

I.O.S.

ESTIMATES OF EXTREME CURRENT SPEEDS
OVER THE CONTINENTAL SLOPE OFF SCOTLAND

BY

D.J.T. CARTER, J. LOYNES AND P.G. CHALENOR

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INSTITUTE OF OCEANOGRAPHIC SCIENCES

WORMLEY

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SUMMARY

A method for estimating return values of current speed from time-series data, based upon the convolution of tidal and non-tidal (residual) components, is described. It is applied to the CONSLEX data set of measurements obtained over the Continental Slope to the northwest of the UK during 1982-83, to obtain estimates of 50-year return values of hourly mean speed along-slope, cross-slope and omni-directional.

The method depends upon the speed of the tidal component being at least comparable with the residual component. This condition is found to hold at most CONSLEX sites west of 4°W but usually not at sites to the east of 4°W .

Histograms are presented showing the observed probability distributions of tidal and residual components of current speed and their convolutions along- and cross-slope for each CONSLEX current meter data set.

1. INTRODUCTION

As exploration for offshore oil and gas resources moves into deeper waters, so the need for estimates of extreme currents also extends into them. In particular, designers of offshore structures require estimates of extreme speeds over the continental slope to the West and North of Scotland in order to assess the feasibility and design of rigs there, where water depths are between 200m and 1000m.

Estimating extreme values of environmental parameters (such as the 50-year return value of wind speed or wave height) generally requires many years of measurements or the use of a well-validated model. Neither is available for estimating ocean currents on the UK continental slope. Fortunately, the forcing periods of the tides are well-established and extreme tidal speeds can be calculated from considerably shorter series of measurements.

If the tidal component is a significant portion of the extreme total current speed, then - as pointed out by Pugh and Vassie (1980) - estimates of extreme values can be made from relatively short data sets. This report develops a method for doing so, and applies it to estimate 50-year return values of hourly mean current speed from the Continental Slope Experiment (CONSLEX) measurements obtained between August 1982 and April 1983 from twenty moorings laid on the slope to the West and North of Scotland (Gould, 1982). The locations of these moorings are shown in Figure 1. Their co-ordinates are given, along with the water depth at each mooring, in Table 1.

Estimating extremes from records covering only about seven months is clearly unsatisfactory, particularly as we have only a limited understanding of the physics of some components of the total current. However, the tidal constituents are obtainable, with good accuracy, from the CONSLEX data; so, where the tidal stream contributes a significant portion of the total current, we might expect a reasonable estimate for the extreme speed - although it is not possible to put confidence limits upon the value - but at some current meters the tide turns out to be relatively small and here the estimates are questionable.

2. METHOD OF ANALYSIS

2.1 Probability distribution of resolved speed

Given a data series of current speed resolved in a specified direction, such as the easterly component of mean values at hourly intervals, and assuming the series is sufficiently long to estimate the tidal component, then the total speed in the specified direction at any hour, U , can be expressed as a tidal component, U_t , and a residual U_r :

$$U = U_t + U_r$$

and histograms can be constructed showing estimates for the probability distributions of U_t and U_r , p_t and p_r .

Assuming the tidal and residual components are independent, then the probability distribution of U , p_{t+r} , is given by a convolution of p_t and p_r , defined by

$$p_{t+r} = \int_{-\infty}^{\infty} p_t(x-z) p_r(z) dz \quad (1)$$

(Feller, 1971, p.144)

It readily follows that the Fourier transform of p_{t+r} equals the product of the transforms of p_t and p_r , that is:

$$p_{t+r}^* = p_t^* \cdot p_r^* \quad (2)$$

where * denotes Fourier transform. Equation 2 provides an efficient method for calculating p_{t+r}^* from p_t^* and p_r^* , and hence, by an inverse Fourier transform, for calculating p_{t+r} .

4. CONCLUSIONS

An inspection of the bracketed (more dubious) estimates in Table 3 for the 50-year return value of hourly mean current speed, U_{50} , indicates that the method proposed in this report might be expected to give reasonable results at CONSLEX sites A to E, but further North at F and G (except at F1 and G1 in less than 200m) the method is less satisfactory; the tidal components are here considerably weaker than the residual currents and often these residuals do not appear to be normally distributed.

The highest estimate for U_{50} from the analysis of the CONSLEX data is 133 cm/s for mooring E4 at 111m, with a water depth of 1015m. This was where the highest recorded current speed of 117 cm/s was obtained. Fig. 3 (E4, 111m) shows apparently anomalous residuals along-slope, towards the North East approaching 100 cm/s, which convolve with the along-slope tidal stream exceeding 30 cm/s. The origin of these anomalous residuals, perhaps associated with the oceanic front separating deep and coastal waters, requires further investigation.

Nearby at E3 at 725m, the estimated value of U_{50} is 94 cm/s while the maximum recorded current speed was 100 cm/s; the greatest recorded residual happened to occur within a few hours of the maximum recorded tide.

At the deep water site of I2, which is off the slope in a depth of 1463m, the method does not give satisfactory estimates of U_{50} at the two current meters below 1000m because the tidal components are small compared to the residuals. The method appears to be reasonable at shallower depths.

2.2 50-year return value of resolved speed

Defining the 50-year return value of hourly mean speed, U_{50} , as that which is exceeded on average once in 50 years, then it is given by

$$\text{Prob}(U_{50} < U) = 1 - 1/(365.25 \times 24 \times 50)$$

i.e.

$$\text{Prob}(U_{50} < U) \approx 0.99999772 \quad (3)$$

Hence U_{50} may be calculated given the distribution p_{t+r} - or rather two values, one from each tail of p_{t+r} , giving the 50-year speed in opposite directions.

With the definition for U_{50} , in terms of only the average interval between exceedances, its value is not affected by any correlation between the data. However, given positive correlation between successive hourly mean values, exceedances of U_{50} will tend to come together, while maintaining the average interval between exceedances of 50 years. So if the 50-year return value is defined as that which is exceeded at least once during one year in 50, then it would have a slightly lower value than that given by (3). However, Pugh and Vassie (1980) examined the effect of correlation upon estimates of return values of surface elevation and decided that any such reduction would in practice be insignificant.

2.3 Probability distribution and extreme value of total speed

Suppose U and V are current speeds resolved orthogonally so that total speed W is given by

$$W = \sqrt{U^2 + V^2}$$

Then, the distributions of U and V can be estimated from data as described above. In theory the distributions of U^2 and V^2 can then be estimated and convolved to give the distribution of W^2 and hence of W (assuming U^2 and V^2 are independent). However, the sizes of the arrays to accommodate the histograms for the distributions of U^2 and V^2 are too large for practical FFT procedures. So we estimate the distribution of W using the numerical approximation for

$$\text{Prob}(W < w) = \iint \sqrt{U^2 + V^2} p(U, V) dU dV$$

where integration is over all U, V such that $0 < \sqrt{U^2 + V^2} < w$ and $p(U, V)$ is the joint probability distribution of U and V .

i.e. $\text{Prob}(W < w) \approx \sum_{i,j} w_{ij} p(U_i, V_j) \delta U \delta V \quad (4)$

where δU and δV are the bin sizes of the histogram representation of the distributions of U and V and summation is over all bins (i, j) such that $w_{ij} < w$ where w_{ij} is the speed at the mid-point of the (i, j) bin. Assuming U and V are independent, then

$$p(U_i, V_j) \delta U \delta V = \text{Prob}(U_i < U < U_{i+1}) \text{Prob}(V_j < V < V_{j+1}) \quad (5)$$

The 50-year return value of W , W_{50} , is given by

$$\text{Prob}(W_{50} < w) \approx 0.99999772 \quad (6)$$

An alternative method for obtaining the distribution of W was considered: histograms for the distributions of the tidal and residual components of W , W_t and W_r , could be obtained, where

$$W = W_t + W_r$$

and these histograms convolved to obtain the distribution of W . But this method fails because W_t and W_r are not independent - since W cannot be negative.

3. APPLICATION TO THE CONSLEX DATA

3.1 General description of the data sets

The method of analysis described above was applied to the CONSLEX data set of hourly mean current speeds associated with 'spot' measurements of direction. The data were obtained from the IOS Marine Information and Advisory Service data base, including the results of tidal analysis carried out at IOS (Bidston).

The CONSLEX data consists of 53 sets of recordings made by DAFS, IOS and SMBA from 20 moorings, using Anderaa current meters deployed between 23 August 1982 and 31 April 1983 - measurements at one site (I2) extended into May 1983. The sites of these moorings and the notation identifying them are shown in Fig. 1 together with the approximate orientation, θ , of the maximum variance of current velocity.

This orientation was calculated for each meter by a principal component analysis of the current velocity. In general it was found to lie along the slope; the flow seems to be constrained by topography. The direction of the line of maximum variance is not specified by this analysis. The direction arrows shown in Fig. 1 were specified in order to fix the co-ordinate system. The variation in θ between meters at any one mooring was generally within $\pm 10^\circ$, and an average direction is shown in Fig. 1. Where the spread was greater than $\pm 10^\circ$, the range of θ is shown. The 'cross-slope' axis was taken as positive to the right of the along-slope, ie. up-slope. The data were analysed in a co-ordinate system defined by

the value of θ for the individual meter - thus ensuring zero correlation between resolved current speeds - but directions are referred to as 'along-slope' and 'up-slope'. Further details, including the depth of each instrument and the values of θ , are given in Table 2.

Site I2 is not on the slope, but in the Rockall Trough with a water depth of 1463m. Section D is on the Wyville-Thomson Ridge; currents at D5 in particular appear unlike those on the slope, as indicated by the wide range of θ with depth - similar to that at I2.

Records from the current meter at G4 at 496m cover only 34 days, and at B1 (130m) only 58 days. The other meter at B1 and both meters at B2 had to be replaced during October 1982 - with the loss of some days of records at B2.

3.2 Maximum observed current speeds

The maximum mean hourly current speed recorded by each instrument and associated direction are included in Table 2.

The maximum recorded hourly mean current speed was 117 cm/s at E4 at a depth of 111m. The only other measurement exceeding 100 cm/s was at G2 at 151m. Generally the maximum speeds at each mooring tended to decrease with increasing meter depth; an exception was at E3 where 100 cm/s was recorded at 725m. The direction of the maximum speed was usually within about 20° of the direction given by the principal component analysis; a notable exception was that of 66 cm/s at E4 at 950m which was 79° away (down-slope).

3.3 Probability distributions of current speeds and estimates of return values

Using the data from each meter, except B1 (130m) and G4 (496m) with less than two months data, histograms showing the distribution of tidal and residual current speeds along-slope and up-slope were constructed with a bin size of 1 cm/s, or 2 cm/s if a component speed exceeded 100 cm/s. These histograms, together with their convolution are shown in the set of figures: Fig. 2. (Strictly, the histograms should be drawn as step functions, but joining mid-points of the bin values gives a clearer picture.)

Fig. 2 shows that the along-slope flow is generally considerably stronger than the up-slope. It also shows that the residual current is usually stronger than the tidal component - but not, for example, at A1 (145m) and at D1 and D2. Sometimes the residual is very much stronger than the tidal component particularly for the up-slope flow, and the convolution is then a smoothed version of the residual histogram, so the tails of the convolution are dominated by the few calculated extreme residual values, eg. F3 at 388m. In these cases it seems preferable to fit a distribution to the residual histogram and to convolve this distribution with the tidal histogram. The set of figures, Fig. 3, show the Gaussian and Laplacian fits to the cumulative distribution of residual components - scaled such that the Gaussian distribution is linear. Generally the Gaussian distribution appears to be a reasonable fit to the residuals; occasionally the observations in the tails deviate from the straight line, but these are determined by only a few values so their sampling variance is high. Construction of confidence limits would require an analysis of the

correlation structure of the data; but where the data approaches the long-tailed Laplace distribution the use of the Gaussian distribution must be expected to underestimate extreme values.

The fifty-year return values of current speed up- and down-slope and in both directions along-slope were estimated using equation 3 and the convolutions with the residual histograms and the Gaussian fit. Results are shown in Table 3.

Values are given to the nearest bin size, that is ± 2 cm/s for the higher values and ± 1 cm/s for the lower.

Note that the fifty-year return values are given by interpolation of the convolution. No extrapolation is required.

The convolution only gives the distribution of the sum of the tidal and residual components if these components are independent. There is no entirely satisfactory method for testing independence, but examples of the joint distributions of the tide and residual components plotted in the set: Fig. 4 show no obvious dependence. On physical grounds, one might expect negative correlation between tide and residual in shallow water or at current meters close to the sea bed, but none is apparent in Fig. 4, or in other joint distributions which we examined. If there were negative correlation then the convolution would overestimate the fifty-year return values.

Table 3 also includes fifty-year return values of total speed, U_{50} , calculated from equations (4)-(6), and the maximum observed speeds from

Table 2. The choice of θ from the principal component analysis ensures no correlation between the measured 'up-slope' and 'along-slope' speeds. The requirement of (5) is stronger, requiring independence between the two distributions, but this seems a not-unreasonable assumption.

The values for U_{50} from the residual histogram are given in brackets if Fig. 2 suggests that the dominant tail of the component convolution has a negligible tidal contribution. The value of U_{50} from the Gaussian fit is in brackets if Fig. 3 indicates that the dominant residual component is not Gaussian.

4. CONCLUSIONS

An inspection of the bracketed (more dubious) estimates in Table 3 for the 50-year return value of hourly mean current speed, U_{50} , indicates that the method proposed in this report might be expected to give reasonable results at CONSLEX sites A to E, but further North at F and G (except at F1 and G1 in less than 200m) the method is less satisfactory; the tidal components are here considerably weaker than the residual currents and often these residuals do not appear to be normally distributed.

The highest estimate for U_{50} from the analysis of the CONSLEX data is 133 cm/s for mooring E4 at 111m, with a water depth of 1015m. This was where the highest recorded current speed of 117 cm/s was obtained. Fig. 3 (E4, 111m) shows apparently anomalous residuals along-slope, towards the North East approaching 100 cm/s, which convolve with the along-slope tidal stream exceeding 30 cm/s. The origin of these anomalous residuals, perhaps associated with the oceanic front separating deep and coastal waters, requires further investigation.

Nearby at E3 at 725m, the estimated value of U_{50} is 94 cm/s while the maximum recorded current speed was 100 cm/s; the greatest recorded residual happened to occur within a few hours of the maximum recorded tide.

At the deep water site of I2, which is off the slope in a depth of 1463m, the method does not give satisfactory estimates of U_{50} at the two current meters below 1000m because the tidal components are small compared to the residuals. The method appears to be reasonable at shallower depths.

However, because of our lack of knowledge of all the mechanisms producing extreme currents at sites off the continental shelf including their within-year variability, estimates of the 50-year return value of current speed made from data recorded over only a few months must be viewed with caution. Even where the method suggested in this report appears to be satisfactory, further data are needed to confirm its applicability and to put confidence limits upon the results.

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Table 1: CONSLEX mooring sites

| Mooring | Latitude (N) | Longitude | Water depth (m) |
|---------|--------------|-----------|-----------------|
| A1 | 57° 20.7' | 9° 07.2'W | 145 |
| A5 | 57° 18.6' | 9° 40.4'W | 1614 |
| B1 | 57° 56.3' | 8° 51.0'W | 155 |
| B2 | 58° 00.7' | 9° 07.7'W | 193 |
| B3 | 58° 06.5' | 9° 33.1'W | 504 |
| B4 | 58° 08.3' | 9° 41.2'W | 1082 |
| C2 | 59° 05.4' | 7° 27.0'W | 514 |
| C3 | 59° 08.5' | 7° 42.4'W | 998 |
| D1 | 59° 39.8' | 6° 02.5'W | 237 |
| D2 | 59° 46.7' | 6° 10.8'W | 370 |
| D5 | 60° 09.9' | 7° 44.5'W | 637 |
| E2 | 60° 13.3' | 4° 31.8'W | 478 |
| E3 | 60° 31.2' | 4° 56.8'W | 1035 |
| E4 | 60° 46.4' | 4° 49.4'W | 1015 |
| F1 | 61° 09.3' | 1° 31.7'W | 189 |
| F3 | 61° 24.8' | 2° 06.1'W | 995 |
| G1 | 61° 30.7' | 0° 02.5'E | 191 |
| G2 | 62° 06.1' | 0° 03.9'E | 550 |
| G4 | 63° 08.8' | 0° 00.9'W | 1611 |
| I2 | 60° 12.7' | 9° 13.3'W | 1463 |

Table 2: CONSLEX current meter records

| Mooring | meter | days of | max. recorded hr mean vely. | dir^n princ. |
|---------|-----------|---------|---|------------------------------|
| | depth (m) | records | speed (cm/s) dir^n towards (° from N) | component (θ°) |
| A1 | 55 | 106 | 59 | 031 046 |
| | 120 | 181 | 44 | 307 042 |
| A5 | 209 | 179 | 57 | 347 333 |
| | 510 | 179 | 45 | 340 333 |
| | 1111 | 179 | 49 | 186 343 |
| | 1562 | 179 | 33 | 339 341 |
| B1 | 55 | 173 | 70 | 033 032 |
| | 130 | 58 | 61 | 194 031 |
| B2 | 43 | 120 | 53 | 023 036 |
| | 168 | 120 | 47 | 033 033 |
| B3 | 104 | 172 | 63 | 035 025 |
| | 257 | 172 | 54 | 028 025 |
| | 457 | 169 | 50 | 043 036 |
| B4 | 169 | 172 | 53 | 023 017 |
| | 477 | 172 | 50 | 014 019 |
| | 1035 | 172 | 38 | 184 013 |
| C2 | 115 | 172 | 82 | 043 051 |
| | 266 | 172 | 77 | 050 048 |
| | 468 | 172 | 76 | 037 035 |
| C3 | 104 | 172 | 58 | 199 041 |
| | 403 | 172 | 52 | 049 046 |
| | 951 | 172 | 46 | 027 008 |
| D1 | 87 | 136 | 80 | 054 049 |
| | 212 | 136 | 82 | 227 050 |
| D2 | 120 | 169 | 86 | 078 061 |
| | 270 | 169 | 79 | 074 065 |
| | 345 | 169 | 69 | 057 066 |
| D5 | 510 | 186 | 88 | 208 051 |
| | 633 | 186 | 85 | 194 007 |

Table 2 continued

| Mooring | meter depth (m) | days of records | max. recorded hr speed (cm/s) | mean vely. dir ⁿ towards (° from N) | dir ⁿ princ. component (θ°) |
|---------|--------------------|--------------------|----------------------------------|--|---|
| E2 | 453 | 162 | 77 | 033 | 047 |
| E3 | 120 | 164 | 95 | 92 | 063 |
| | 419 | 164 | 83 | 027 | 052 |
| | 725 | 164 | 100 | 212 | 055 |
| E4 | 111 | 184 | 117 | 063 | 053 |
| | 950 | 181 | 66 | 158 | 057 |
| F1 | 39 | 163 | 88 | 076 | 081 |
| F3 | 79 | 80 | 89 | 084 | 063 |
| | 388 | 161 | 66 | 046 | 035 |
| | 694 | 161 | 60 | 244 | 049 |
| | 945 | 161 | 66 | 030 | 044 |
| G1 | 41 | 117 | 48 | 133 | 108 |
| | 166 | 117 | 33 | 117 | 107 |
| G2 | 151 | 162 | 114 | 073 | 073 |
| | 299 | 162 | 89 | 069 | 062 |
| | 500 | 162 | 84 | 106 | 079 |
| G4 | 195 | 164 | 64 | 98 | 053 |
| | 496 | 34 | 26 | 021 | 028 |
| | 1104 | 164 | 32 | 212 | 051 |
| | 1554 | 164 | 34 | 206 | 044 |
| I2 | 251 | 216 | 60 | 331 | 022 |
| | 654 | 222 | 45 | 106 | 038 |
| | 1055 | 216 | 67 | 182 | 020 |
| | 1440 | 222 | 75 | 144 | 343 |

Table 3: Estimates of 50-year current speeds (cm/s)

| Mooring | meter depth (m) | Residual Histogram | | | | | | Gaussian fit | | | | | | MAX. OBS. SPEED |
|---------|-----------------------|--------------------|-----|----------|----|----------------|-------------|--------------|----------|----|----------------|----|--|-----------------------|
| | | Along-slope | | up-slope | | TOTAL SPEED | Along-slope | | up-slope | | TOTAL SPEED | | | |
| | | + | - | + | - | | + | - | + | - | | | | |
| A1 | 55 | 65 | 66 | 51 | 58 | 69 | 62 | 60 | 53 | 54 | 66 | 59 | | |
| | 120 | 52 | 50 | 44 | 47 | 55 | 49 | 51 | 45 | 46 | 54 | 44 | | |
| A5 | 209 | 58 | 43 | 47 | 29 | (63) | 75 | 55 | 42 | 36 | 75 | 57 | | |
| | 510 | 47 | 32 | 36 | 23 | (50) | 63 | 46 | 34 | 29 | 63 | 45 | | |
| | 1111 | 46 | 50 | 29 | 27 | 50 | 52 | 46 | 28 | 28 | (52) | 49 | | |
| | 1562 | 39 | 33 | 27 | 29 | (40) | 42 | 37 | 27 | 29 | 42 | 33 | | |
| | | | | | | | | | | | | | | |
| B1 | 55 | 95 | 75 | 54 | 47 | 96 | 99 | 83 | 45 | 43 | 101 | 70 | | |
| B2 | 43 | 79 | 69 | 56 | 45 | 81 | 81 | 79 | 55 | 51 | 83 | 53 | | |
| | 168 | 63 | 54 | 34 | 27 | 63 | 60 | 52 | 29 | 30 | 60 | 47 | | |
| B3 | 104 | 73 | 41 | 32 | 37 | 74 | 77 | 48 | 33 | 36 | 77 | 63 | | |
| | 257 | 59 | 33 | 21 | 28 | 59 | 64 | 38 | 25 | 29 | 65 | 54 | | |
| | 457 | 57 | 36 | 24 | 30 | 58 | 62 | 41 | 25 | 31 | 62 | 50 | | |
| | 169 | 64 | 48 | 38 | 31 | 65 | 70 | 53 | 32 | 33 | 70 | 53 | | |
| B4 | 477 | 59 | 38 | 26 | 28 | 60 | 62 | 50 | 22 | 24 | 62 | 50 | | |
| | 1035 | 42 | 44 | 10 | 13 | 44 | 49 | 46 | 10 | 12 | 49 | 38 | | |
| | | | | | | | | | | | | | | |
| C2 | 115 | 97 | 45 | 27 | 45 | 97 | 101 | 45 | 25 | 47 | 101 | 82 | | |
| | 266 | 88 | 38 | 24 | 33 | 89 | 93 | 42 | 20 | 35 | 93 | 77 | | |
| | 468 | 90 | 37 | 31 | 32 | 91 | 81 | 44 | 28 | 33 | (82) | 76 | | |
| C3 | 104 | 67 | 71 | 52 | 35 | 72 | 80 | 62 | 48 | 49 | (80) | 58 | | |
| | 403 | 59 | 51 | 29 | 27 | 60 | 61 | 48 | 33 | 34 | (62) | 52 | | |
| | 951 | 60 | 51 | 41 | 39 | 62 | 63 | 54 | 40 | 39 | 64 | 46 | | |
| D1 | 87 | 95 | 89 | 49 | 45 | 97 | 107 | 91 | 49 | 43 | 107 | 80 | | |
| | 212 | 82 | 94 | 30 | 41 | 94 | 95 | 83 | 31 | 33 | (95) | 82 | | |
| D2 | 120 | 95 | 65 | 57 | 41 | 97 | 99 | 73 | 59 | 43 | 101 | 86 | | |
| | 270 | 95 | 61 | 51 | 39 | 97 | 95 | 73 | 51 | 41 | 97 | 79 | | |
| | 345 | 97 | 65 | 49 | 47 | 99 | 93 | 71 | 49 | 43 | 93 | 69 | | |
| D5 | 510 | 81 | 101 | 57 | 74 | 102 | 83 | 91 | 65 | 69 | (91) | 88 | | |
| | 633 | 65 | 103 | 49 | 75 | (103) | 59 | 102 | 51 | 57 | 102 | 85 | | |

Table 3 continued

| Mooring | meter depth (m) | Residual Histogram | | | | | | Gaussian fit | | | | | | MAX. OBS. SPEED |
|---------|-----------------------|--------------------|----|----------|----|----------------|-------------|--------------|----------|-----|----------------|-----|--|-----------------------|
| | | Along-slope | | up-slope | | TOTAL SPEED | Along-slope | | up-slope | | TOTAL SPEED | | | |
| | | + | - | + | - | | + | - | + | - | | | | |
| E2 | 453 | 87 | 64 | 43 | 46 | 88 | 109 | 63 | 37 | 45 | 109 | 77 | | |
| E3 | 120 | 101 | 84 | 79 | 91 | 113 | 113 | 109 | 99 | 103 | 119 | 95 | | |
| | 419 | 83 | 78 | 51 | 58 | 89 | 87 | 91 | 69 | 71 | 93 | 83 | | |
| | 725 | 58 | 93 | 57 | 37 | 94 | 65 | 78 | 47 | 43 | (78) | 100 | | |
| E4 | 111 | 131 | 95 | 79 | 63 | 133 | 115 | 111 | 93 | 85 | (119) | 117 | | |
| | 950 | 46 | 86 | 77 | 24 | 92 | 60 | 75 | 51 | 39 | (75) | 66 | | |
| F1 | 39 | 97 | 53 | 44 | 61 | 98 | 94 | 64 | 42 | 65 | 96 | 88 | | |
| F3 | 79* | 117 | 51 | 48 | 73 | (121) | 115 | 67 | 63 | 81 | (117) | 89 | | |
| | 388 | 71 | 71 | 38 | 47 | (74) | 90 | 70 | 52 | 52 | 91 | 66 | | |
| | 694 | 73 | 69 | 43 | 43 | (74) | 85 | 111 | 37 | 41 | (111) | 60 | | |
| | 945 | 78 | 64 | 36 | 40 | (78) | 89 | 102 | 35 | 37 | (102) | 66 | | |
| G1 | 41 | 73 | 65 | 57 | 49 | 75 | 71 | 60 | 59 | 56 | 73 | 48 | | |
| | 166 | 50 | 40 | 40 | 33 | 50 | 47 | 40 | 37 | 36 | 47 | 33 | | |
| G2 | 151 | 128 | 29 | 67 | 67 | (129) | 134 | 47 | 61 | 69 | 135 | 114 | | |
| | 299 | 98 | 23 | 53 | 47 | (100) | 127 | 77 | 47 | 47 | (127) | 89 | | |
| | 500 | 81 | 31 | 68 | 52 | (87) | 90 | 46 | 54 | 60 | 92 | 84 | | |
| G4 | 195 | 58 | 44 | 49 | 57 | (71) | 78 | 65 | 59 | 63 | 79 | 64 | | |
| | 1104 | 30 | 31 | 20 | 26 | (35) | 42 | 37 | 31 | 31 | (43) | 32 | | |
| | 1554 | 34 | 35 | 22 | 22 | (37) | 43 | 36 | 31 | 30 | (44) | 34 | | |
| I2 | 251 | 59 | 63 | 103 | 55 | 103 | 61 | 59 | 103 | 51 | 103 | 60 | | |
| | 654 | 46 | 47 | 50 | 41 | 58 | 51 | 48 | 52 | 46 | (56) | 45 | | |
| | 1055 | 35 | 71 | 53 | 41 | (73) | 55 | 71 | 45 | 46 | (71) | 67 | | |
| | 1440 | 69 | 85 | 68 | 49 | (92) | 71 | 86 | 71 | 40 | (89) | 75 | | |

* F3(79m): only 80 days of records.

Fig.1: CONSLEX mooring sites and direction of axis determined by principal component analysis of current records. (A range is shown where directions from each meter on a mooring differed by more than 10° .)



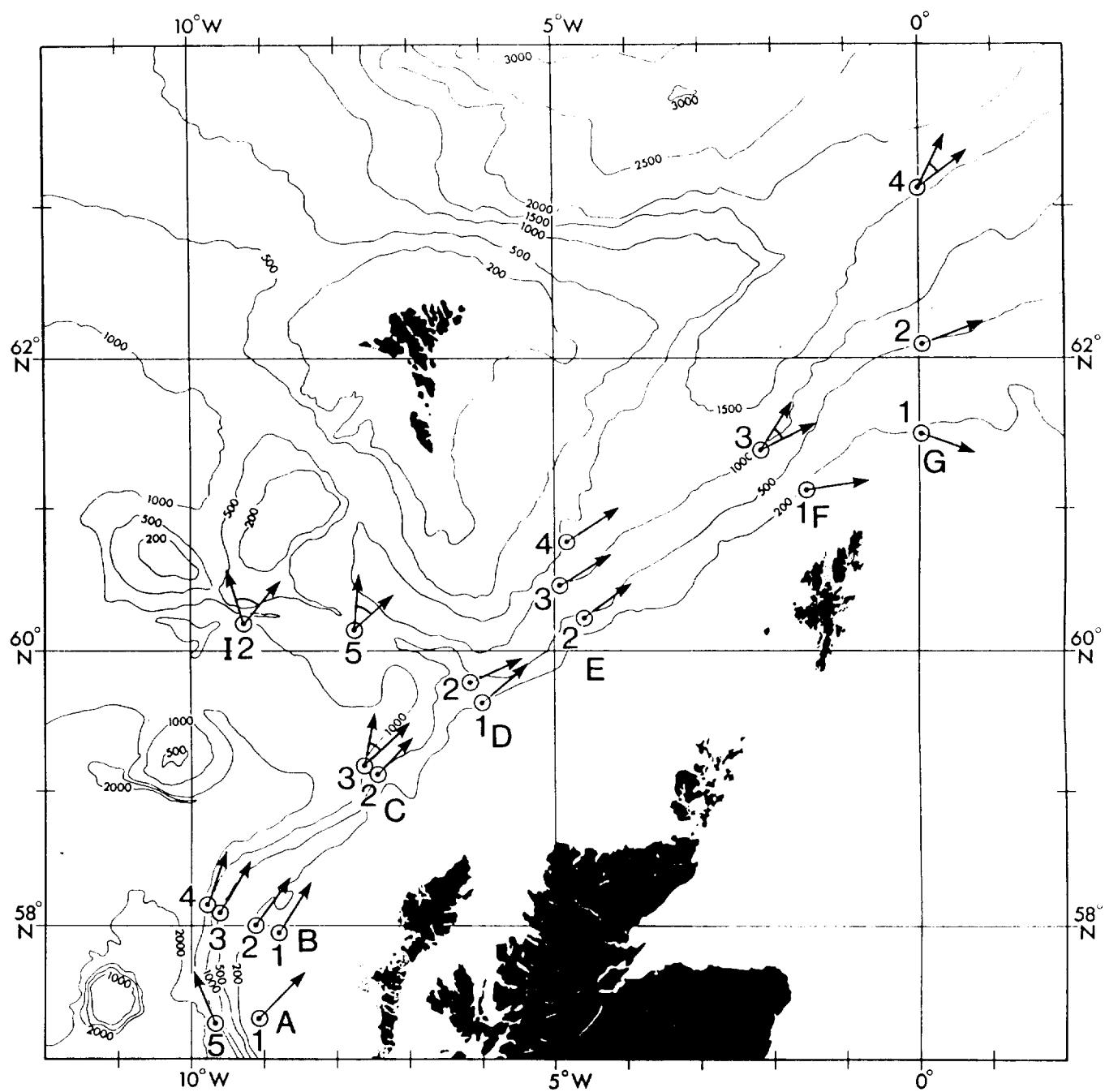
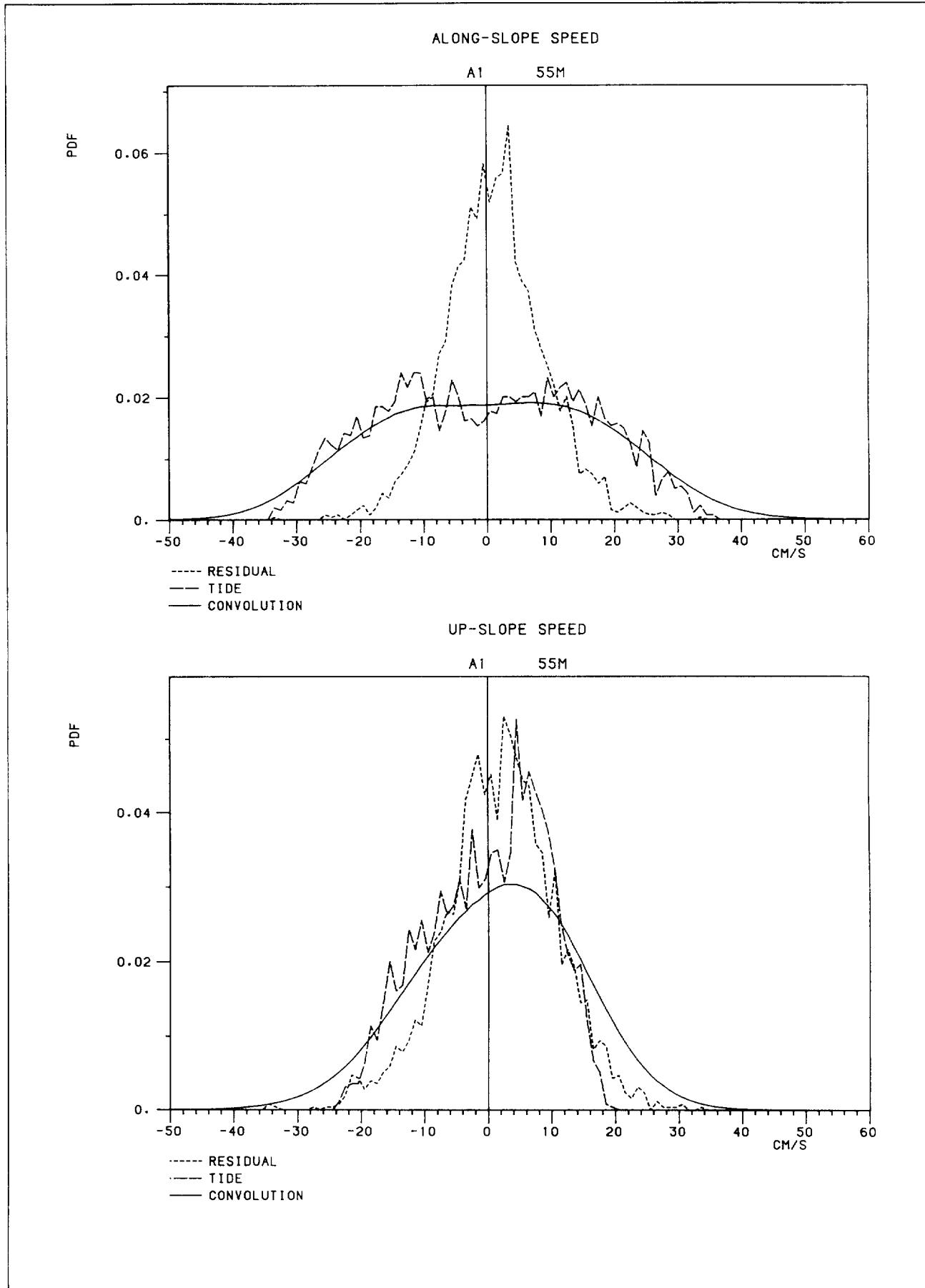
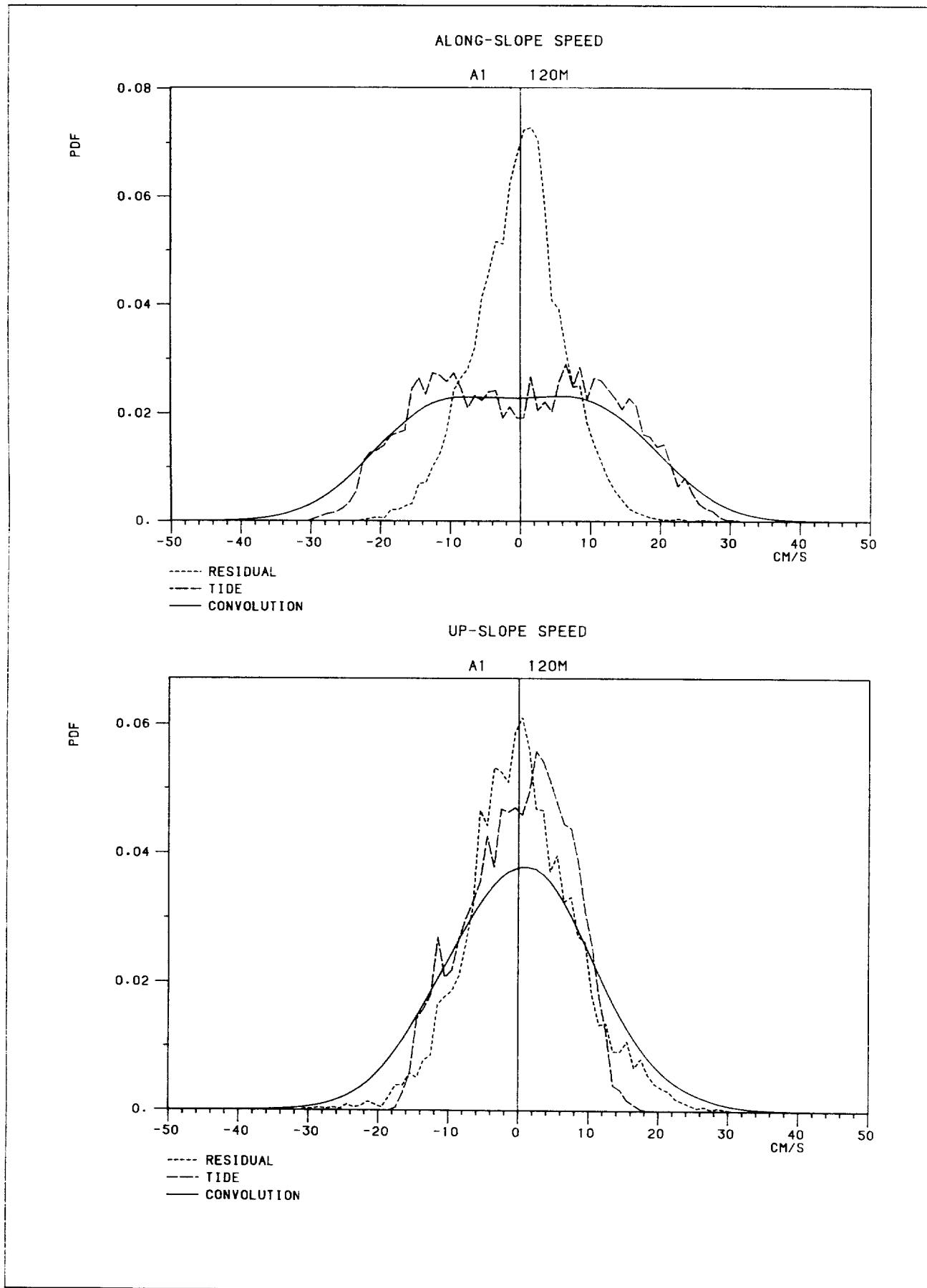
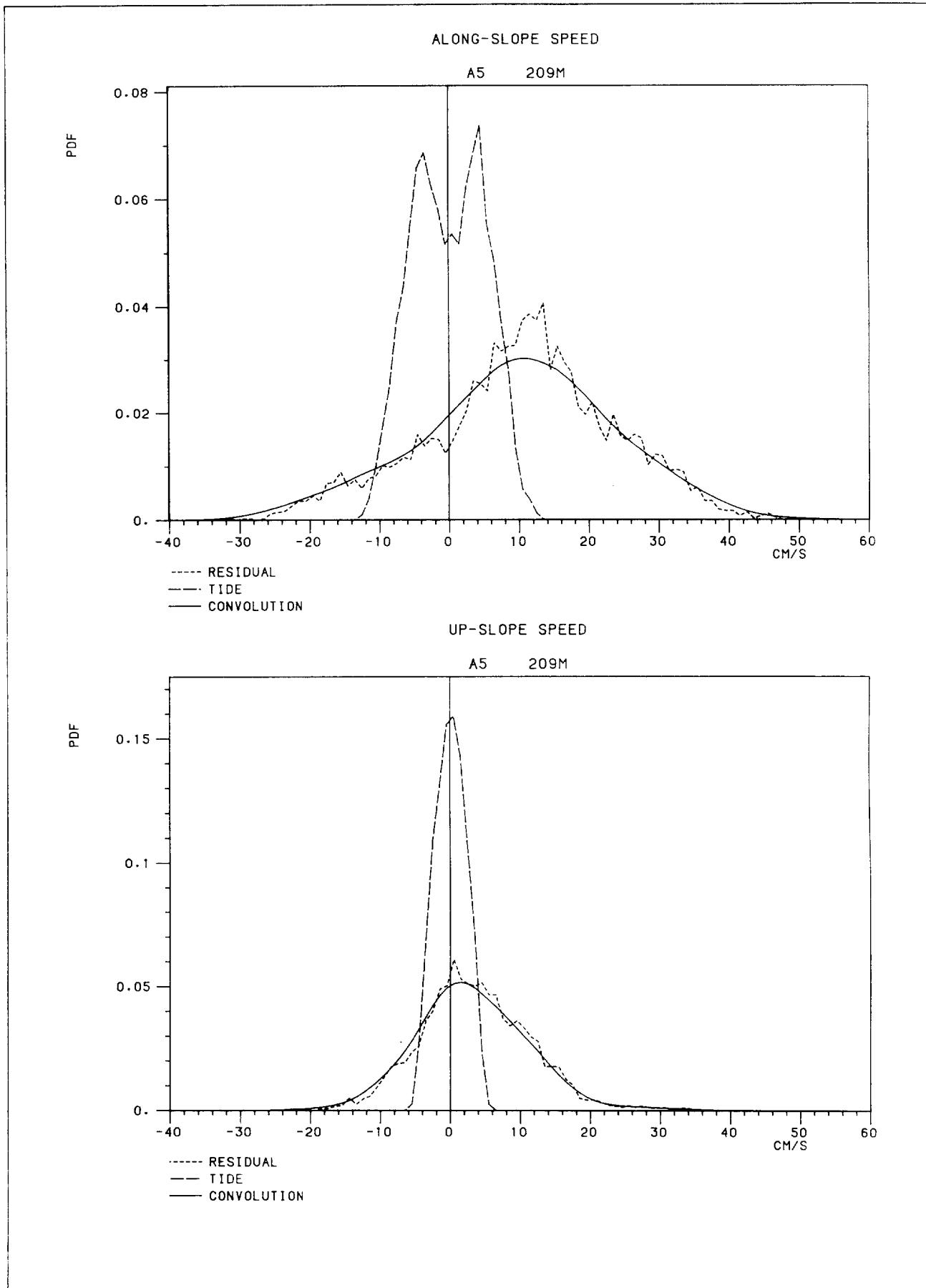


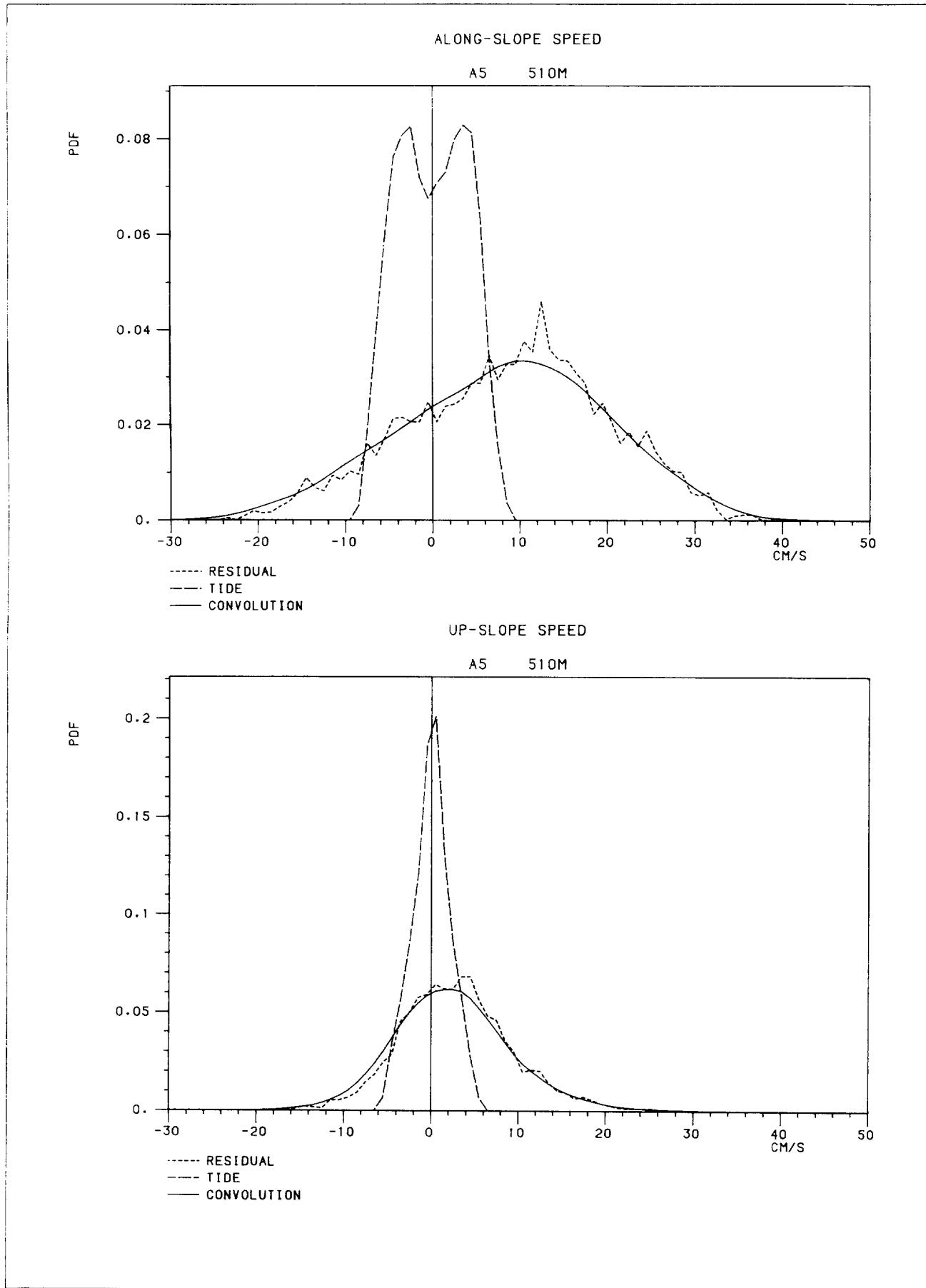
Fig.2: Probability distribution functions of residual and tidal current speeds along- and up-slope from speeds recorded by each current meter and their convolutions. (The meter is identified by the mooring and by the depth of the meter below the sea surface.)

