	889	891	896	903	914	944	954	958	957	957	952	946	938	936	939	940	932.3	920.55	912.6	-1.4
g	4	1	628	643	660	678	695	711	727	744	762	776	792	796	800	804	800	791	782	780	780	780	786.8	797.96	809.0	2.0
h	4	1	195	203	211	218	220	216	205	188	169	144	136	133	135	148	167	191	212	232	247	262	272.6	282.07	286.4	0.4
g	4	2	660	653	644	631	616	601	584	565	550	544	528	510	504	479	461	438	398	361	325	290	250.0	210.65	166.6	-8.9
h	4	2	-69	-77	-90	-109	-134	-163	-195	-226	-252	-276	-278	-274	-278	-269	-266	-265	-257	-249	-240	-236	-231.9	-225.23	-211.2	3.2
g	4	3	-361	-380	-400	-416	-424	-426	-422	-415	-405	-421	-408	-397	-394	-390	-395	-405	-419	-424	-423	-418	-403.0	-379.86	-357.1	4.4
h	4	3	-210	-201	-189	-173	-153	-130	-109	-90	-72	-55	-37	-23	3	13	26	39	53	69	84	97	119.8	145.15	164.4	3.6
g	4	4	134	146	160	178	199	217	234	249	265	304	303	290	269	252	234	216	199	170	141	122	111.3	100.00	89.7	-2.3
h	4	4	-75	-65	-55	-51	-57	-70	-90	-114	-141	-178	-210	-230	-255	-269	-279	-288	-297	-297	-299	-306	-303.8	-305.36	-309.2	-0.8
g	5	0	-184	-192	-201	-211	-221	-230	-237	-241	-241	-253	-240	-229	-222	-219	-216	-218	-218	-214	-214	-214	-218.8	-227.00	-231.1	-0.5
g	5	1	328	328	327	327	326	326	327	329	334	346	349	360	362	358	359	356	357	355	353	352	351.4	354.41	357.2	0.5
h	5	1	-210	-193	-1/2	-148	-122	-96	-72	-51	-33	-12	3	15	16	19	26	31	46	4/	46	46	43.8	42.72	44.7	0.5
g	5	2	264	259	253	245	236	226	218	211	208	194	211	230	242	254	262	264	261	253	245	235	222.3	208.95	200.3	-1.5
n	5	2	55	30	5/	38	28	28 28	22	04	22	20	20	22	125	128	139	148	150	150	100	105	1/1.9	180.25	188.9	1.5
g	5	3	22	-1	-9	-10	-23	-28	-32	-33	-33	-20	-20	-23	-20	-51	120	-39	-/4	-93	-109	-118	-130.4	-130.34	-141.2	-0.7
	5	3	-55	-32	-55	-54	-36	125	-35	126	-75	-07	-07	-90	-117	-120	-139	-132	-151	-134	-133	-145	-133.1	-123.43	-110.1	1.2
B b	5	4	-00	-93	-102	-111	-119	-123	-131	-130	-141	-142	-147	-132	-130	-137	-100	-1.59	-102	-104	-105	-100	-108.0	-108.05	-105.1	3.7
	J	4	-124	-125	-120	-120	-12.5	-122	-110	-115	-115	-117	Continued a	=121	-114	-71	-71	-03	-70	-75	-07	-55	-57.5	-17.37	0.1	5.1

