

INVESTIGATION OF STORM SURGES IN THE TORRES STRAIT

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SUMMARY

One year of simultaneous tidal observations from six stations in the Torres Strait have been analysed and in each case 110 harmonic constituents were resolved. analysis showed that tides in this region are mixed i.e. both diurnal and semidiurnal components are strong. For the surge analysis, hourly residuals (observed elevations - tidal predictions) were produced by using the resolved constituents to compute the tidal predictions for the full period of available observations. An examination of the residuals showed that Frederick Point and Twin Island have similar responses to meteorological effects, similarly the response of Booby Island, Goods Island and Turtle Head have common characteristics, but differing from those at Frederick Point and Twin Island. The surges observed at Booby Island, Goods Island and Turtle Head are greater in magnitude and opposite in sign from those observed at Twin Island and Frederick Point. Ince Point sea levels are hardly affected by meteorological effects. It was found that the east-west component of surface winds is mainly responsible for the generation and propagation of surges, whereas winds of velocity less than 12 metres/second have very little effect and are insignificant in the generation of surges. Winds from the west develop positive surges on the west of Ince Point and negative surges on the east of Ince Point while the reverse is true for winds from the east. The north-south line through Ince Point appears to act almost as a barrier. A regression technique was used to develop a system for forecasting surges using meteorological data available from near-by meteorological stations. The method proved to be reasonably satisfactory despite the limitations which were imposed by the meteorological observations. The pressure gradients in space may appear to be small but when the distance between two recording stations is of such a length that a low or high pressure zone can be present in the middle, the apparent gradient is clearly not representative of the mechanism investigated in this paper. Some variations in mean sea level, and damped oscillations of periods 3-4 days were observed. These oscillations were not simply related to any local meteorological effects and are considered to have their origin either in the Indian Ocean to the west, or in the Coral Sea to the east. It is suggested that surges generated outside the Torres Strait may affect surge levels within the Strait both directly due to the associated surge level and indirectly by modulating local surges.

INTRODUCTION

In regions of shallow water such as the Torres Strait the effects of both spatial variation in barometric pressure and direct operation of wind force induce surges of such a magnitude that these become of greater importance than tides for navigational purposes. The observed sea level ζ , measured as the deviation of true sea level from the mean sea level value, at a particular place at any time t can be expressed as;

$$\zeta_{t} = \zeta_{t}^{(T)} + s_{t} + z_{t}$$
 (1.1)

where t is the time,

 $\zeta^{(\mathrm{T})}$ is the tidal component,

- S is the weather induced perturbation 'surge',
- Z is the residual variation which is not accountable in terms of readily measured forces.

The prediction of sea level, therefore requires accurate predicting procedures for both tides and surges. The established methods of predicting tides, the Improved Response method of Munk and Cartwright (1966) and the Extended Harmonic method of Rossiter and Lennon (1968) are both well developed and generally extremely accurate.

Subtracting the tidal component from the observations, equation (1.1) can be rewritten as;

$$R_t = \zeta_t - \zeta_t^{(T)} = S_t + Z_t$$
 (1.2)

where the residual R is composed of surge component and noise.

The principal techniques for surge forecasting are (a) a regression on local barometric pressure gradients, first used by Close (1918) and Doodson (1924); (b) a more elaborate regression technique as developed by Cartwright (1968), related to the Response Method for tides; and (c) numerical models, e.g. Heaps (1969). Numerical models have been shown to be the most comprehensive, because of their flexibility in simulating the dynamics of the ocean system. However, meteorological data, used as input for such numerical models must be specified at the grid points of some predesigned representation which precludes these methods being used in the Torres Strait, where suitable meteorological data is available