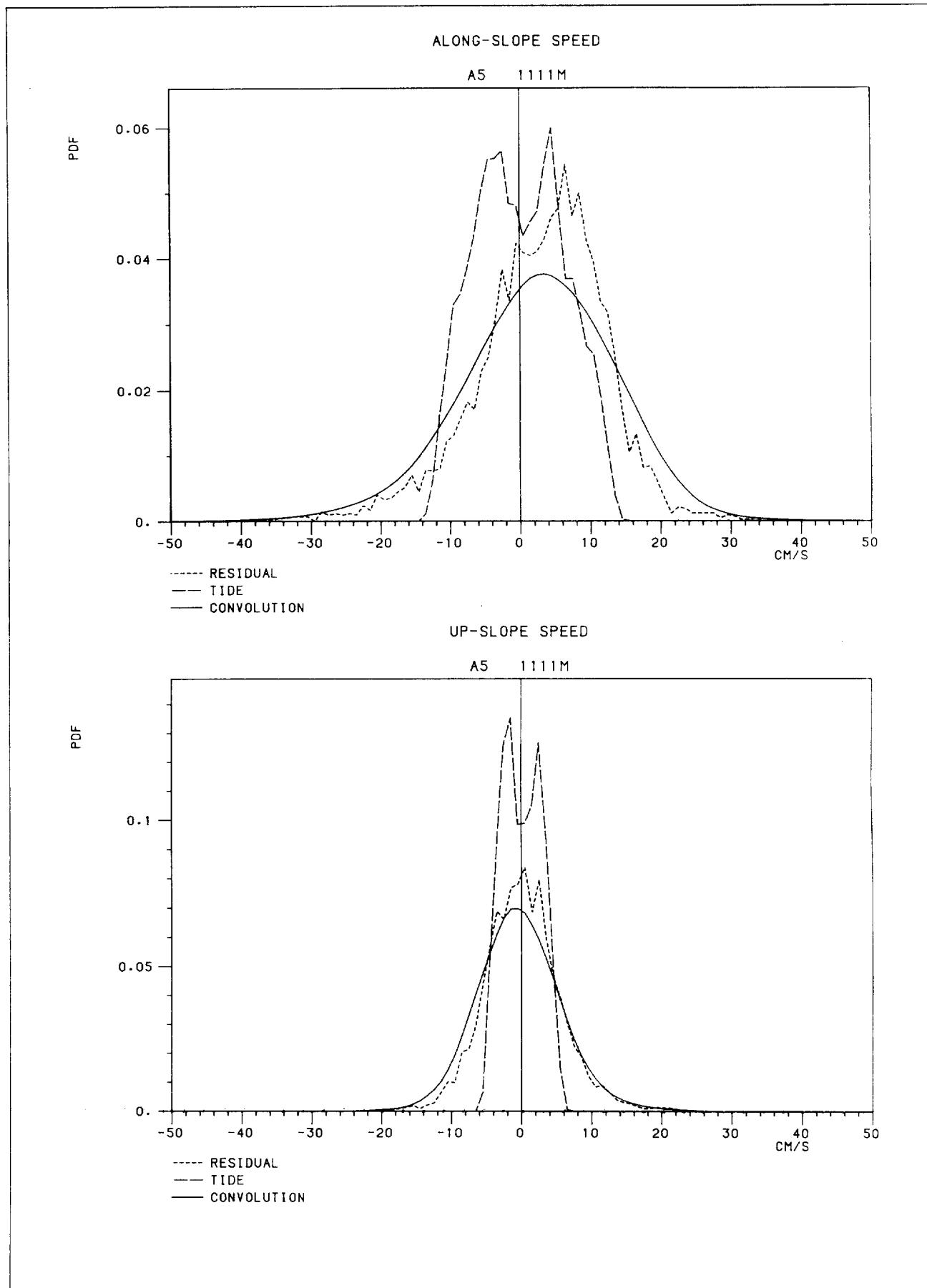


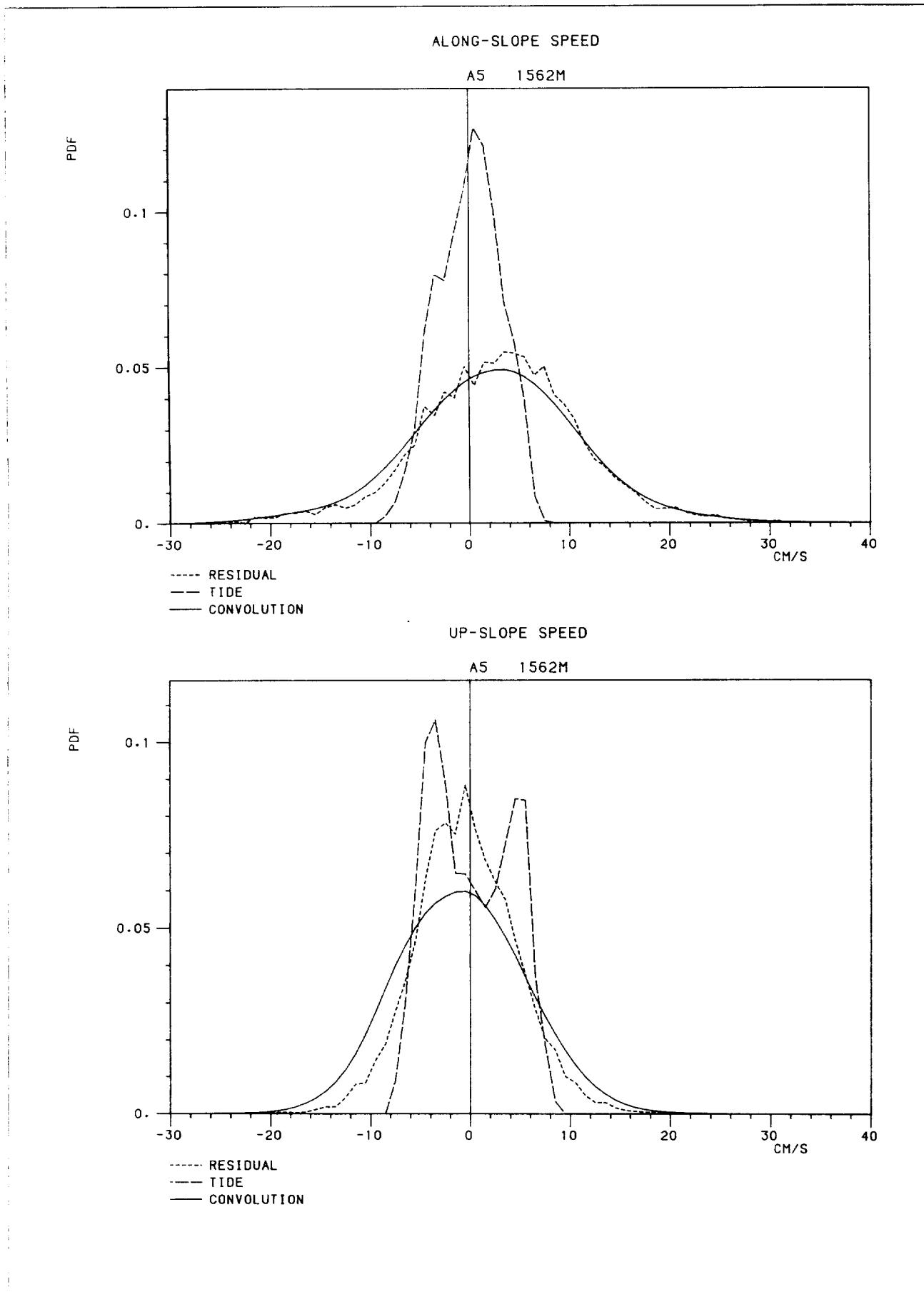


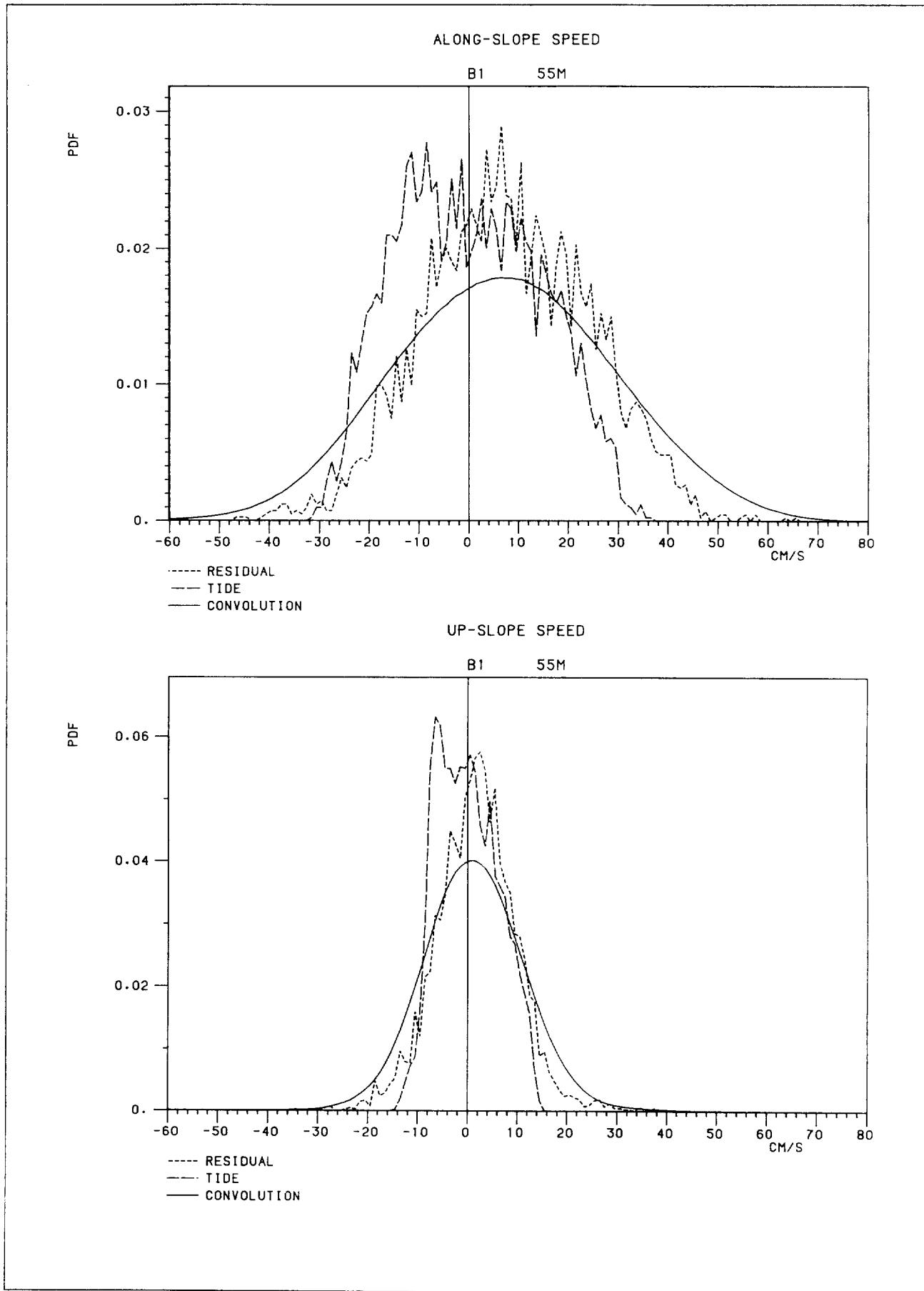


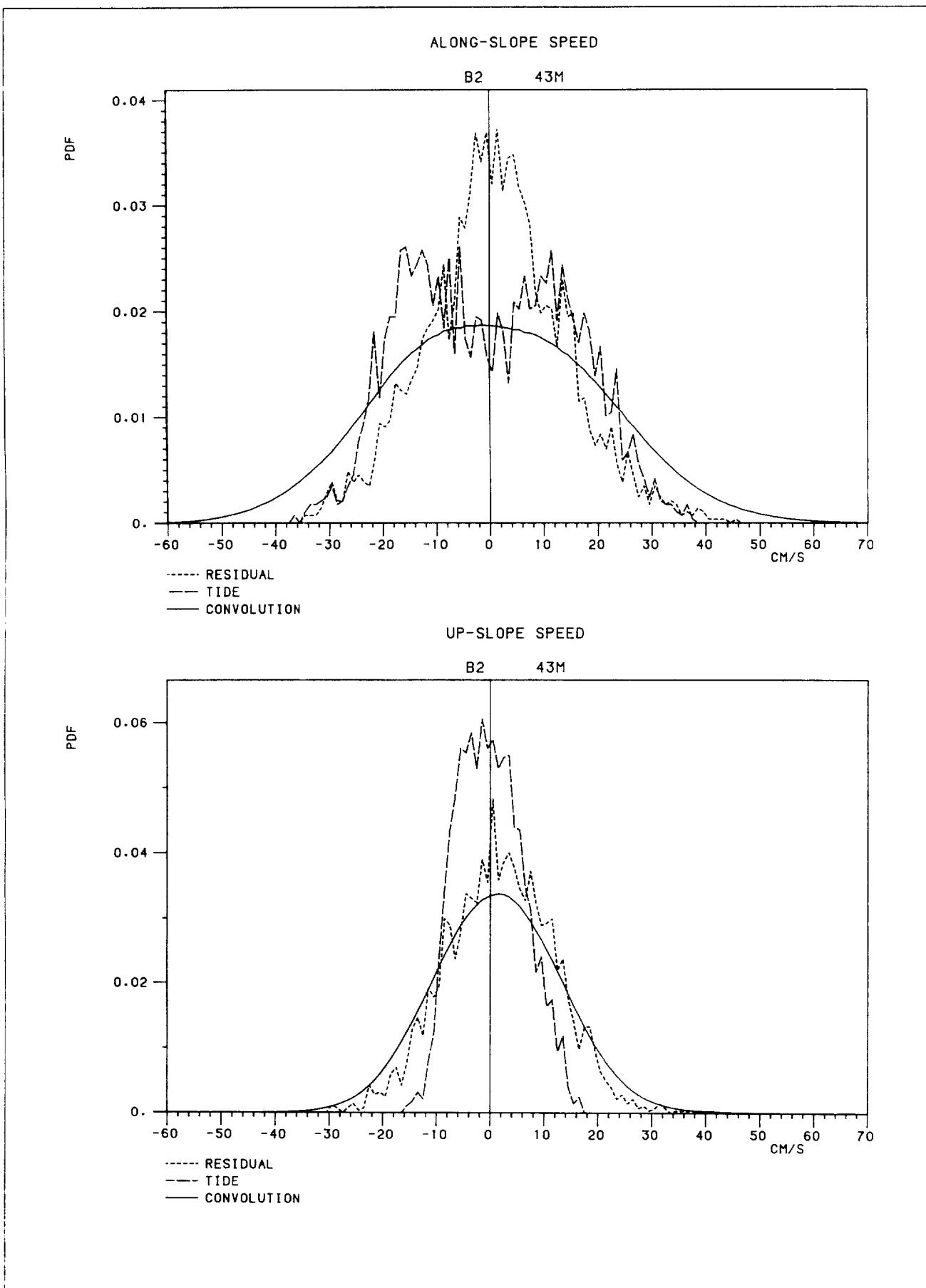


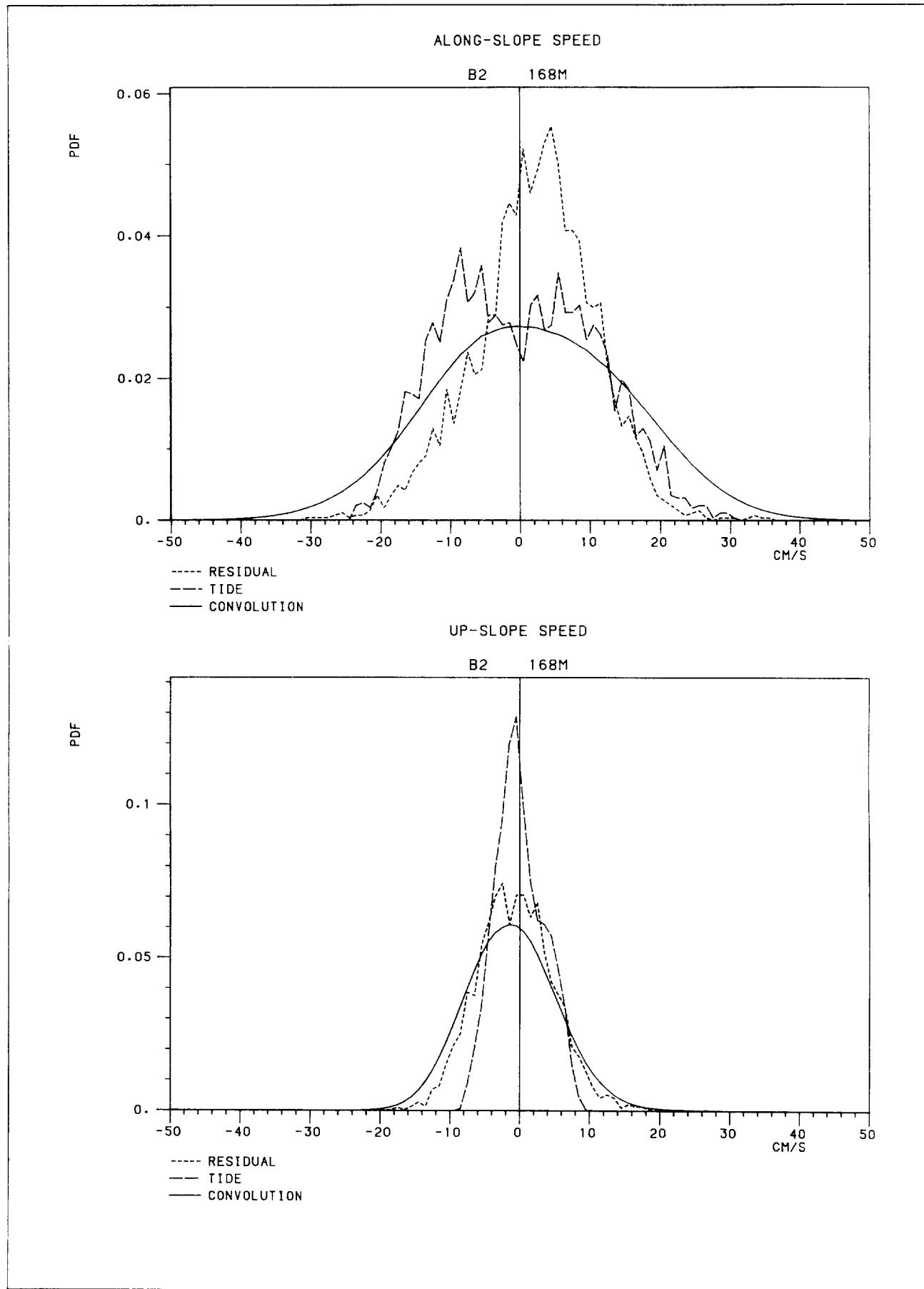


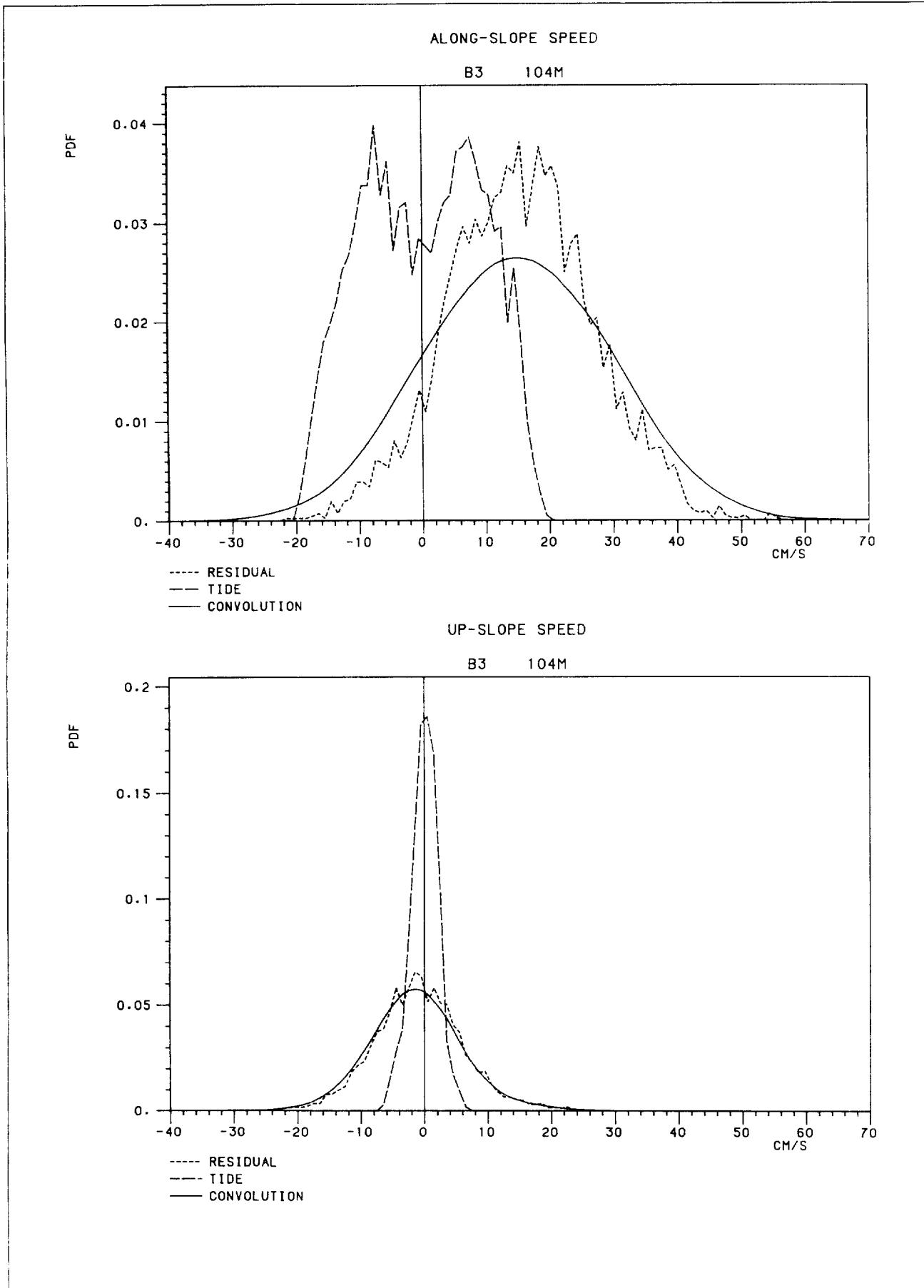


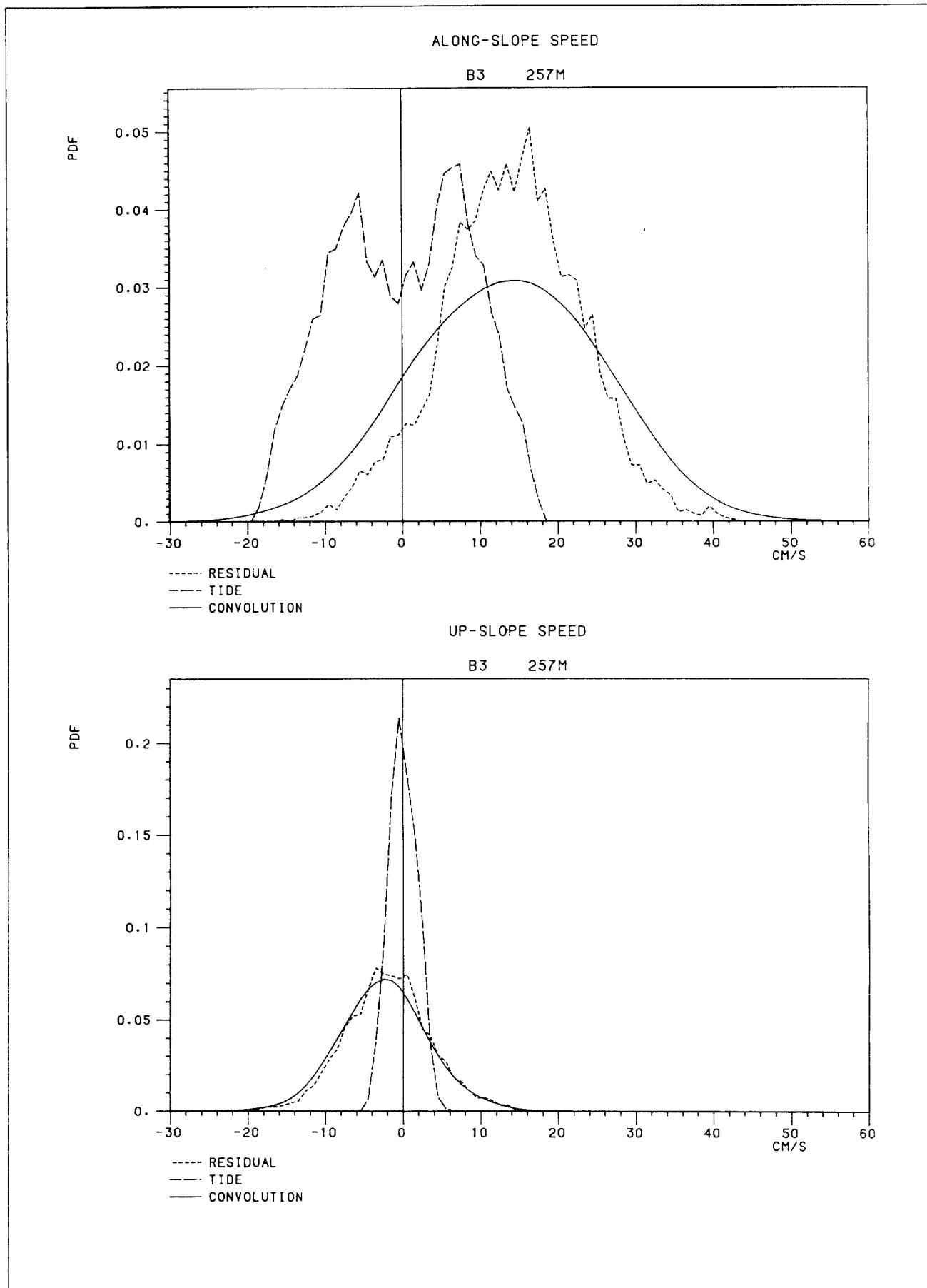


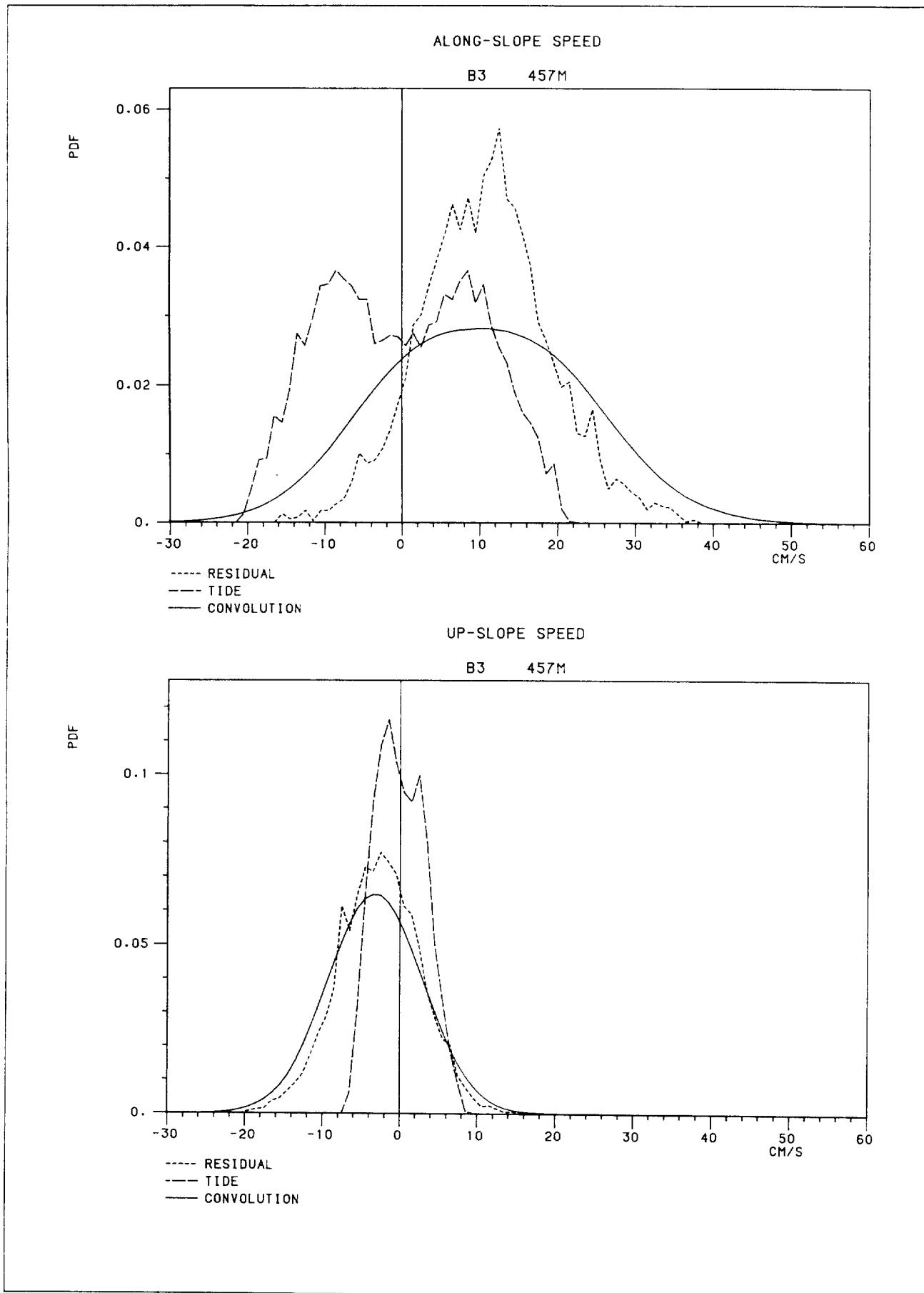


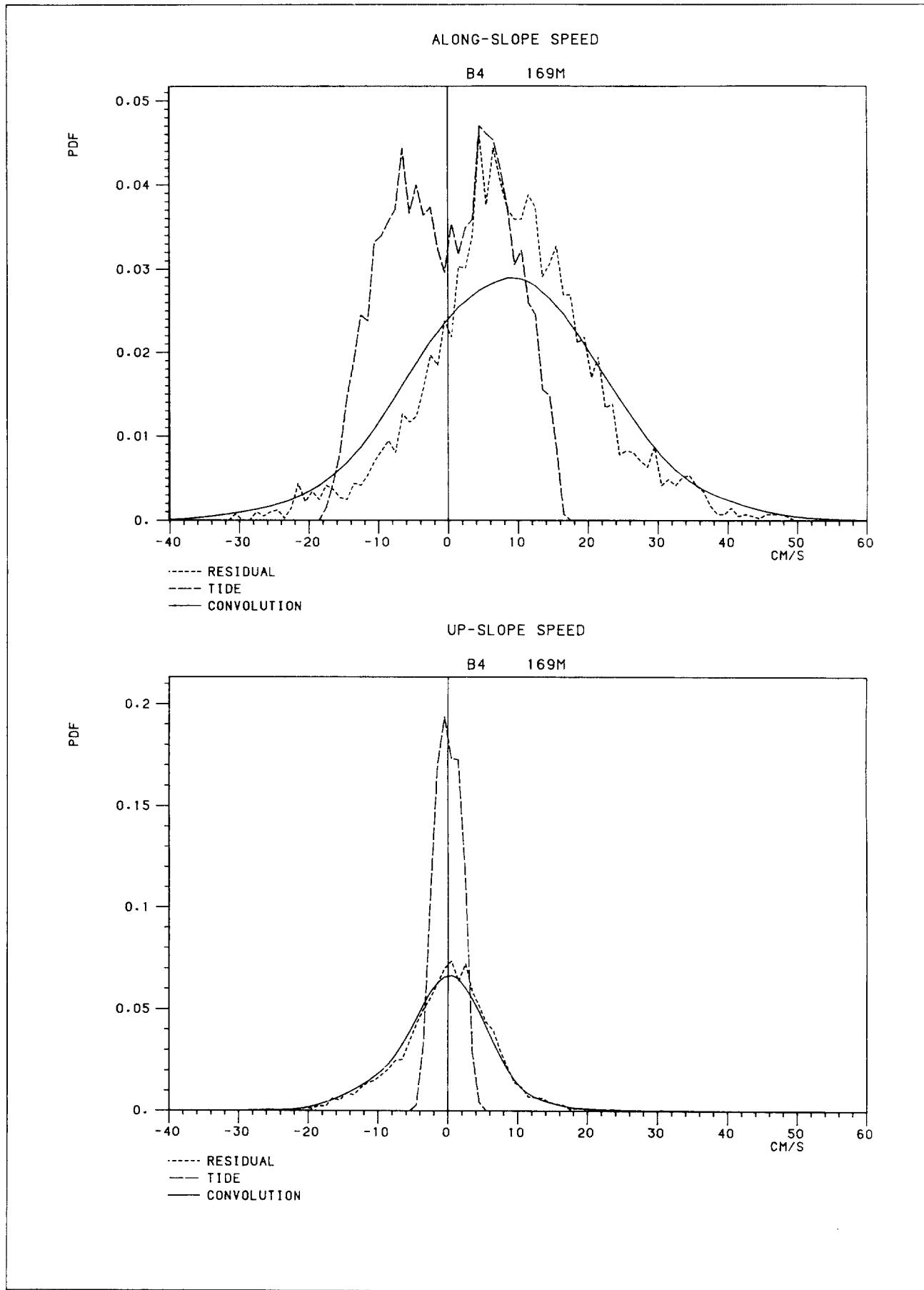


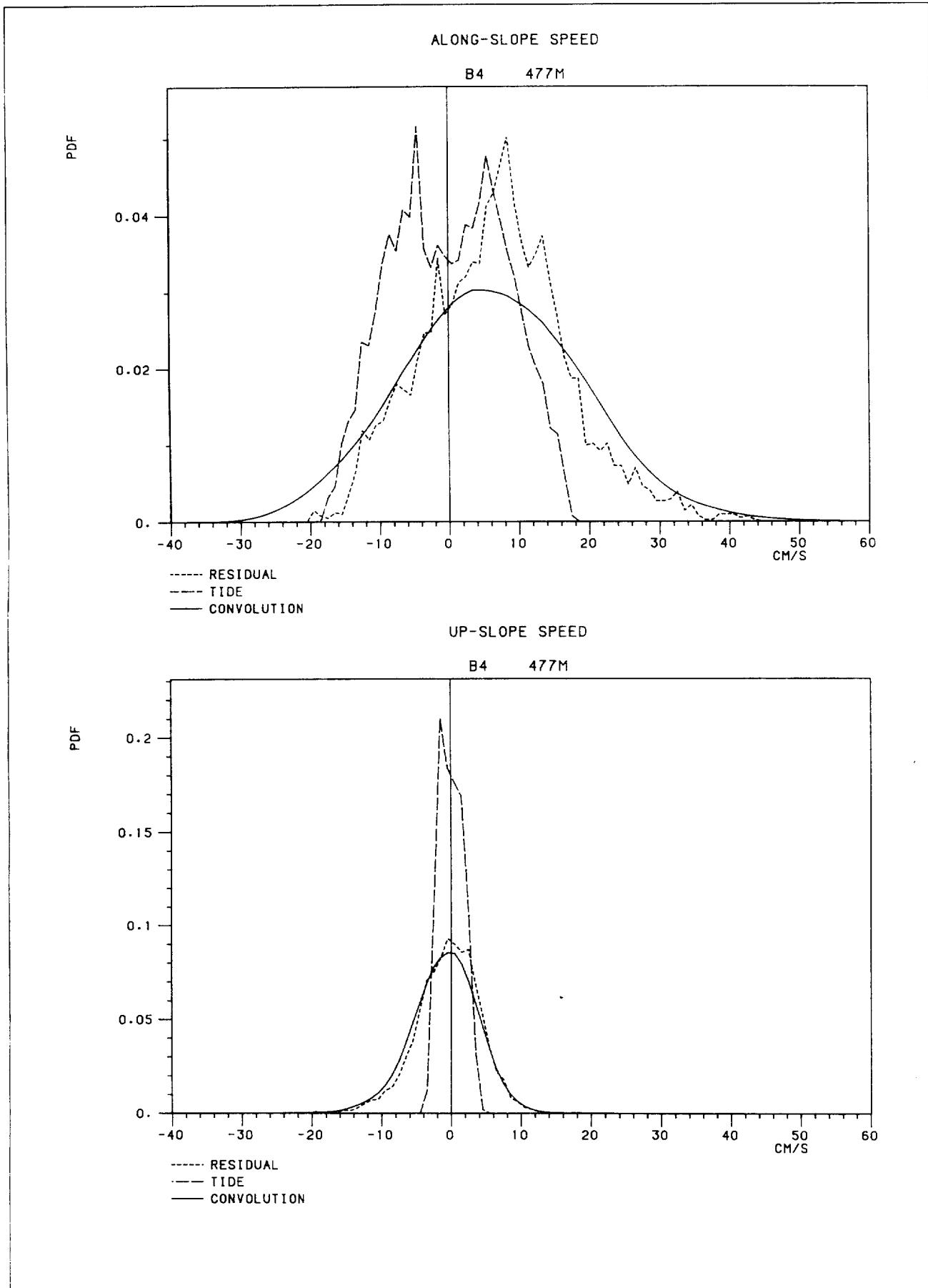


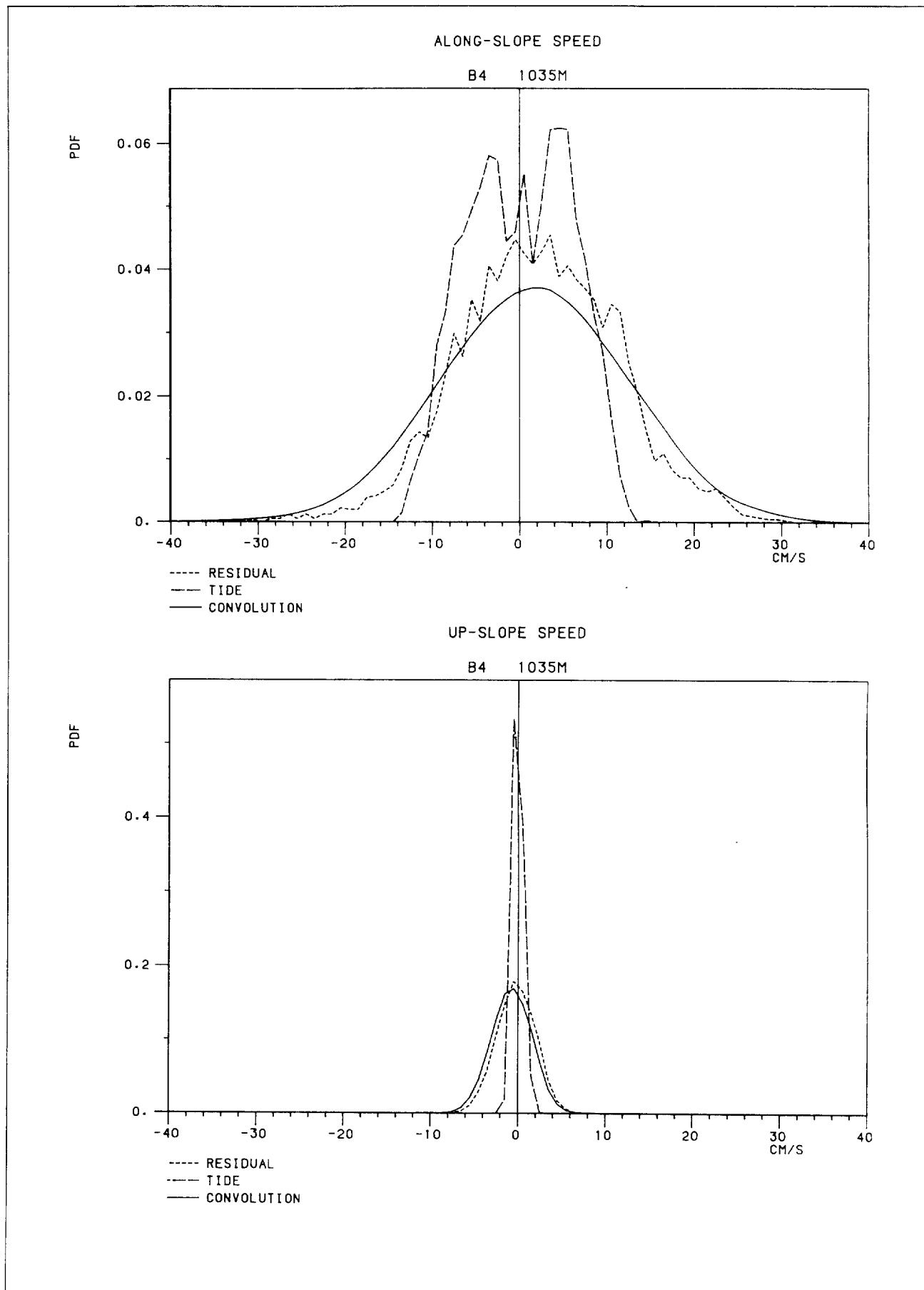


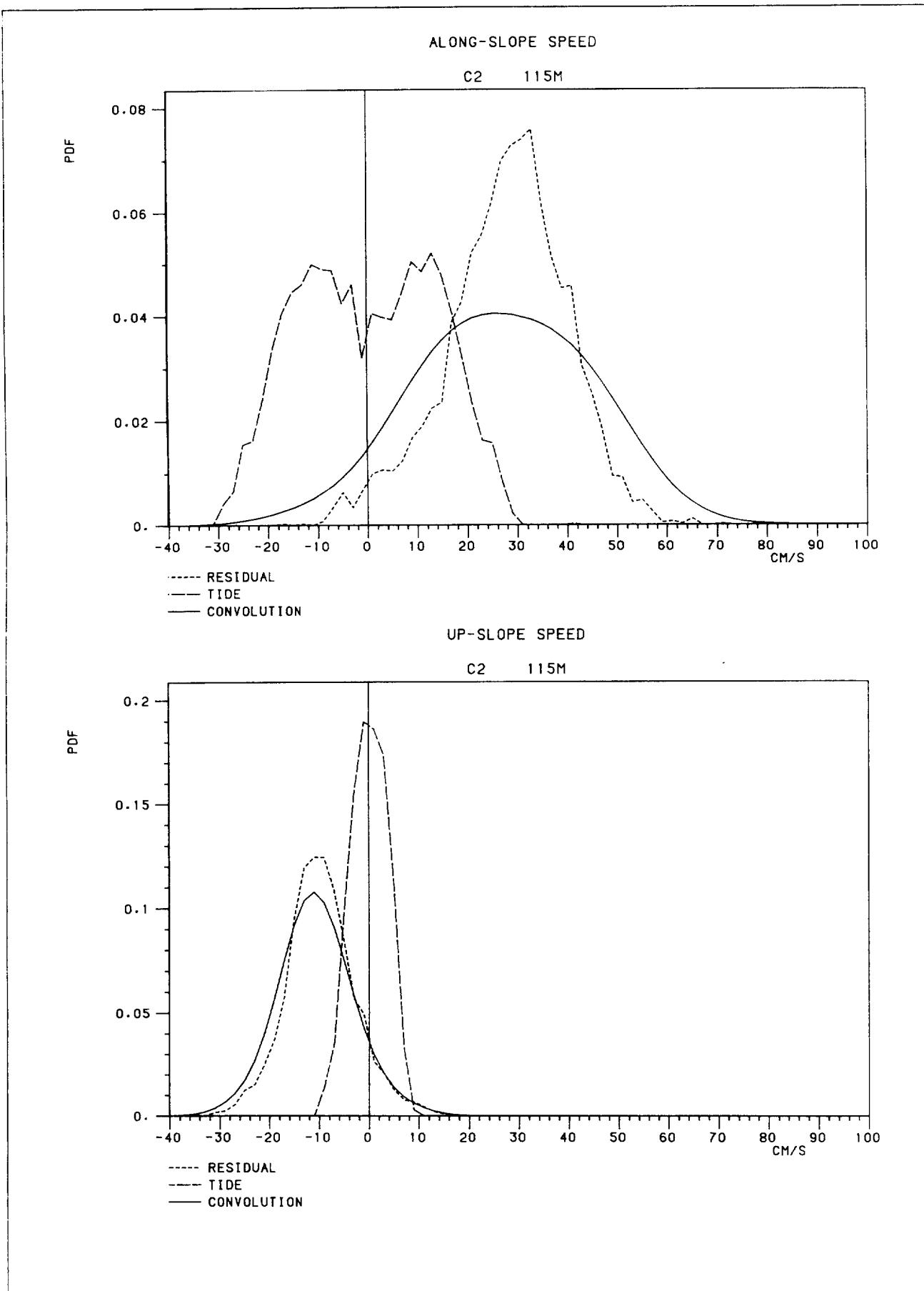


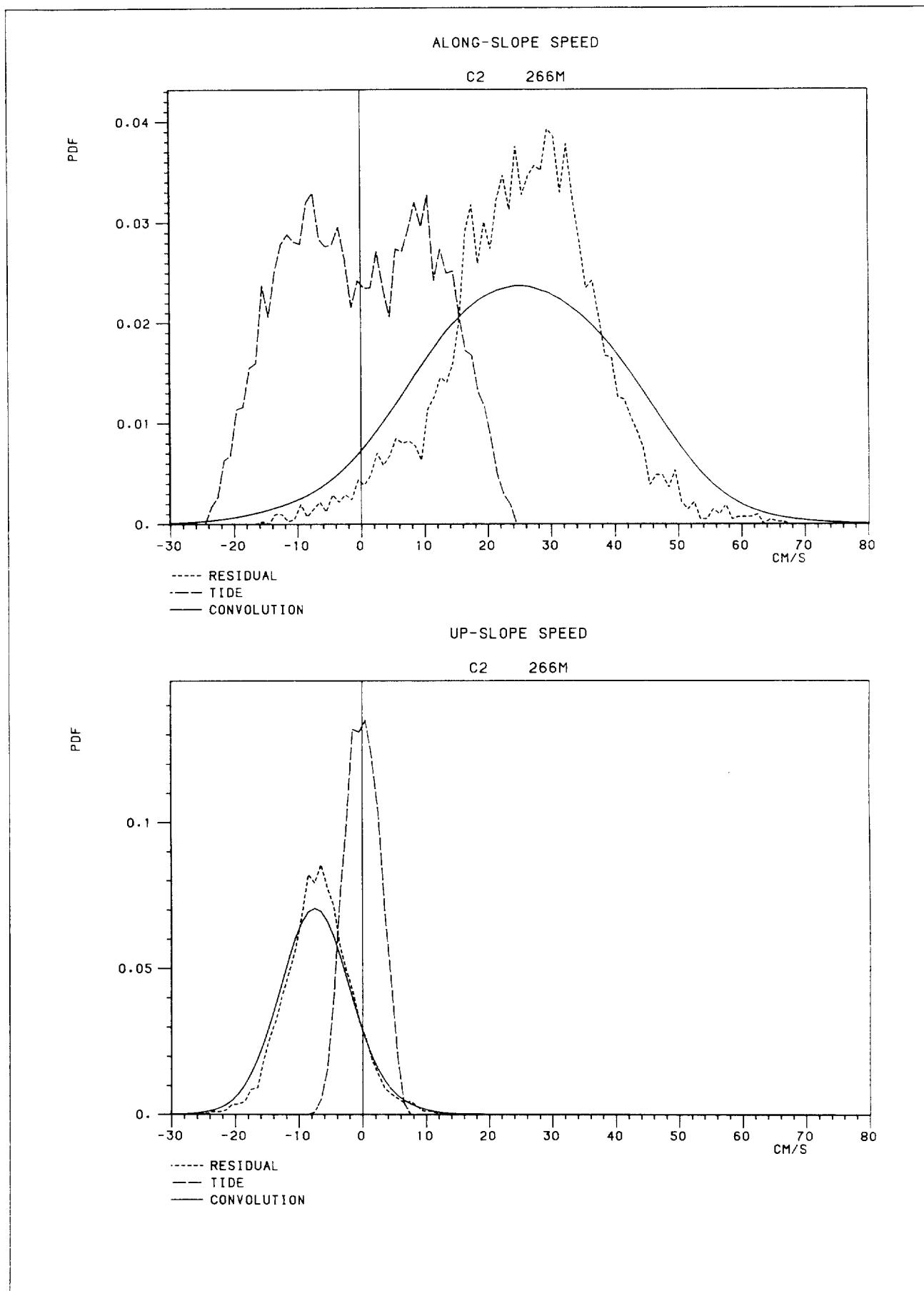


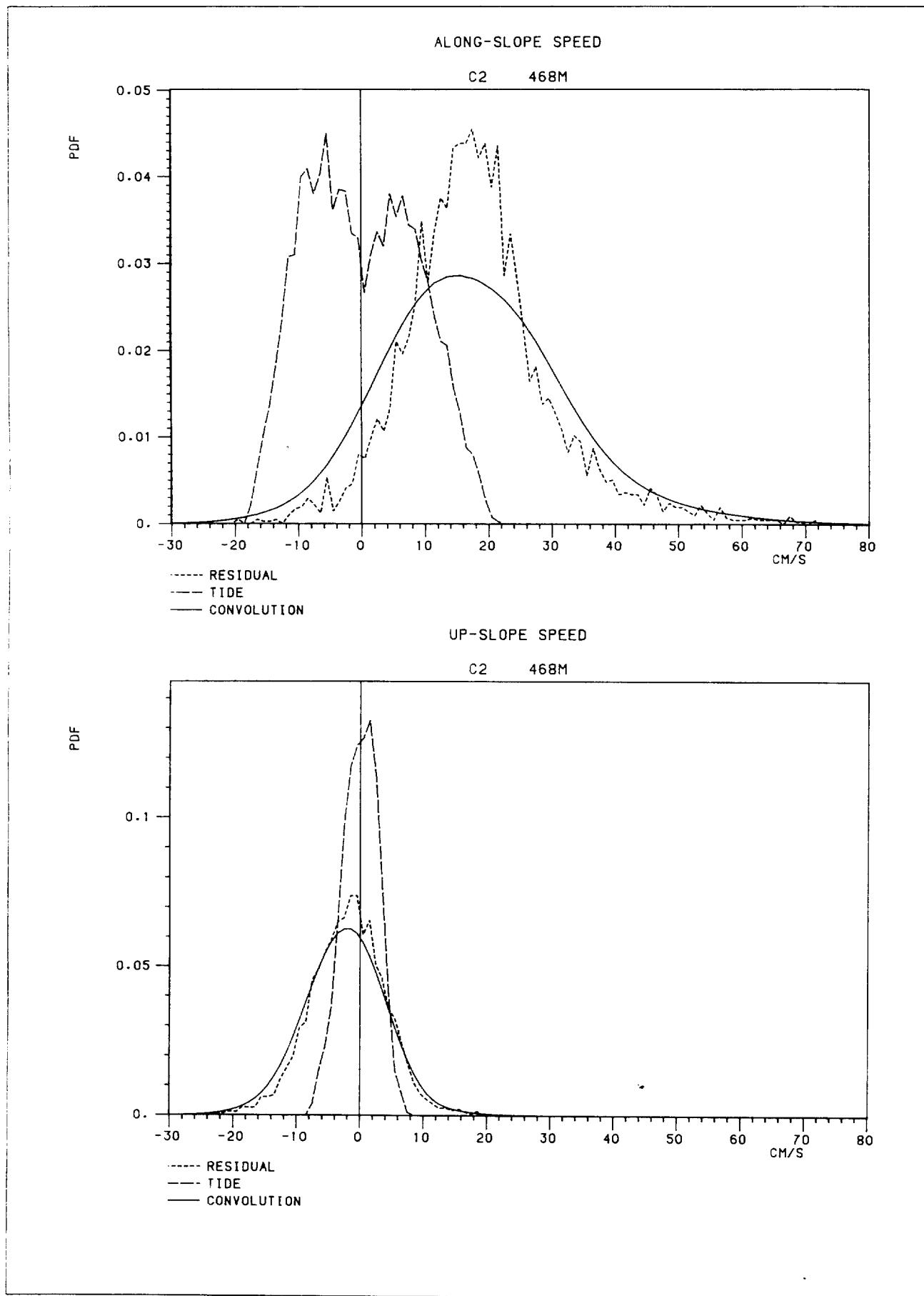


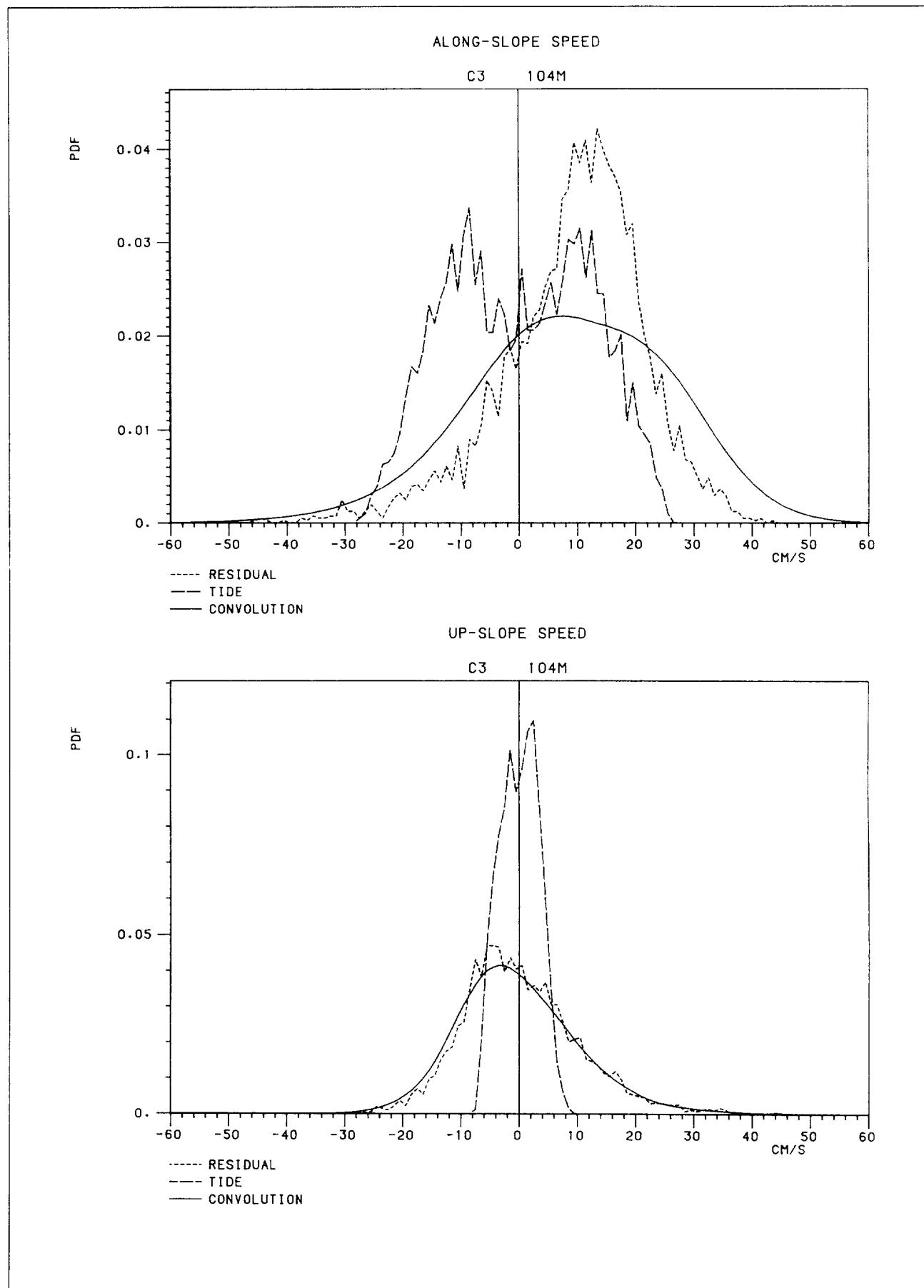


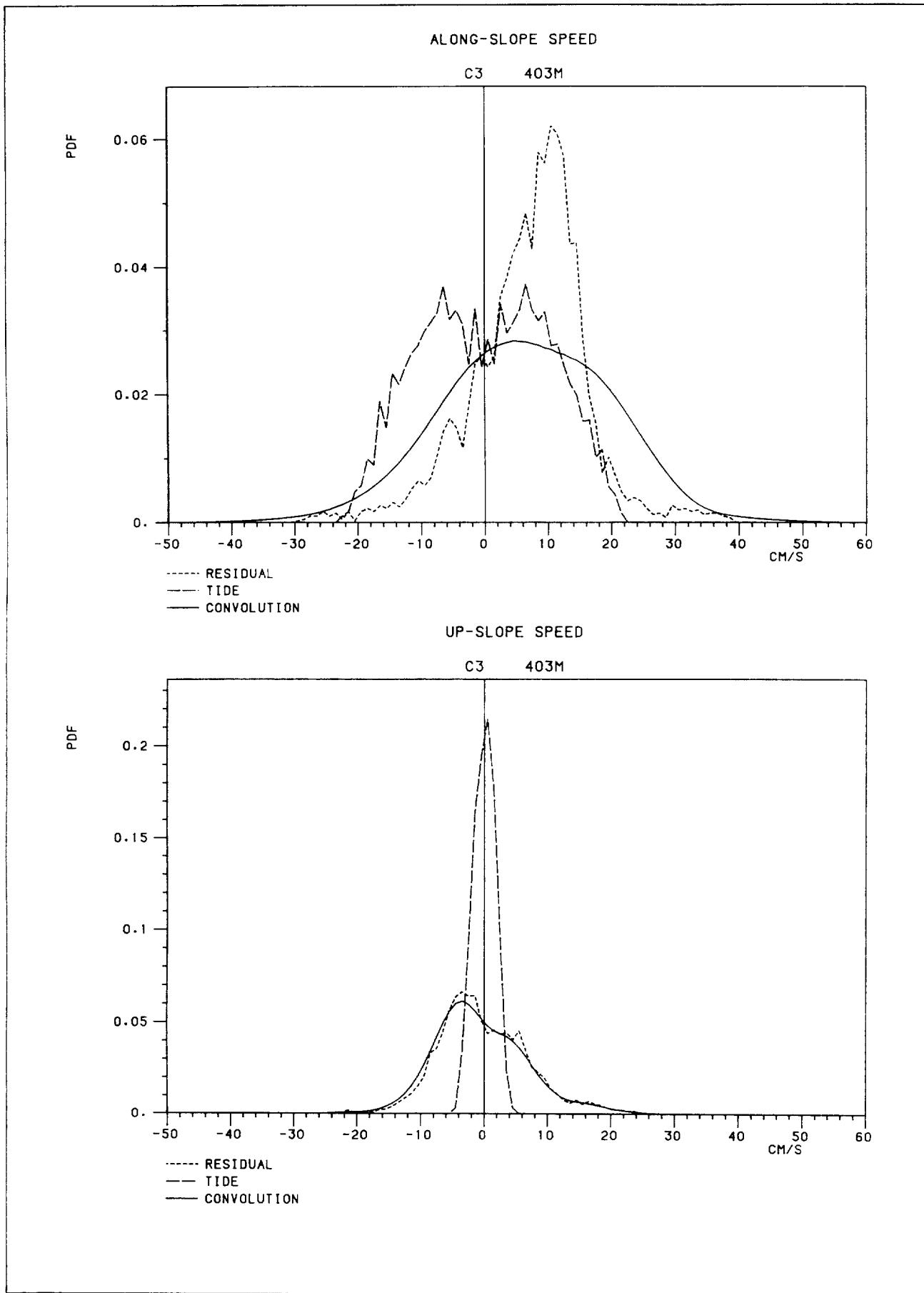


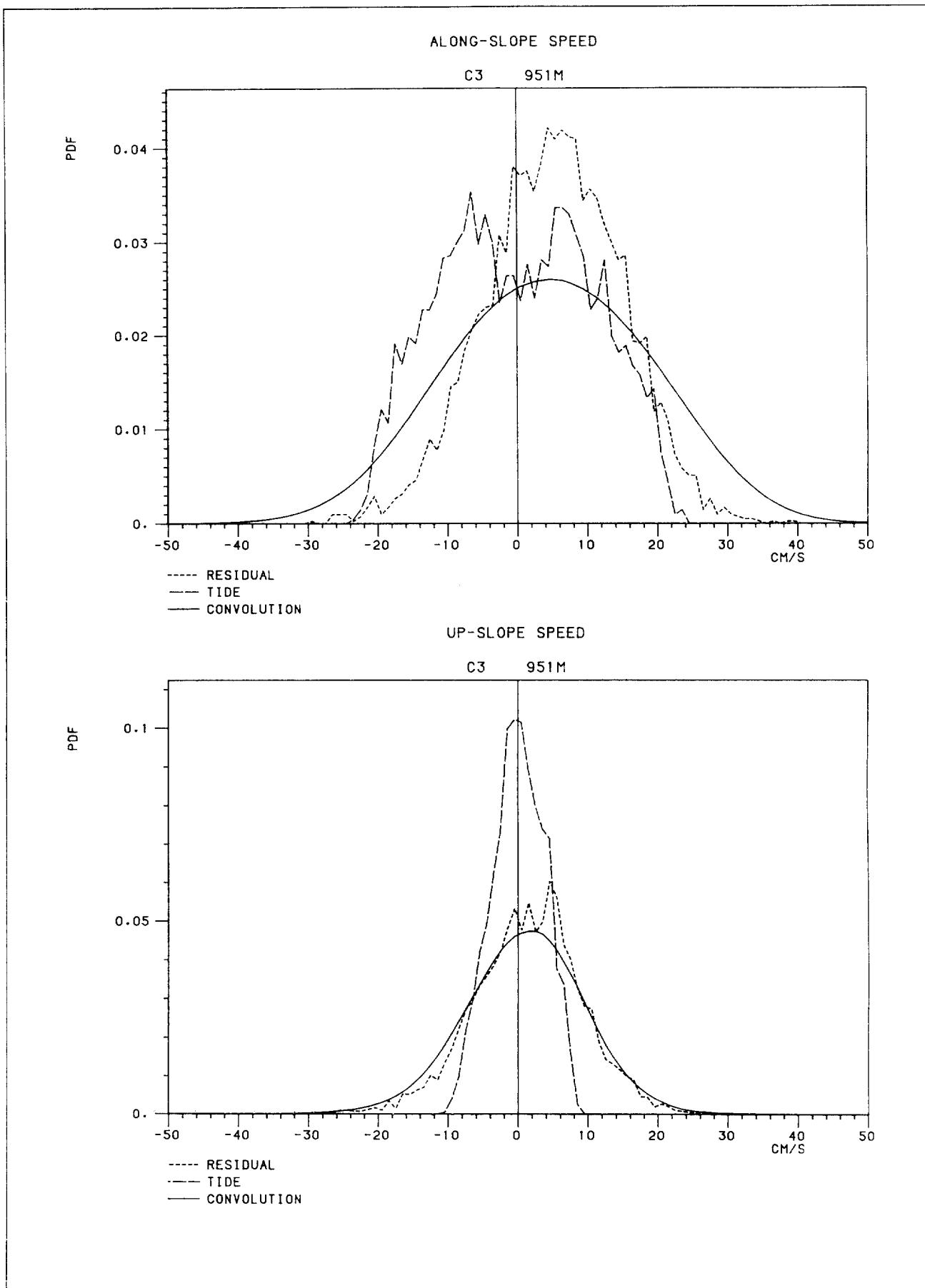


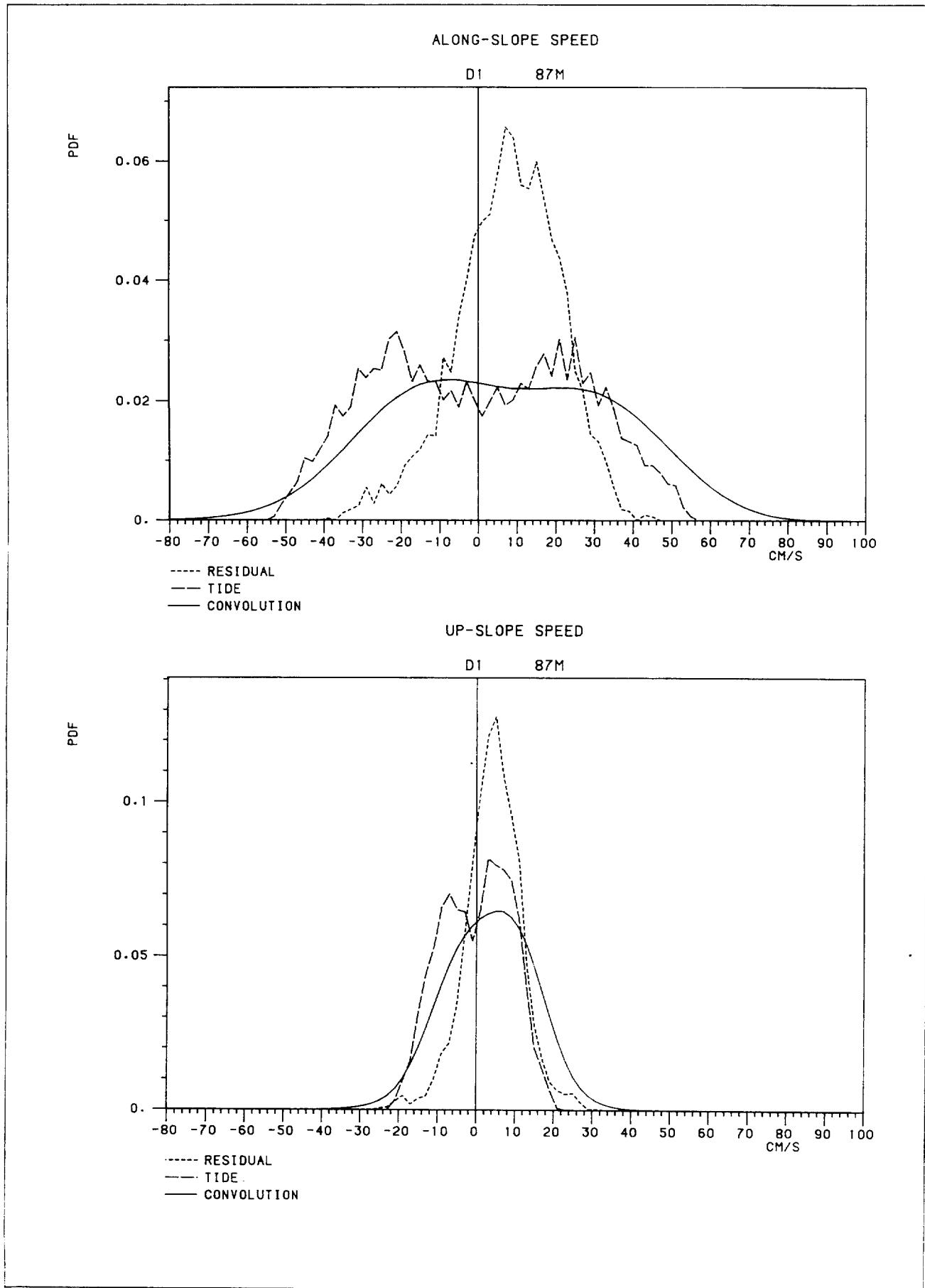


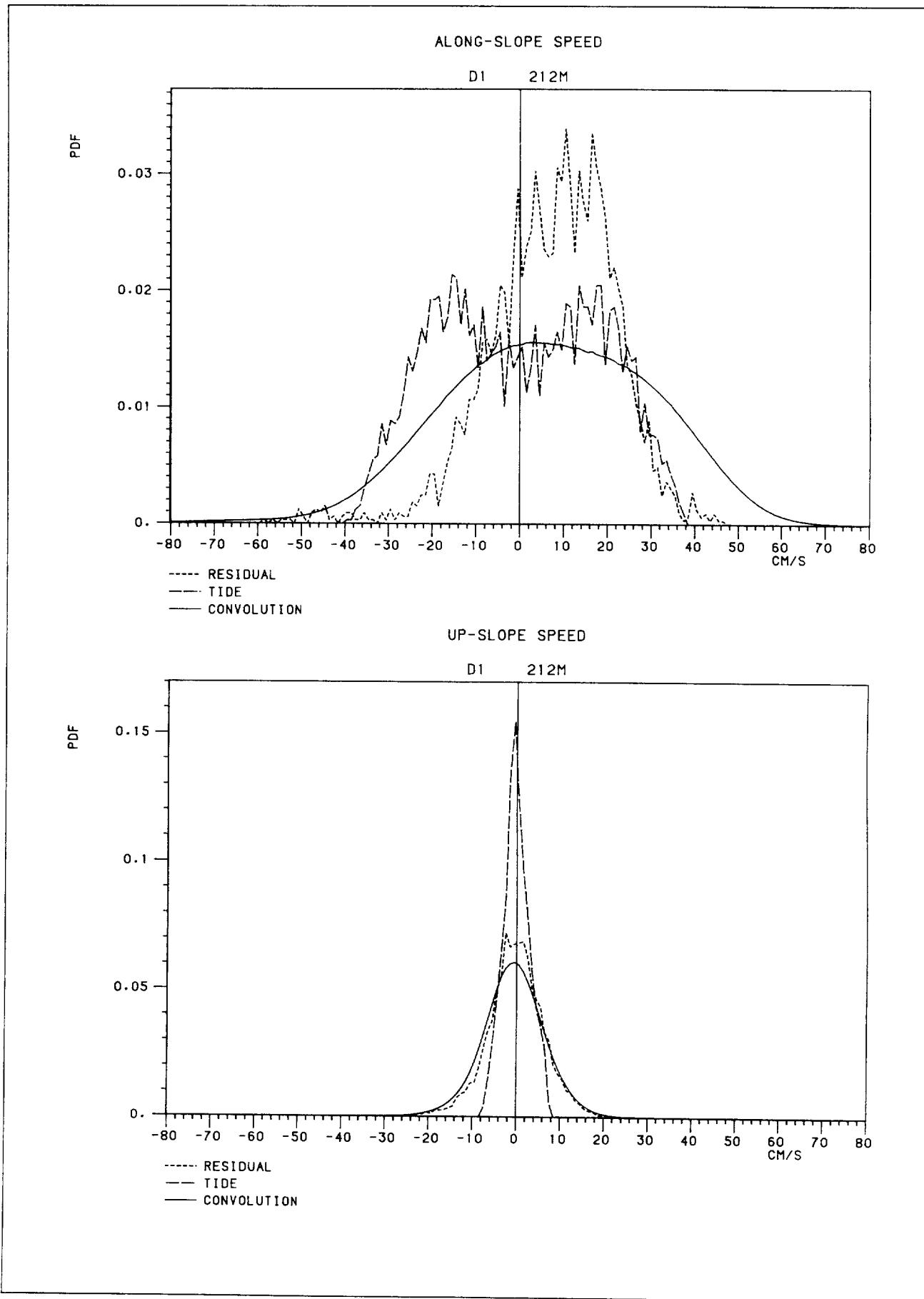


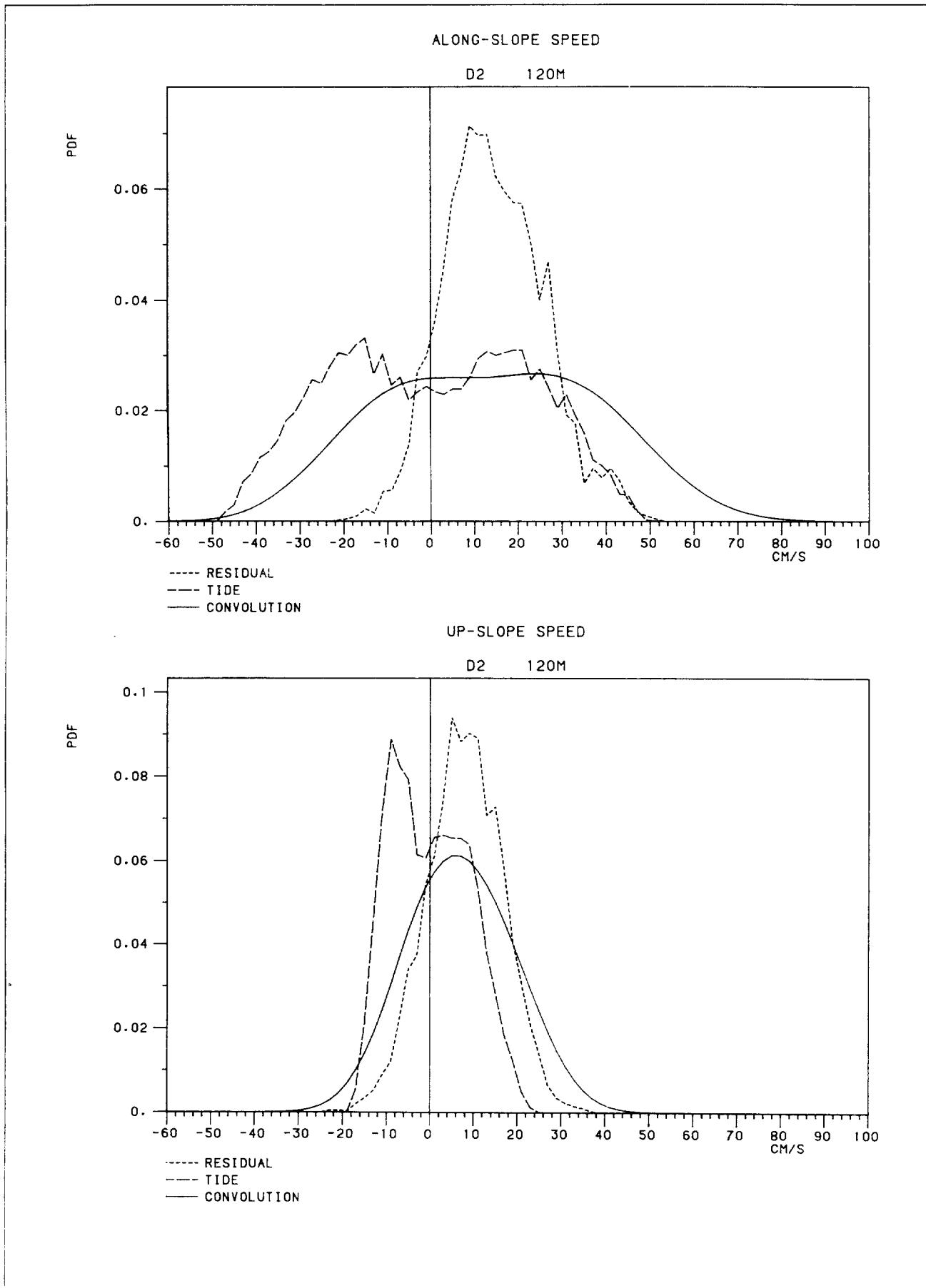


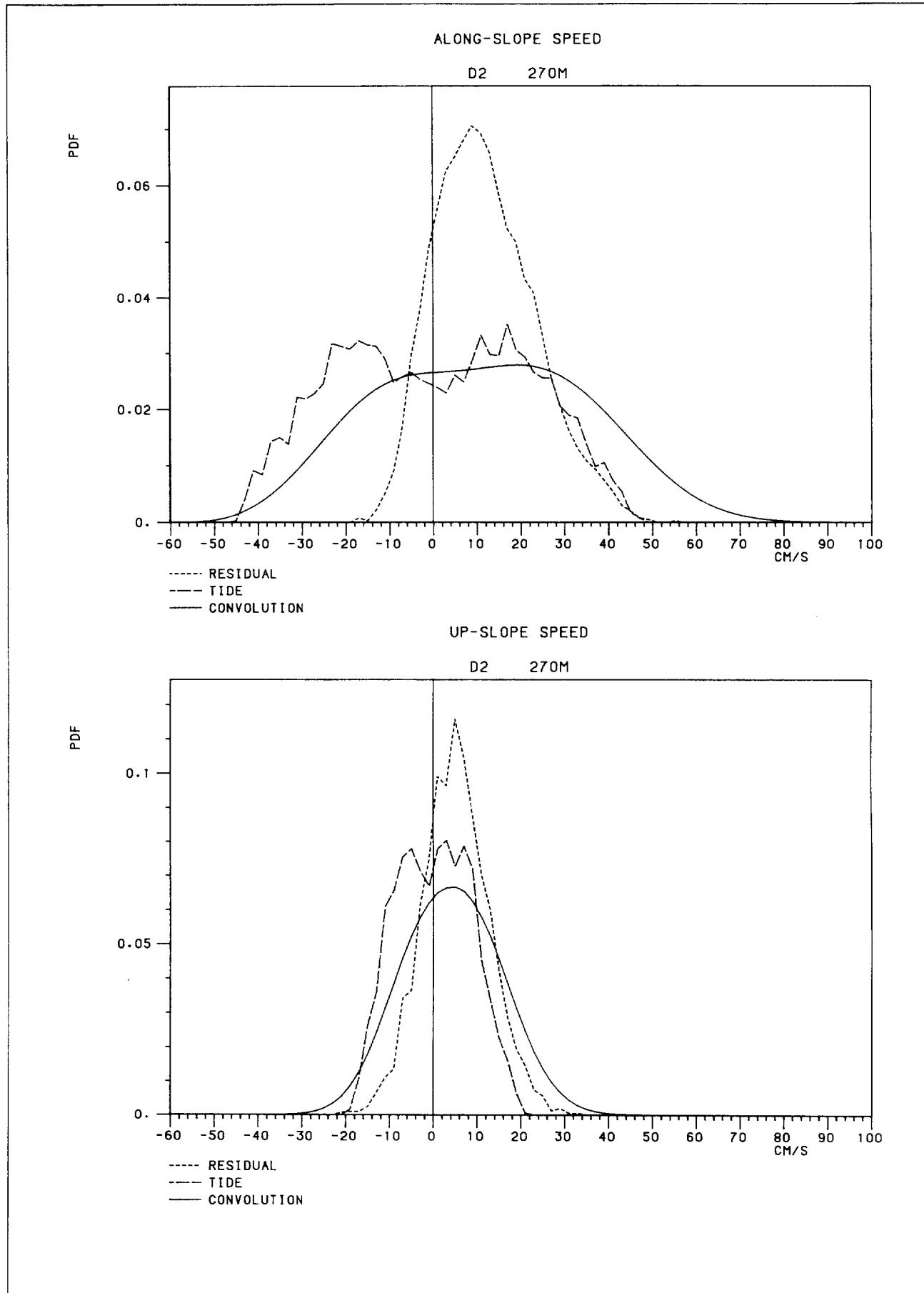


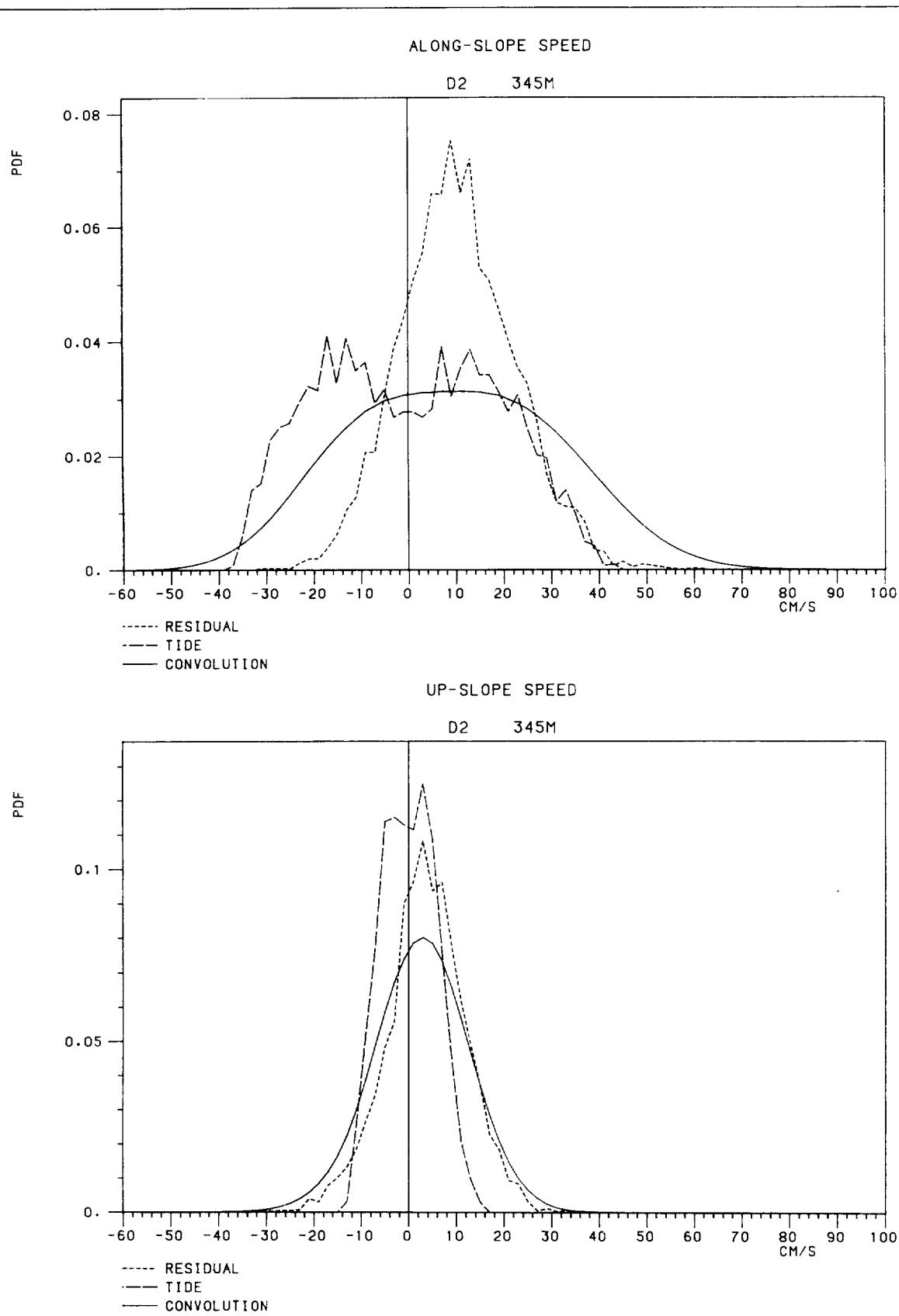


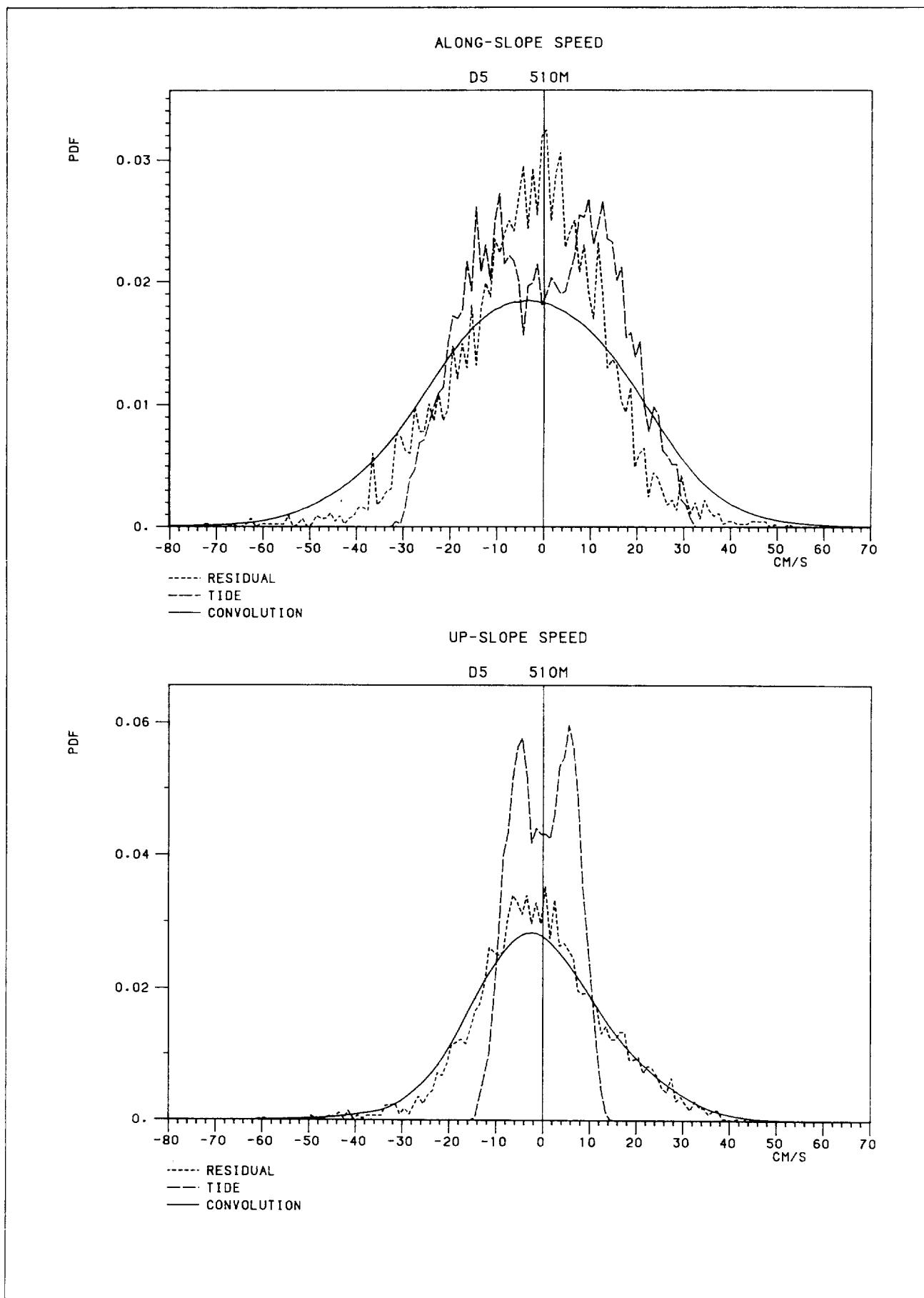


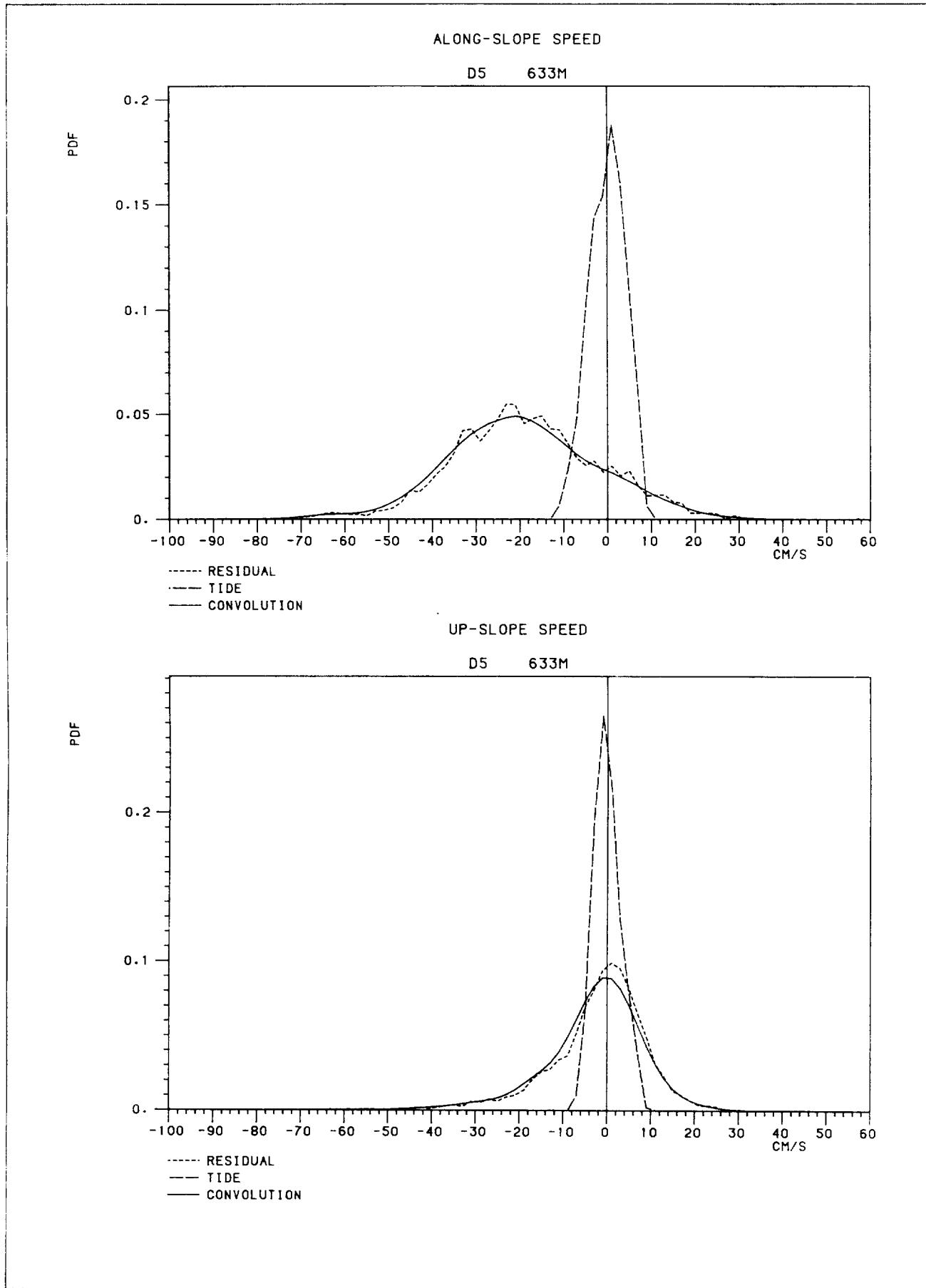


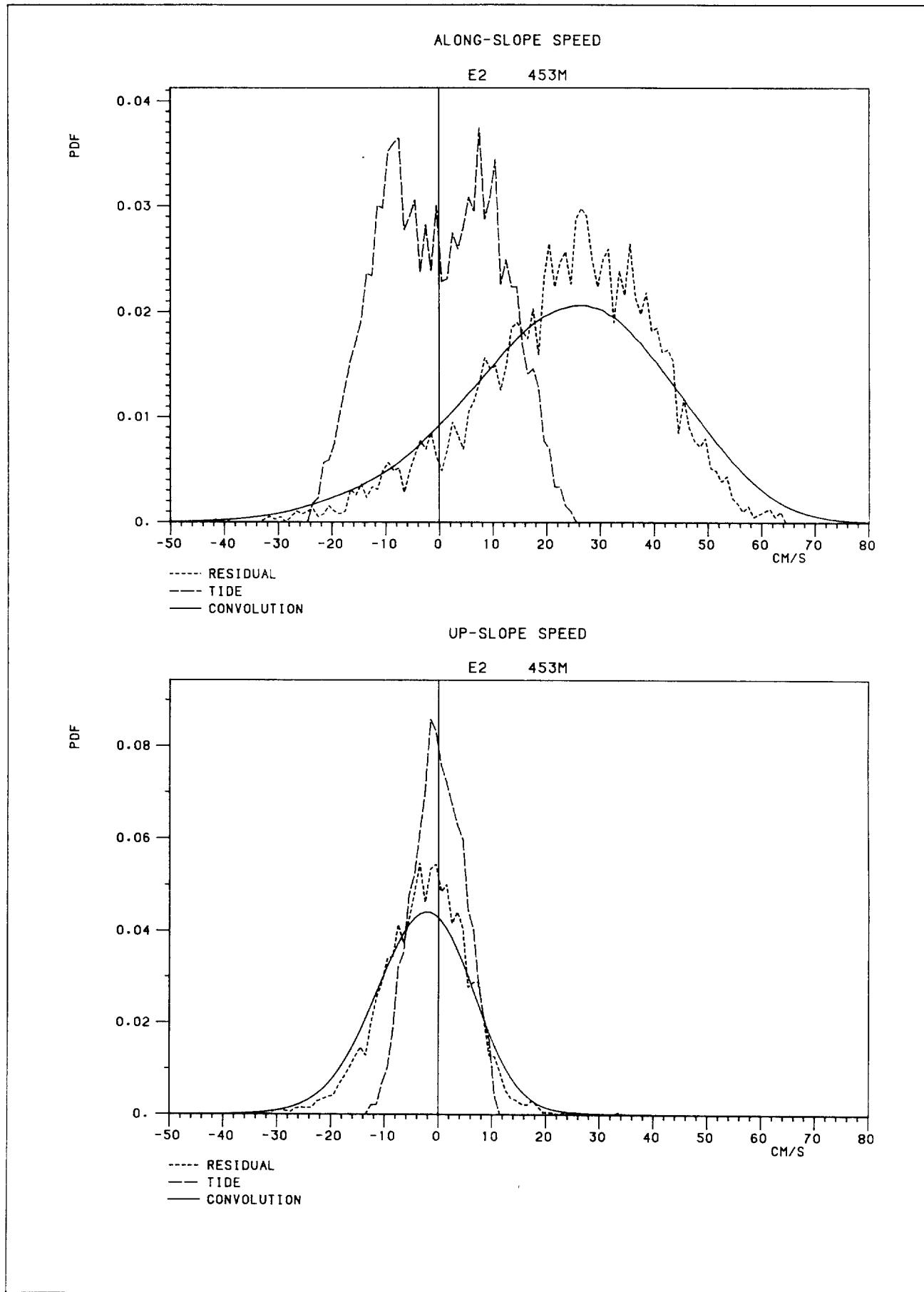


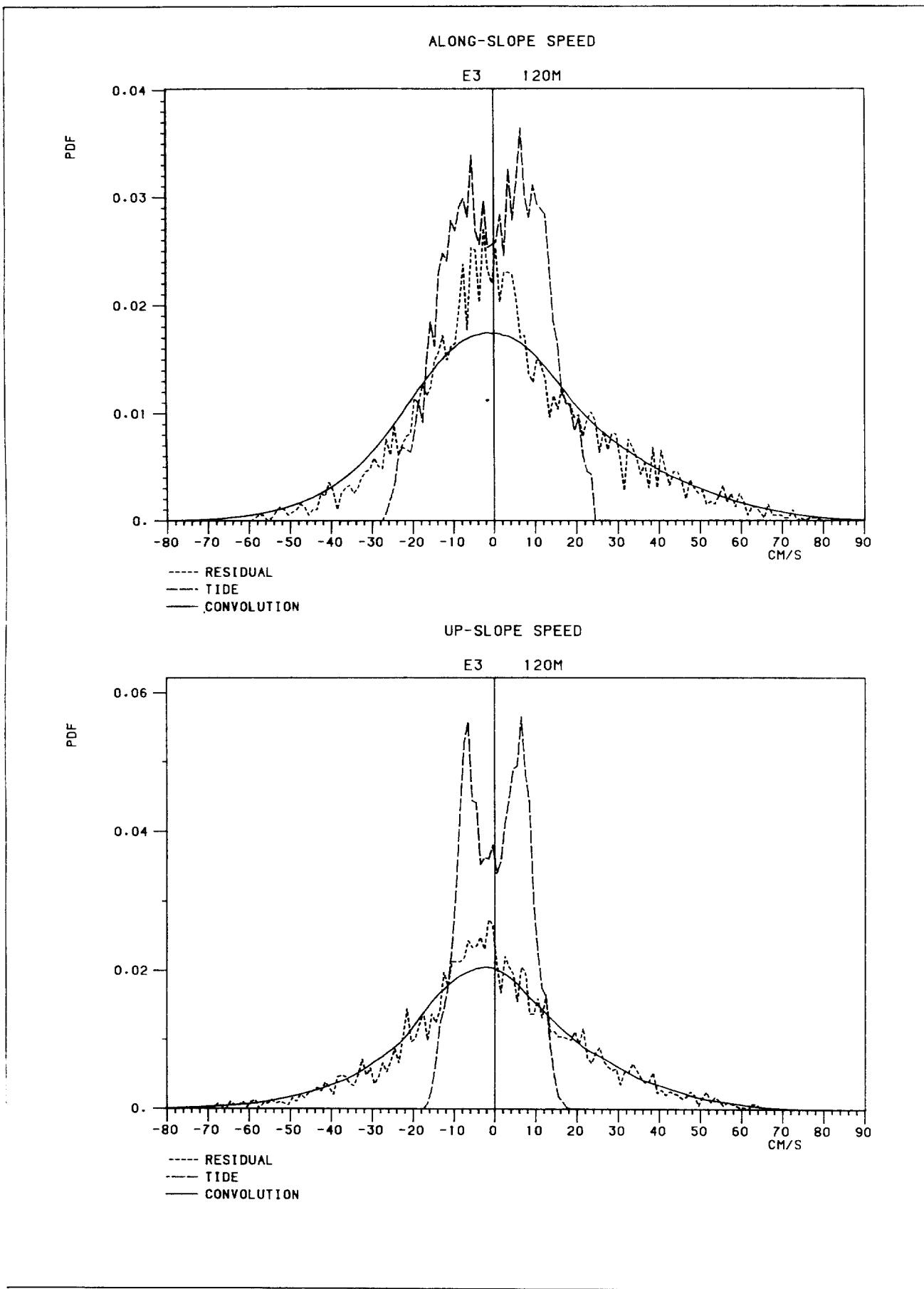


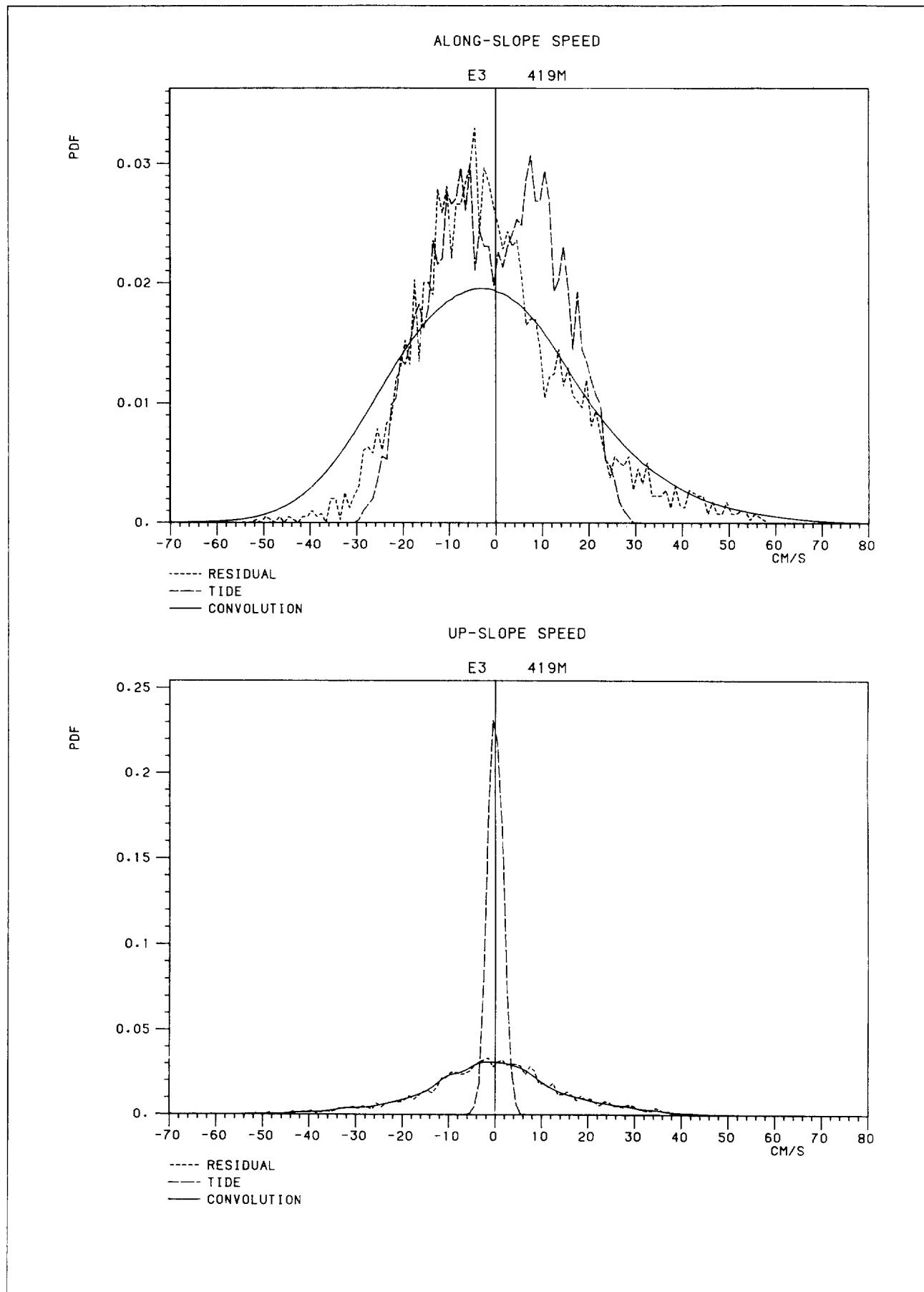


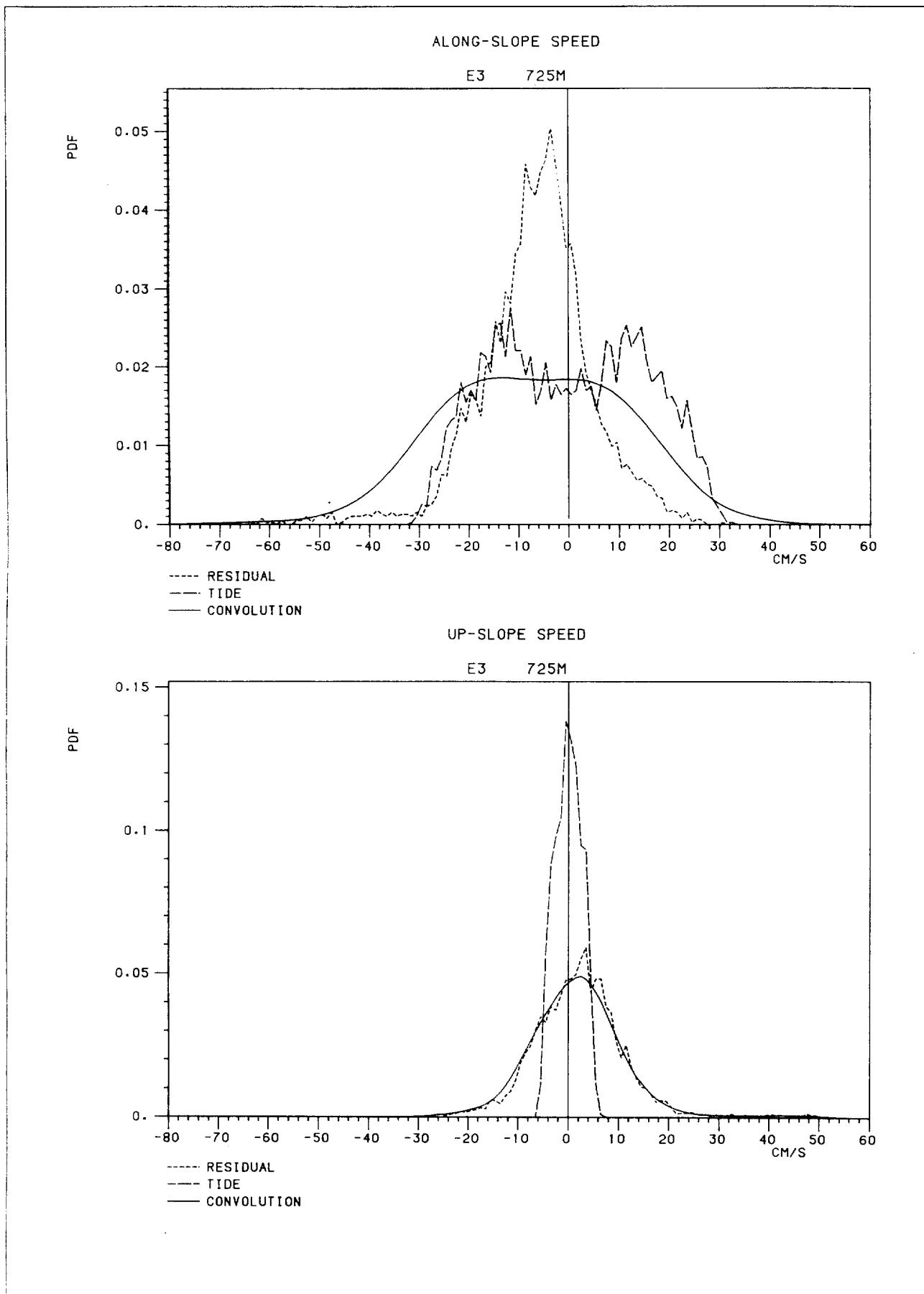


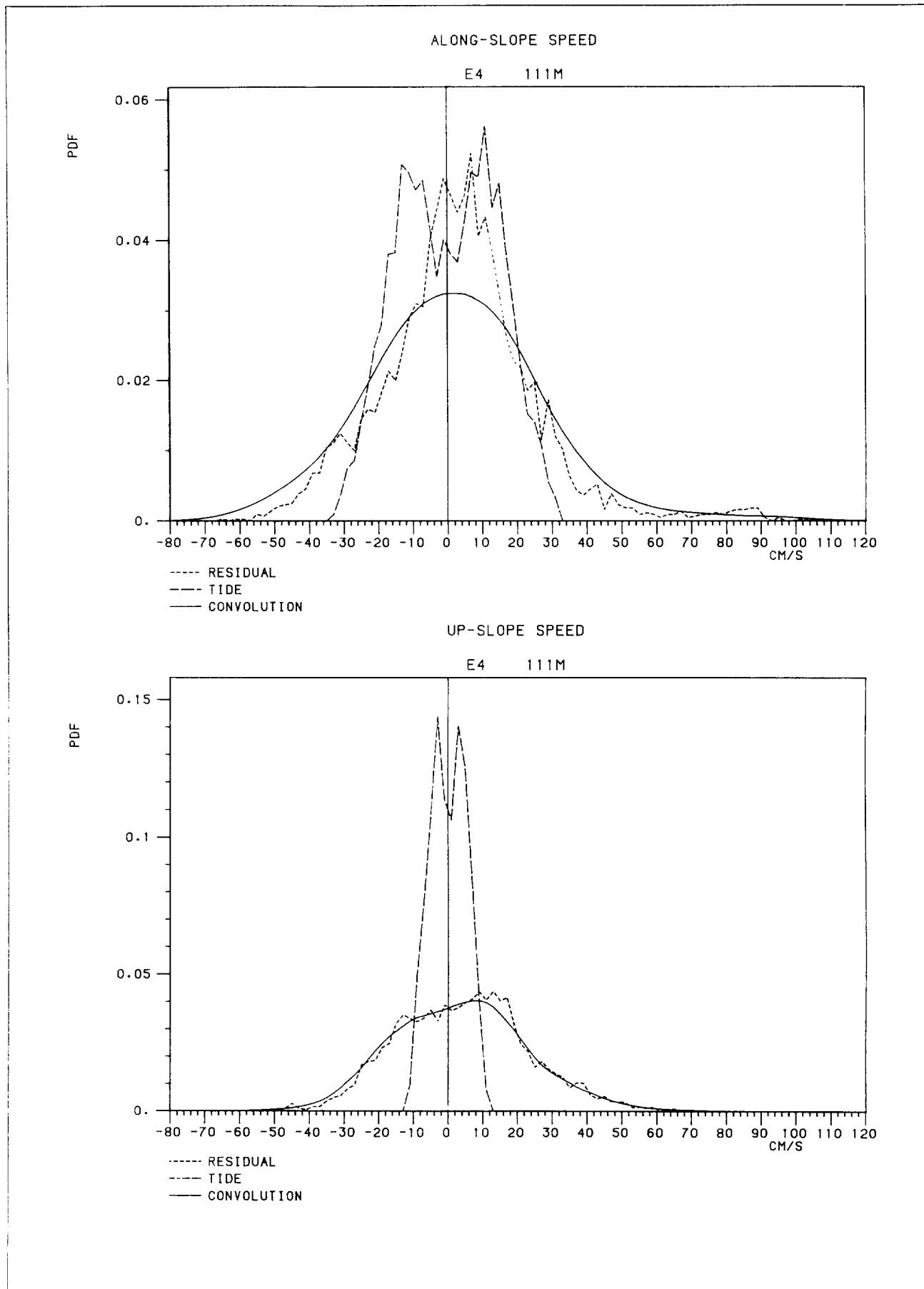


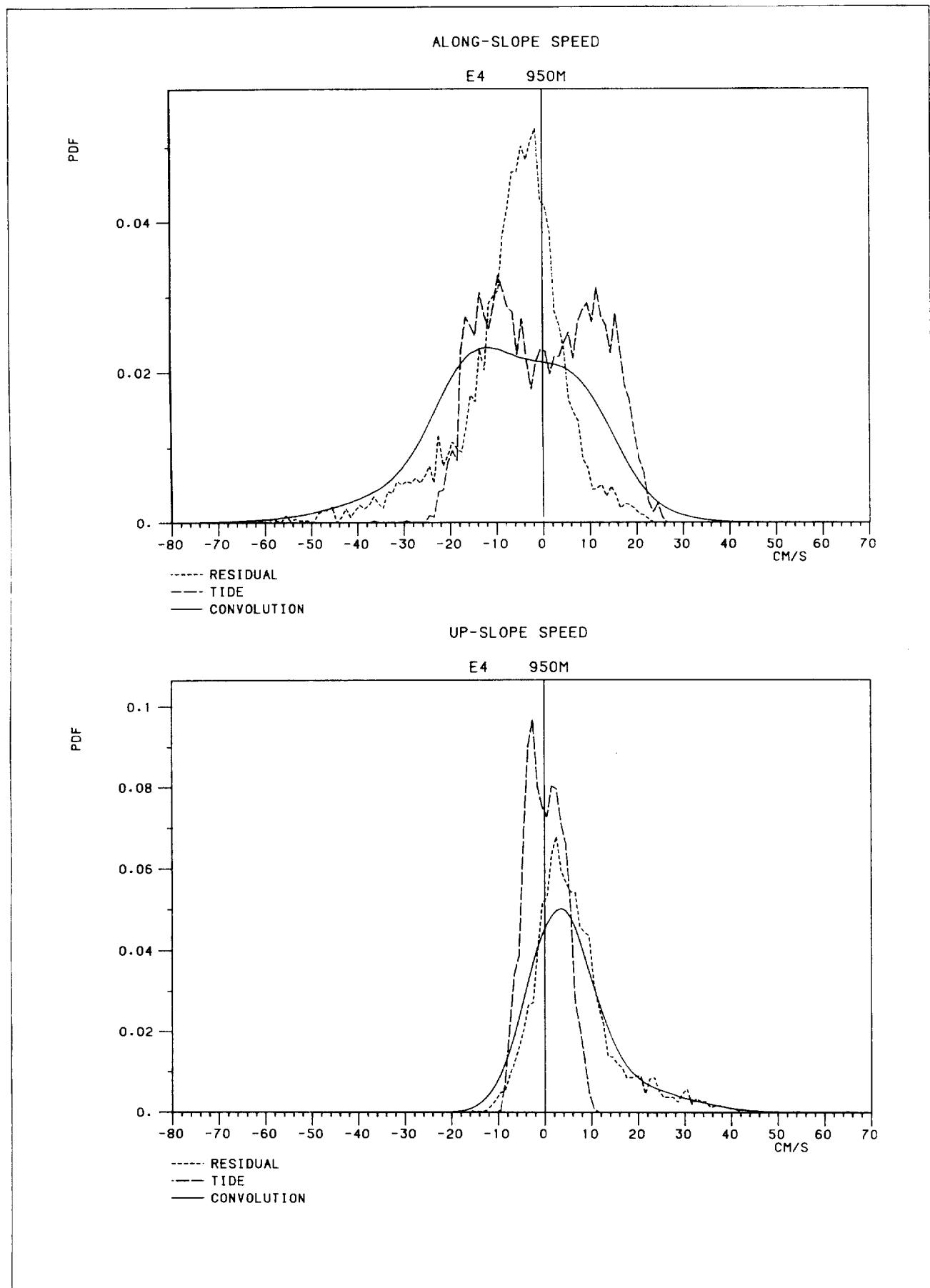


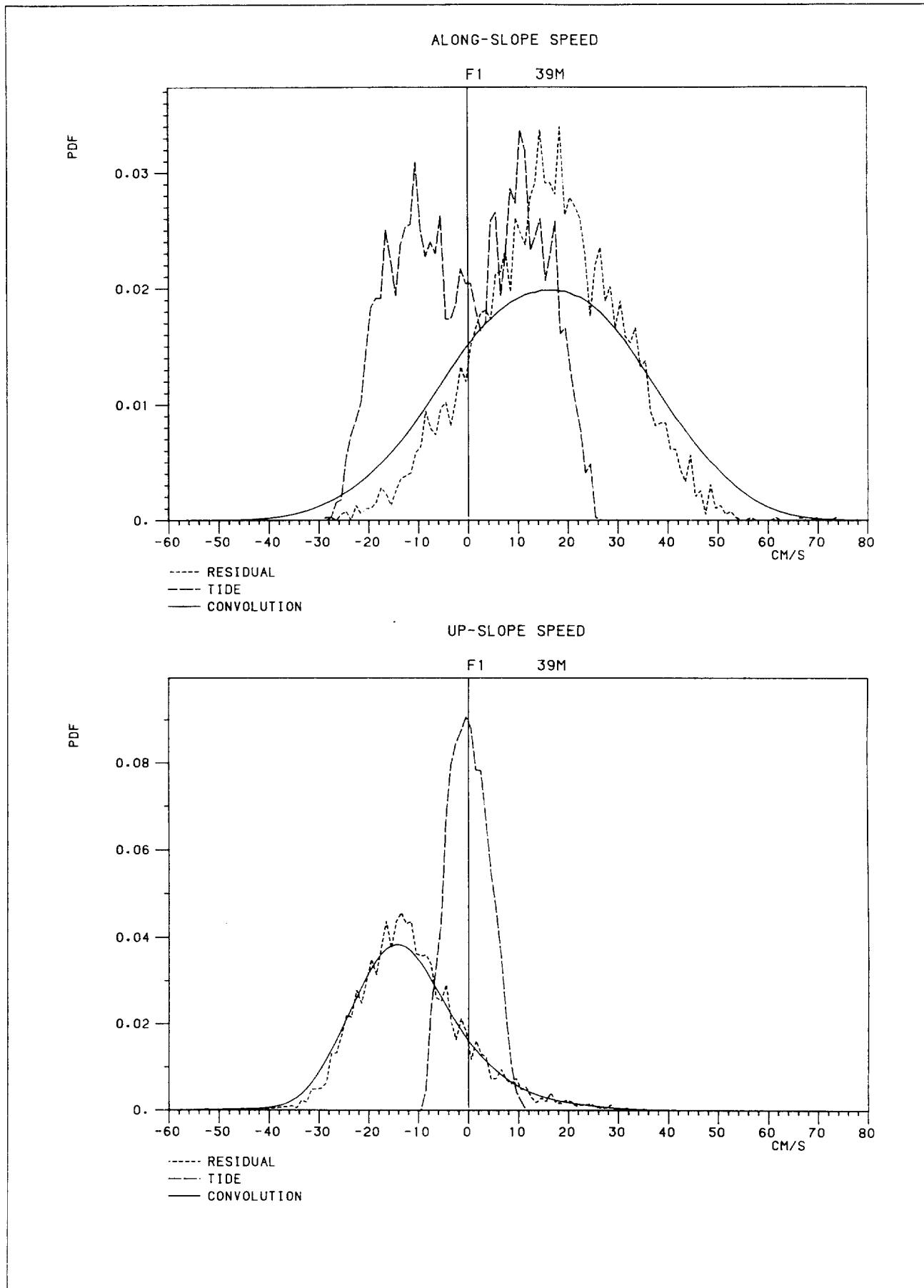


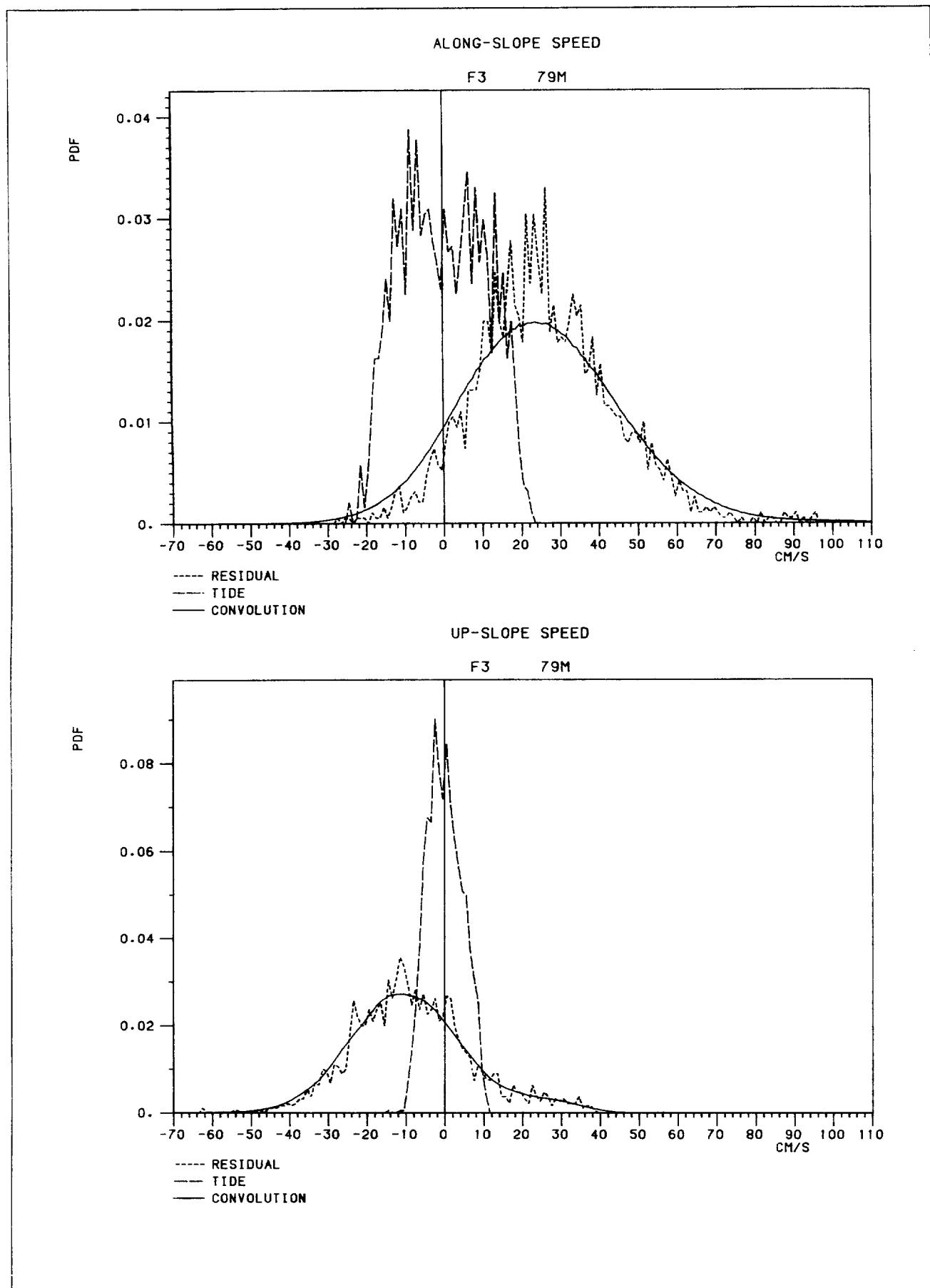


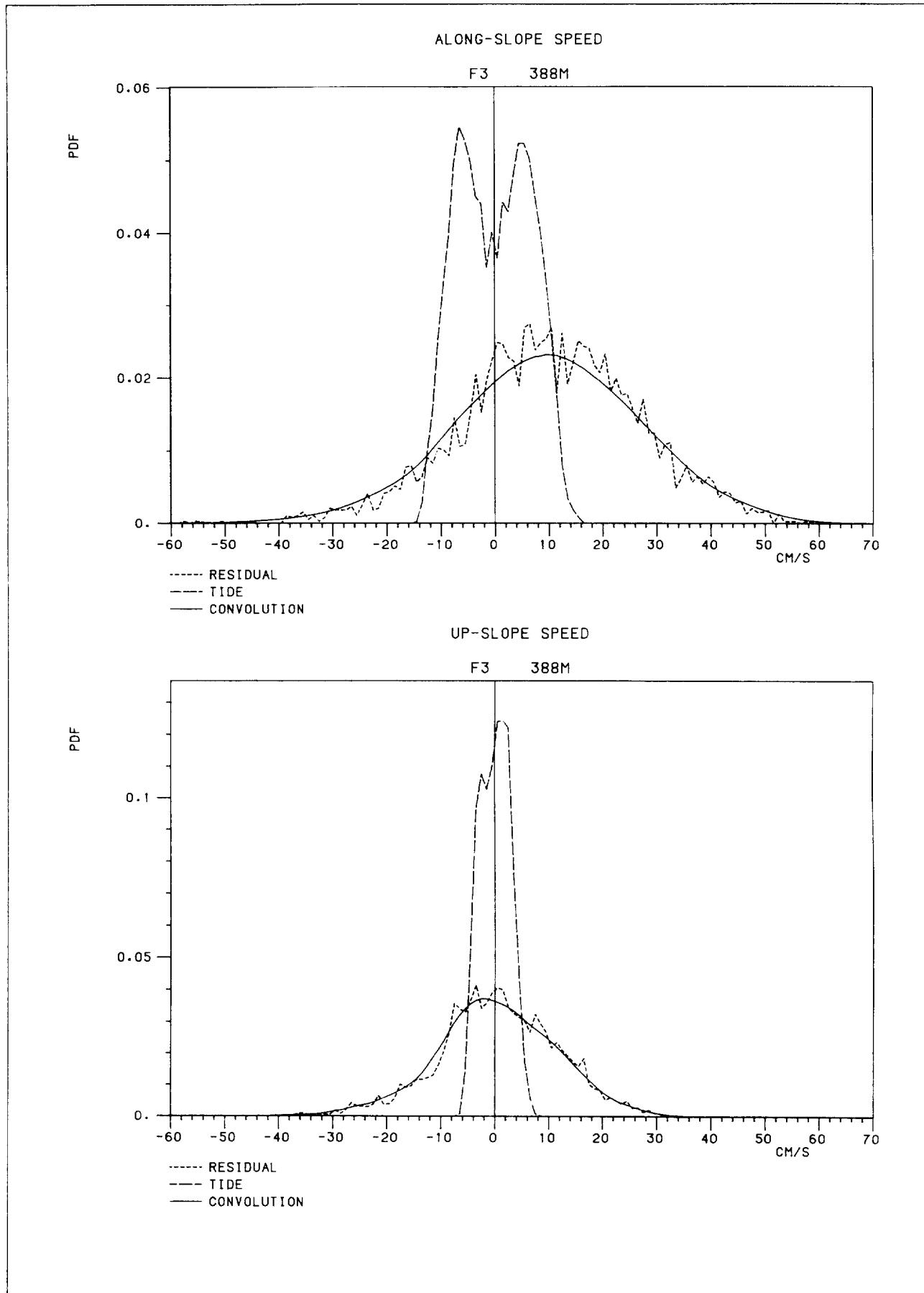


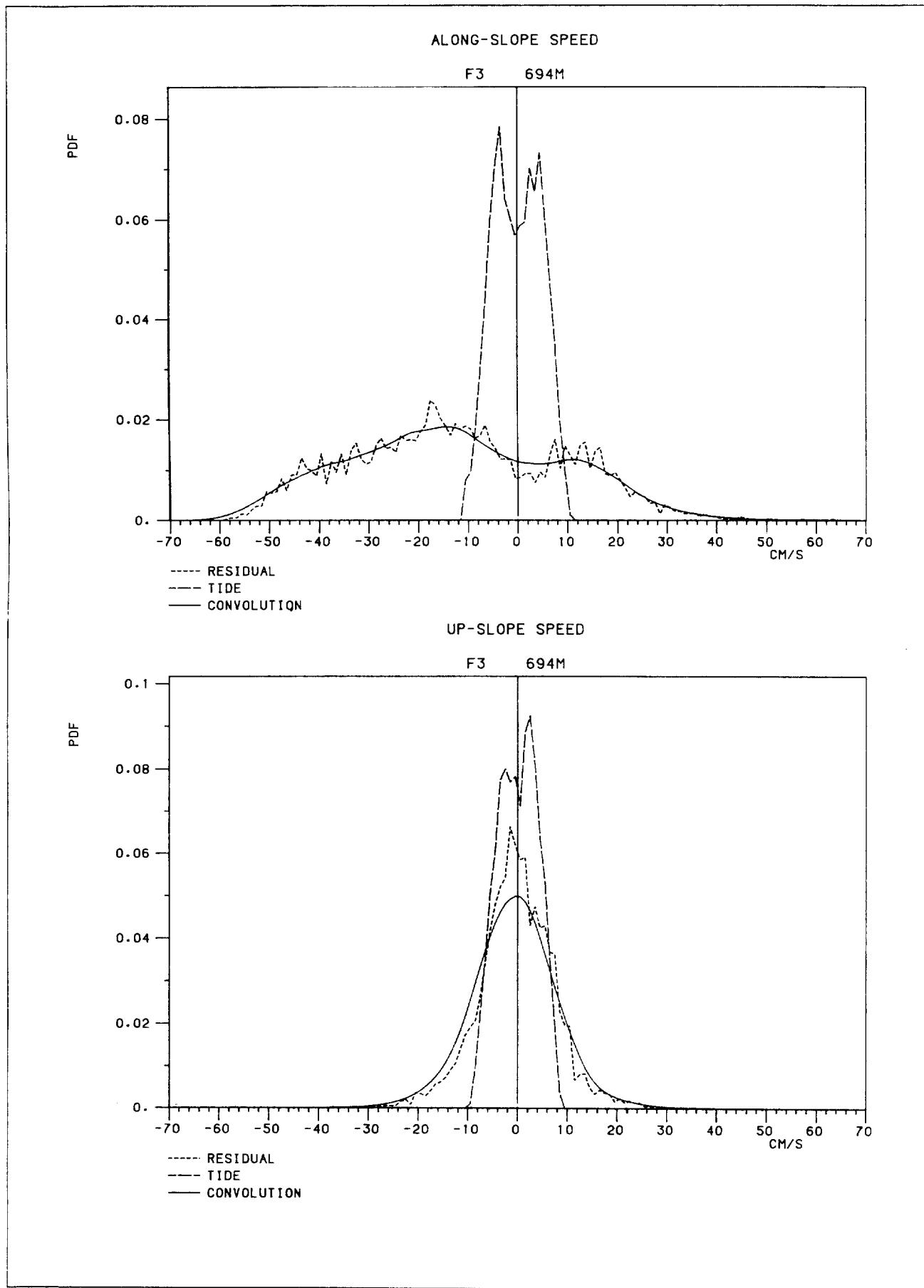


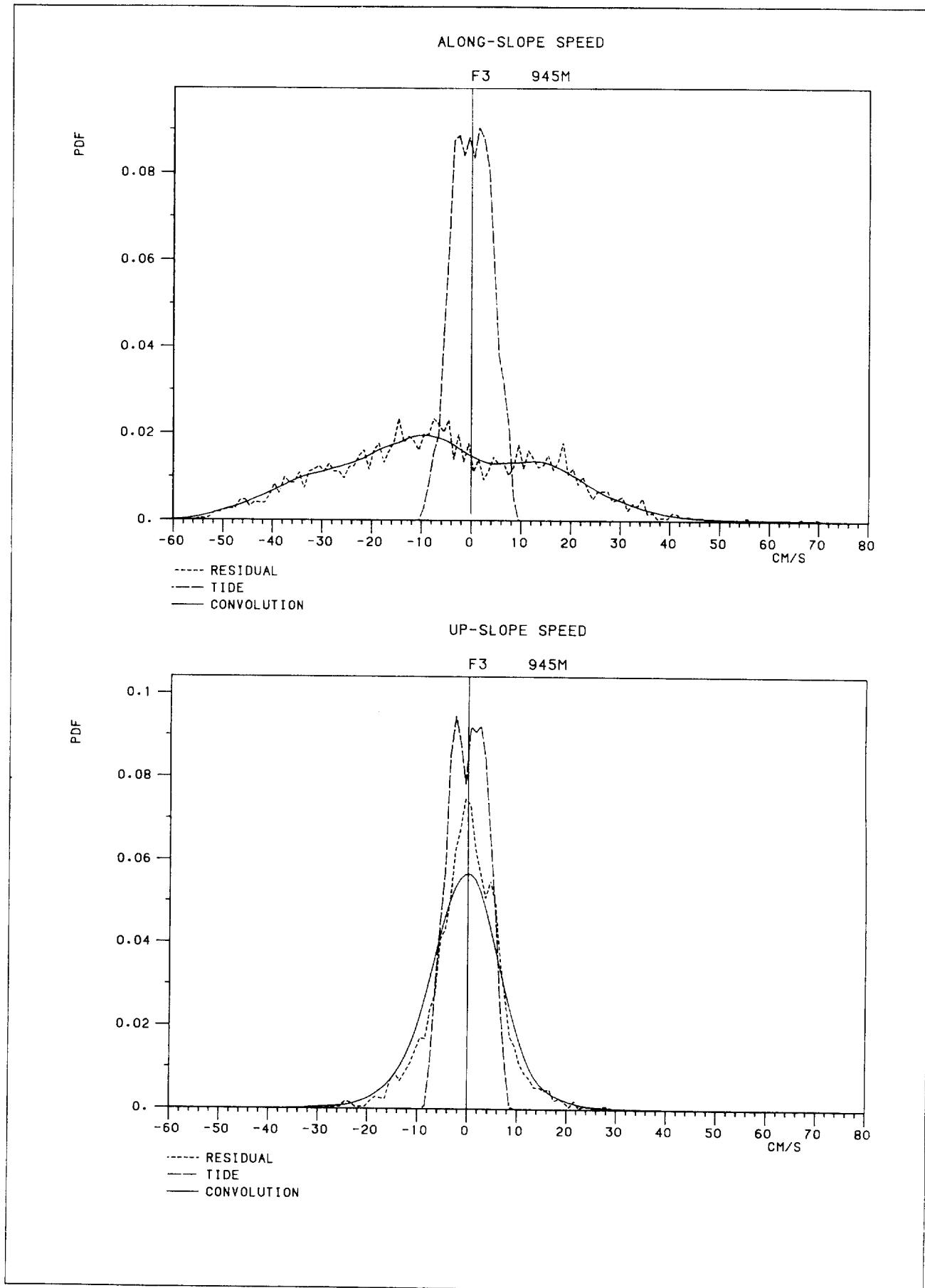


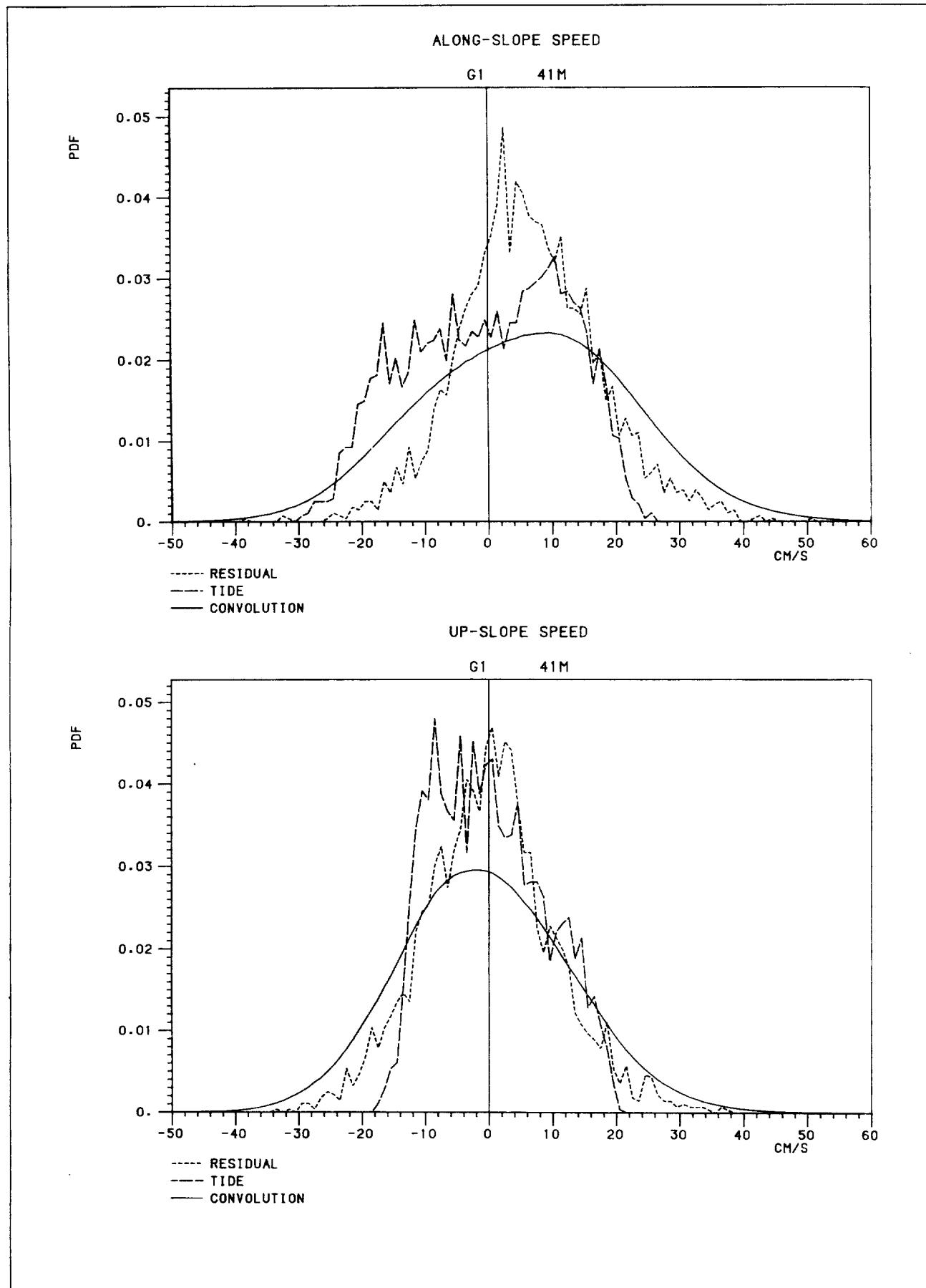


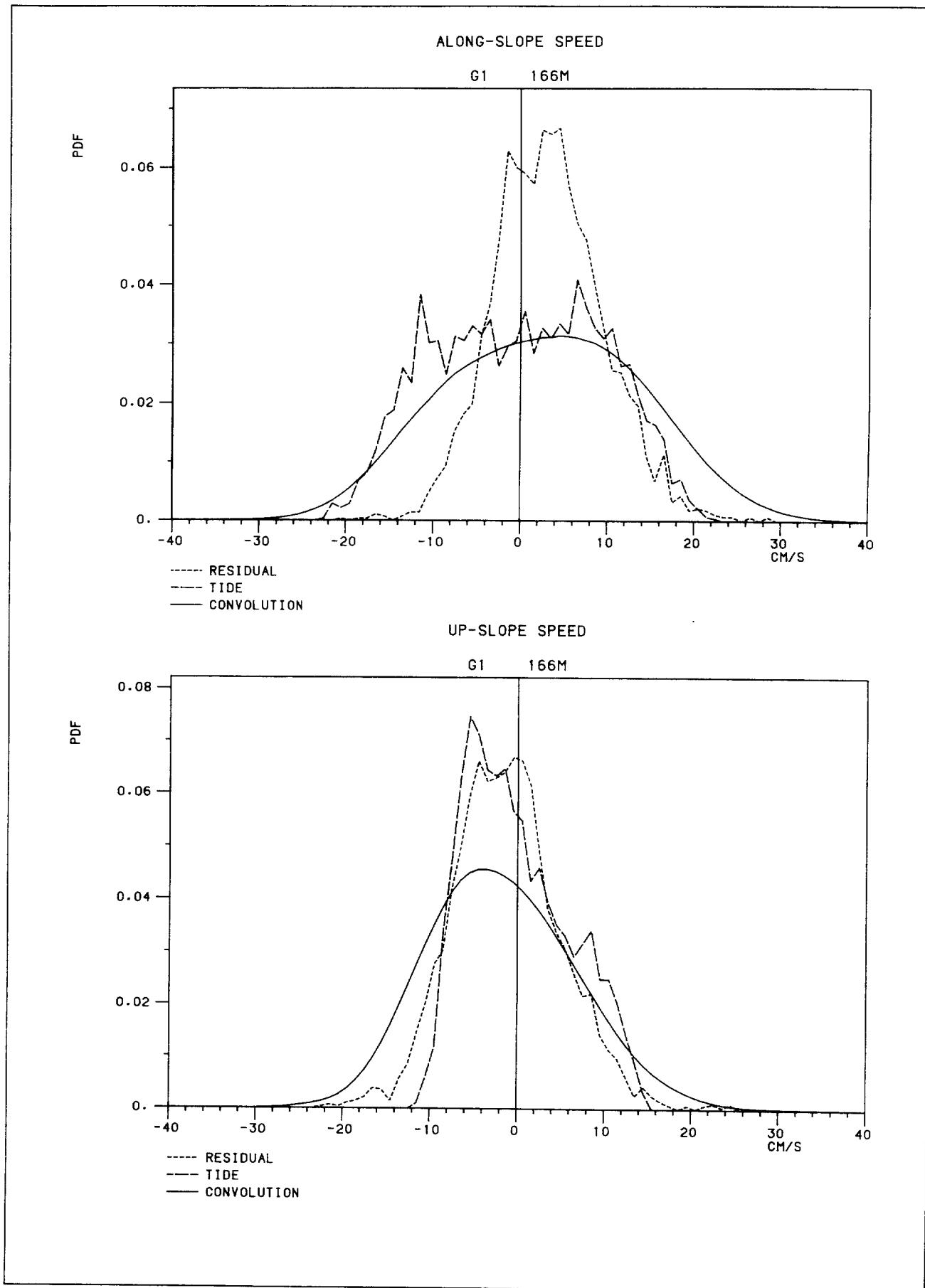


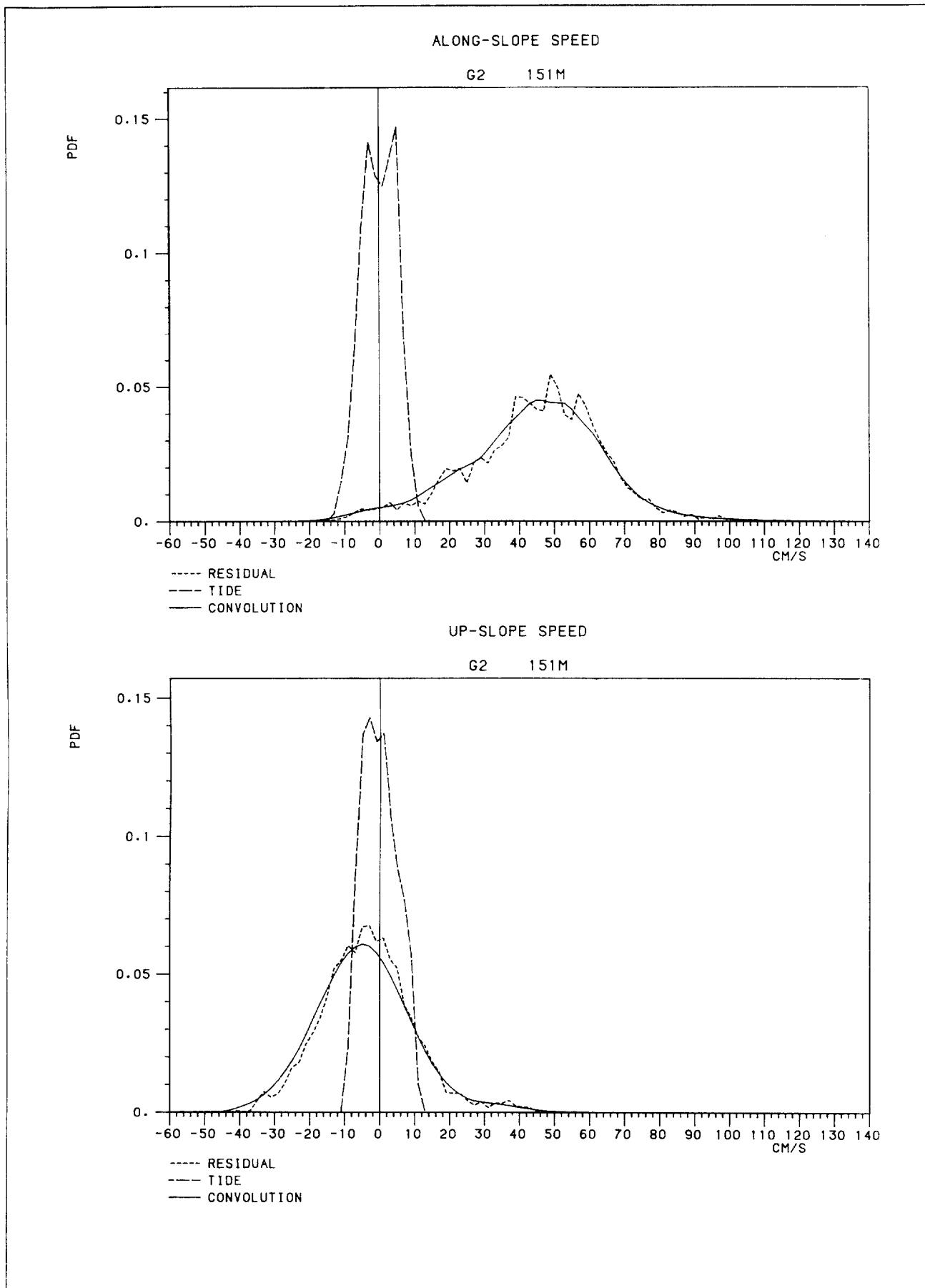


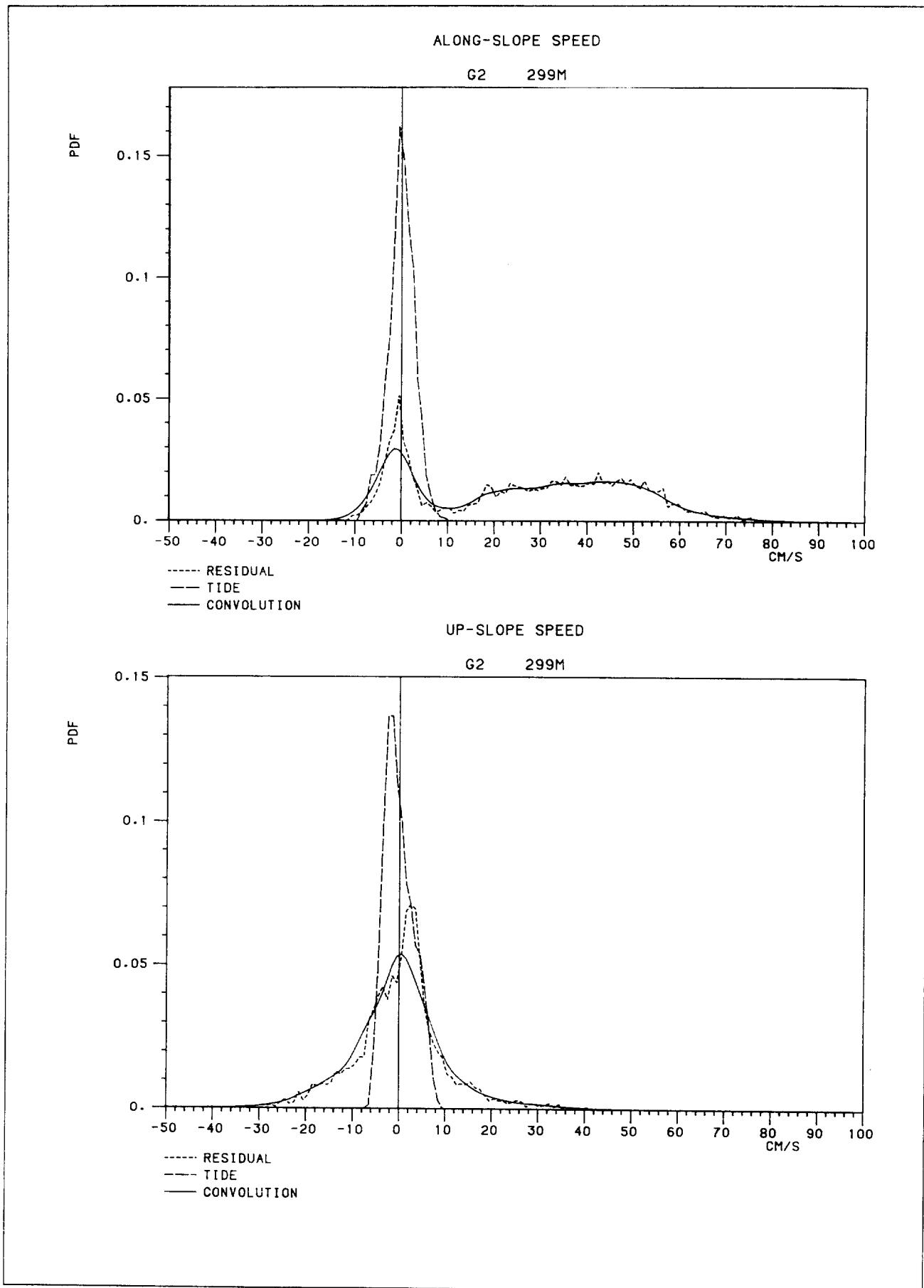


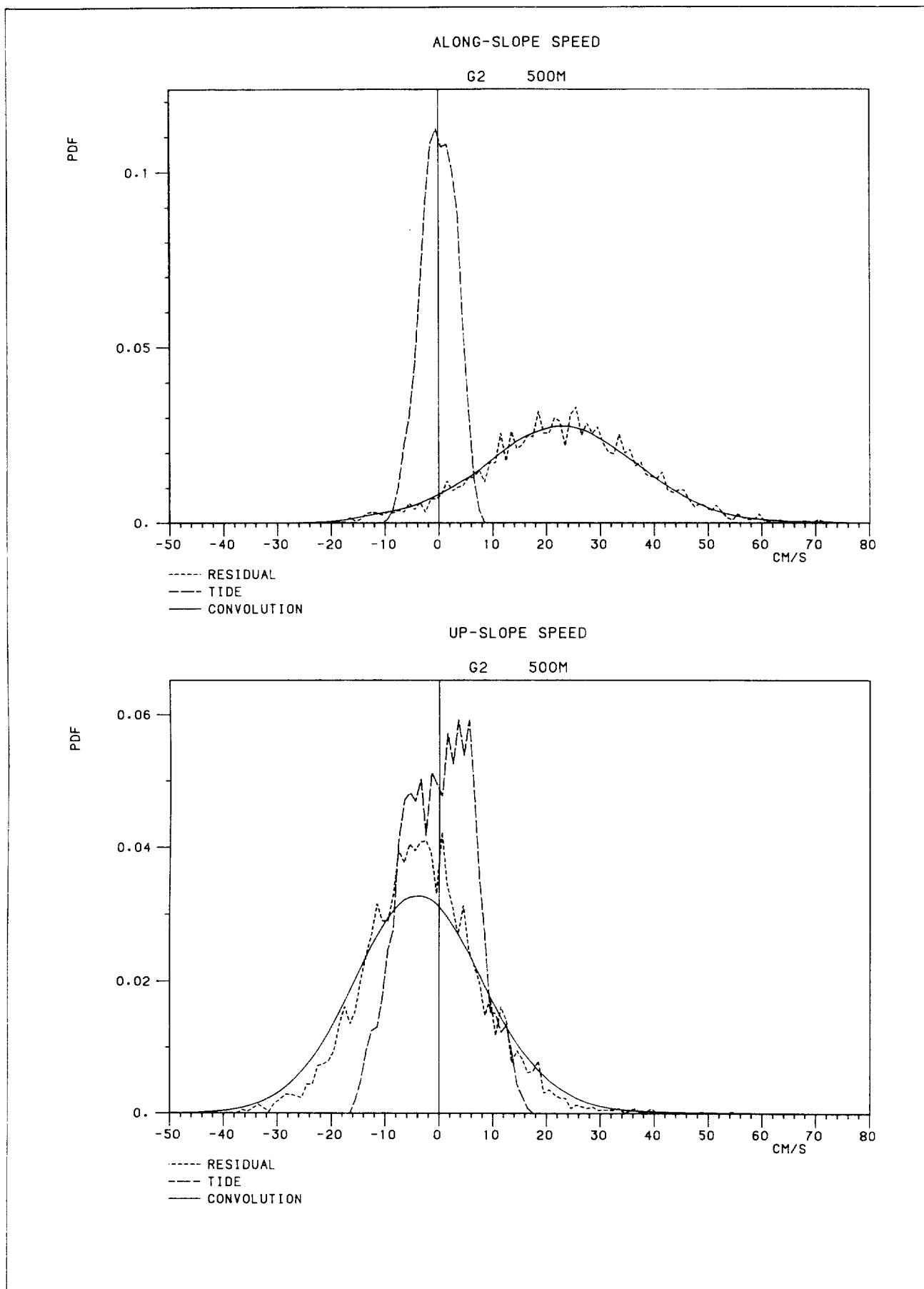


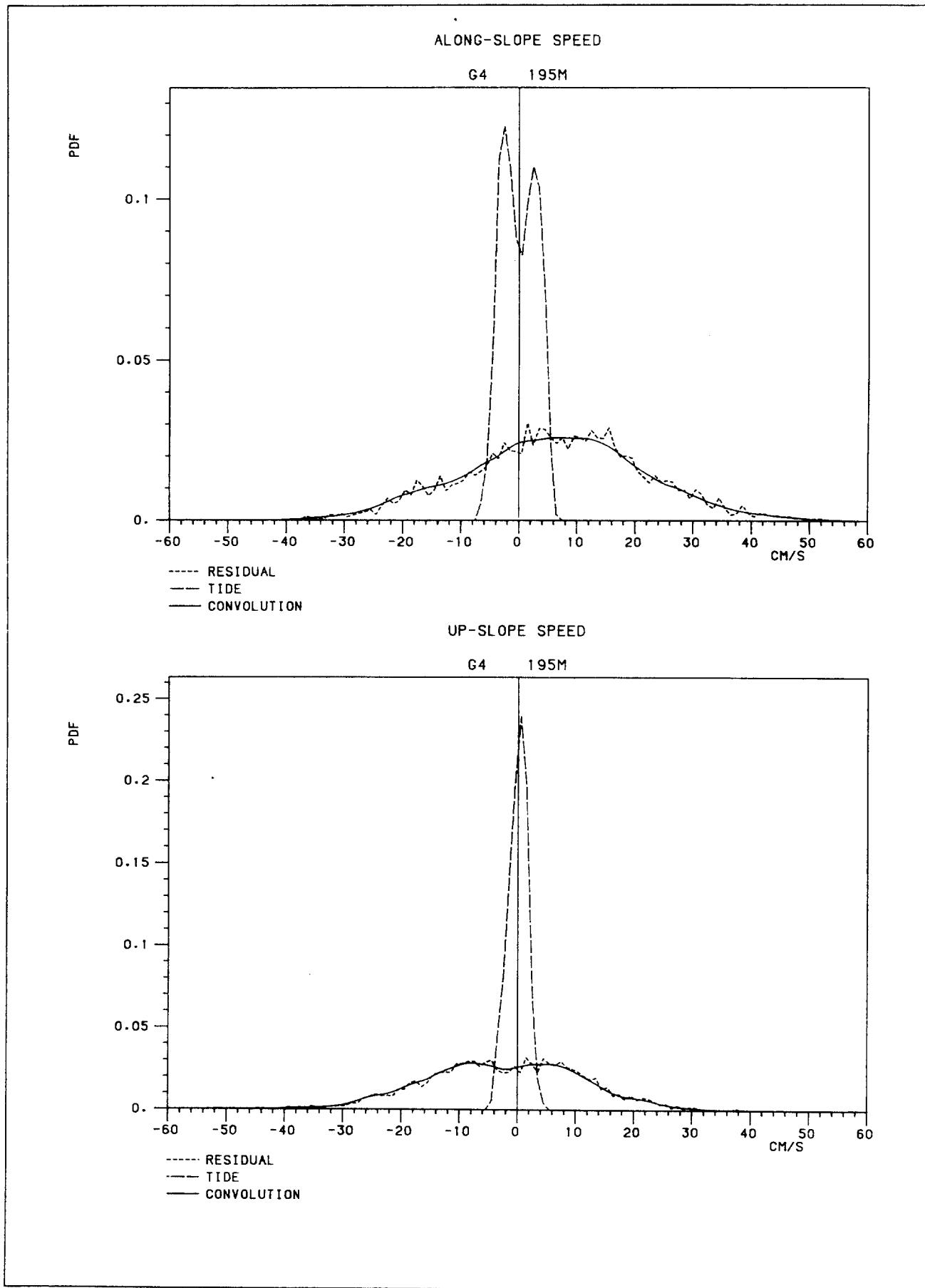


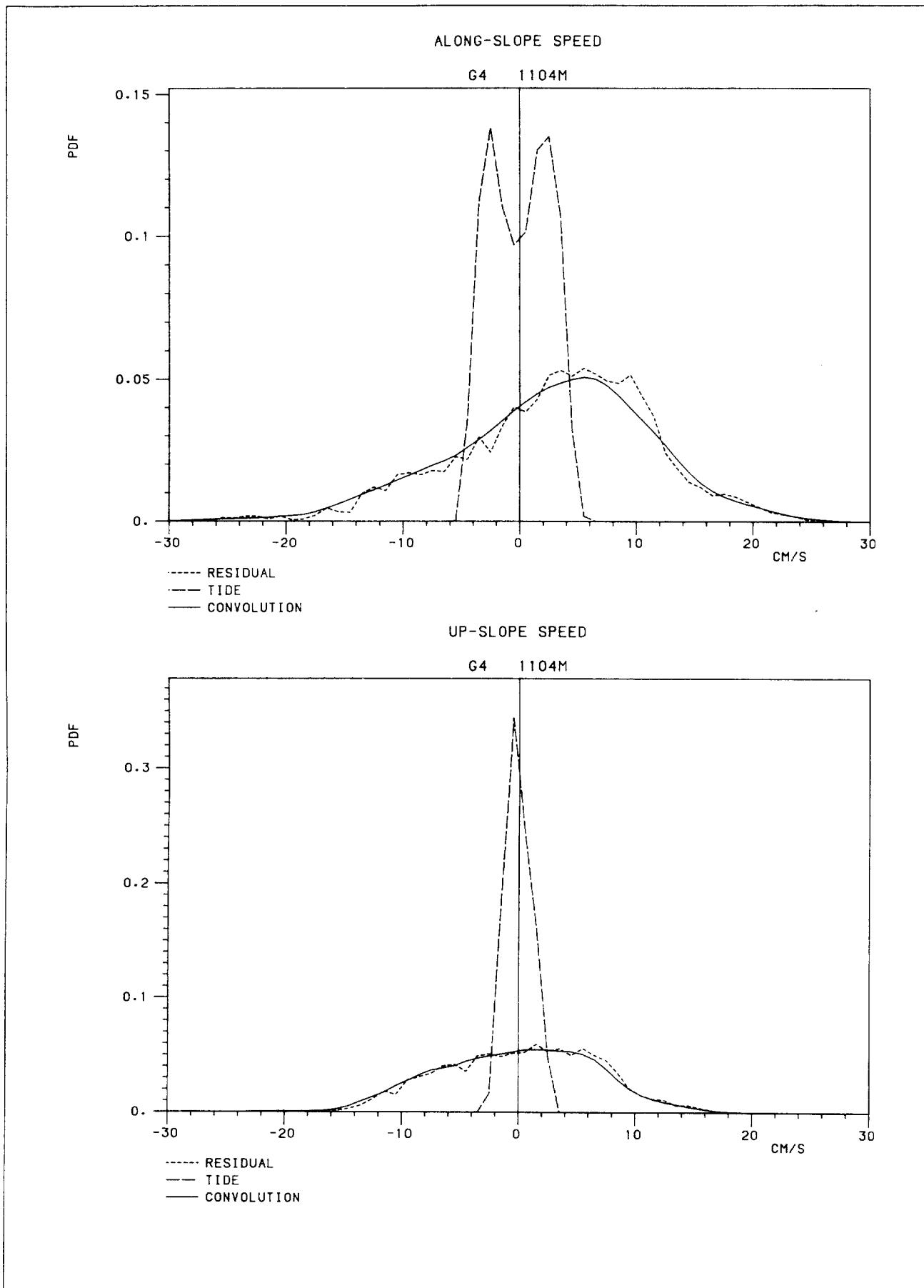


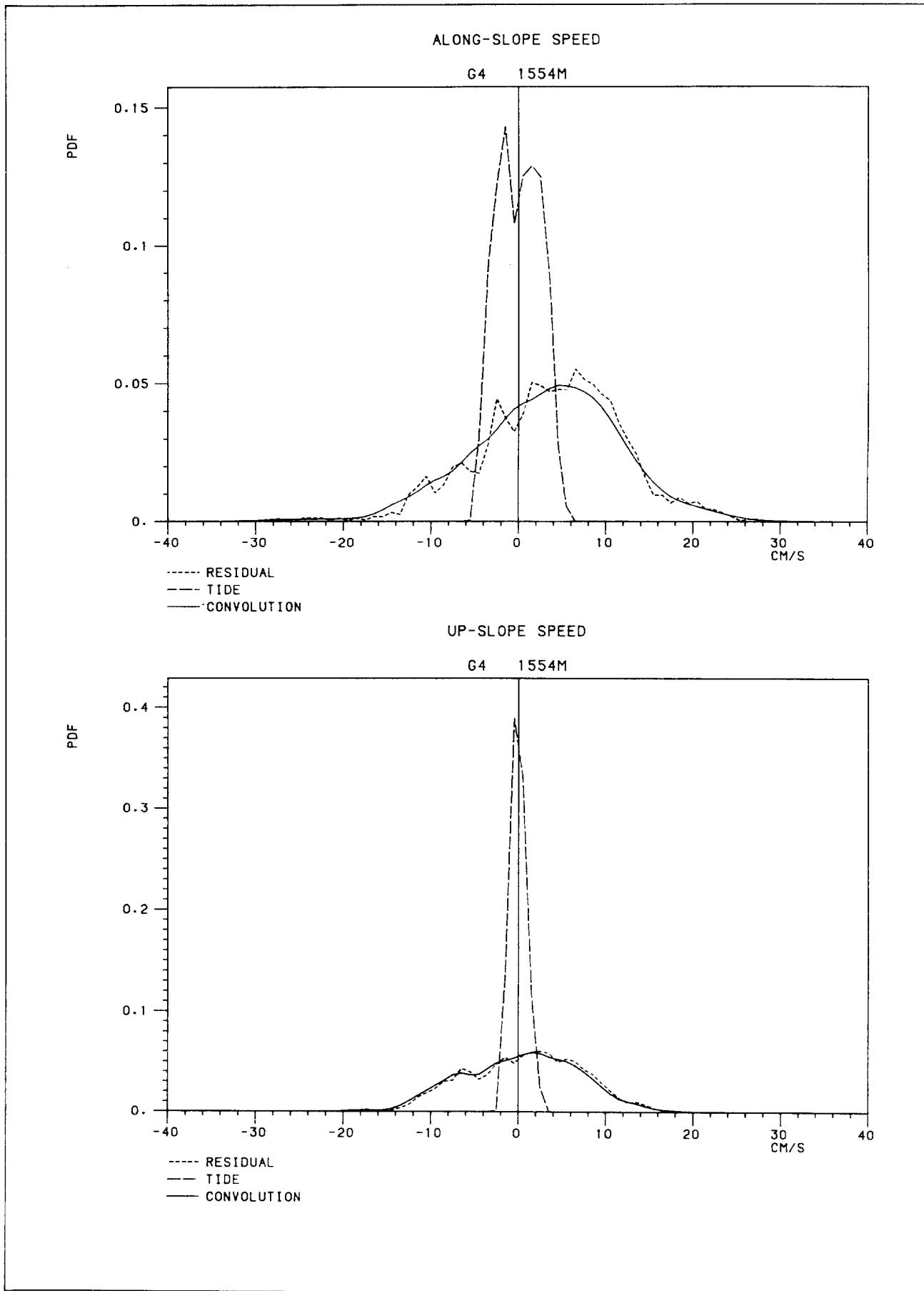


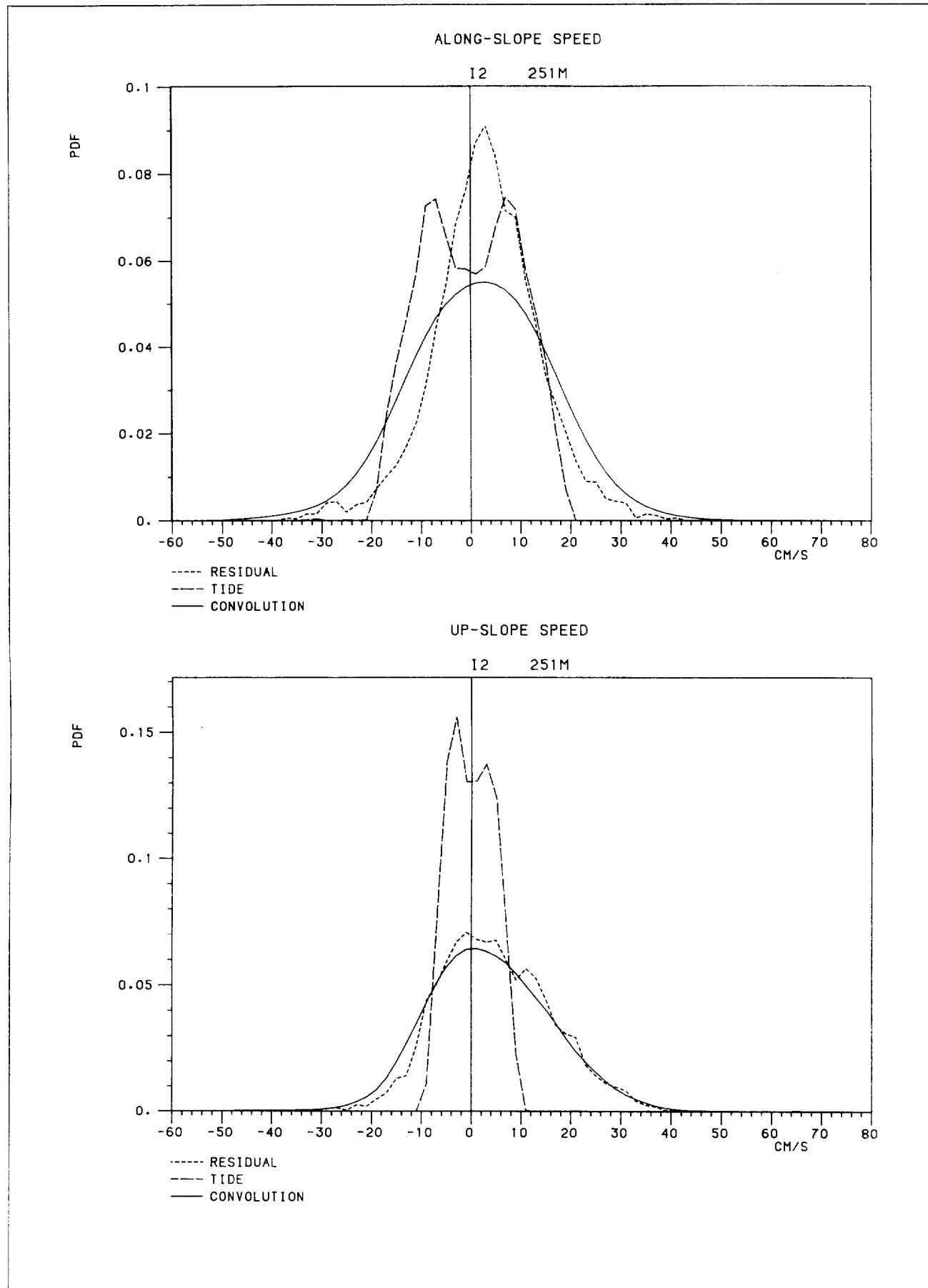


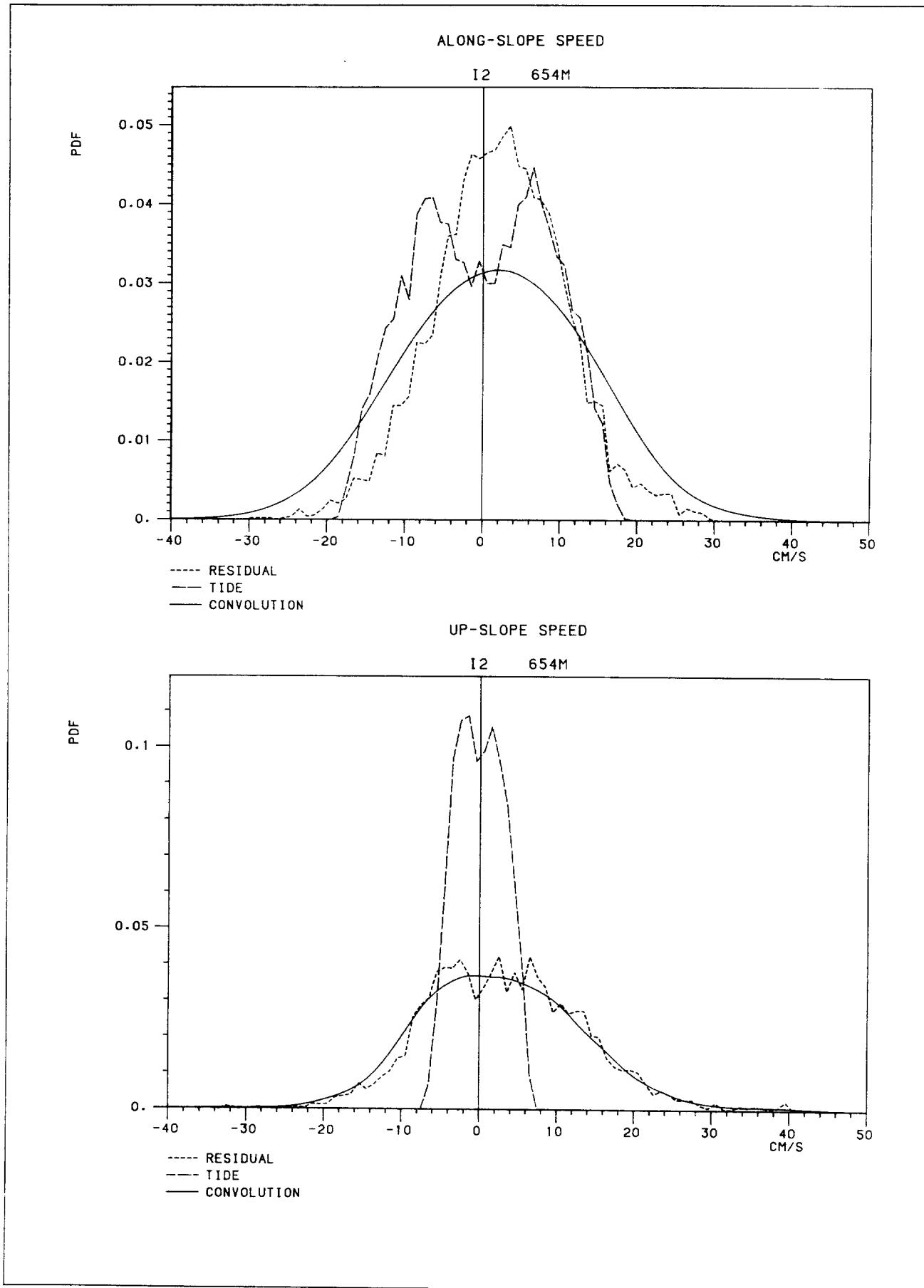


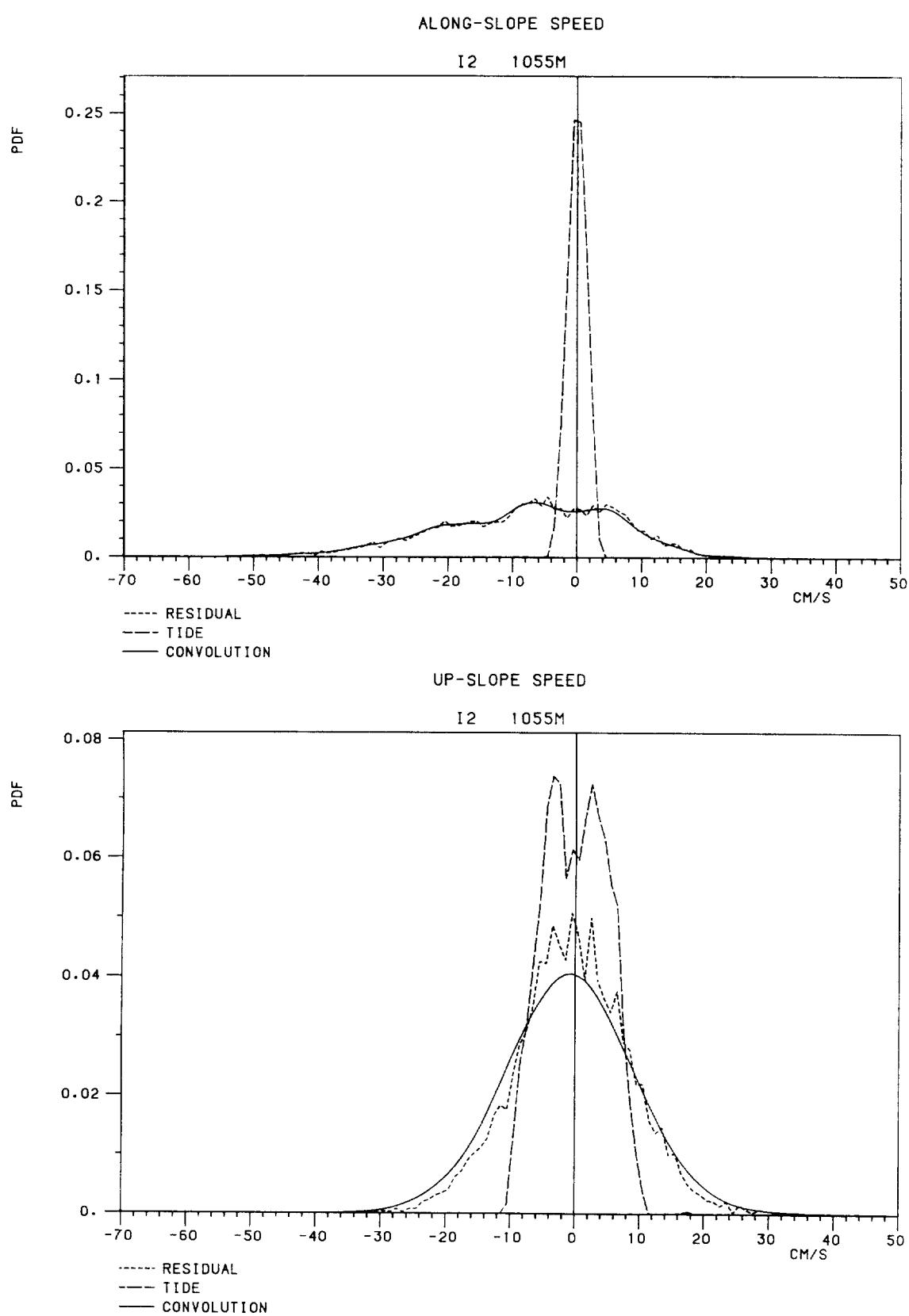












2.2 50-year return value of resolved speed

Defining the 50-year return value of hourly mean speed, U_{50} , as that which is exceeded on average once in 50 years, then it is given by

$$\text{Prob}(U_{50} < U) = 1 - 1/(365.25 \times 24 \times 50)$$

i.e.

$$\text{Prob}(U_{50} < U) \approx 0.99999772 \quad (3)$$

Hence U_{50} may be calculated given the distribution p_{t+r} - or rather two values, one from each tail of p_{t+r} , giving the 50-year speed in opposite directions.