	Degree	Order	IGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	IGRF	SV								
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
g	5	5	-16	-26	-38	-51	-62	-69	-74	-76	-76	-82	-76	-69	-63	-62	-56	-49	-48	-46	-36	-17	-12.9	-13.55	-7.7	1.4
h	5	5	3	11	21	32	43	51	58	64	69	82	80	78	81	81	83	88	92	95	97	107	106.3	103.85	100.9	-0.6
g	6	0	63	62	62	61	61	61	60	59	57	59	54	47	46	45	43	45	48	53	61	68	72.3	73.60	72.8	-0.3
g	6	1	61	60	58	57	55	54	53	53	54	57	57	57	58	61	64	66	66	65	65	67	68.2	69.56	68.6	-0.3
h	6	1	-9	-7	-5	-2	0	3	4	4	4	6	-1	-9	-10	-11	-12	-13	-15	-16	-16	-17	-17.4	-20.33	-20.8	-0.1
g	6	2	-11	-11	-11	-10	-10	-9	-9	-8	-7	6	4	3	1	8	15	28	42	51	59	68	74.2	76.74	76.0	-0.3
h	6	2	83	86	89	93	96	99	102	104	105	100	99	96	99	100	100	99	93	88	82	72	63.7	54.75	44.2	-2.1
g	6	3	-217	-221	-224	-228	-233	-238	-242	-246	-249	-246	-247	-247	-237	-228	-212	-198	-192	-185	-178	-170	-160.9	-151.34	-141.4	1.9
h	6	3	2	4	5	8	11	14	19	25	33	16	33	48	60	68	72	75	71	69	69	67	65.1	63.63	61.5	-0.4
g	6	4	-58	-57	-54	-51	-46	-40	-32	-25	-18	-25	-16	-8	-1	4	2	1	4	4	3	-1	-5.9	-14.58	-22.9	-1.6
h	6	4	-35	-32	-29	-26	-22	-18	-16	-15	-15	-9	-12	-16	-20	-32	-37	-41	-43	-48	-52	-58	-61.2	-63.53	-66.3	-0.5
g	6	5	59	57	54	49	44	39	32	25	18	21	12	7	-2	1	3	6	14	16	18	19	16.9	14.58	13.1	-0.2
h	6	5	36	32	28	23	18	13	8	4	0	-16	-12	-12	-11	-8	-6	-4	-2	-1	1	1	0.7	0.24	3.1	0.8
g	6	6	-90	-92	-95	-98	-101	-103	-104	-106	-107	-104	-105	-107	-113	-111	-112	-111	-108	-102	-96	-93	-90.4	-86.36	-77.9	1.8
h	6	0	-69	-67	-65	-62	-57	-52	-46	-40	-33	-39	-30	-24	-17	-/	1	- 11	17	21	24	36	43.8	50.94	54.9	0.5
g	7	0	70	70	71	72	73	73	74	74	74	70	65	65	67	75	72	71	72	74	77	77	79.0	79.88	80.4	0.2
g	7	1	-55	-54	-54	-54	-54	-54	-54	-53	-53	-40	-55	-56	-56	-57	-57	-56	-59	-62	-64	-72	-/4.0	-/4.46	-75.0	-0.1
n 	7	2	-43	-40	-47	-40	-49	-50	-51	-52	-32	-4.5	-55	-30	-55	-01	-70	-//	-62	-0.5	-80	-09	-04.0	-01.14	-57.6	0.0
s h	7	2	-13	-14	-14	-14	-14	-14	-15	-17	-18	-18	-17	-24	-28	-27	-27	-26	-27	-27	-26	-25	-24.2	-1.05		-0.0
, n	7	3	34	33	32	31	29	27	25	23	20	0	-1,	10	15	13	14	16	21	24	26	28	33.3	38.73	45.3	1.4
5 h	7	3	-10	-11	-12	-12	-13	-14	-14	-14	-14	2	0	-4	-6	-2	-4	-5	-5	-2	0	4	62	6.82	66	-0.2
g	7	4	-41	-41	-40	-38	-37	-35	-34	-33	-31	-29	-40	-32	-32	-26	-22	-14	-12	-6	-1	5	9.1	12.30	14.0	0.3
h	7	4	-1	0	1	2	4	5	6	7	7	6	10	8	7	6	8	10	16	20	21	24	24.0	25.35	24.9	-0.1
g	7	5	-21	-20	-19	-18	-16	-14	-12	-11	-9	-10	-7	-11	-7	-6	-2	0	1	4	5	4	6.9	9.37	10.4	0.1
h	7	5	28	28	28	28	28	29	29	29	29	28	36	28	23	26	23	22	18	17	17	17	14.8	10.93	7.0	-0.8
g	7	6	18	18	18	19	19	19	18	18	17	15	5	9	17	13	13	12	11	10	9	8	7.3	5.42	1.6	-0.8
h	7	6	-12	-12	-13	-15	-16	-17	-18	-19	-20	-17	-18	-20	-18	-23	-23	-23	-23	-23	-23	-24	-25.4	-26.32	-27.7	-0.3
g	7	7	6	6	6	6	6	6	6	6	5	29	19	18	8	1	-2	-5	-2	0	0	-2	-1.2	1.94	4.9	0.4
h	7	7	-22	-22	-22	-22	-22	-21	-20	-19	-19	-22	-16	-18	-17	-12	-11	-12	-10	-7	-4	-6	-5.8	-4.64	-3.4	0.2
g	8	0	11	11	11	11	11	11	11	11	11	13	22	11	15	13	14	14	18	21	23	25	24.4	24.80	24.3	-0.1
g	8	1	8	8	8	8	7	7	7	7	7	7	15	9	6	5	6	6	6	6	5	6	6.6	7.62	8.2	0.1
h	8	1	8	8	8	8	8	8	8	8	8	12	5	10	11	7	7	6	7	8	10	11	11.9	11.20	10.9	0.0
g	8	2	-4	-4	-4	-4	-3	-3	-3	-3	-3	-8	-4	-6	-4	-4	-2	-1	0	0	-1	-6	-9.2	-11.73	-14.5	-0.5
h	8	2	-14	-15	-15	-15	-15	-15	-15	-15	-14	-21	-22	-15	-14	-12	-15	-16	-18	-19	-19	-21	-21.5	-20.88	-20.0	0.2
g	8	3	-9	-9	-9	-9	-9	-9	-9	-9	-10	-5	-1	-14	-11	-14	-13	-12	-11	-11	-10	-9	-7.9	-6.88	-5.7	0.3
h	8	3	7	7	6	6	6	6	5	5	5	-12	0	5	7	9	6	4	4	5	6	8	8.5	9.83	11.9	0.5
g	8	4	1	1	1	2	2	2	2	1	1	9	11	6	2	0	-3	-8	-7	-9	-12	-14	-16.6	-18.11	-19.3	-0.3
h	8	4	-13	-13	-13	-13	-14	-14	-14	-15	-15	-7	-21	-23	-18	-16	-17	-19	-22	-23	-22	-23	-21.5	-19.71	-17.4	0.4
1													Continued of	n next page												