only from a small number of stations. A knowledge of surges, tides and currents at boundary points also contributes to the accuracy of modelling results, again a requirement that cannot be met in this study. The Response method computes a response of sea level, known as the admittance function, to the meteorological variables across a wide band of frequencies. This method, operating in the frequency domain has certain advantages because of its ability to assign different weights to different frequency components in any one parameter, but this method also was developed on the basis of data available at some 6-9 points. Additionally, it would require filtering of meteorological data. The regression technique is similar to the response method but applied in time domain. Although it is less developed than other methods it is capable of operating with considerably less meteorological data which in turn can be incorporated from random locations. Close (1918) and Doodson (1924) applied a regression technique to compute the contribution of pressure gradients on daily and monthly sea level means. Lennon (unpublished report on 'Research into storm surges at Avonmouth and Liverpool') used similar techniques and included the effects of local free oscillations in his investigation of surges in the Bristol Channel and Liverpool Bay. This approach proved to be successful in a regional sense for Avonmouth, but did not assist in the prediction of Liverpool surges because it was difficult to establish any single resonance period. Hunt (1972) and Townsend (1975) applied similar regression techniques to the surges on the east coast of Great Britain but with an additional term to account for the effects of 'external surges', that is surges which originate outside the area of investigation. To deal with external surges they included a surge from some distant port as an additional indepednent variable along with the meteorological variables, a technique also used by Cartwright (1968). This process has proved to be fairly successful and is currently used in Great Britain by the Storm Tide Warning Service. It is interesting to note that in the regression formula obtained by Townsend (1975), the external surge has the largest coefficient. However, the concept of 'external surge' is arbitrary.

DATA

The geographical positions of the stations from which sea levels and meteorological observations were available are shown in Figure 1.

Their latitudes, longitudes and recording times are listed in Table 1. The tide gauges for sea level observations were operated by the Department of Transport, Melbourne and simultaneous analogue records spanning over one and a half years were obtained from the middle of July 1974 to the end of 1975. Commonwealth Scientific and Industrial Research Organisations (CSIRO) digitized these analogue records to a resolution of one millimetre, providing final hourly values to an accuracy of ½ 2 cm. There were six gaps, not exceeding 2 or 3 days, when observations were not recorded at Frederick Point. Twin Island records have two gaps each of about 10 days, and Ince Point also has two gaps of 4 and 5 days. Booby Island and Turtle Head records were continuous. However, there were some problems in Goods Island observations due to breakdowns of the tide gauge. These series of observations were checked by CSIRO (details are given in an unpublished report on 'Digitizing of Torres Strait tidal records' by M. Greig, CSIRO) for digitizing errors by comparing each value with a computed level 5 based upon seven point Langrangian interpolation formula with a time interval of one hour,

$$\zeta_{t}^{(c1)} = -0.0049 \zeta_{t-7} + 0.0410 \zeta_{t-5} - 0.1709 \zeta_{t-3} + 0.6836 \zeta_{t-1} + 0.5127 \zeta_{t+1} - 0.0684 \zeta_{t+3} + 0.0068 \zeta_{t+5}$$

and also with computed levels based upon five-point Langrangian interpolations over time intervals of 25 hours and one hour.

$$\zeta_{t}^{(c2)} = 1/6 \left(-\zeta_{t-50} + 4\zeta_{t-25} + 4\zeta_{t+25} - \zeta_{t+50} \right)$$

$$\zeta_{t}^{(c3)} = 1/6 \left(-\zeta_{t-2} + 4\zeta_{t-1} + 4\zeta_{t+1} - \zeta_{t+2} \right)$$

Where the difference $\left|\int_{\mathbf{t}} - \left|\int_{\mathbf{t}}^{(\mathbf{c})}\right|$ exceeded 10 cm., the elevation $\left|\int_{\mathbf{t}}$ was flagged. Any such value would have been corrected only if a genuine error was found after visual examination of the analogue record. Almost simultaneous data sets spanning over a year at each station were analysed at IOS Bidston to resolve 110 harmonic constituents was based on the consideration that the tides, being mixed, could possibly have shallow water constituents of any origin, i.e. diurnal or semi-diurnal. List of constituents and frequencies is given in Table 2. These constituents, once resolved, were used to compute residuals (observed elevations - tidal predictions). The variances of residuals covering the periods of observations, are listed in Table 3. Some exceptionally high tidal oscillations are