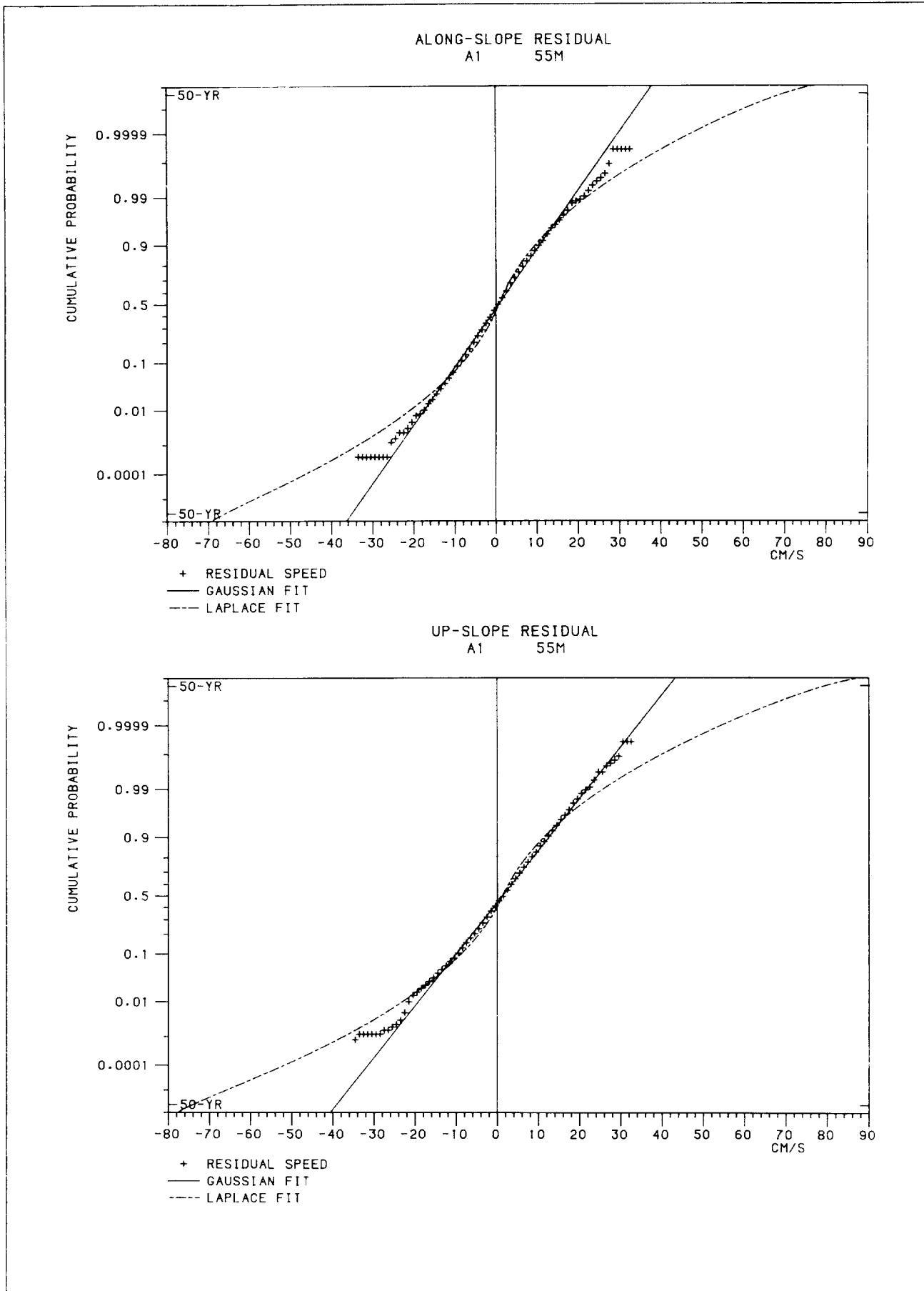
With the definition for U_{50} , in terms of only the average interval between exceedances, its value is not affected by any correlation between the data. However, given positive correlation between successive hourly mean values, exceedances of U_{50} will tend to come together, while maintaining the average interval between exceedances of 50 years. So if the 50-year return value is defined as that which is exceeded at least once during one year in 50, then it would have a slightly lower value than that given by (3). However, Pugh and Vassie (1980) examined the effect of correlation upon estimates of return values of surface elevation and decided that any such reduction would in practice be insignificant.

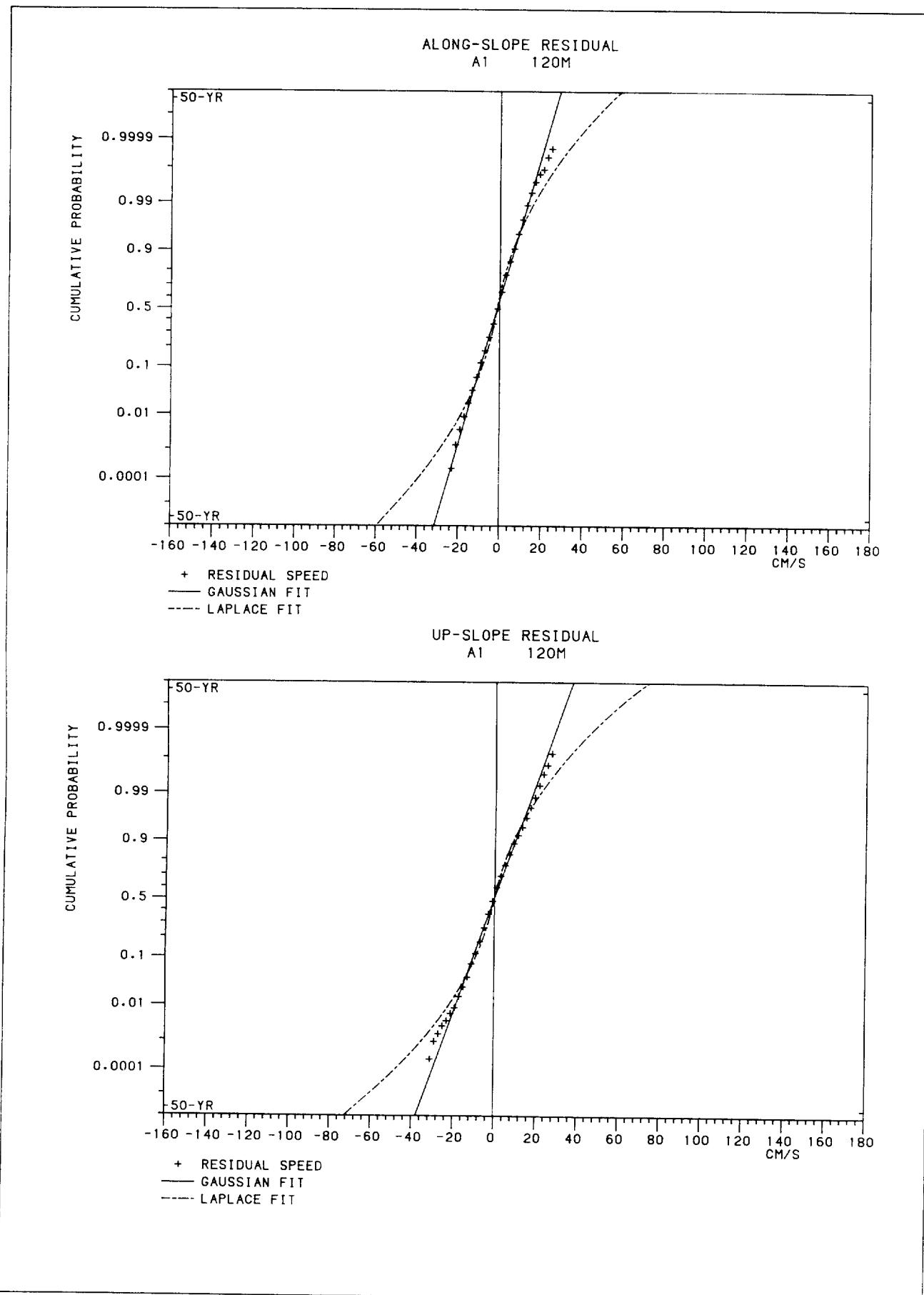
2.3 Probability distribution and extreme value of total speed

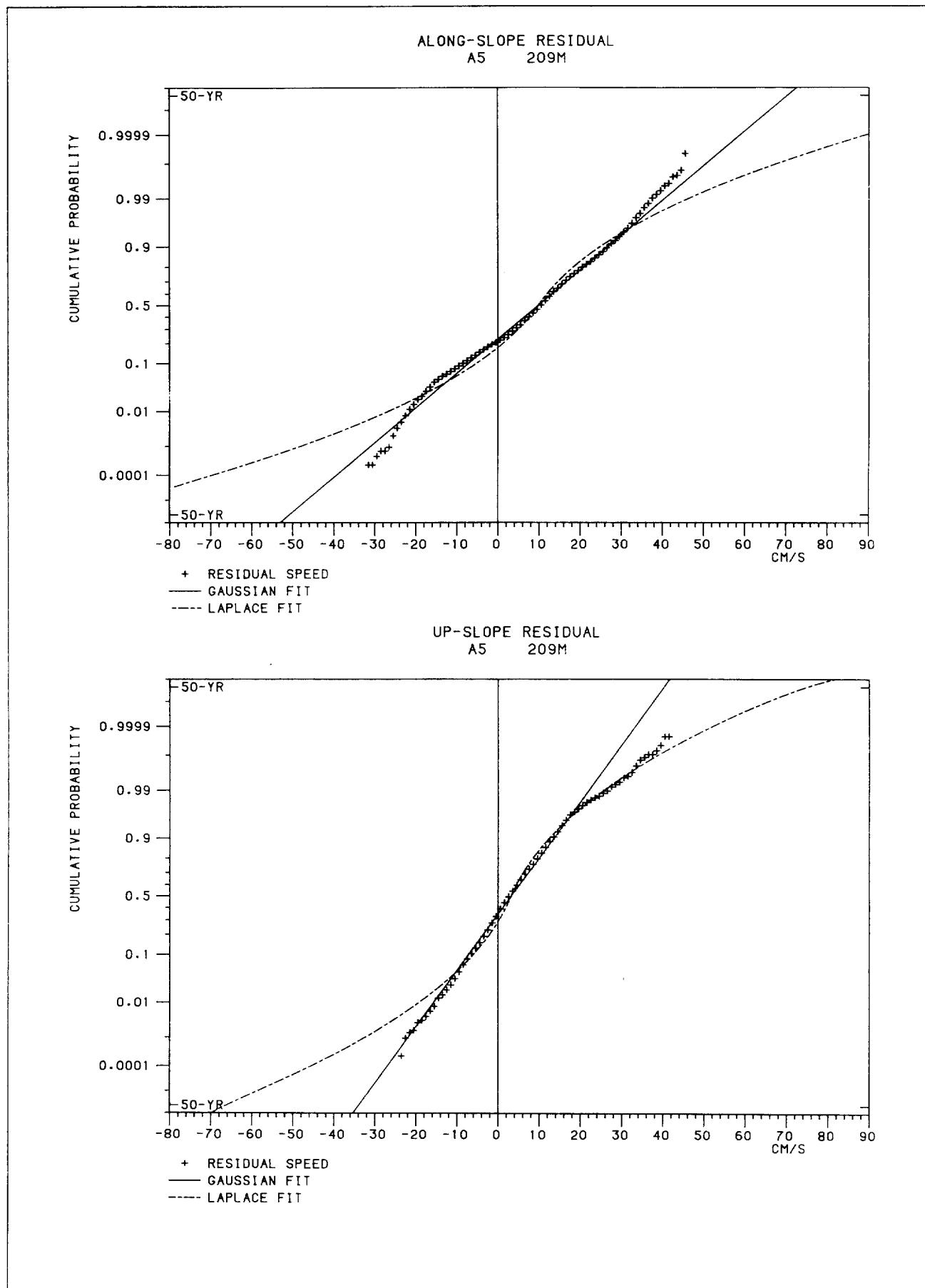
Suppose U and V are current speeds resolved orthogonally so that total speed W is given by

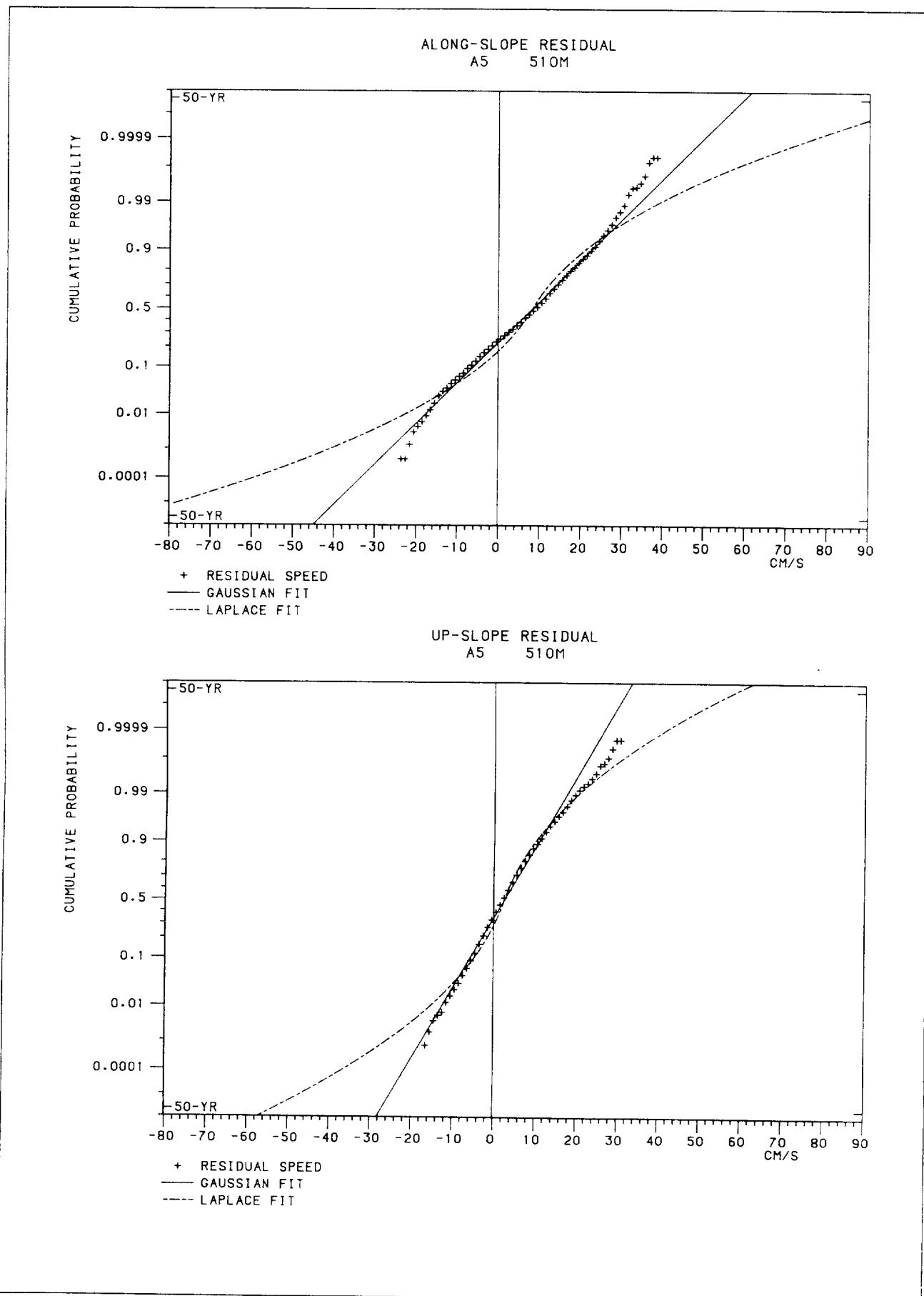
$$W = \sqrt{U^2 + V^2}$$

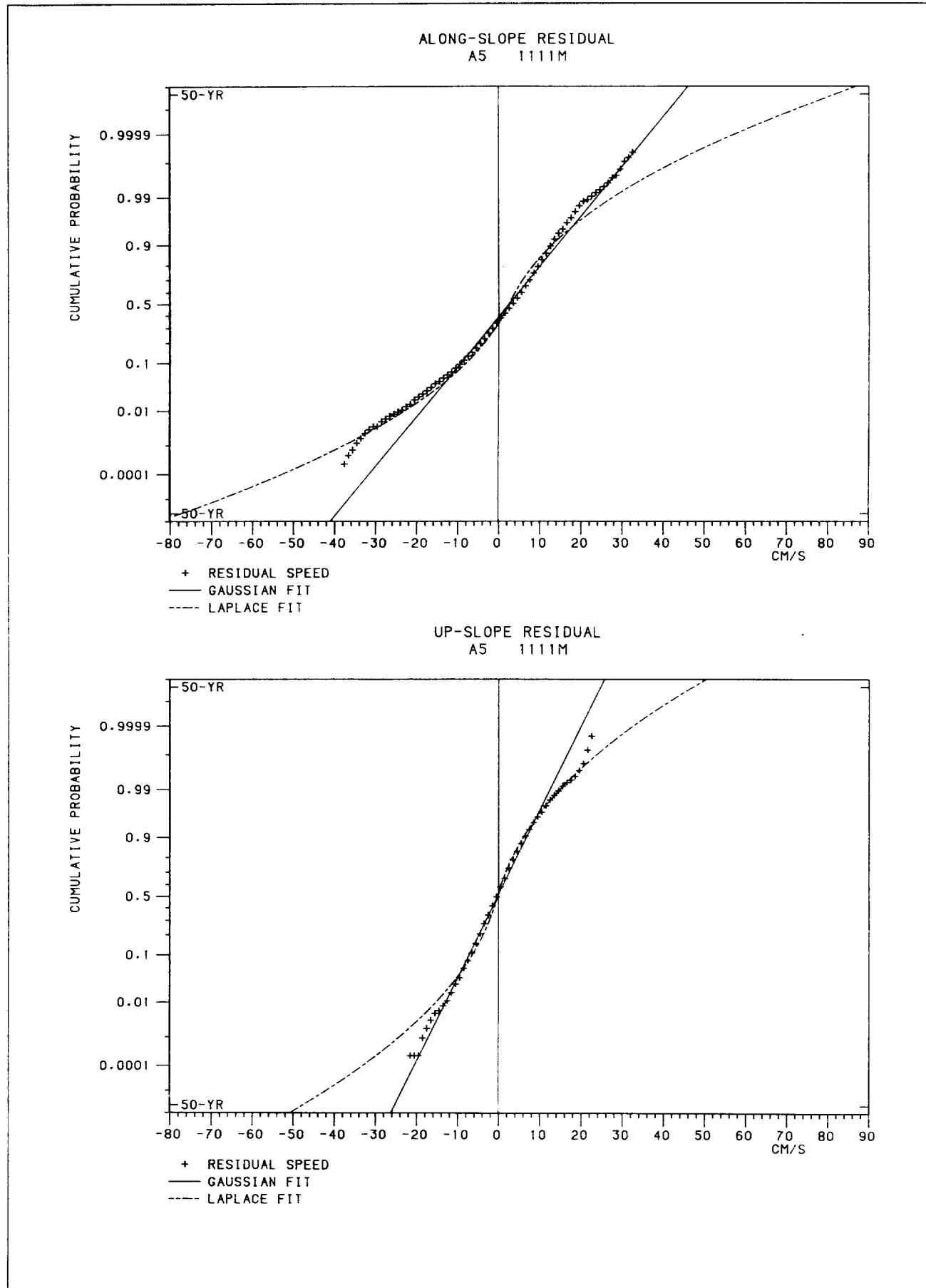
Fig.3: Cumulative probability distributions of residual current speed along-and up-slope from records at each current meter and fitted Gaussian and Laplacian fits. (The meter is identified by the mooring and by the depth of the meter below the sea surface.)