	Degree	Order	IGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	IGRF	SV								
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
g	8	5	2	2	2	3	4	4	5	6	6	7	15	10	10	8	5	4	4	4	3	9	9.1	10.17	11.6	0.3
h	8	5	5	5	5	5	5	5	5	5	5	2	-8	3	4	4	6	6	9	11	12	15	15.5	16.22	16.7	0.1
g	8	6	-9	-8	-8	-8	-7	-7	-6	-6	-5	-10	-13	-7	-5	-1	0	0	3	4	4	6	7.0	9.36	10.9	0.2
h	8	6	16	16	16	16	17	17	18	18	19	18	17	23	23	24	21	18	16	14	12	11	8.9	7.61	7.1	-0.1
g	8	7	5	5	5	6	6	7	8	8	9	7	5	6	10	11	11	10	6	4	2	-5	-7.9	-11.25	-14.1	-0.5
h	8	7	-5	-5	-5	-5	-5	-5	-5	-5	-5	3	-4	-4	1	-3	-6	-10	-13	-15	-16	-16	-14.9	-12.76	-10.8	0.4
g	8	8	8	8	8	8	8	8	8	7	7	2	-1	9	8	4	3	1	-1	-4	-6	-7	-7.0	-4.87	-3.7	0.2
h	8	8	-18	-18	-18	-18	-19	-19	-19	-19	-19	-11	-17	-13	-20	-17	-16	-17	-15	-11	-10	-4	-2.1	-0.06	1.7	0.4
g	9	0	8	8	8	8	8	8	8	8	8	5	3	4	4	8	8	7	5	5	4	4	5.0	5.58	5.4	-
g	9	1	10	10	10	10	10	10	10	10	10	-21	-7	9	6	10	10	10	10	10	9	9	9.4	9.76	9.4	-
h	9	1	-20	-20	-20	-20	-20	-20	-20	-20	-21	-27	-24	-11	-18	-22	-21	-21	-21	-21	-20	-20	-19.7	-20.11	-20.5	-
g	9	2	1	1	1			1	1	1	1	1	-1	-4	0	2	2	2	1	1	1	3	3.0	3.58	3.4	-
n	9	2	14	14	14	14	14	14	14	15	15	17	19	12	12	15	10	10	10	15	15	15	15.4	6.04	5.2	-
g h	9	3	-11	-11	-11	-11	-11	-11	-12	-12	-12	-11	-23	-5	-9	-13	-12	-12	-12	-12	-12	-10	-0.4	-0.94	-3.5	-
g	9	4	12	12	12	12	12	12	12	11	11	3	10	2	- 1	10	10	10	9	9	9	8	6.3	5.01	3.1	_
h	9	4	-3	-3	-3	-3	-3	-3	-3	-3	-3	-9	2	6	0	-4	-4	-4	-5	-6	-7	-6	-6.2	-6.72	-7.2	
g	9	5	1	1	1	1	1	1	1	1	1	16	5	4	4	-1	-1	-1	-3	-3	-4	-8	-8.9	-10.76	-12.4	-
h	9	5	-2	-2	-2	-2	-2	-2	-2	-3	-3	4	2	-2	-3	-5	-5	-5	-6	-6	-7	-8	-8.4	-8.16	-7.4	-
g	9	6	-2	-2	-2	-2	-2	-2	-2	-2	-2	-3	-5	1	-1	-1	0	-1	-1	-1	-2	-1	-1.5	-1.25	-0.8	-
h	9	6	8	8	8	8	9	9	9	9	9	9	8	10	9	10	10	10	9	9	9	8	8.4	8.10	8.0	-
g	9	7	2	2	2	2	2	2	3	3	3	-4	-2	2	-2	5	3	4	7	7	7	10	9.3	8.76	8.4	-
h	9	7	10	10	10	10	10	10	10	11	11	6	8	7	8	10	11	11	10	9	8	5	3.8	2.92	2.2	-
g	9	8	-1	0	0	0	0	0	0	0	1	-3	3	2	3	1	1	1	2	1	1	-2	-4.3	-6.66	-8.4	-
h	9	8	-2	-2	-2	-2	-2	-2	-2	-2	-2	1	-11	-6	0	-4	-2	-3	-6	-7	-7	-8	-8.2	-7.73	-6.1	-
g	9	9	-1	-1	-1	-1	-1	-1	-2	-2	-2	-4	8	5	-1	-2	-1	-2	-5	-5	-6	-8	-8.2	-9.22	-10.1	-
h	9	9	2	2	2	2	2	2	2	2	2	8	-7	5	5	1	1	1	2	2	2	3	4.8	6.01	7.0	-
g	10	0	-3	-3	-3	-3	-3	-3	-3	-3	-3	-3	-8	-3	1	-2	-3	-3	-4	-4	-3	-3	-2.6	-2.17	-2.0	-
g	10	1	-4	-4	-4	-4	-4	-4	-4	-4	-4	11	4	-5	-3	-3	-3	-3	-4	-4	-4	-6	-6.0	-6.12	-6.3	-
h	10	1	2	2	2	2	2	2	2	2	2	5	13	-4	4	2	1	1	1	1	2	1	1.7	2.19	2.8	-
g	10	2	2	2	2	2	2	2	2	2	2	1	-1	-1	4	2	2	2	2	3	2	2	1.7	1.42	0.9	-
h	10	2	1	1	1	1	1	1	1	1	1	1	-2	0	1	1	1	1	0	0	1	0	0.0	0.10	-0.1	-
g	10	3	-5	-5	-5	-5	-5	-5	-5	-5	-5	2	13	2	0	-5	-5	-5	-5	-5	-5	-4	-3.1	-2.35	-1.1	-
h	10	3	2	2	2		2	2	2	2	2	-20	-10	-8	0	2	3	3	3	3	3	4	4.0	4.46	4.7	-
g	10	4	-2	-2	-2	-2	-2	-2	-2	-2	-2	-5	-4	-3	-1	-2	-1	-2	-2	-2	-2	-1	-0.5	-0.15	-0.2	-
h	10	4	0	0	0	0	0	0	0	0	0	-1	2	-2		0	4	4	6	0	0	5	4.9	4.70	4.4	-
g F	10	5	0	0	0	0	0	0	0	0	0	-1	4		4	4	o ,	3	5	5	4	4	5./	5.00	2.5	-
11 g	10	6	-4	4	-4	4	4	4	4	4	4	-0	12	4	-5	-+	-+	4	-4	-+	-+	2	-5.9	0.29	-7.2	
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	Degree	Order	IGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	IG₽	SV								
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
h	10	6	0	0	0	0	0	0	0	0	0	6	6	1	1	0	0	-1	0	0	0	-1	-1.2	-1.01	-1.0	-
g	10	7	0	0	0	0	0	0	0	0	0	-1	3	-2	1	0	1	1	1	1	1	2	2.0	2.06	2.2	-
h	10	7	-2	-2	-2	-2	-2	-2	-2	-1	-1	-4	-3	-3	-1	-2	-1	-1	-1	-1	-2	-2	-2.9	-3.47	-4.0	-
g	10	8	2	2	2	1	1	1	1	2	2	-3	2	6	-1	2	0	0	2	2	3	5	4.2	3.77	3.1	-
h	10	8	4	4	4	4	4	4	4	4	4	-2	6	7	6	3	3	3	4	4	3	1	0.2	-0.86	-2.0	-
g	10	9	2	2	2	2	3	3	3	3	3	5	10	-2	2	2	3	3	3	3	3	1	0.3	-0.21	-1.0	-
h	10	9	0	0	0	0	0	0	0	0	0	0	11	-1	0	0	1	1	0	0	-1	-2	-2.2	-2.31	-2.0	-
g	10	10	0	0	0	0	0	0	0	0	0	-2	3	0	0	0	-1	-1	0	0	0	0	-1.1	-2.09	-2.8	-
h	10	10	-6	-6	-6	-6	-6	-6	-6	-6	-6	-2	8	-3	-7	-6	-4	-5	-6	-6	-6	-7	-7.4	-7.93	-8.3	-
g	11	0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	2.7	2.95	3.0	-
g	11	1	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-1.7	-1.60	-1.5	-
h	11	1	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.1	0.26	0.1	-
g	11	2	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-1.9	-1.88	-2.1	-
h	11	2	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	1.3	1.44	1.7	-
g	11	3	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	1.5	1.44	1.6	-
h	11	3	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.9	-0.77	-0.6	-
g	11	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.1	-0.31	-0.5	-
h	11	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-2.6	-2.27	-1.8	-