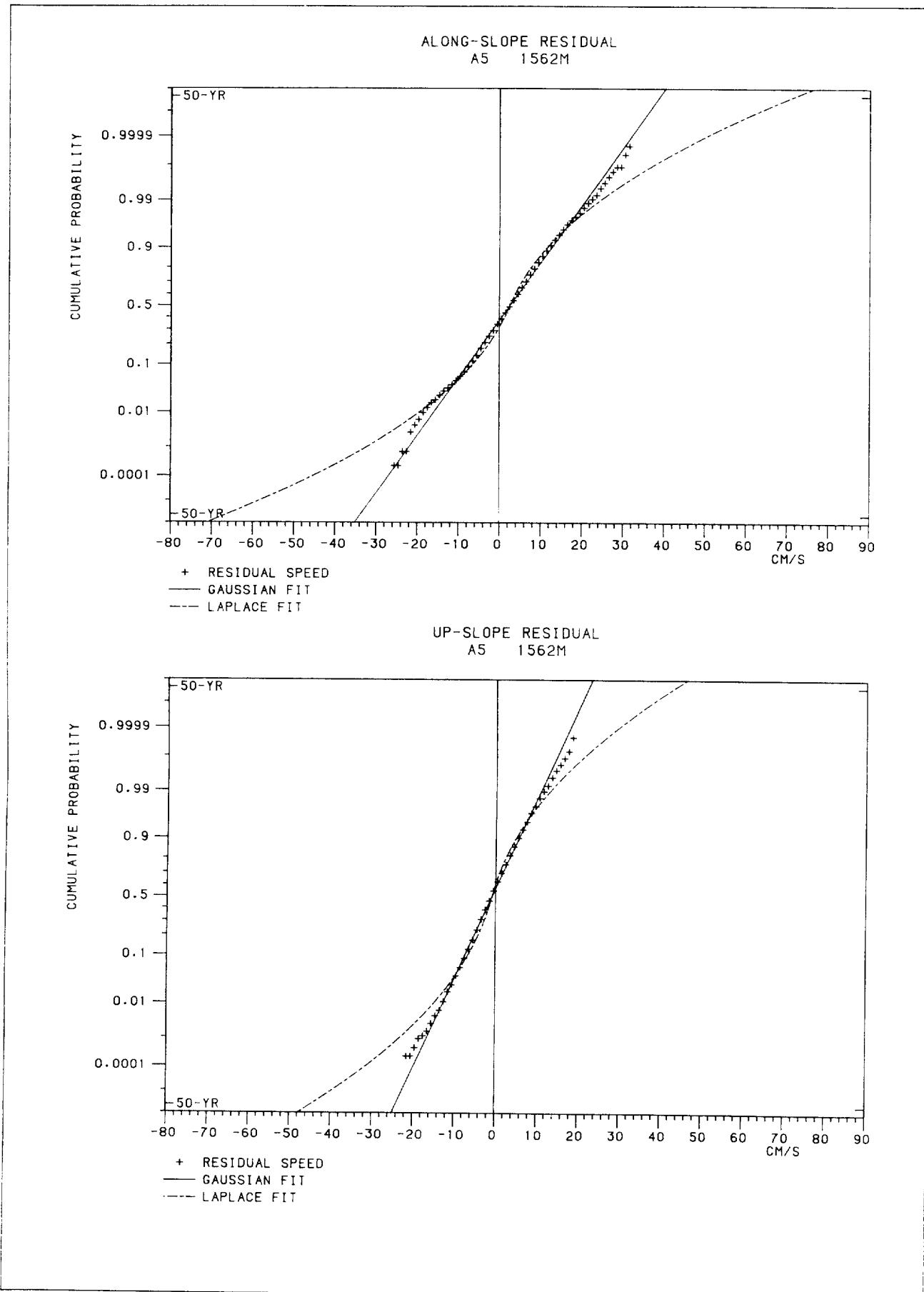


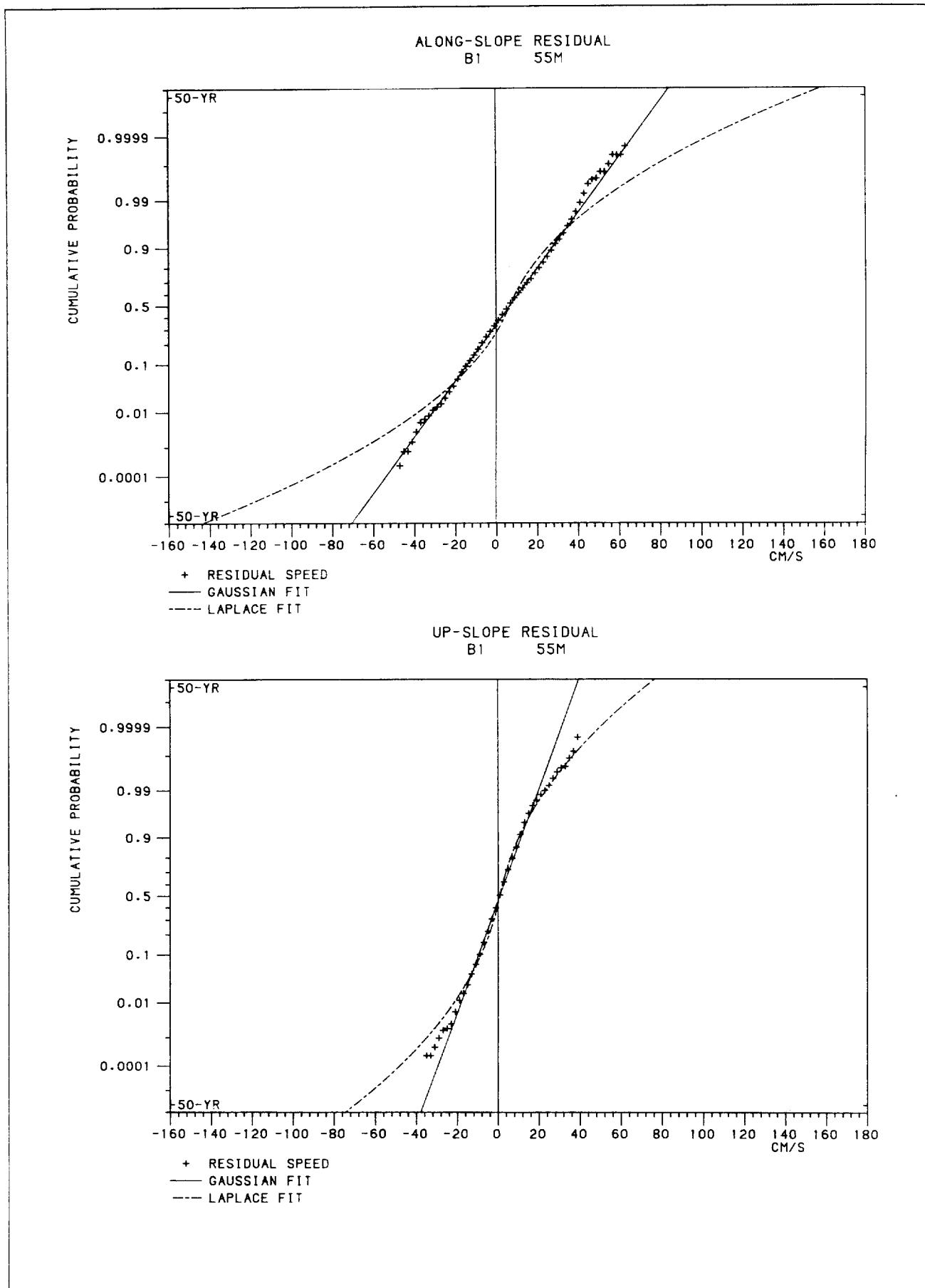


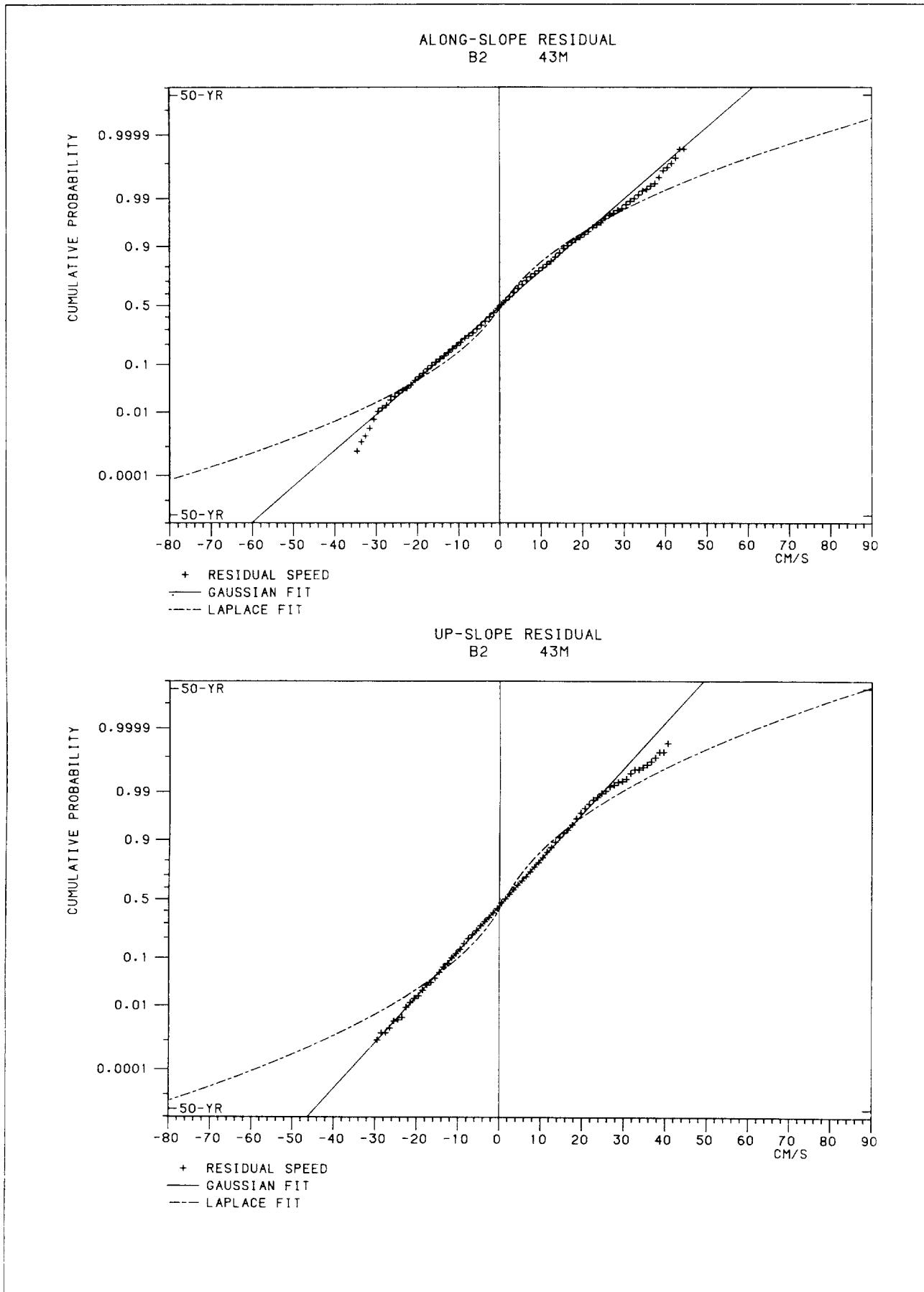


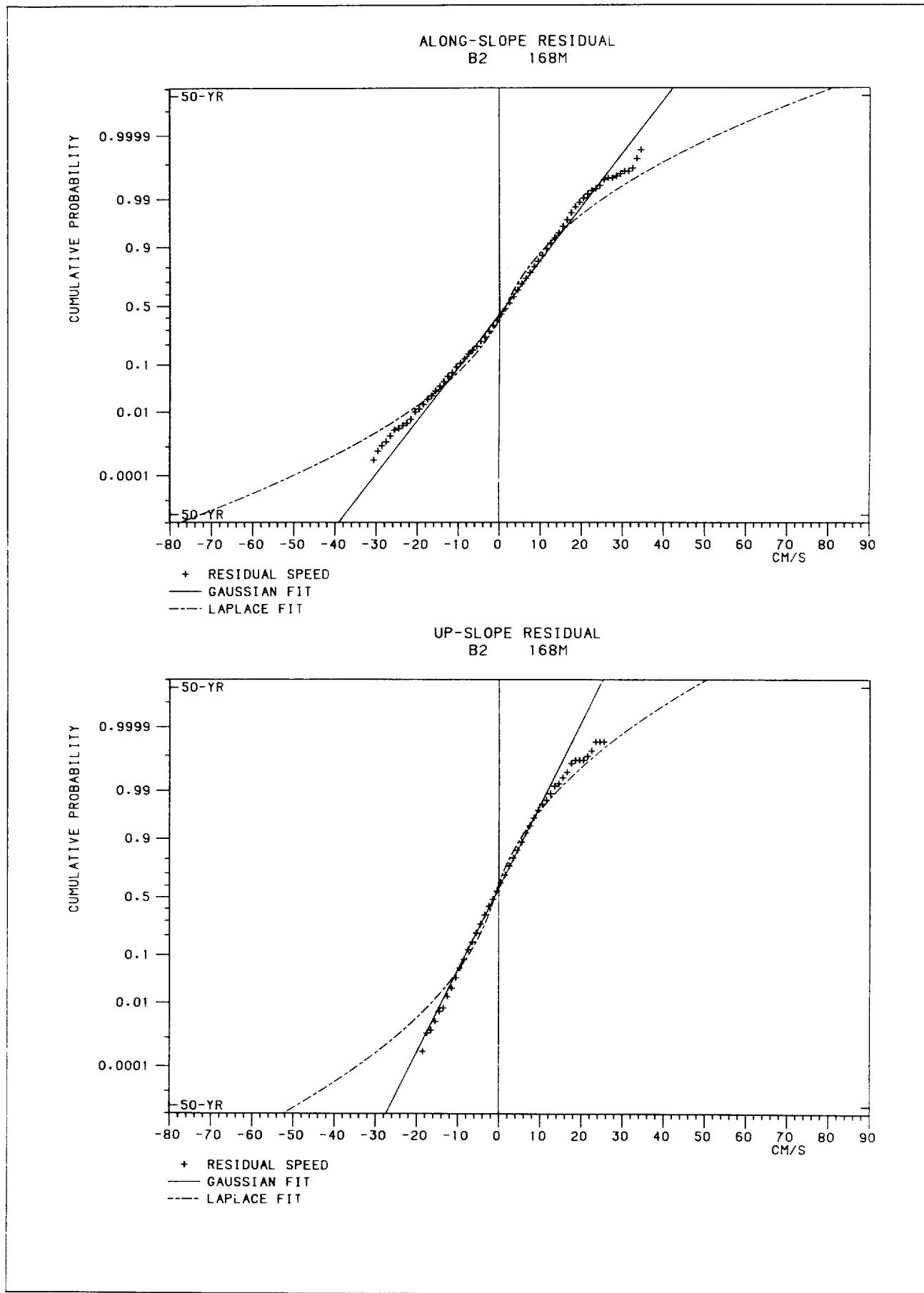


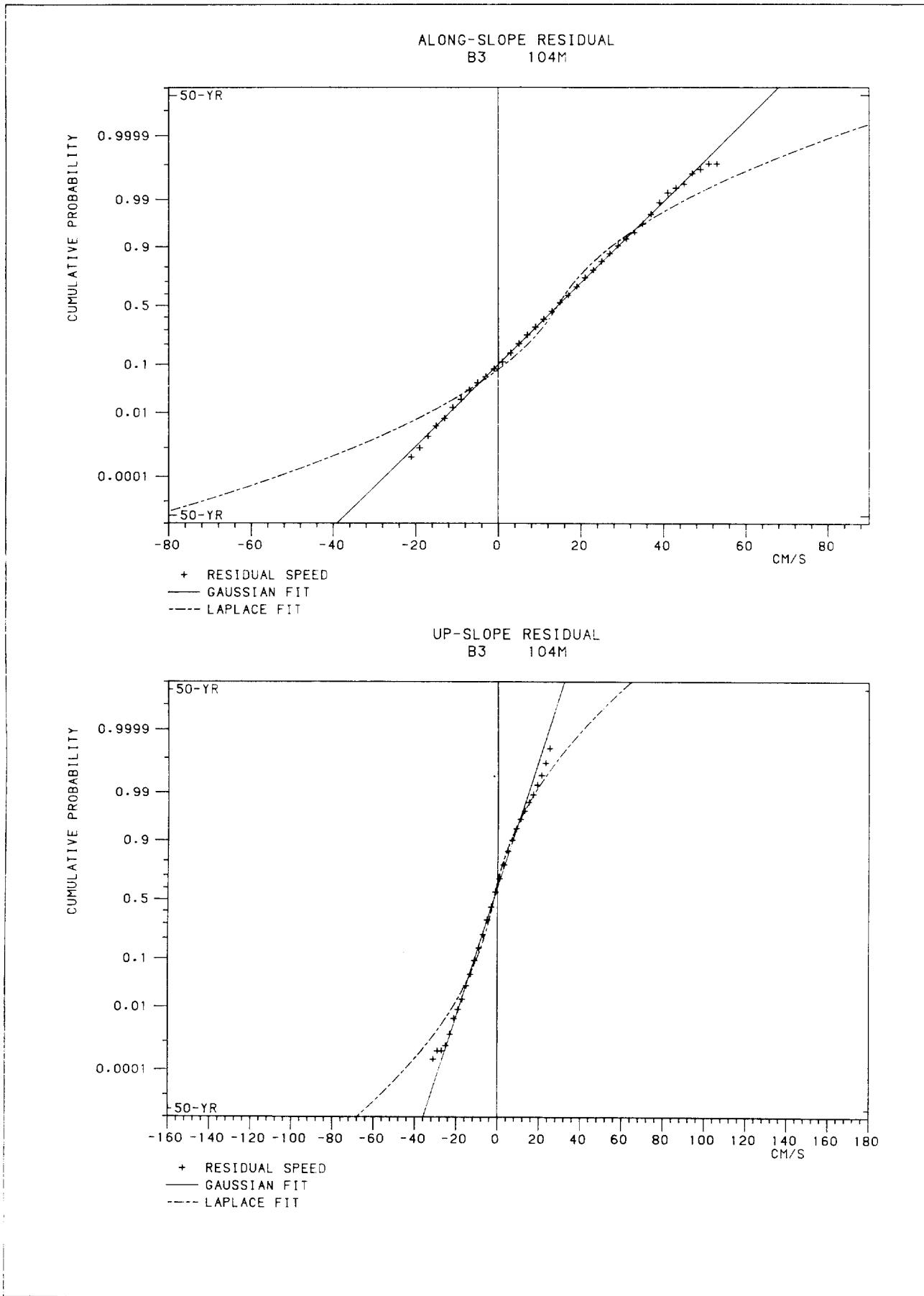


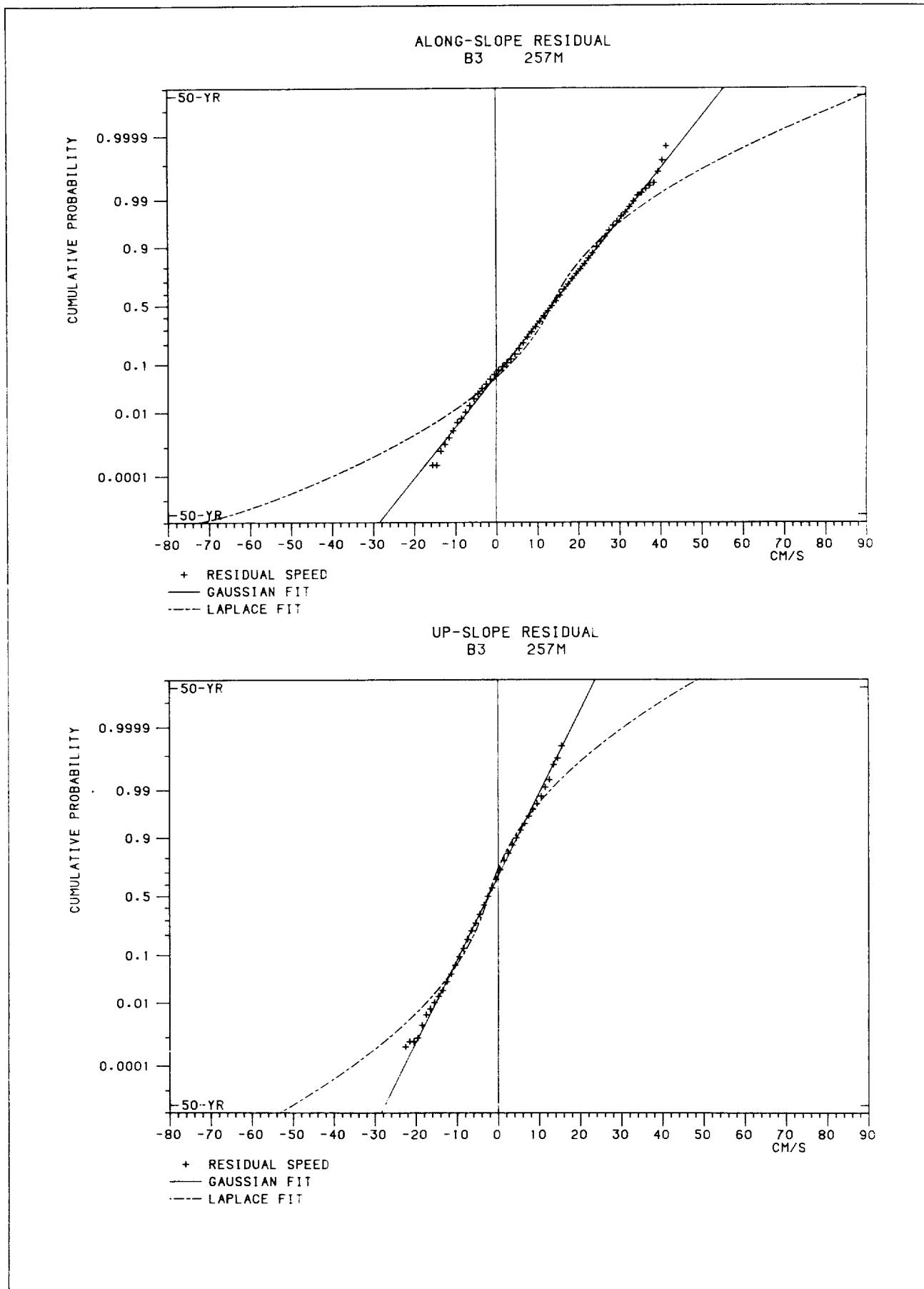


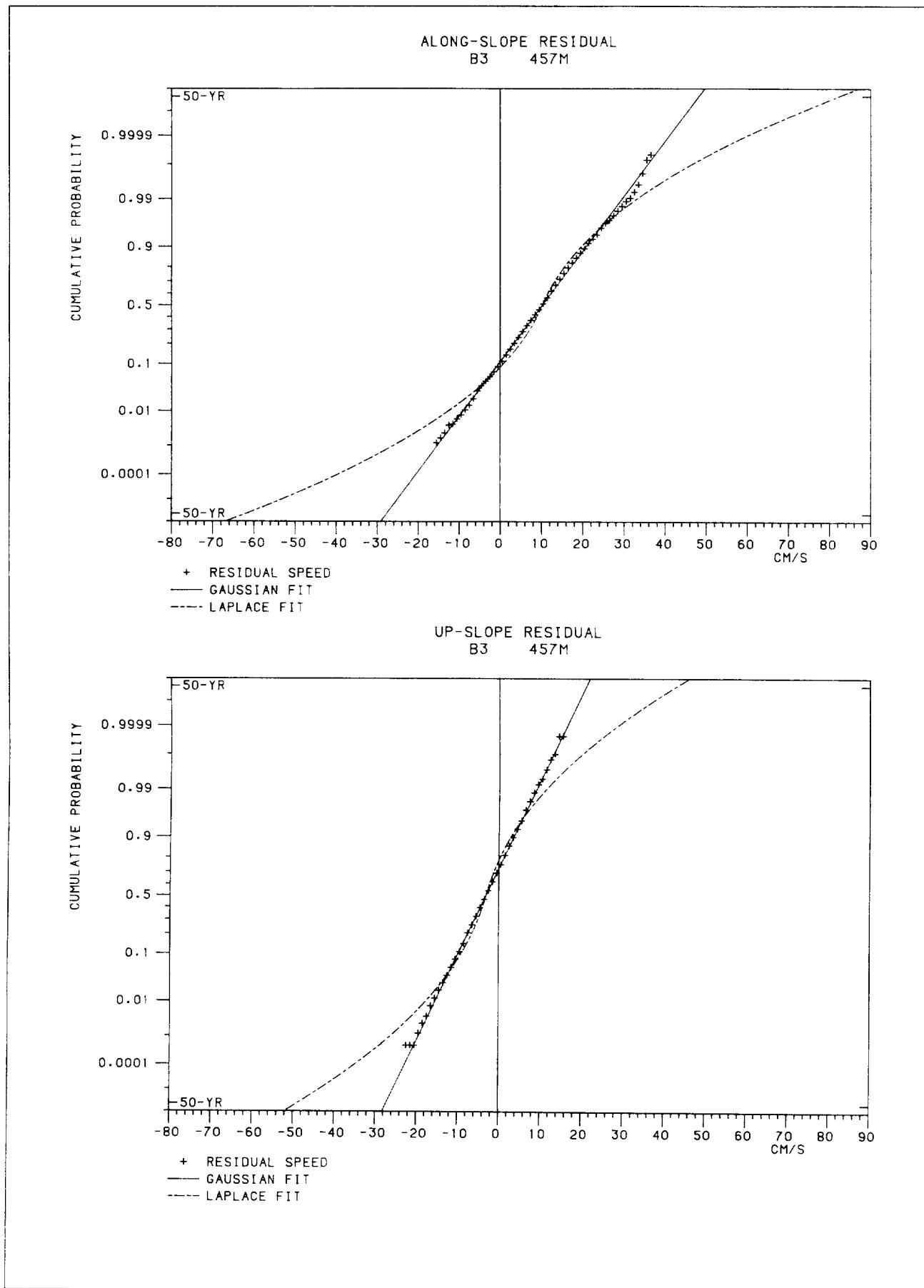


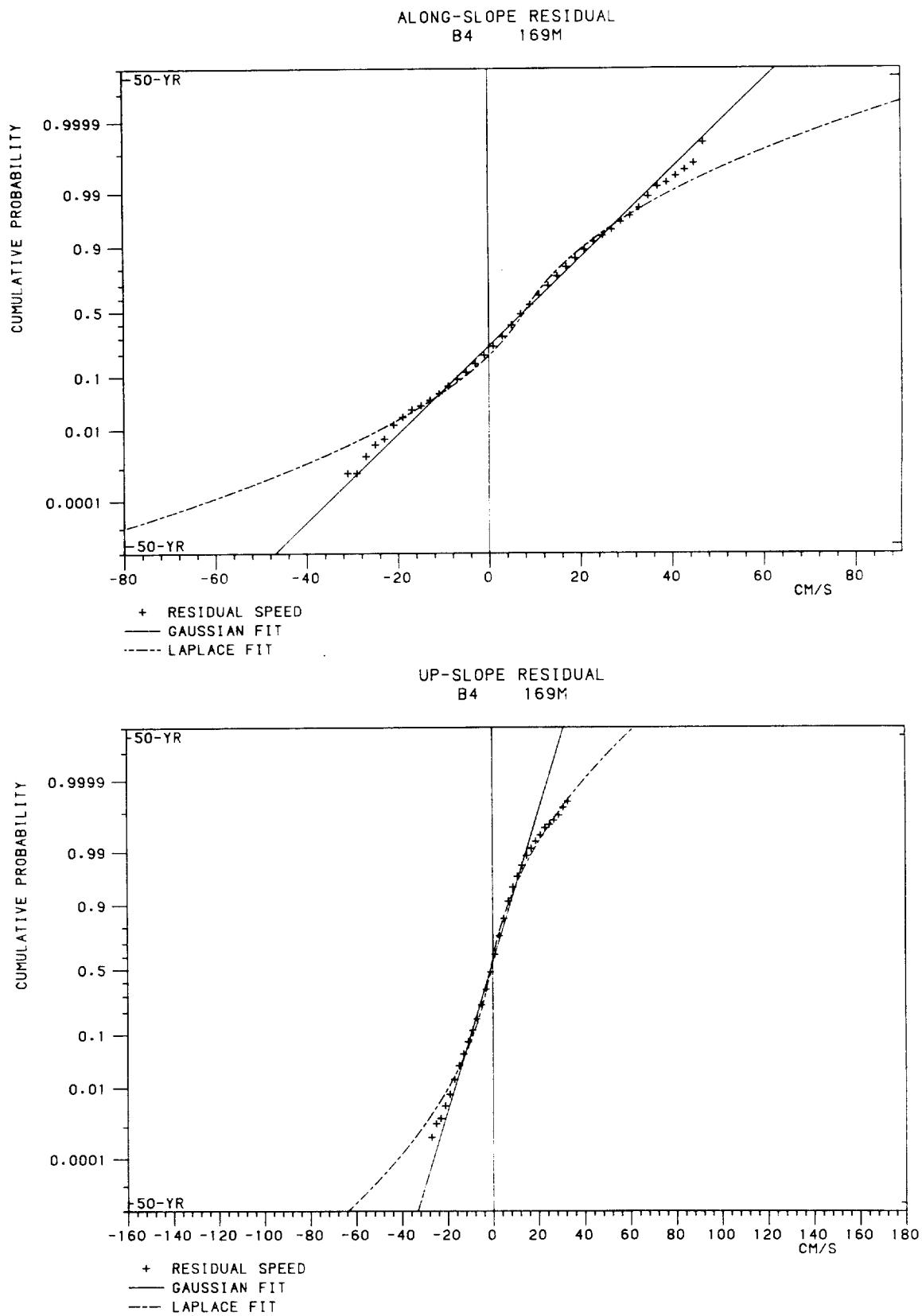


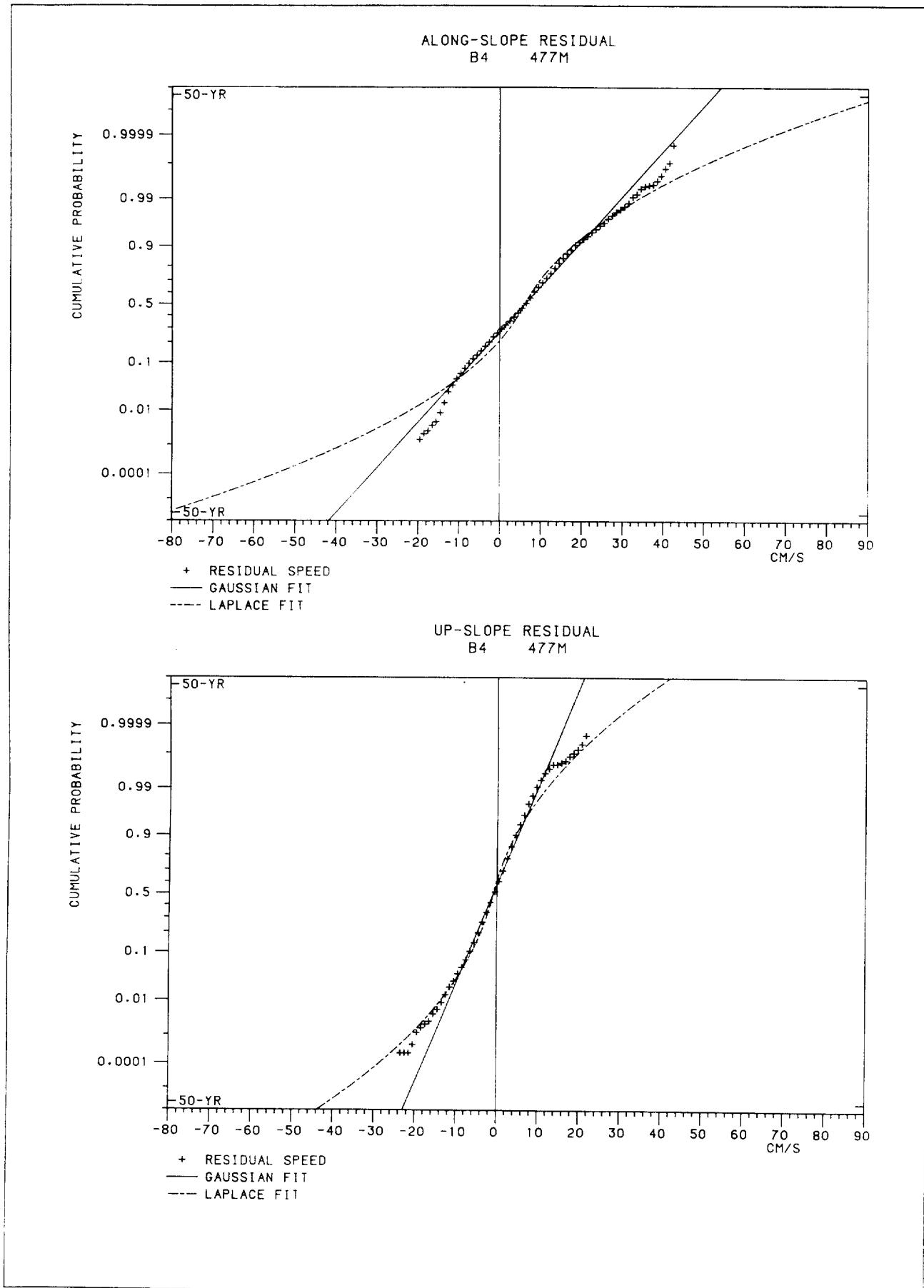


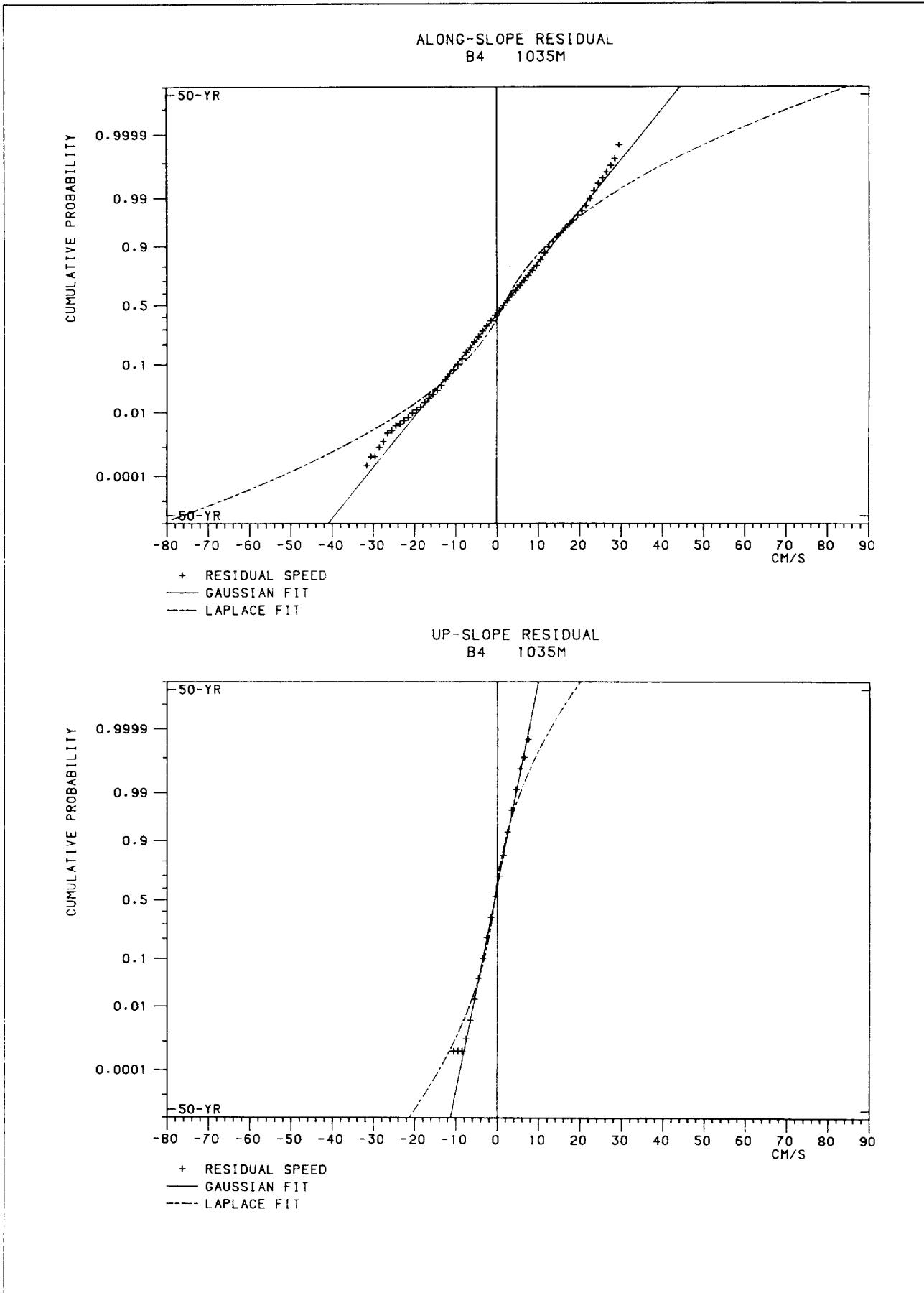


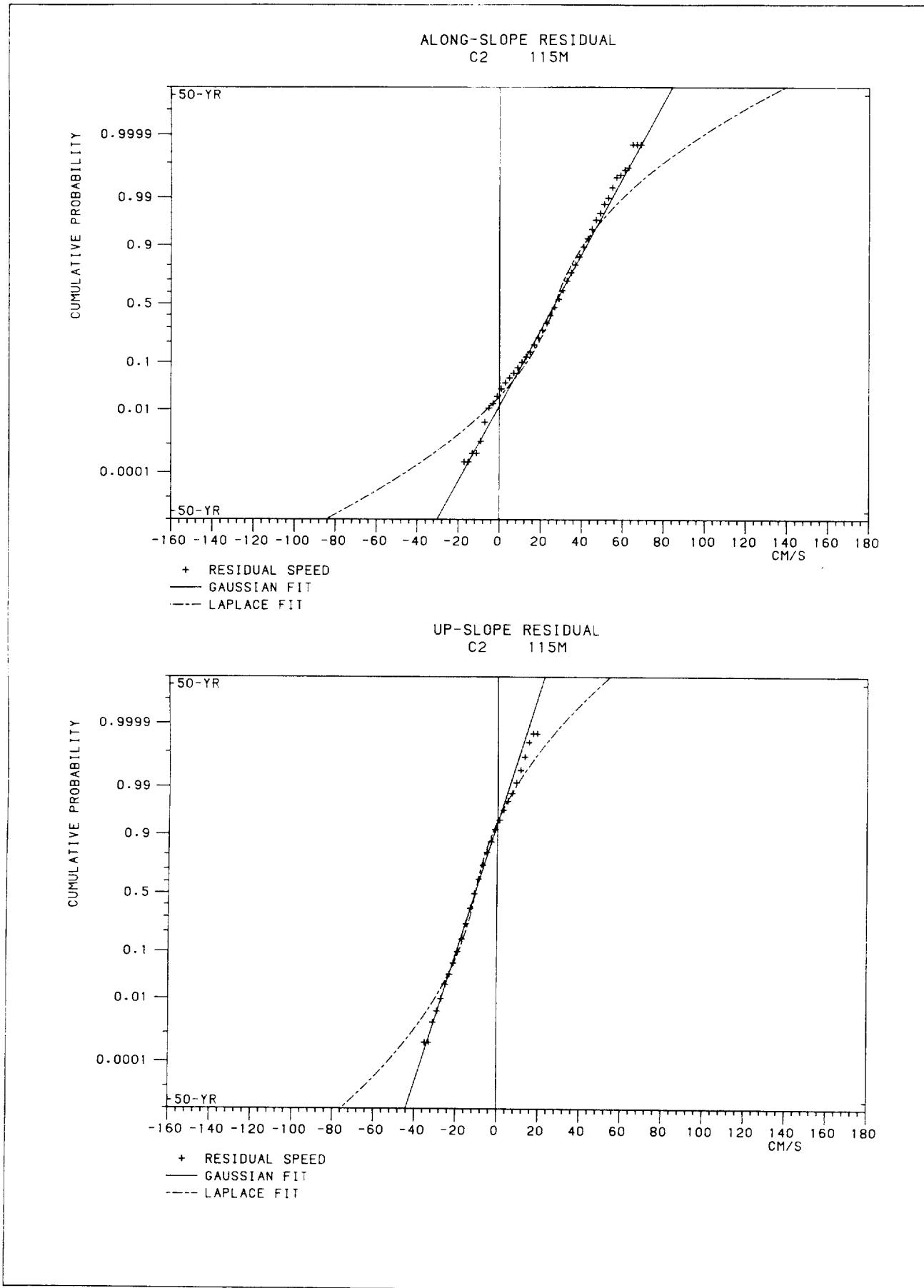


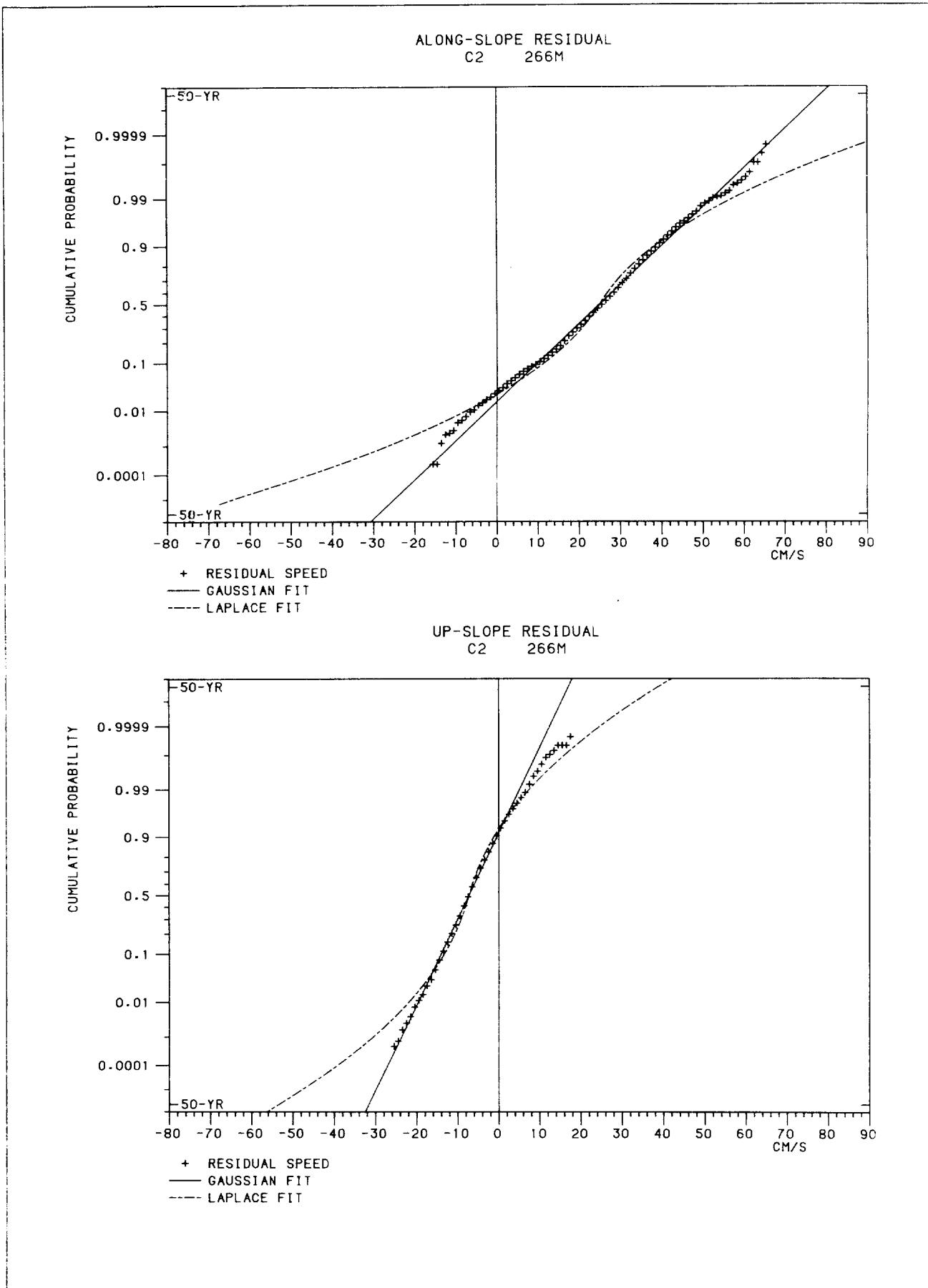


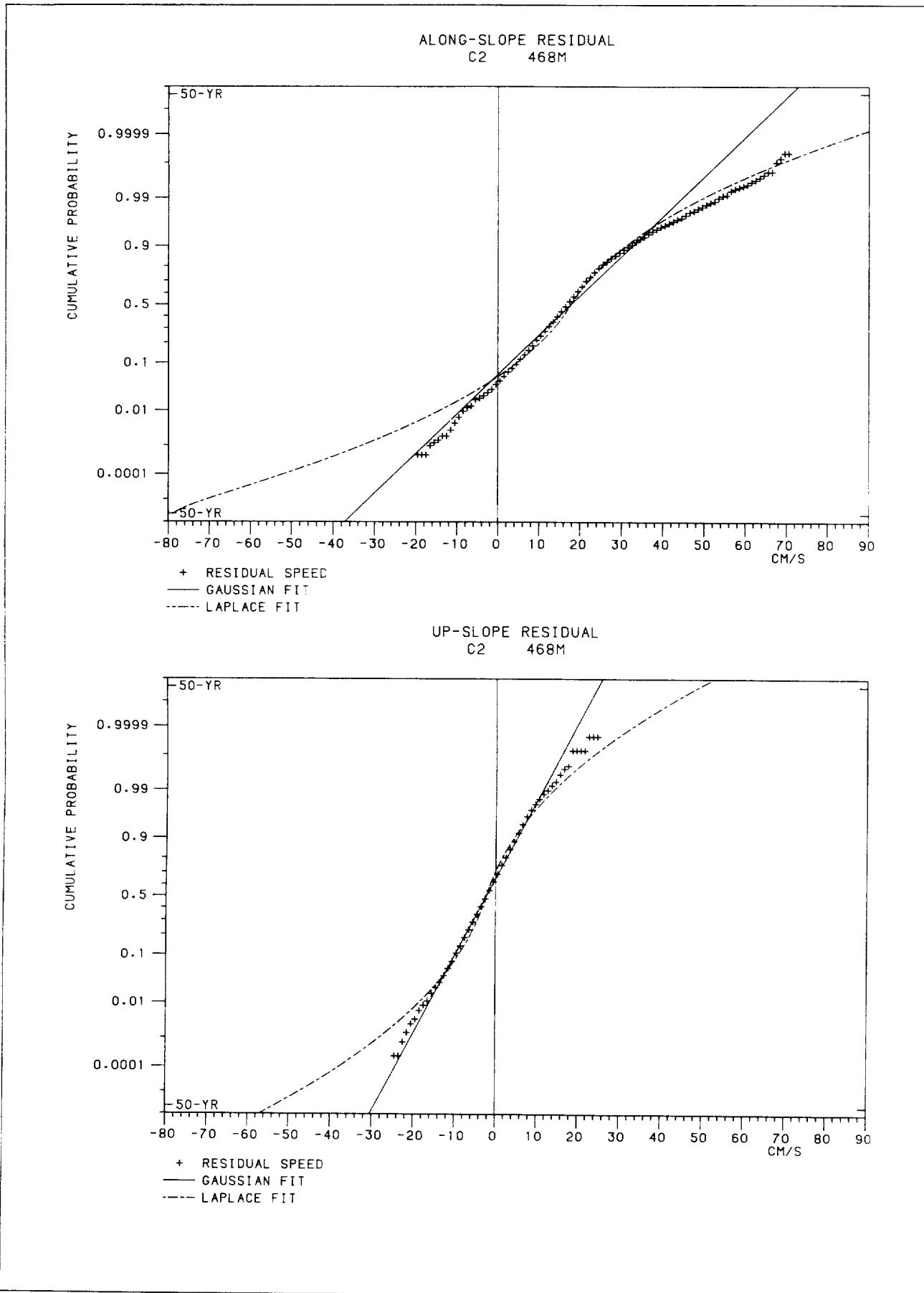


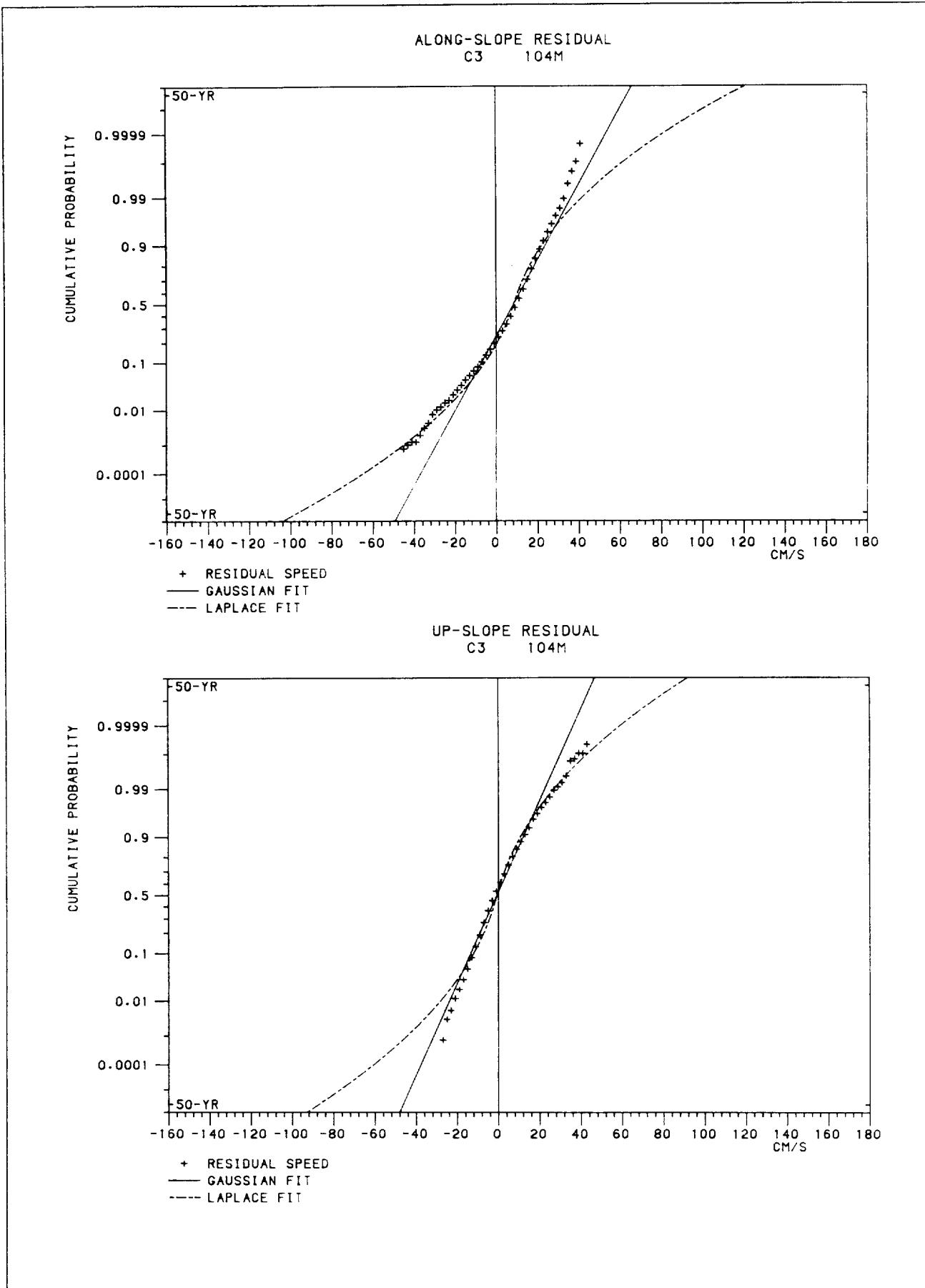


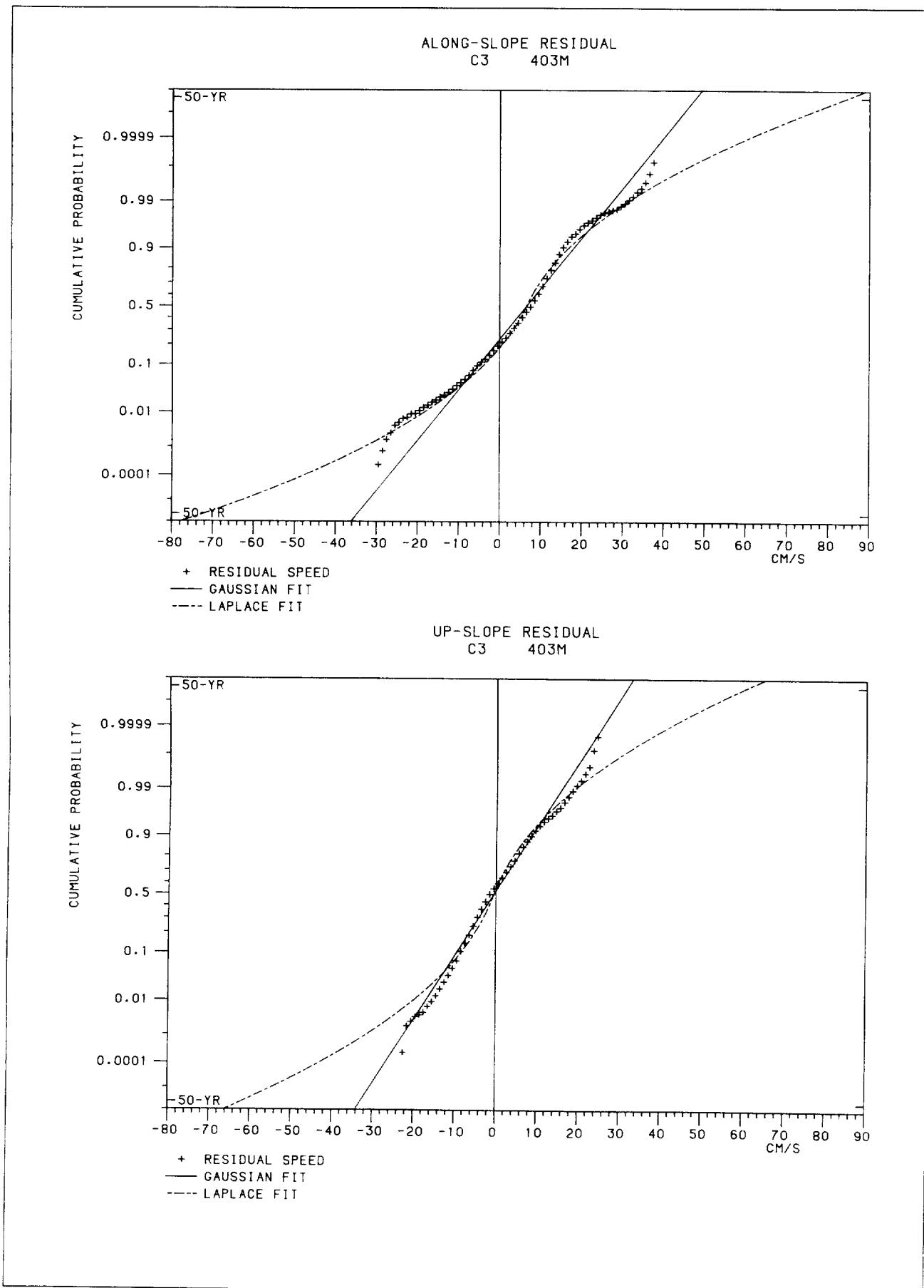


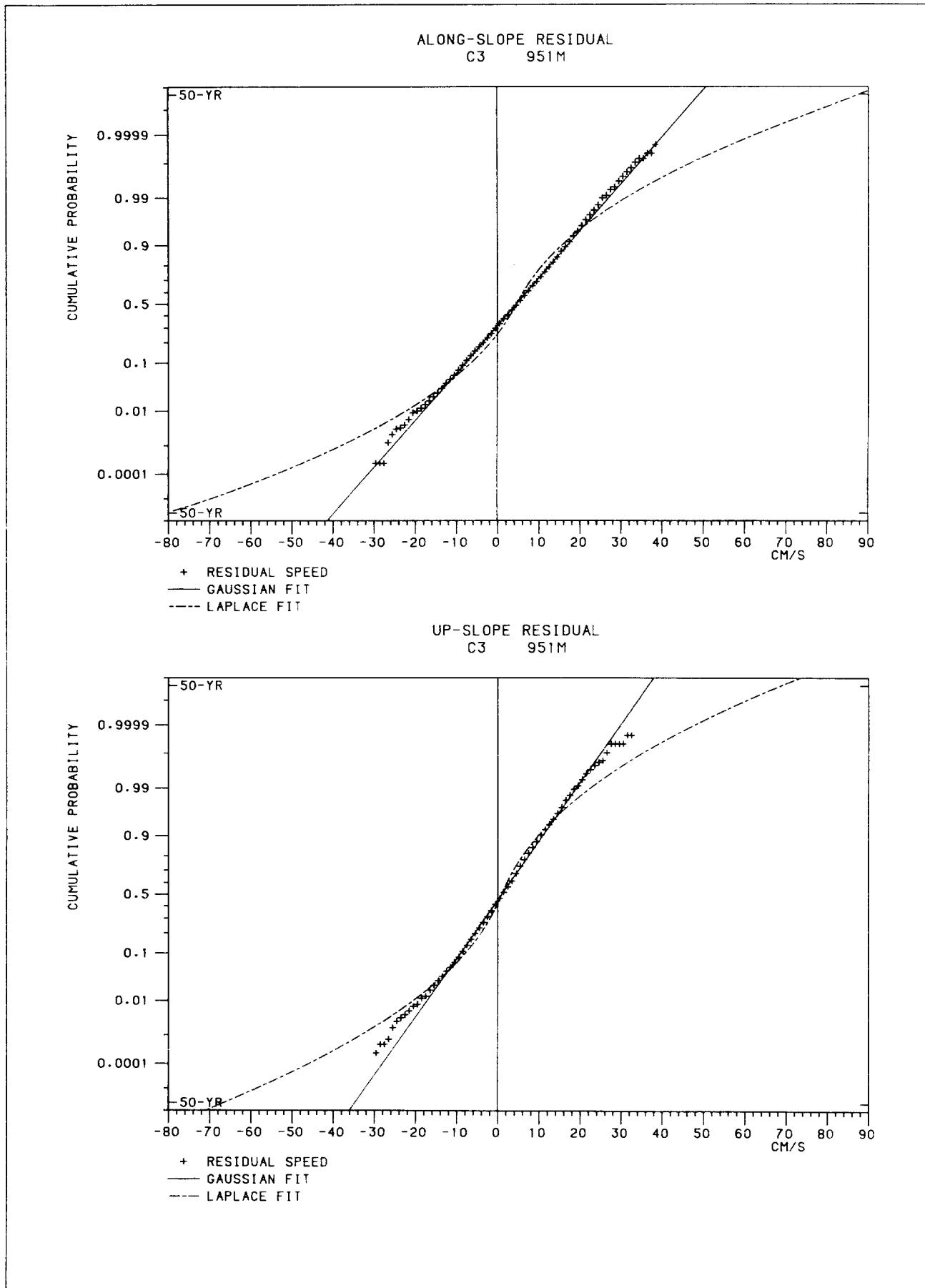


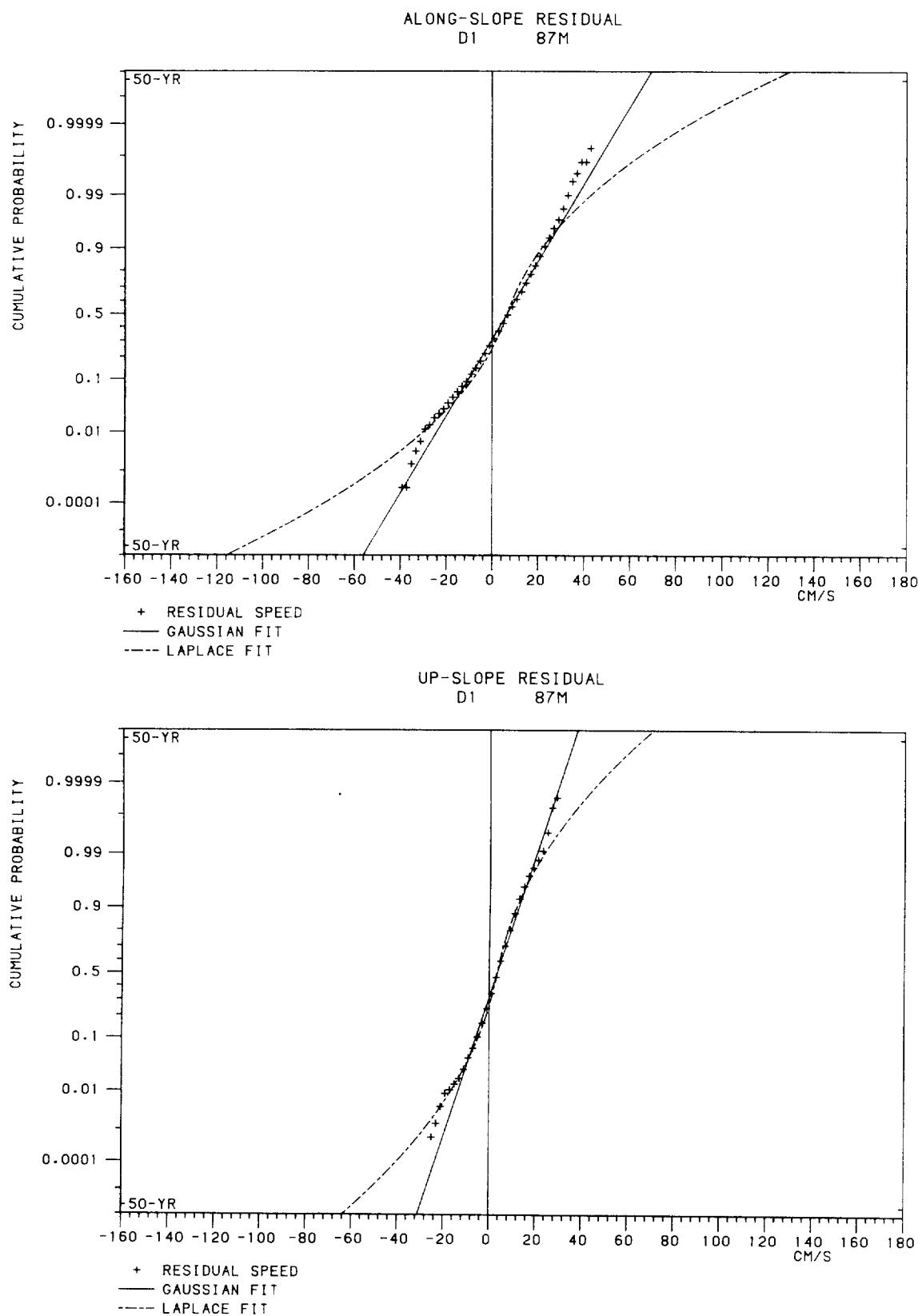


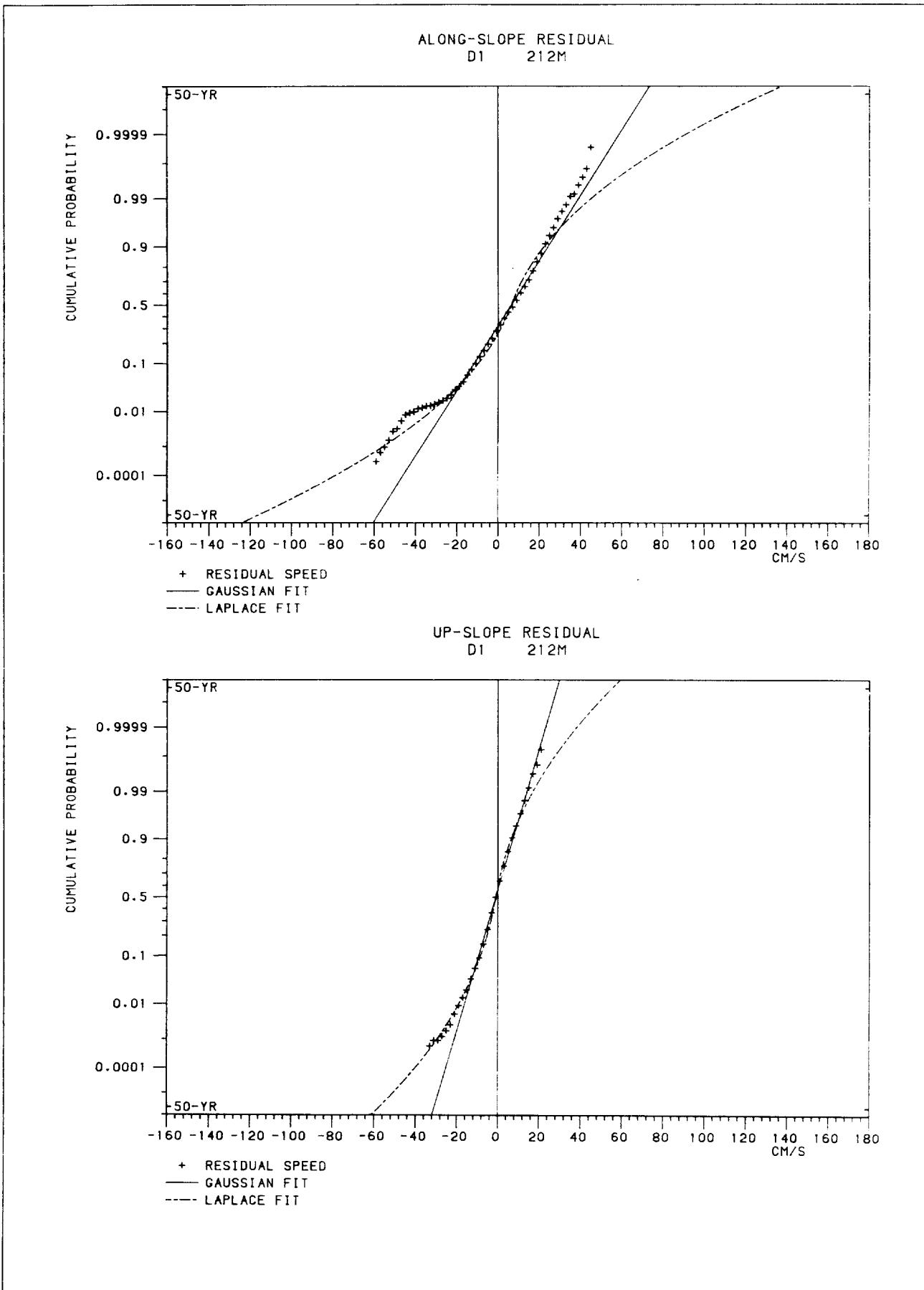


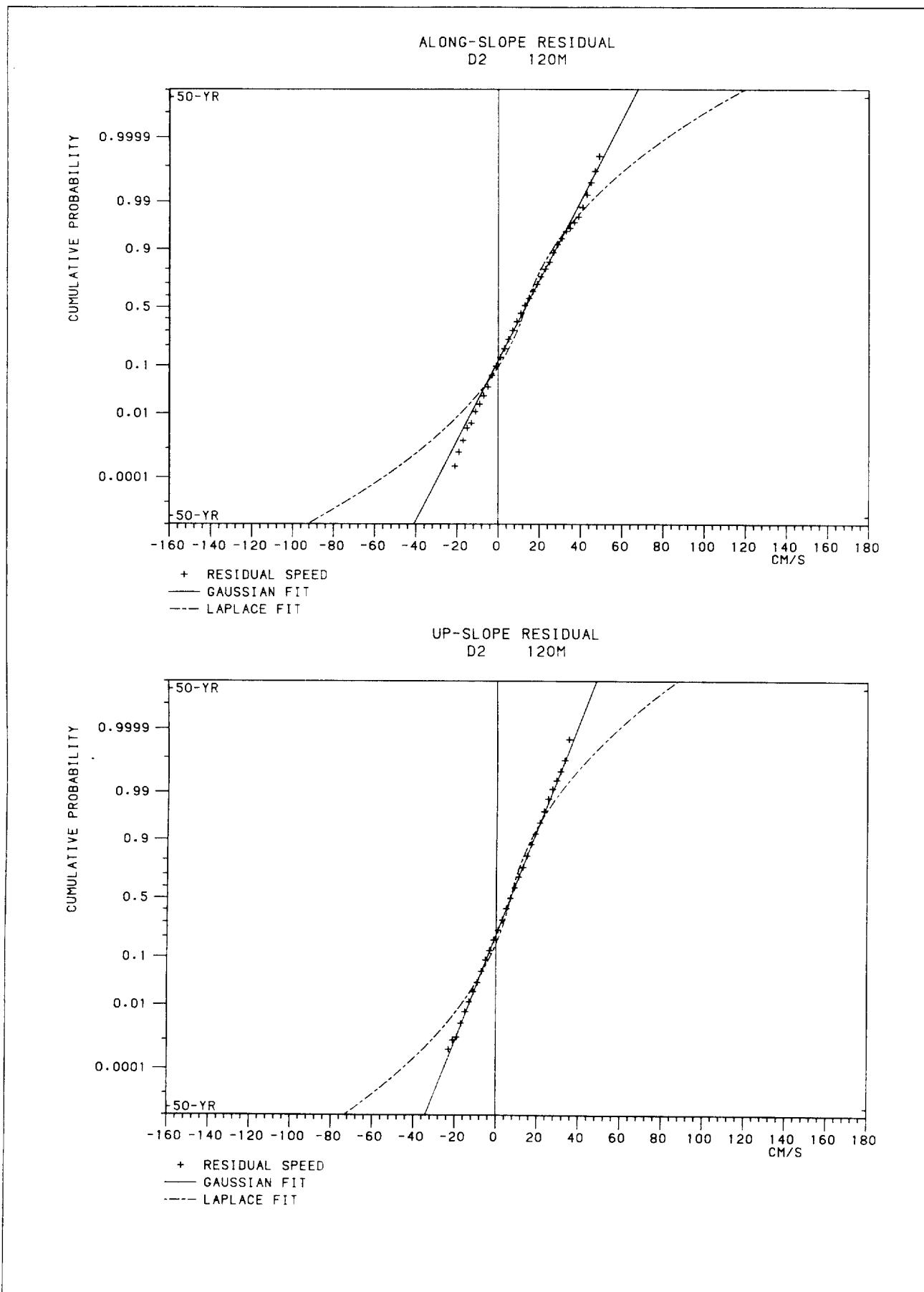


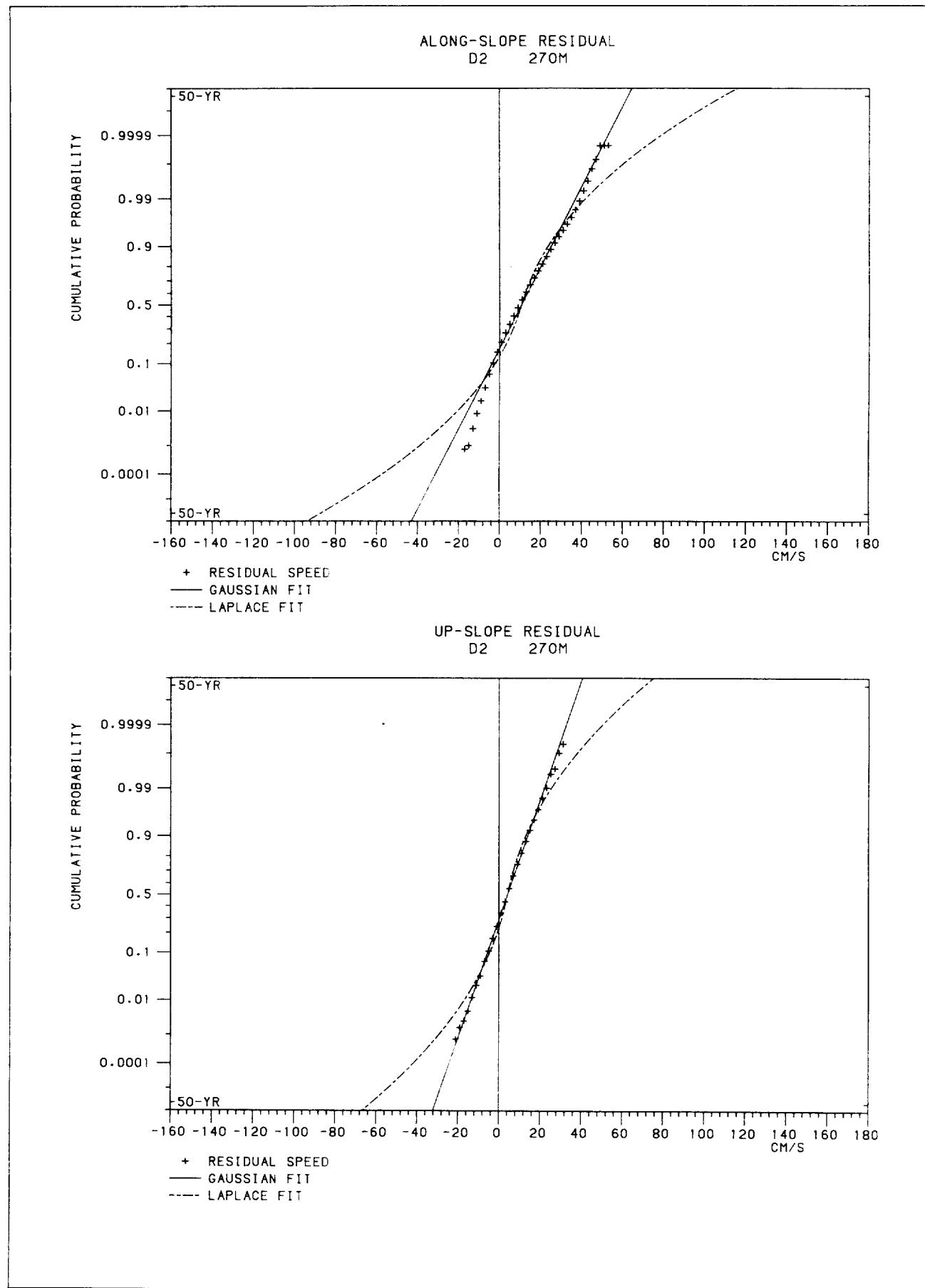


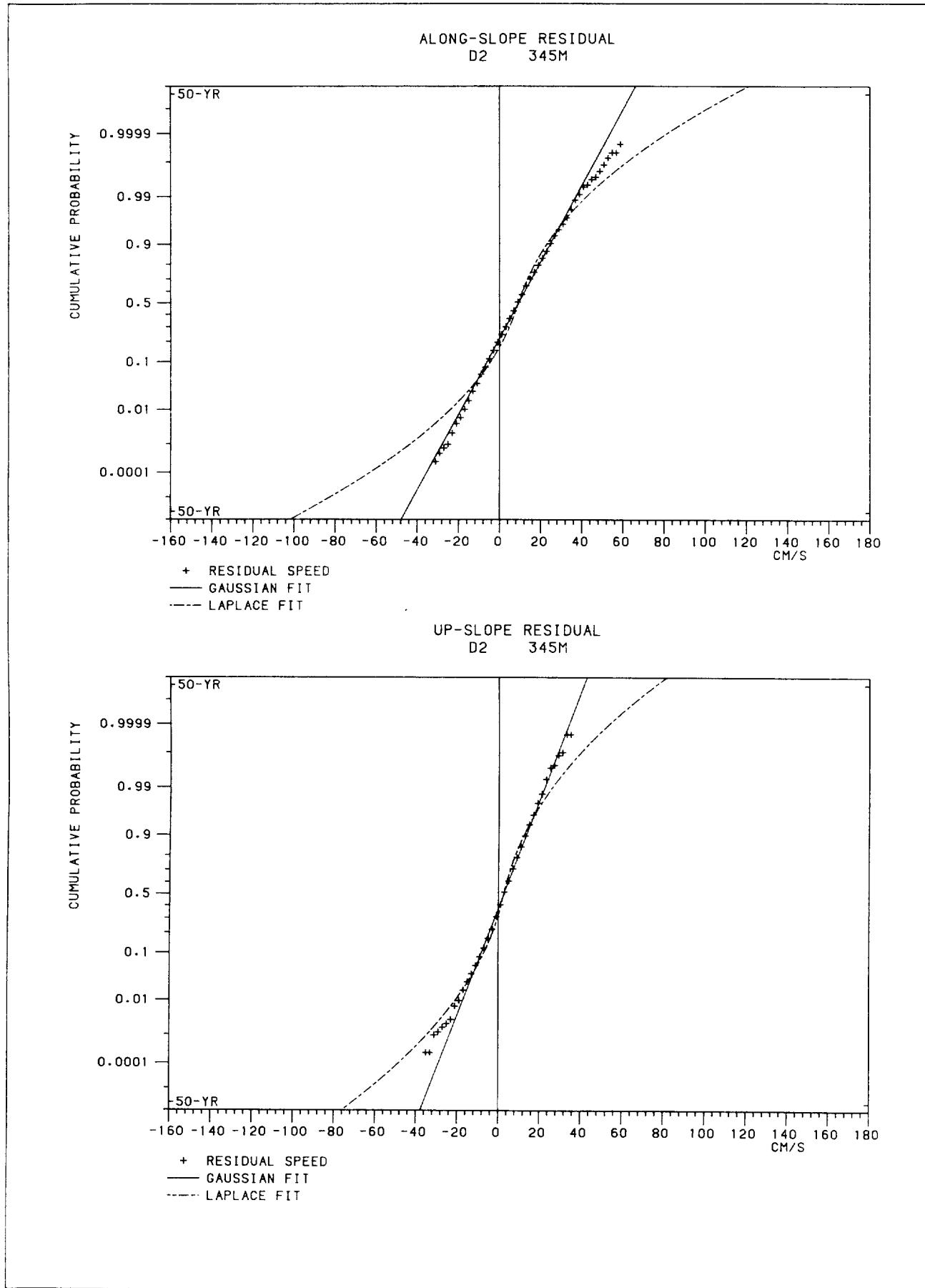


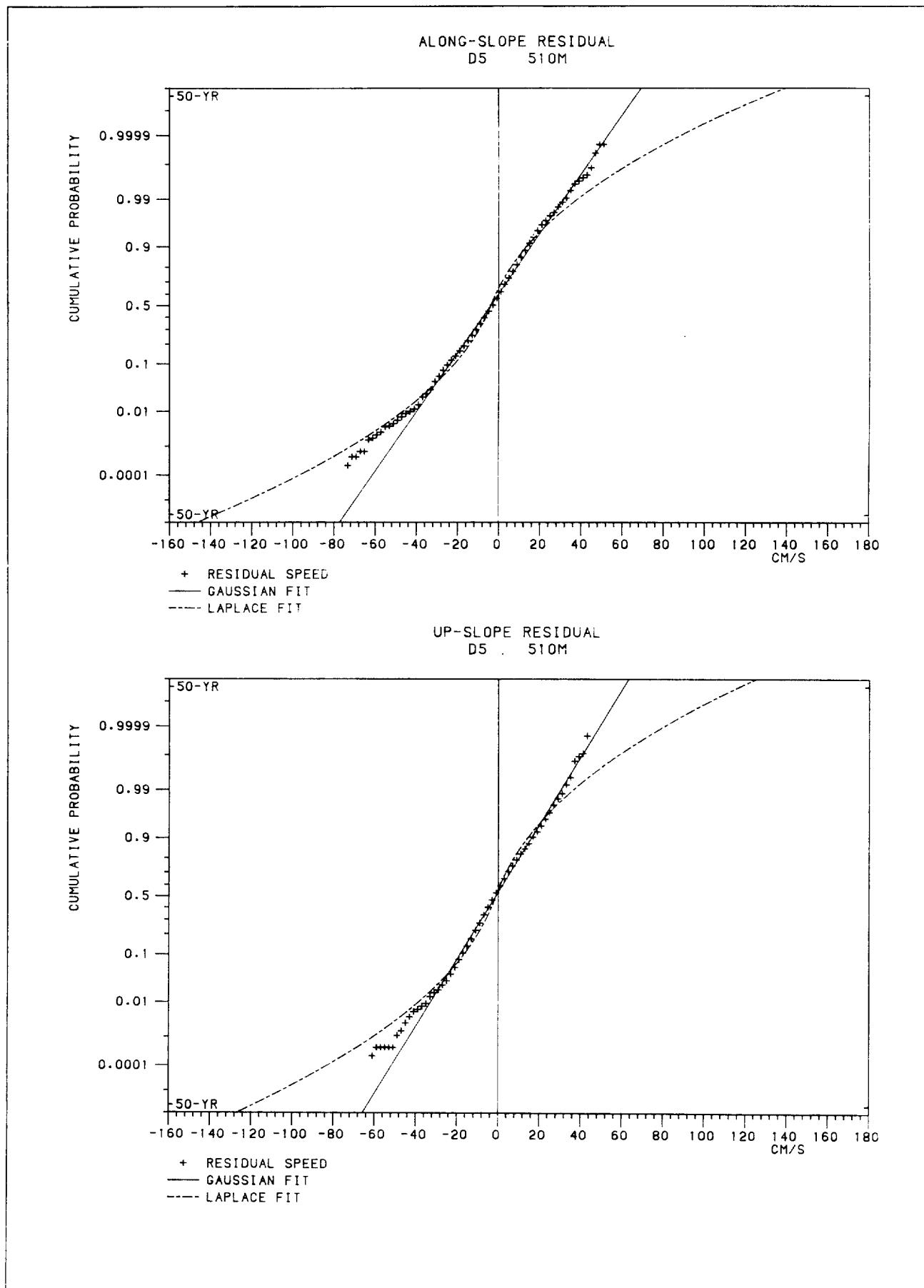


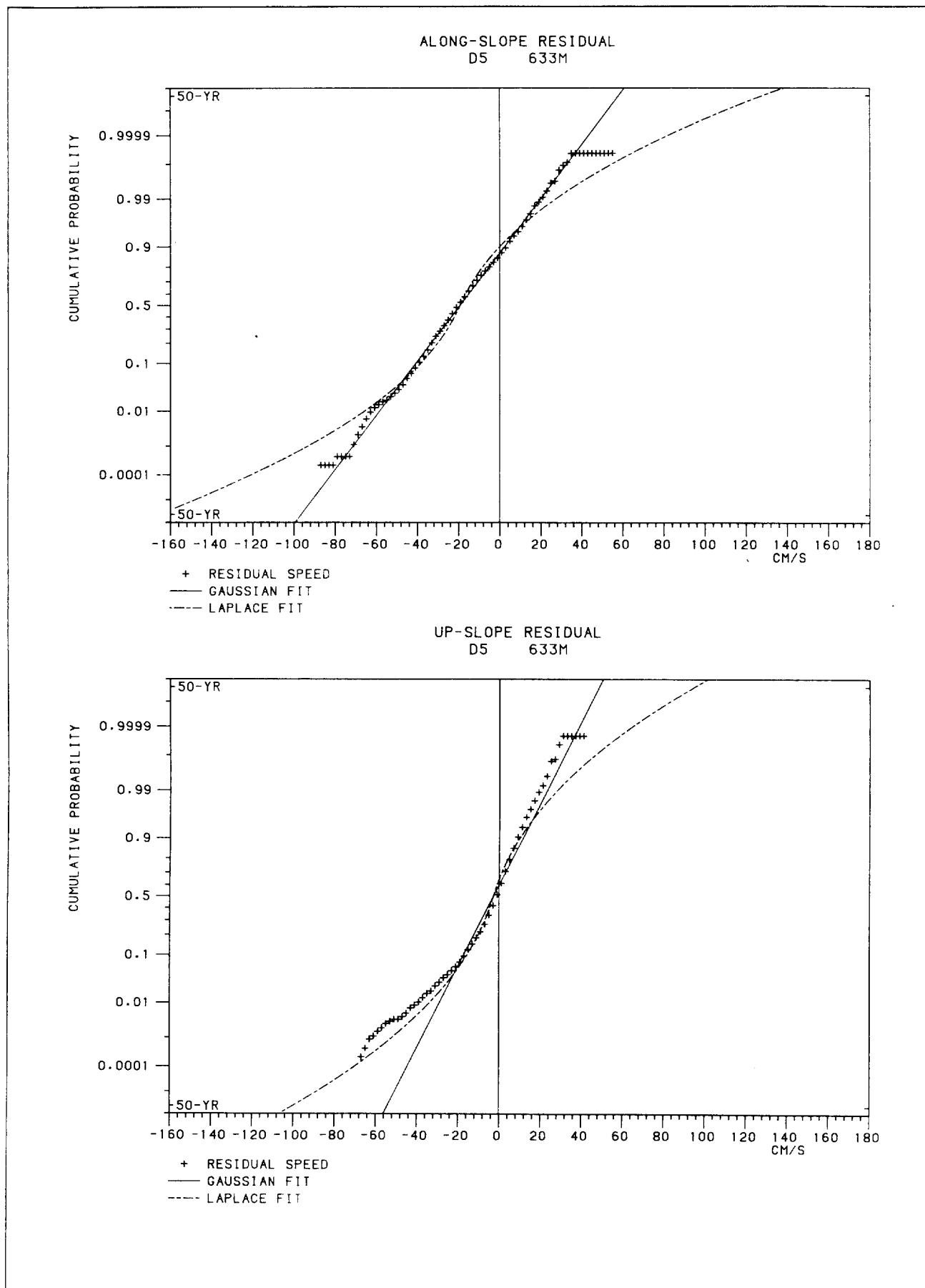


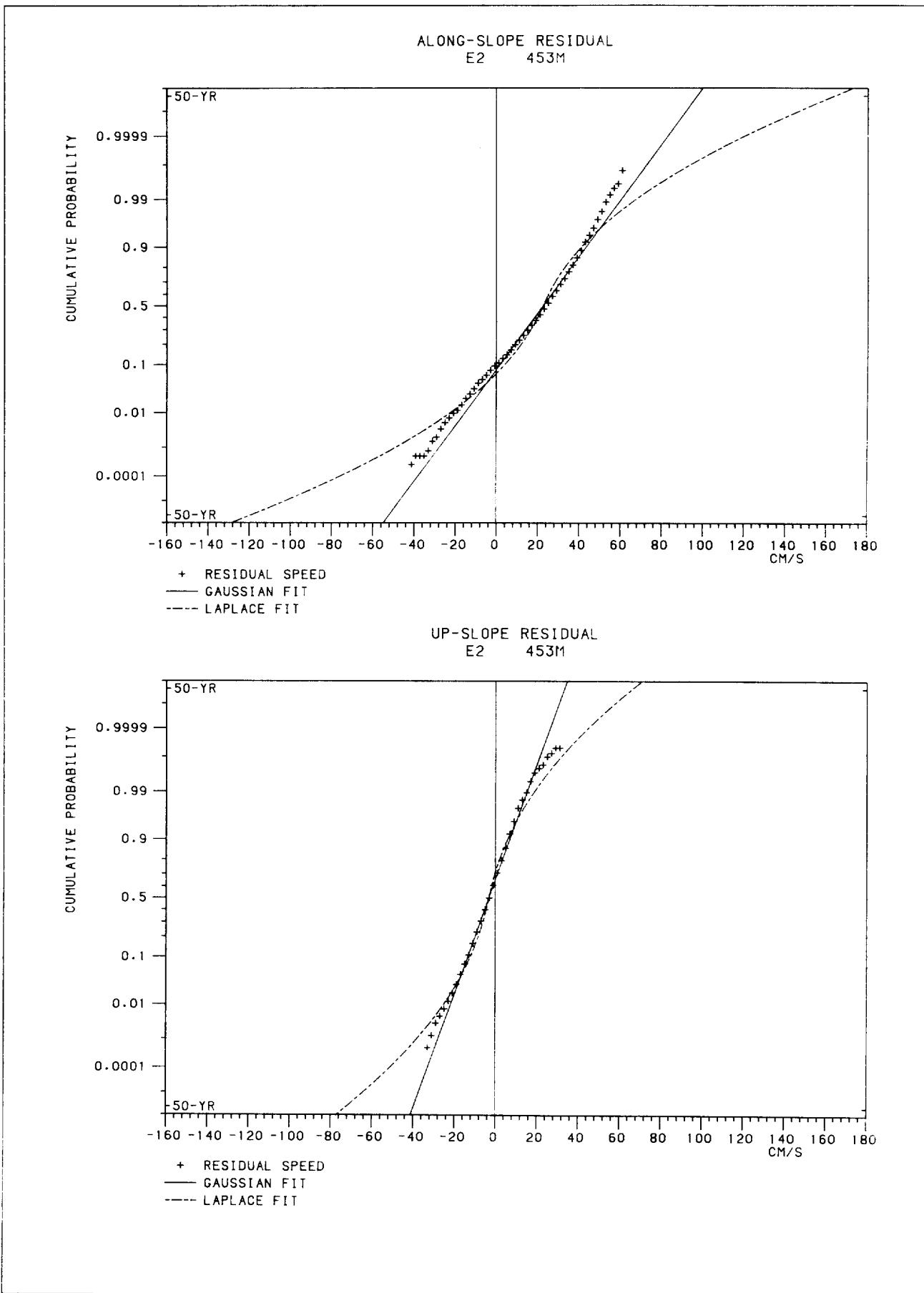


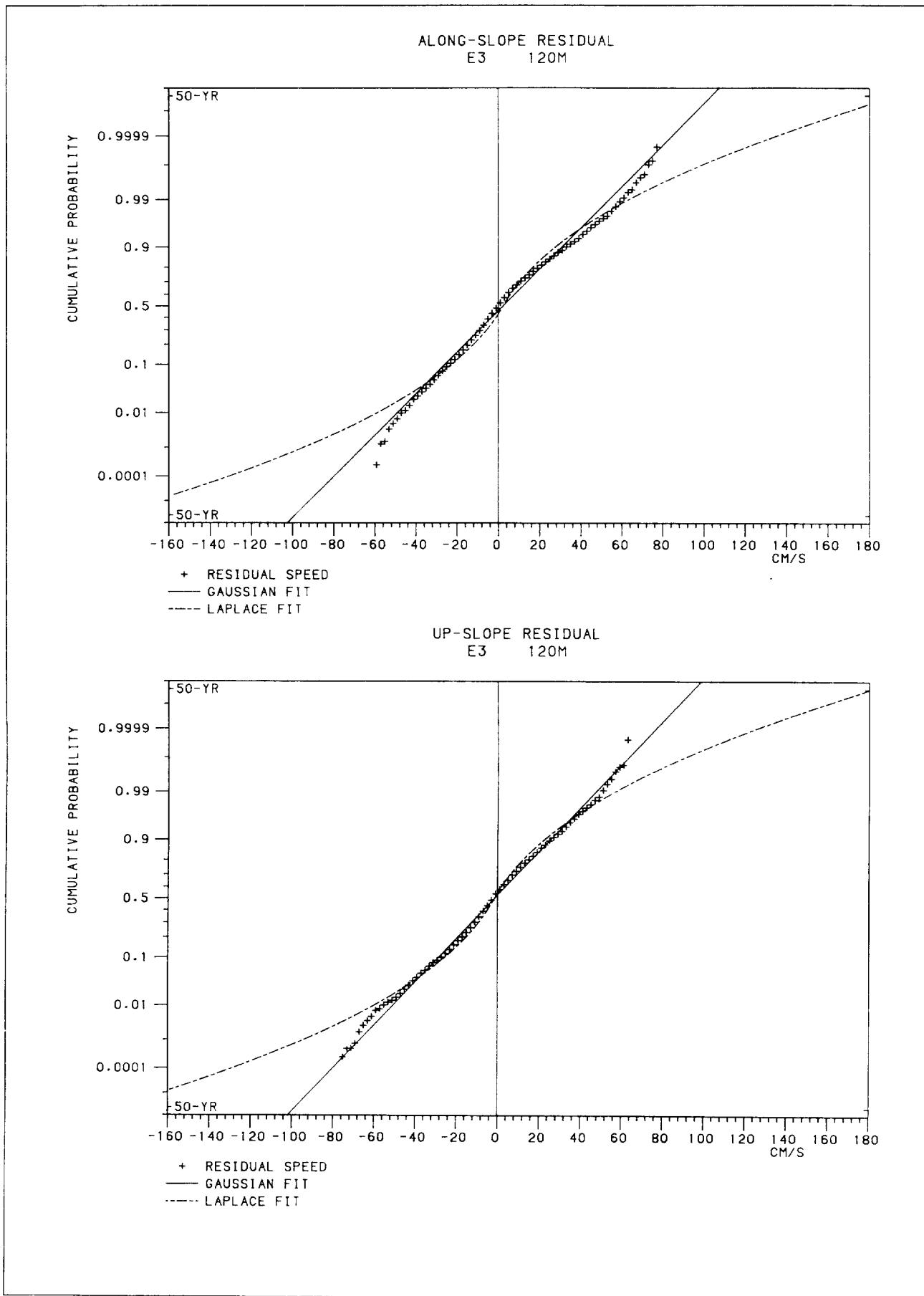


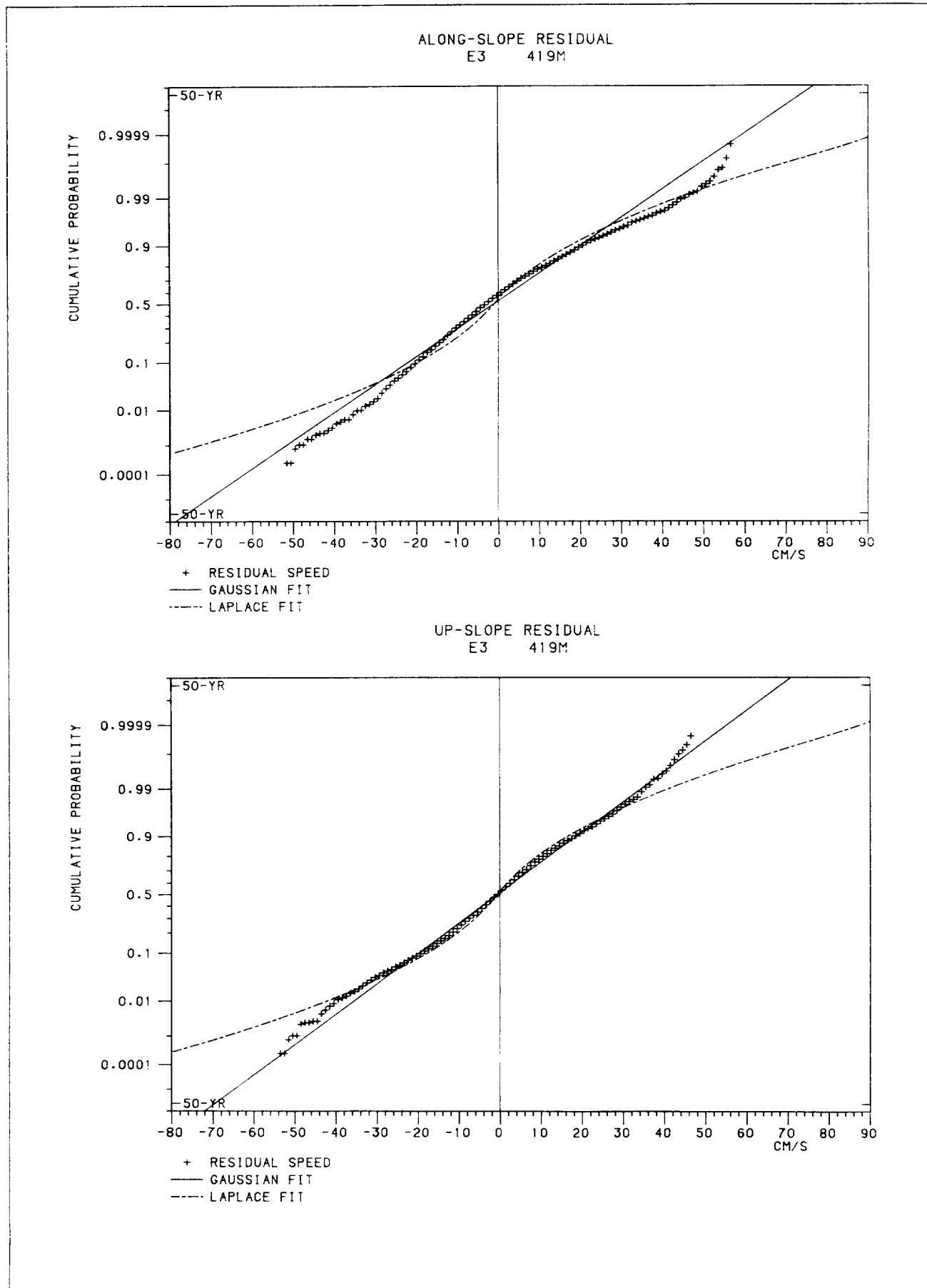


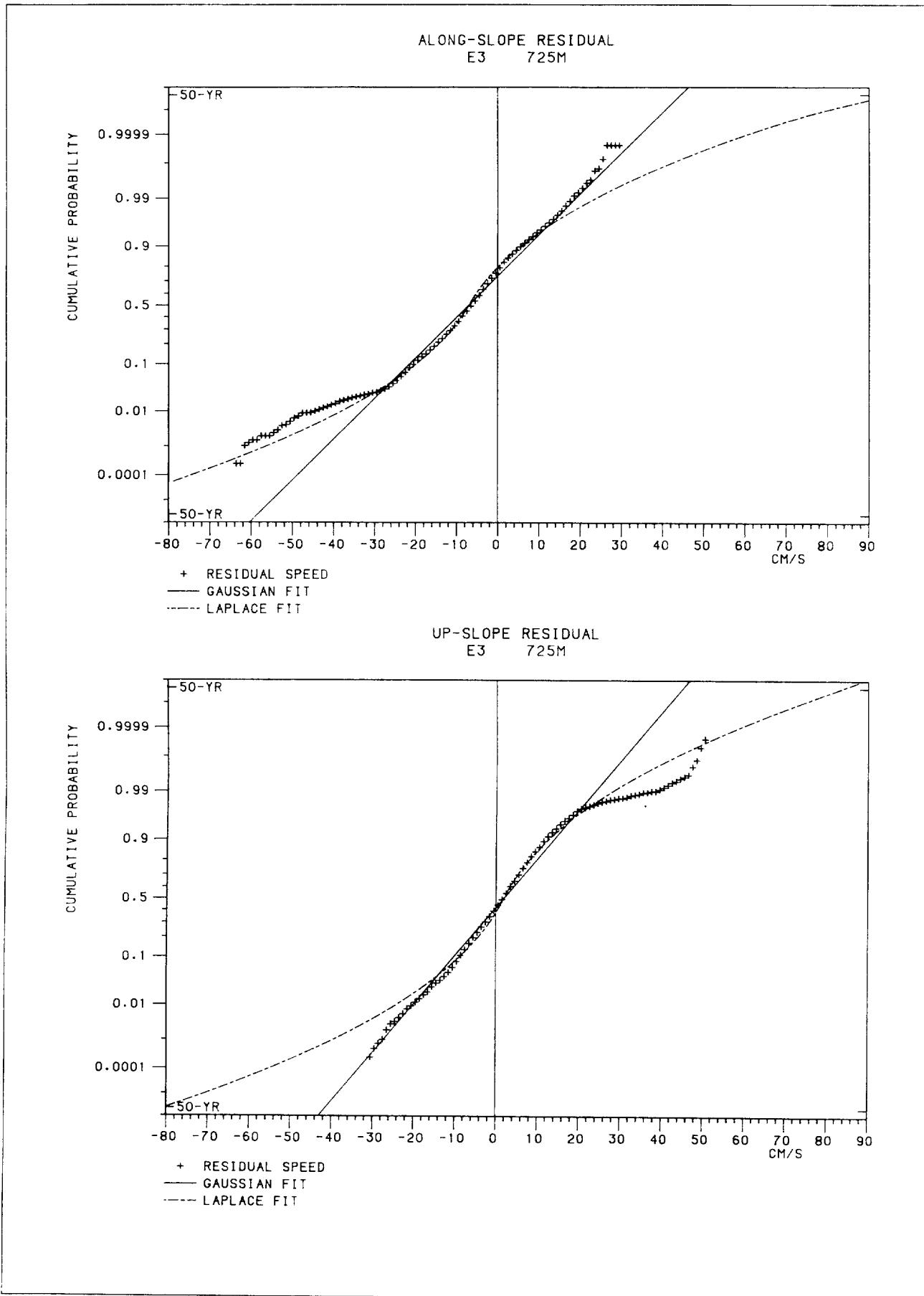


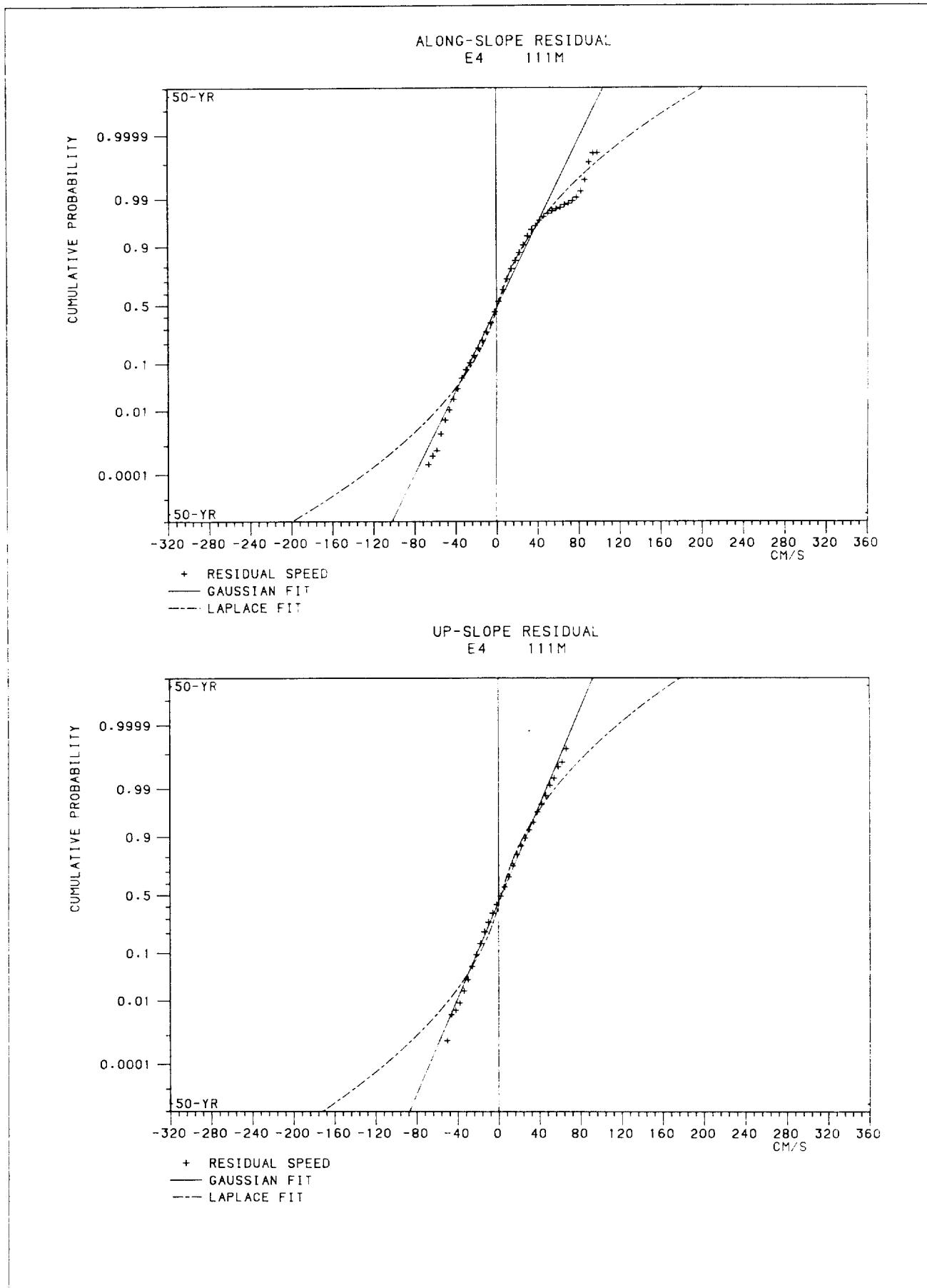


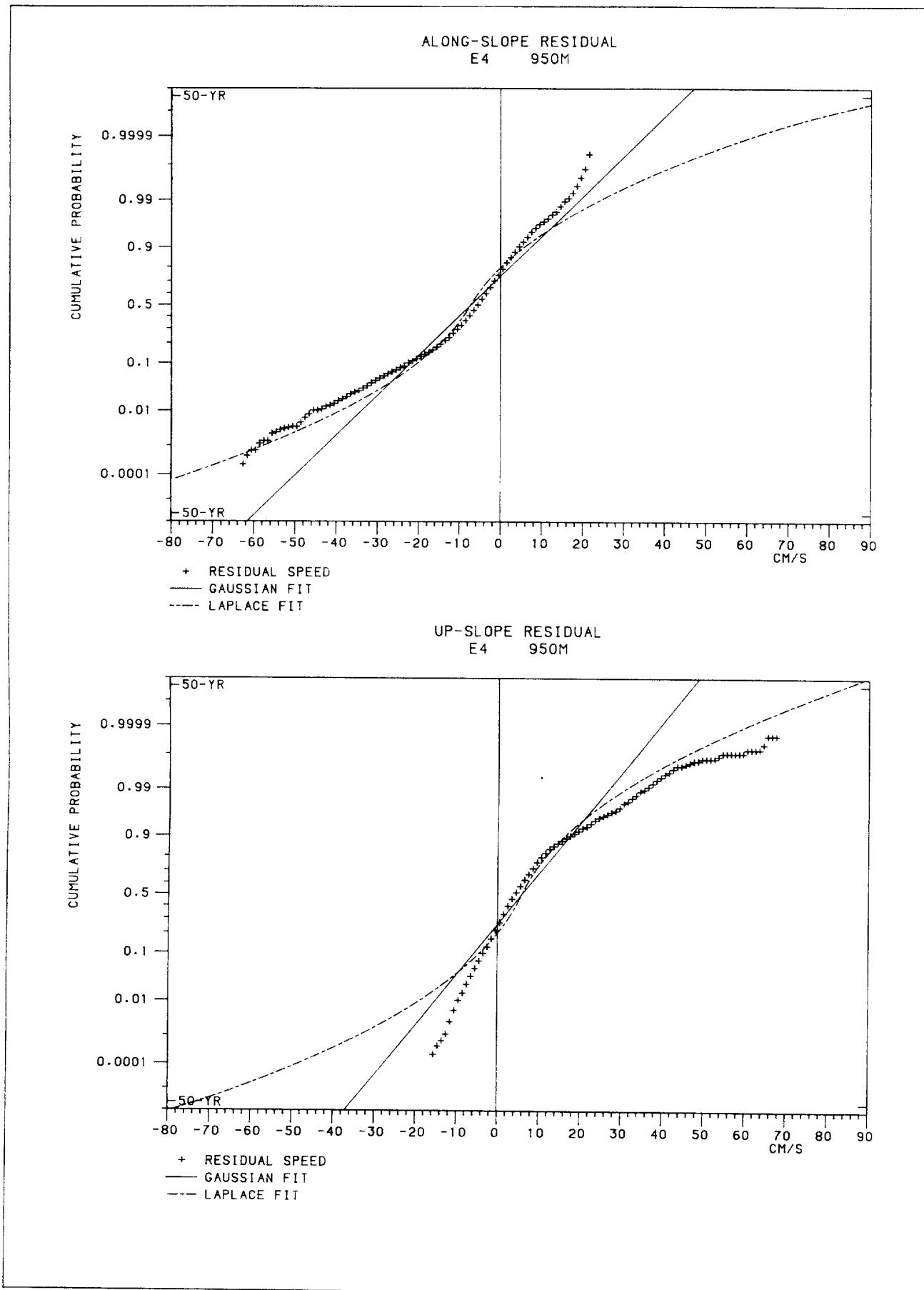




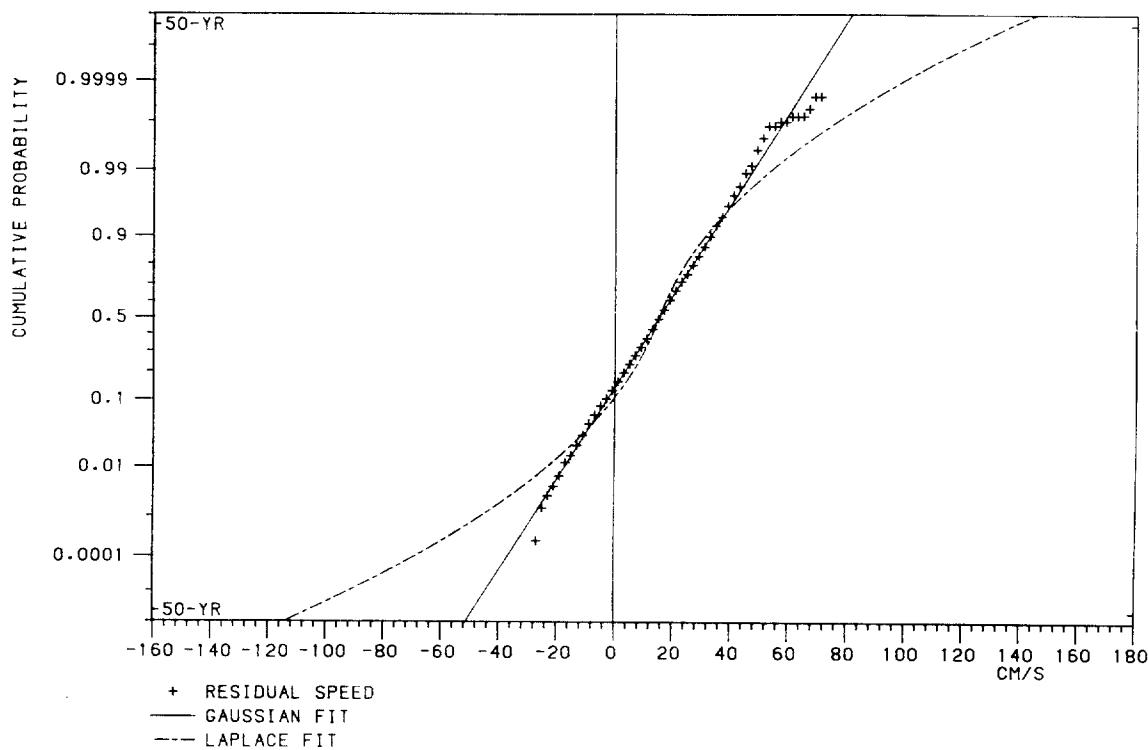