g	11	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.1	0.29	0.5	-
h	11	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.9	0.90	0.9	-
g	11	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.7	-0.79	-0.8	-
h	11	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.7	-0.58	-0.4	-
g		7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.7	0.53	0.4	-
h	11	7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-2.8	-2.69	-2.5	-
g L	11	0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	1./	1.60	1.0	-
n a	11	0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.9	-1.08	-1.5	-
b B	11	<i>y</i> 0							-														-1.2	-1.58	-2.1	-
, "	11	10								_	_			-		-					-		12	0.96	0.8	_
5 h	11	10	-	_		_	_				-	_				-	_	_			-	-	-19	-1.90	-19	_
 σ	11	11					_			_				-				_			_		4.0	3.99	3.8	_
h	11	11	-	-	-	-	-	-	-	-	-	-	-		-	-	-	-	-	-	-	-	-0.9	-1.39	-1.8	-
g	12	0	-	-	-	-	-	-			-	-		-	-	-	-	-	-		-	-	-2.2	-2.15	-2.1	-
g	12	1	-	-	-	-	-	-	-	-	-	-	-		-	-	-	-	-	-		-	-0.3	-0.29	-0.2	-
h	12	1	-	-		-	-	-	-	-	-	-	-		-	-	-	-	-	-	-	-	-0.4	-0.55	-0.8	-
g	12	2	-	-	-	-	-	-	-	-		-	-		-	-	-	-	-	-		-	0.2	0.21	0.3	-
h	12	2	-	-	-	-	-	-	-	-		-	-		-	-	-	-	-	-	-	-	0.3	0.23	0.3	-
g	12	3	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.9	0.89	1.0	-
h	12	3	-	-	-	-	-	-	-	-	-	-	-		-	-	-	-	-	-	-	-	2.5	2.38	2.2	-
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	Degree	Order	IGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	DGRF	IGRF	SV								
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
g	12	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.2	-0.38	-0.7	-
h	12	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-2.6	-2.63	-2.5	-
g	12	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.9	0.96	0.9	-
h	12	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.7	0.61	0.5	-
g	12	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.5	-0.30	-0.1	-
h	12	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.40	0.6	-
g	12	7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.46	0.5	-
h	12	7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.0	0.01	0.0	-
g	12	8	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.3	-0.35	-0.4	-
h	12	8	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.0	0.02	0.1	-
g	12	9	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.36	-0.4	-
h	12	9	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.28	0.3	-
g	12	10	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.1	0.08	0.2	-
h	12	10	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.9	-0.87	-0.9	-
g	12	11	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.2	-0.49	-0.8	-
h	12	11	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.34	-0.2	-
g	12	12	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.08	0.0	-
h	12	12	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.8	0.88	0.8	-
g	13	0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.2	-0.16	-0.2	-
g	13	1	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.9	-0.88	-0.9	-
h	13	1	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.9	-0.76	-0.8	-
g	13	2	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.30	0.3	-
h	13	2	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.2	0.33	0.3	-
g	13	3	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.1	0.28	0.4	-
h	13	3	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	1.8	1.72	1.7	-
g	13	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.43	-0.4	-
h	13	4	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.54	-0.6	-
g	13	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	1.3	1.18	1.1	-
h	13	5	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-1.0	-1.07	-1.2	-
g	13	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.37	-0.3	-
h	13	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.1	-0.04	-0.1	-
g	13	7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.7	0.75	0.8	-
h	13	7	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.7	0.63	0.5	-
g	13	8	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.4	-0.26	-0.2	-
h	13	8	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.21	0.1	-
g	13	9	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.35	0.4	-
h	13	9	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.6	0.53	0.5	-
g	13	10	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.1	-0.05	0.0	-
h	13	10	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.3	0.38	0.4	-
													Continued of	on next page											i	

	Degree	Order	IGRF	DGRF	IGRE	SV																				
g/h	n	m	1900.0	1905.0	1910.0	1915.0	1920.0	1925.0	1930.0	1935.0	1940.0	1945.0	1950.0	1955.0	1960.0	1965.0	1970.0	1975.0	1980.0	1985.0	1990.0	1995.0	2000.0	2005.0	2010.0	2010-15
g	13	11	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.4	0.41	0.4	-
h	13	11	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.2	-0.22	-0.2	-
g	13	12	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.0	-0.10	-0.3	-
h	13	12	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-0.5	-0.57	-0.5	-
g	13	13	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	0.1	-0.18	-0.3	-
h	13	13	-	-	-	-	-	-	-	-	-	-	-	-	-	-		-	-	-	-	-	-0.9	-0.82	-0.8	-

Maps of the Declination D, Inclination I and Total Intensity F at Earth's surface in 2010 are dis-132 played in Figure 1. Together these quantities completely define the vector magnetic field. Noteworthy 133 features include the fact that there are three agonic lines (lines of zero D), while a more dipolar-type 134 field would have only two. These correspond to the one that passes approximately north-south through 135 the Americas, and the one located to the east of Asia continuing down through Indonesia then to the 136 west of Australia. The extra one passes down through central Europe extending as far south as Kenya 137 before looping back northward via India. Moreover, D is rather small over a large region spanning 138 mid and low latitudes extending from northeastern Africa east to the Philippine islands. The map of 139 I in the middle panel of Figure 1 displays a distinctive deflection in the dip equator southwards at 140 South America, an offset in the maximum of I from the geographic south pole towards Australia and 141 also a tongue of high I extending westwards from Southern Africa. The map of F in 2010 in the 142 bottom panel of Fig. 1 shows that the regions with highest field intensity are located in Siberia in the 143 northern hemisphere and in the Southern Ocean and Antarctica southwards of Australia in the south-144 ern hemisphere. Perhaps the most striking feature of all is the low field intensity anomaly currently 145 centred around Southern Brazil and Paraguay. This feature is often referred to as the South Atlantic 146 Anomaly, and it is known to have important consequences regarding the impact of space weather on 147 the near-Earth electromagnetic environment (Gledhill, 1976; Heirtzler, 2002; Facius & Reitz, 2007). 148

All the features mentioned above are well known from previous global field models; they have ex-149 isted for at least several hundred years and have slowly evolved to their present configuration (Jackson 150 et al., 2000). The current evolution of main field is illustrated in Fig. 2 which shows the IGRF-11 pre-151 diction of the average annual rate of change (SV) in the Declination D, Inclination I and Total Intensity 152 F between 2010 and 2015. The predicted changes in D are small in the Pacific hemisphere, and con-153 sistent with a continued westward motion of field features in the Atlantic hemisphere. Changes in I are 154 predicted to be largest at low latitudes, with the maximum negative change occurring near northeastern 155 Brazil (close to where the dip equator is presently being deflected southwards) while the maximum 156 positive change is predicted to occur close to Southern India. Considering the predicted changes in 157 F, the largest decreases are predicted over eastern North America as well as below South America. 158 The later involves a continued deepening and westward motion of the South Atlantic Anomaly. The 159 largest increases in F are predicted to take place in central equatorial Atlantic, in the southern Indian 160 ocean (southeast of Africa), and in the region encompassing Iran, Kazakhstan, Afghanistan, Pakistan 161 and India. Understanding of the future evolution of these field features requires detailed knowledge 162 of the magnetohydrodynamic motional induction processes taking place in the liquid iron outer core. 163 Such processes are only partly understood at present, but are the focus of much active research (Olson, 164 2007). 165



Figure 1. Maps of the magnetic declination D (top, units are degrees), inclination I (middle, units are degrees), and total intensity F (bottom, units are nT) at the Earth's surface in 2010 from the new field model IGRF 2010.0. Molleweide projection is used, zero line is shown in green, positive contours in red and negative contours in blue.