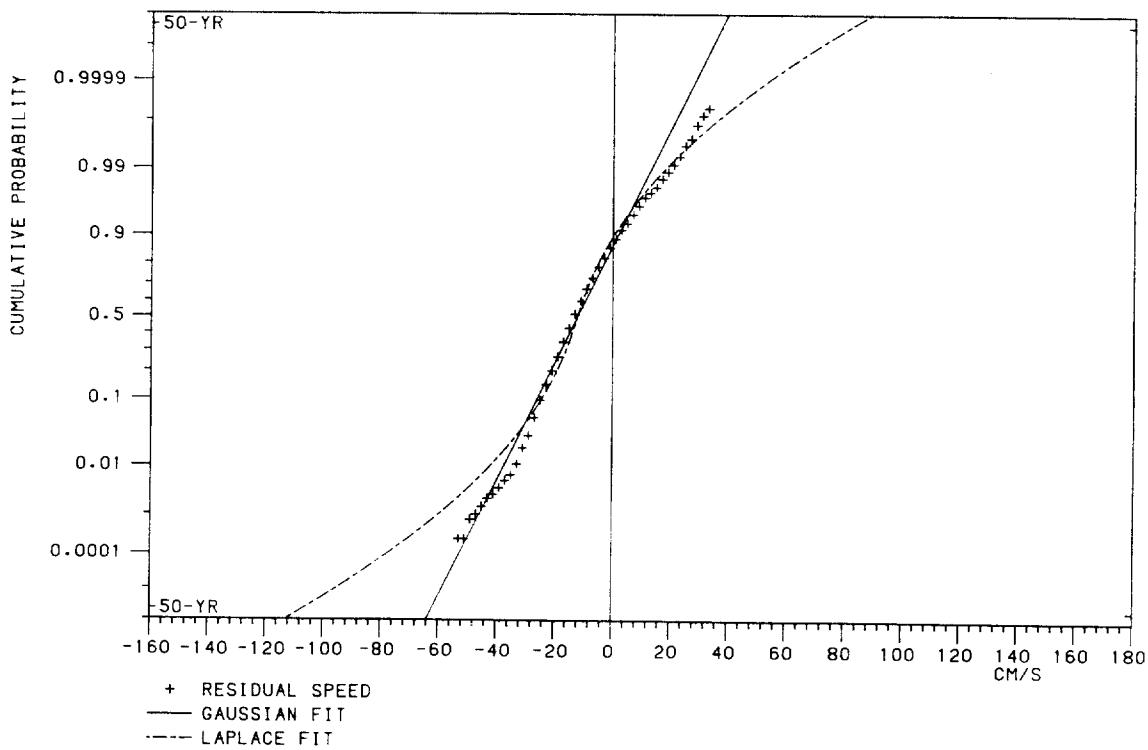


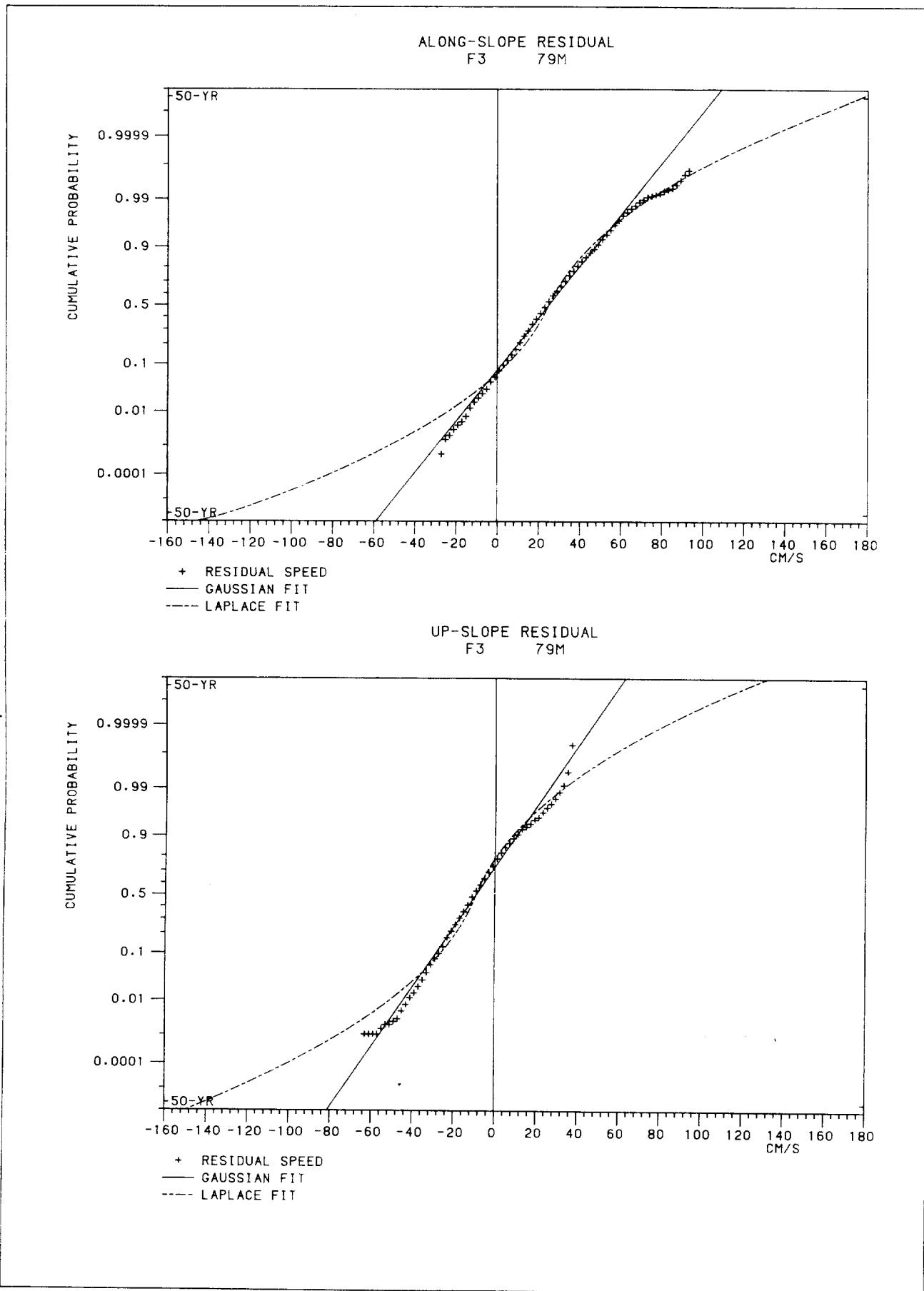


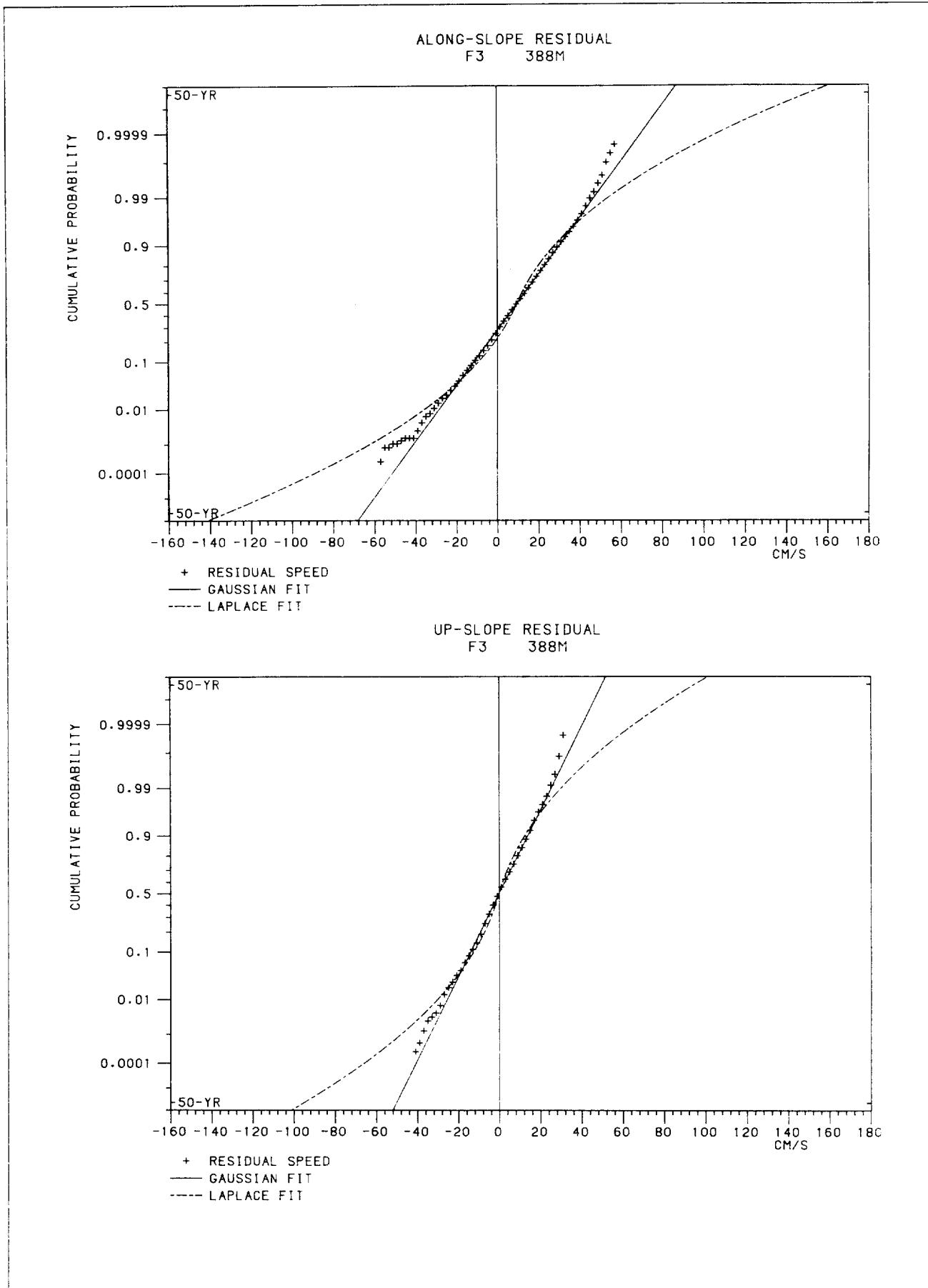
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F1 39M

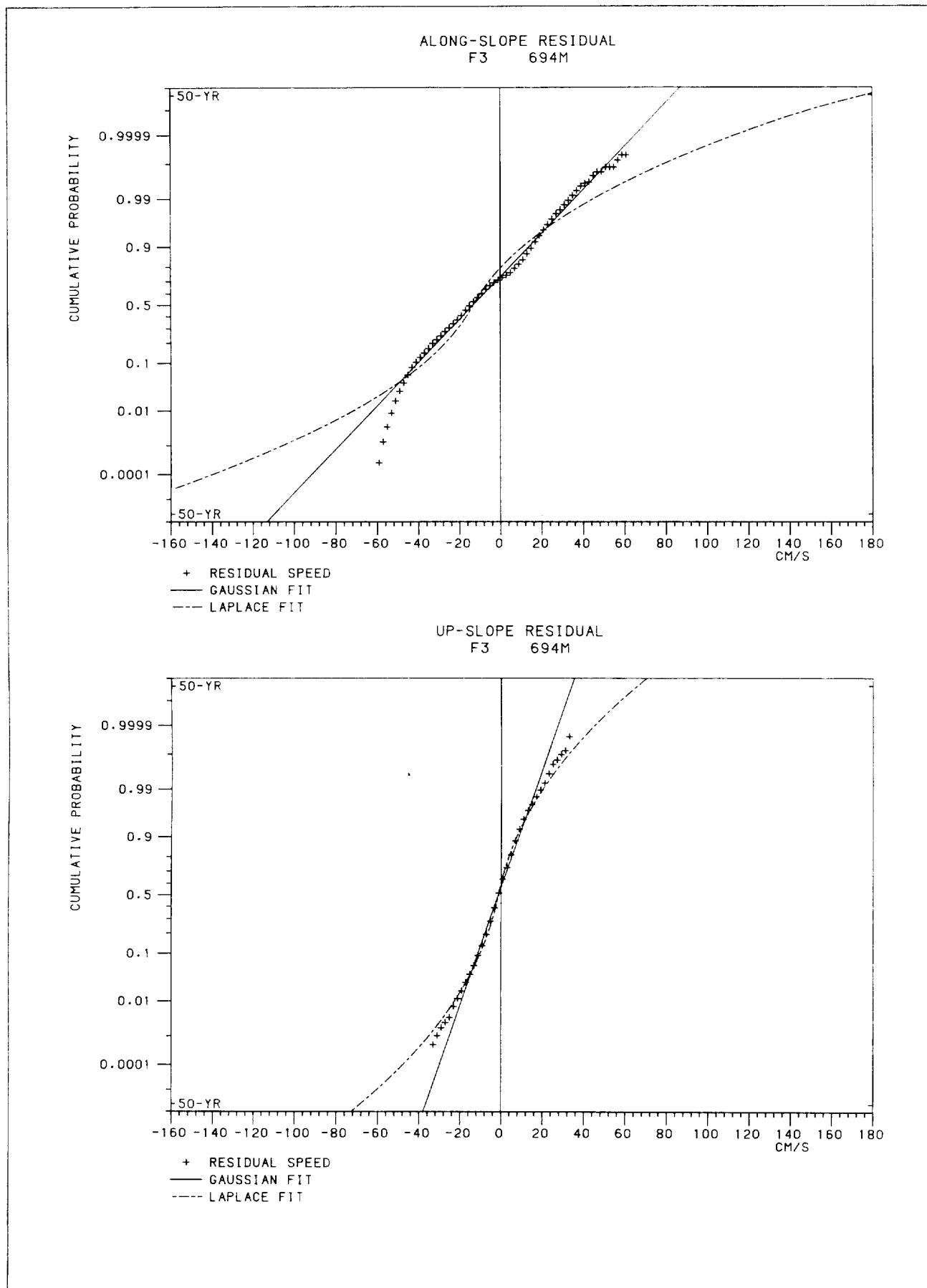


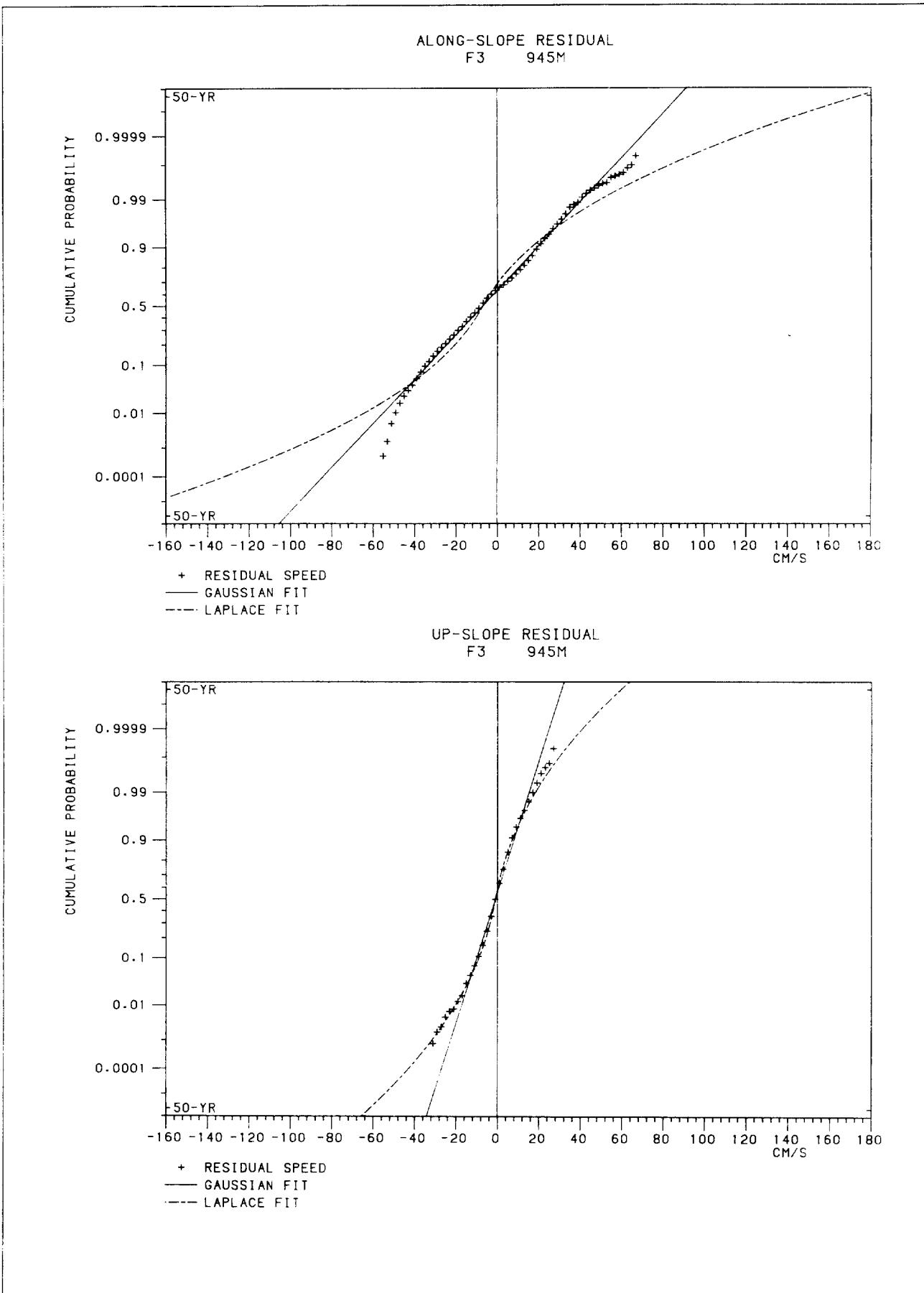
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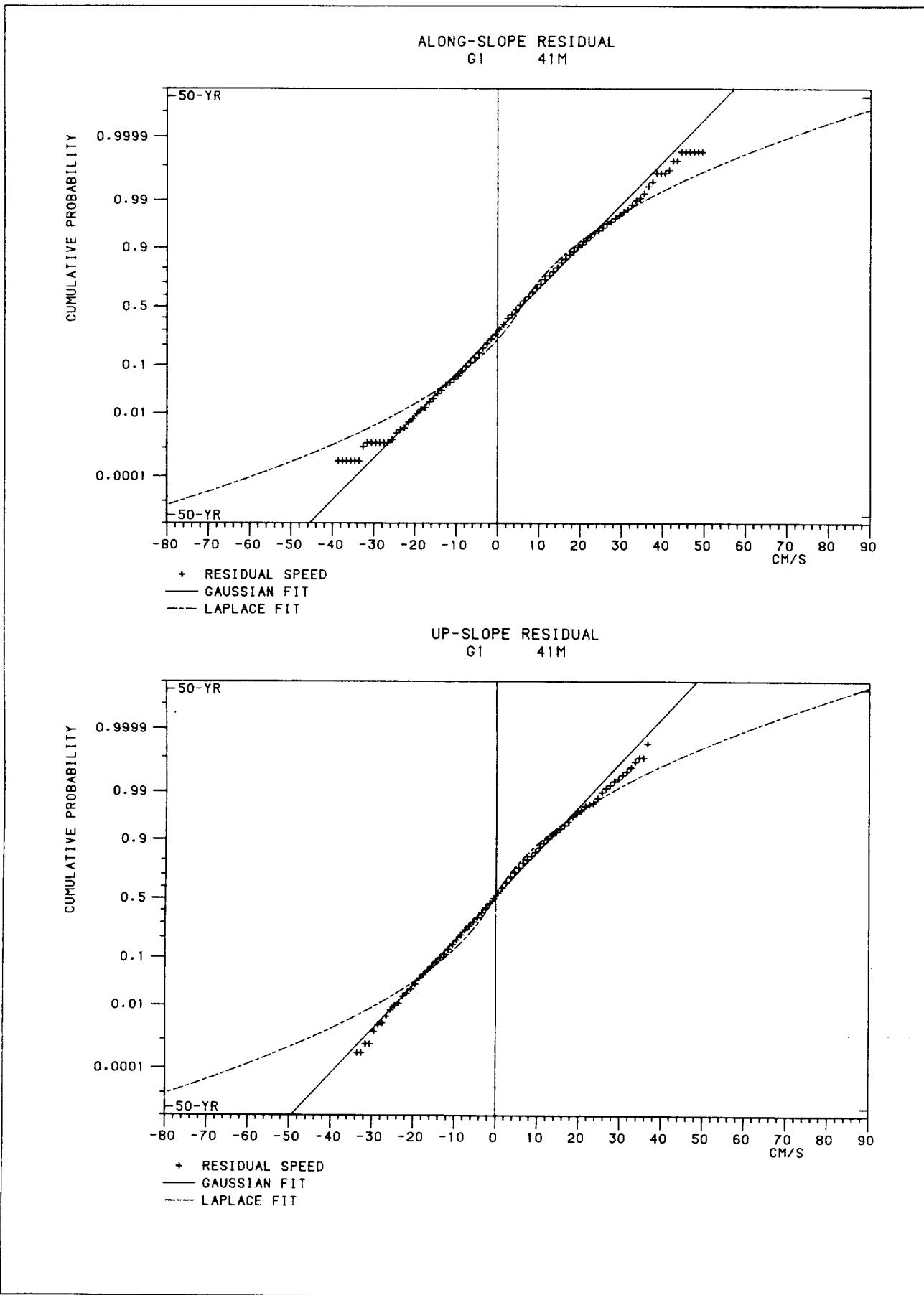


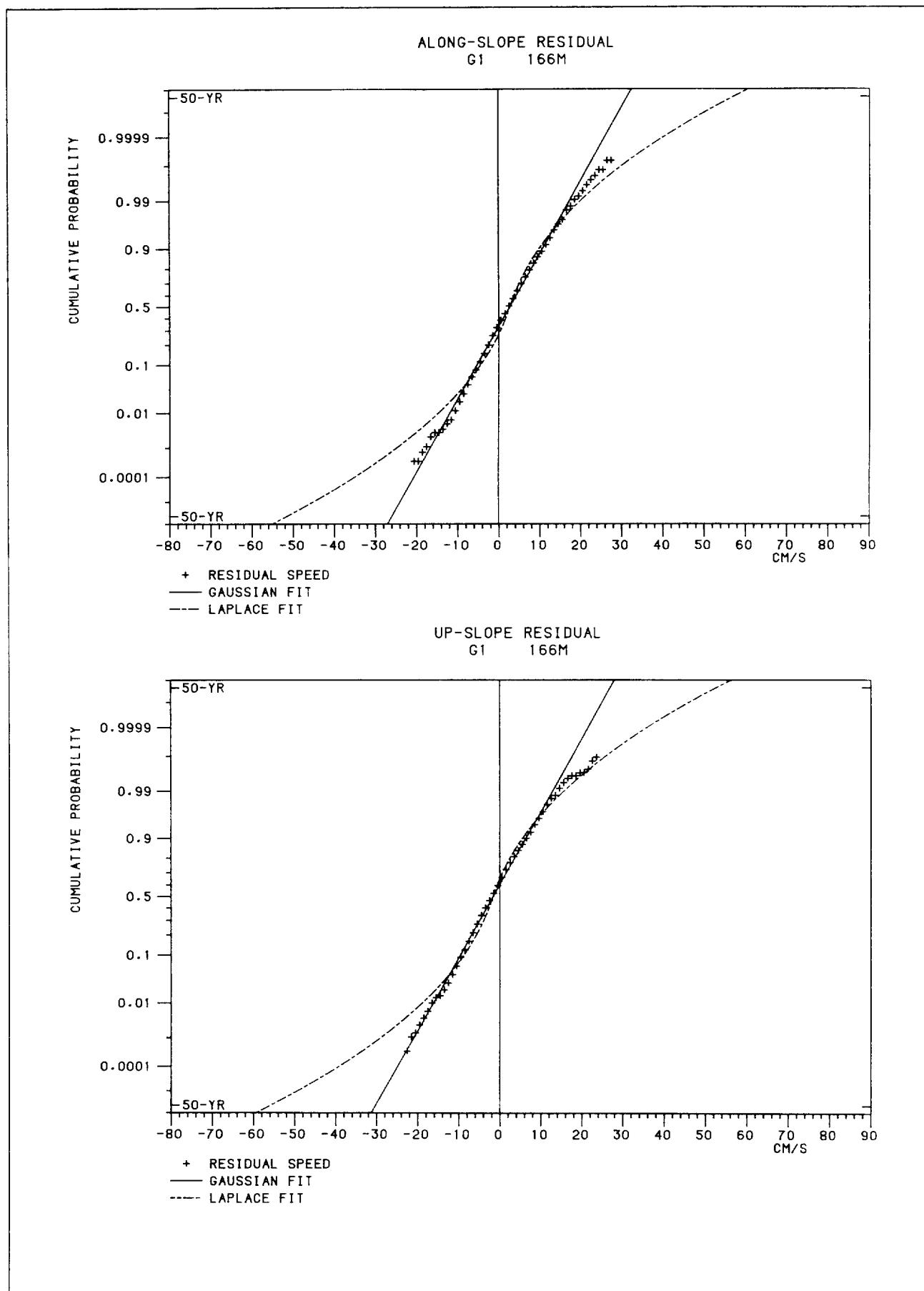


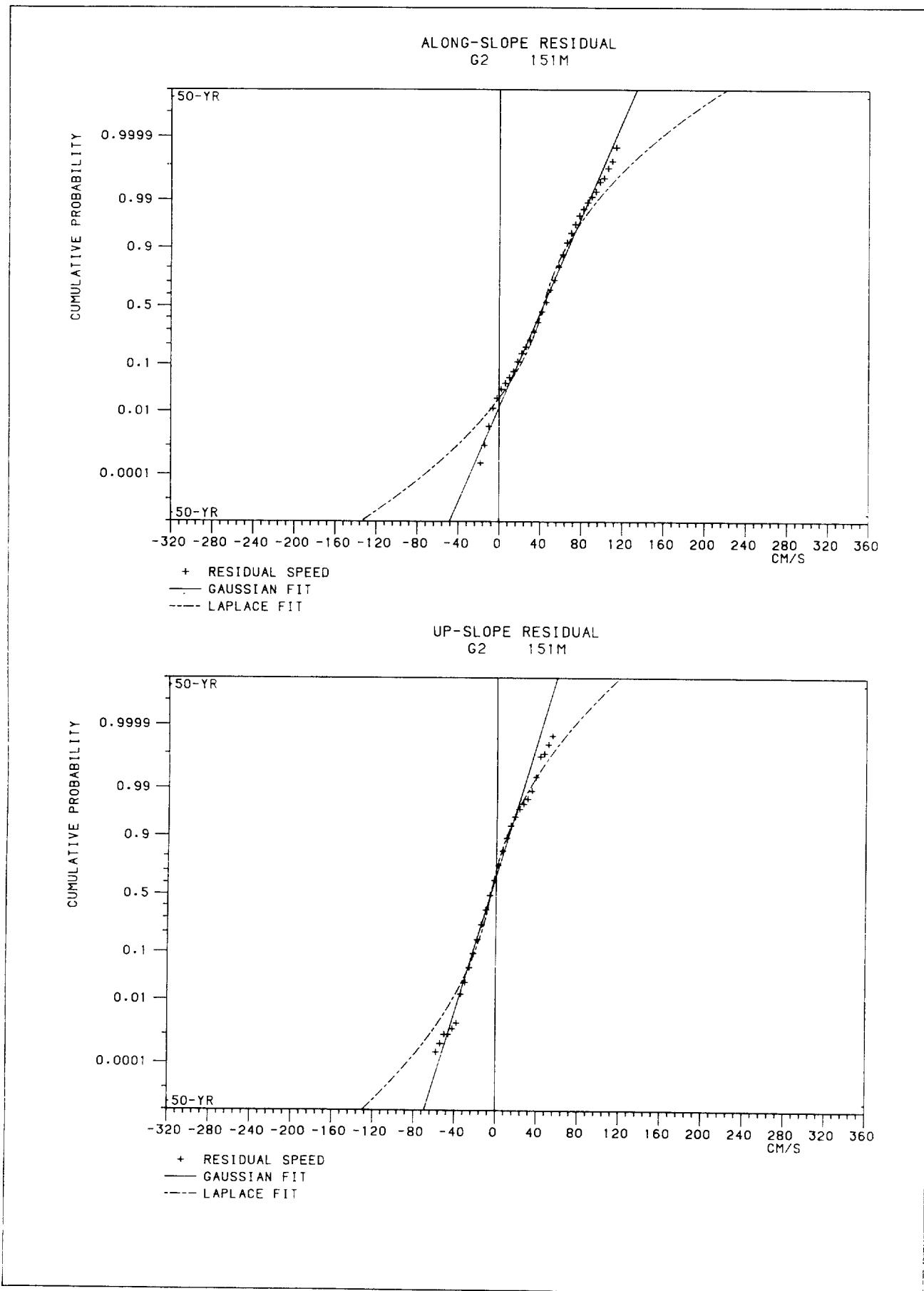


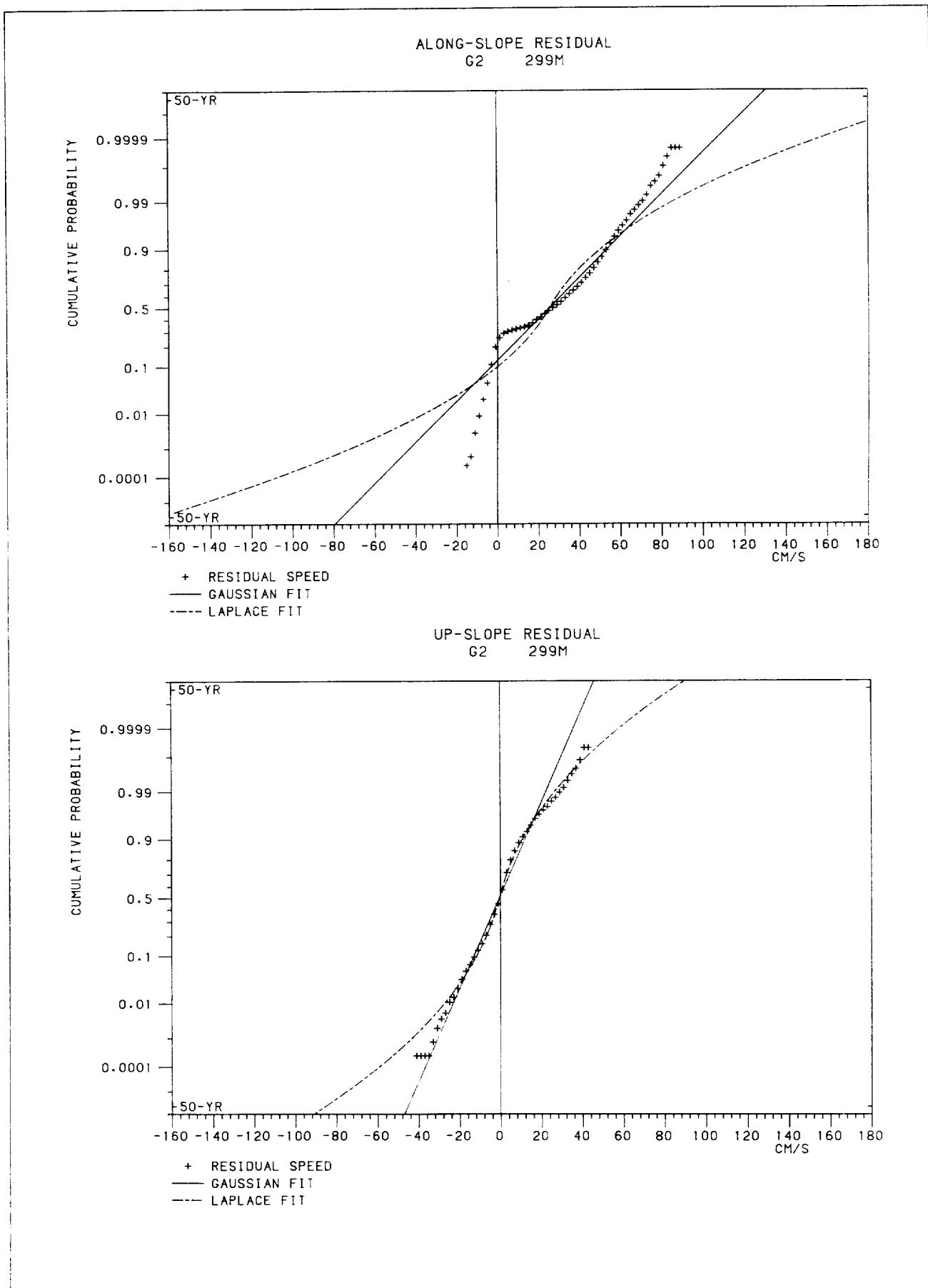


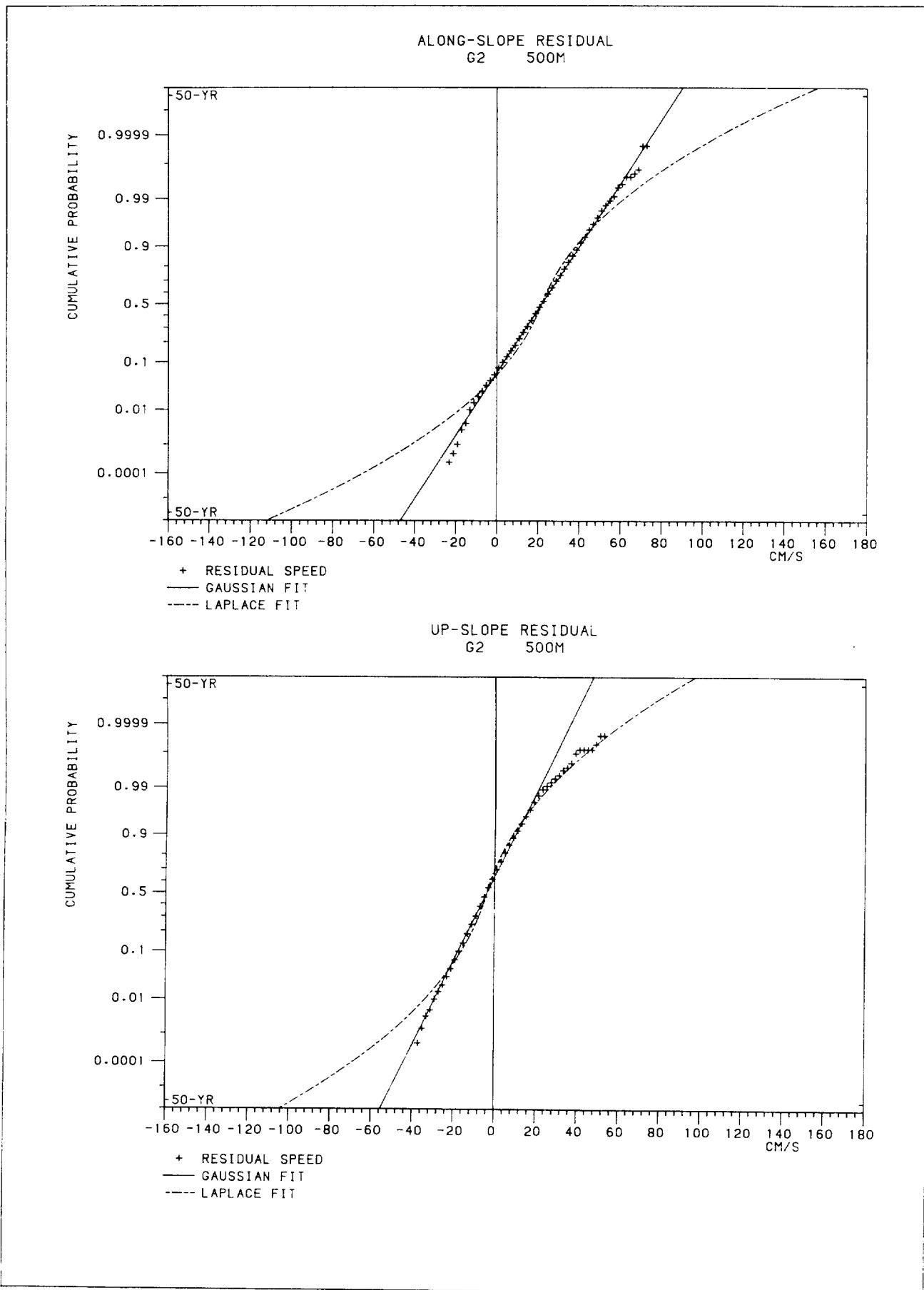


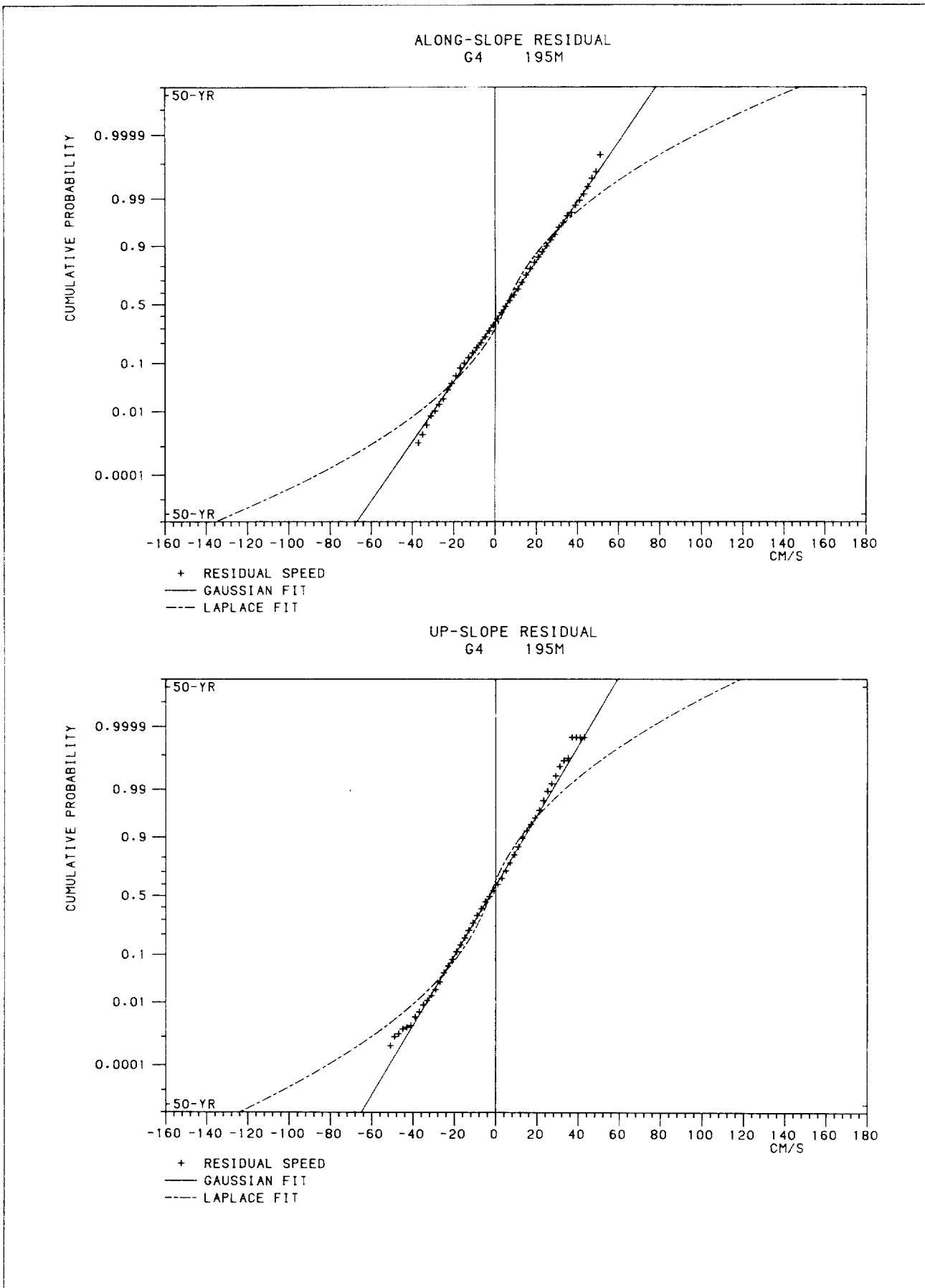


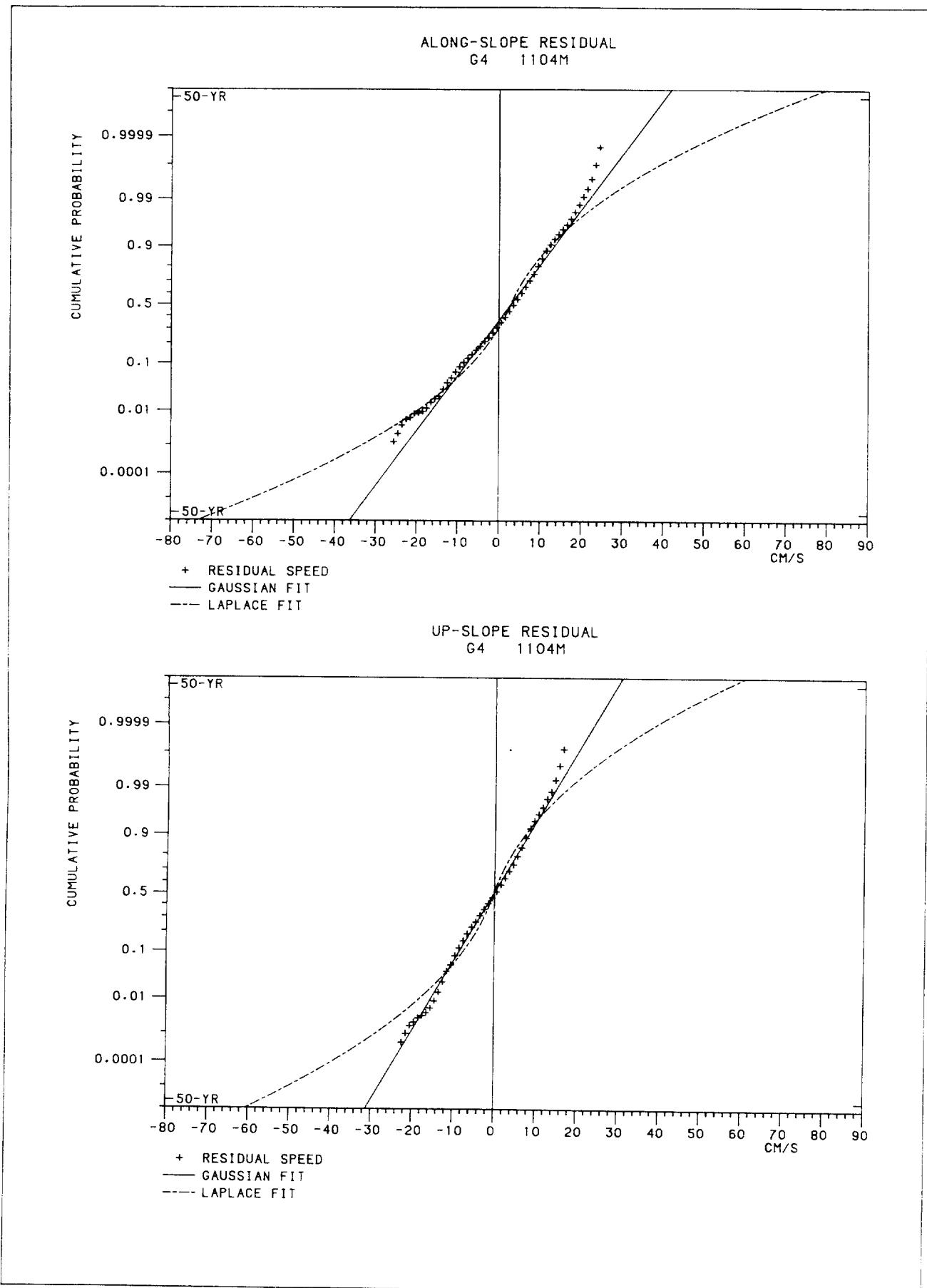


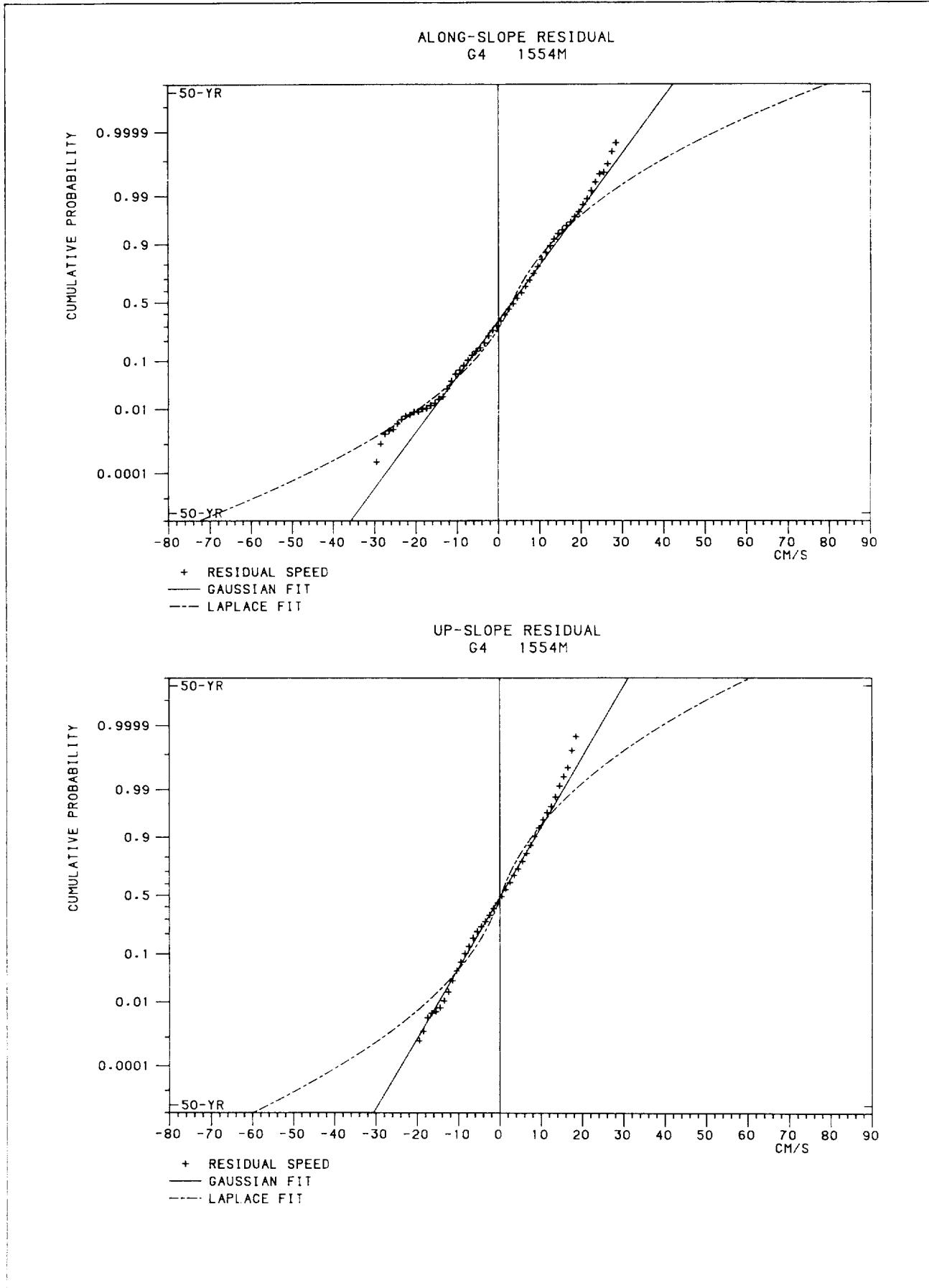


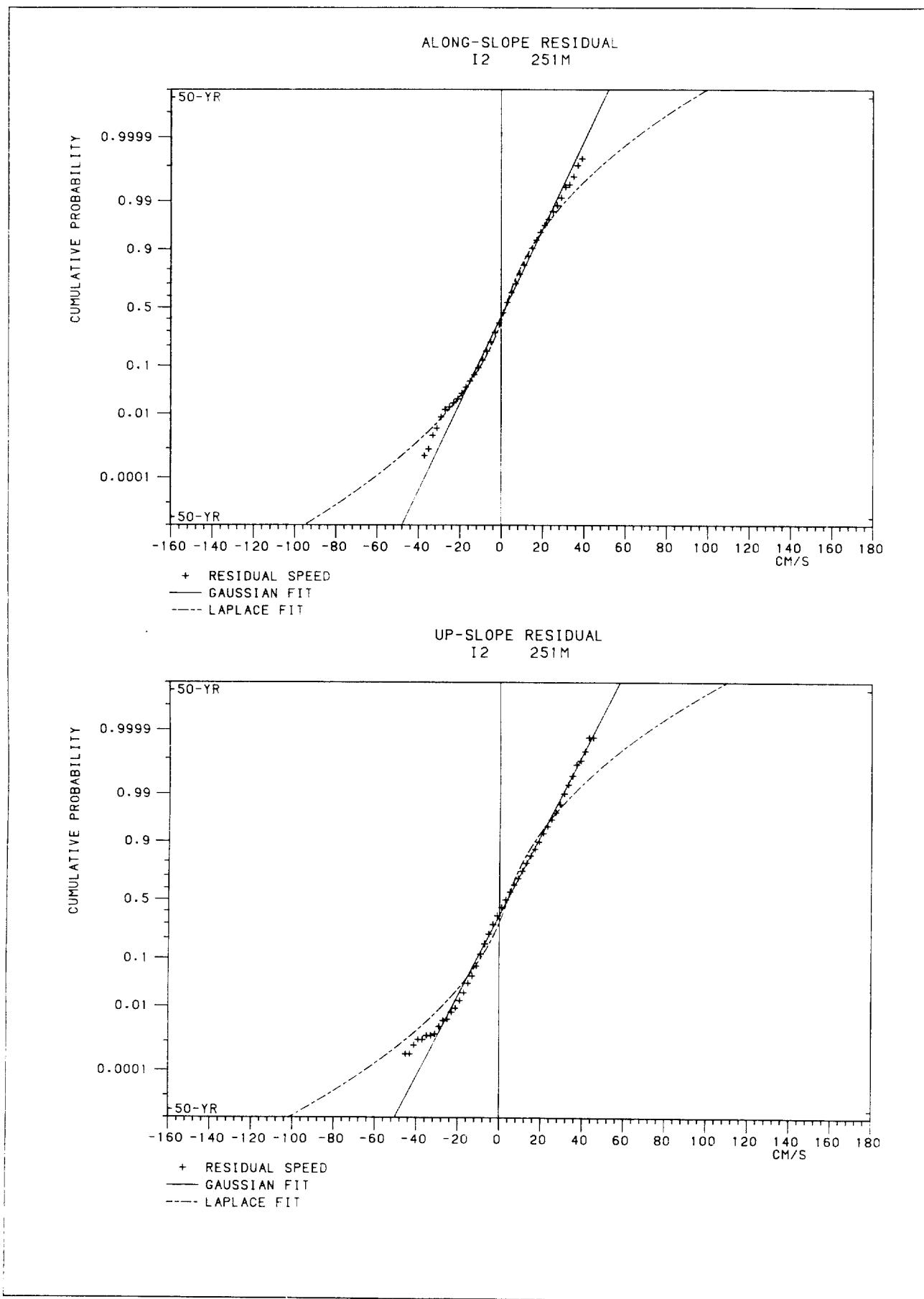


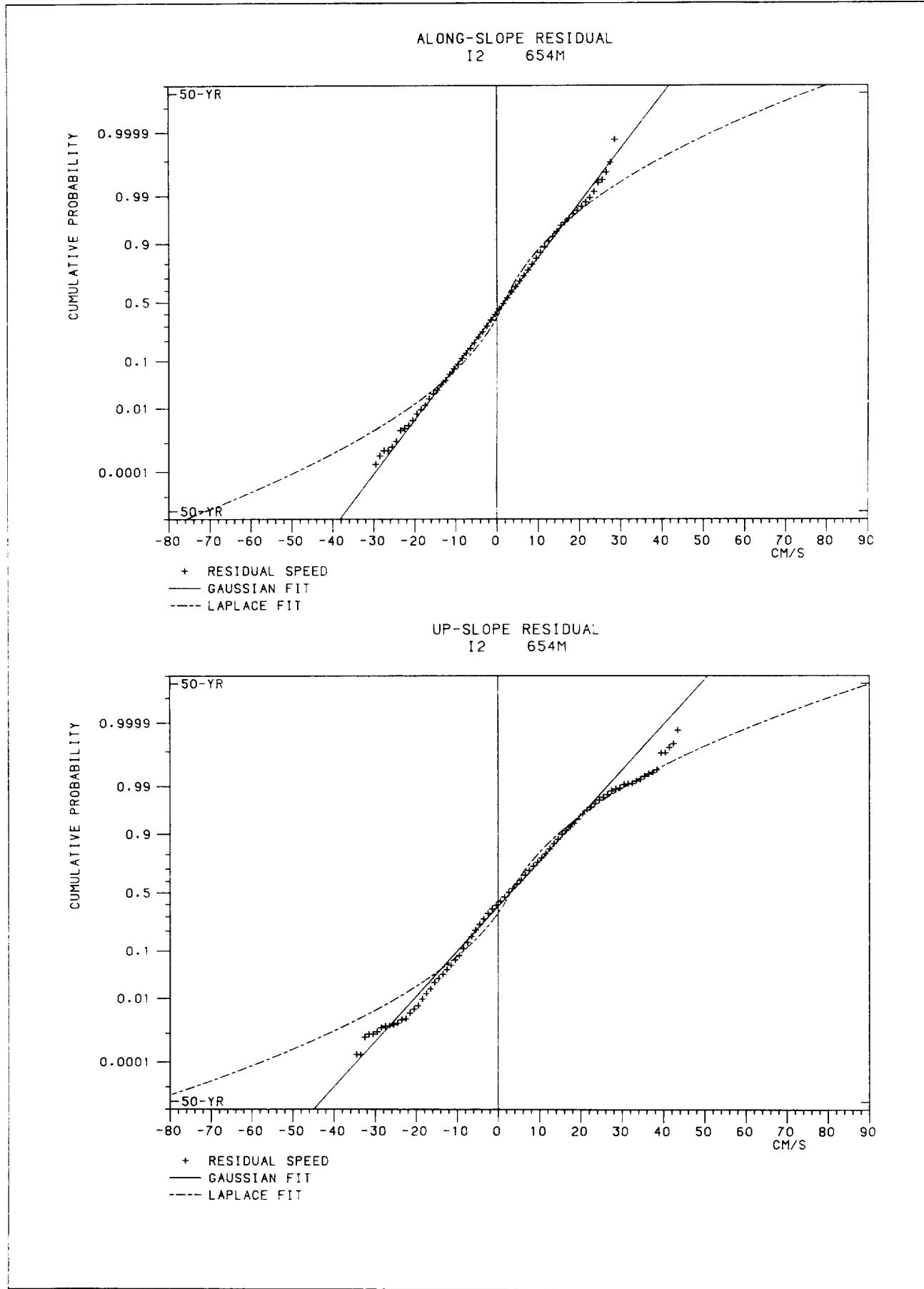


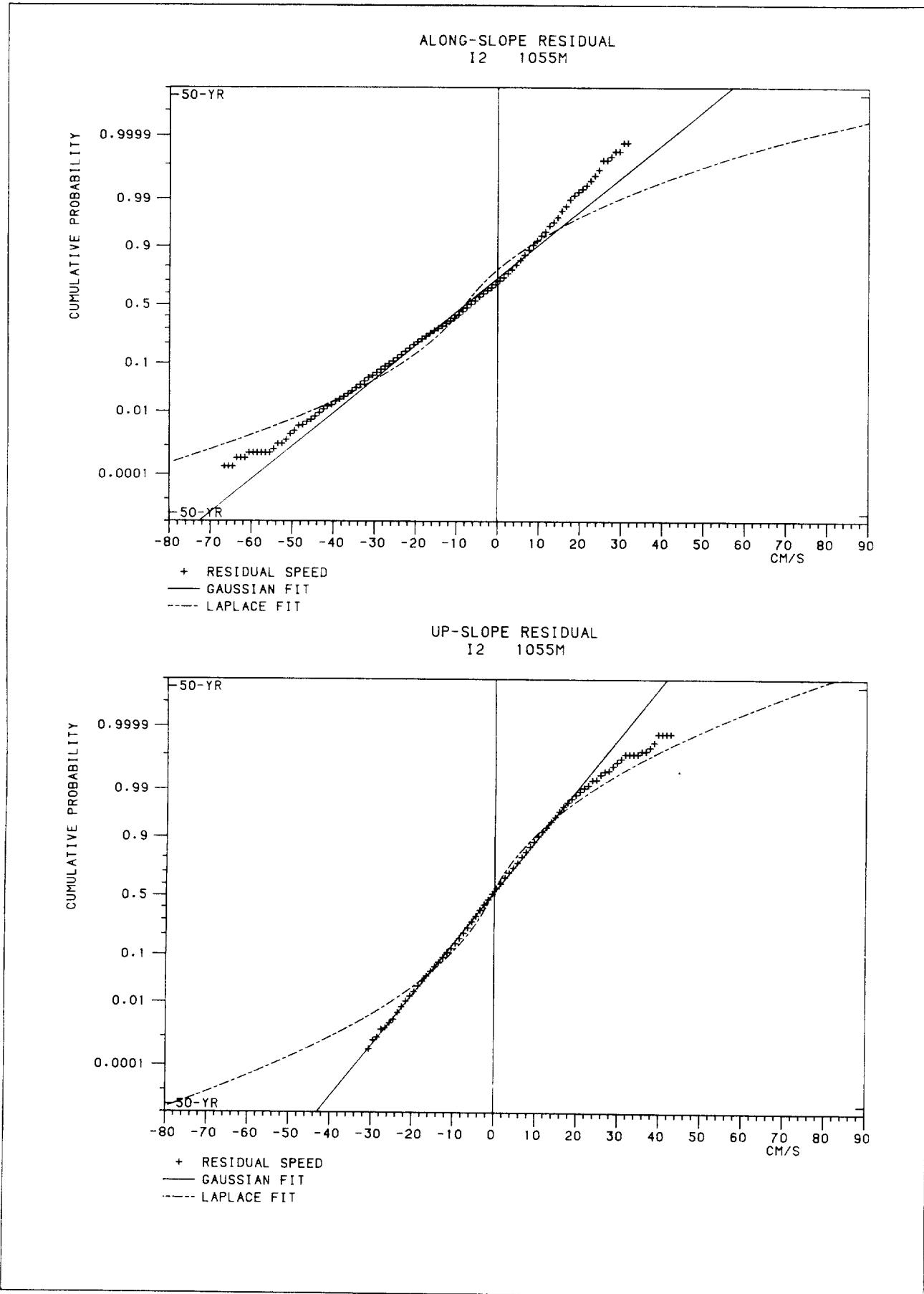












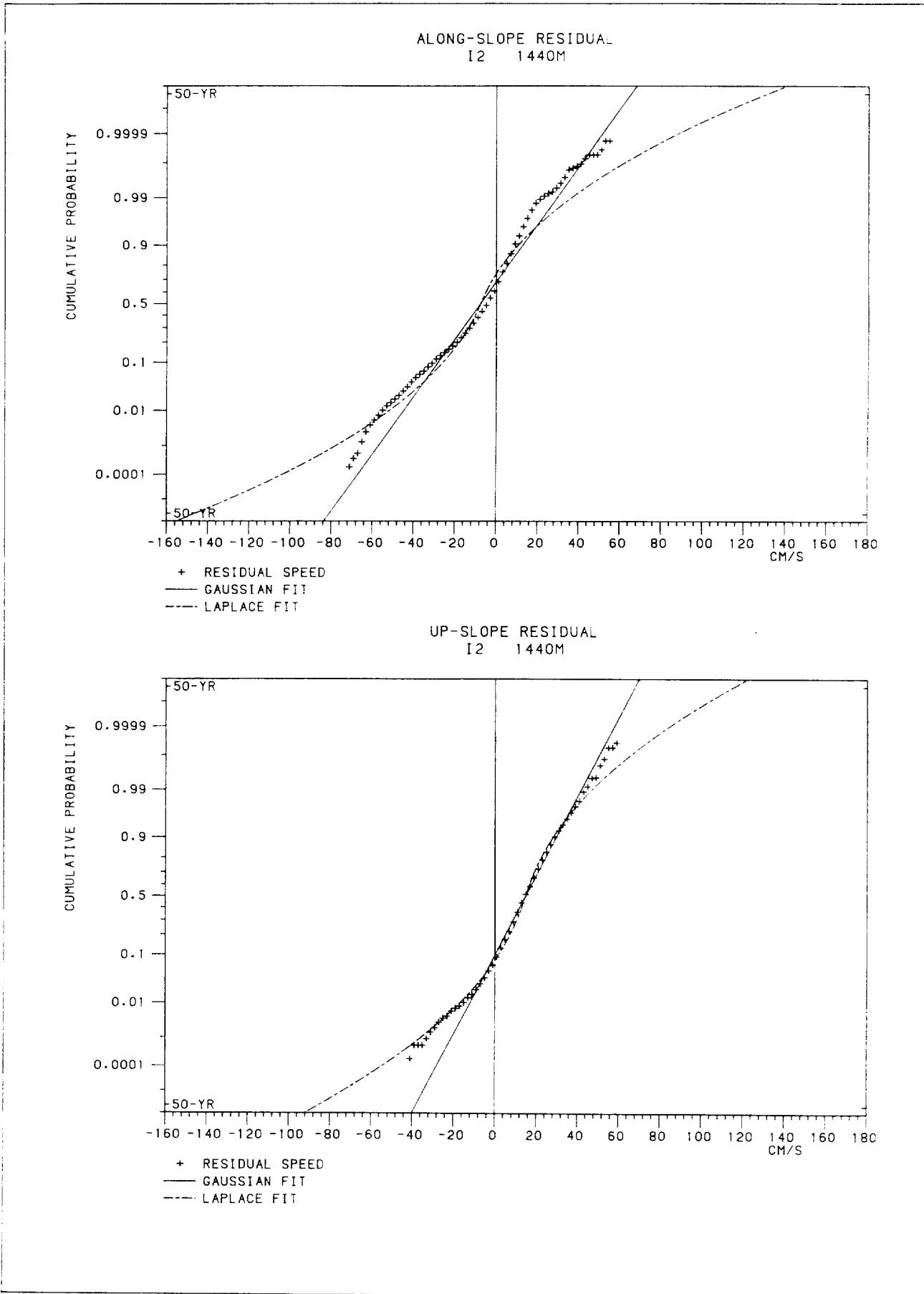
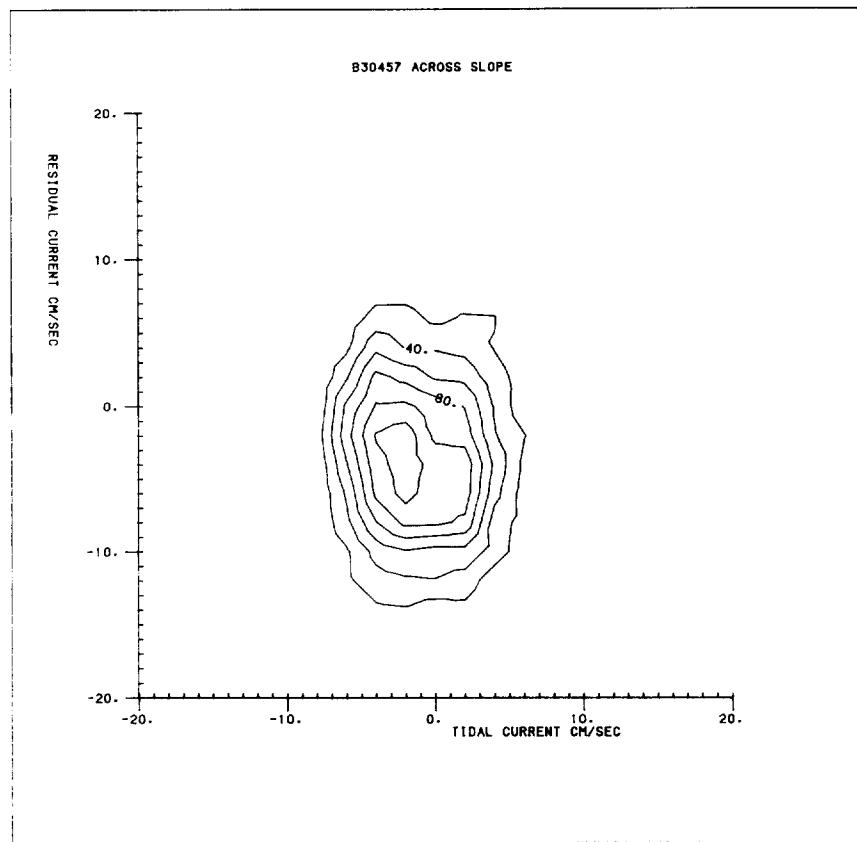
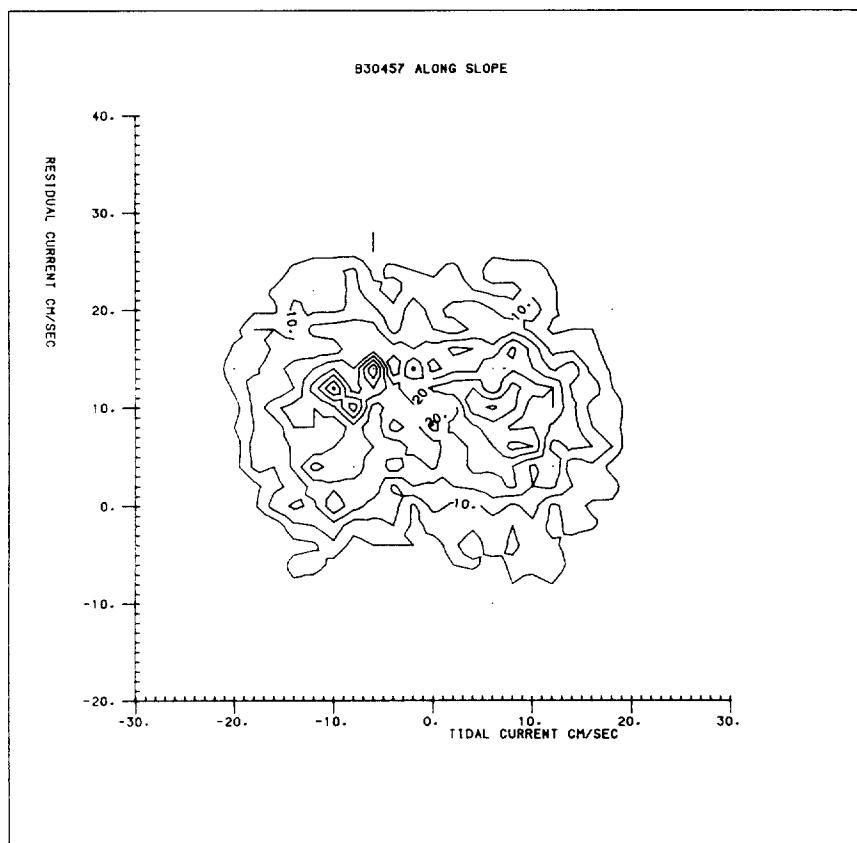
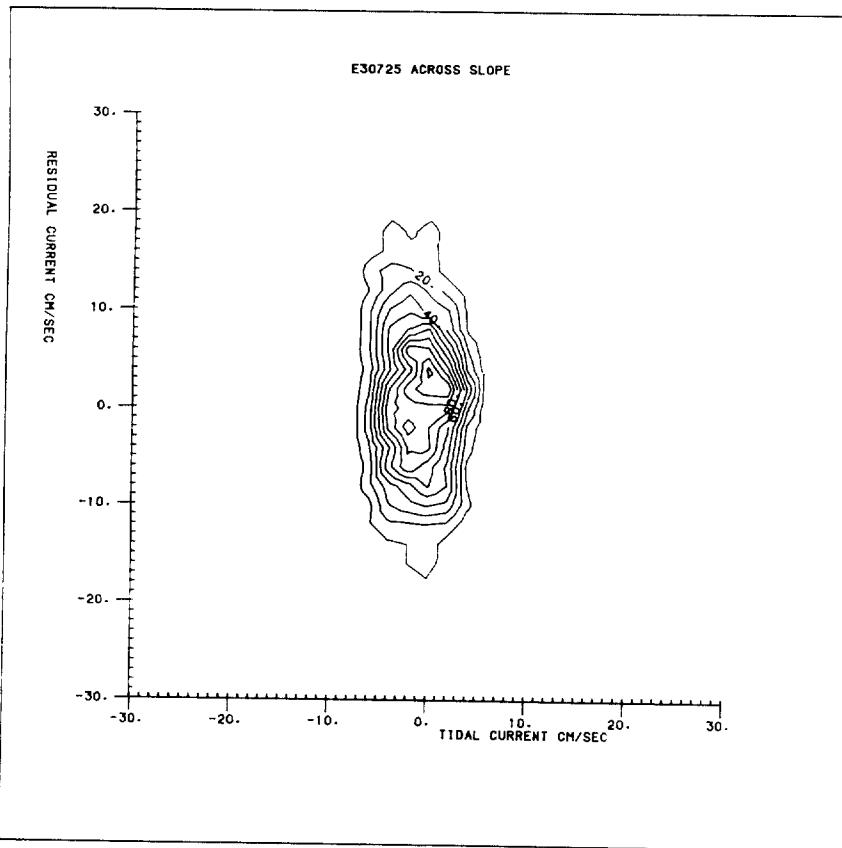
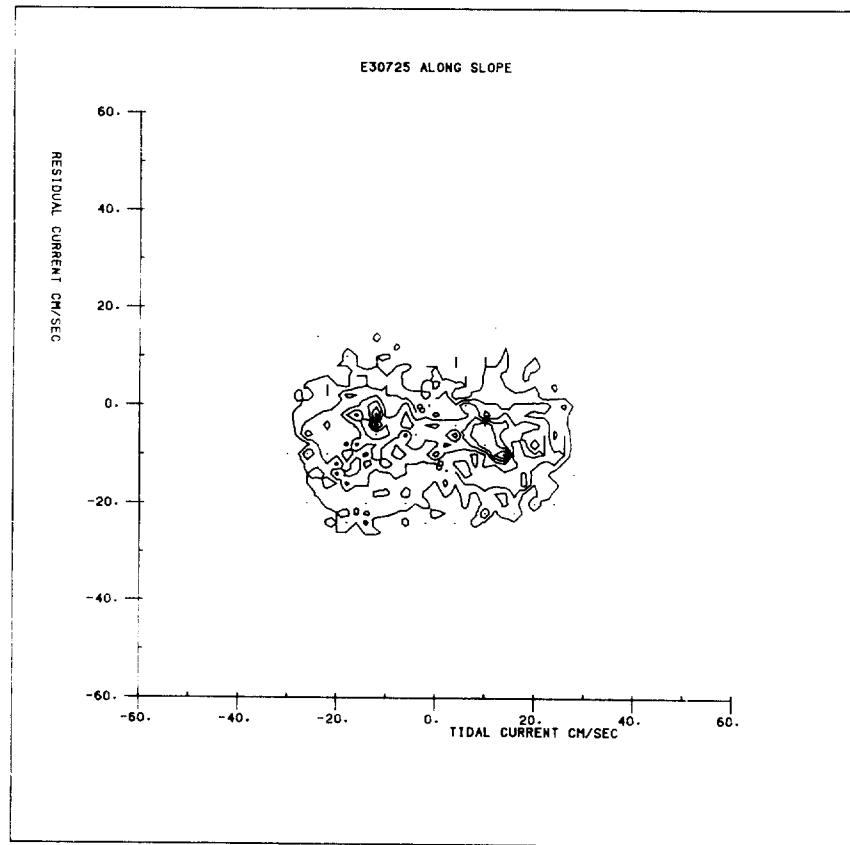
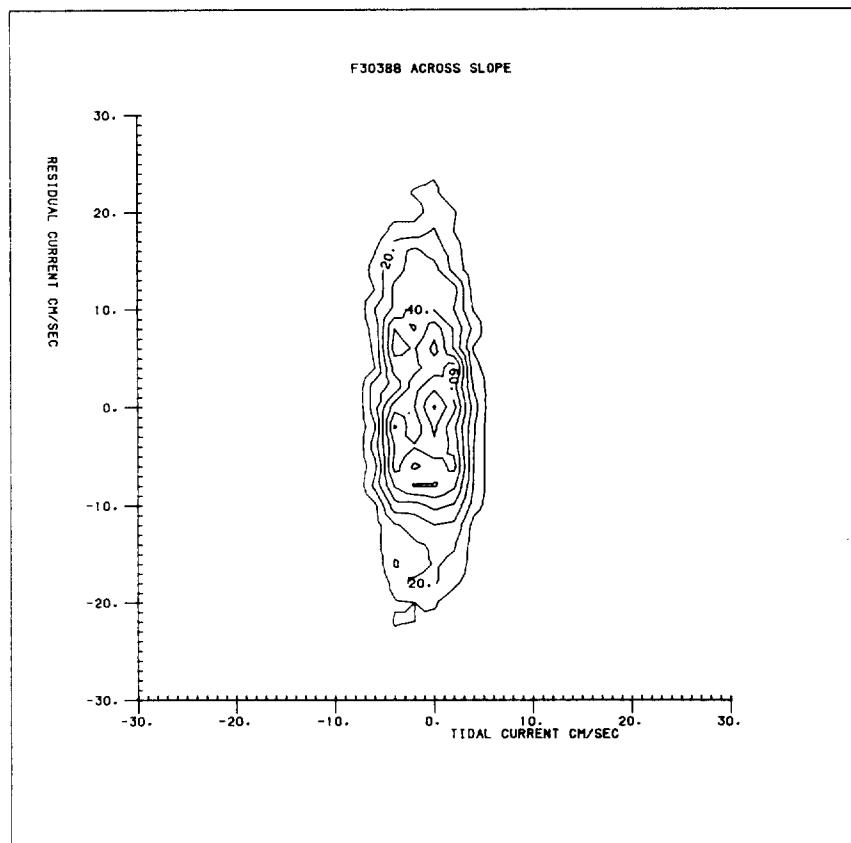
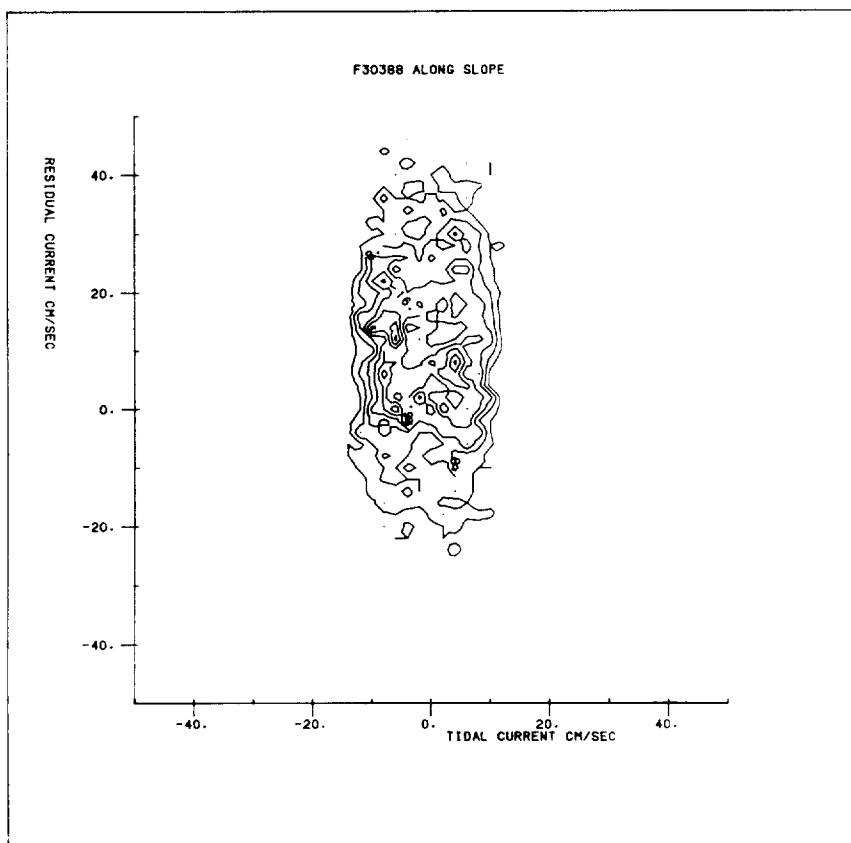
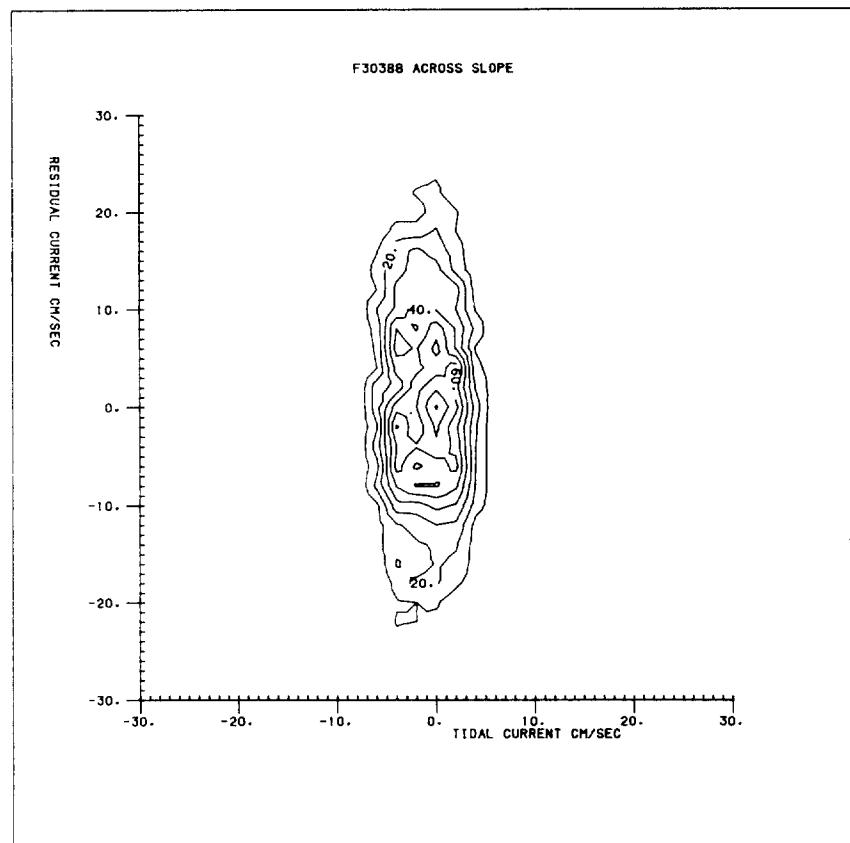
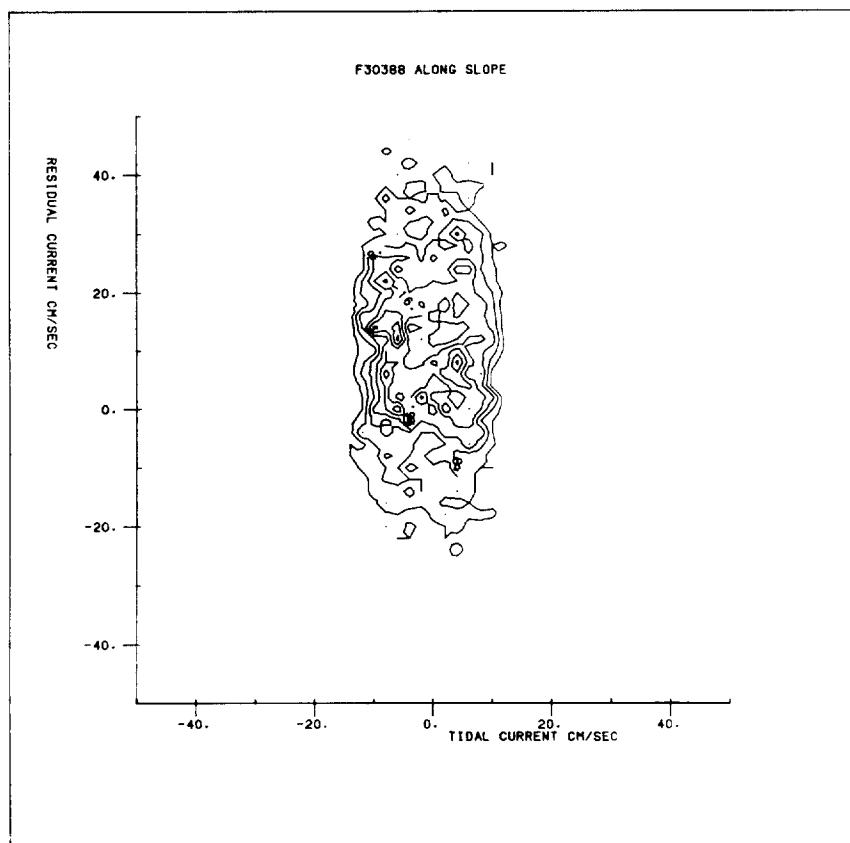


Fig.4: Examples of the joint probability distribution of tidal and residual currents.









I.O.S.

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OVER THE CONTINENTAL SLOPE OFF SCOTLAND

BY

D.J.T. CARTER, J. LOYNES AND P.G. CHALENOR

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WORMLEY

Estimates of extreme current speeds
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D.J.T. Carter, J. Loynes* and P.G. Challenor

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SUMMARY

A method for estimating return values of current speed from time-series data, based upon the convolution of tidal and non-tidal (residual) components, is described. It is applied to the CONSLEX data set of measurements obtained over the Continental Slope to the northwest of the UK during 1982-83, to obtain estimates of 50-year return values of hourly mean speed along-slope, cross-slope and omni-directional.

The method depends upon the speed of the tidal component being at least comparable with the residual component. This condition is found to hold at most CONSLEX sites west of 4°W but usually not at sites to the east of 4°W .

Histograms are presented showing the observed probability distributions of tidal and residual components of current speed and their convolutions along- and cross-slope for each CONSLEX current meter data set.

1. INTRODUCTION

As exploration for offshore oil and gas resources moves into deeper waters, so the need for estimates of extreme currents also extends into them. In particular, designers of offshore structures require estimates of extreme speeds over the continental slope to the West and North of Scotland in order to assess the feasibility and design of rigs there, where water depths are between 200m and 1000m.

Estimating extreme values of environmental parameters (such as the 50-year return value of wind speed or wave height) generally requires many years of measurements or the use of a well-validated model. Neither is available for estimating ocean currents on the UK continental slope. Fortunately, the forcing periods of the tides are well-established and extreme tidal speeds can be calculated from considerably shorter series of measurements.

If the tidal component is a significant portion of the extreme total current speed, then - as pointed out by Pugh and Vassie (1980) - estimates of extreme values can be made from relatively short data sets. This report develops a method for doing so, and applies it to estimate 50-year return values of hourly mean current speed from the Continental Slope Experiment (CONSLEX) measurements obtained between August 1982 and April 1983 from twenty moorings laid on the slope to the West and North of Scotland (Gould, 1982). The locations of these moorings are shown in Figure 1. Their co-ordinates are given, along with the water depth at each mooring, in Table 1.

Estimating extremes from records covering only about seven months is clearly unsatisfactory, particularly as we have only a limited understanding of the physics of some components of the total current. However, the tidal constituents are obtainable, with good accuracy, from the CONSLEX data; so, where the tidal stream contributes a significant portion of the total current, we might expect a reasonable estimate for the extreme speed - although it is not possible to put confidence limits upon the value - but at some current meters the tide turns out to be relatively small and here the estimates are questionable.

2. METHOD OF ANALYSIS

2.1 Probability distribution of resolved speed

Given a data series of current speed resolved in a specified direction, such as the easterly component of mean values at hourly intervals, and assuming the series is sufficiently long to estimate the tidal component, then the total speed in the specified direction at any hour, U , can be expressed as a tidal component, U_t , and a residual U_r :

$$U = U_t + U_r$$

and histograms can be constructed showing estimates for the probability distributions of U_t and U_r , p_t and p_r .

Assuming the tidal and residual components are independent, then the probability distribution of U , p_{t+r} , is given by a convolution of p_t and p_r , defined by

$$p_{t+r} = \int_{-\infty}^{\infty} p_t(x-z) p_r(z) dz \quad (1)$$

(Feller, 1971, p.144)

It readily follows that the Fourier transform of p_{t+r} equals the product of the transforms of p_t and p_r , that is:

$$p_{t+r}^* = p_t^* \cdot p_r^* \quad (2)$$

where * denotes Fourier transform. Equation 2 provides an efficient method for calculating p_{t+r}^* from p_t^* and p_r^* , and hence, by an inverse Fourier transform, for calculating p_{t+r} .

An estimate for p_{t+r} might be obtained by constructing the histogram from observations of U . The reason for using the convolution to estimate p_{t+r} is that by assuming independence of tide and residual we can essentially recombine the N observations, assuming random sampling, to give N^2 values from which to estimate p_{t+r} . Hence we obtain a smoother distribution with generally better-defined tails. However, if the tidal component U_t is much less than U_r , so that p_t is a relatively narrow distribution, then the tail of the compounded distribution p_{t+r} is dominated by p_r - or in our case by the histogram approximation for p_r . In this case, a better estimate for the tail of p_{t+r} might be obtained by fitting a distribution to the histogram for p_r and convolving this distribution with p_t . But estimates of extreme currents from the tail will then depend upon the choice of distribution. There is no theoretical or physical justification for using any particular distribution. In practice with the CONSLEX data we found that the Gaussian distribution often appeared a reasonable fit to the residual histogram p_r , but at some sites the histogram tails extended beyond the Gaussian distributions, and were closer to a Laplace distribution although this was not a good fit to the entire histogram (The Laplace distribution consists of two negative exponential distributions 'back-to-back' so is sharply peaked at the mean).

The method of moments was used to fit these distributions. The hourly residual speeds are correlated so there is no simple goodness-of-fit test apart from a visual estimate, and even here with so many data sets being analysed a few poor fits are likely to appear.

2.2 50-year return value of resolved speed

Defining the 50-year return value of hourly mean speed, U_{50} , as that which is exceeded on average once in 50 years, then it is given by

$$\text{Prob}(U_{50} < U) = 1 - 1/(365.25 \times 24 \times 50)$$

i.e.

$$\text{Prob}(U_{50} < U) \approx 0.99999772 \quad (3)$$

Hence U_{50} may be calculated given the distribution p_{t+r} - or rather two values, one from each tail of p_{t+r} , giving the 50-year speed in opposite directions.

With the definition for U_{50} , in terms of only the average interval between exceedances, its value is not affected by any correlation between the data. However, given positive correlation between successive hourly mean values, exceedances of U_{50} will tend to come together, while maintaining the average interval between exceedances of 50 years. So if the 50-year return value is defined as that which is exceeded at least once during one year in 50, then it would have a slightly lower value than that given by (3). However, Pugh and Vassie (1980) examined the effect of correlation upon estimates of return values of surface elevation and decided that any such reduction would in practice be insignificant.

2.3 Probability distribution and extreme value of total speed

Suppose U and V are current speeds resolved orthogonally so that total speed W is given by

$$W = \sqrt{U^2 + V^2}$$

Then, the distributions of U and V can be estimated from data as described above. In theory the distributions of U^2 and V^2 can then be estimated and convolved to give the distribution of W^2 and hence of W (assuming U^2 and V^2 are independent). However, the sizes of the arrays to accommodate the histograms for the distributions of U^2 and V^2 are too large for practical FFT procedures. So we estimate the distribution of W using the numerical approximation for

$$\text{Prob}(W < w) = \iint \sqrt{U^2 + V^2} p(U, V) dU dV$$

where integration is over all U, V such that $0 < \sqrt{U^2 + V^2} < w$ and $p(U, V)$ is the joint probability distribution of U and V .

i.e. $\text{Prob}(W < w) \approx \sum_{i,j} w_{ij} p(U_i, V_j) \delta U \delta V \quad (4)$

where δU and δV are the bin sizes of the histogram representation of the distributions of U and V and summation is over all bins (i, j) such that $w_{ij} < w$ where w_{ij} is the speed at the mid-point of the (i, j) bin. Assuming U and V are independent, then

$$p(U_i, V_j) \delta U \delta V = \text{Prob}(U_i < U < U_{i+1}) \text{Prob}(V_j < V < V_{j+1}) \quad (5)$$

The 50-year return value of W , W_{50} , is given by

$$\text{Prob}(W_{50} < w) \approx 0.99999772 \quad (6)$$

An alternative method for obtaining the distribution of W was considered: histograms for the distributions of the tidal and residual components of W , W_t and W_r , could be obtained, where

$$W = W_t + W_r$$

and these histograms convolved to obtain the distribution of W . But this method fails because W_t and W_r are not independent - since W cannot be negative.

3. APPLICATION TO THE CONSLEX DATA

3.1 General description of the data sets

The method of analysis described above was applied to the CONSLEX data set of hourly mean current speeds associated with 'spot' measurements of direction. The data were obtained from the IOS Marine Information and Advisory Service data base, including the results of tidal analysis carried out at IOS (Bidston).

The CONSLEX data consists of 53 sets of recordings made by DAFS, IOS and SMBA from 20 moorings, using Anderaa current meters deployed between 23 August 1982 and 31 April 1983 - measurements at one site (I2) extended into May 1983. The sites of these moorings and the notation identifying them are shown in Fig. 1 together with the approximate orientation, θ , of the maximum variance of current velocity.

This orientation was calculated for each meter by a principal component analysis of the current velocity. In general it was found to lie along the slope; the flow seems to be constrained by topography. The direction of the line of maximum variance is not specified by this analysis. The direction arrows shown in Fig. 1 were specified in order to fix the co-ordinate system. The variation in θ between meters at any one mooring was generally within $\pm 10^\circ$, and an average direction is shown in Fig. 1. Where the spread was greater than $\pm 10^\circ$, the range of θ is shown. The 'cross-slope' axis was taken as positive to the right of the along-slope, ie. up-slope. The data were analysed in a co-ordinate system defined by

the value of θ for the individual meter - thus ensuring zero correlation between resolved current speeds - but directions are referred to as 'along-slope' and 'up-slope'. Further details, including the depth of each instrument and the values of θ , are given in Table 2.

Site I2 is not on the slope, but in the Rockall Trough with a water depth of 1463m. Section D is on the Wyville-Thomson Ridge; currents at D5 in particular appear unlike those on the slope, as indicated by the wide range of θ with depth - similar to that at I2.

Records from the current meter at G4 at 496m cover only 34 days, and at B1 (130m) only 58 days. The other meter at B1 and both meters at B2 had to be replaced during October 1982 - with the loss of some days of records at B2.

3.2 Maximum observed current speeds

The maximum mean hourly current speed recorded by each instrument and associated direction are included in Table 2.

The maximum recorded hourly mean current speed was 117 cm/s at E4 at a depth of 111m. The only other measurement exceeding 100 cm/s was at G2 at 151m. Generally the maximum speeds at each mooring tended to decrease with increasing meter depth; an exception was at E3 where 100 cm/s was recorded at 725m. The direction of the maximum speed was usually within about 20° of the direction given by the principal component analysis; a notable exception was that of 66 cm/s at E4 at 950m which was 79° away (down-slope).

3.3 Probability distributions of current speeds and estimates of return values

Using the data from each meter, except B1 (130m) and G4 (496m) with less than two months data, histograms showing the distribution of tidal and residual current speeds along-slope and up-slope were constructed with a bin size of 1 cm/s, or 2 cm/s if a component speed exceeded 100 cm/s. These histograms, together with their convolution are shown in the set of figures: Fig. 2. (Strictly, the histograms should be drawn as step functions, but joining mid-points of the bin values gives a clearer picture.)

Fig. 2 shows that the along-slope flow is generally considerably stronger than the up-slope. It also shows that the residual current is usually stronger than the tidal component - but not, for example, at A1 (145m) and at D1 and D2. Sometimes the residual is very much stronger than the tidal component particularly for the up-slope flow, and the convolution is then a smoothed version of the residual histogram, so the tails of the convolution are dominated by the few calculated extreme residual values, eg. F3 at 388m. In these cases it seems preferable to fit a distribution to the residual histogram and to convolve this distribution with the tidal histogram. The set of figures, Fig. 3, show the Gaussian and Laplacian fits to the cumulative distribution of residual components - scaled such that the Gaussian distribution is linear. Generally the Gaussian distribution appears to be a reasonable fit to the residuals; occasionally the observations in the tails deviate from the straight line, but these are determined by only a few values so their sampling variance is high. Construction of confidence limits would require an analysis of the

correlation structure of the data; but where the data approaches the long-tailed Laplace distribution the use of the Gaussian distribution must be expected to underestimate extreme values.

The fifty-year return values of current speed up- and down-slope and in both directions along-slope were estimated using equation 3 and the convolutions with the residual histograms and the Gaussian fit. Results are shown in Table 3.

Values are given to the nearest bin size, that is ± 2 cm/s for the higher values and ± 1 cm/s for the lower.

Note that the fifty-year return values are given by interpolation of the convolution. No extrapolation is required.

The convolution only gives the distribution of the sum of the tidal and residual components if these components are independent. There is no entirely satisfactory method for testing independence, but examples of the joint distributions of the tide and residual components plotted in the set: Fig. 4 show no obvious dependence. On physical grounds, one might expect negative correlation between tide and residual in shallow water or at current meters close to the sea bed, but none is apparent in Fig. 4, or in other joint distributions which we examined. If there were negative correlation then the convolution would overestimate the fifty-year return values.

Table 3 also includes fifty-year return values of total speed, U_{50} , calculated from equations (4)-(6), and the maximum observed speeds from

Table 2. The choice of θ from the principal component analysis ensures no correlation between the measured 'up-slope' and 'along-slope' speeds. The requirement of (5) is stronger, requiring independence between the two distributions, but this seems a not-unreasonable assumption.

The values for U_{50} from the residual histogram are given in brackets if Fig. 2 suggests that the dominant tail of the component convolution has a negligible tidal contribution. The value of U_{50} from the Gaussian fit is in brackets if Fig. 3 indicates that the dominant residual component is not Gaussian.

4. CONCLUSIONS

An inspection of the bracketed (more dubious) estimates in Table 3 for the 50-year return value of hourly mean current speed, U_{50} , indicates that the method proposed in this report might be expected to give reasonable results at CONSLEX sites A to E, but further North at F and G (except at F1 and G1 in less than 200m) the method is less satisfactory; the tidal components are here considerably weaker than the residual currents and often these residuals do not appear to be normally distributed.

The highest estimate for U_{50} from the analysis of the CONSLEX data is 133 cm/s for mooring E4 at 111m, with a water depth of 1015m. This was where the highest recorded current speed of 117 cm/s was obtained. Fig. 3 (E4, 111m) shows apparently anomalous residuals along-slope, towards the North East approaching 100 cm/s, which convolve with the along-slope tidal stream exceeding 30 cm/s. The origin of these anomalous residuals, perhaps associated with the oceanic front separating deep and coastal waters, requires further investigation.

Nearby at E3 at 725m, the estimated value of U_{50} is 94 cm/s while the maximum recorded current speed was 100 cm/s; the greatest recorded residual happened to occur within a few hours of the maximum recorded tide.

At the deep water site of I2, which is off the slope in a depth of 1463m, the method does not give satisfactory estimates of U_{50} at the two current meters below 1000m because the tidal components are small compared to the residuals. The method appears to be reasonable at shallower depths.

However, because of our lack of knowledge of all the mechanisms producing extreme currents at sites off the continental shelf including their within-year variability, estimates of the 50-year return value of current speed made from data recorded over only a few months must be viewed with caution. Even where the method suggested in this report appears to be satisfactory, further data are needed to confirm its applicability and to put confidence limits upon the results.

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Table 1: CONSLEX mooring sites

| Mooring | Latitude (N) | Longitude | Water depth (m) |
|---------|--------------|-----------|-----------------|
| A1 | 57° 20.7' | 9° 07.2'W | 145 |
| A5 | 57° 18.6' | 9° 40.4'W | 1614 |
| B1 | 57° 56.3' | 8° 51.0'W | 155 |
| B2 | 58° 00.7' | 9° 07.7'W | 193 |
| B3 | 58° 06.5' | 9° 33.1'W | 504 |
| B4 | 58° 08.3' | 9° 41.2'W | 1082 |
| C2 | 59° 05.4' | 7° 27.0'W | 514 |
| C3 | 59° 08.5' | 7° 42.4'W | 998 |
| D1 | 59° 39.8' | 6° 02.5'W | 237 |
| D2 | 59° 46.7' | 6° 10.8'W | 370 |
| D5 | 60° 09.9' | 7° 44.5'W | 637 |
| E2 | 60° 13.3' | 4° 31.8'W | 478 |
| E3 | 60° 31.2' | 4° 56.8'W | 1035 |
| E4 | 60° 46.4' | 4° 49.4'W | 1015 |
| F1 | 61° 09.3' | 1° 31.7'W | 189 |
| F3 | 61° 24.8' | 2° 06.1'W | 995 |
| G1 | 61° 30.7' | 0° 02.5'E | 191 |
| G2 | 62° 06.1' | 0° 03.9'E | 550 |
| G4 | 63° 08.8' | 0° 00.9'W | 1611 |
| I2 | 60° 12.7' | 9° 13.3'W | 1463 |

Table 2: CONSLEX current meter records

| Mooring | meter | days of | max. recorded hr mean vely. | dir^n princ. |
|---------|-----------|---------|---|------------------------------|
| | depth (m) | records | speed (cm/s) dir^n towards (° from N) | component (θ°) |
| A1 | 55 | 106 | 59 | 031 046 |
| | 120 | 181 | 44 | 307 042 |
| A5 | 209 | 179 | 57 | 347 333 |
| | 510 | 179 | 45 | 340 333 |
| | 1111 | 179 | 49 | 186 343 |
| | 1562 | 179 | 33 | 339 341 |
| B1 | 55 | 173 | 70 | 033 032 |
| | 130 | 58 | 61 | 194 031 |
| B2 | 43 | 120 | 53 | 023 036 |
| | 168 | 120 | 47 | 033 033 |
| B3 | 104 | 172 | 63 | 035 025 |
| | 257 | 172 | 54 | 028 025 |
| | 457 | 169 | 50 | 043 036 |
| B4 | 169 | 172 | 53 | 023 017 |
| | 477 | 172 | 50 | 014 019 |
| | 1035 | 172 | 38 | 184 013 |
| C2 | 115 | 172 | 82 | 043 051 |
| | 266 | 172 | 77 | 050 048 |
| | 468 | 172 | 76 | 037 035 |
| C3 | 104 | 172 | 58 | 199 041 |
| | 403 | 172 | 52 | 049 046 |
| | 951 | 172 | 46 | 027 008 |
| D1 | 87 | 136 | 80 | 054 049 |
| | 212 | 136 | 82 | 227 050 |
| D2 | 120 | 169 | 86 | 078 061 |
| | 270 | 169 | 79 | 074 065 |
| | 345 | 169 | 69 | 057 066 |
| D5 | 510 | 186 | 88 | 208 051 |
| | 633 | 186 | 85 | 194 007 |

Table 2 continued

| Mooring | meter depth (m) | days of records | max. recorded hr speed (cm/s) | mean vely. dir ⁿ towards (° from N) | dir ⁿ princ. component (θ°) |
|---------|--------------------|--------------------|----------------------------------|--|---|
| E2 | 453 | 162 | 77 | 033 | 047 |
| E3 | 120 | 164 | 95 | 92 | 063 |
| | 419 | 164 | 83 | 027 | 052 |
| | 725 | 164 | 100 | 212 | 055 |
| E4 | 111 | 184 | 117 | 063 | 053 |
| | 950 | 181 | 66 | 158 | 057 |
| F1 | 39 | 163 | 88 | 076 | 081 |
| F3 | 79 | 80 | 89 | 084 | 063 |
| | 388 | 161 | 66 | 046 | 035 |
| | 694 | 161 | 60 | 244 | 049 |
| | 945 | 161 | 66 | 030 | 044 |
| G1 | 41 | 117 | 48 | 133 | 108 |
| | 166 | 117 | 33 | 117 | 107 |
| G2 | 151 | 162 | 114 | 073 | 073 |
| | 299 | 162 | 89 | 069 | 062 |
| | 500 | 162 | 84 | 106 | 079 |
| G4 | 195 | 164 | 64 | 98 | 053 |
| | 496 | 34 | 26 | 021 | 028 |
| | 1104 | 164 | 32 | 212 | 051 |
| | 1554 | 164 | 34 | 206 | 044 |
| I2 | 251 | 216 | 60 | 331 | 022 |
| | 654 | 222 | 45 | 106 | 038 |
| | 1055 | 216 | 67 | 182 | 020 |
| | 1440 | 222 | 75 | 144 | 343 |

Table 3: Estimates of 50-year current speeds (cm/s)

| Mooring | meter depth (m) | Residual Histogram | | | | | | Gaussian fit | | | | | | MAX. OBS. SPEED |
|---------|-----------------------|--------------------|-----|----------|----|----------------|-------------|--------------|----------|----|----------------|----|--|-----------------------|
| | | Along-slope | | up-slope | | TOTAL SPEED | Along-slope | | up-slope | | TOTAL SPEED | | | |
| | | + | - | + | - | | + | - | + | - | | | | |
| A1 | 55 | 65 | 66 | 51 | 58 | 69 | 62 | 60 | 53 | 54 | 66 | 59 | | |
| | 120 | 52 | 50 | 44 | 47 | 55 | 49 | 51 | 45 | 46 | 54 | 44 | | |
| A5 | 209 | 58 | 43 | 47 | 29 | (63) | 75 | 55 | 42 | 36 | 75 | 57 | | |
| | 510 | 47 | 32 | 36 | 23 | (50) | 63 | 46 | 34 | 29 | 63 | 45 | | |
| | 1111 | 46 | 50 | 29 | 27 | 50 | 52 | 46 | 28 | 28 | (52) | 49 | | |
| | 1562 | 39 | 33 | 27 | 29 | (40) | 42 | 37 | 27 | 29 | 42 | 33 | | |
| | | | | | | | | | | | | | | |
| B1 | 55 | 95 | 75 | 54 | 47 | 96 | 99 | 83 | 45 | 43 | 101 | 70 | | |
| B2 | 43 | 79 | 69 | 56 | 45 | 81 | 81 | 79 | 55 | 51 | 83 | 53 | | |
| | 168 | 63 | 54 | 34 | 27 | 63 | 60 | 52 | 29 | 30 | 60 | 47 | | |
| B3 | 104 | 73 | 41 | 32 | 37 | 74 | 77 | 48 | 33 | 36 | 77 | 63 | | |
| | 257 | 59 | 33 | 21 | 28 | 59 | 64 | 38 | 25 | 29 | 65 | 54 | | |
| | 457 | 57 | 36 | 24 | 30 | 58 | 62 | 41 | 25 | 31 | 62 | 50 | | |
| | 169 | 64 | 48 | 38 | 31 | 65 | 70 | 53 | 32 | 33 | 70 | 53 | | |
| B4 | 477 | 59 | 38 | 26 | 28 | 60 | 62 | 50 | 22 | 24 | 62 | 50 | | |
| | 1035 | 42 | 44 | 10 | 13 | 44 | 49 | 46 | 10 | 12 | 49 | 38 | | |
| | | | | | | | | | | | | | | |
| C2 | 115 | 97 | 45 | 27 | 45 | 97 | 101 | 45 | 25 | 47 | 101 | 82 | | |
| | 266 | 88 | 38 | 24 | 33 | 89 | 93 | 42 | 20 | 35 | 93 | 77 | | |
| | 468 | 90 | 37 | 31 | 32 | 91 | 81 | 44 | 28 | 33 | (82) | 76 | | |
| C3 | 104 | 67 | 71 | 52 | 35 | 72 | 80 | 62 | 48 | 49 | (80) | 58 | | |
| | 403 | 59 | 51 | 29 | 27 | 60 | 61 | 48 | 33 | 34 | (62) | 52 | | |
| | 951 | 60 | 51 | 41 | 39 | 62 | 63 | 54 | 40 | 39 | 64 | 46 | | |
| D1 | 87 | 95 | 89 | 49 | 45 | 97 | 107 | 91 | 49 | 43 | 107 | 80 | | |
| | 212 | 82 | 94 | 30 | 41 | 94 | 95 | 83 | 31 | 33 | (95) | 82 | | |
| D2 | 120 | 95 | 65 | 57 | 41 | 97 | 99 | 73 | 59 | 43 | 101 | 86 | | |
| | 270 | 95 | 61 | 51 | 39 | 97 | 95 | 73 | 51 | 41 | 97 | 79 | | |
| | 345 | 97 | 65 | 49 | 47 | 99 | 93 | 71 | 49 | 43 | 93 | 69 | | |
| D5 | 510 | 81 | 101 | 57 | 74 | 102 | 83 | 91 | 65 | 69 | (91) | 88 | | |
| | 633 | 65 | 103 | 49 | 75 | (103) | 59 | 102 | 51 | 57 | 102 | 85 | | |

Table 3 continued

| Mooring | meter depth (m) | Residual Histogram | | | | | | Gaussian fit | | | | | | MAX. OBS. SPEED |
|---------|-----------------------|--------------------|----|----------|----|----------------|-------------|--------------|----------|-----|----------------|-----|--|-----------------------|
| | | Along-slope | | up-slope | | TOTAL SPEED | Along-slope | | up-slope | | TOTAL SPEED | | | |
| | | + | - | + | - | | + | - | + | - | | | | |
| E2 | 453 | 87 | 64 | 43 | 46 | 88 | 109 | 63 | 37 | 45 | 109 | 77 | | |
| E3 | 120 | 101 | 84 | 79 | 91 | 113 | 113 | 109 | 99 | 103 | 119 | 95 | | |
| | 419 | 83 | 78 | 51 | 58 | 89 | 87 | 91 | 69 | 71 | 93 | 83 | | |
| | 725 | 58 | 93 | 57 | 37 | 94 | 65 | 78 | 47 | 43 | (78) | 100 | | |
| E4 | 111 | 131 | 95 | 79 | 63 | 133 | 115 | 111 | 93 | 85 | (119) | 117 | | |
| | 950 | 46 | 86 | 77 | 24 | 92 | 60 | 75 | 51 | 39 | (75) | 66 | | |
| F1 | 39 | 97 | 53 | 44 | 61 | 98 | 94 | 64 | 42 | 65 | 96 | 88 | | |
| F3 | 79* | 117 | 51 | 48 | 73 | (121) | 115 | 67 | 63 | 81 | (117) | 89 | | |
| | 388 | 71 | 71 | 38 | 47 | (74) | 90 | 70 | 52 | 52 | 91 | 66 | | |
| | 694 | 73 | 69 | 43 | 43 | (74) | 85 | 111 | 37 | 41 | (111) | 60 | | |
| | 945 | 78 | 64 | 36 | 40 | (78) | 89 | 102 | 35 | 37 | (102) | 66 | | |
| G1 | 41 | 73 | 65 | 57 | 49 | 75 | 71 | 60 | 59 | 56 | 73 | 48 | | |
| | 166 | 50 | 40 | 40 | 33 | 50 | 47 | 40 | 37 | 36 | 47 | 33 | | |
| G2 | 151 | 128 | 29 | 67 | 67 | (129) | 134 | 47 | 61 | 69 | 135 | 114 | | |
| | 299 | 98 | 23 | 53 | 47 | (100) | 127 | 77 | 47 | 47 | (127) | 89 | | |
| | 500 | 81 | 31 | 68 | 52 | (87) | 90 | 46 | 54 | 60 | 92 | 84 | | |
| G4 | 195 | 58 | 44 | 49 | 57 | (71) | 78 | 65 | 59 | 63 | 79 | 64 | | |
| | 1104 | 30 | 31 | 20 | 26 | (35) | 42 | 37 | 31 | 31 | (43) | 32 | | |
| | 1554 | 34 | 35 | 22 | 22 | (37) | 43 | 36 | 31 | 30 | (44) | 34 | | |
| I2 | 251 | 59 | 63 | 103 | 55 | 103 | 61 | 59 | 103 | 51 | 103 | 60 | | |
| | 654 | 46 | 47 | 50 | 41 | 58 | 51 | 48 | 52 | 46 | (56) | 45 | | |
| | 1055 | 35 | 71 | 53 | 41 | (73) | 55 | 71 | 45 | 46 | (71) | 67 | | |
| | 1440 | 69 | 85 | 68 | 49 | (92) | 71 | 86 | 71 | 40 | (89) | 75 | | |

* F3(79m): only 80 days of records.

Fig.1: CONSLEX mooring sites and direction of axis determined by principal component analysis of current records. (A range is shown where directions from each meter on a mooring differed by more than 10° .)



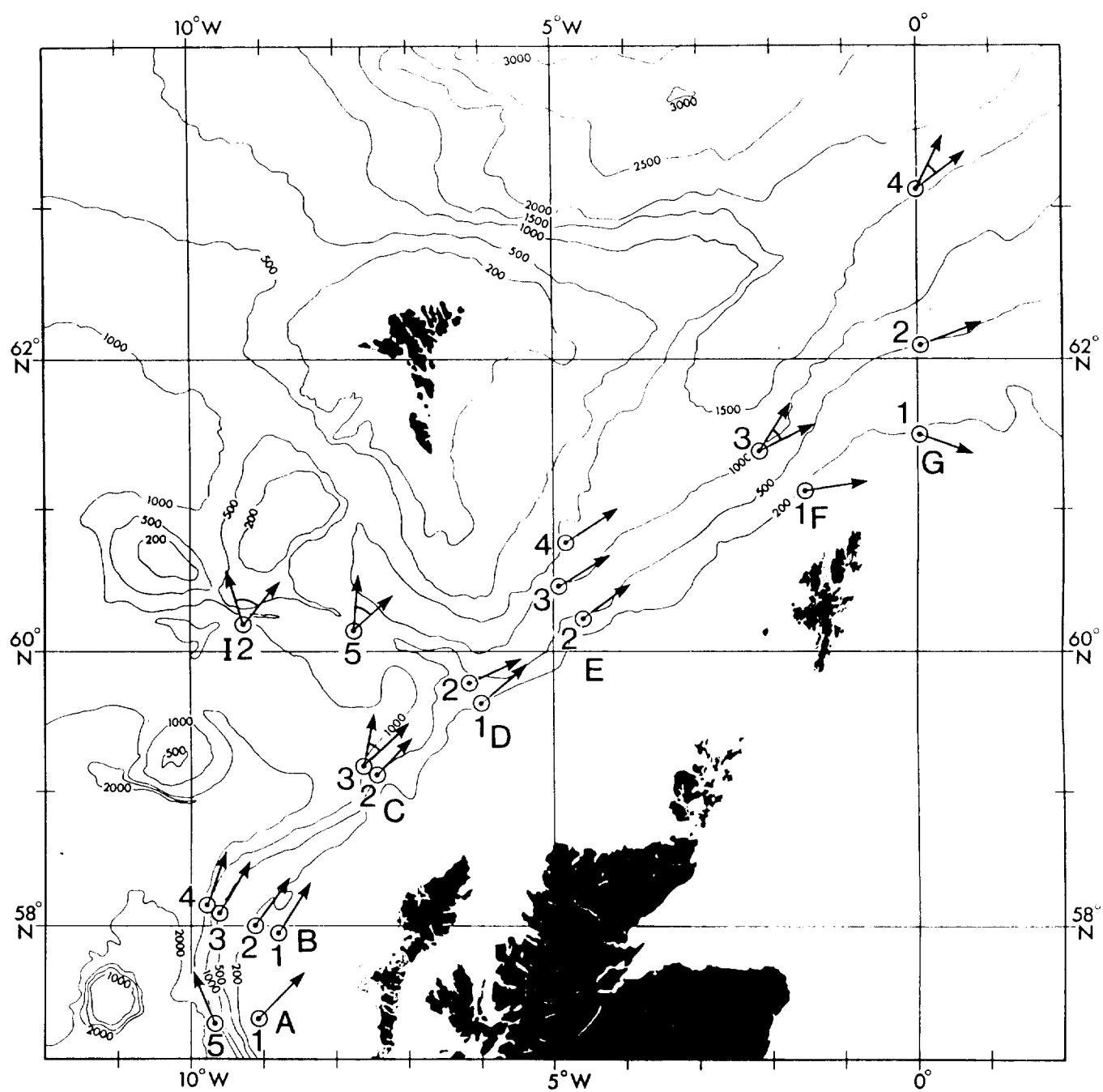
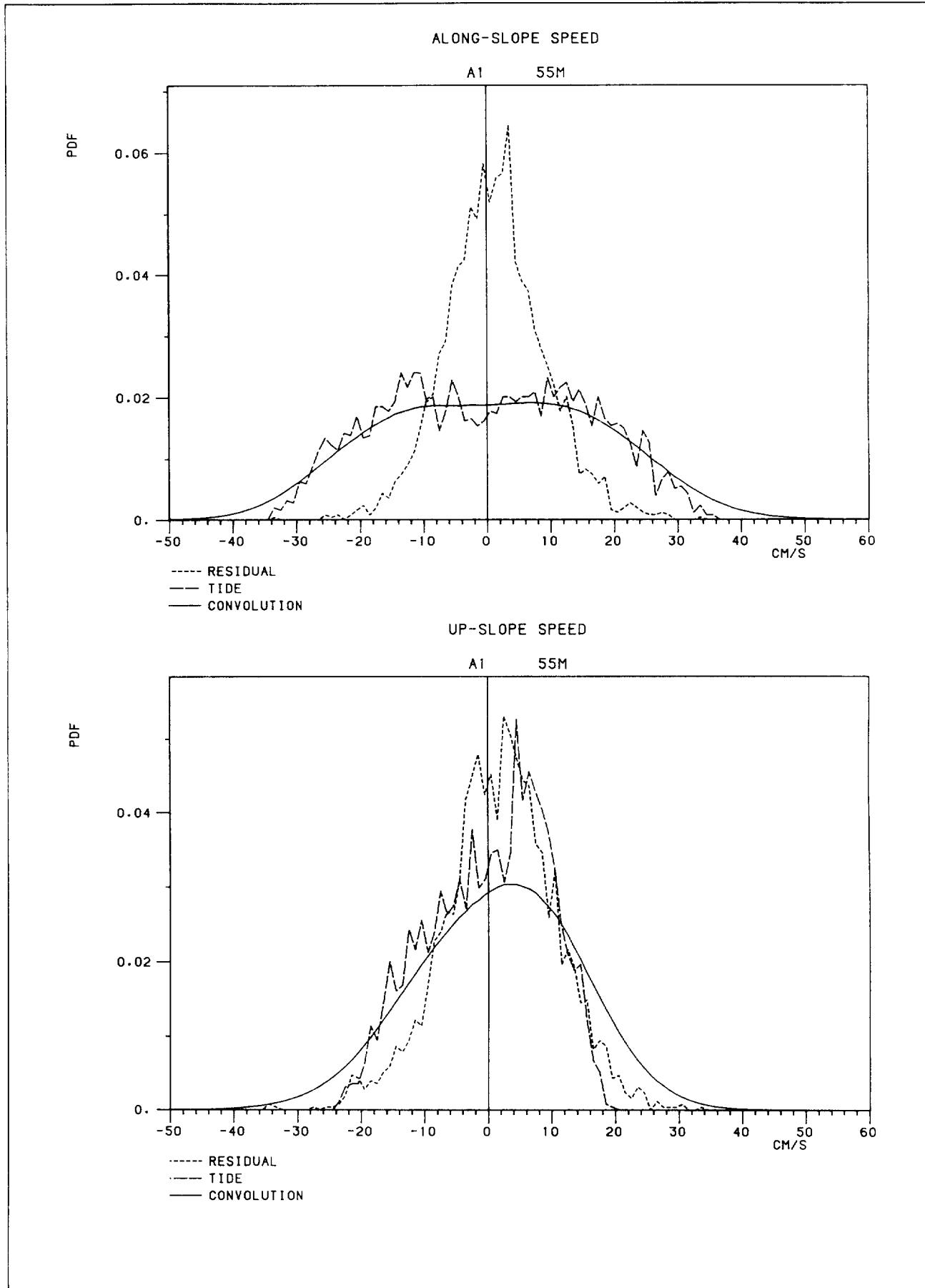
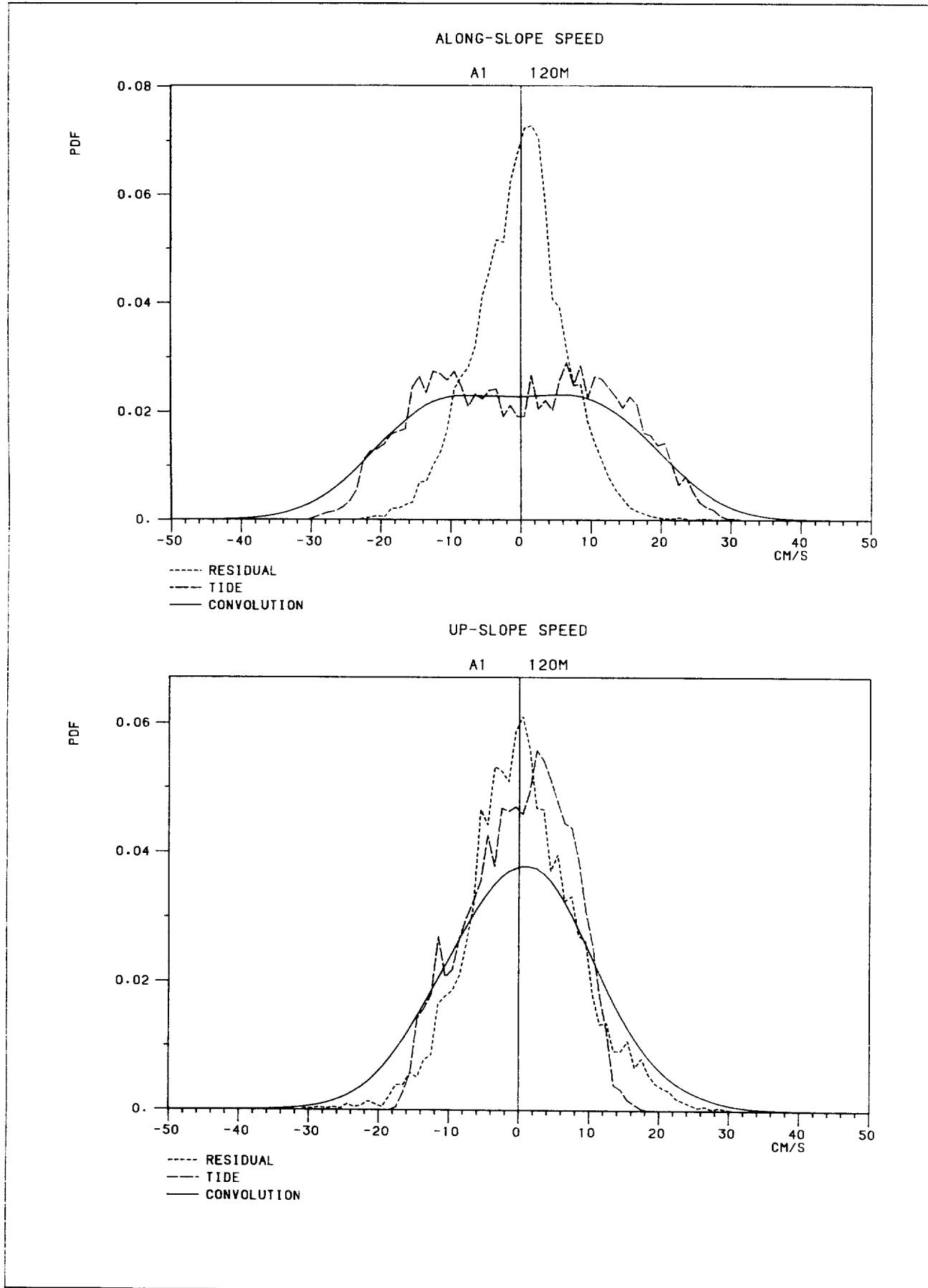
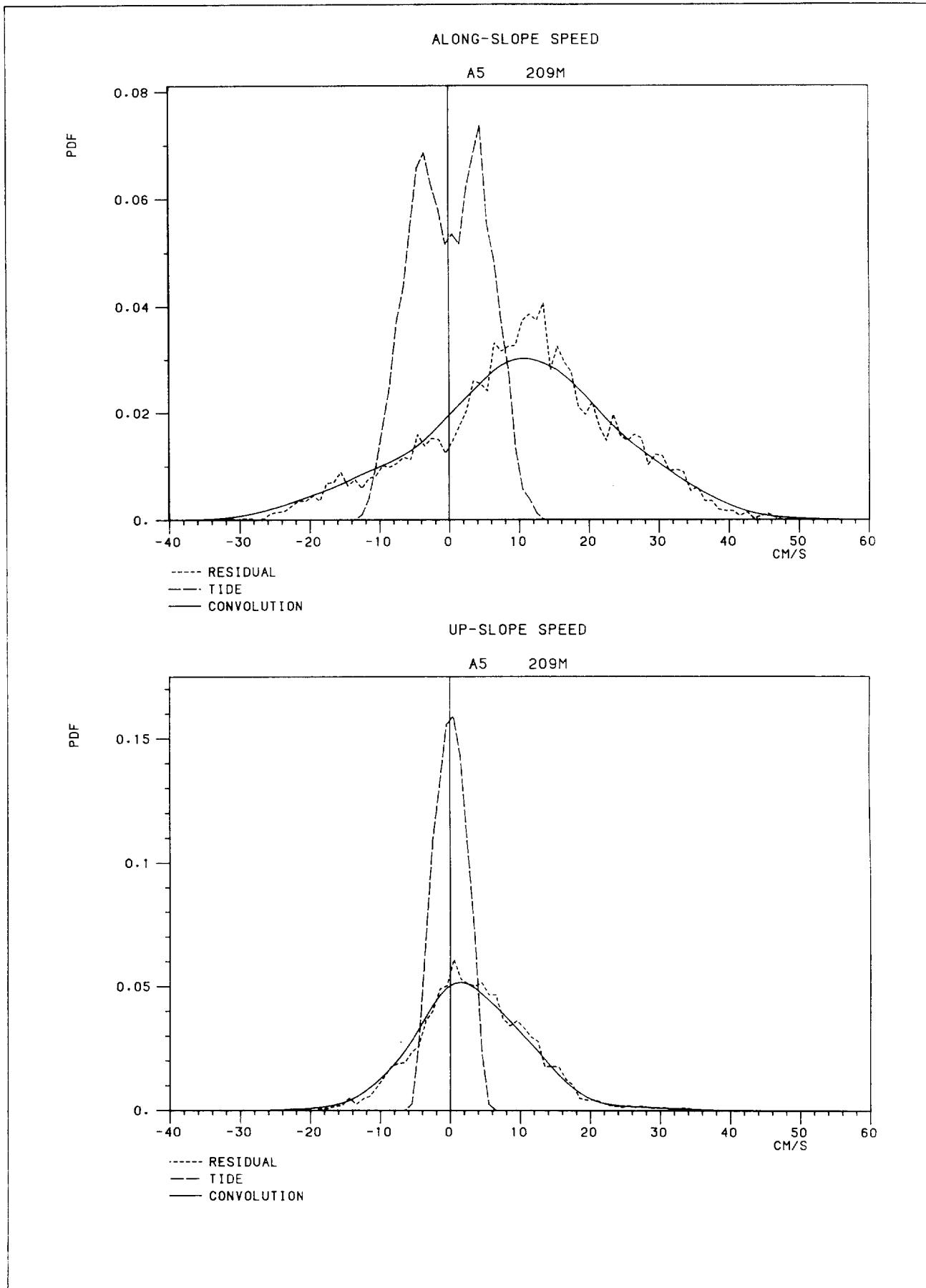
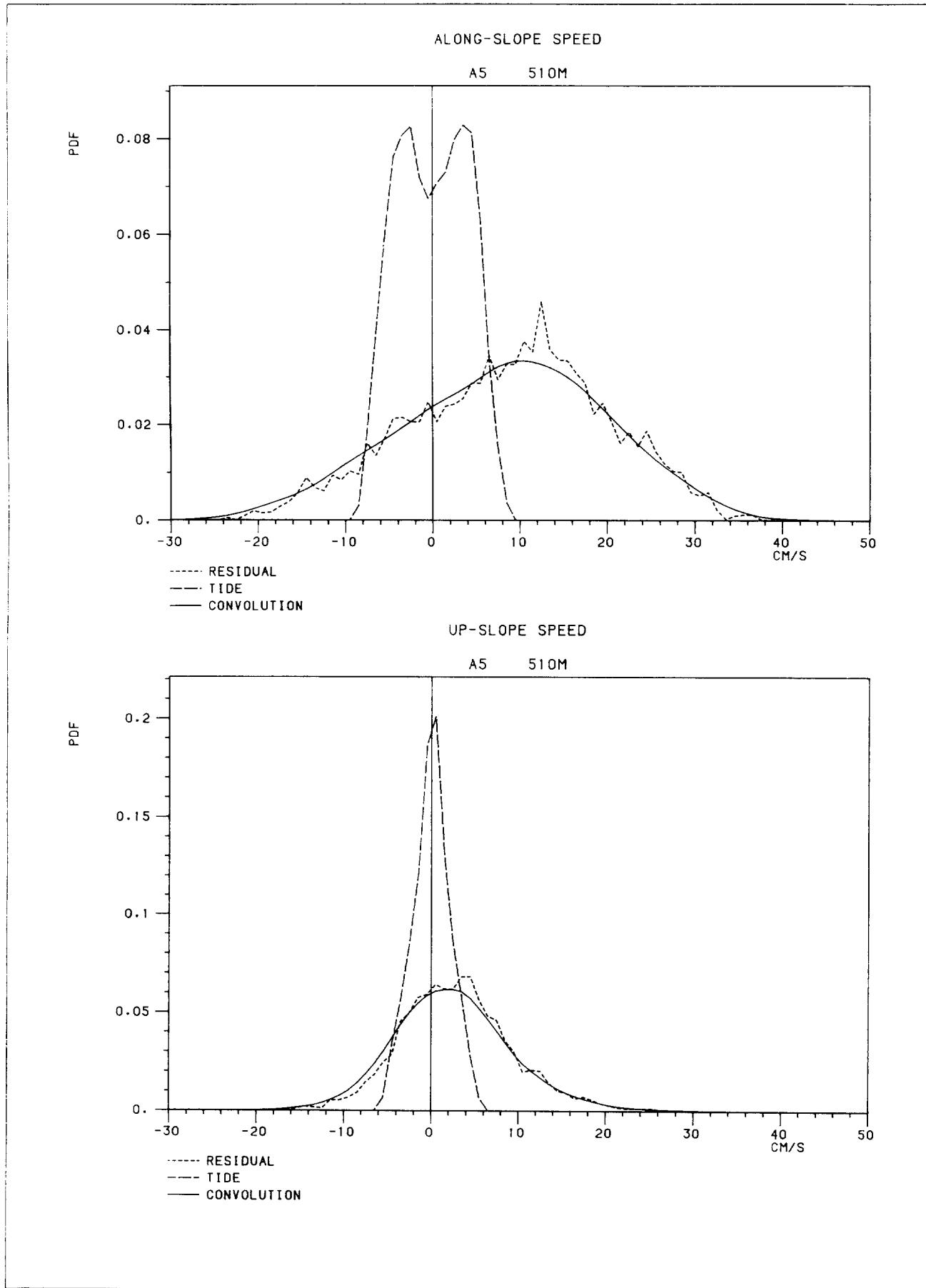


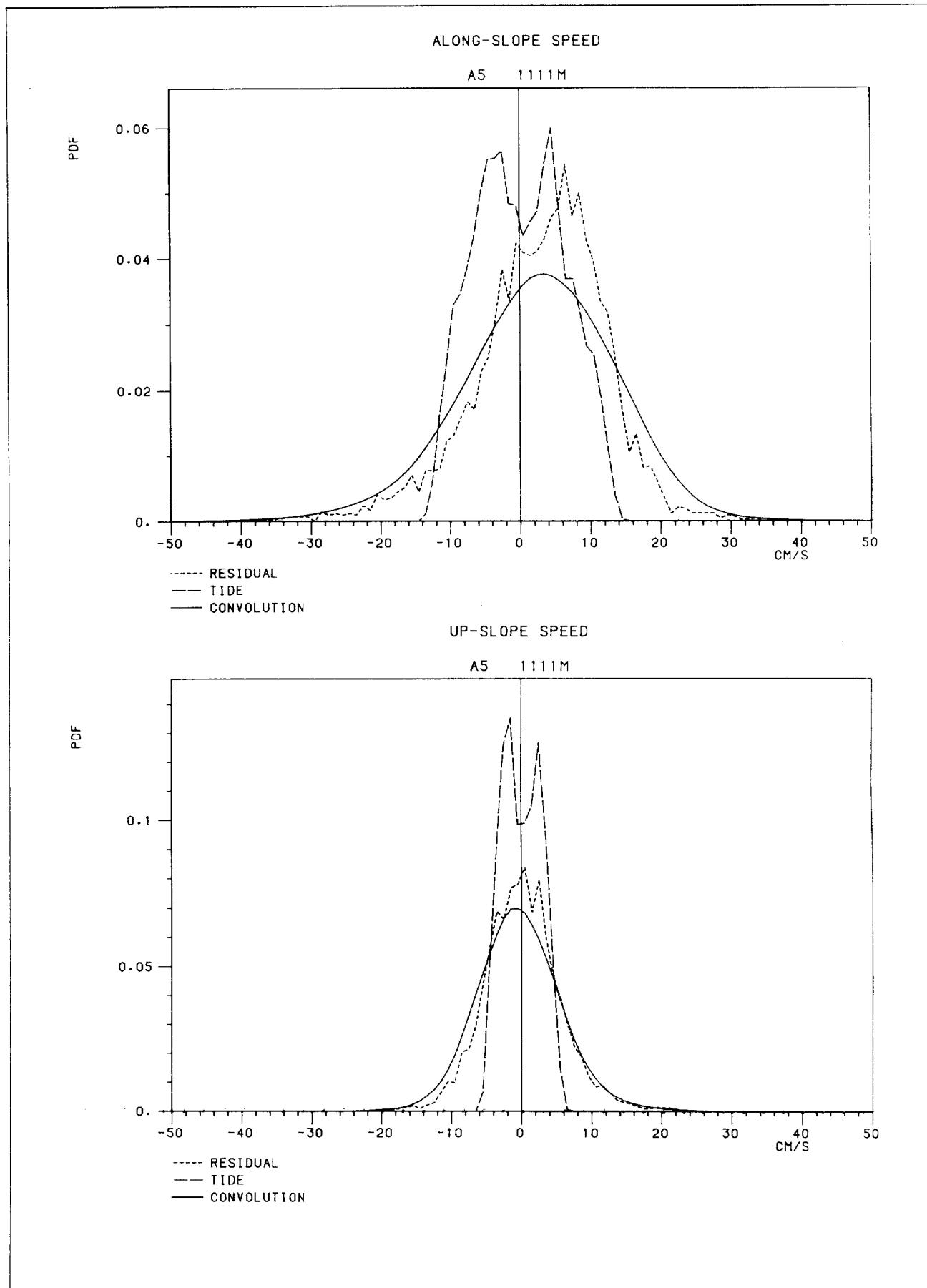
Fig.2: Probability distribution functions of residual and tidal current speeds along- and up-slope from speeds recorded by each current meter and their convolutions. (The meter is identified by the mooring and by the depth of the meter below the sea surface.)