Figure 2. Maps of the predicted rate of change per year in the Declination D (top, units are degrees/yr), the Inclination I (middle, units are degrees/yr), and Total Intensity F (bottom, units are nT/yr) at the Earth's surface for the interval 2010-2015 as predicted by IGRF-11. Molleweide projection is used, zero line is shown in green, positive contours in red and negative contours in blue.

Further details concerning the evolution of the South Atlantic Anomaly since 1900 as captured 166 by IGRF-11 are presented in Fig. 3 (see also Macmillan et al., 2009). The left plot shows how the 167 lowest field intensity F within the South Atlantic Anomaly has systematically decreased since 1900. 168 The decrease has been almost linear since 1940 (when the lowest intensity was 24954 nT) until the 169 present (the lowest intensity in 2010 was 22590 nT) with an average decrease of 34 nT/yr. There is 170 no sign that the decrease of field intensity in the South Atlantic Anomaly is abating, with a further 171 decrease to 22430 nT predicted by 2015. The right hand plot documents the motion of the location 172 of this point of lowest field intensity every 5 years from 1900.0 to 2015.0, where the final point is 173 a prediction. The position of lowest intensity has moved both southward and westward, but almost 174 exclusively westwards since 1955. This analysis describes only the position with lowest intensity; the 175 spatial extent of the south Atlantic anomaly has also increased during the past century, as measured, 176 for example, by the area within the 28000nT contour of F. Note however, that the exact position of 177 the lowest intensity point is known only rather crudely, particularly before 1960 when there was larger 178 uncertainty in the field models. 179

Finally in Fig. 4 we present the positions of the magnetic dip pole (where inclination I as determined from the complete field model, is vertical) and the geomagnetic pole (as determined only from the dipole, n = 1, field coefficients alone) calculated from IGRF-11 and plotted as a function of time since 1900. Pole positions are also tabulated in Table 3. It is noteworthy that the North magnetic dip pole is currently moving at a high speed of over 50 km/yr, as has recently been investigated by Newitt et al. (2009).

¹⁸⁶ Due to the changes currently taking place in the internal geomagnetic field, including the devel-¹⁸⁷ opment of the South Atlantic Anomaly and the motions of the geomagnetic poles described above, ¹⁸⁸ continued careful monitoring is essential. The CHAMP and Ørsted satellites that were crucial sources ¹⁸⁹ of observations for IGRF-11 are now approaching the end of their lifetimes, but fortunately one of ¹⁹⁰ the aims of the upcoming ESA Swarm mission (Friis-Christensen et al., 2006) is to provide the high ¹⁹¹ quality satellite data that will be of great importance to the next IGRF revision.



Total Intensity F / nT

Figure 3. Evolution of the South Atlantic Anomaly during the twentieth century: Top plot (a) shows how the minimum F at the Earth's surface (in the South Atlantic Anomaly where the magnitude of the field is smallest) has decreased from 1900 towards the present day, units are nT. The bottom plot (b) tracks the location of the point of lowest field magnitude with time; the colour scale indicates the magnitude of F, with blue representing smallest F, units are nT.

(b)



Figure 4. Motion of the magnetic dip pole (red) and geomagnetic pole (blue) since 1900 from IGRF-11 in the northern hemisphere (top) and the southern hemisphere (bottom). Stereographic projection is employed. The scale bar gives an indication of distance that is correct along lines of constant longitude and also along the middle lines of latitude shown (± 80 degrees).

	North	dip pole	South	dip pole	North geor	nagnetic pole	South geor	nagnetic pole
Epoch	Latitude	Longitude	Latitude	Longitude	Latitude	Longitude	Latitude	Longitude
1900.0	70.46	-96.19	-71.72	148.32	78.68	-68.79	-78.68	111.21
1905.0	70.66	-96.48	-71.46	148.55	78.68	-68.75	-78.68	111.25
1910.0	70.79	-96.72	-71.15	148.64	78.66	-68.72	-78.66	111.28
1915.0	71.03	-97.03	-70.80	148.54	78.64	-68.57	-78.64	111.43
1920.0	71.34	-97.39	-70.41	148.20	78.63	-68.38	-78.63	111.62
1925.0	71.79	-98.00	-69.99	147.63	78.62	-68.27	-78.62	111.73
1930.0	72.27	-98.69	-69.52	146.79	78.60	-68.26	-78.60	111.74
1935.0	72.80	-99.34	-69.06	145.77	78.57	-68.36	-78.57	111.64
1940.0	73.30	-99.87	-68.57	144.60	78.55	-68.51	-78.55	111.49
1945.0	73.93	-100.24	-68.15	144.44	78.55	-68.53	-78.55	111.47
1950.0	74.64	-100.86	-67.89	143.55	78.55	-68.85	-78.55	111.15
1955.0	75.18	-101.41	-67.19	141.50	78.54	-69.16	-78.54	110.84
1960.0	75.30	-101.03	-66.70	140.23	78.58	-69.47	-78.58	110.53
1965.0	75.63	-101.34	-66.33	139.53	78.60	-69.85	-78.60	110.15
1970.0	75.88	-100.98	-66.02	139.40	78.66	-70.18	-78.66	109.82
1975.0	76.15	-100.64	-65.74	139.52	78.76	-70.47	-78.76	109.53
1980.0	76.91	-101.68	-65.42	139.34	78.88	-70.76	-78.88	109.24
1985.0	77.40	-102.61	-65.13	139.18	79.04	-70.90	-79.04	109.10
1990.0	78.09	-103.68	-64.91	138.90	79.21	-71.13	-79.21	108.87
1995.0	79.09	-105.42	-64.79	138.76	79.39	-71.42	-79.39	108.58
2000.0	80.97	-109.64	-64.66	138.30	79.61	-71.57	-79.61	108.43
2005.0	83.19	-118.24	-64.55	137.85	79.82	-71.81	-79.82	108.19
2010.0	85.01	-132.66	-64.43	137.32	80.08	-72.22	-80.08	107.78
2015.0	86.07	-153.27	-64.30	136.74	80.36	-72.62	-80.36	107.38

Table 3. Magnetic pole positions since 1900 as determined from IGRF-11.