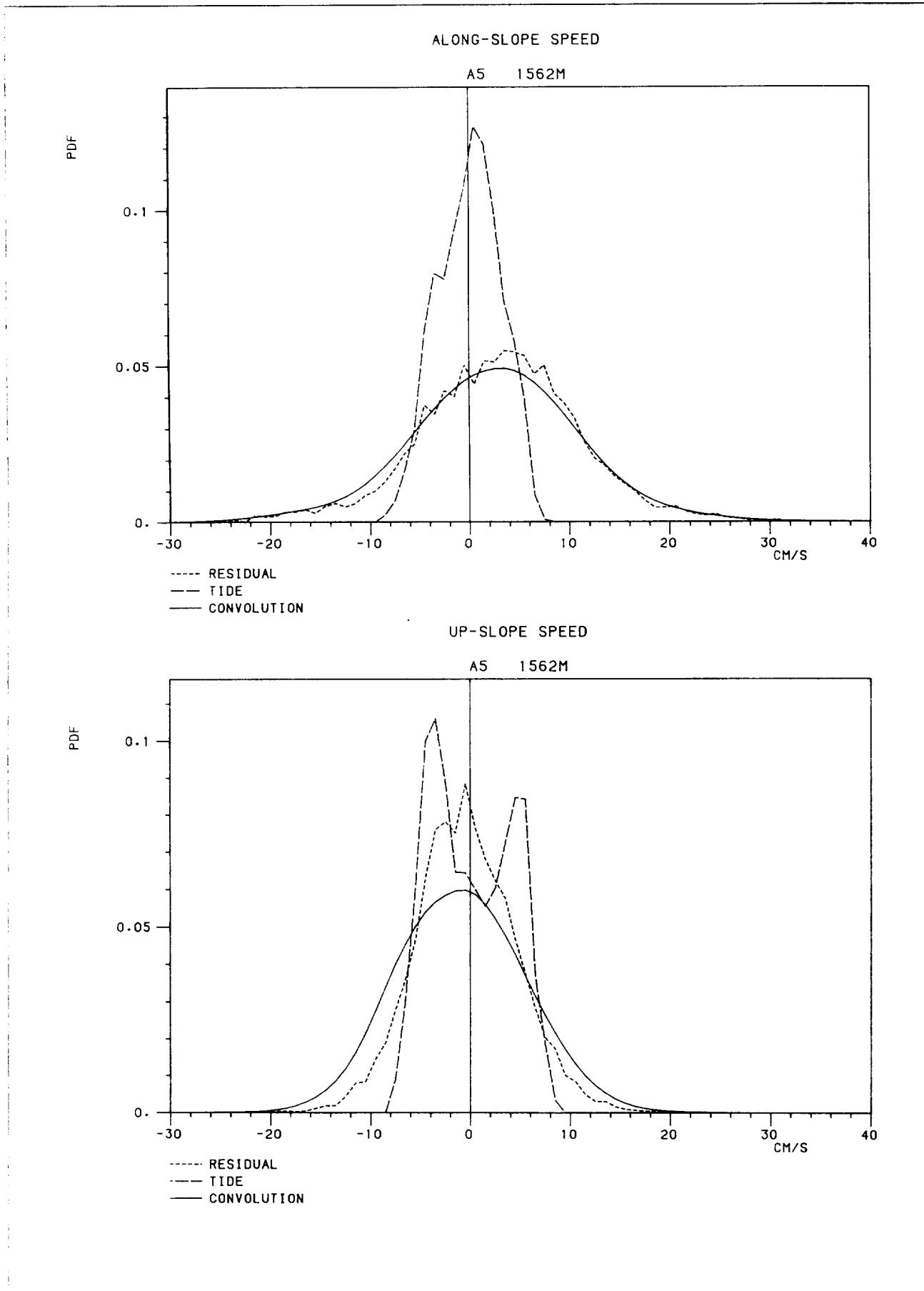


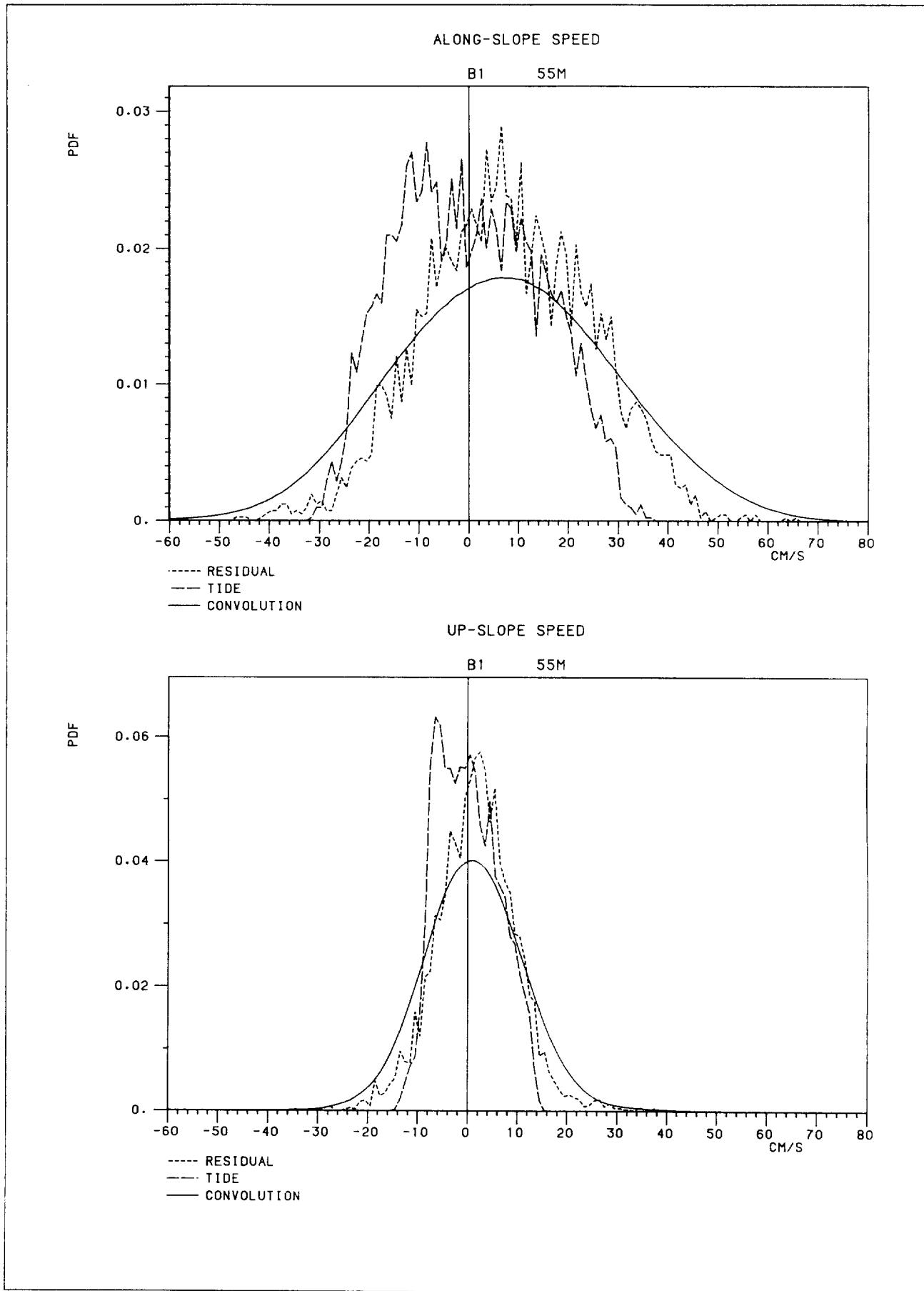


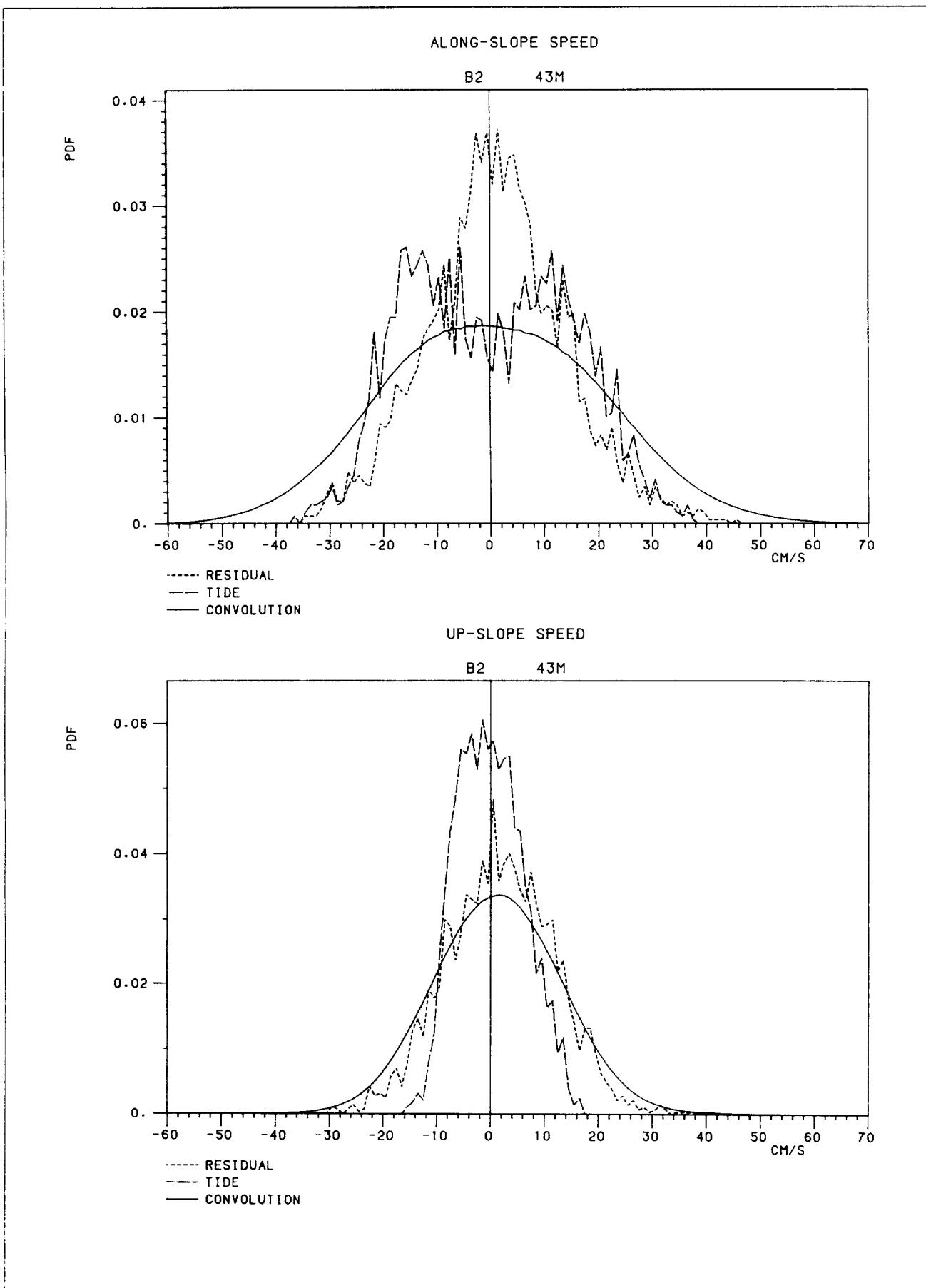


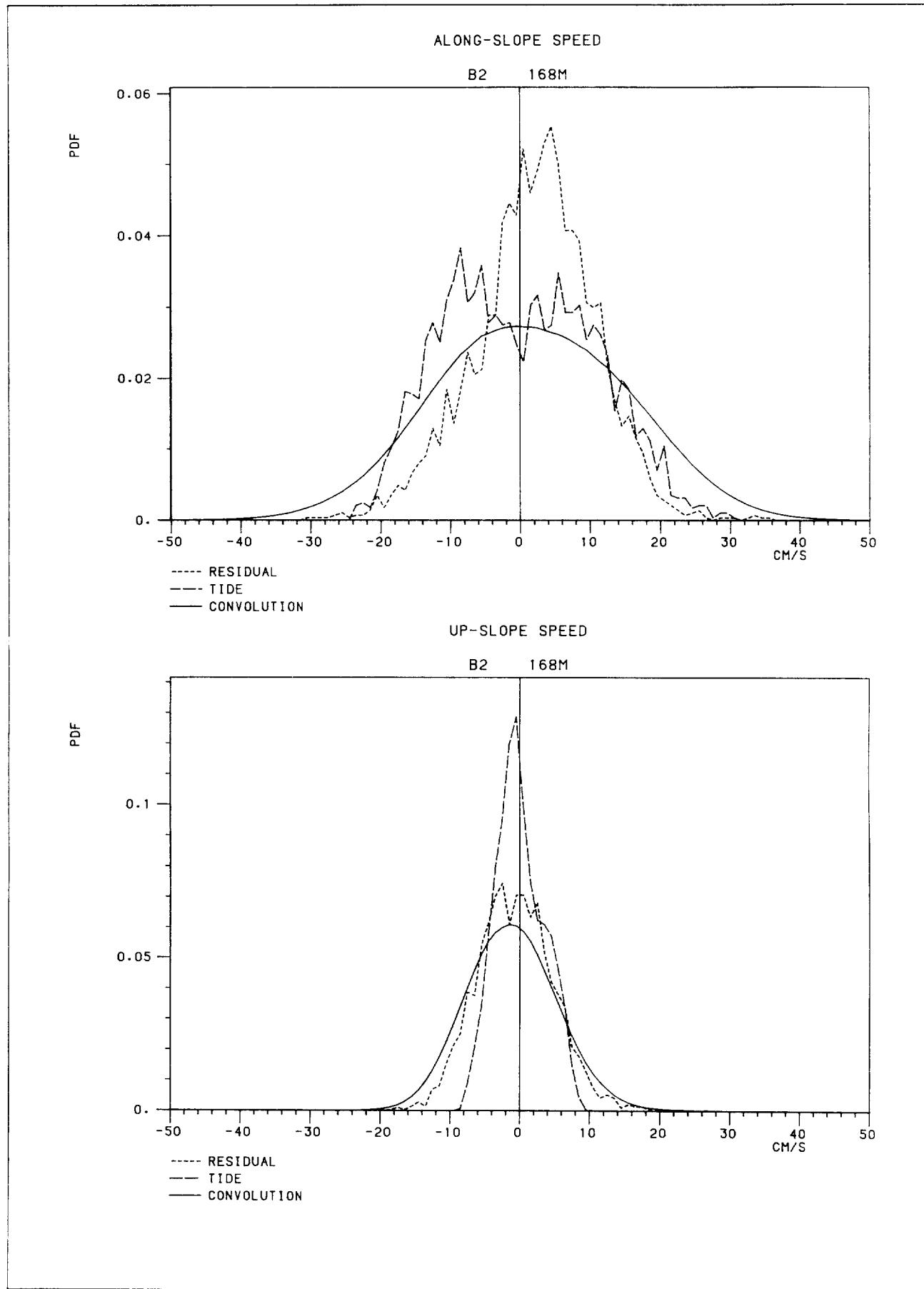


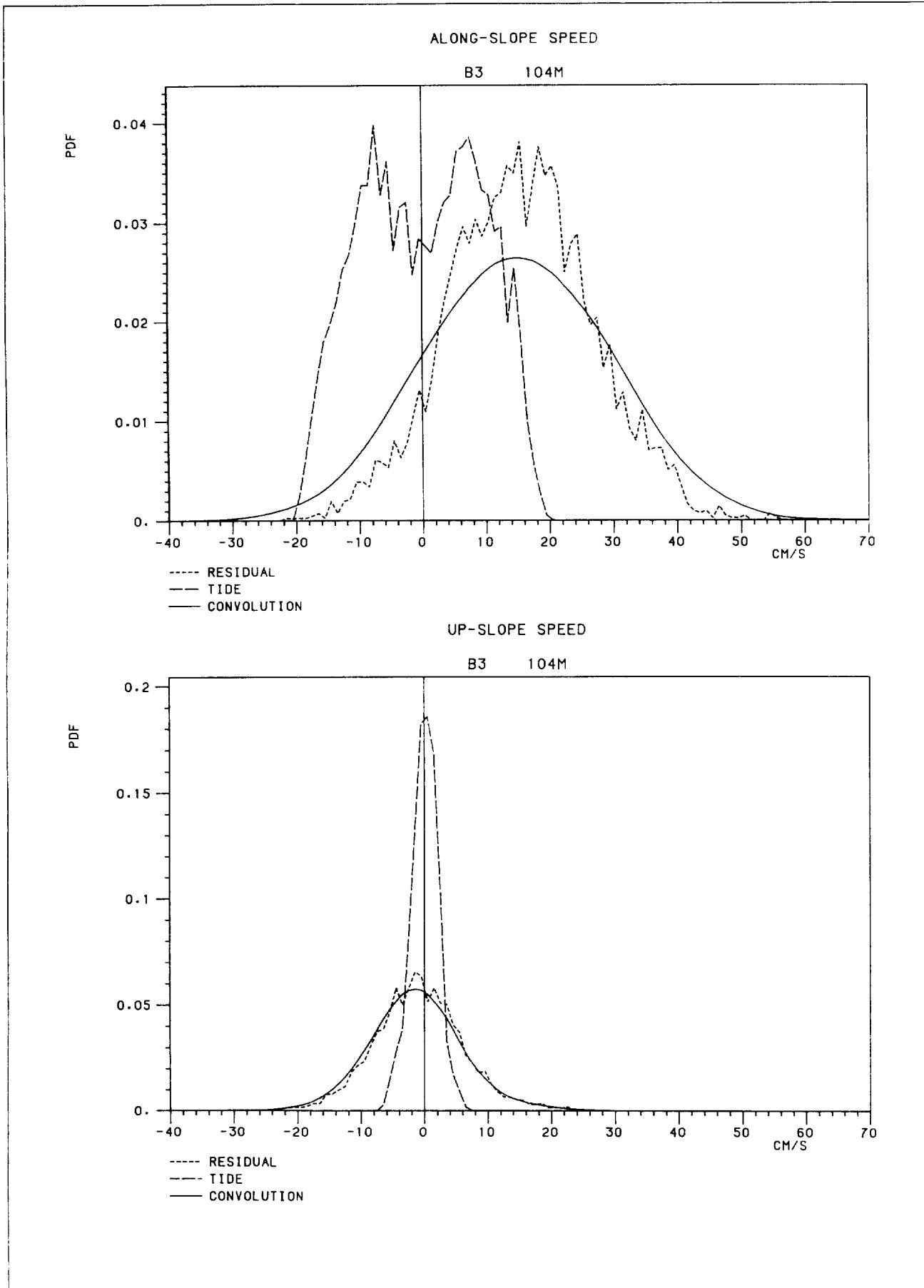


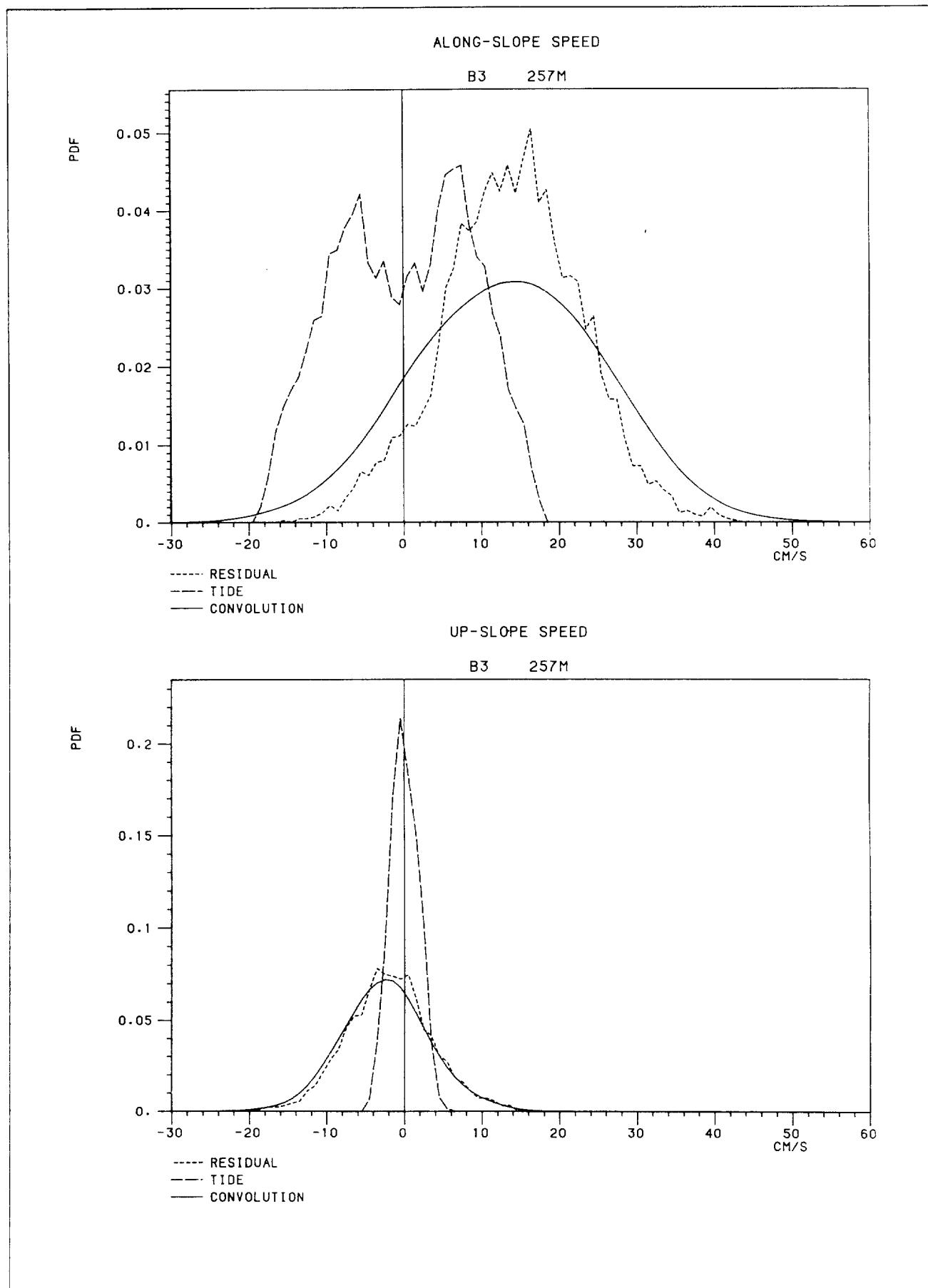


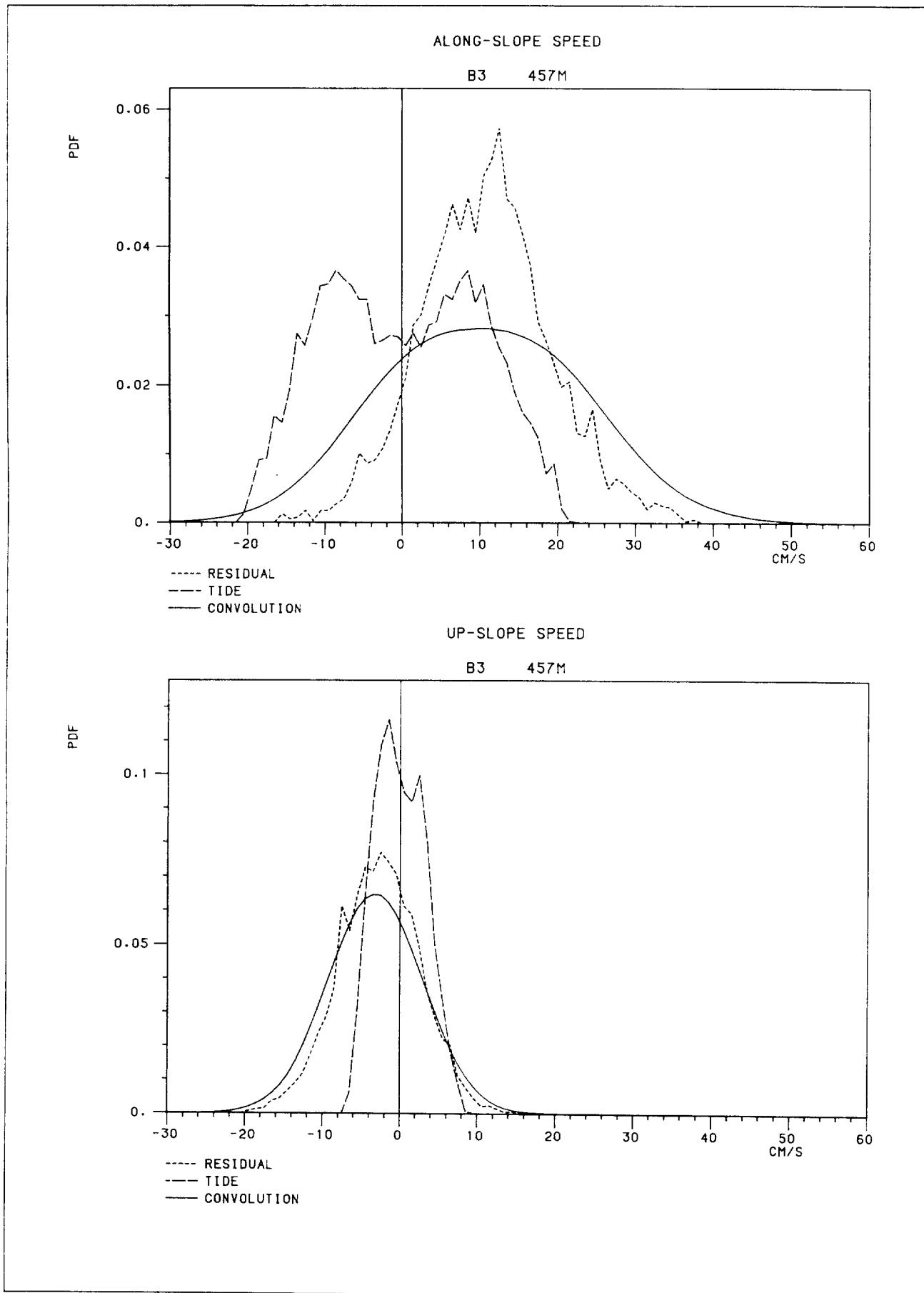


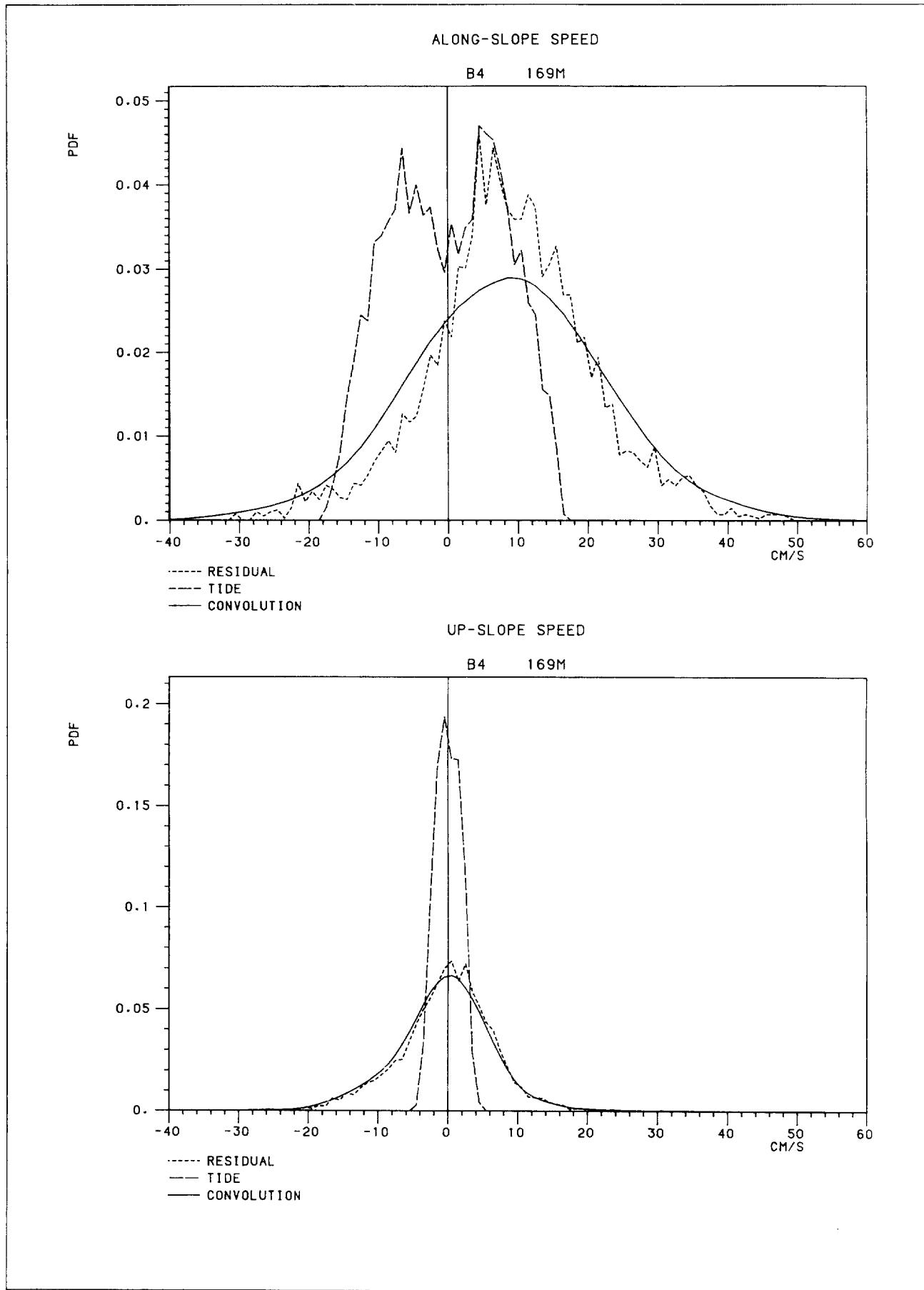


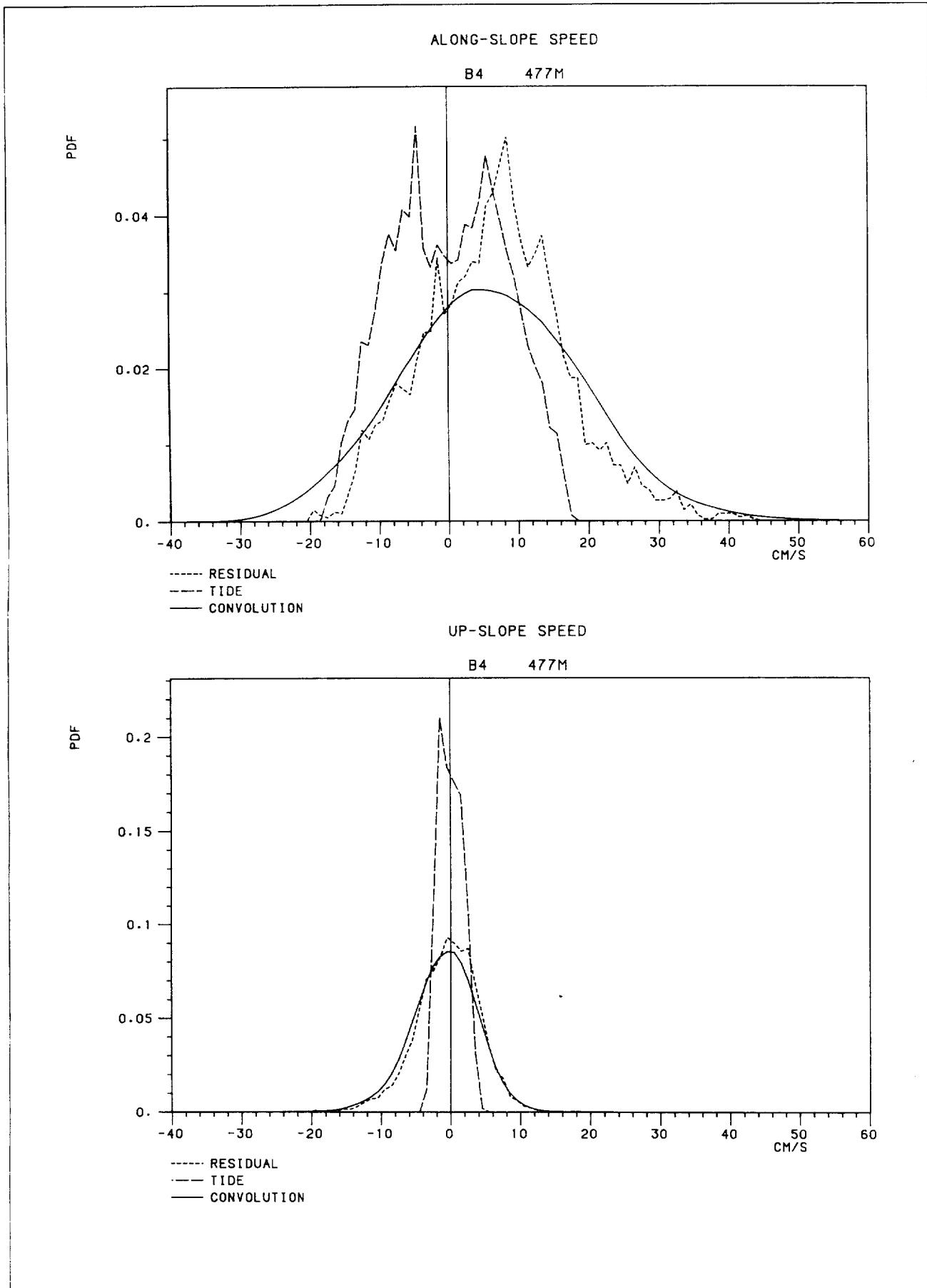


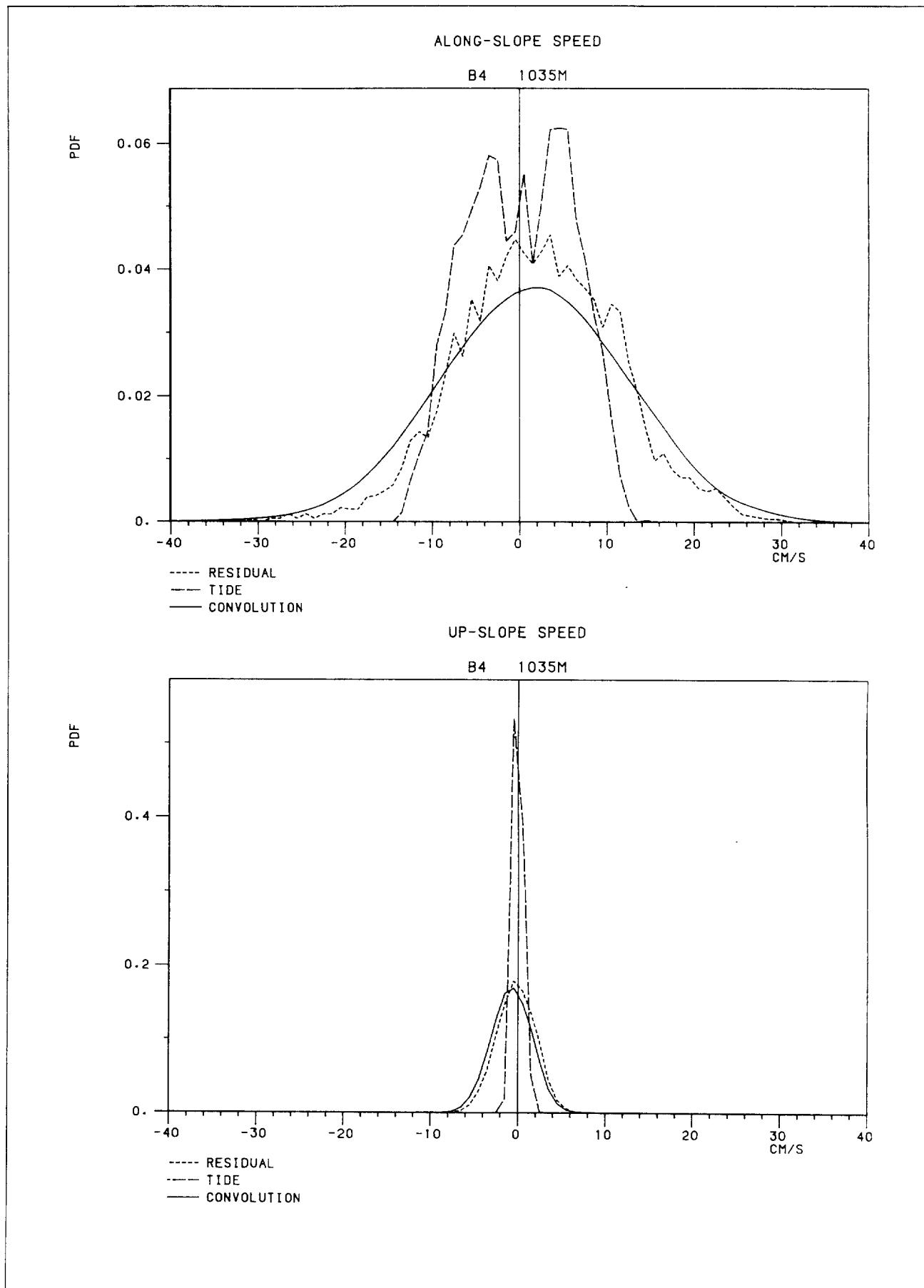


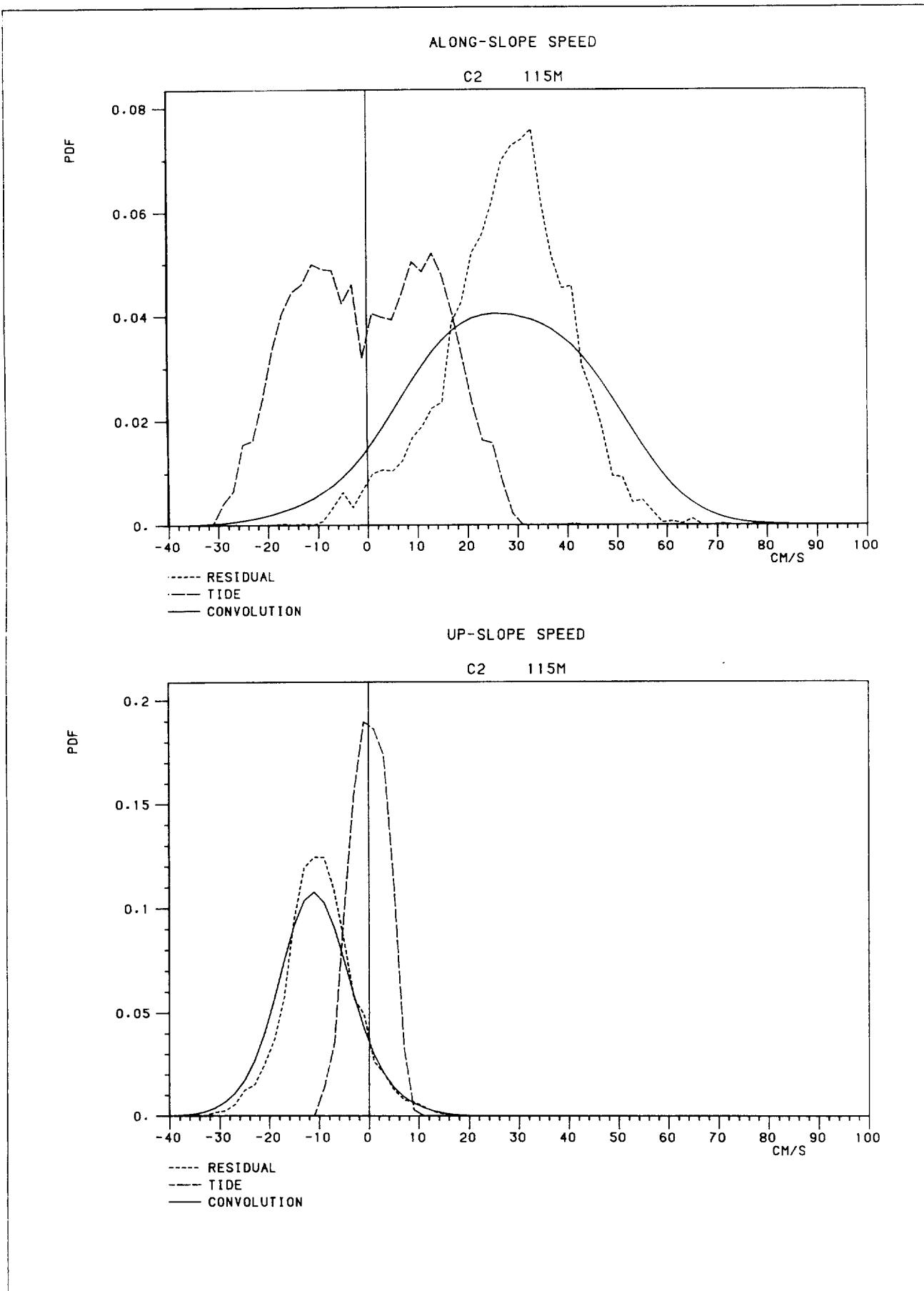


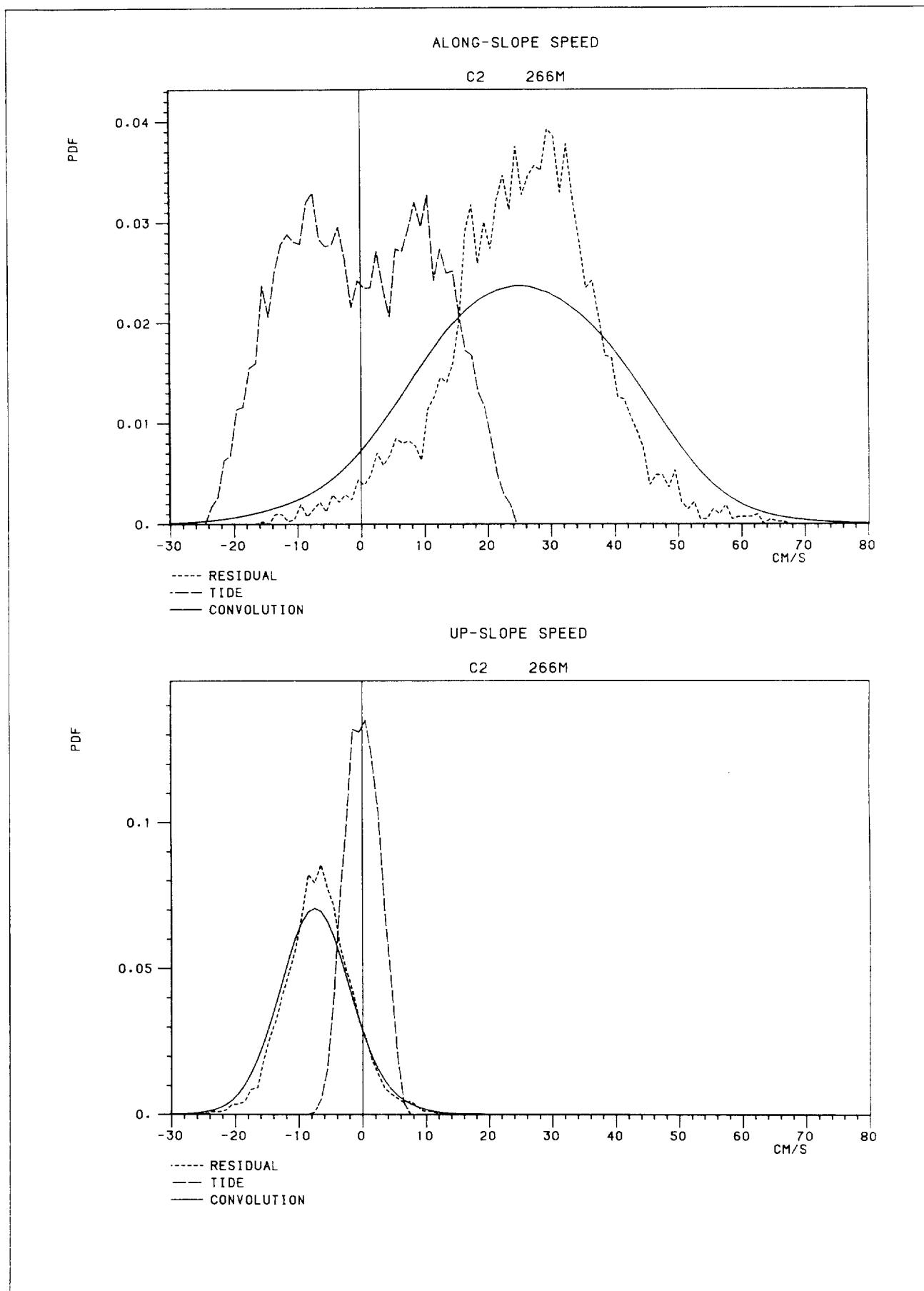


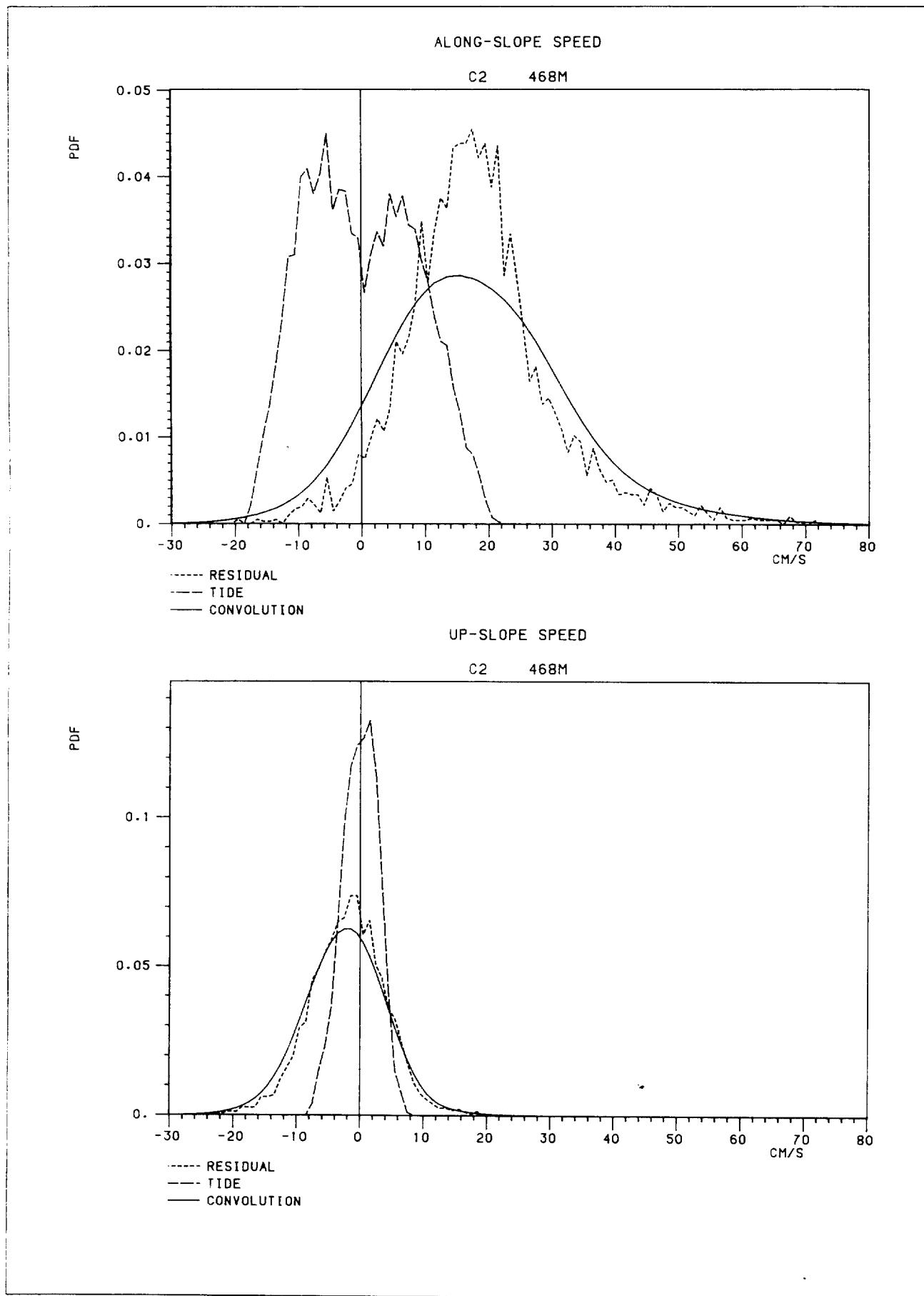


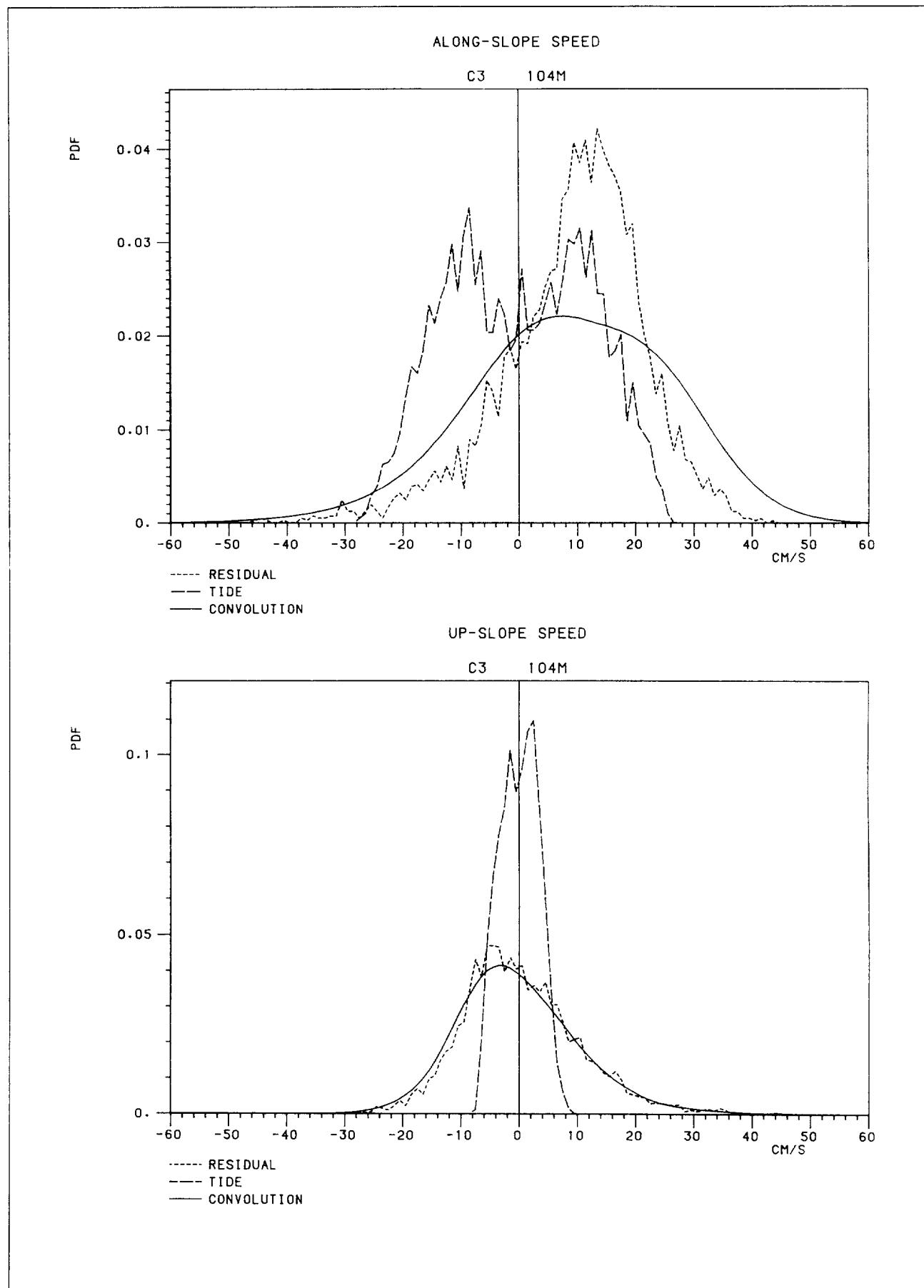


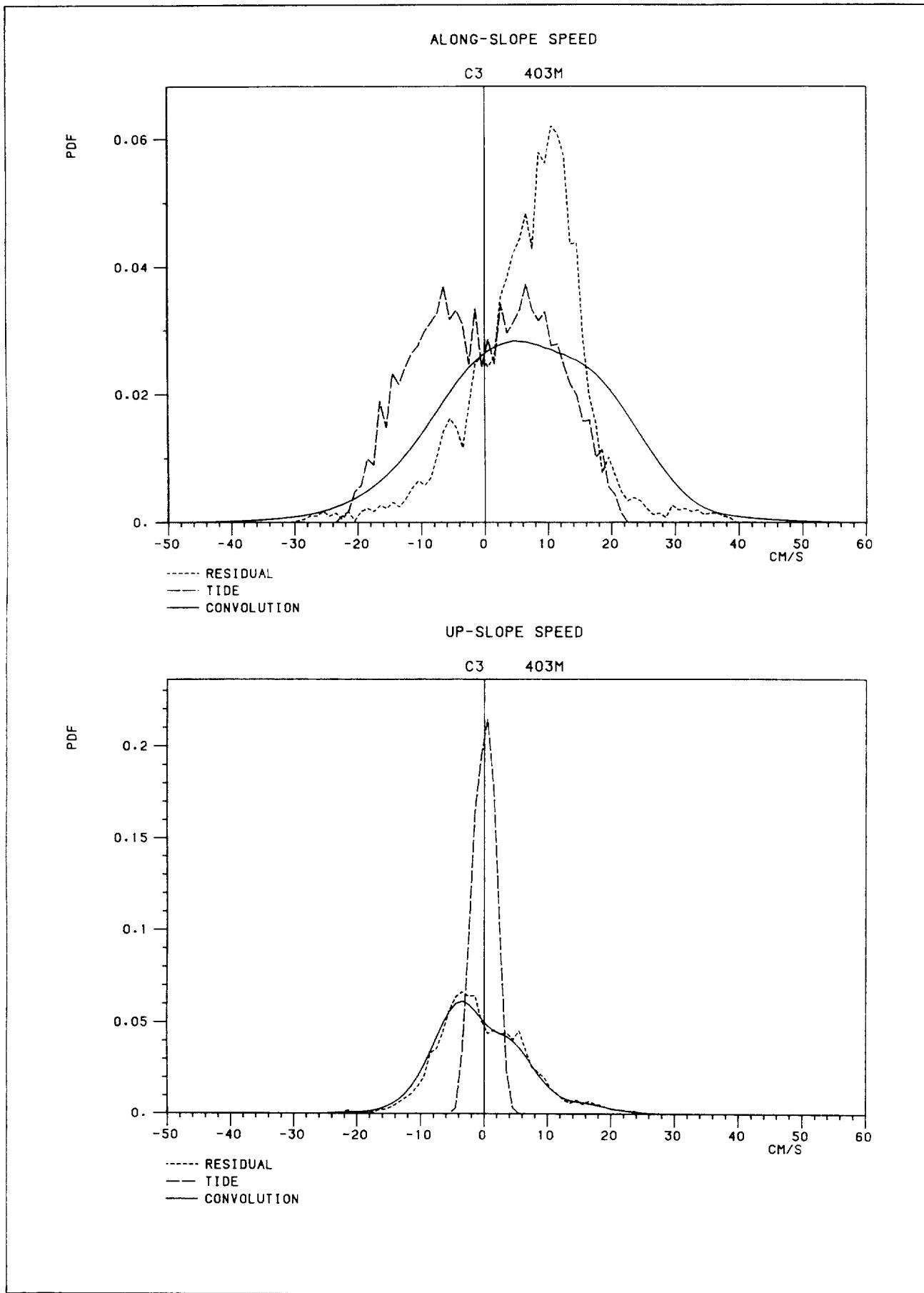


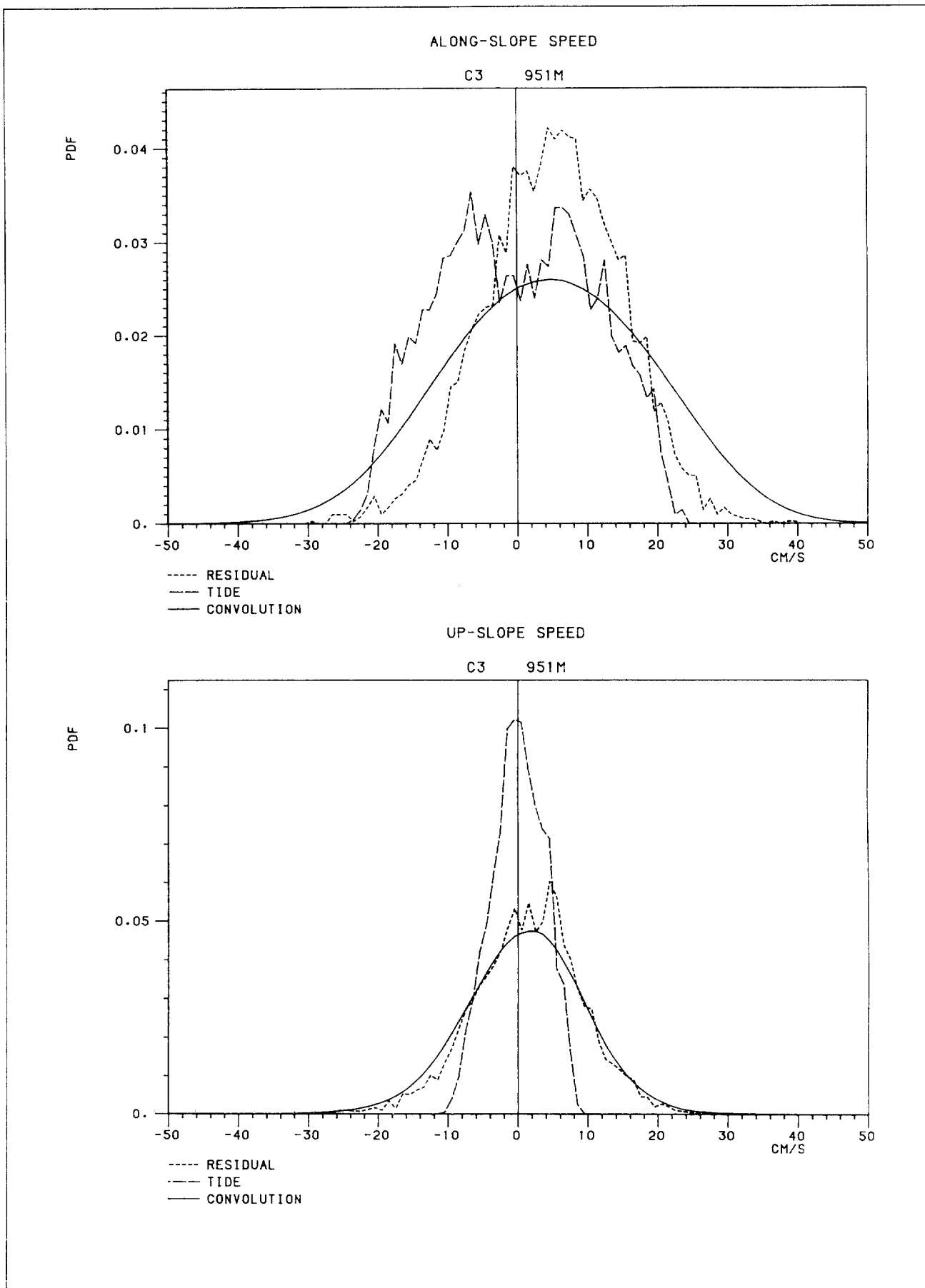


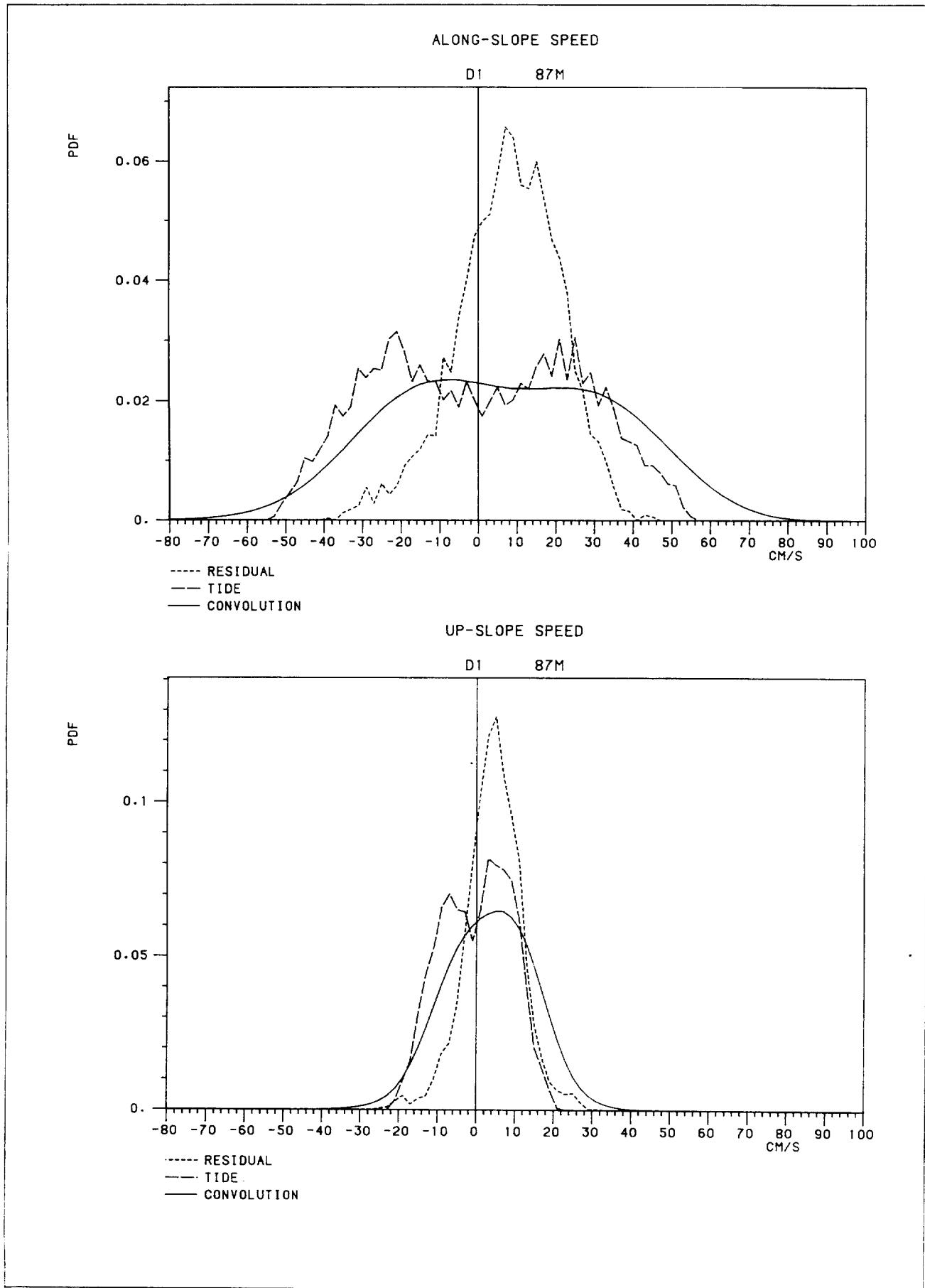


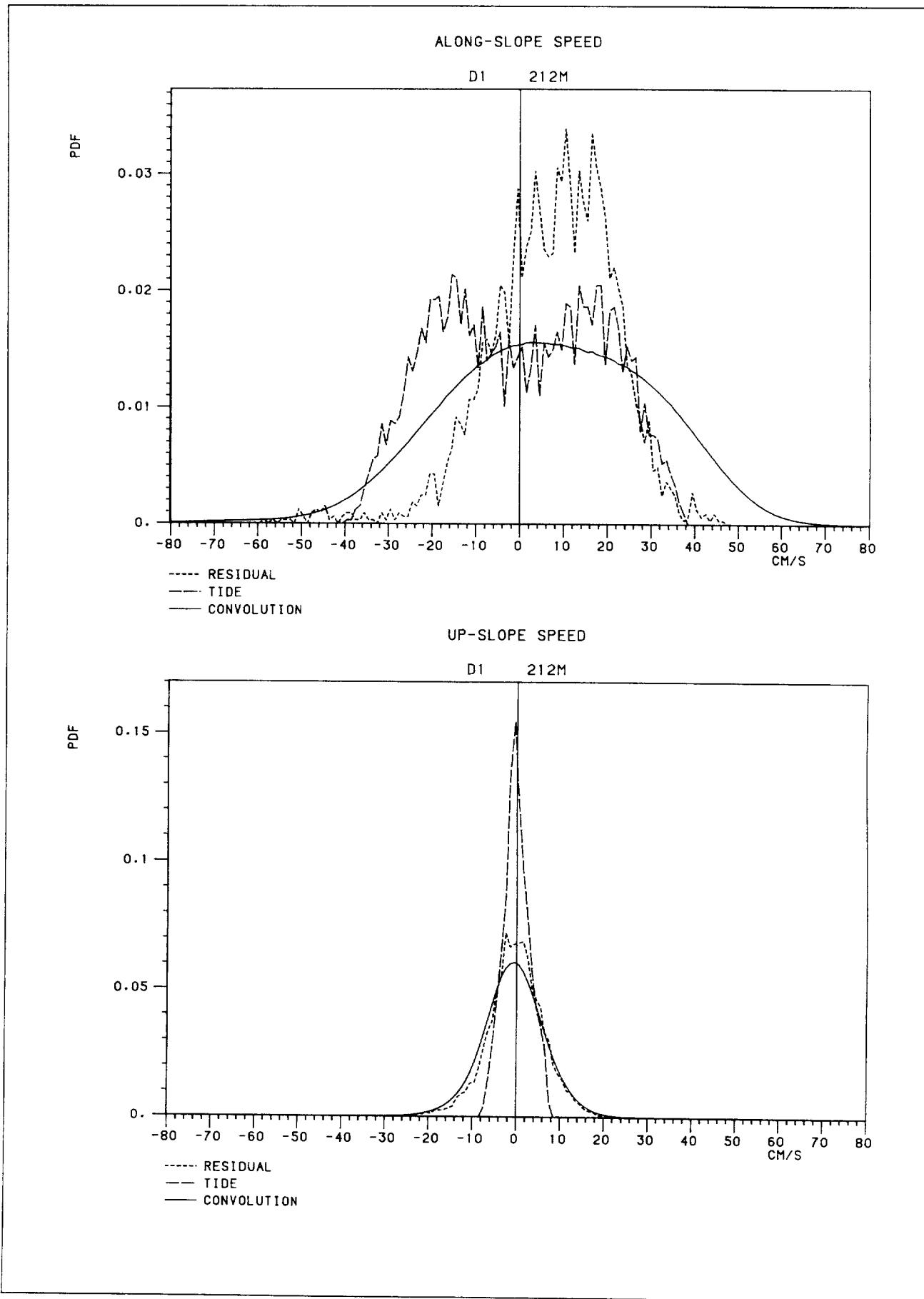


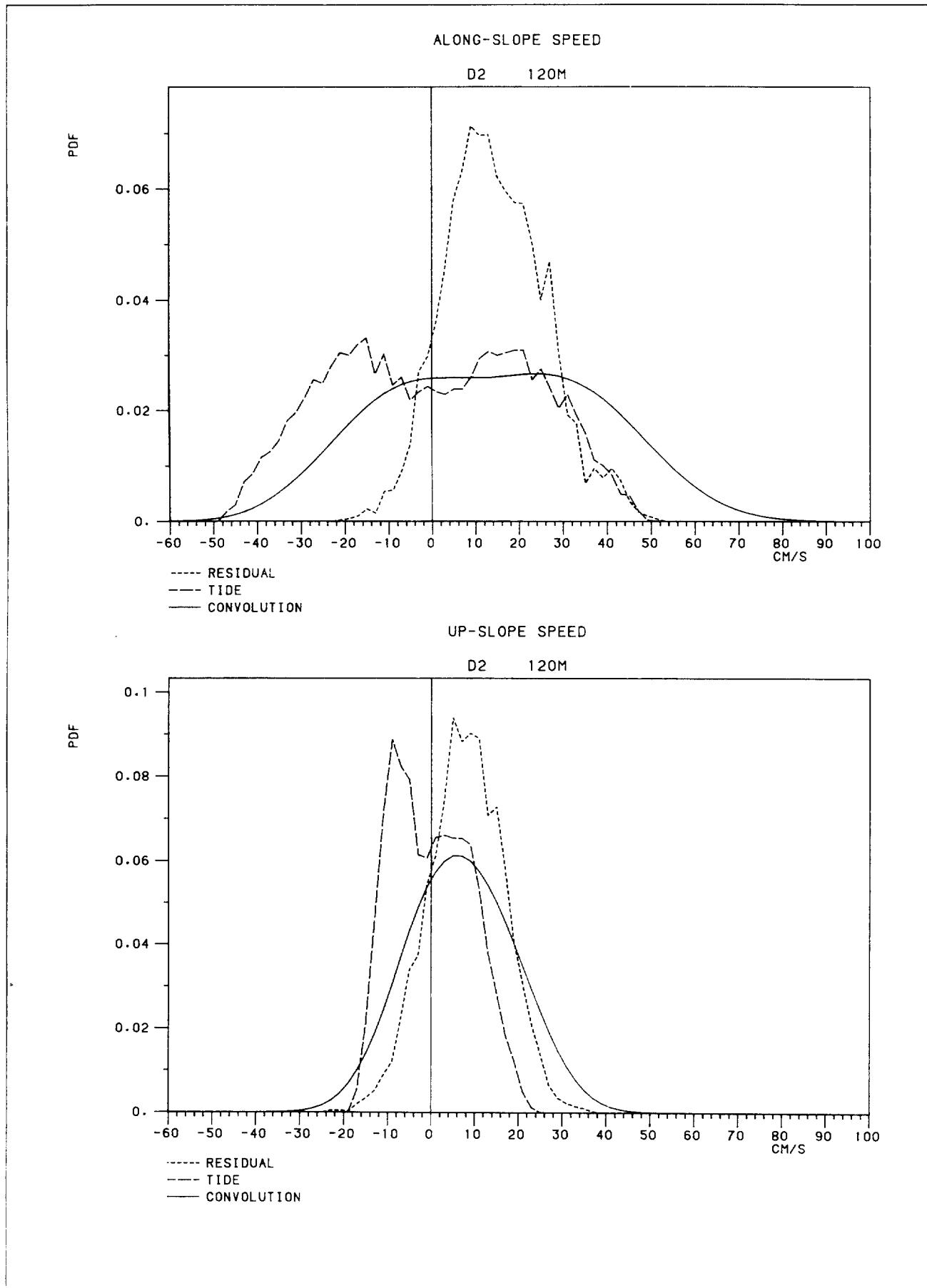


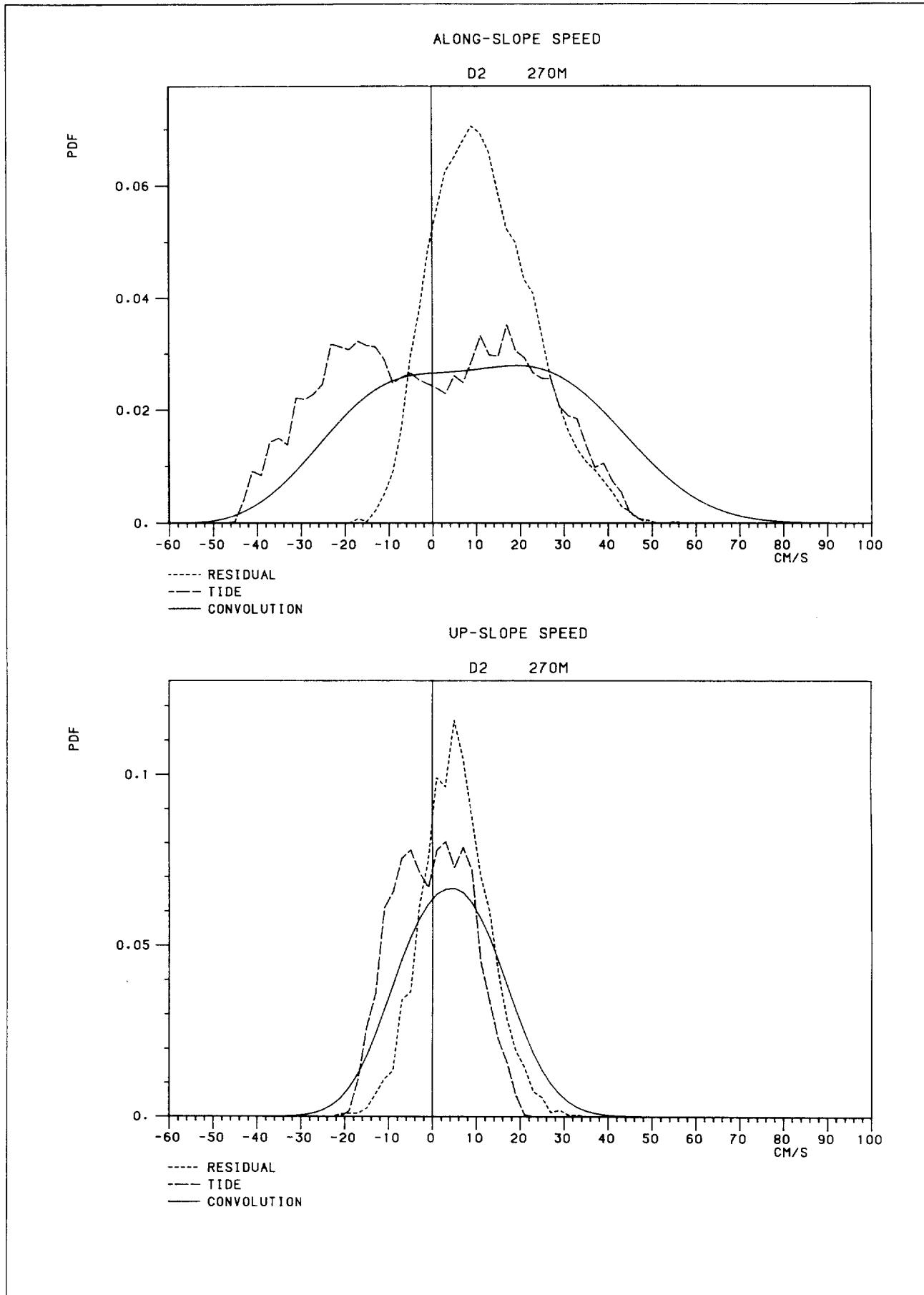


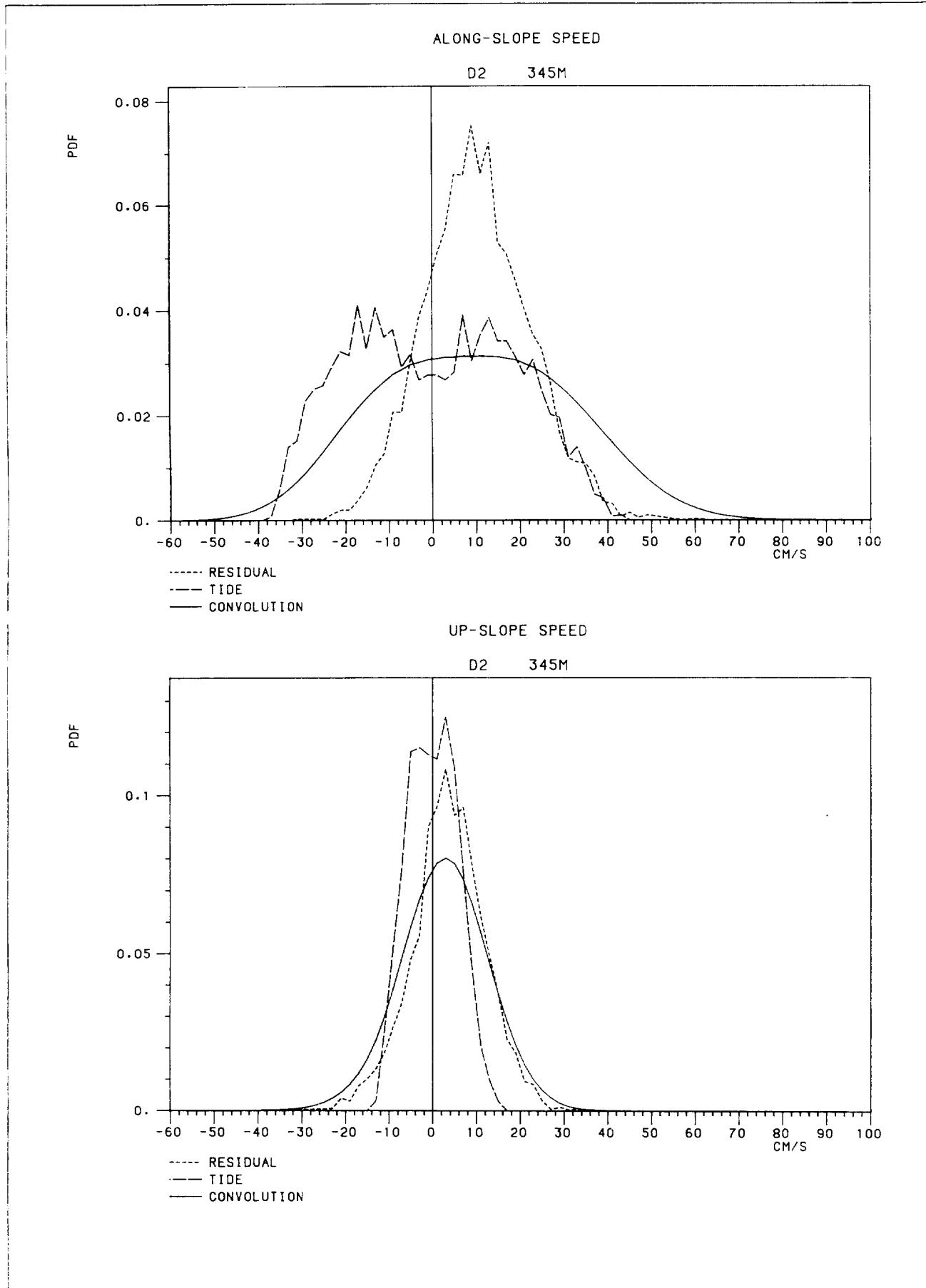


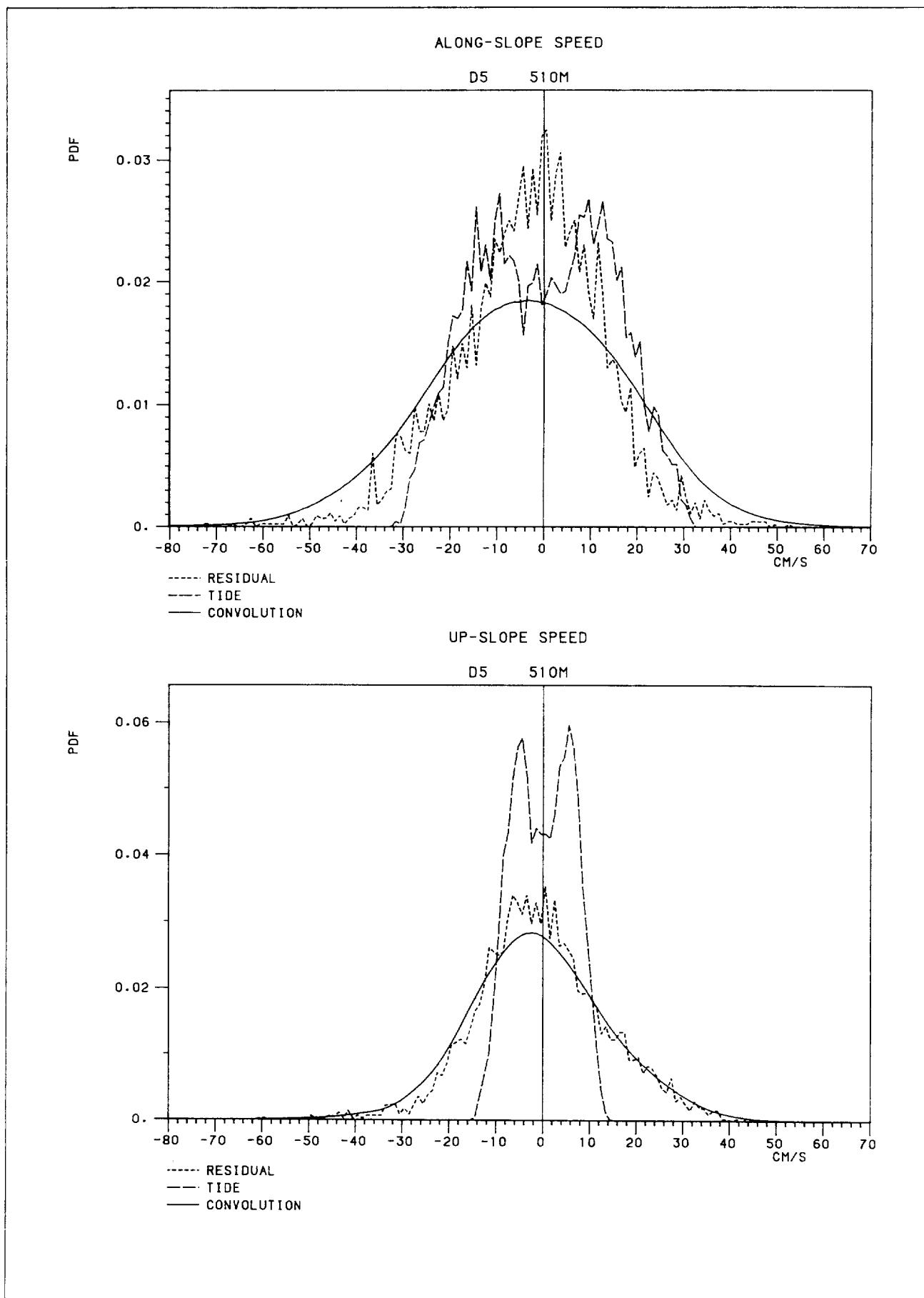


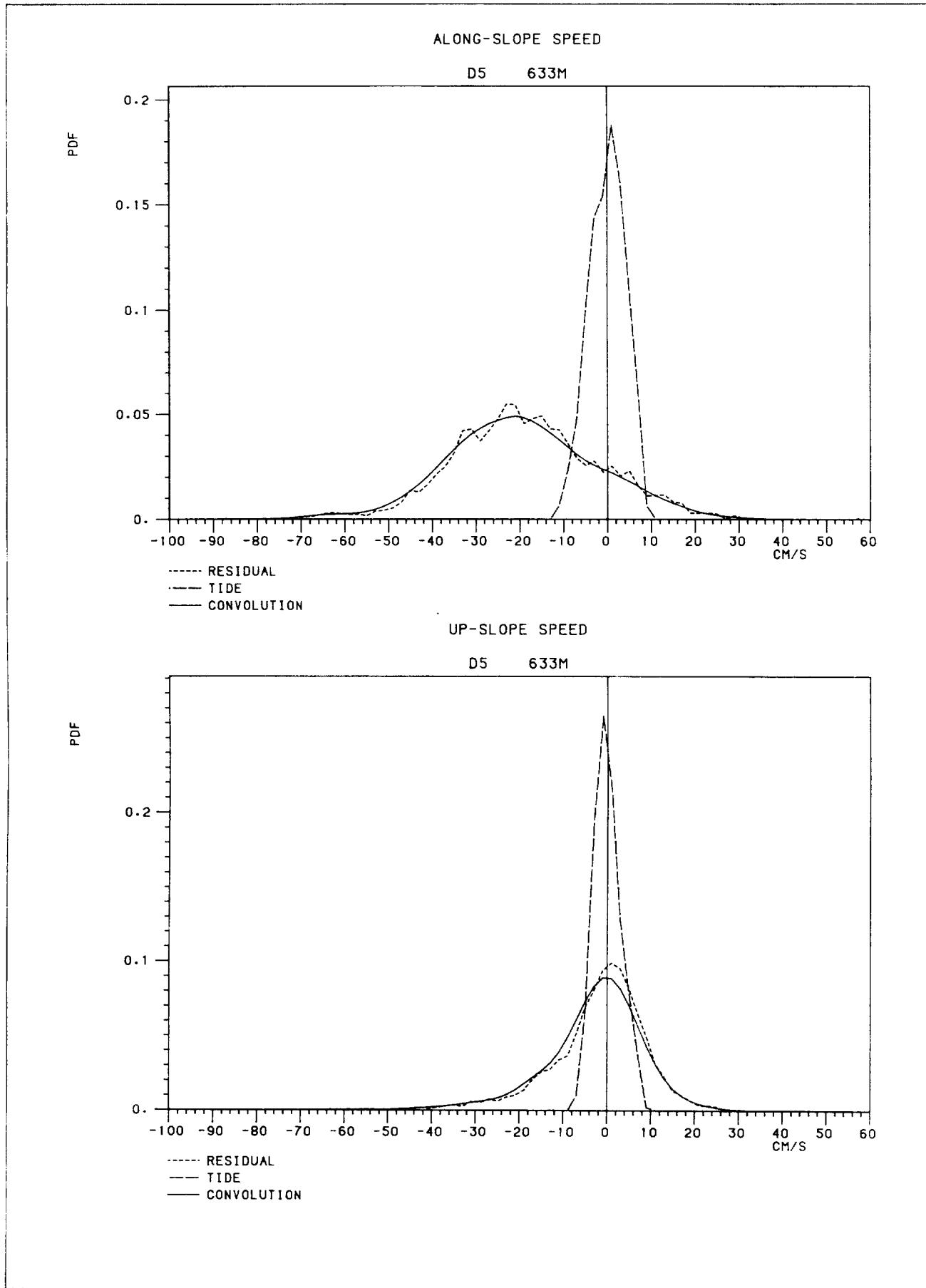


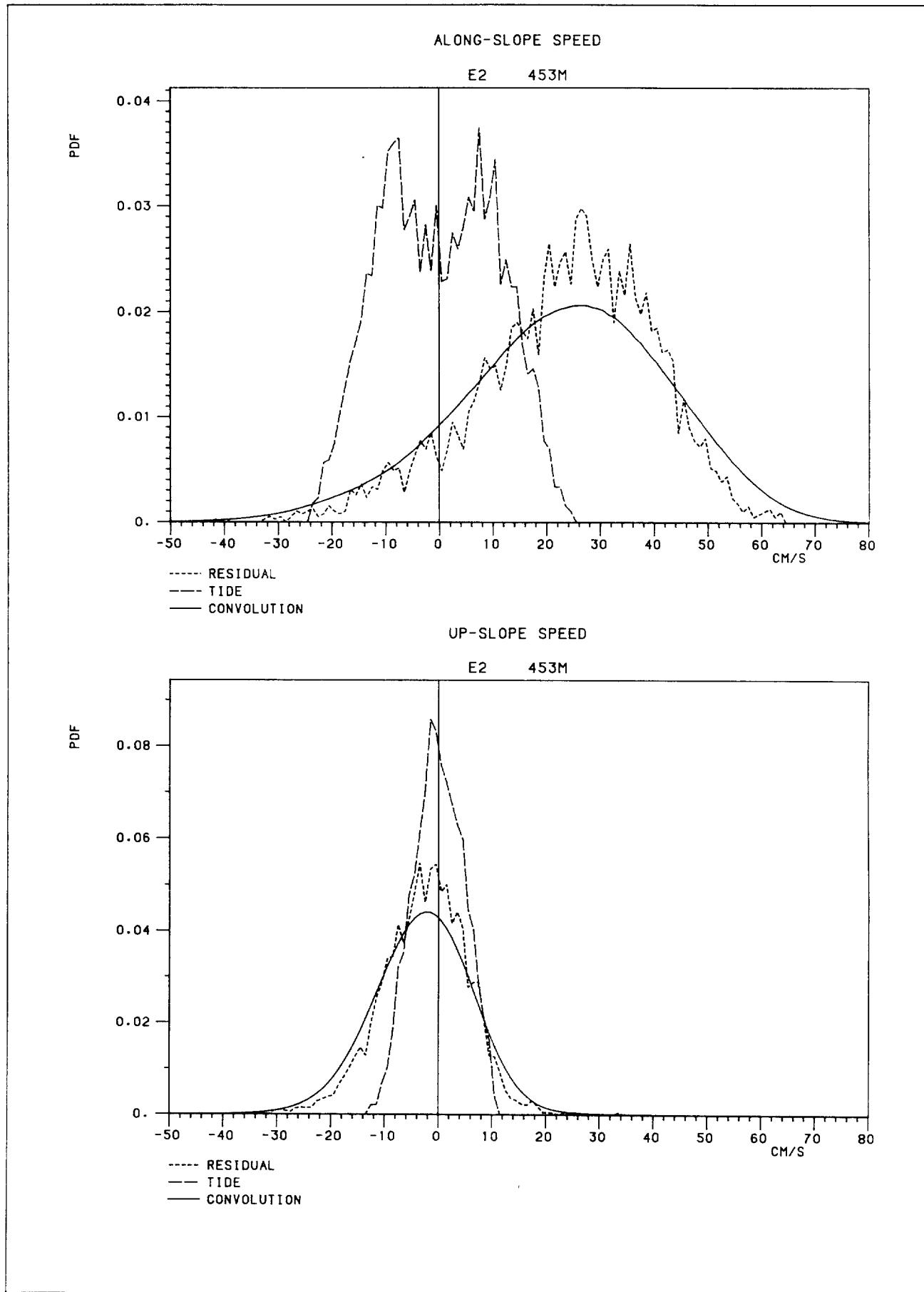


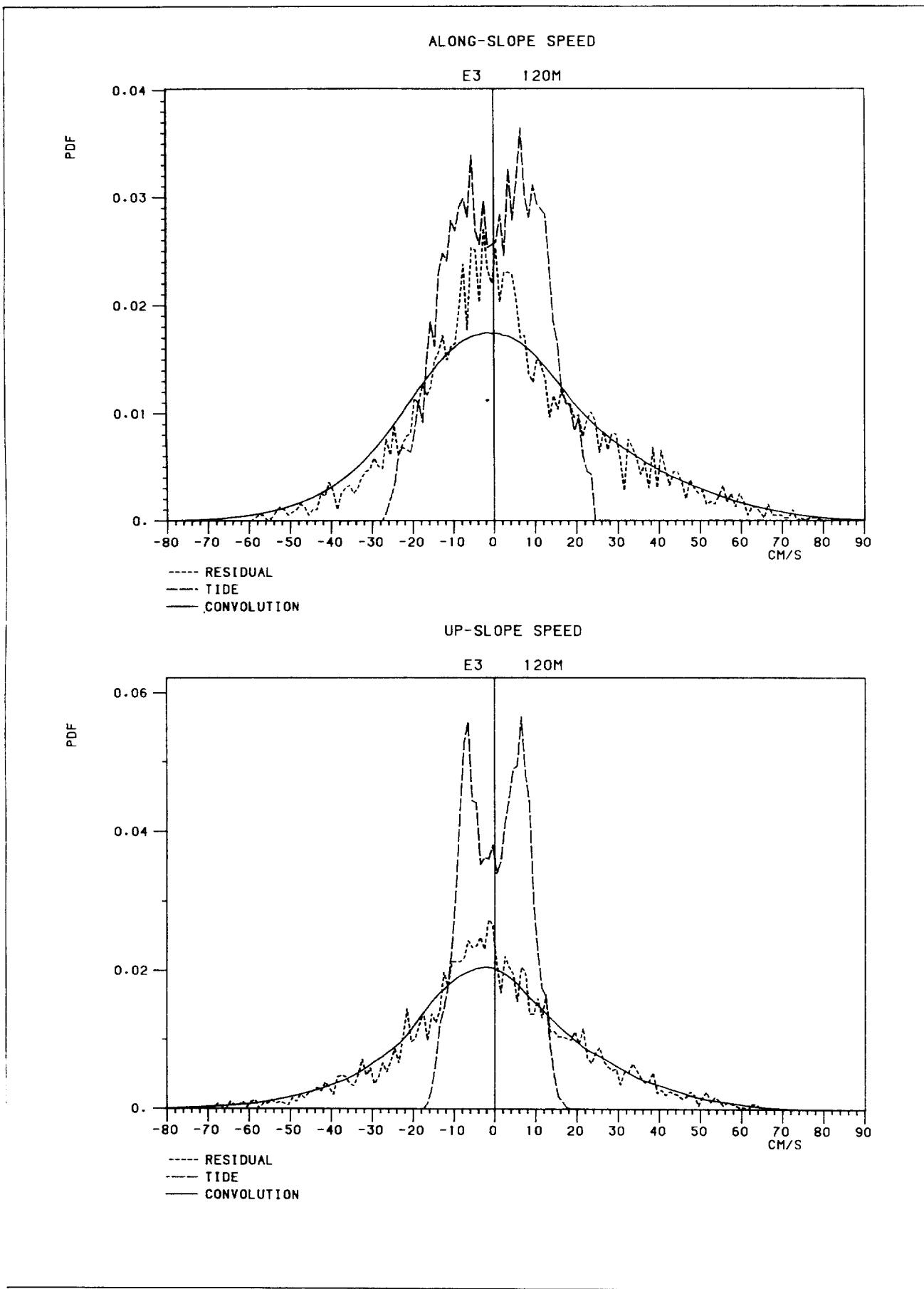


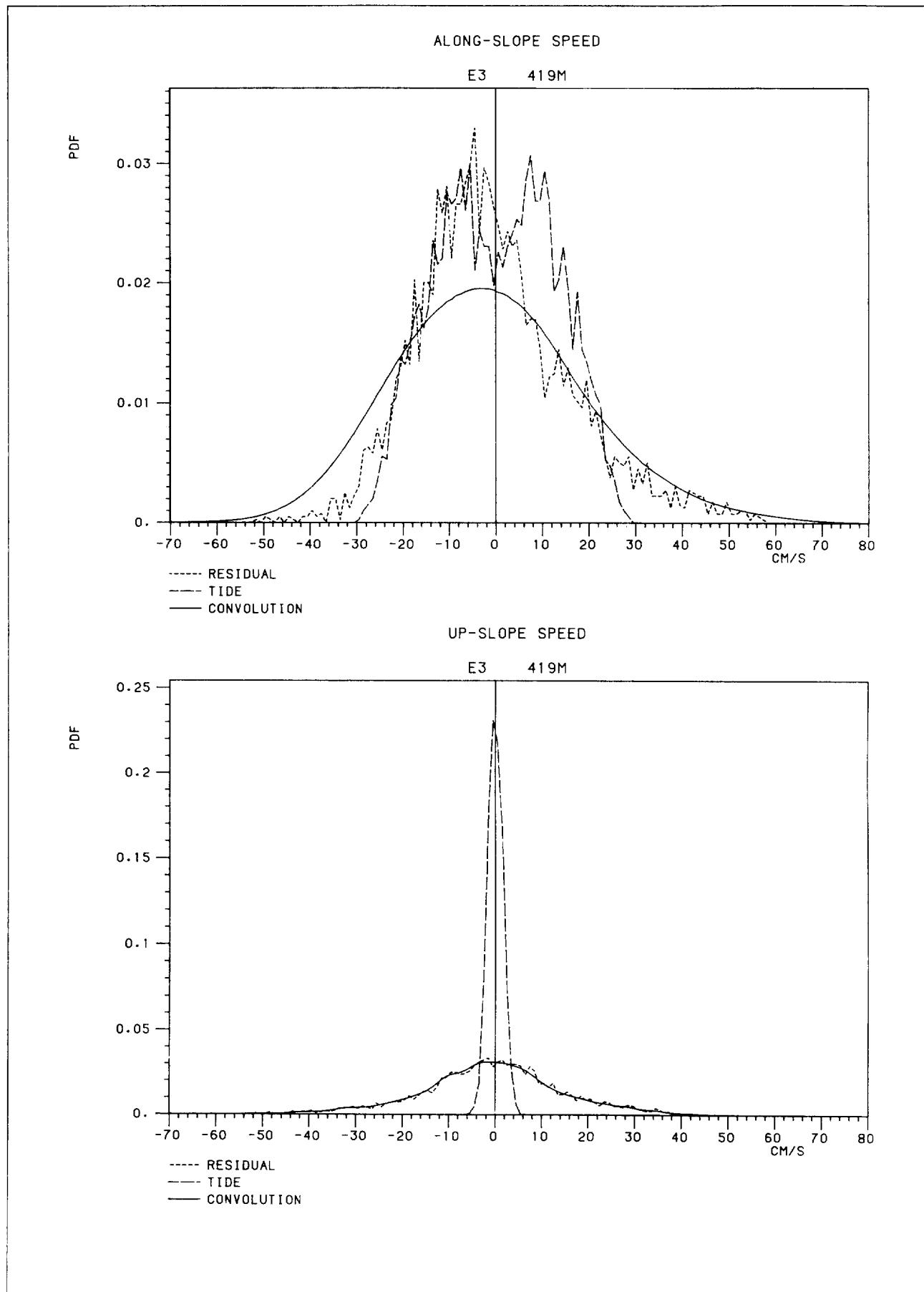


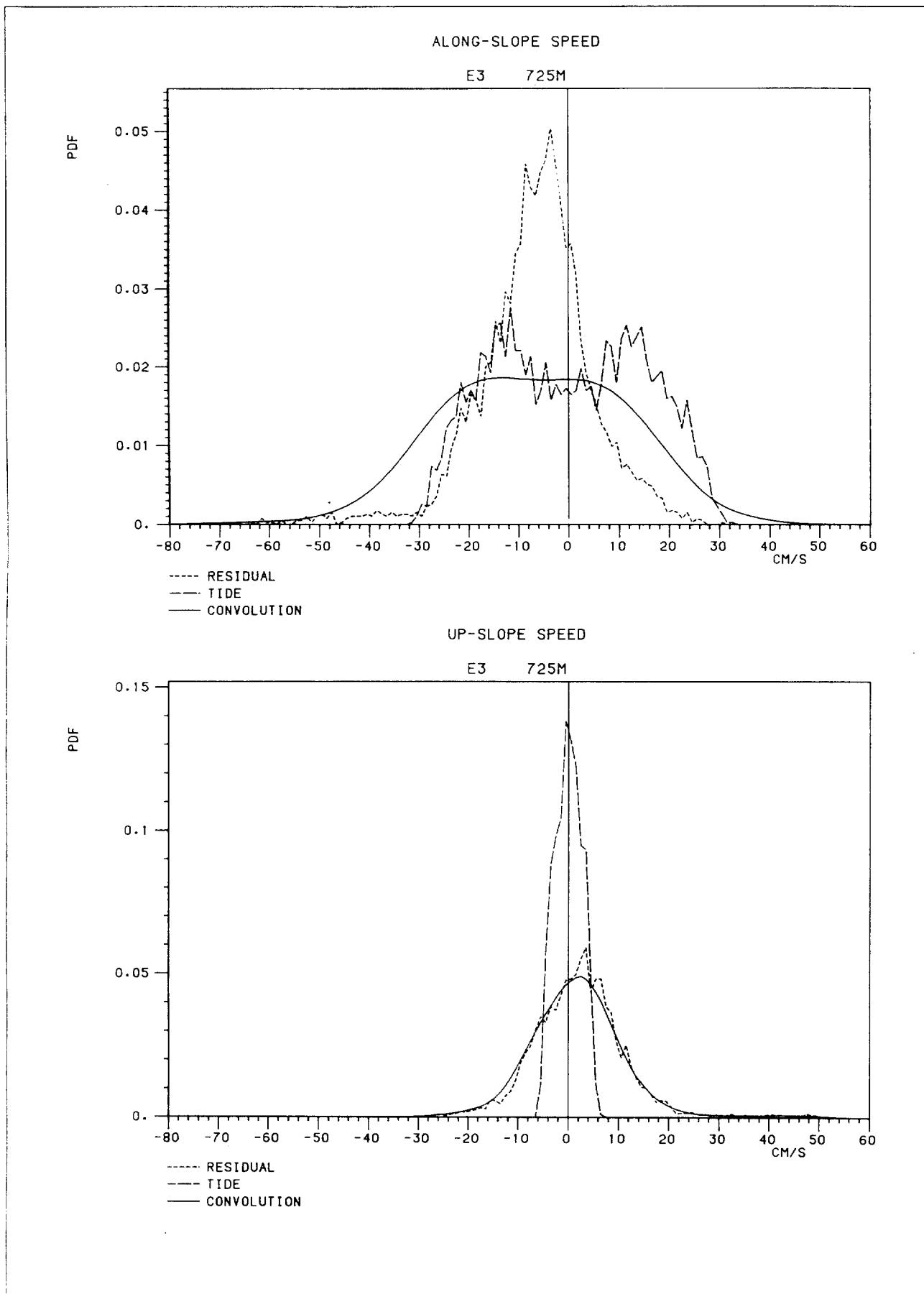


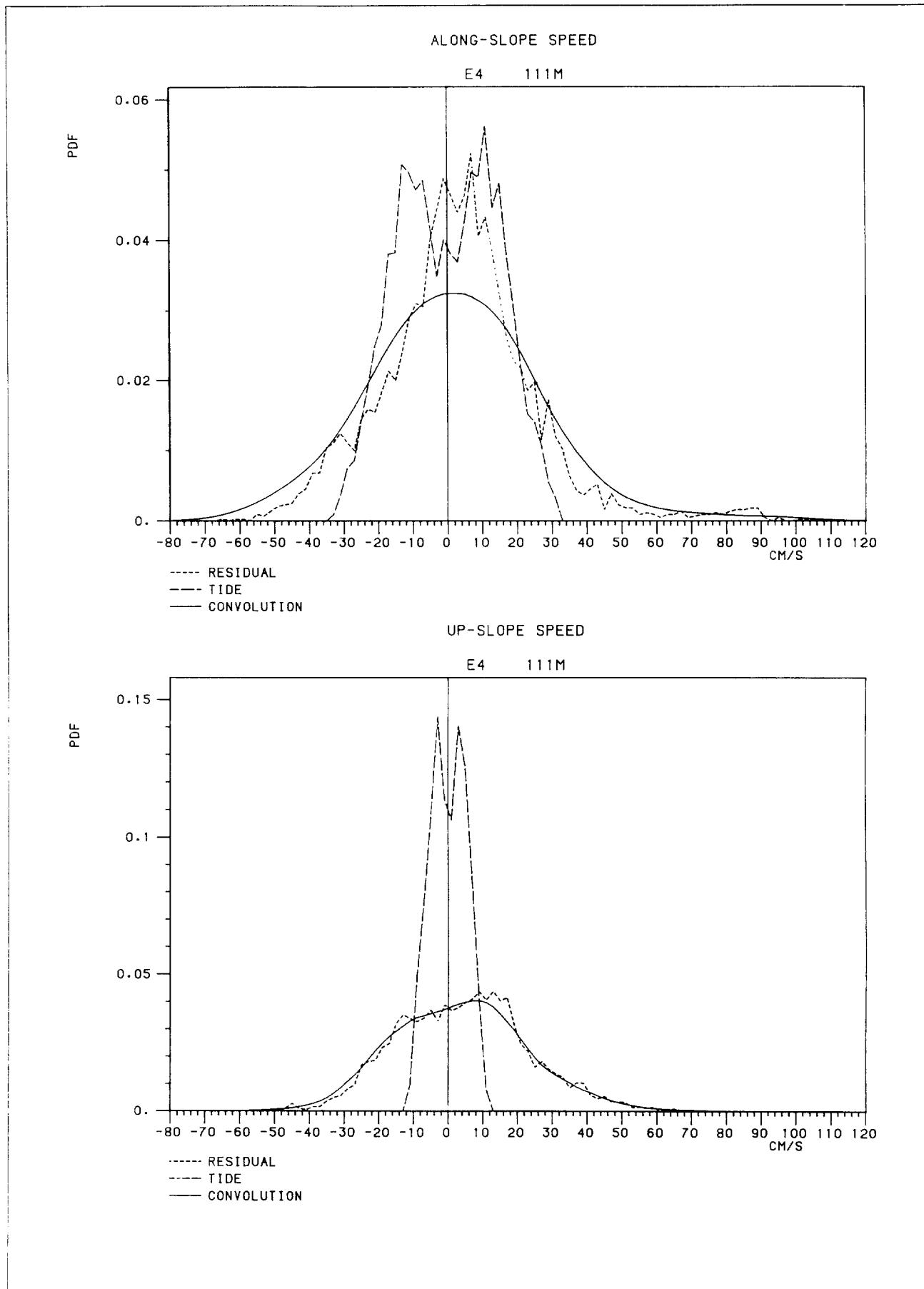


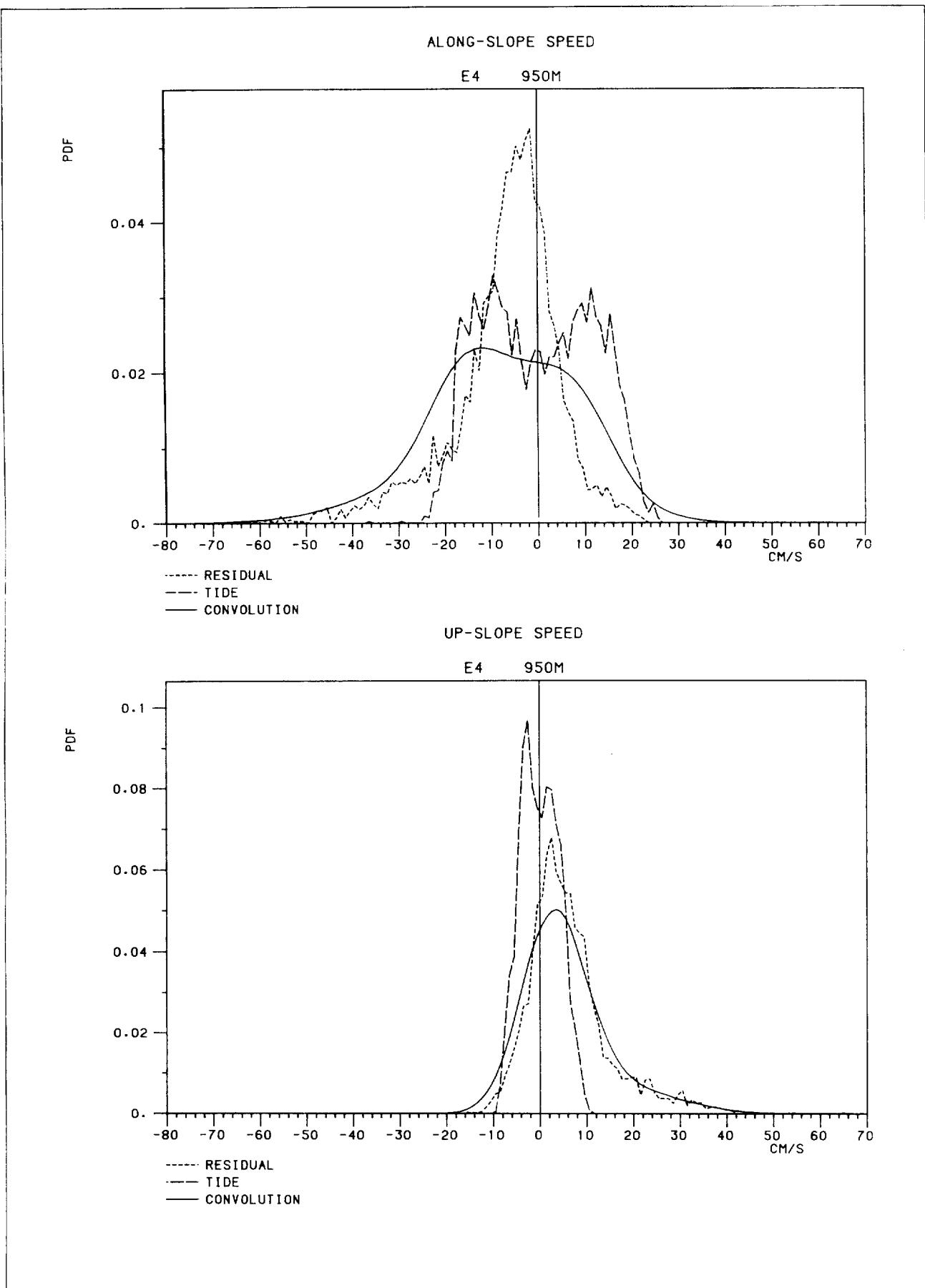


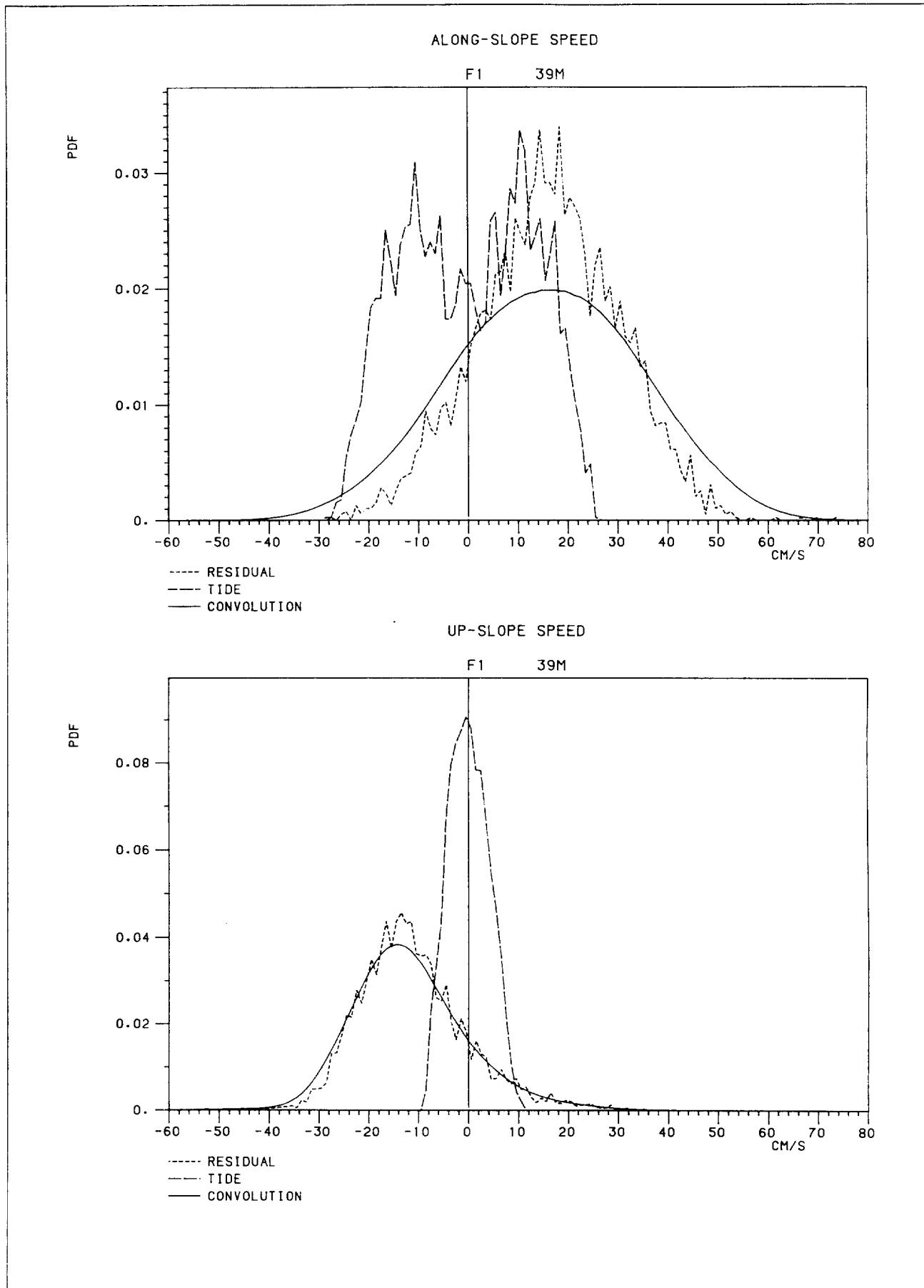


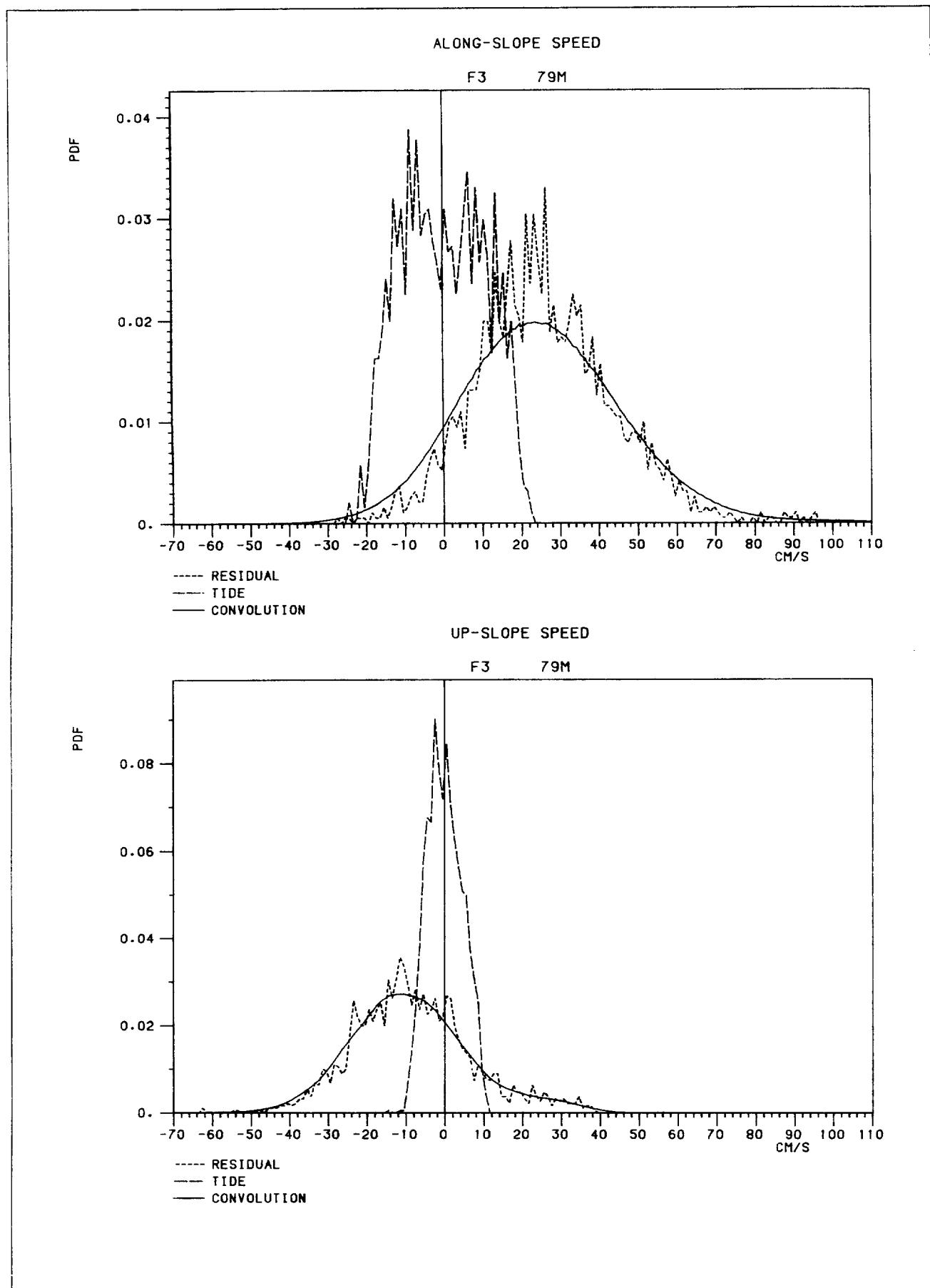


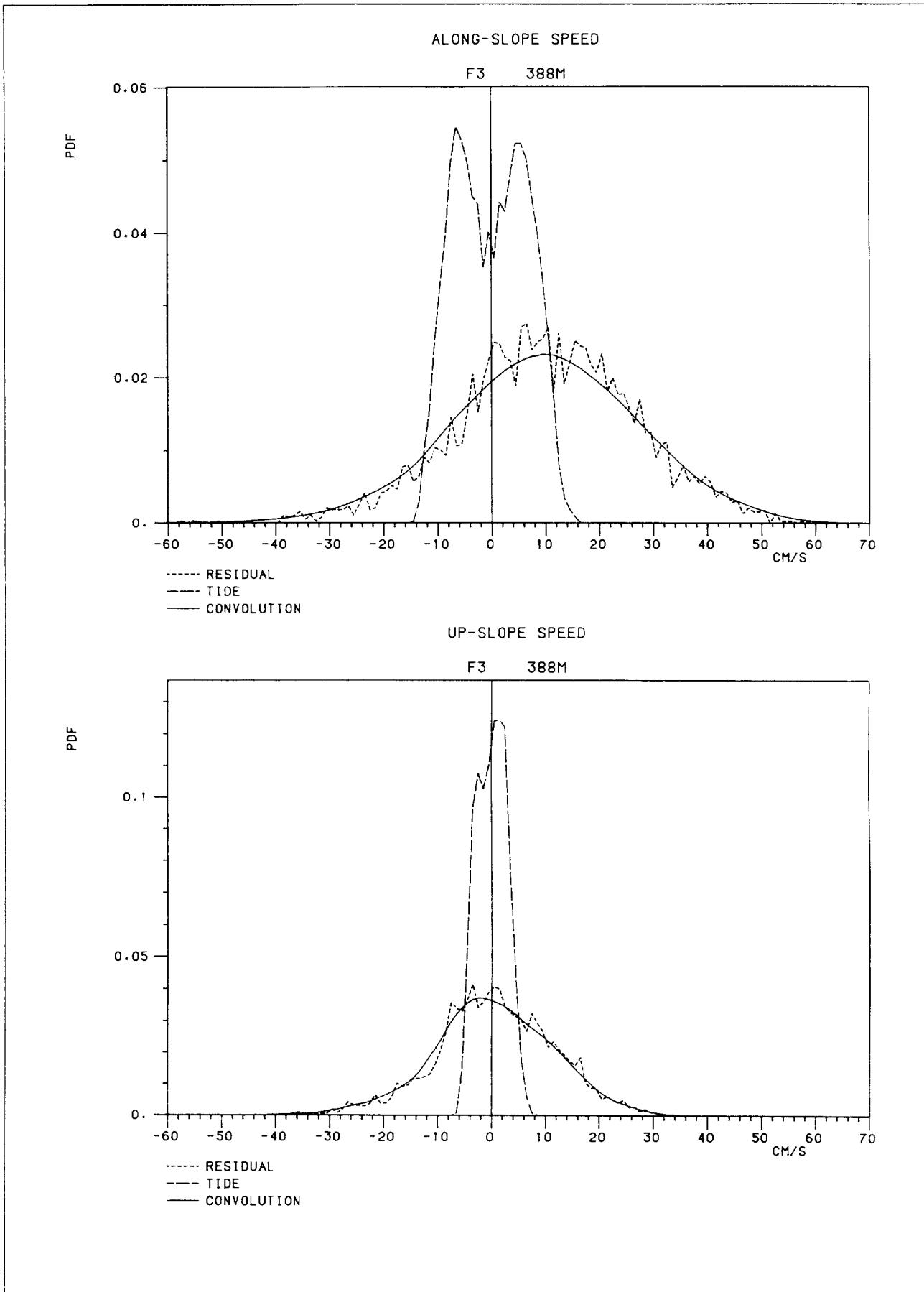


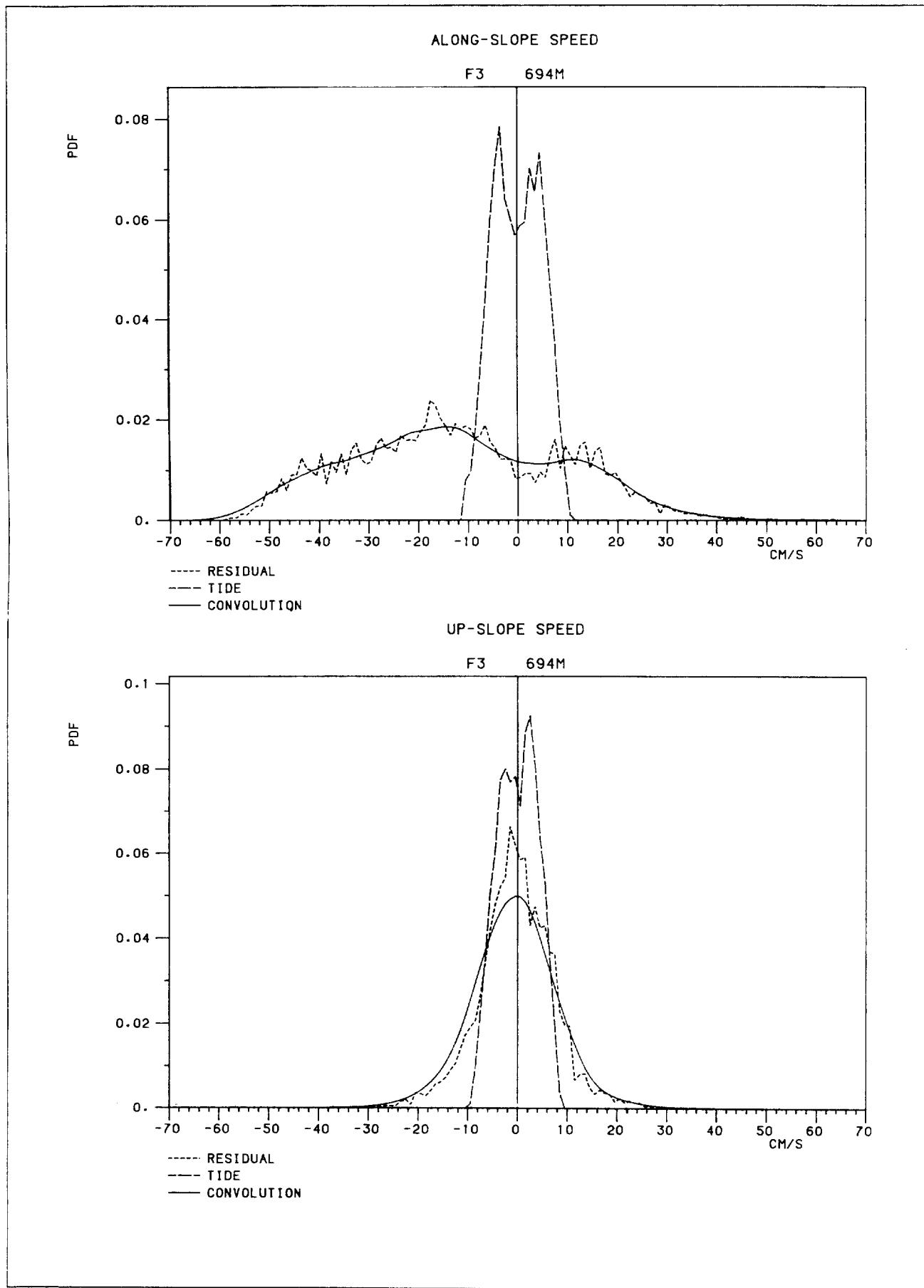


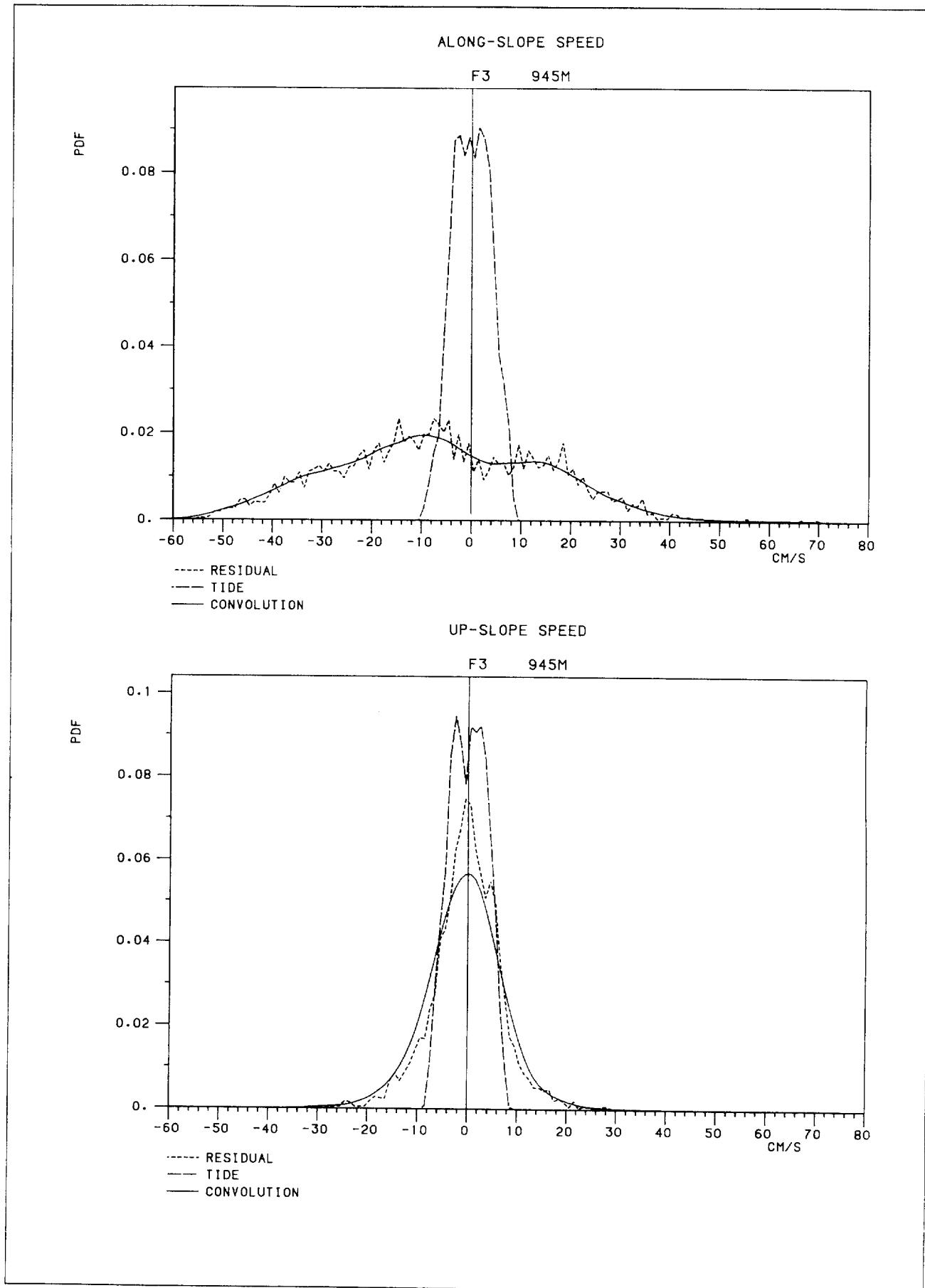


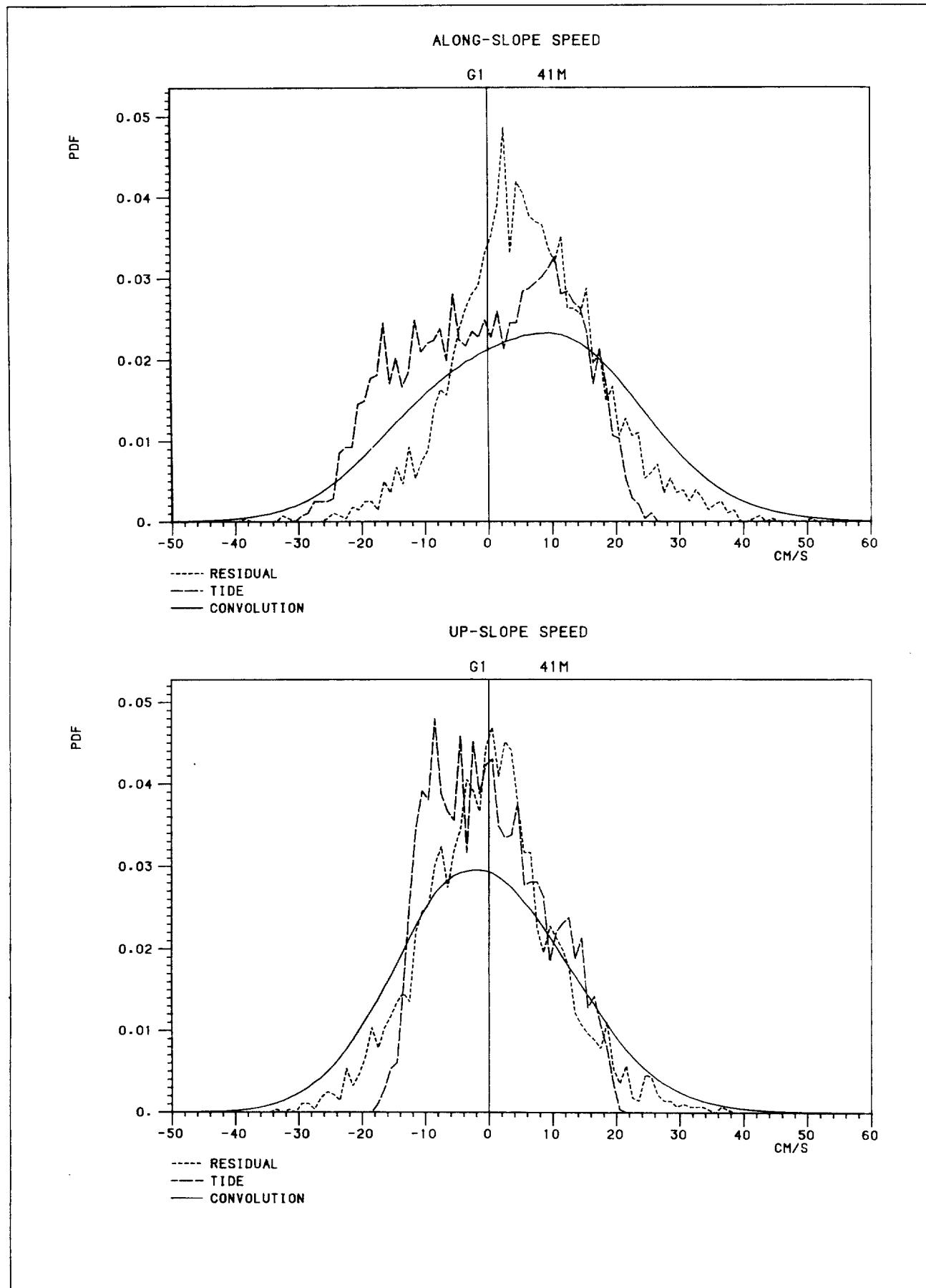


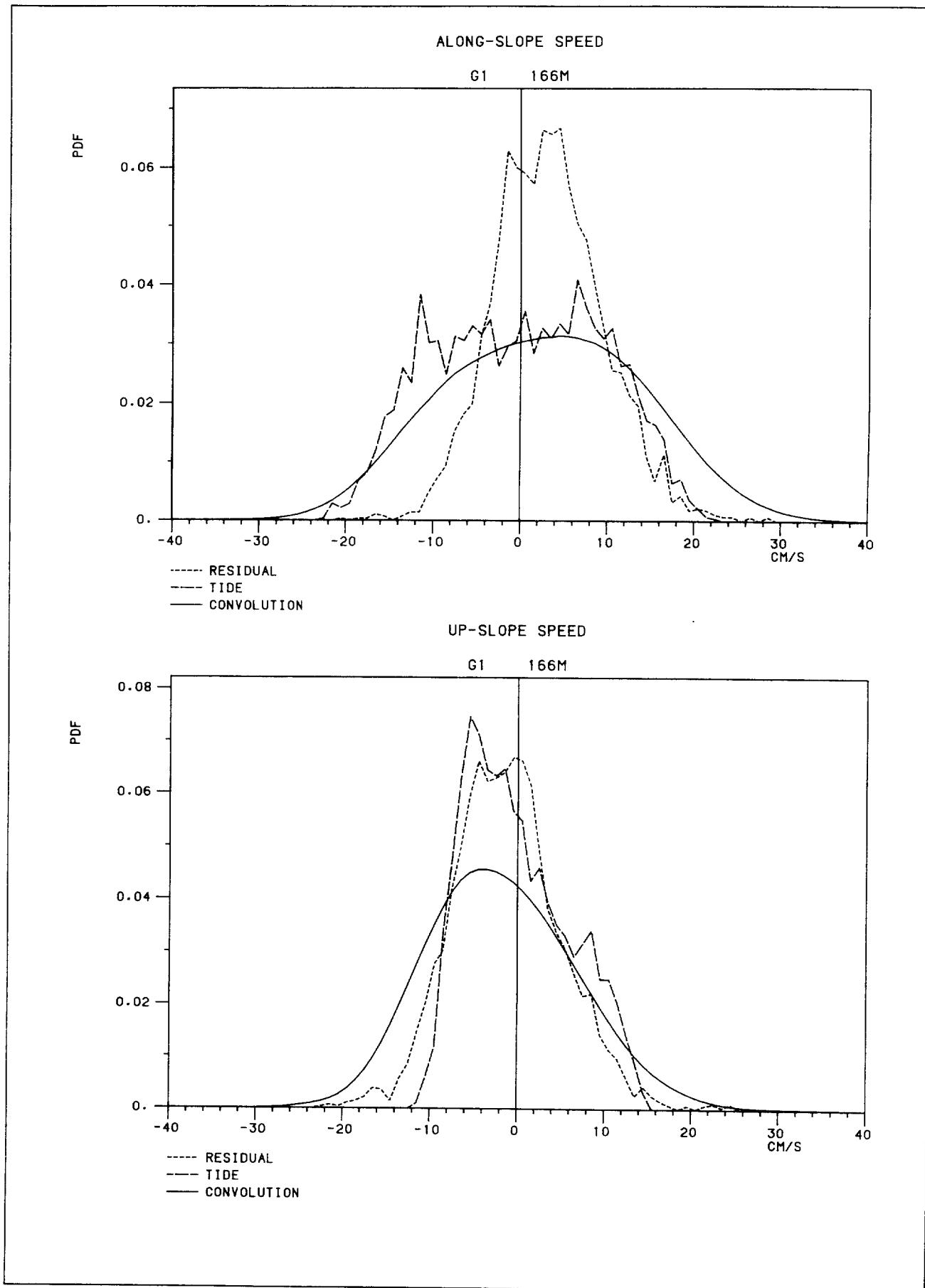


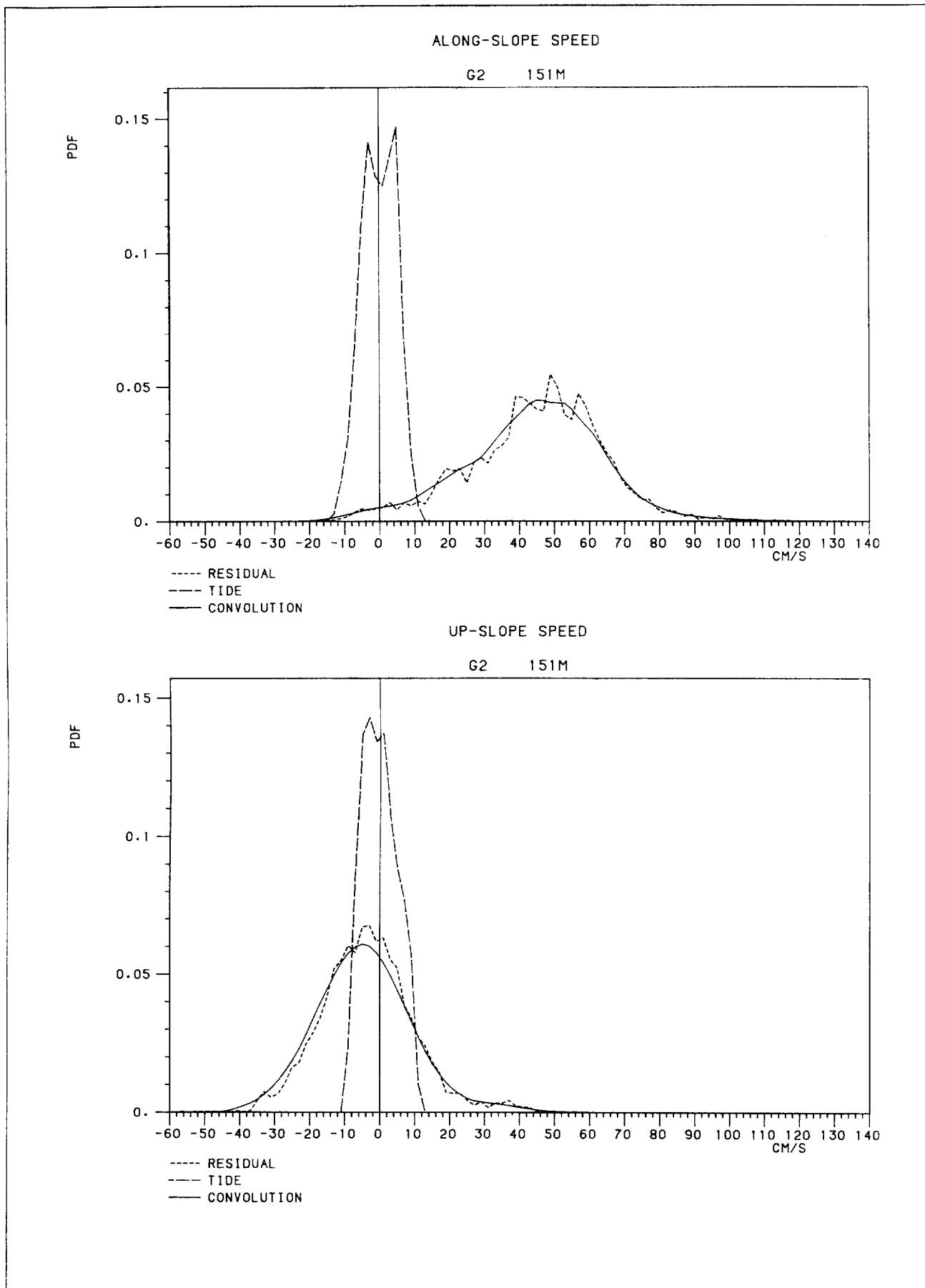


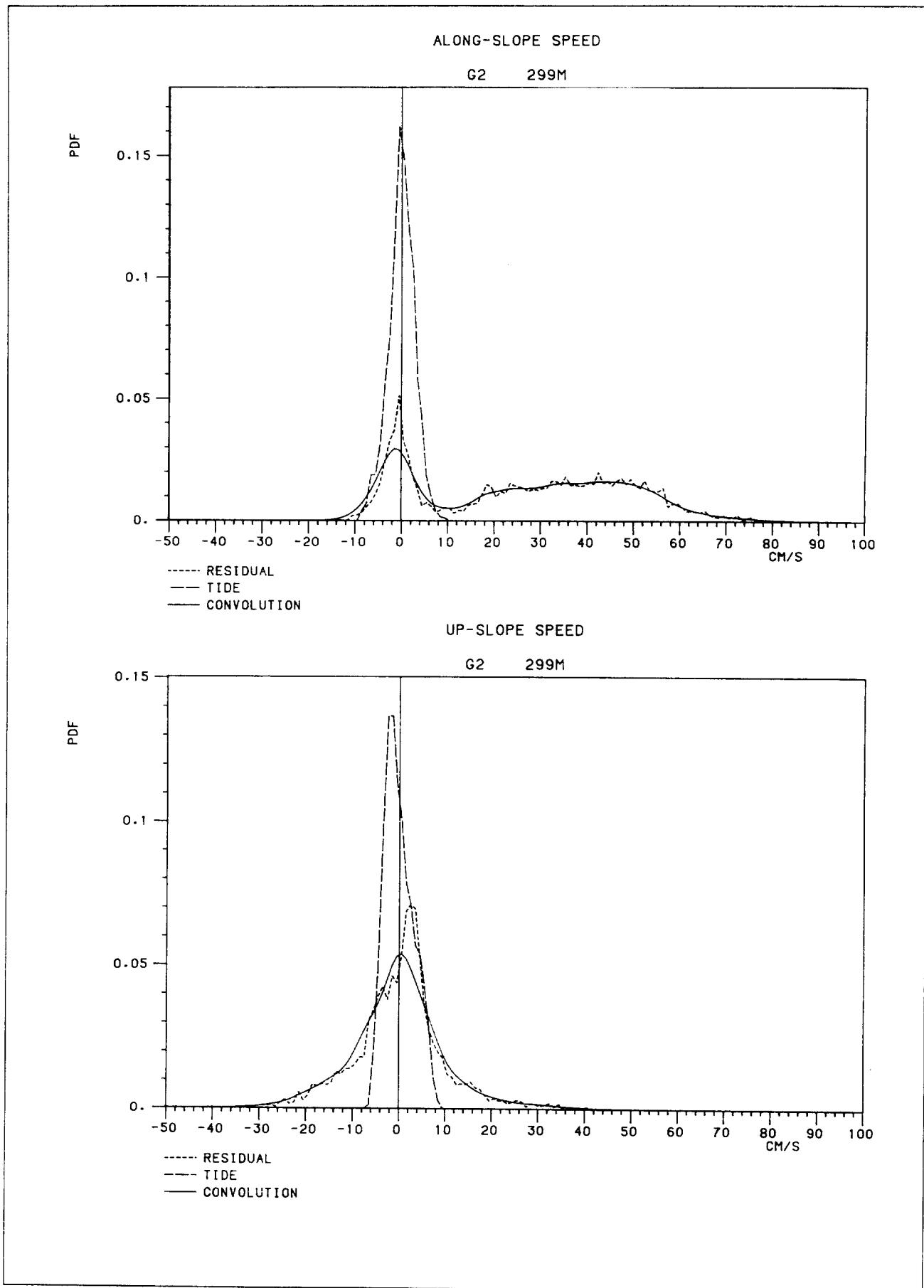


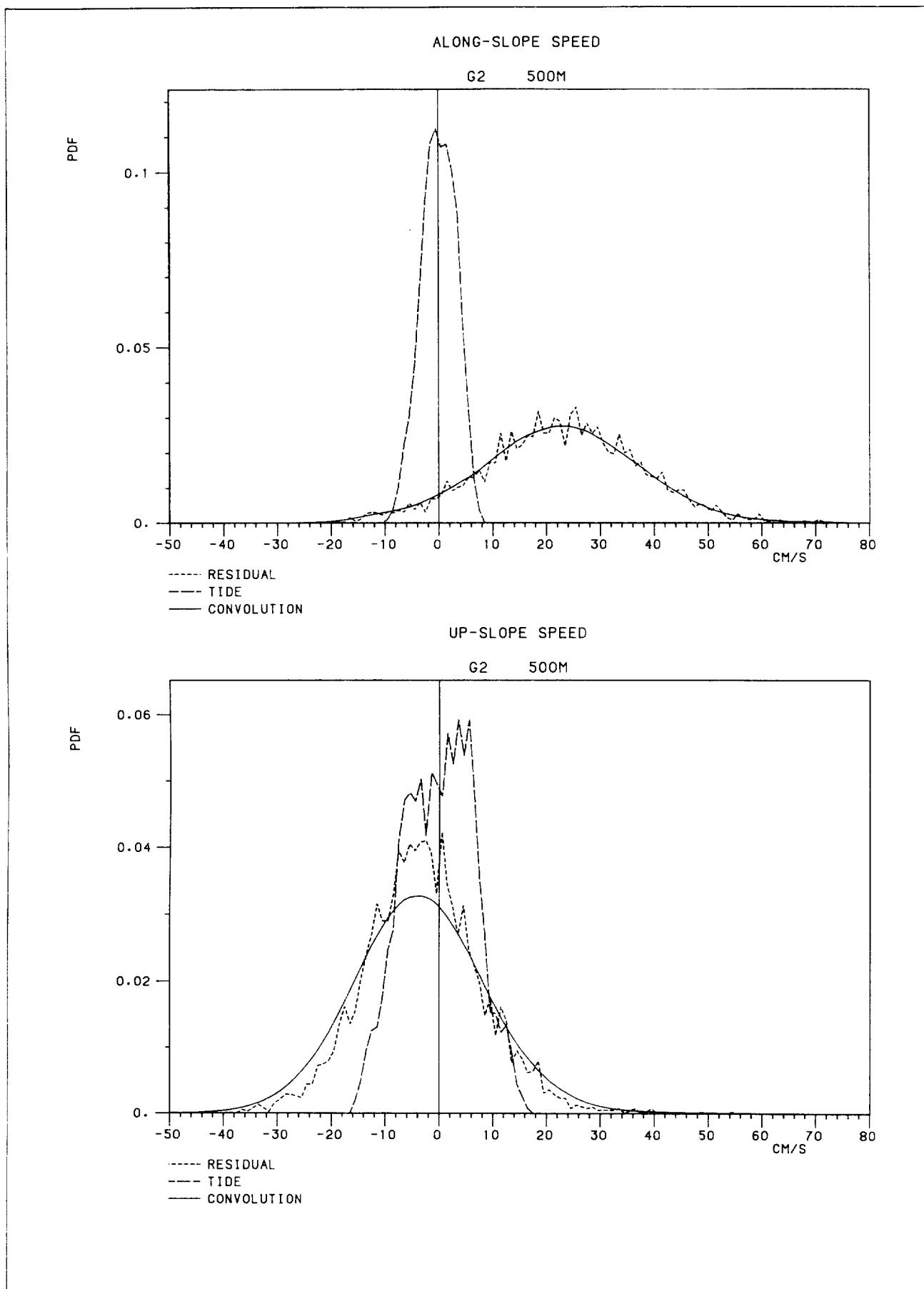


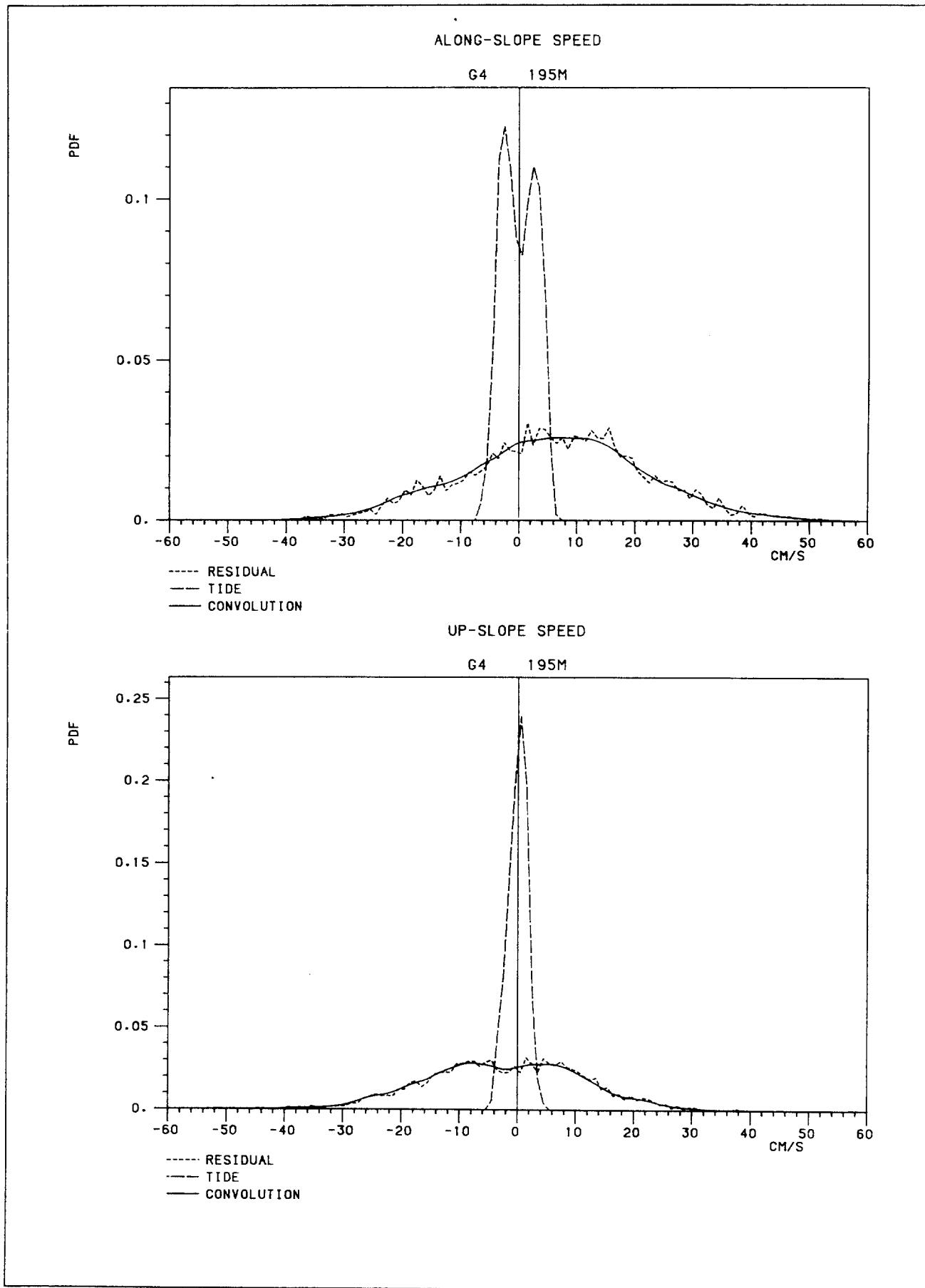


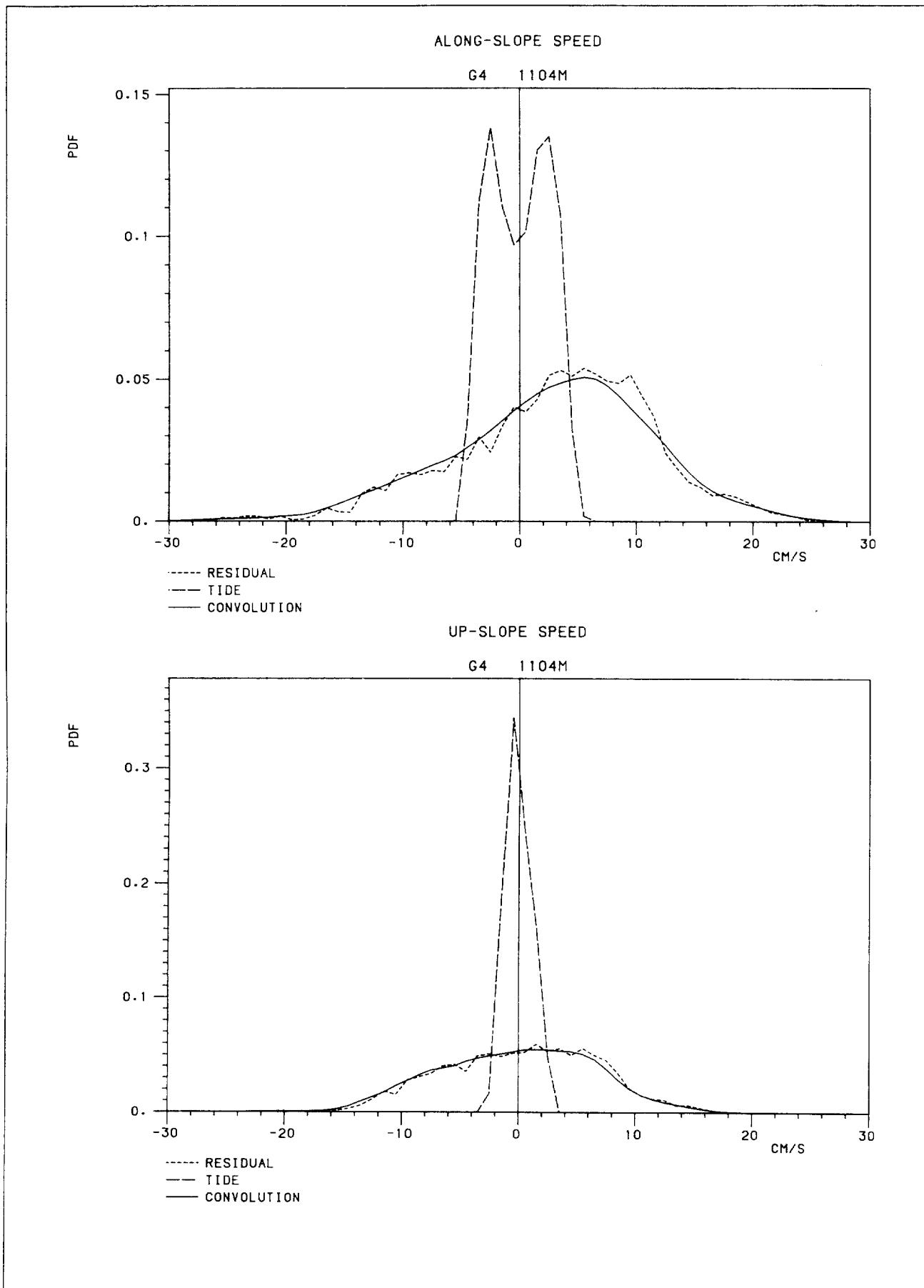


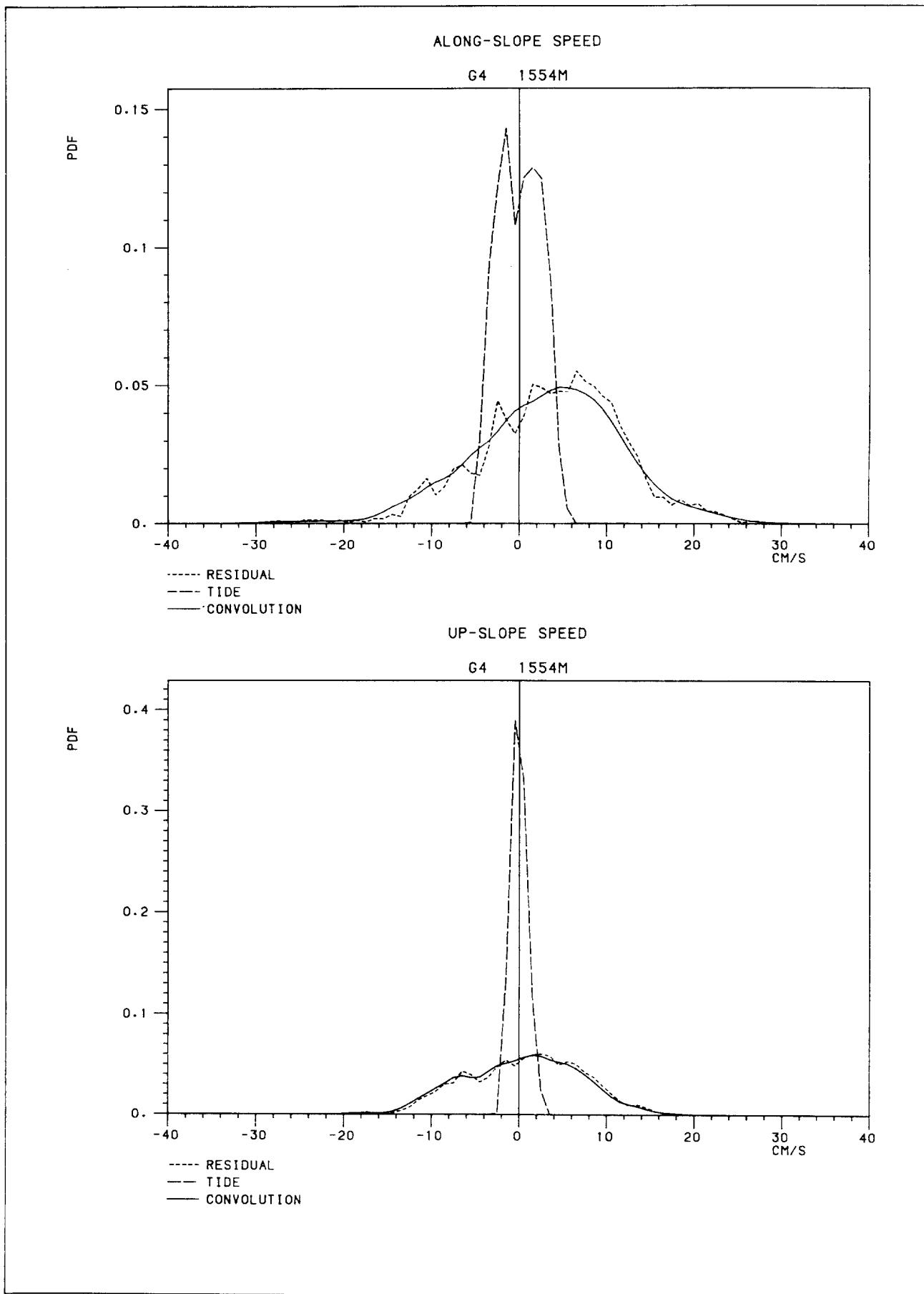


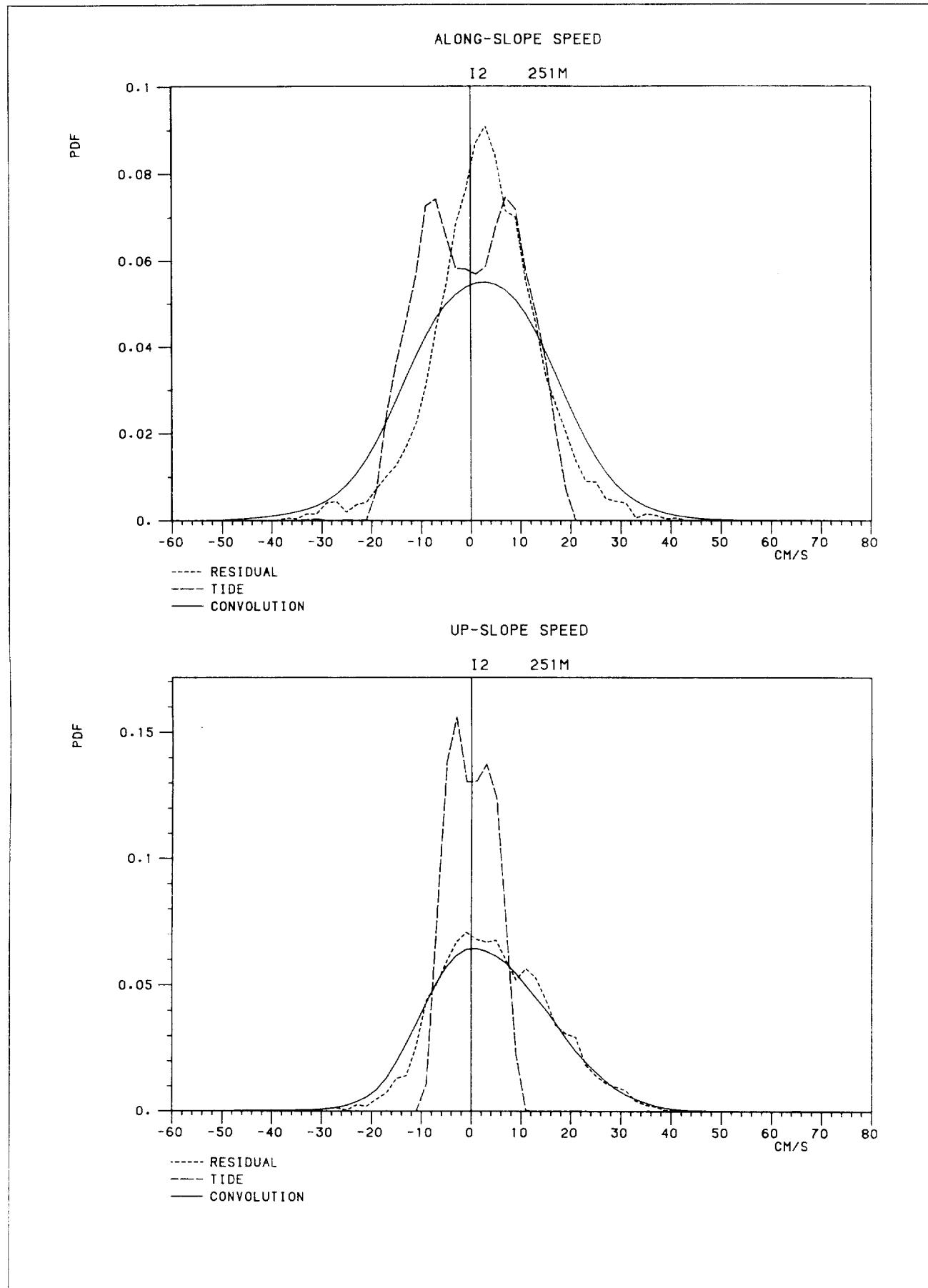


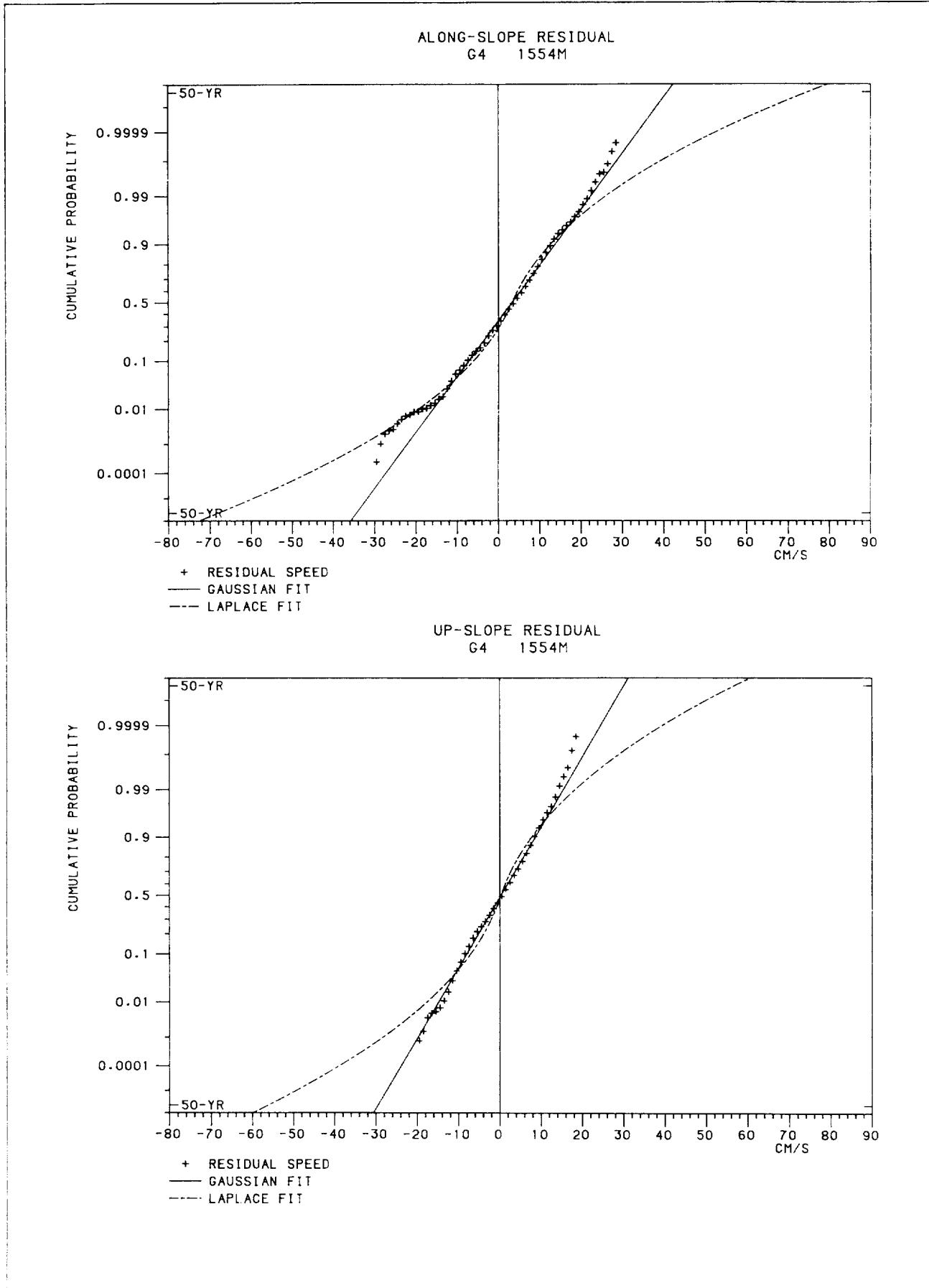


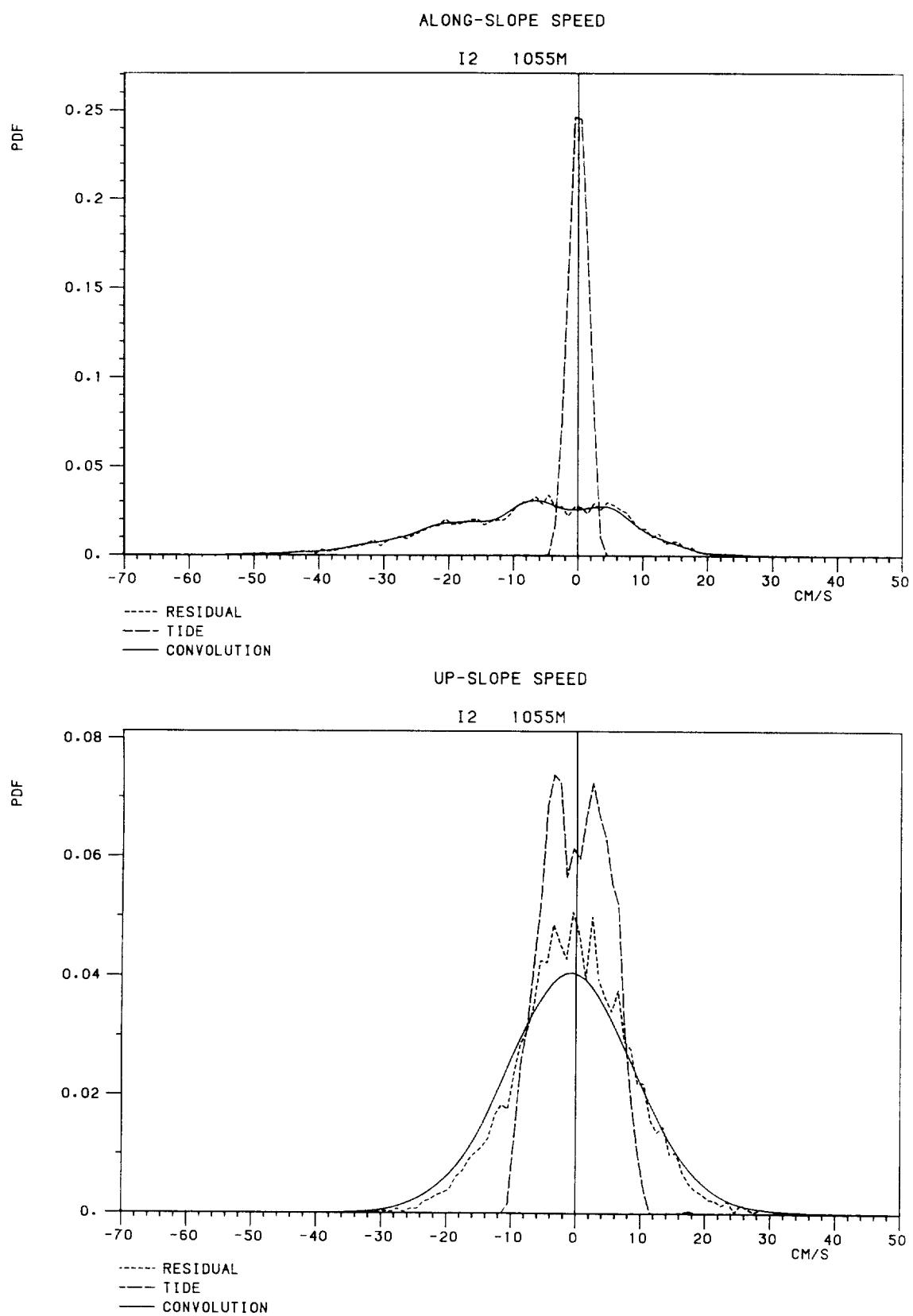












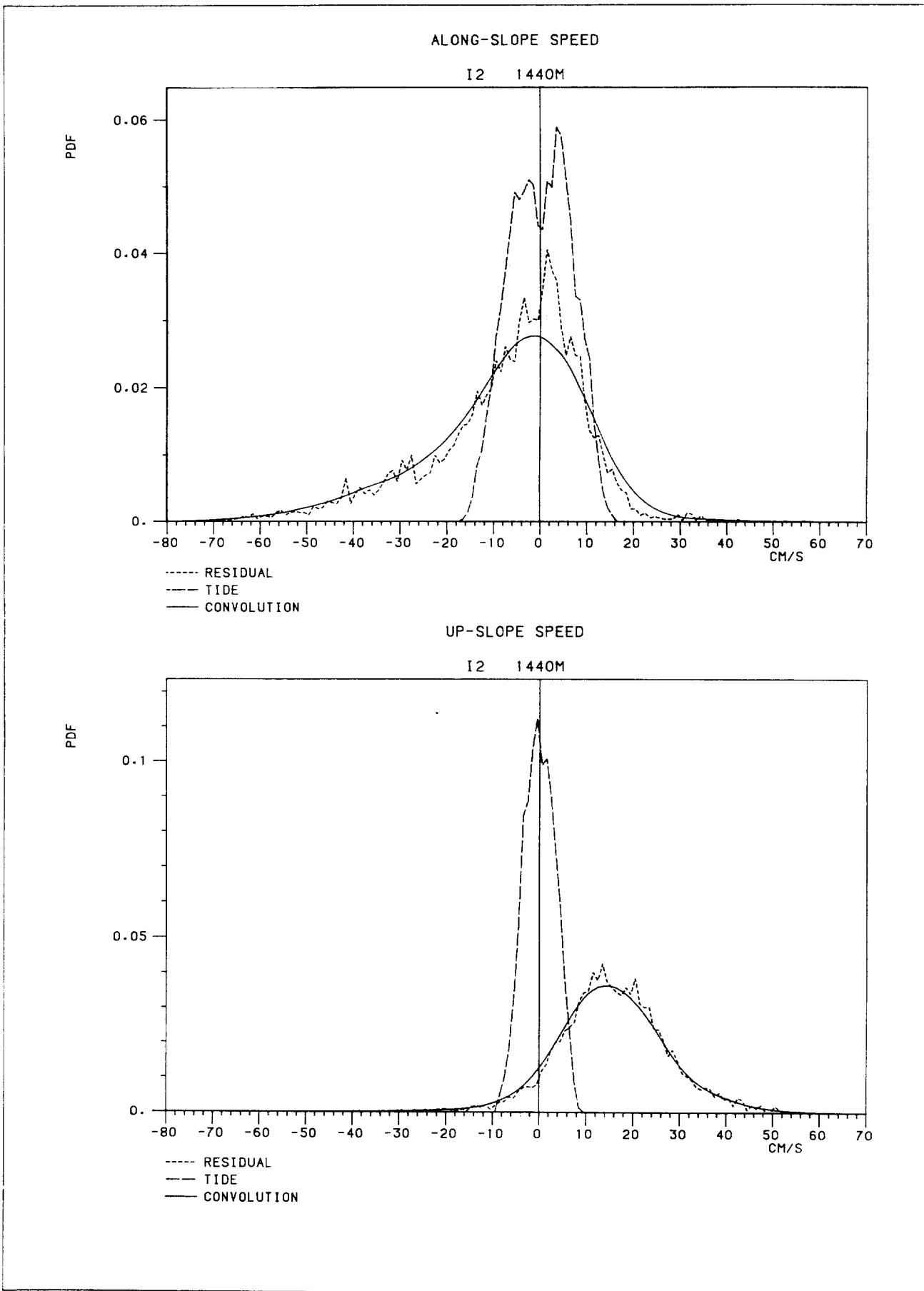
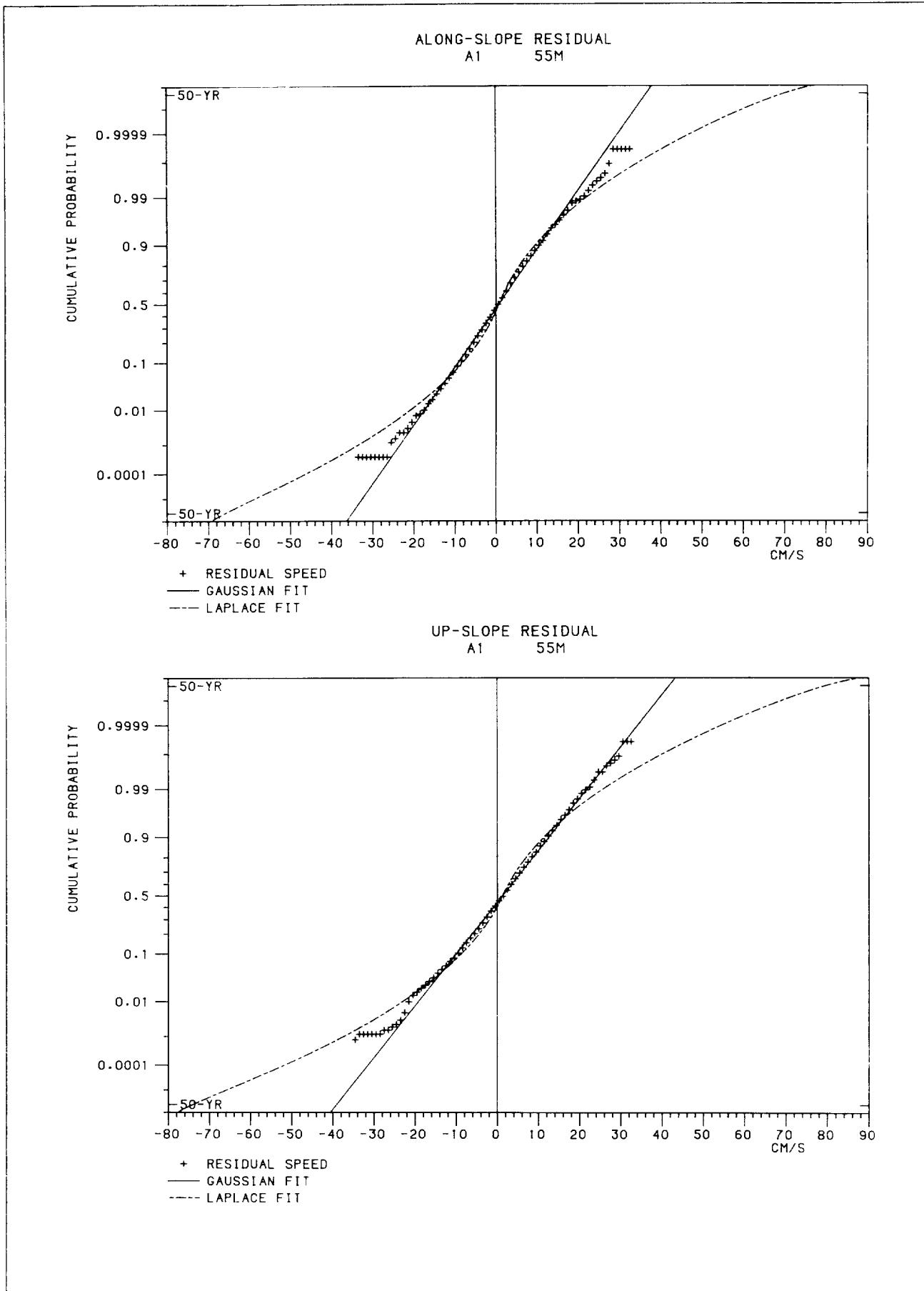
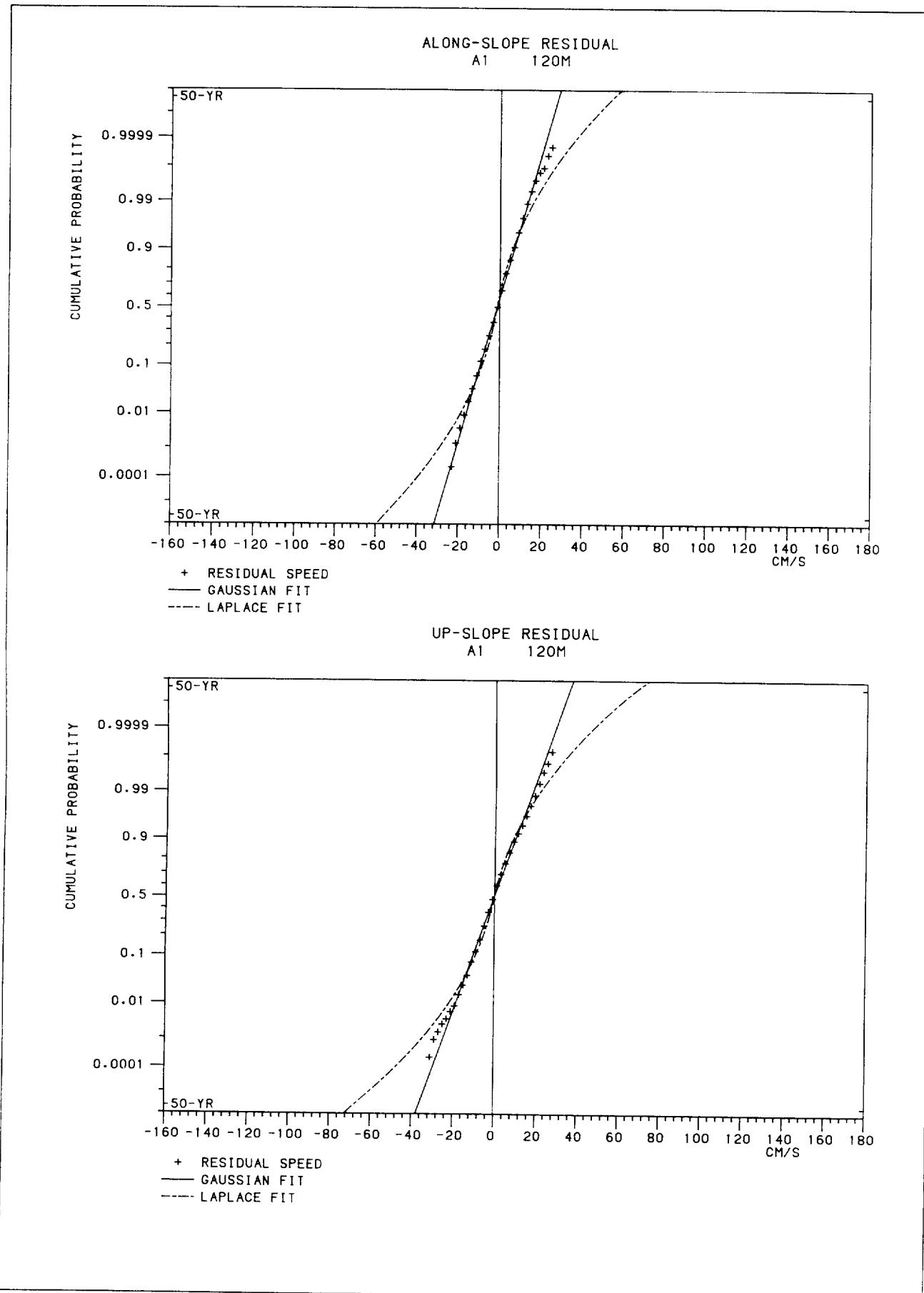
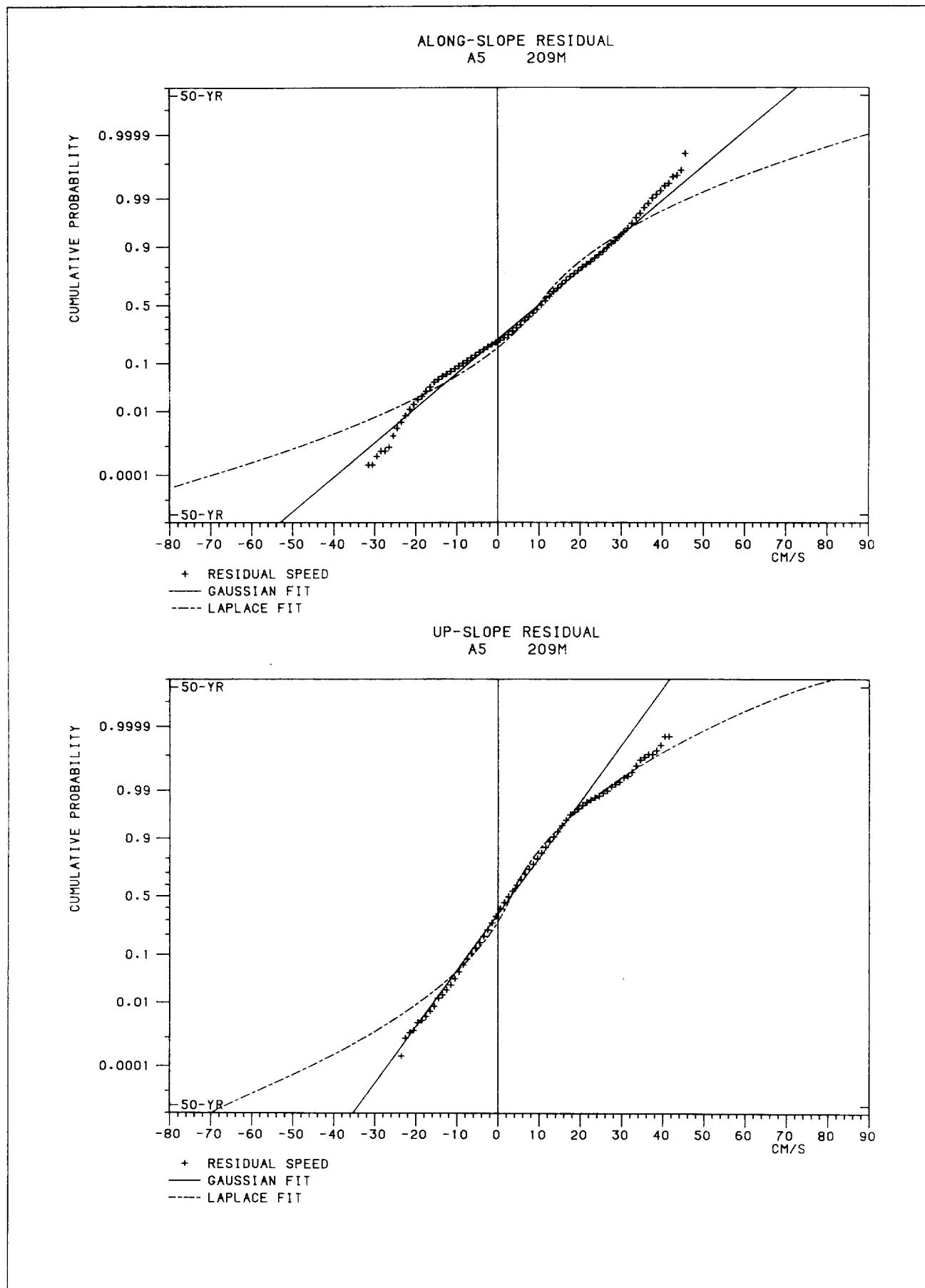
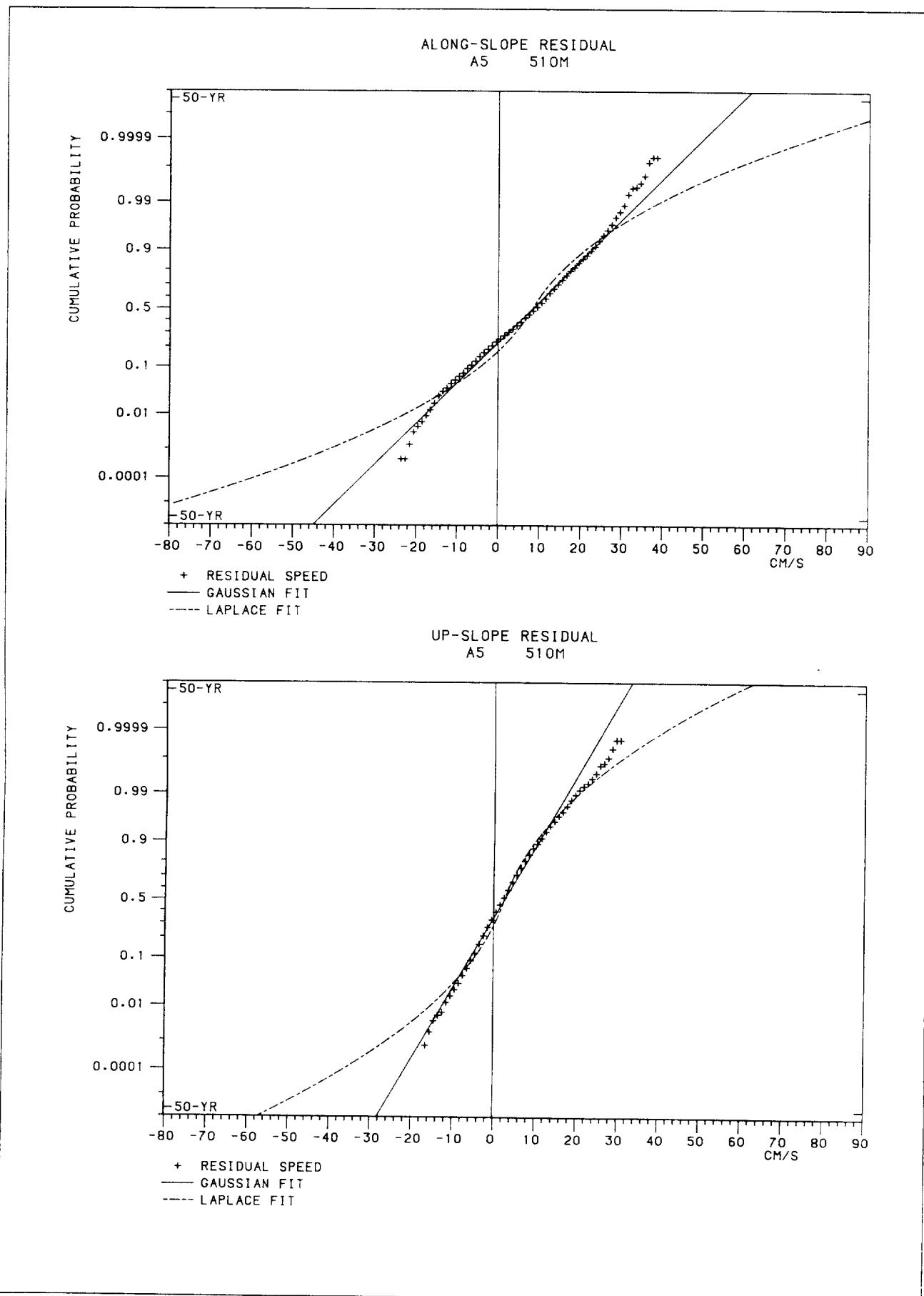


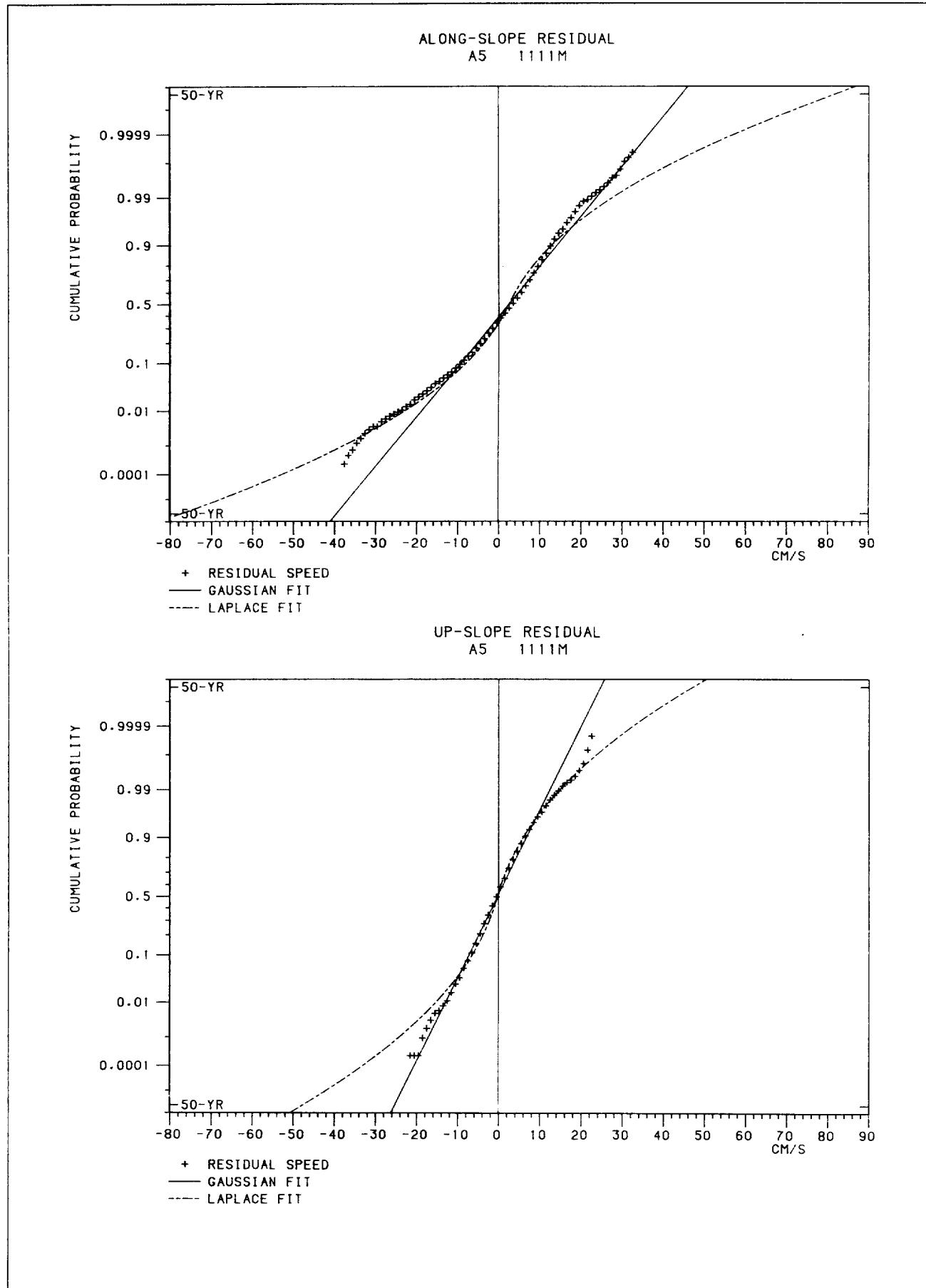
Fig.3: Cumulative probability distributions of residual current speed along-and up-slope from records at each current meter and fitted Gaussian and Laplacian fits. (The meter is identified by the mooring and by the depth of the meter below the sea surface.)