192 5 IGRF-11 ONLINE DATA PRODUCTS

- ¹⁹³ Further general information about the IGRF:
- http://www.ngdc.noaa.gov/IAGA/vmod/igrf.html.
- ¹⁹⁵ The coefficients of IGRF-11 in various file formats:
- http://www.ngdc.noaa.gov/IAGA/vmod/igrf11coeffs.txt
- ¹⁹⁷ Fortran software for synthesizing the field from the coefficients:
- http://www.ngdc.noaa.gov/IAGA/vmod/igrf11.f
- ¹⁹⁹ C software for synthesizing the field from the coefficients (Linux):
- 200 http://www.ngdc.noaa.gov/IAGA/vmod/geomag70_linux.tar.gz

- ²⁰¹ C software for synthesizing the field from the coefficients (Windows):
- 202 http://www.ngdc.noaa.gov/IAGA/vmod/geomag70_windows.zip

203

- ²⁰⁴ Online computation of field components from the IGRF-11 model:
- 205 http://www.ngdc.noaa.gov/geomagmodels/IGRFWMM.jsp
- 206 http://www.geomag.bgs.ac.uk/gifs/igrf_form.shtml
- 207 http://wdc.kugi.kyoto-u.ac.jp/igrf/point/index.html
- 208
- ²⁰⁹ Archive of legacy versions of the IGRF model:
- 210 http://www.ngdc.noaa.gov/IAGA/vmod/igrf_old_models.html
- 211

²¹² Candidate models contributing to IGRF-11, and various test models are available for evaluation pur-²¹³ poses:

214 http://www.ngdc.noaa.gov/IAGA/vmod/candidatemodels.html

215

The 11th generation IGRF was computed from candidate models produced and evaluated by participating members of IAGA Working Group V-MOD who are listed as co-authors of this paper. Their institutes and the many organizations involved in operating the magnetic satellites CHAMP, Ørsted and SAC-C, observatories (see Appendix for a list), magnetic survey programmes and the World Data Centres are thanked for their continued support of the IGRF project.

221 APPENDIX

222 World Data Centres

- 223 WORLD DATA CENTRE FOR GEOPHYSICS AND MARINE GEOLOGY, BOULDER
- 224 National Geophysical Data Center
- E/GC 325 Broadway
- 226 Boulder, Colorado
- 227 USA 80305-3328
- ²²⁸ TEL: +01 303 497 6826
- ²²⁹ FAX: +01 303 497 6513
- 230 EMAIL: ngdc.info@noaa.gov
- 231 INTERNET: http://www.ngdc.noaa.gov/geomag/wdc/index.html
- 232
- 233 WORLD DATA CENTRE FOR GEOMAGNETISM, COPENHAGEN
- 234 DTU Space, Juliane Maries vej 30
- 235 DK-2100, Copenhagen
- 236 DENMARK
- 237 TEL: +45 3532 5700
- ²³⁸ FAX: +45 353 62475
- 239 EMAIL: jrgm@space.dtu.dk
- 240 INTERNET:http://www.space.dtu.dk/English/Research/Scientific_data_and_models
- 241

242 WORLD DATA CENTRE FOR GEOMAGNETISM, EDINBURGH

- 243 British Geological Survey
- ²⁴⁴ Murchison House, West Mains Road
- 245 Edinburgh, EH9 3LA
- 246 UNITED KINGDOM
- ²⁴⁷ TEL: +44 131 650 0234
- ²⁴⁸ FAX: +44 131 668 4368
- 249 EMAIL: wdcgeomag@bgs.ac.uk
- ²⁵⁰ INTERNET: http://www.wdc.bgs.ac.uk/catalog/master.html

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252 WORLD DATA CENTRE FOR GEOMAGNETISM, KYOTO
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- ²⁵³ Data Analysis Center for Geomagnetism and Space Magnetism
- ²⁵⁴ Graduate School of Science, Kyoto University
- 255 Kitashirakawa-Oiwake Cho, Sakyo-ku
- 256 Kyoto, 606-8502, JAPAN
- ²⁵⁷ TEL: +81 75 753 3929
- ²⁵⁸ FAX: +81 75 722 7884
- ²⁵⁹ EMAIL: iyemori@kugi.kyoto-u.ac.jp
- 260 INTERNET: http://wdc.kugi.kyoto-u.ac.jp
- 261

262 WORLD DATA CENTRE FOR GEOMAGNETISM, MUMBAI

- ²⁶³ Indian Institute of Geomagnetism
- ²⁶⁴ Colaba, Mumbai, 400 005, INDIA
- ²⁶⁵ TEL: +91 22 215 0293
- 266 FAX: +91 22 218 9568
- 267 EMAIL: abh@iigs.iigm.res.in
- ²⁶⁸ INTERNET: http:///iigm.res.in
- 269