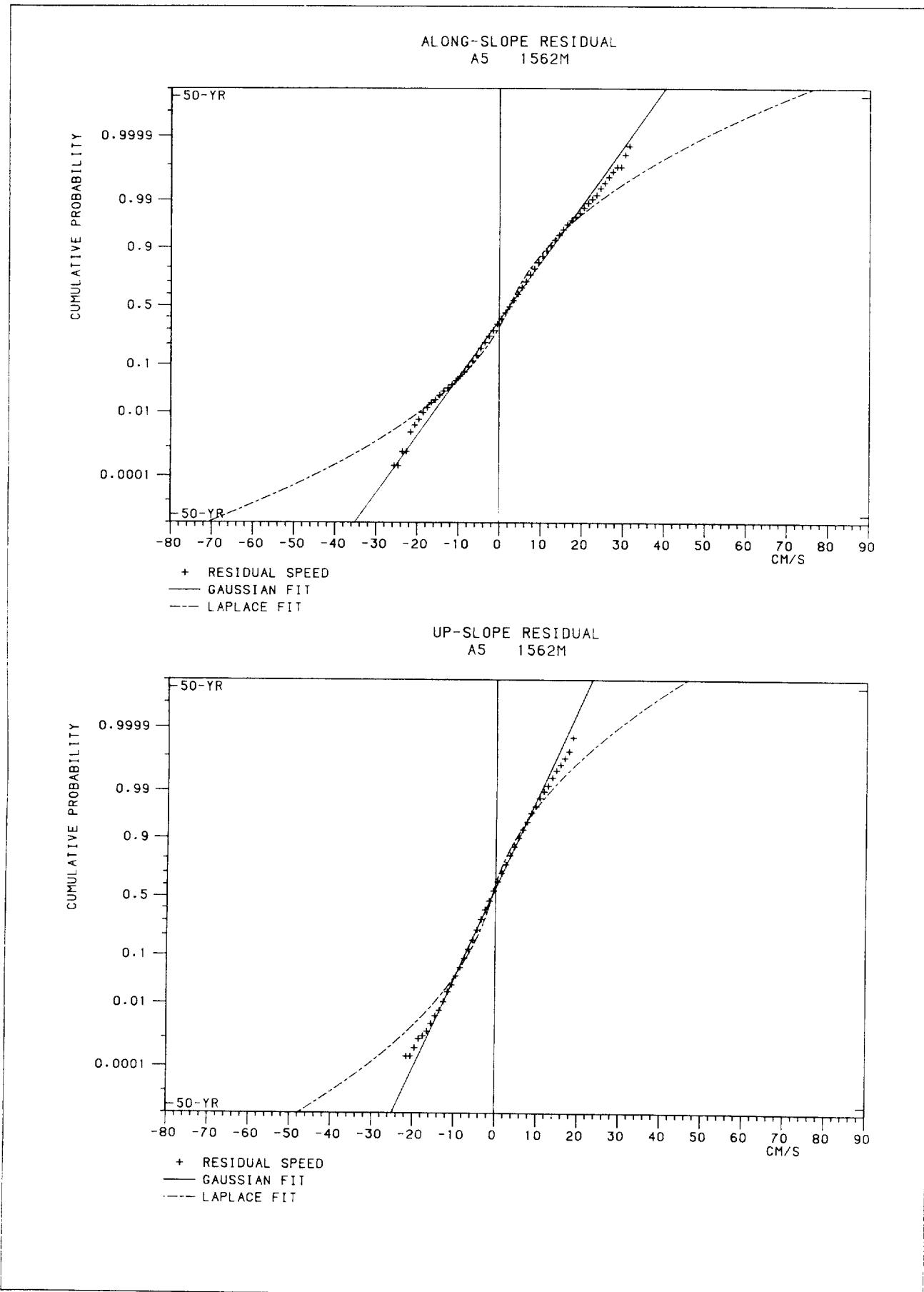


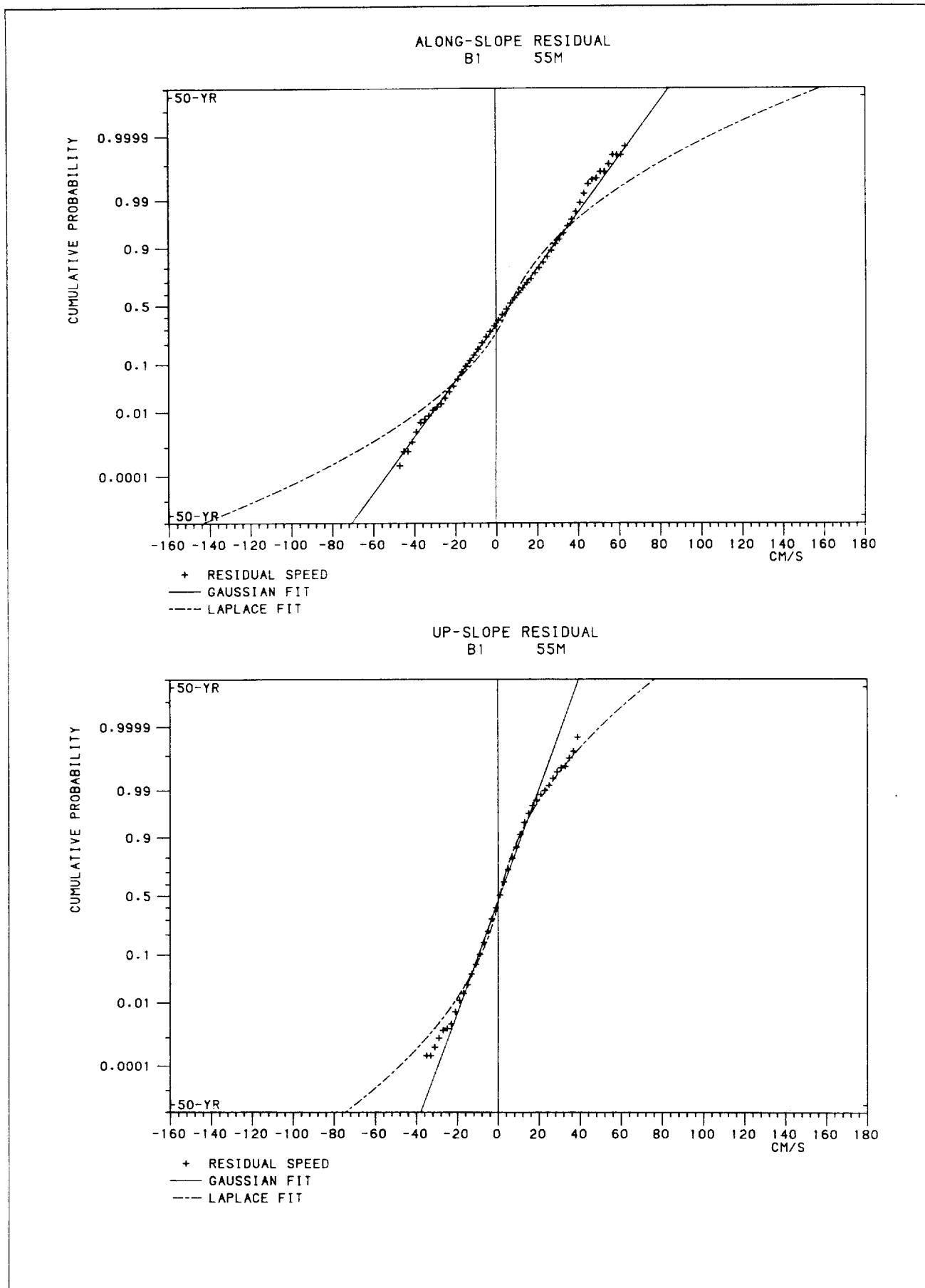


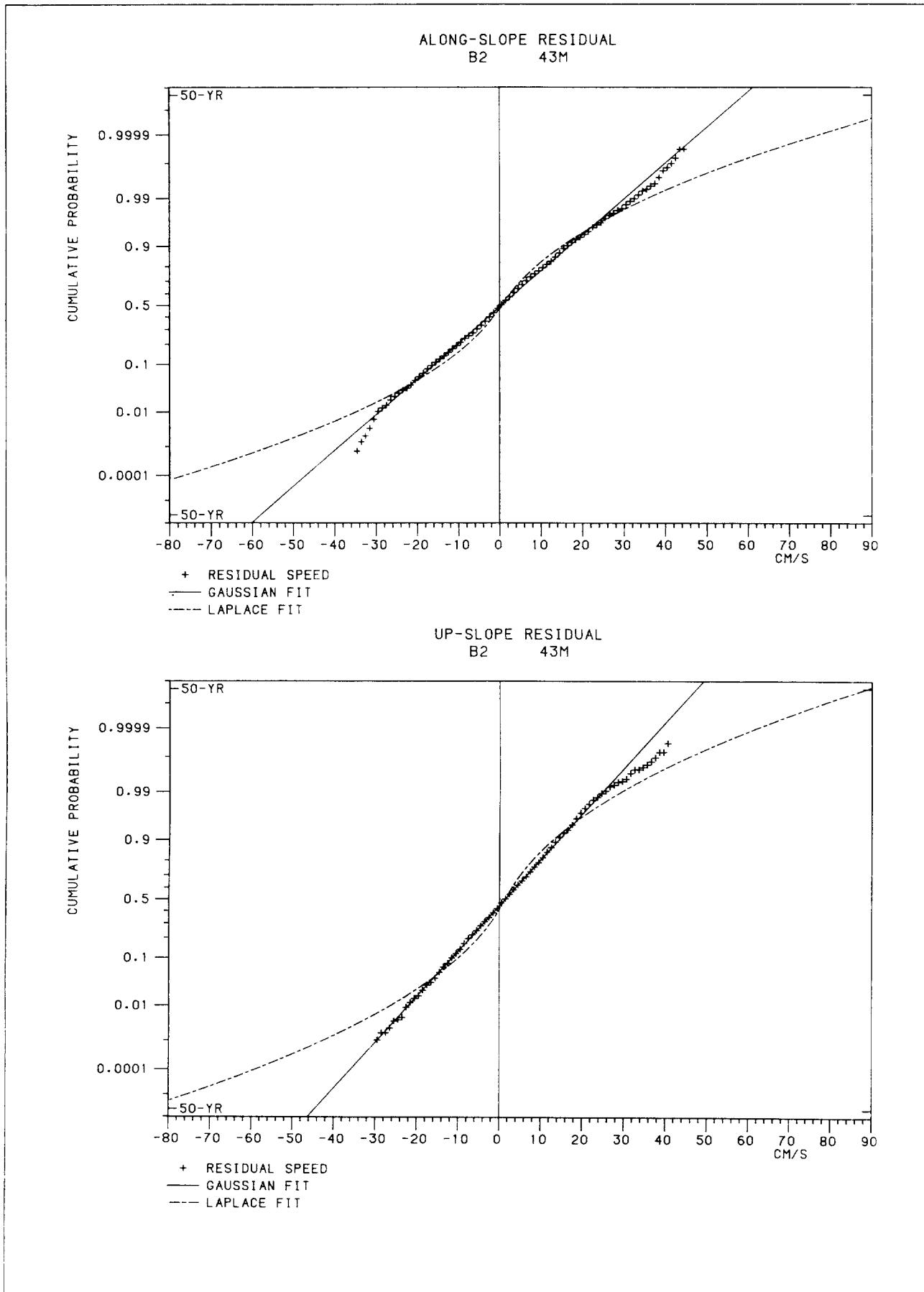


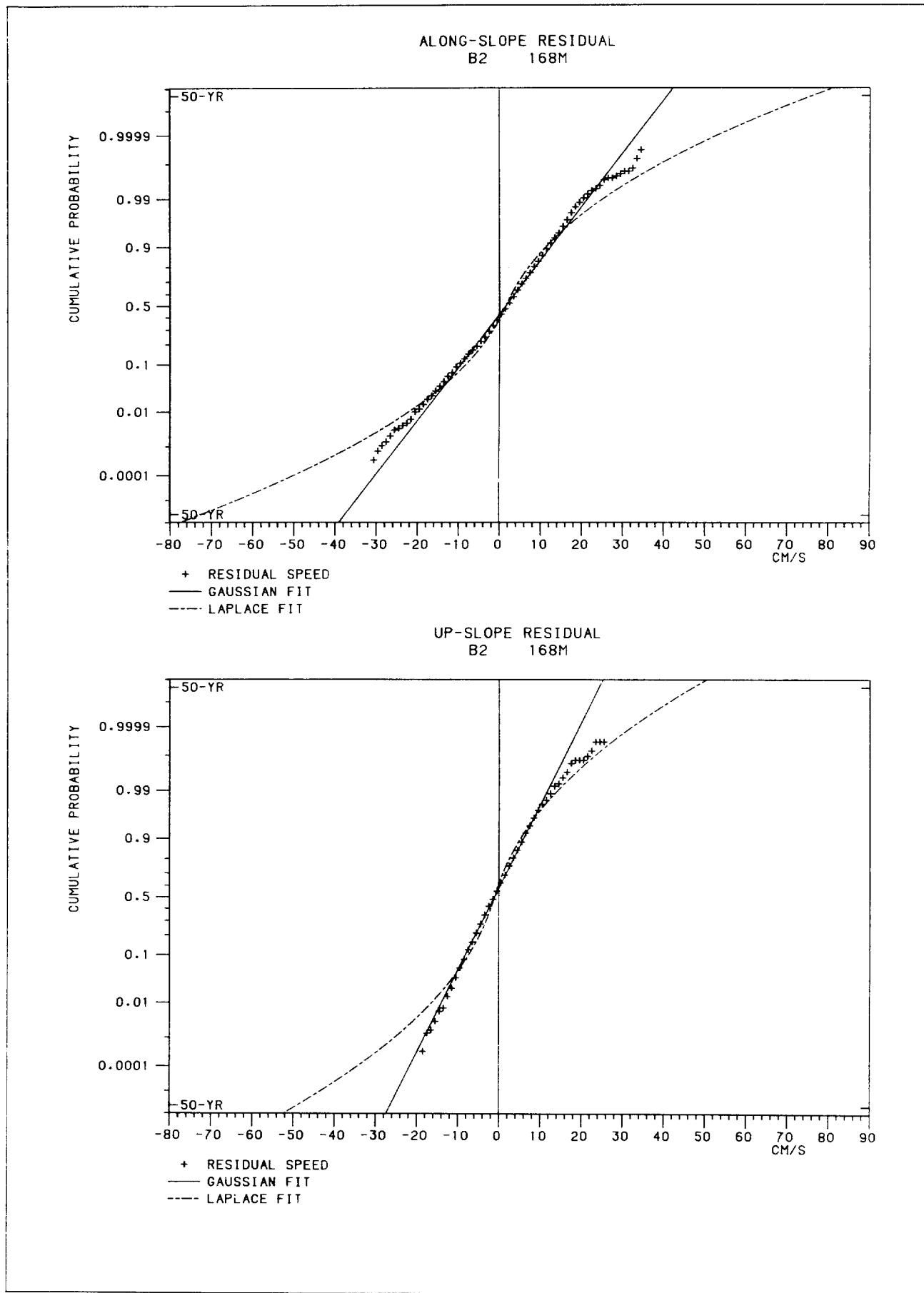


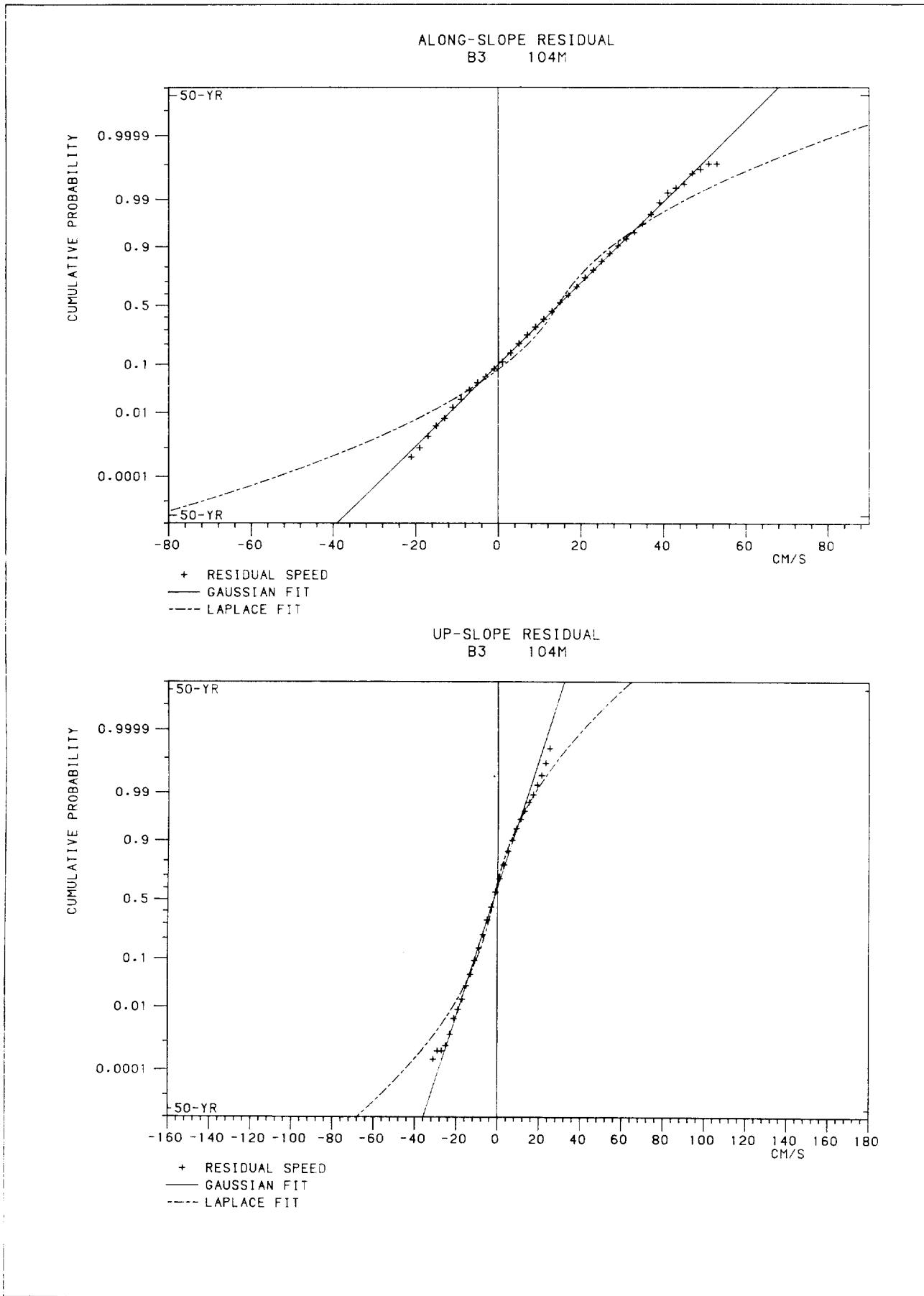


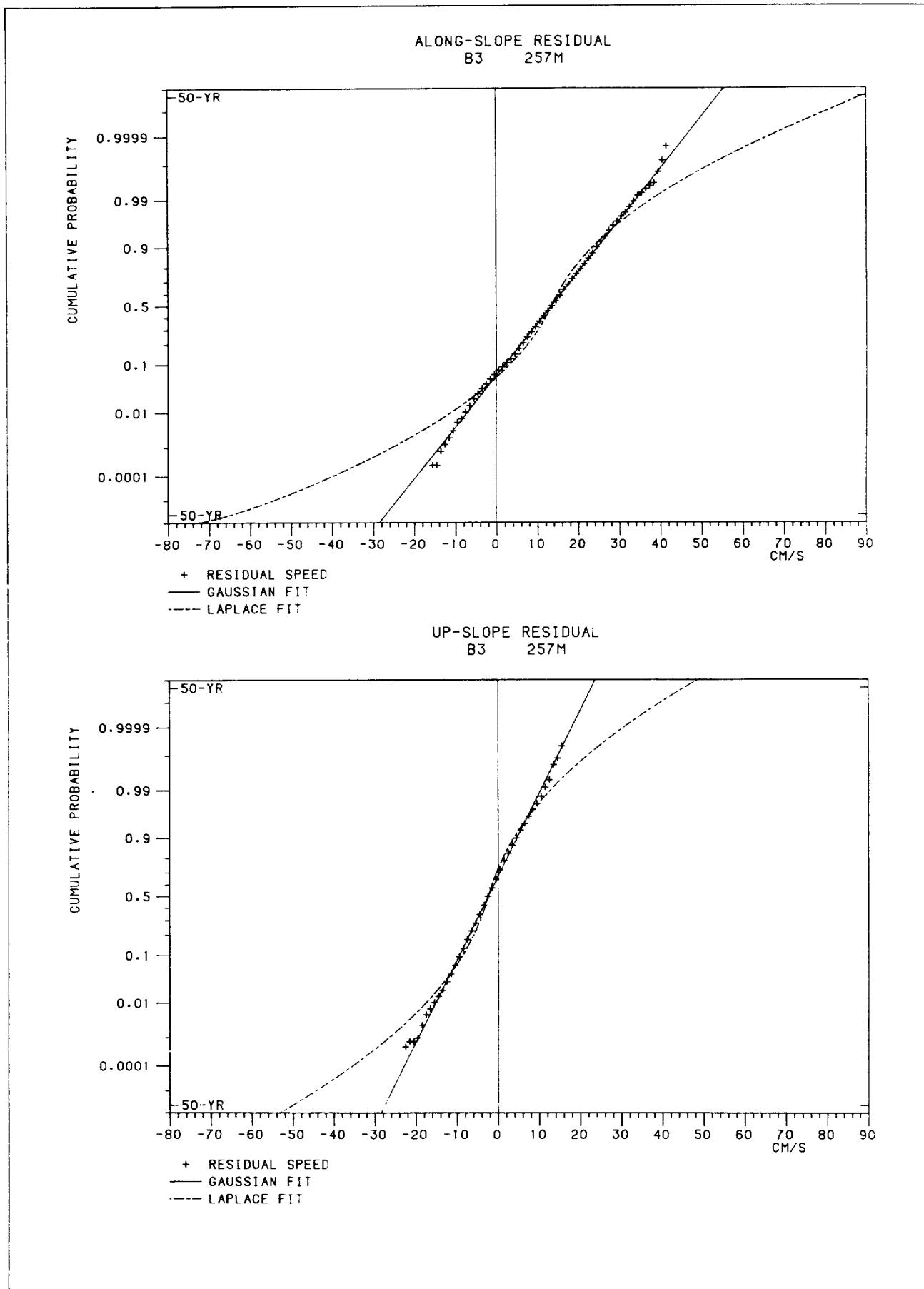


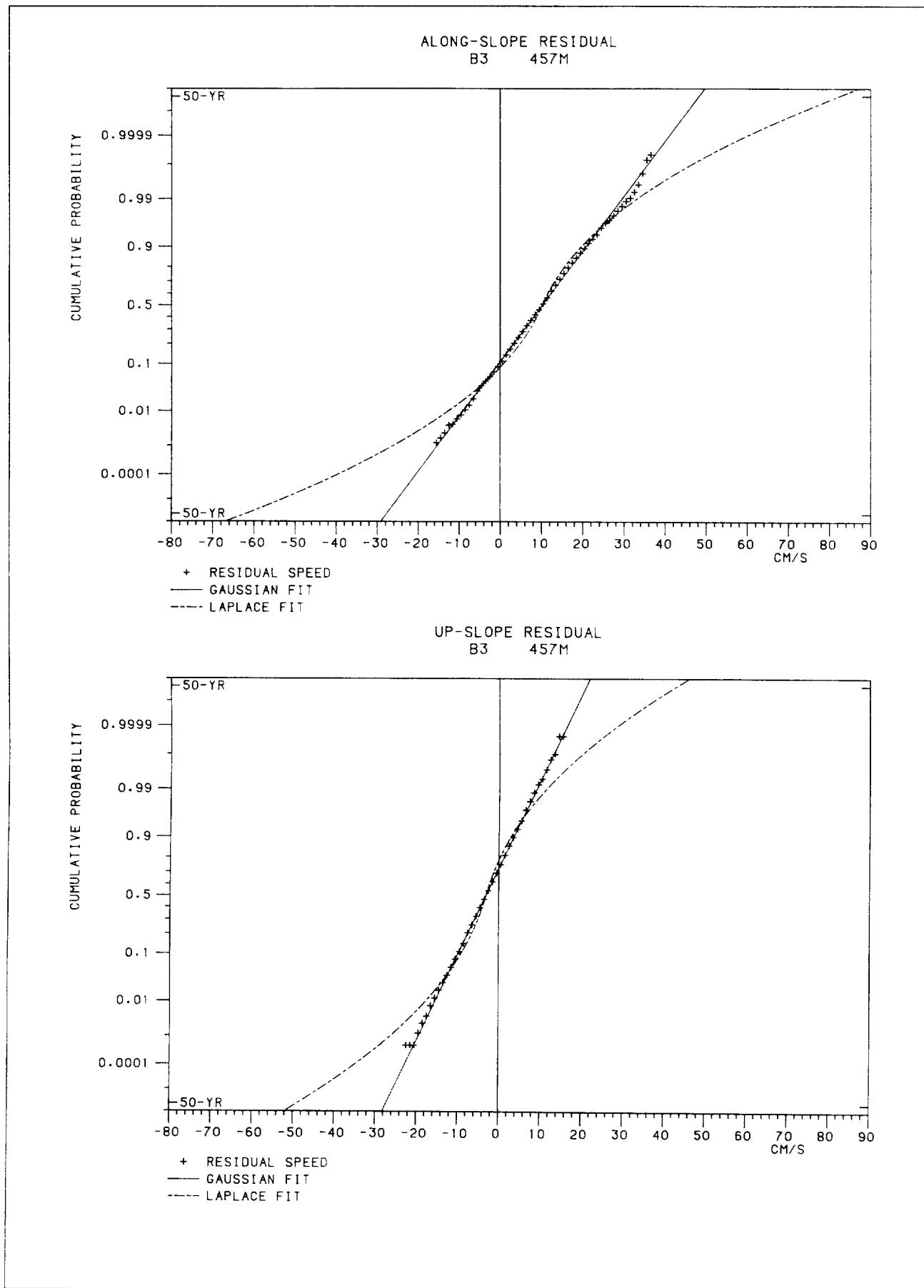


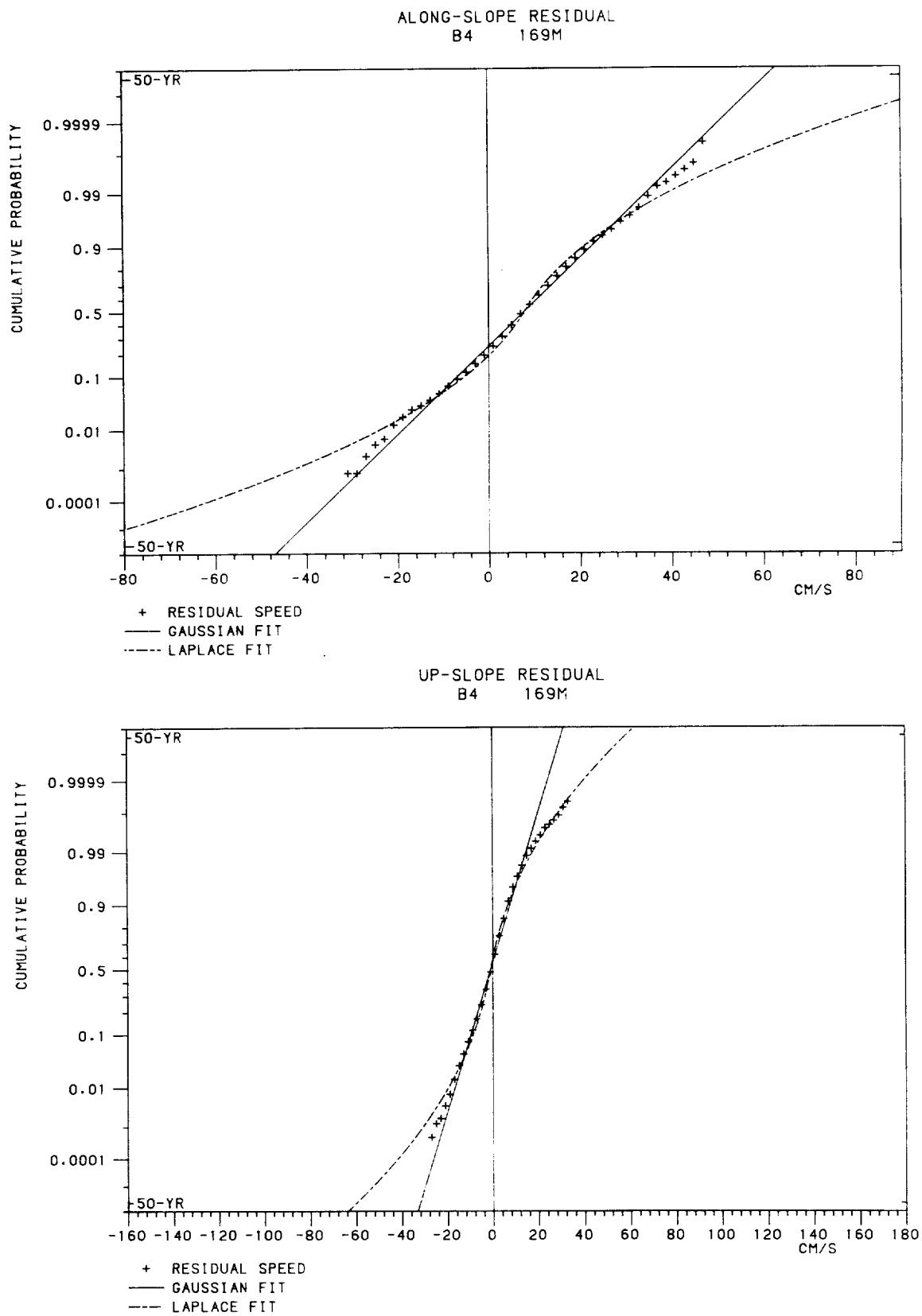


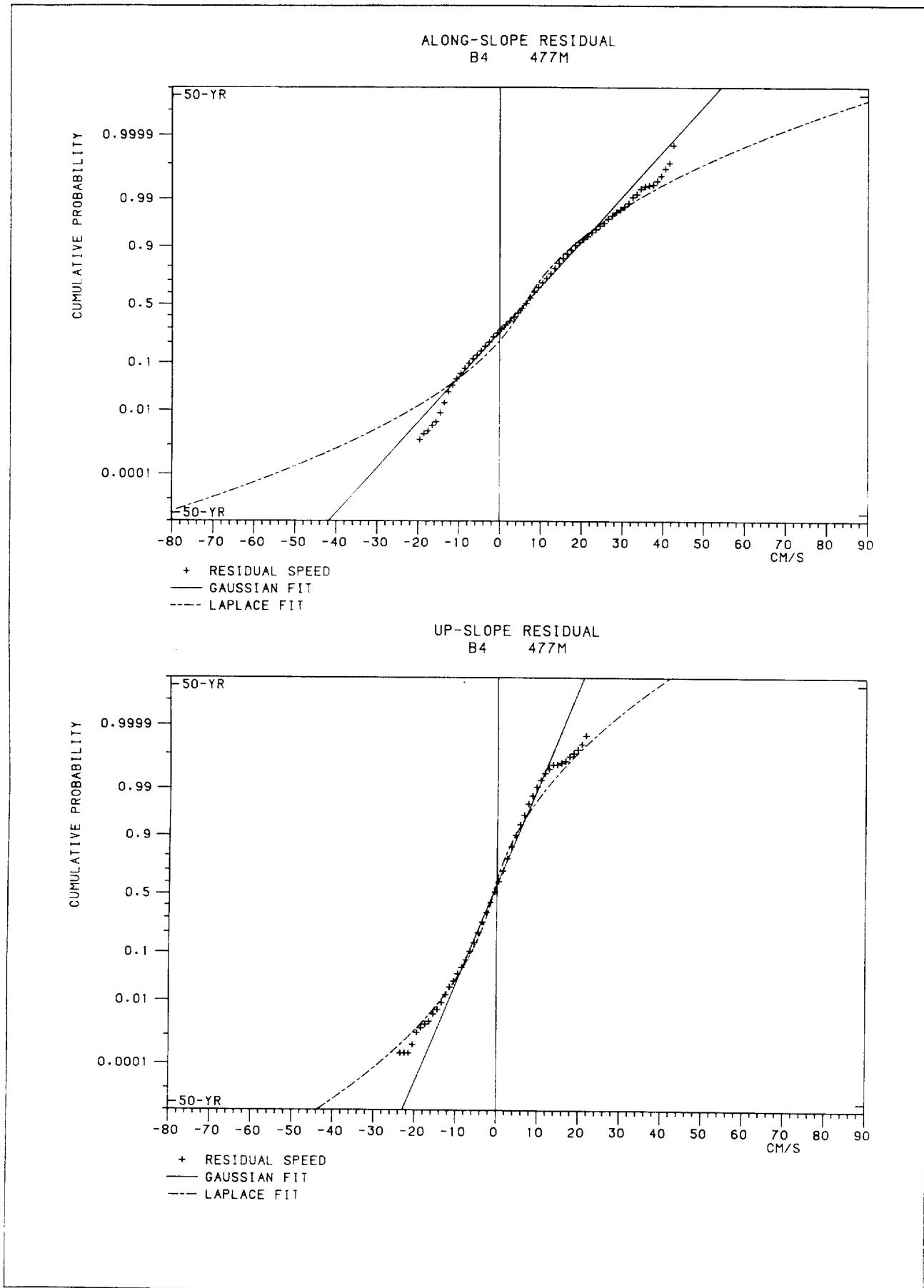


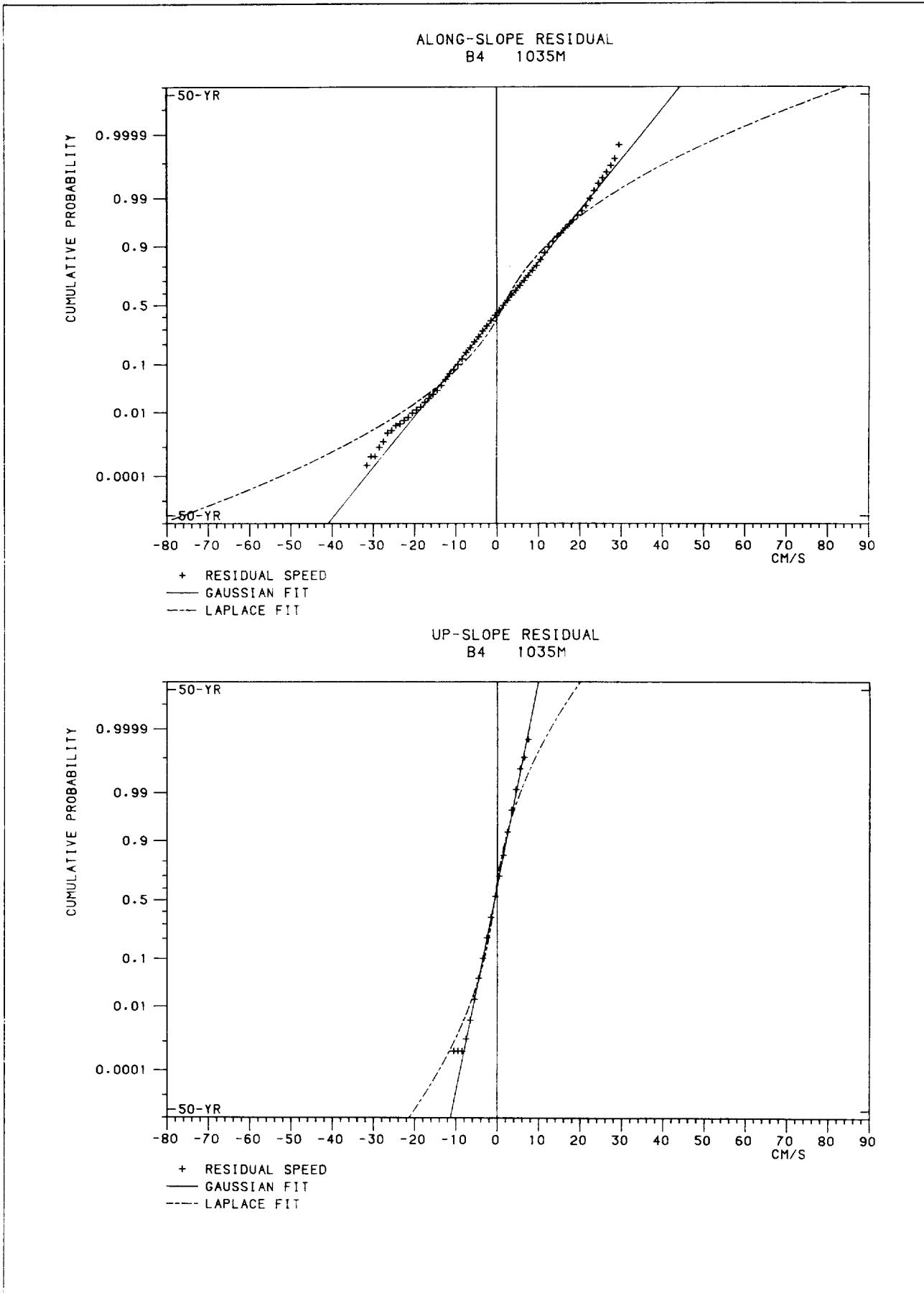


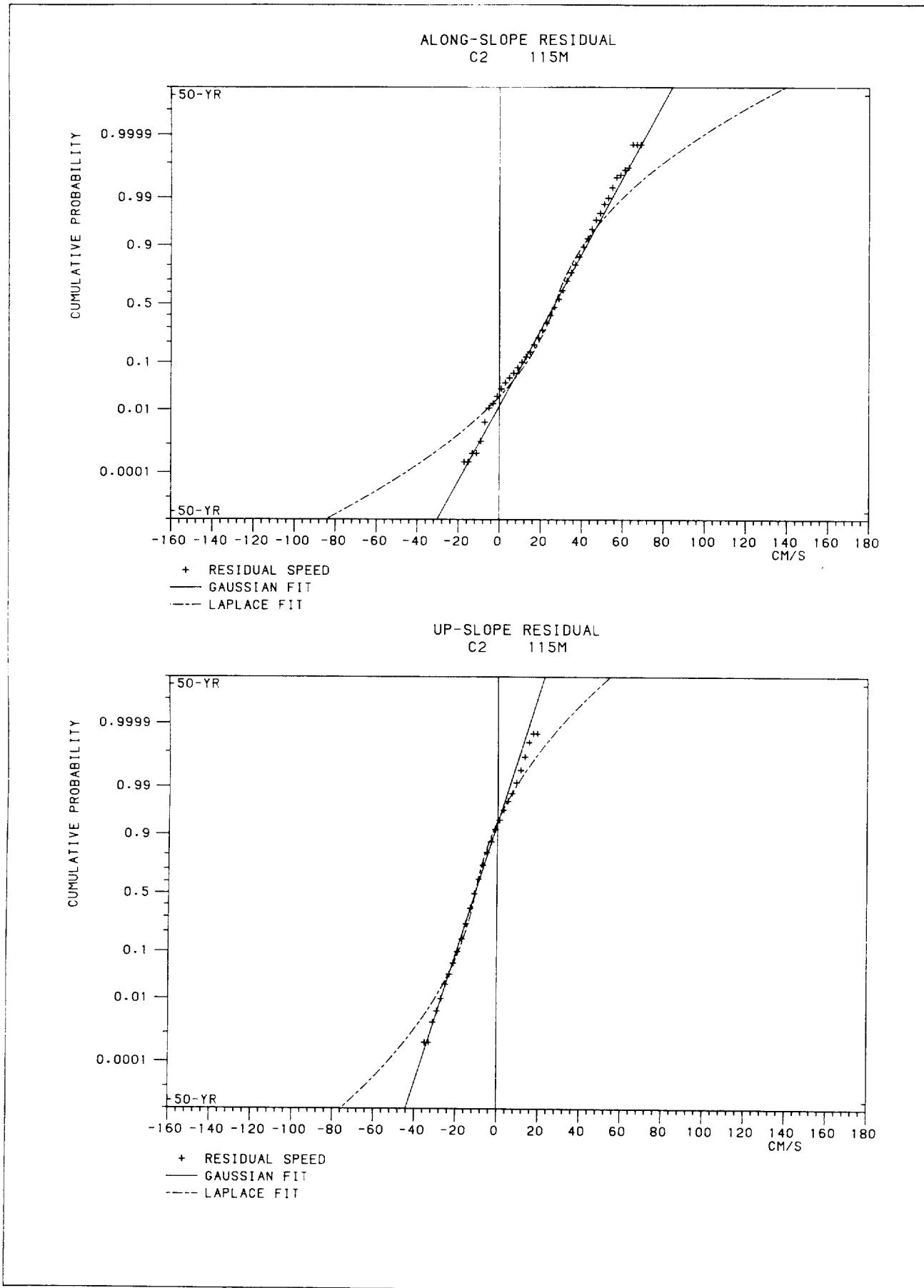


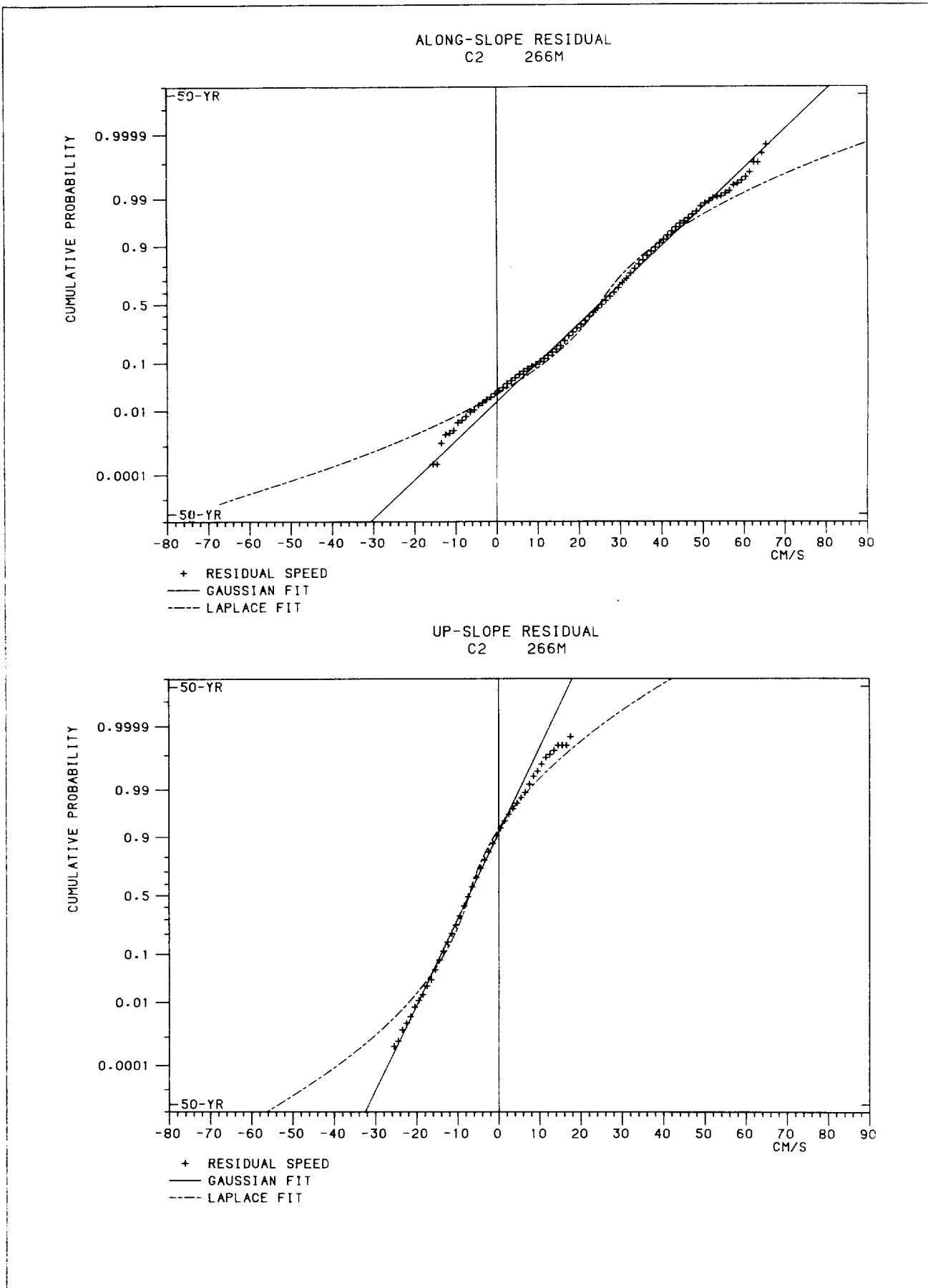


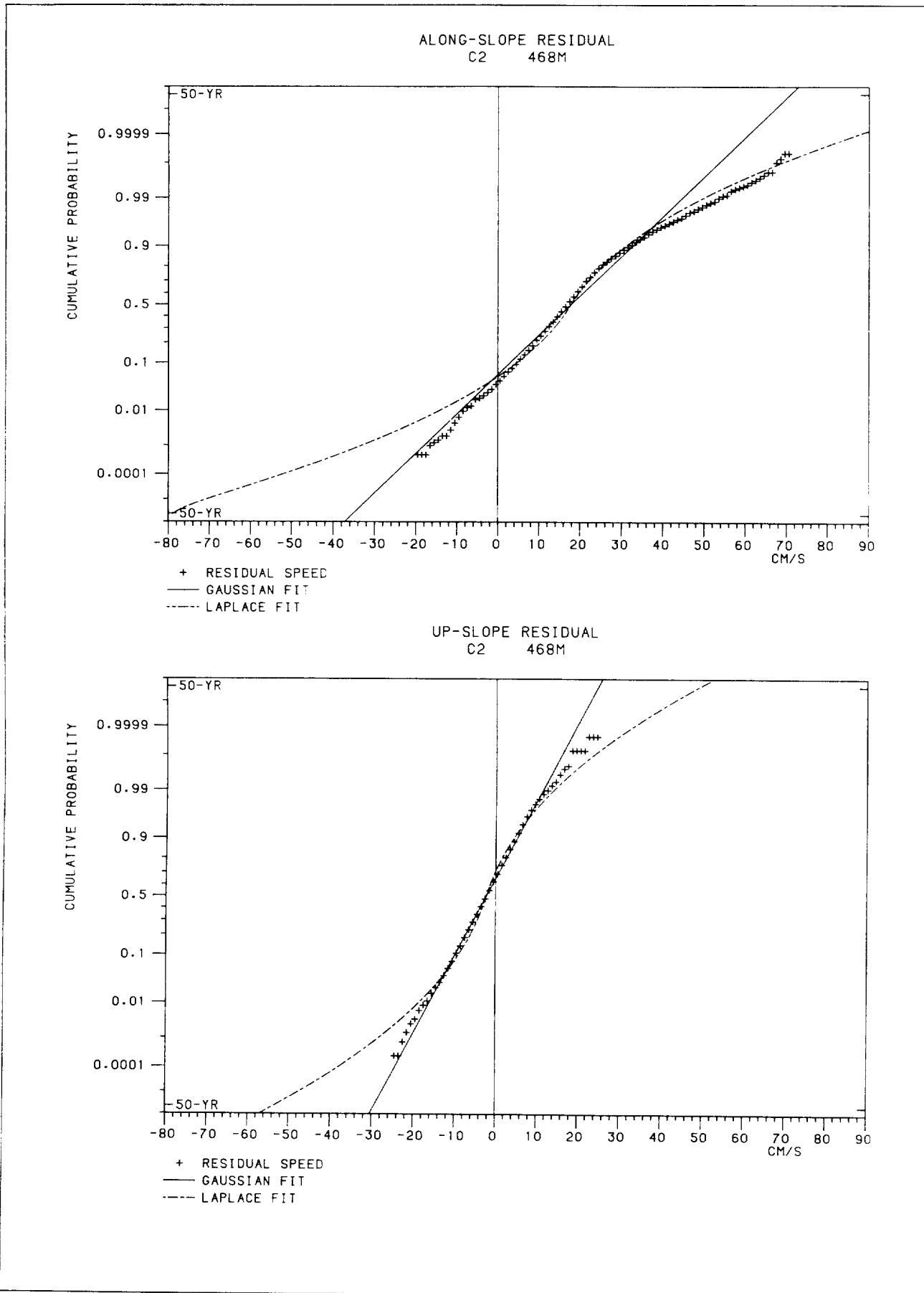


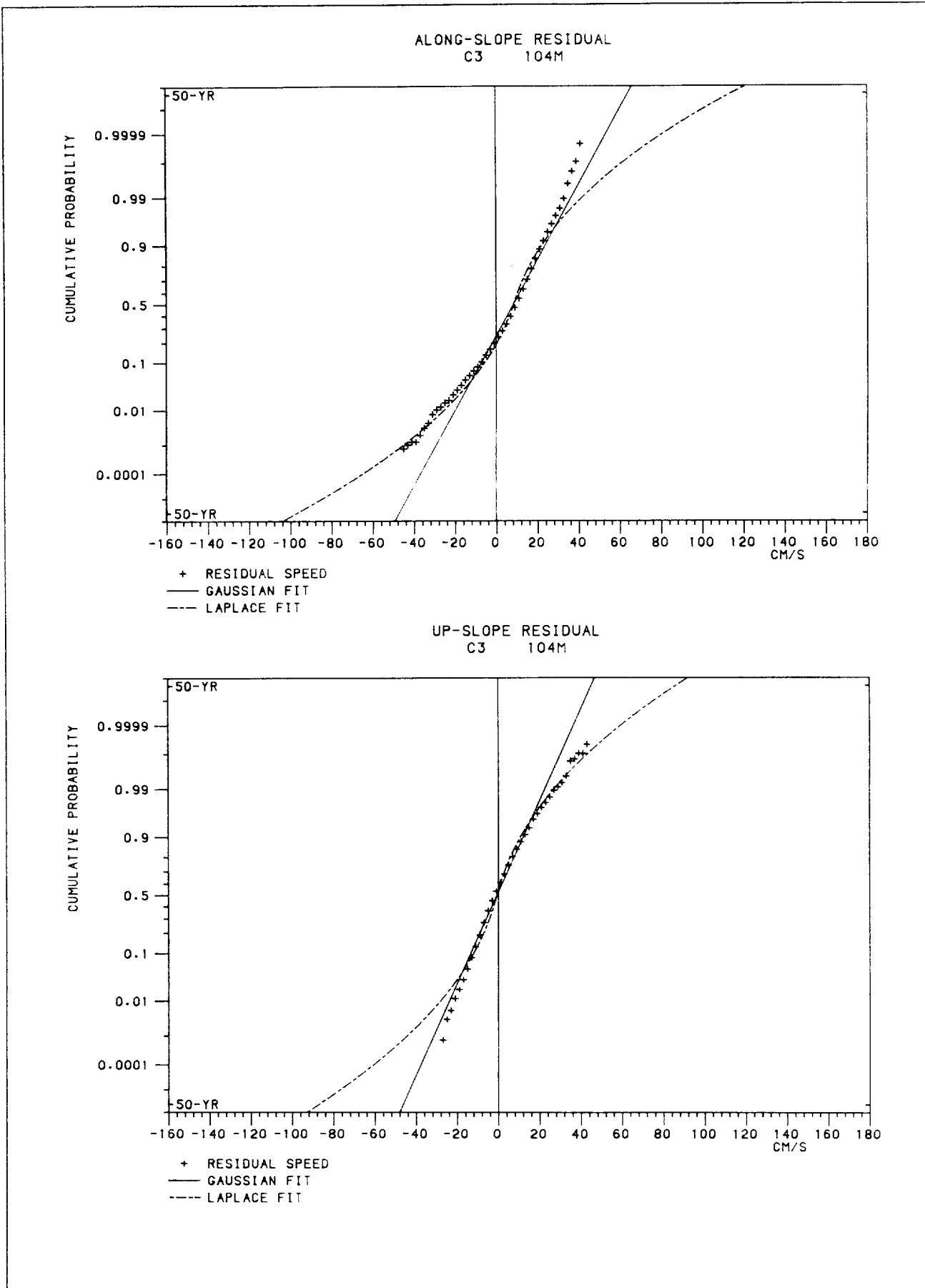


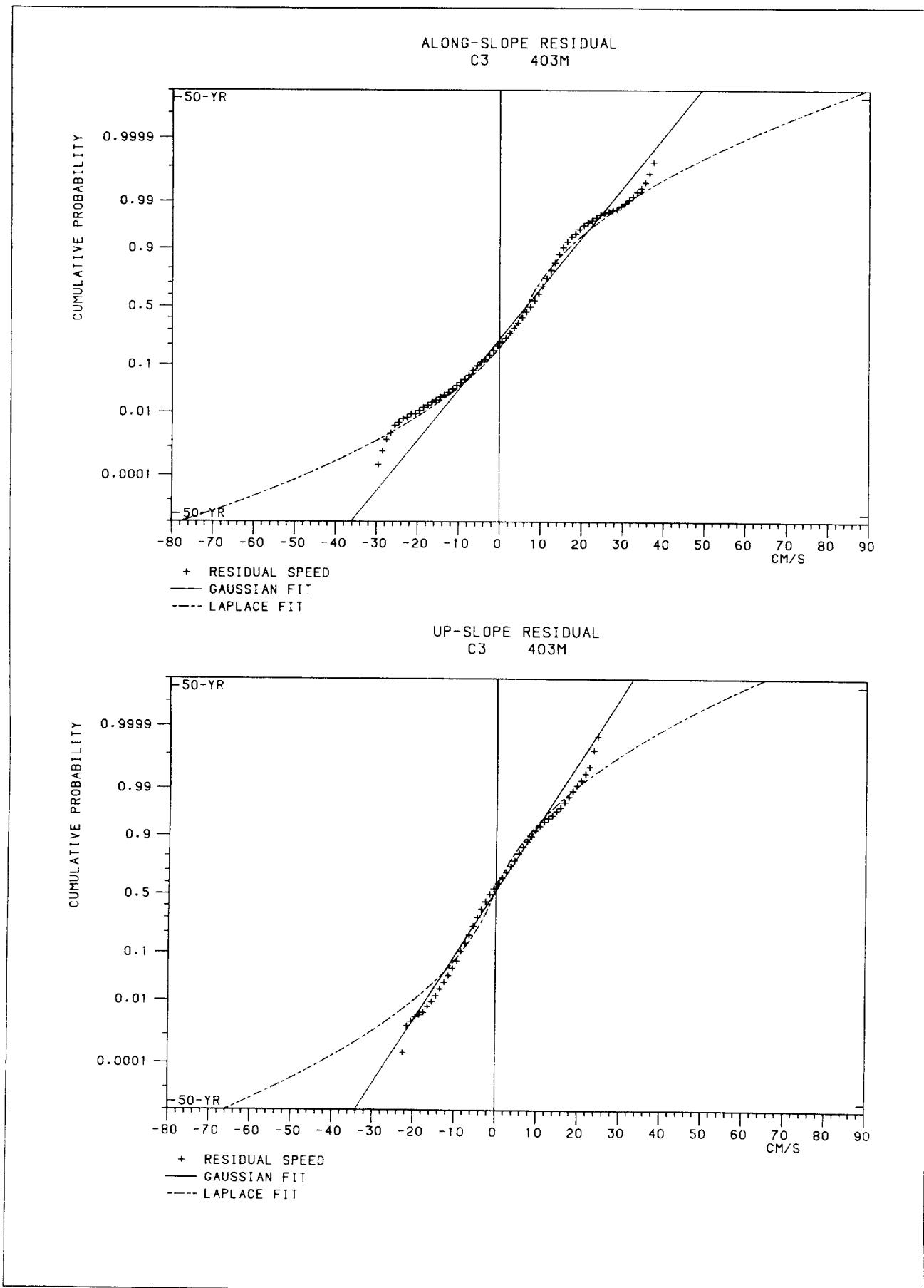


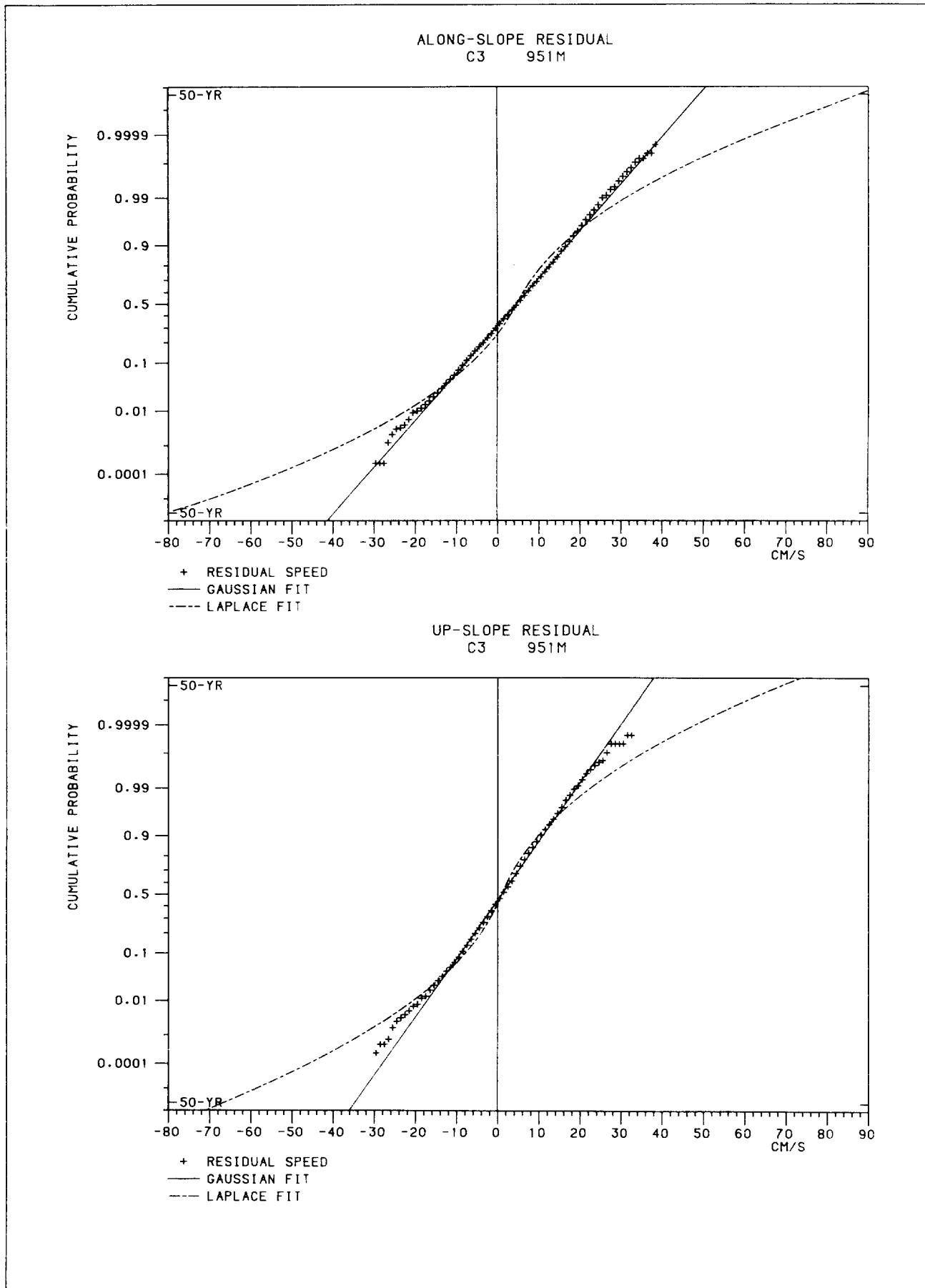


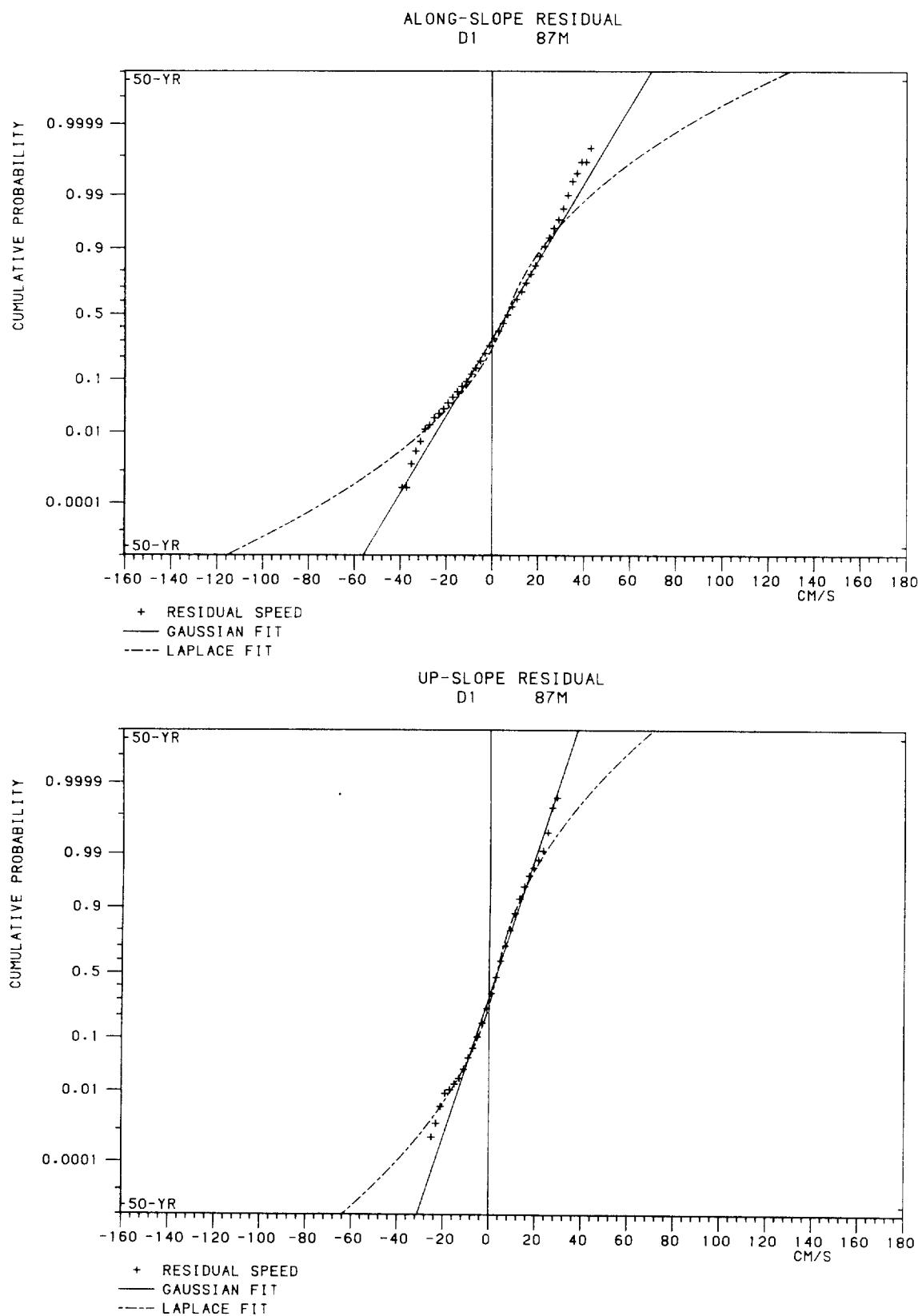


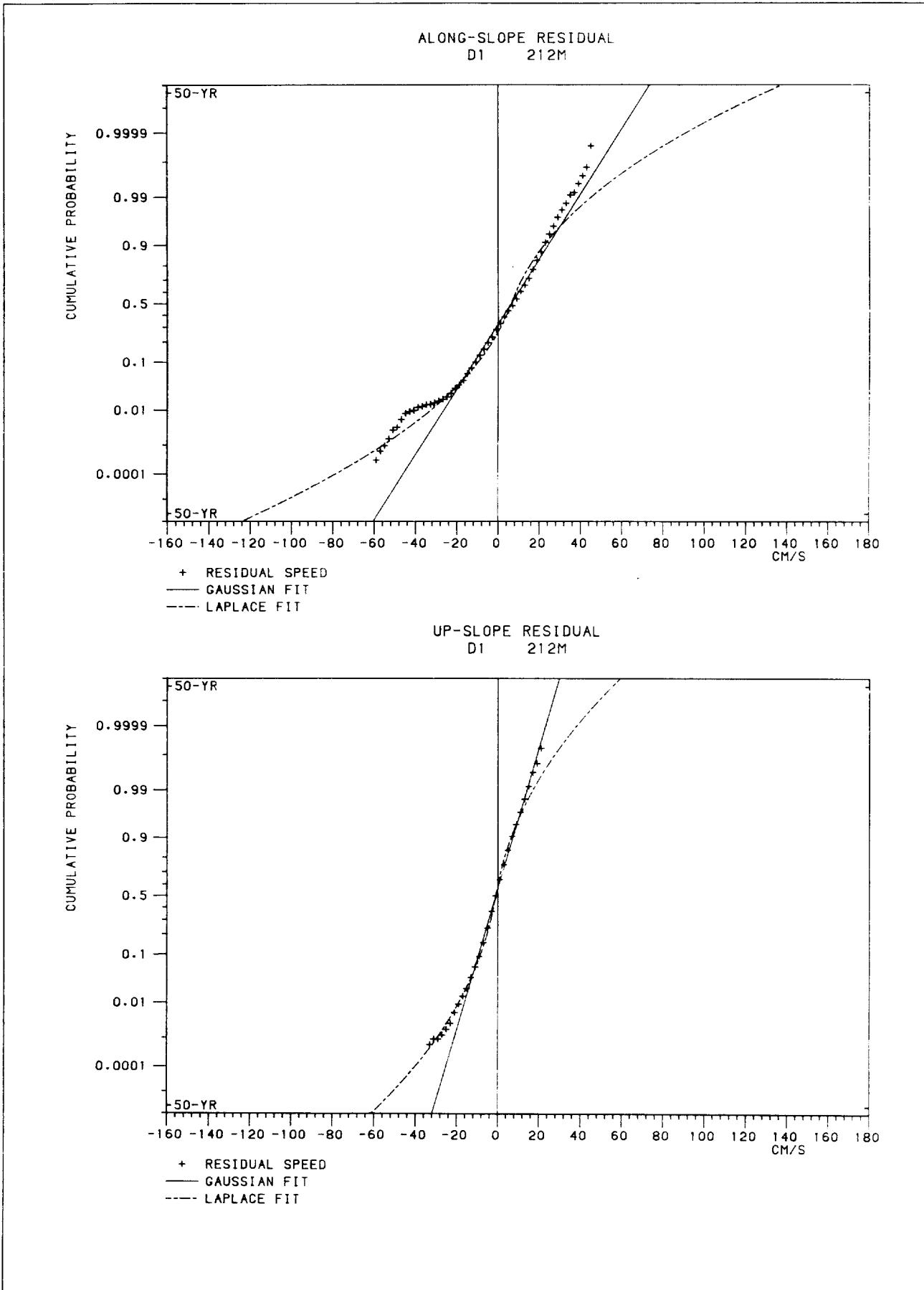


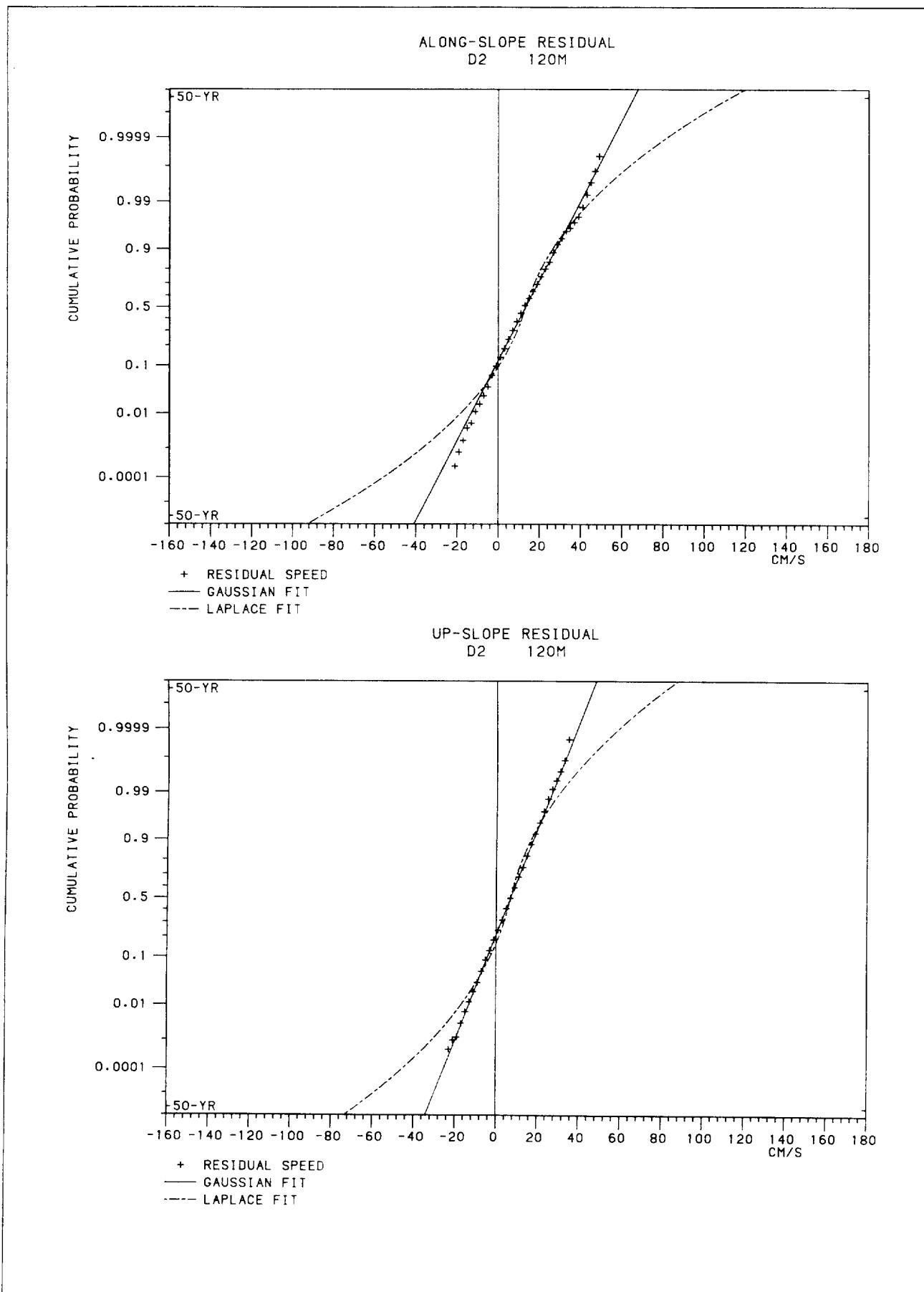


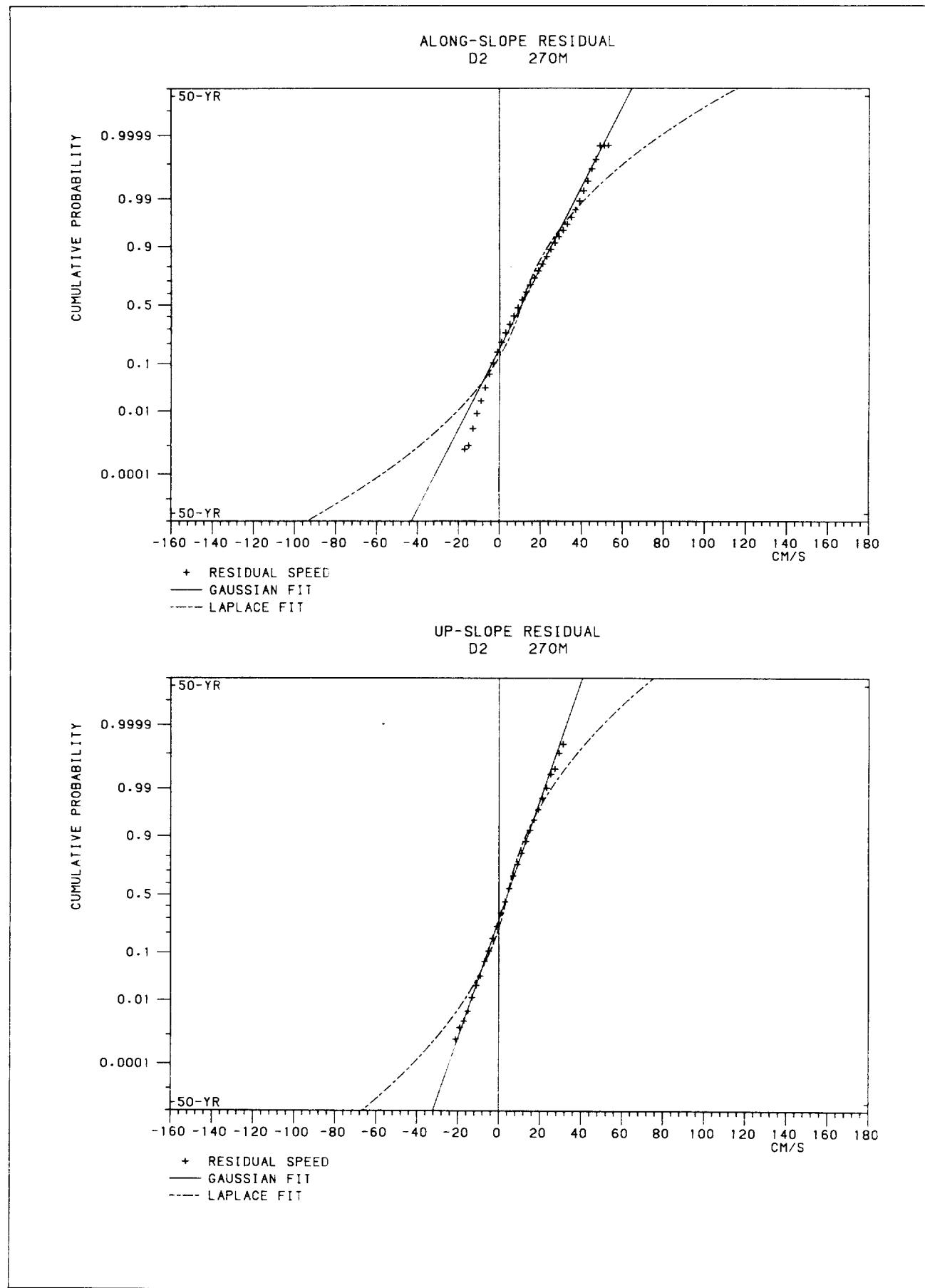


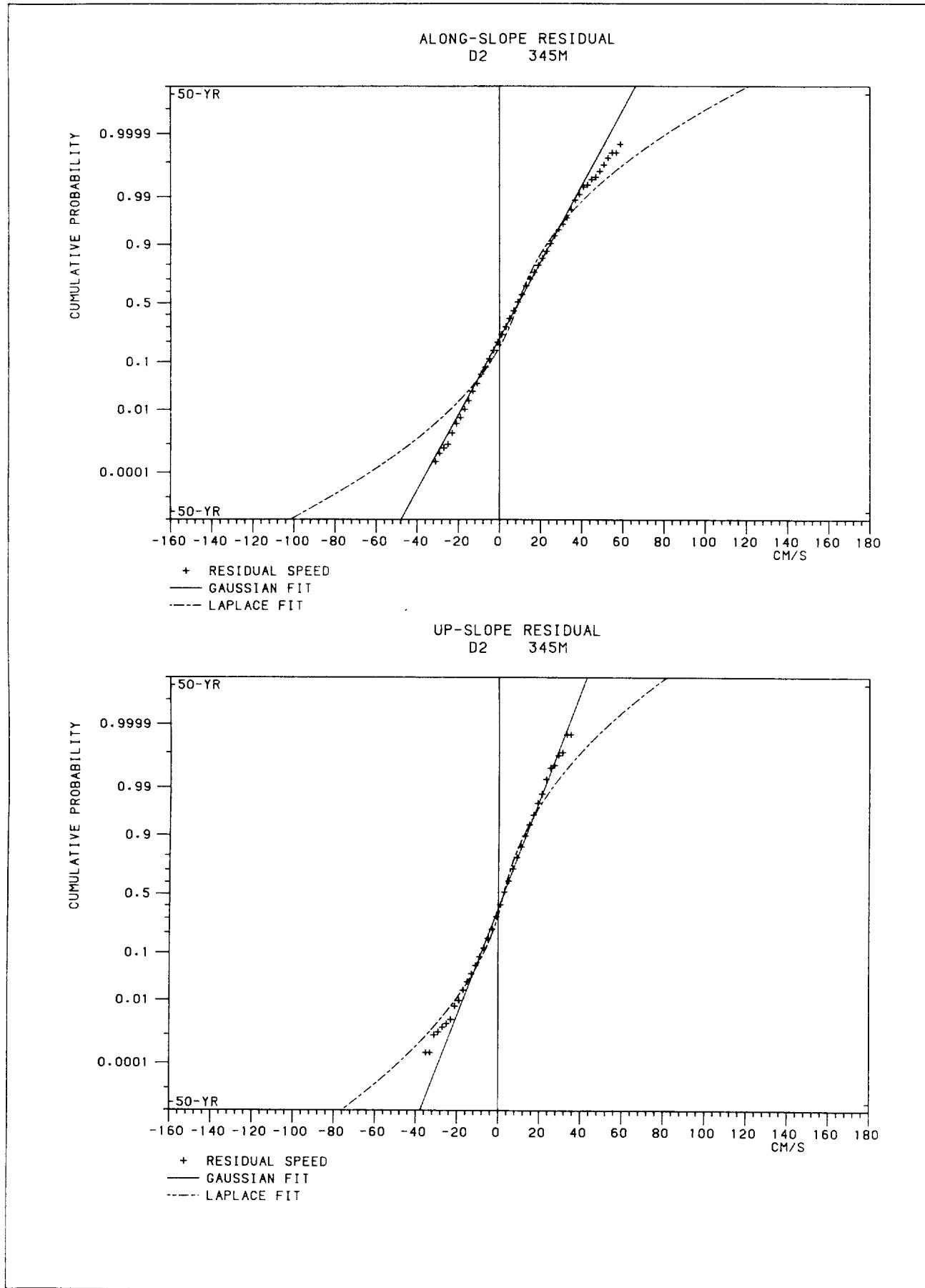


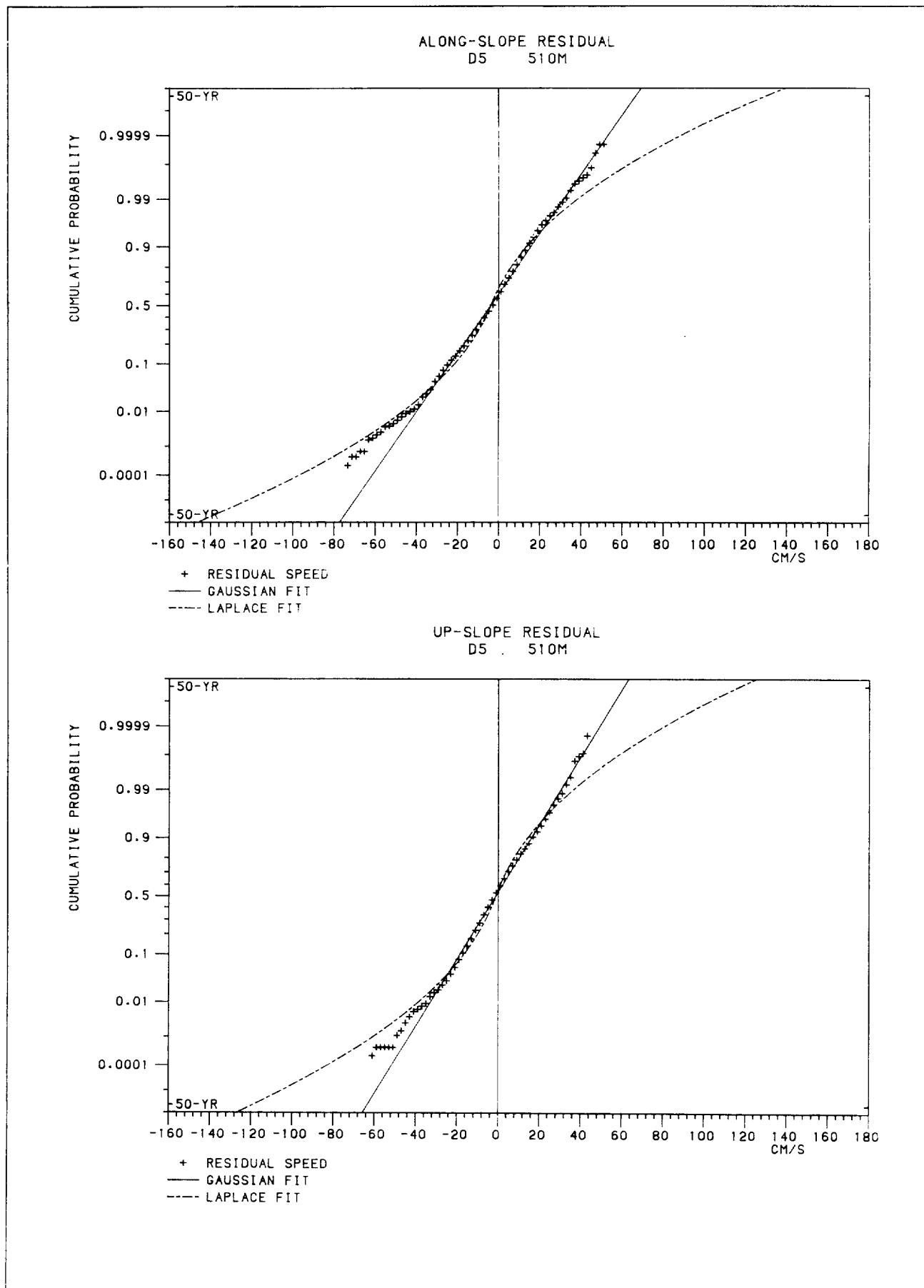


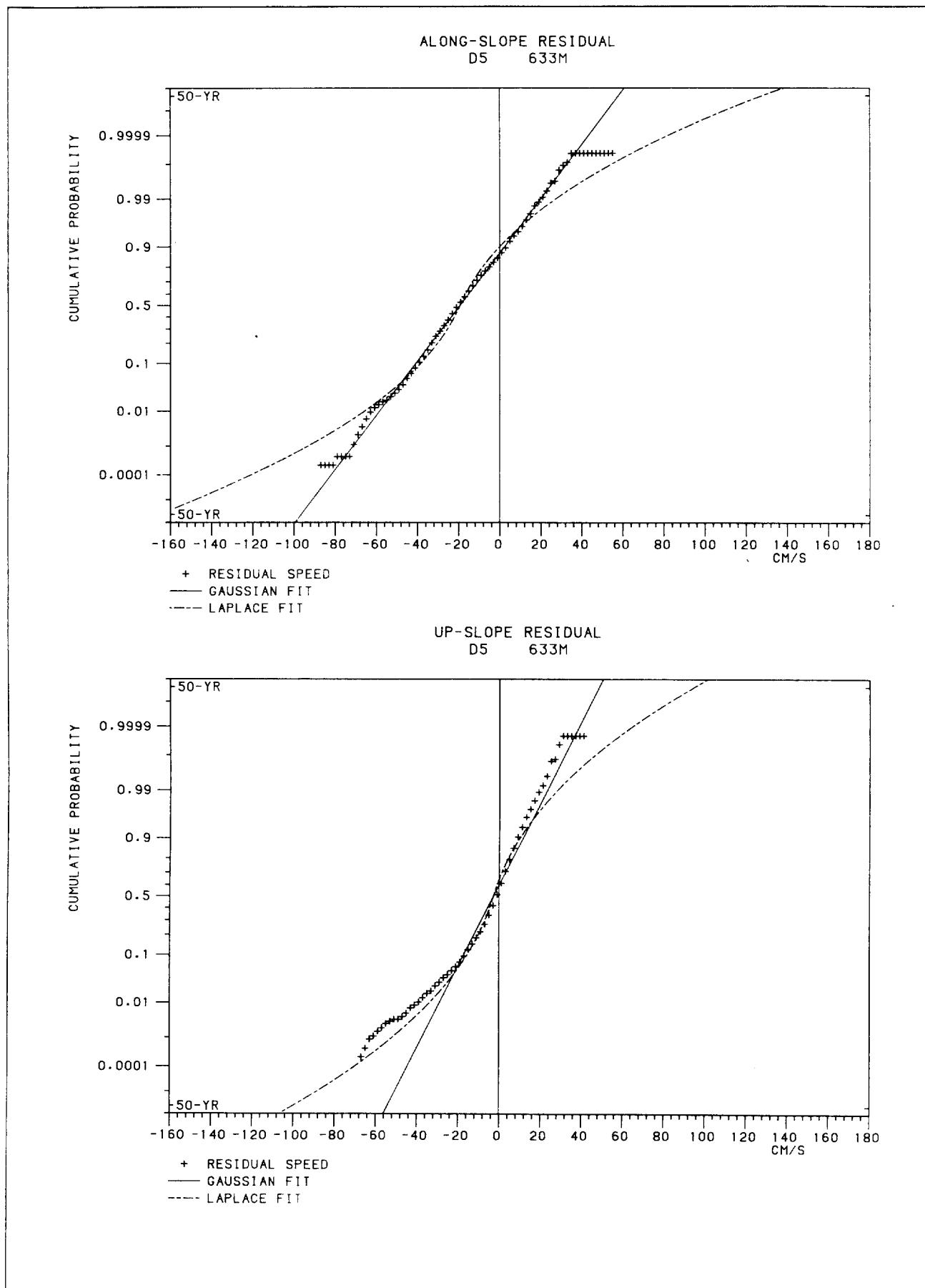


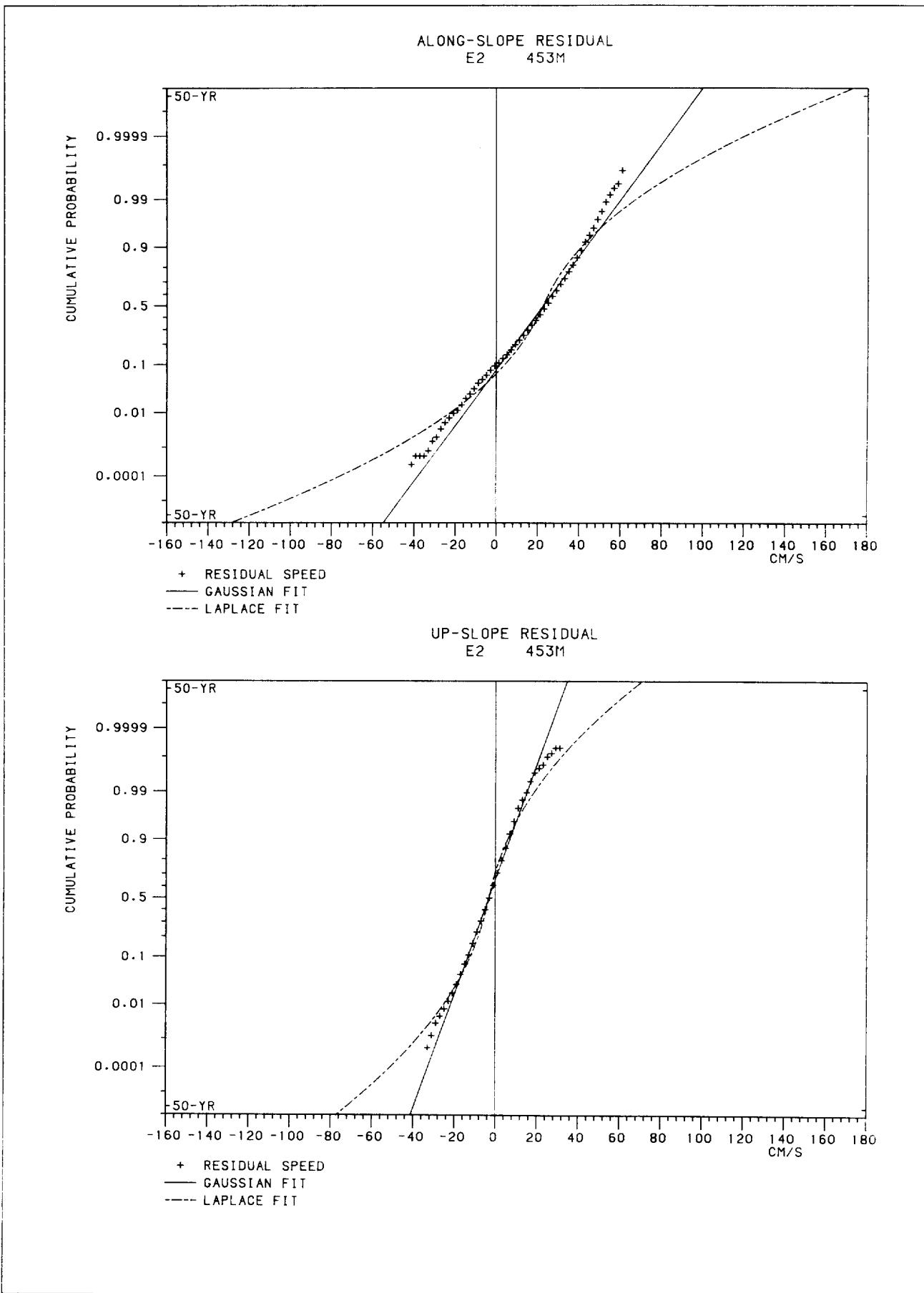


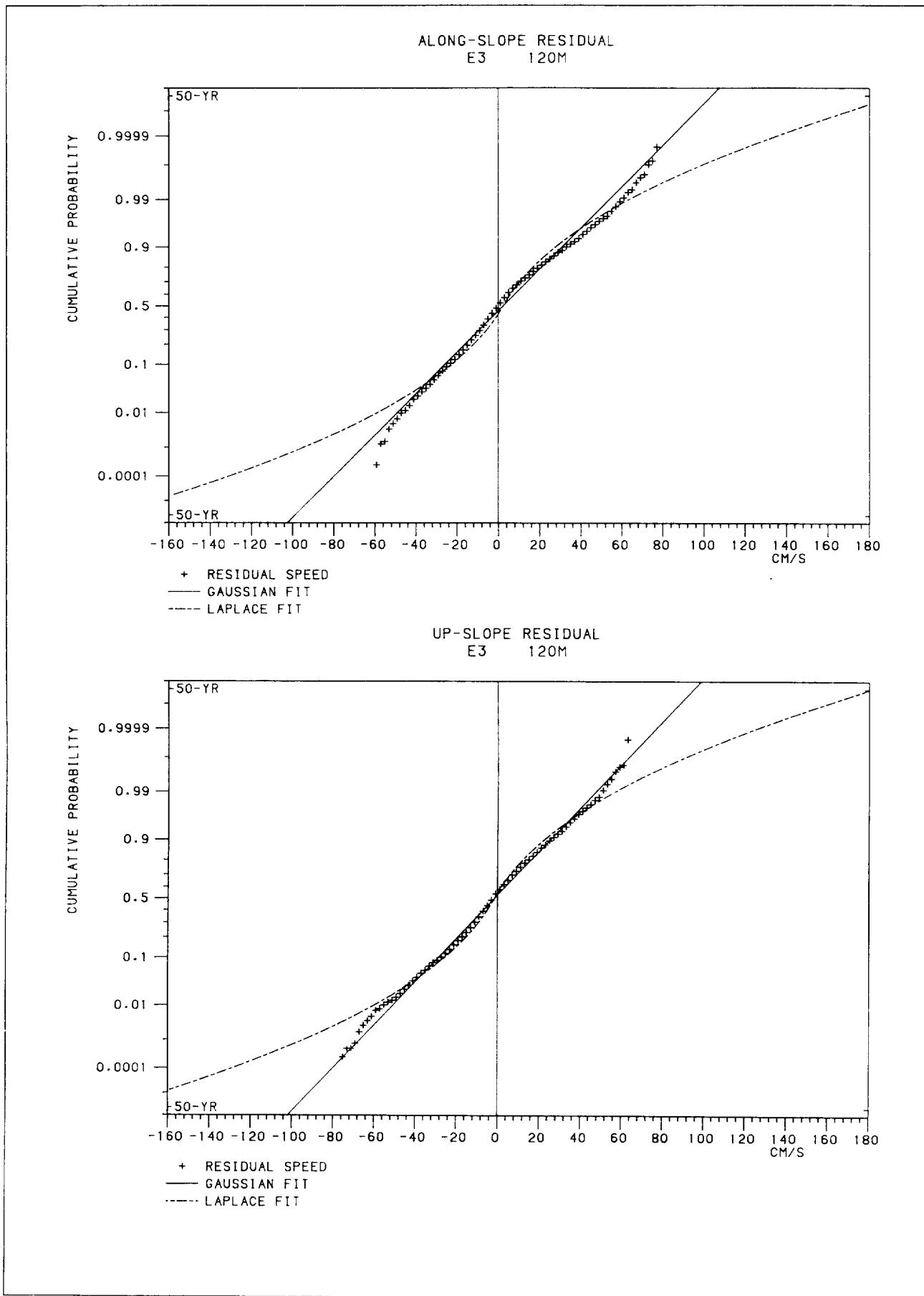


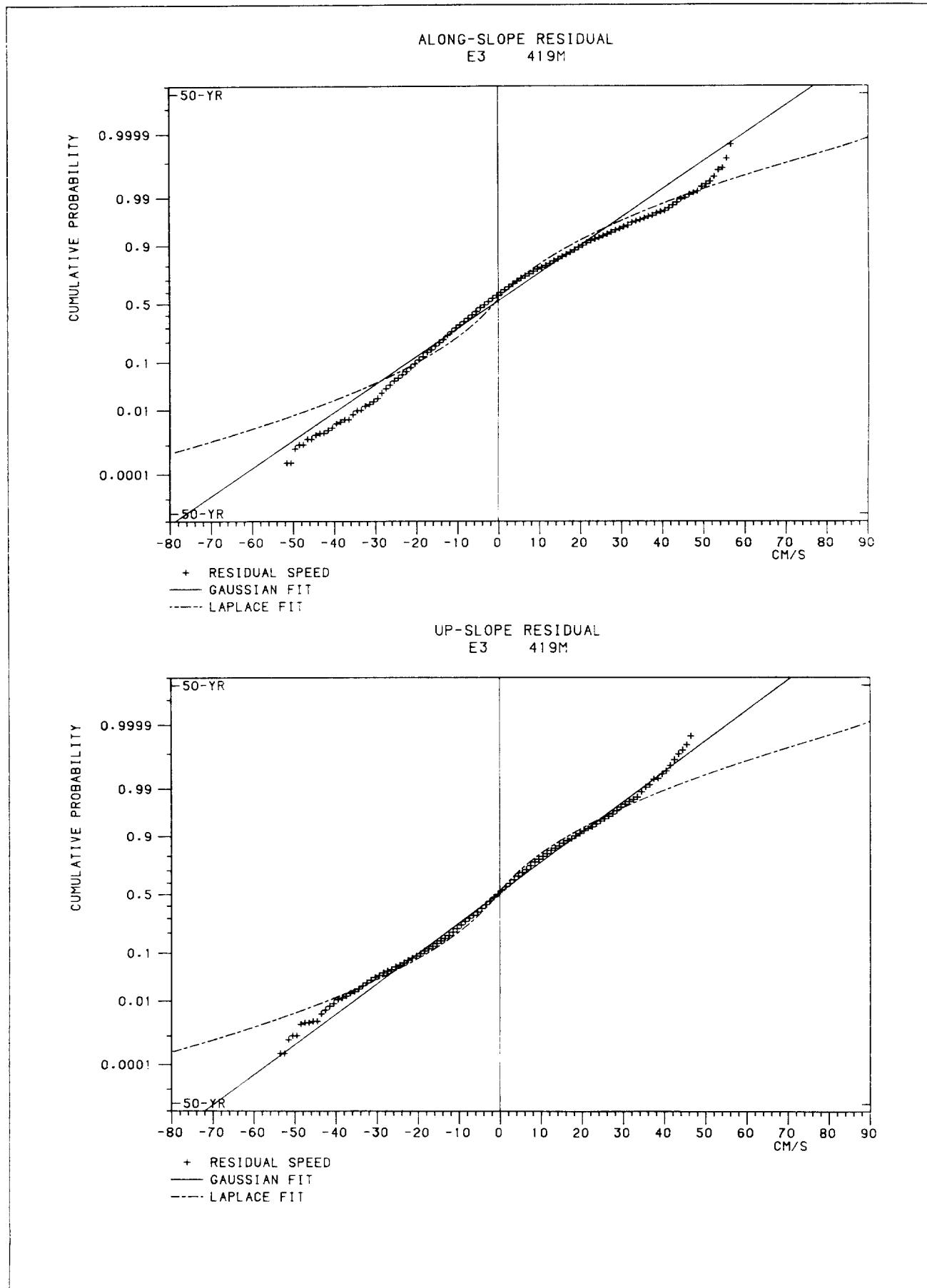


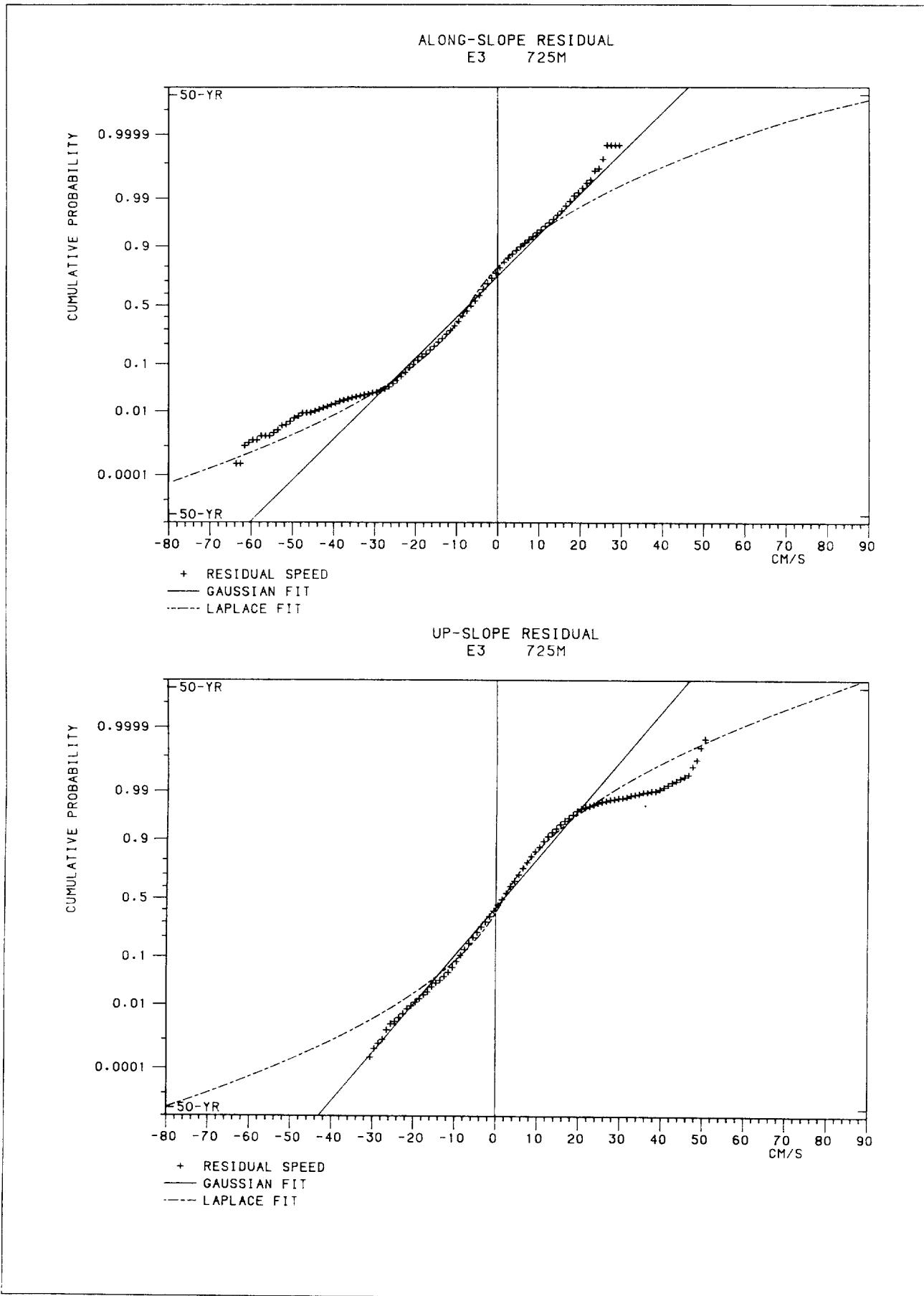


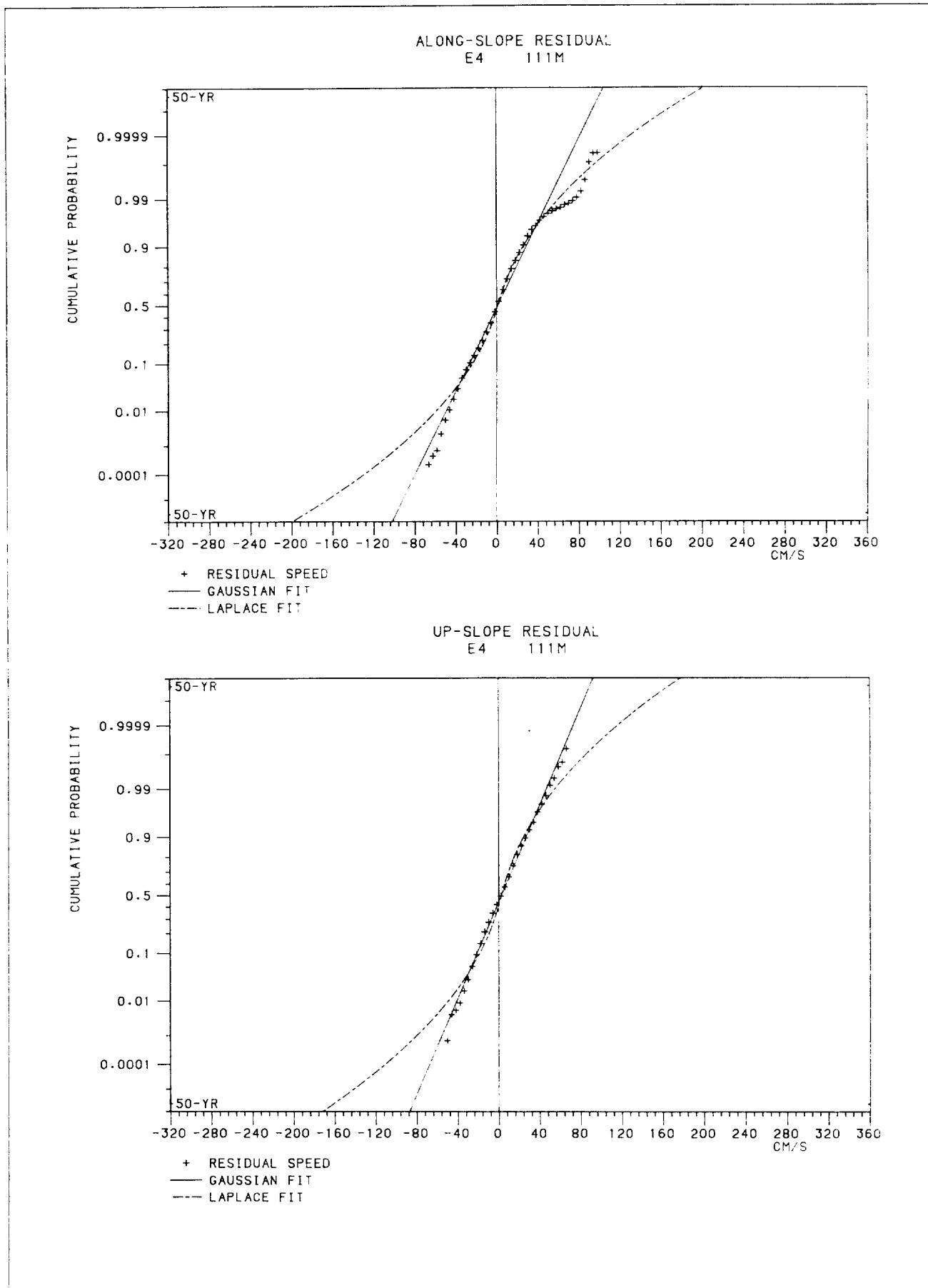


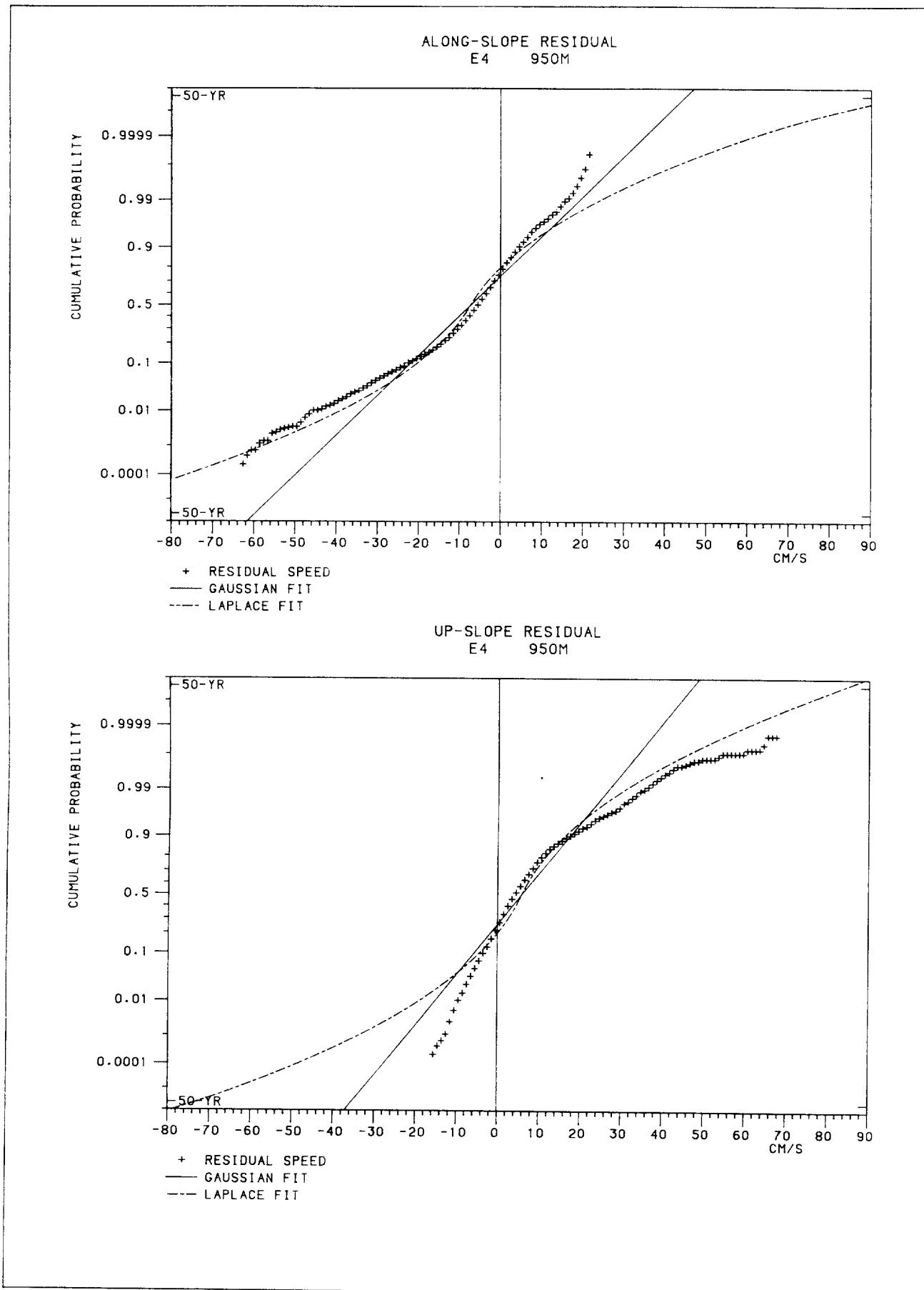




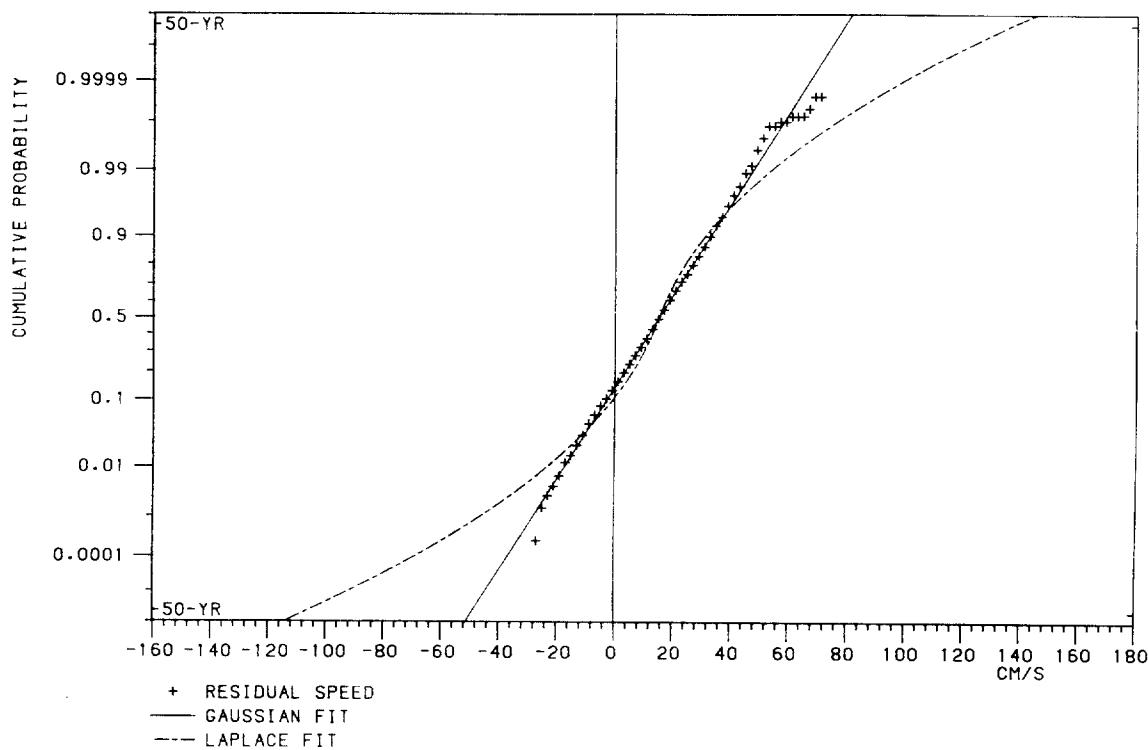




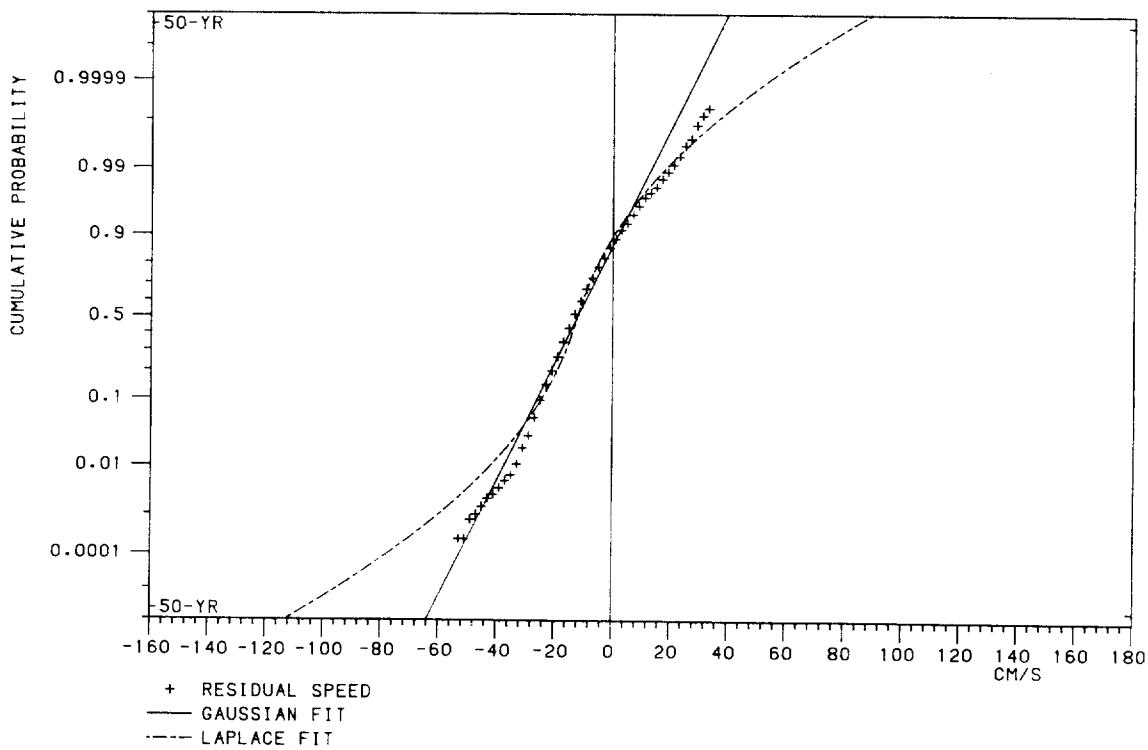


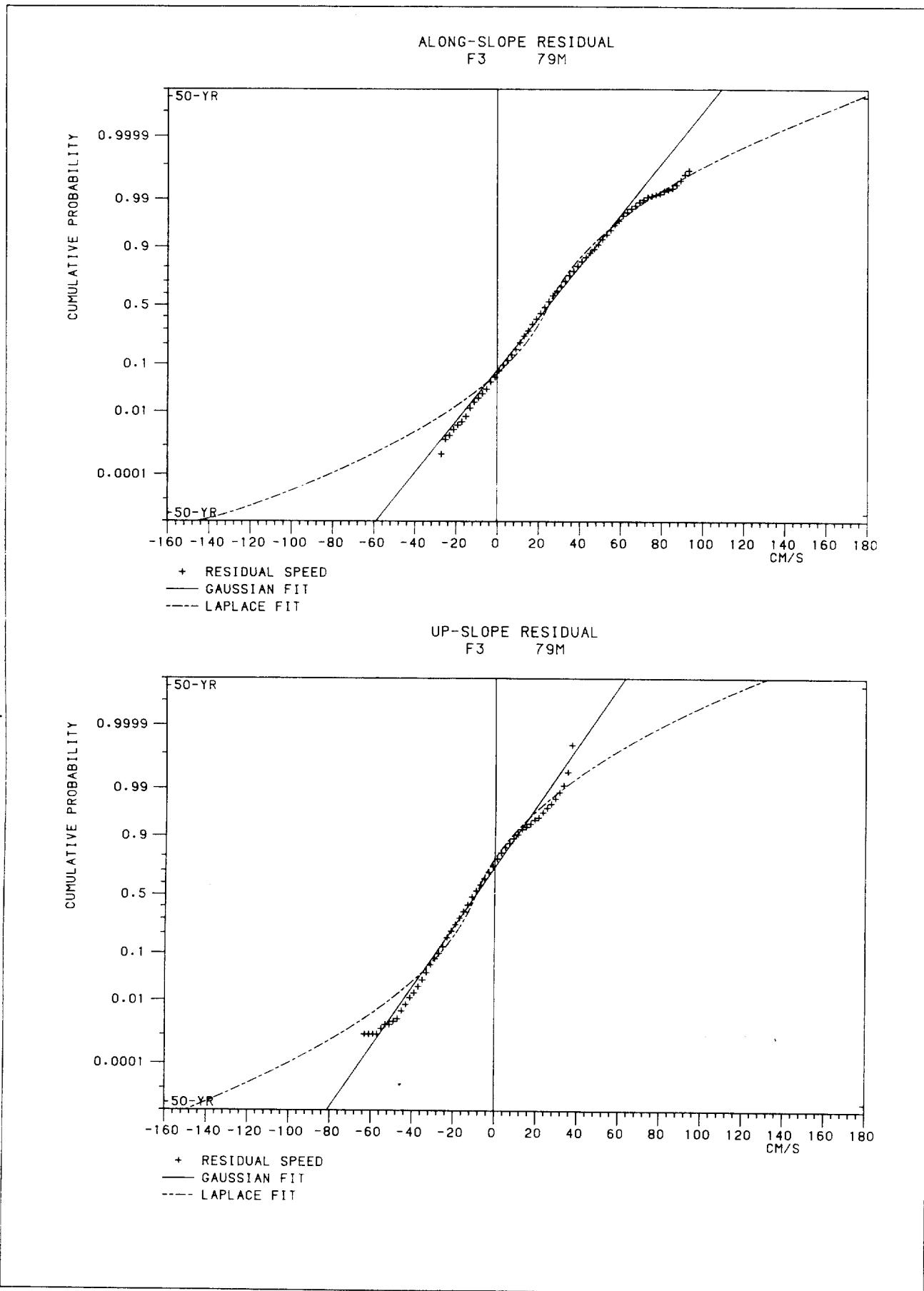


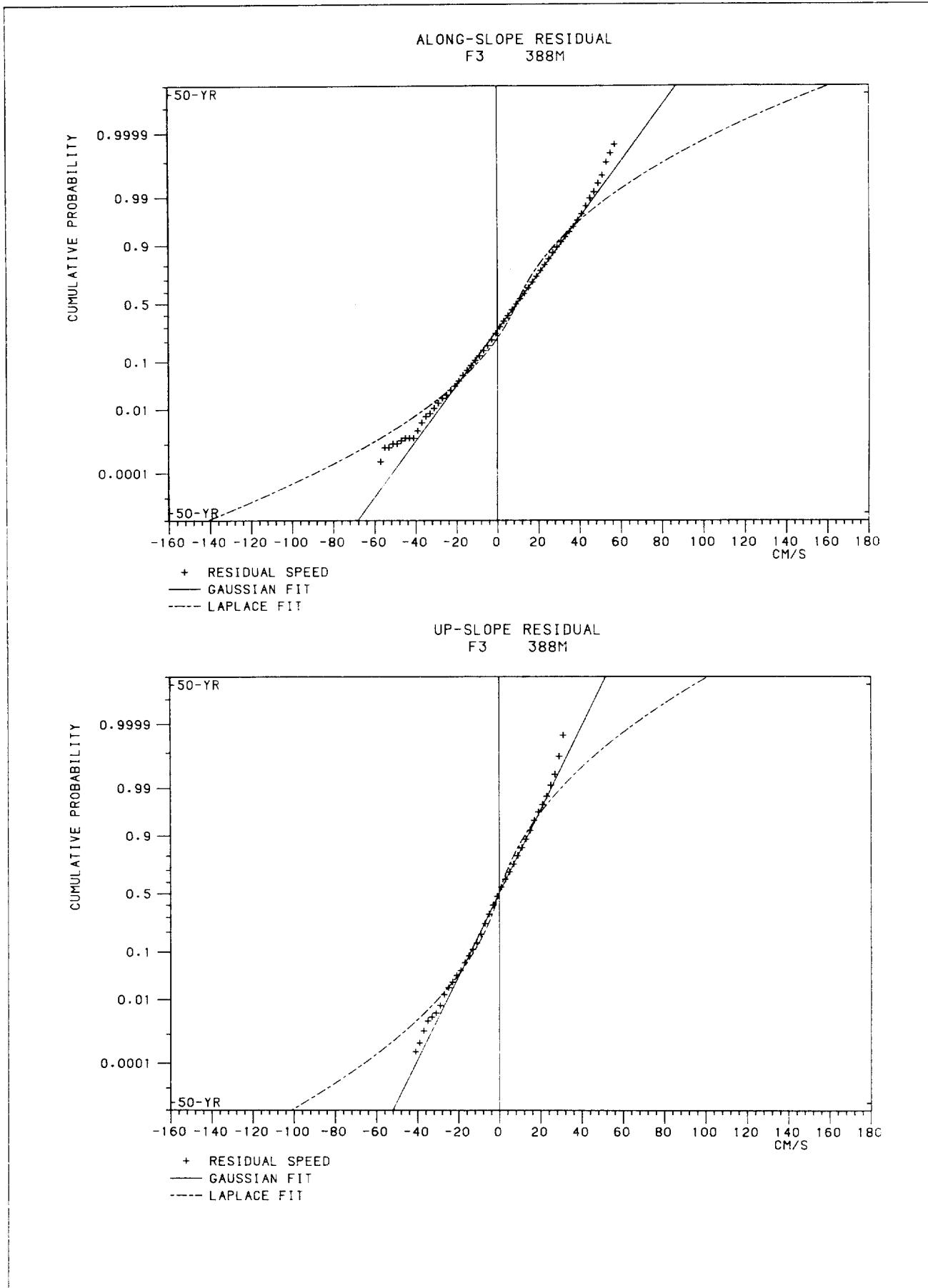
ALONG-SLOPE RESIDUAL
F1 39M

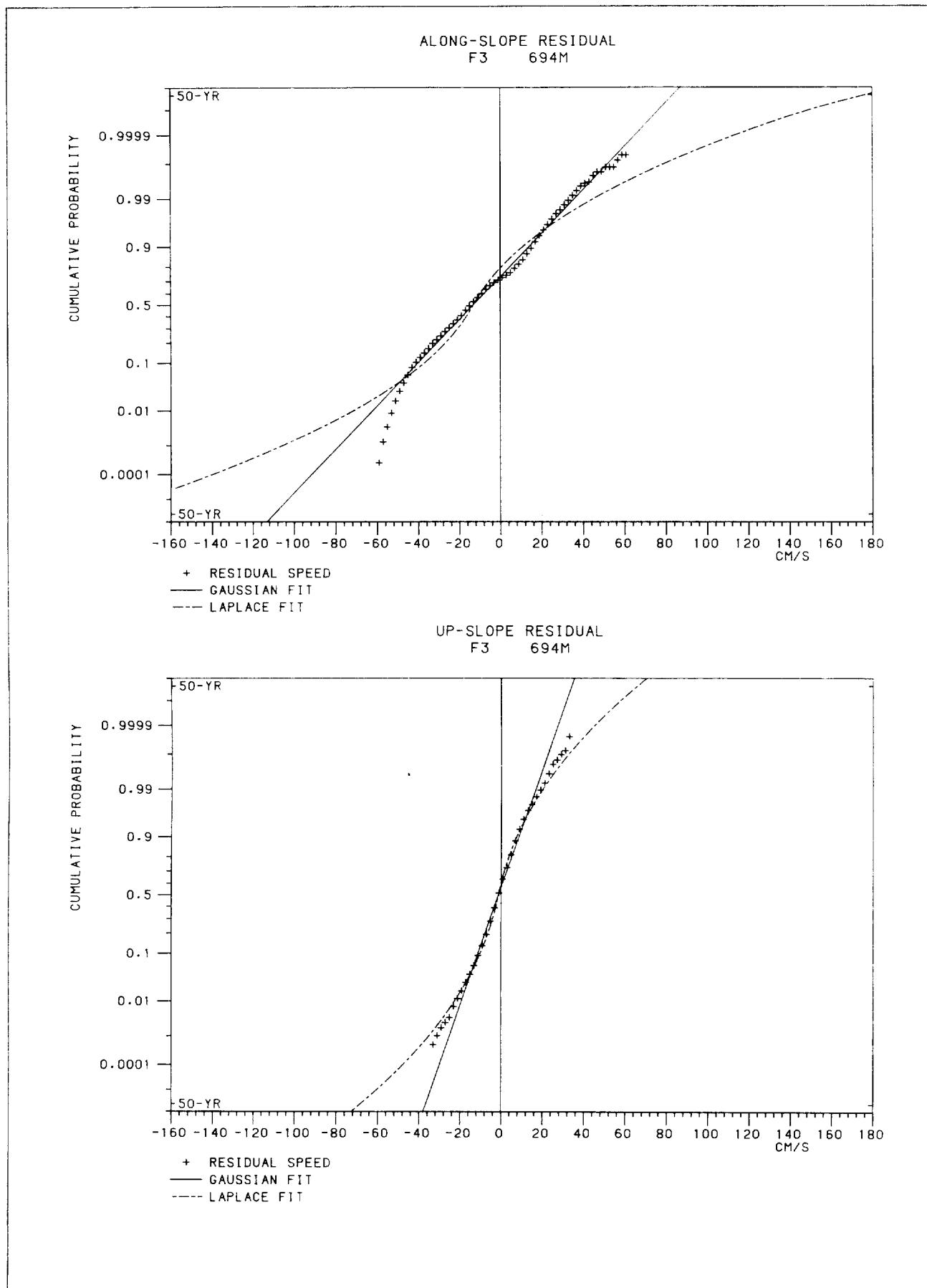


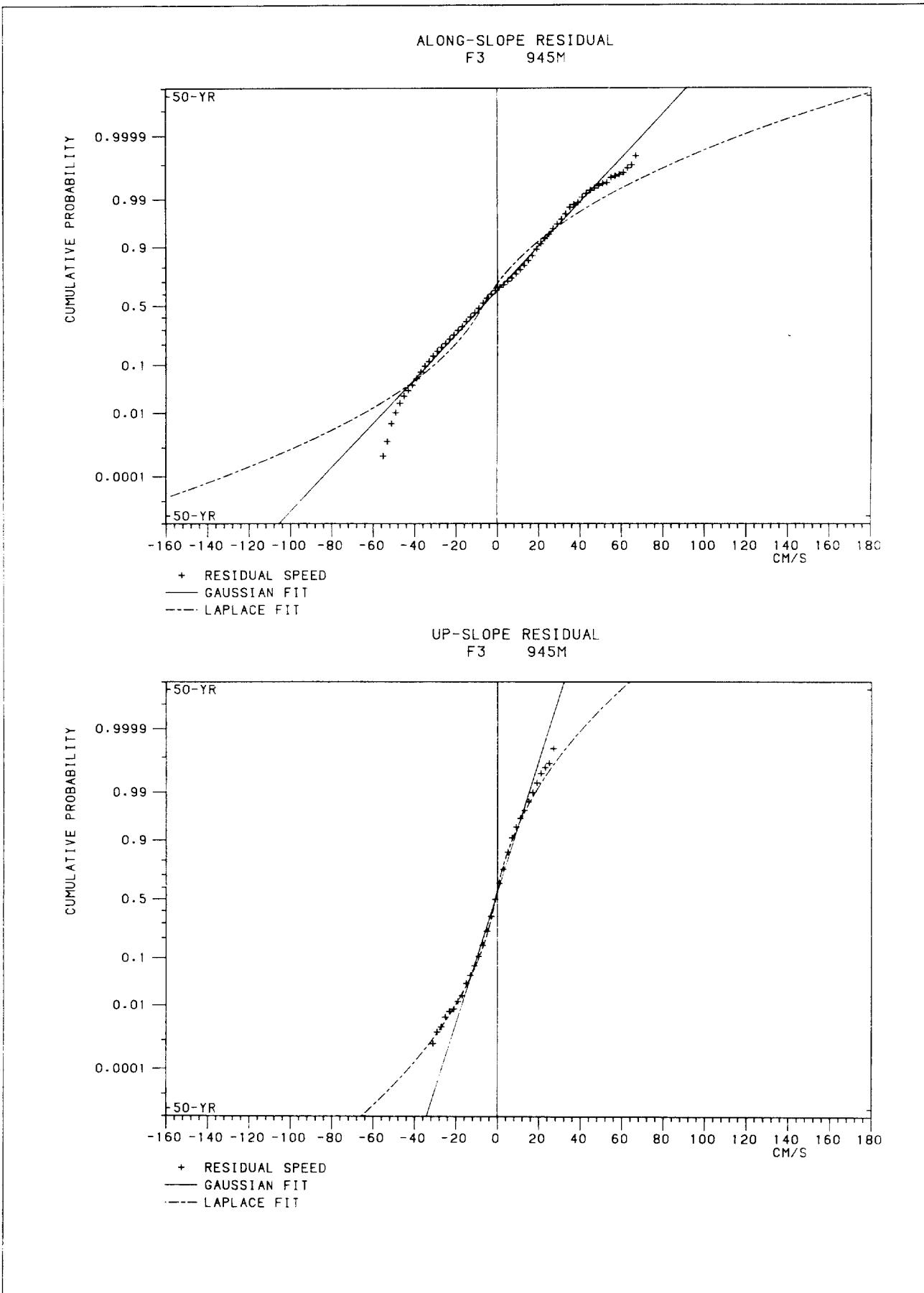
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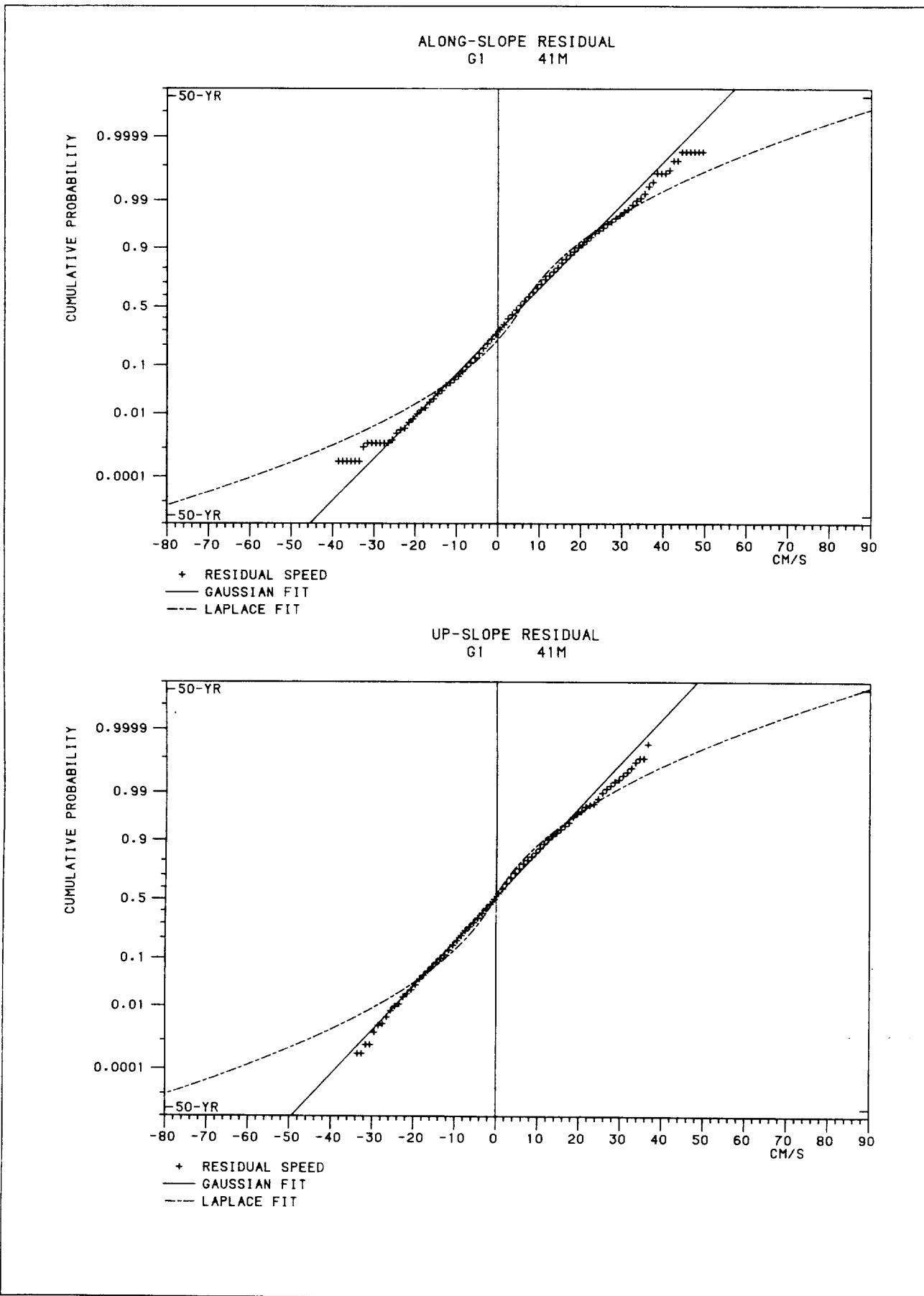


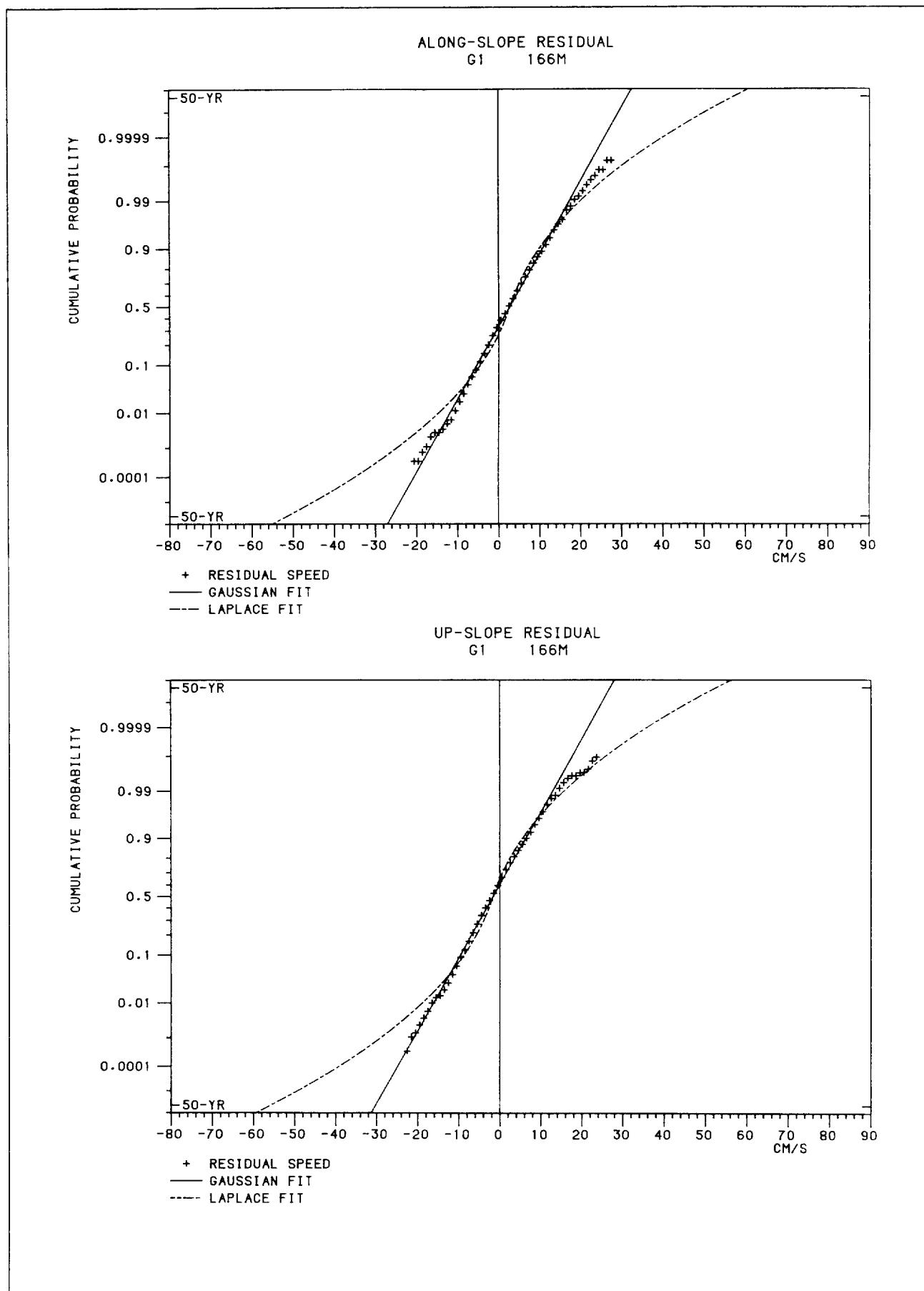


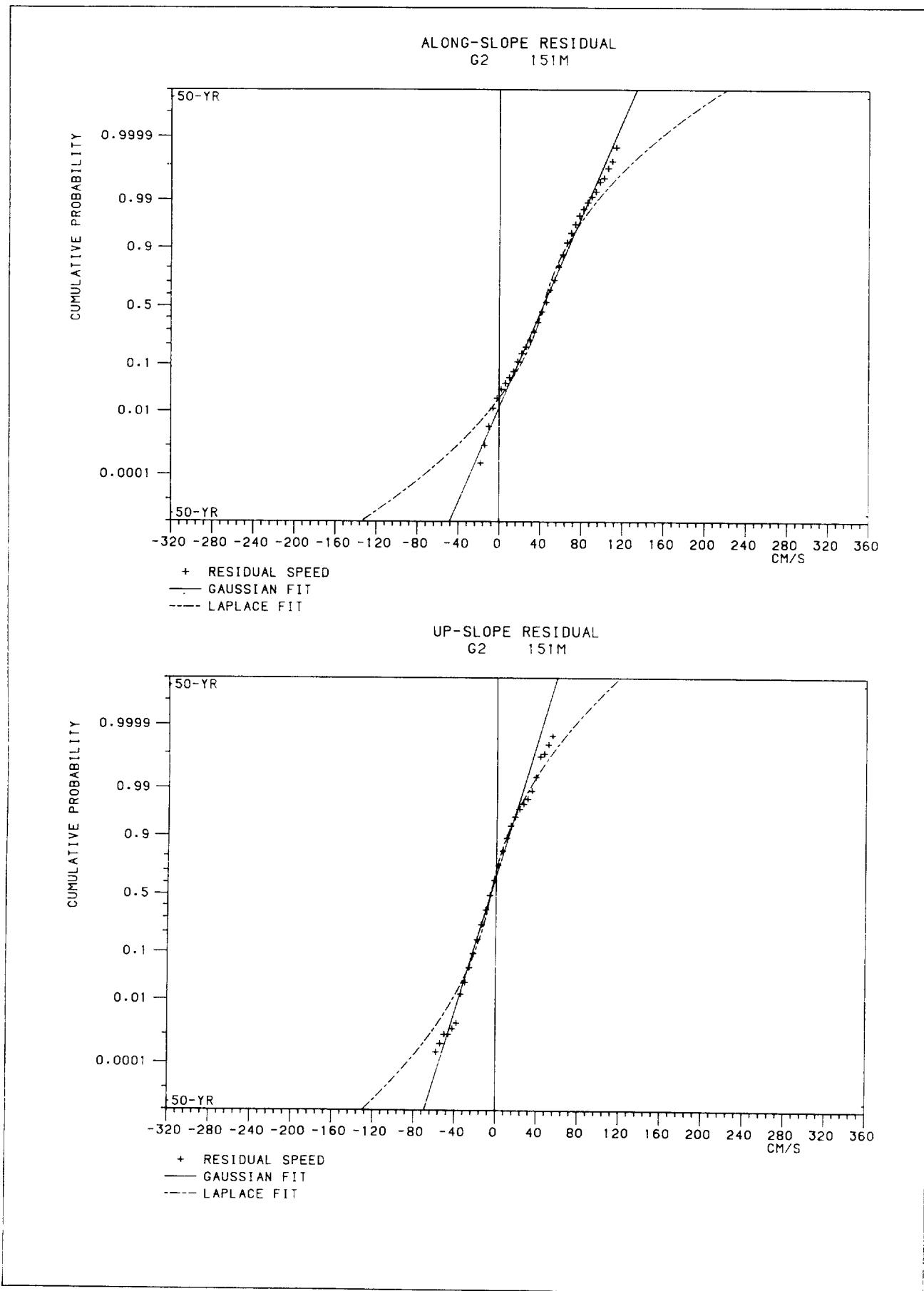


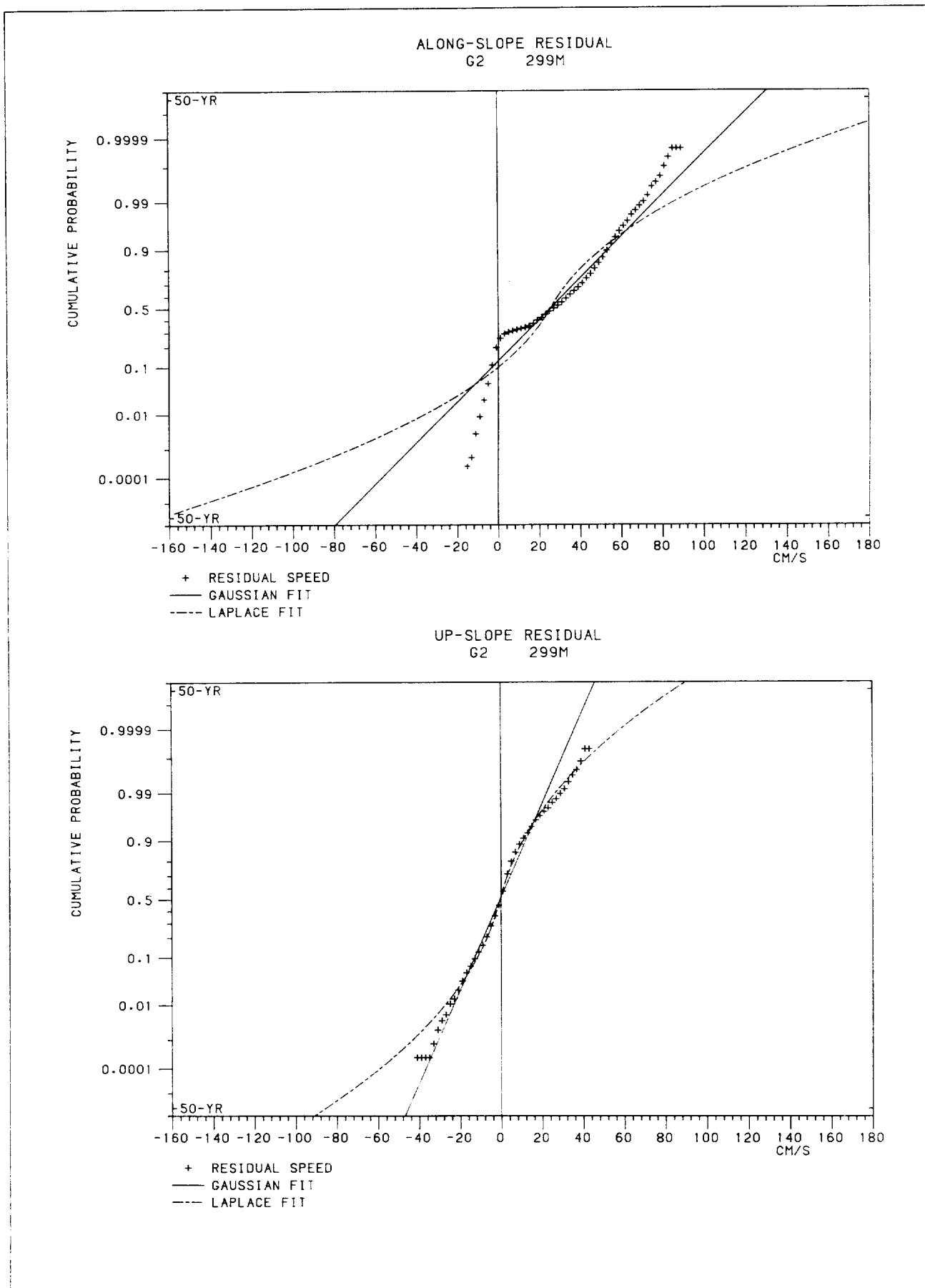


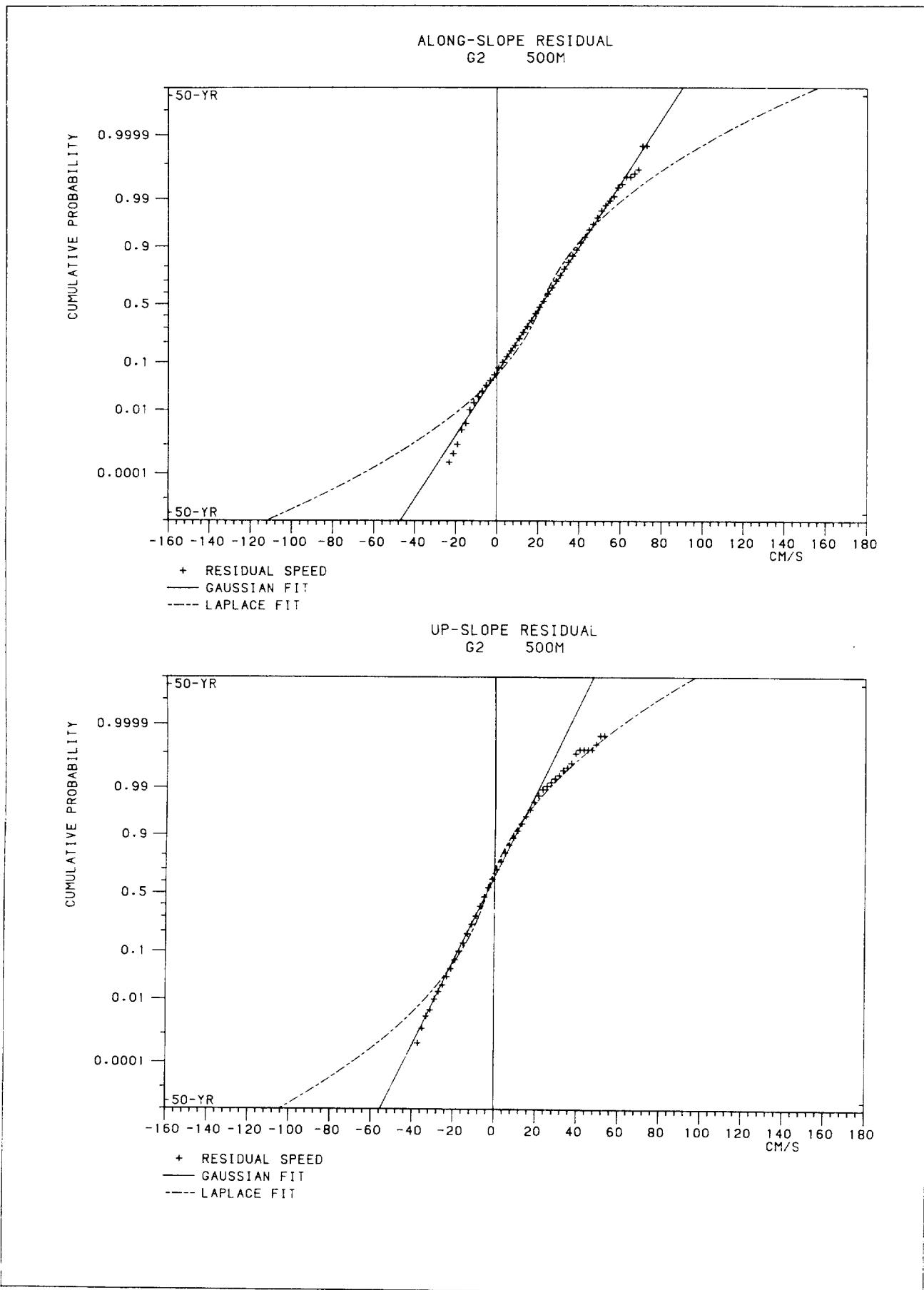


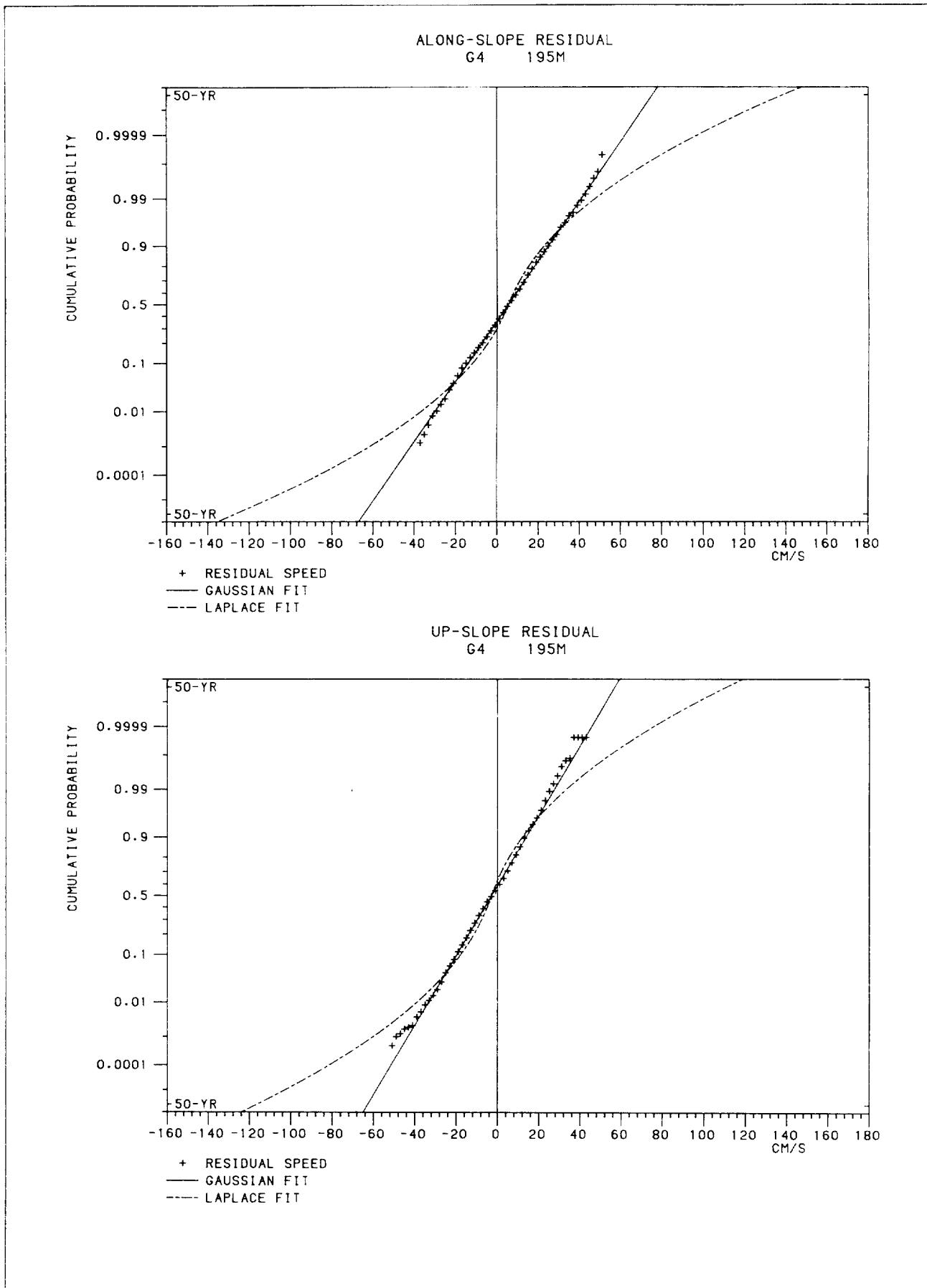


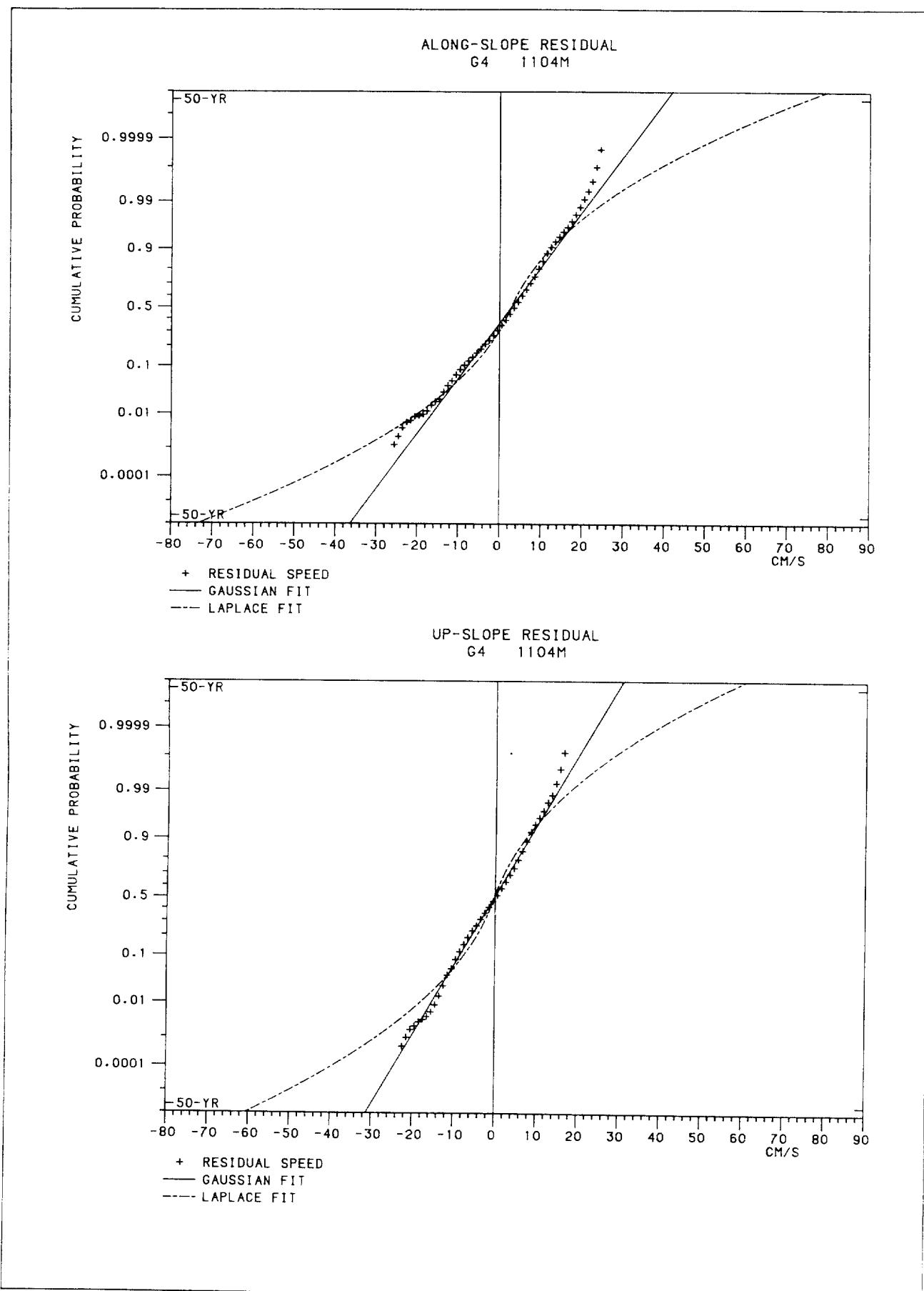


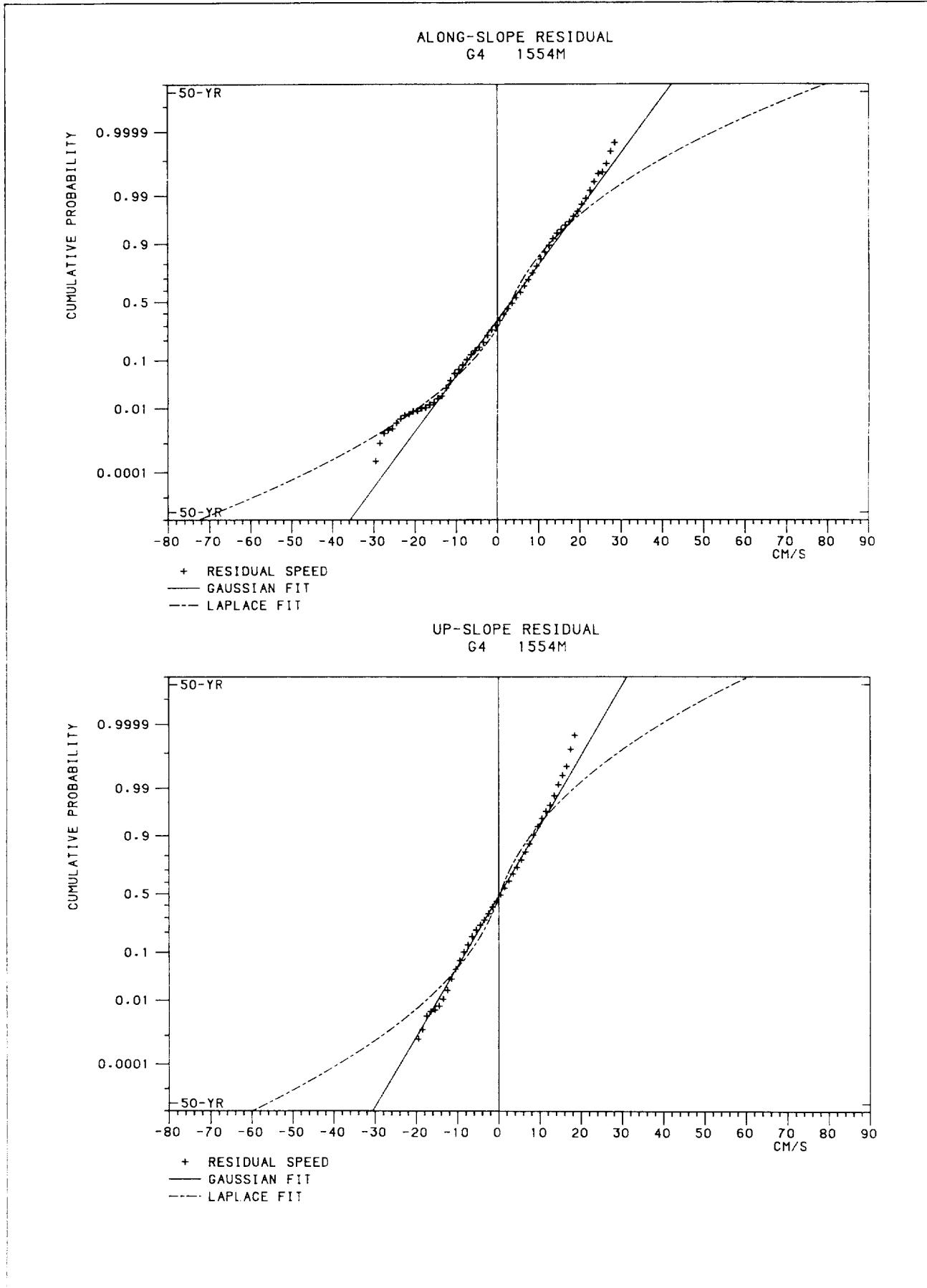


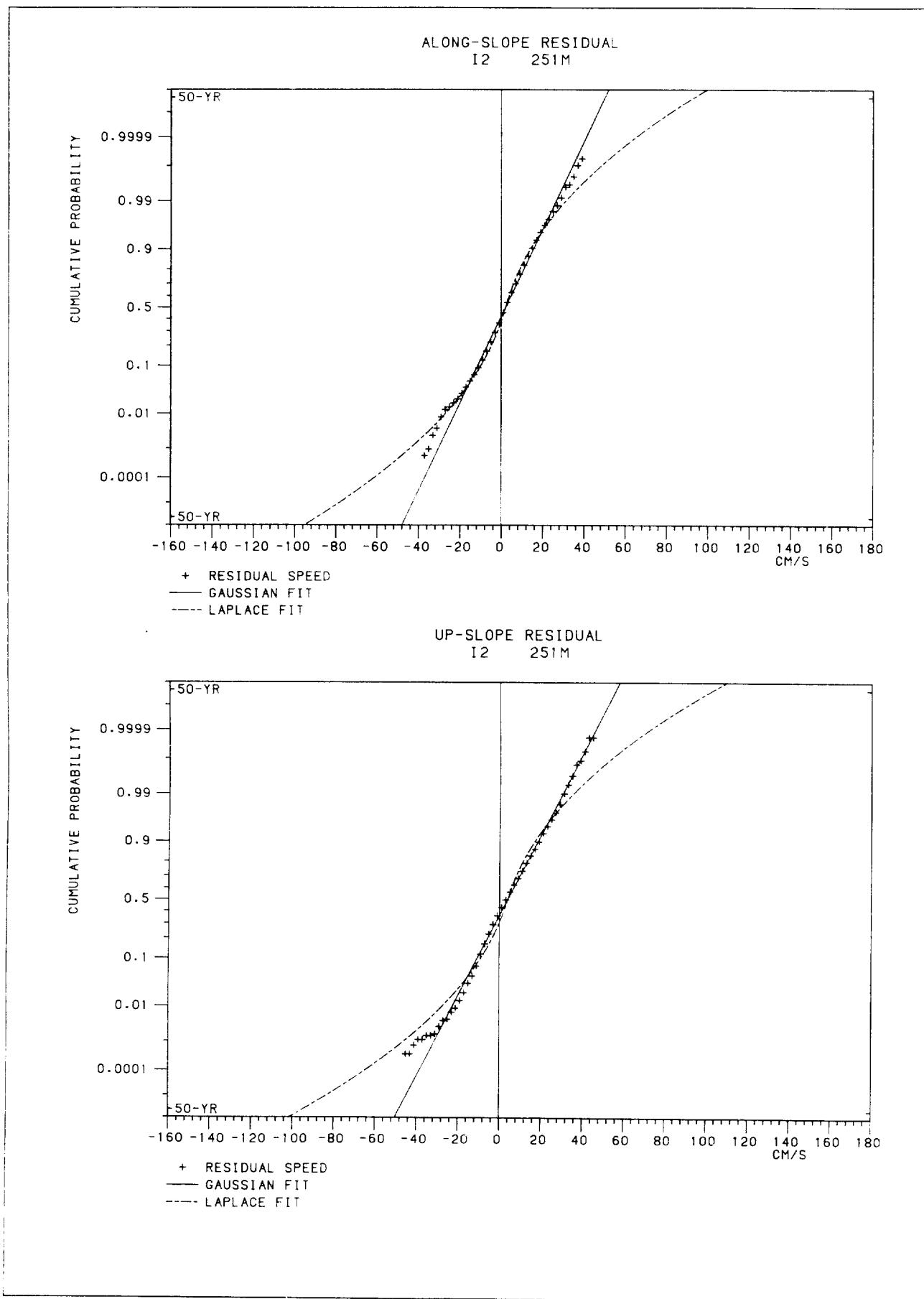


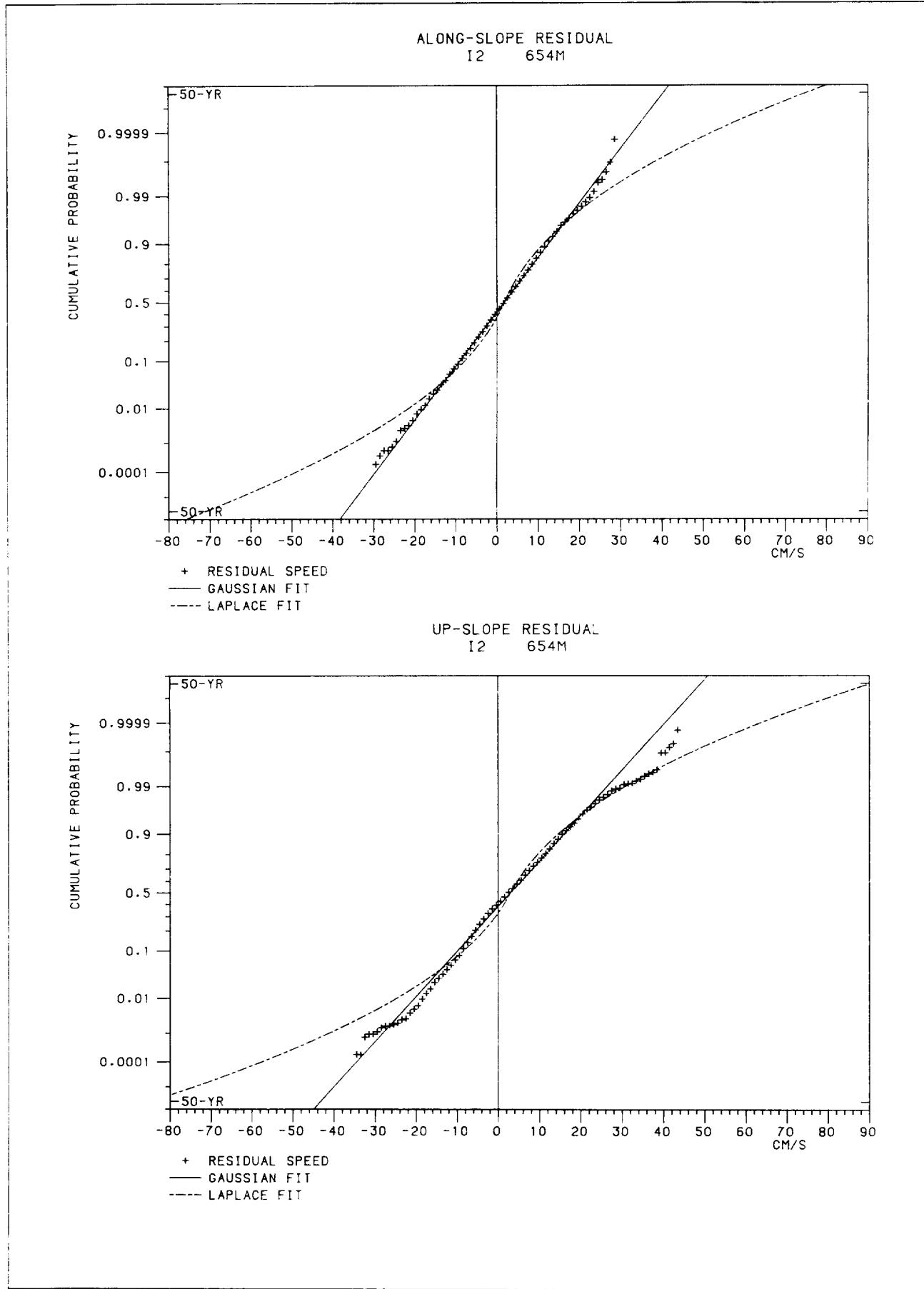


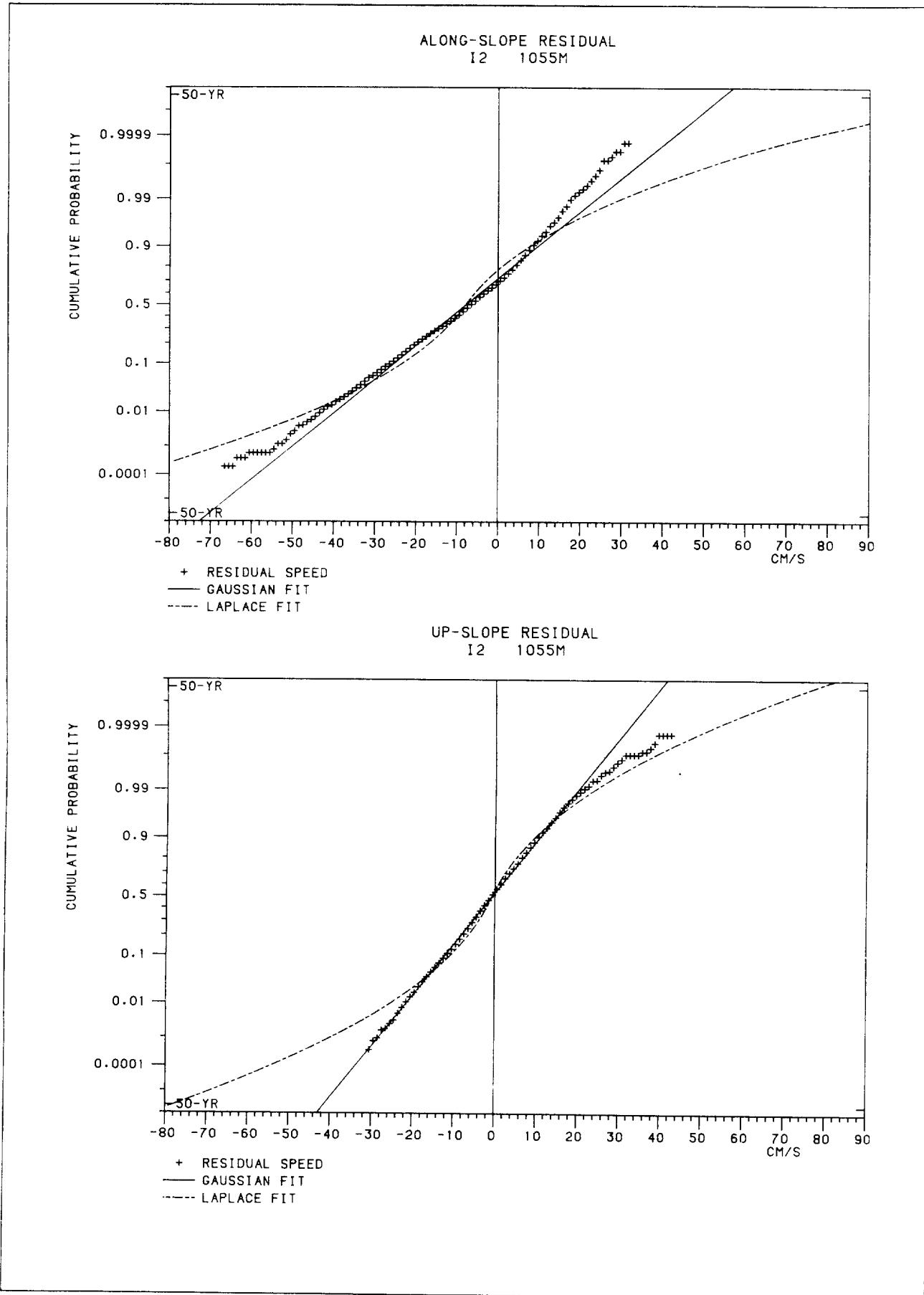












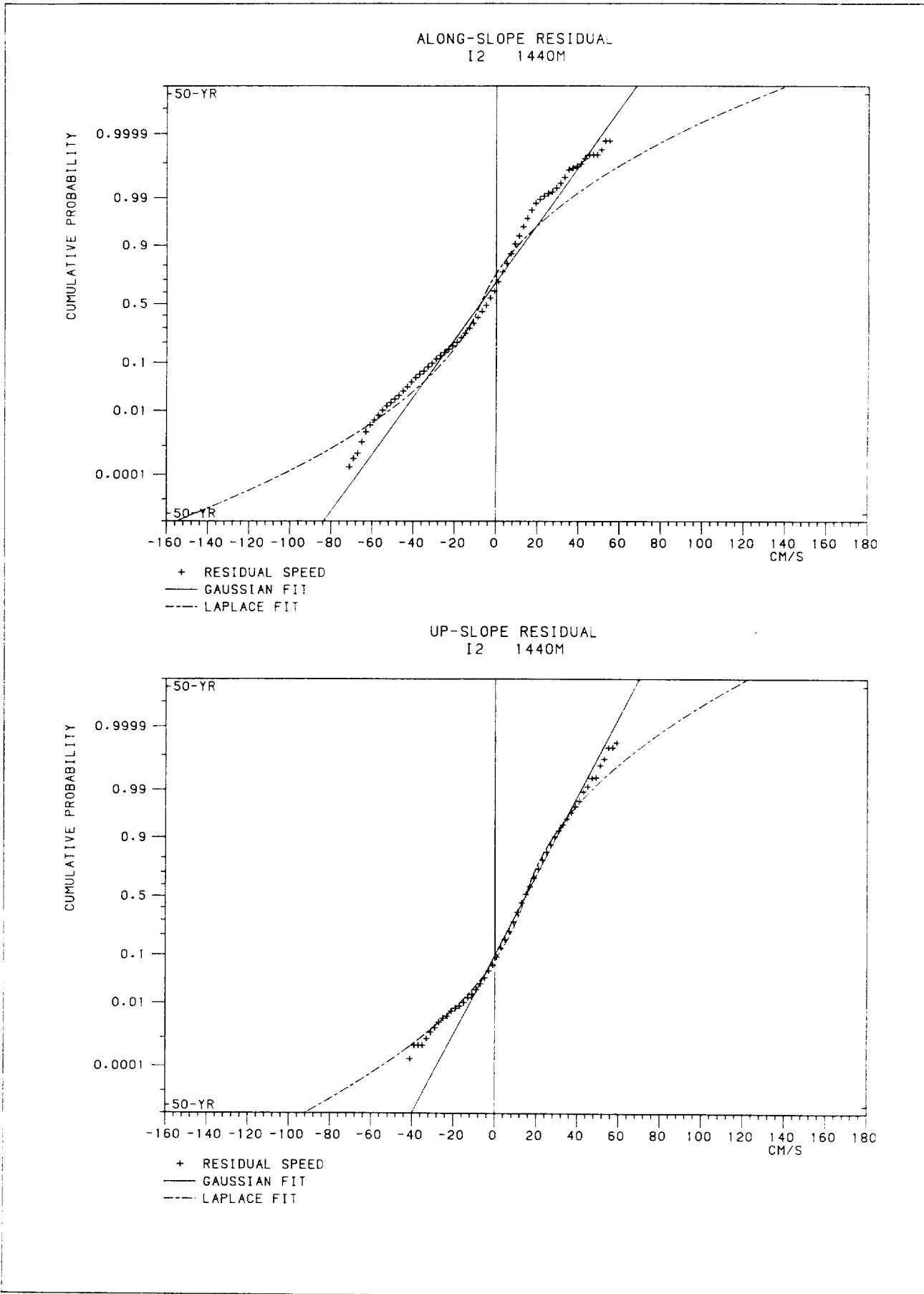


Fig.4: Examples of the joint probability distribution of tidal and residual currents.