270 Magnetic observatories contributing data used in the construction of IGRF-11

Supporting Agencies	Country	Observatory IAGA code								
Centre de Recherche en Astronomie, Astrophysique et Geophysique	ALGERIA	ТАМ								
Universidad Nacional de la Plata	ARGENTINA	TRW								
Geoscience Australia	AUSTRALIA	ASP, CNB, CSY, CTA, DVS, GNA, KDU, LRM, MAW, MCQ								
Zentralanstalt für Meteorologie und Geodynamik	AUSTRIA	WIK								
Institut Royal Météorologique	BELGIUM	DOU, MAB								
CNPq-Observatorio Nacional	BRAZIL	VSS								
Academy of Sciences	BULGARIA	PAG								
Geological Survey of Canada	CANADA	ALE, BLC, CBB, FCC, IQA, MEA, OTT, PBQ, RES, STJ, VIC, YKC								
Academy of Sciences	CHINA	BMT								
China Earthquake Adminstration	CHINA	CDP, CNH, GLM, GZH, KSH, LZH, MZL, QGZ, QIX, SSH, THJ, WHN								
Instituto Geográfico Agustín Codazzi	COLOMBIA	FUQ								
Academy of Sciences	CZECH REPUBLIC	BDV								
Danish Meteorological Institute / DTU Space	DENMARK	BFE, GDH, NAQ, THL								
Addis Ababa University	ETHIOPIA	AAE								
Finnish Meteorological Institute	FINLAND	NUR								
Continued on next page										

Supporting Agencies	Country	Observatory IAGA code
Geophysical Observatory	FINLAND	SOD
Institut de Physique du Globe de Paris	FRANCE	AAE, BOX, CLF, KOU, LZH,PHU, QSB, PPT, TAM
Ecole et Observatoire des Sciences de la Terre	FRANCE	AMS, CZT, DRV, PAF, TAN
Institut Français de Recherche Scientifique pour le Développement	FRANCE	BNG, MBO
Academy of Sciences	GEORGIA	TFS
Universität München	GERMANY	FUR
Alfred-Wegener-Institute for Polar Marine Research &	GERMANY	VNA
GFZ Hemholtz Centre Potsdam	GERMANY	NGK, WNG
Universität Stuttgart	GERMANY	BFO
Institute of Geology and Mineral Exploration	GREECE	PEG
Academy of Sciences	HUNGARY	NCK
Eötvös Loránd Geophysical Institute	HUNGARY	THY
University of Iceland	ICELAND	LRV
Indian Institute of Geomagnetism	INDIA	ABG, NGP, PND, SIL, TIR, UJJ, VSK
Badan Meteorologi dan Geofisika	INDONESIA	TND, TUN
Meteorological Service	IRELAND	VAL
Survey of Israel	ISRAEL	AMT, BGY, ELT
Instituto Nazionale di Geofisica e Vulcanologia	ITALY	AQU
Japan Coast Guard	JAPAN	НТҮ
Japan Meteorological Agency	JAPAN	CBI, KAK, KNY, MMB
Geographical Survey Institute	JAPAN	ESA, KNZ, MIZ
Science for Institute of the Ionosphere	KAZAKHSTAN	ААА
National Centre for Geophysical Research	LEBANON	QSB
Université dAntananarivo	MADAGASCAR	TAN
Universidad Nacional Autonoma de México	MEXICO	TEO
Institute of Geological and Nuclear Sciences	NEW ZEALAND	API, EYR, SBA
University of Tromsø	NORWAY	BJN, DOB, TRO
Instituto Geofisico del Peru	PERU	HUA
Academy of Sciences	POLAND	BEL, HLP, HRN
Directorate General of Telecommunications	REPUBLIC OF CHINA	LNP
Instituto Nacional de Geologia	REPÚ BLICA DE MOÇAMBIQUE	LMM
Geological Survey of Romania	ROMANIA	SUA
Academy of Sciences	RUSSIA	ARS, BOX, LVV, MOS, NVS
Institute of Solar-Terrestrial Physics	RUSSIA	IRT
Dept. of Agriculture, Forestry, Fisheries & Meteorology	SAMOA	API
Geomagnetic College Grocka	SERBIA & MONTENEGRO	GCK
Slovenska Akademia Vied	SLOVAKIA	HRB
National Research Foundation	SOUTH AFRICA	HBK, HER, TSU
Observatori de lEbre	SPAIN	EBR, LIV
Real Instituto y Observatorio de la Armada	SPAIN	SFS
Instituto Geográfico Nacional	SPAIN	GUI, SPT
Sveriges Geologiska Undersökning	SWEDEN	ABK, LOV, UPS
	Continued on next page	•

Supporting Agencies	Country	Observatory IAGA code
Swedish Institute of Space Physics	SWEDEN	KIR
Bŏgaziçi University	TURKEY	IZN
Academy of Sciences	UKRAINE	AIA
British Geological Survey	UNITED KINGDOM	ASC, ESK, HAD, LER, PST
US Geological Survey	UNITED STATES	BRW, BOU, BSL, CMO, DLR, FRD, FRN, GUA
		HON, MID, NEW, SIT, SJG, SHU, TUC
Academy of Science and Technology	VIETNAM	PHU

Table 4: List of agencies supporting observatories whose data was used in deriving constituent models for IGRF-11.

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