observed in Goods Island* residuals, particularly before the breakdown of the tide gauge. This anomaly is not completely resolved but the timing system of the recording device appears to be responsible since the recorded sea levels for that period appeared to be of the correct tidal height. Ince Point residuals have the smallest variance and Booby Island residuals have the largest. The meteorological data were supplied by the Australian and Papua New Guinea Meteorological Offices, and consist of barometric pressures, surface wind speeds and directions, and synoptic charts of north Australia. The observations from the various meteorological stations were recorded at different time intervals. In order to adopt a uniform timing system of three hourly observations, the interpolation of certain data was necessary. In some cases interpolation was not satisfactory because of the many missing values or the unsuitable recording time intervals (e.g. at 9.0 and 15.0 hours only). Meteorological data were tested for exceptionally large errors only. The annual mean of barometric pressures was computed for every station and each series of barometric pressure was adjusted so as to be relative to its annual mean to the least count of 1/10 of a millibar. Surface winds were resolved into two components, a u-component in the east-west direction, and a v-component in the north-south direction. These components were converted into metres/sec. (1 Knot = .51677 metres/sec.) units. The u and v-components were considered as positive when they appear to be coming from the west, and the south respectively. The means and variances of these meteorological variables are listed in Table 4. It should be noted that these statistical functions were computed from recorded values which were not at regular intervals.

Multiple regression technique for the analysis and forecasting of surges

The oceanic system which transforms the meteorological perturbations (input) into storm surges (output) is shown in Figure 2.

^{*} Because of its location this station was highly influenced by NW surge effects.

Shortly after commissioning, the foundations which had been suspect, crumbled and despite repairs the tower tended to vibrate in high winds.

In such a system any surge S_{t} can be expressed in a multi-regression equation as:

$$S_{t} - \overline{S} = \swarrow_{1} (X_{t}^{(1)} - \overline{X^{(1)}}) + \swarrow_{2} (X_{t}^{(2)} - \overline{X^{(2)}}).....$$

$$X^{(1)}, X^{(2)}, \dots \text{ are meteorological variables, such as, barometric pressures or wind speeds from a station.}$$

$$\swarrow_{1}, \swarrow_{2}, \dots \text{ are pregression coefficients for variables } X^{(1)}, X^{(2)}, \dots \text{ respectively.}$$

$$\overline{X^{(1)}}, \overline{X^{(2)}} \dots \text{ are the means of } X^{(1)}, X^{(2)}, \dots \text{ respectively,}$$

$$\overline{S} \dots \text{ is the mean of the residual elevations } (\overline{S} = \overline{R} \text{ as } \overline{Z} = 0)$$

Here the means are computed over the time interval selected to cover the appropriate surge event. The definition of time interval of surge, in a broad sense, is that period during which weather conditions are considered to be favourable to generate a surge of sufficient magnitude, such that the event can readily be isolated from the noise of residuals. The selection of this interval can be highly subjective, particularly in any forecasting procedure, when it is not necessarily true that a surge will in fact arise within what would be considered as locally favourable weather conditions. On the other hand it is relatively easy to define such intervals in past observation and these in turn can vary considerably from surge to surge.

Equation (4.1) may be written as:

$$R_t - \overline{R} = o_1^{\ell} (x_t^{(1)} - \overline{x^{(1)}}) + o_2^{\ell} (x_t^{(2)} - \overline{x^{(2)}}) + \dots + Z_t$$
 (4.2)

In equation (4.2) the response of sea level at a particular place is assumed to be instantaneous. However, in reality, various time delays are expected for the sea level at a station to respond to different meteorological variables from different stations. Thus, by introducing a time lag 7 associated with each variable, it is possible to account for any effective time delay between the occurrence of a particular meteorological event and the manifestation of the associated storm surge.

Equation (4.2) may then be written as,

$$R_{+} - \overline{R} = \propto (X_{t+71}^{(1)} - \overline{X^{(1)}}) + \propto (X_{t+72}^{(2)} - \overline{X^{(2)}}) + \dots + Z_{t}$$
 (4.3)

or

$$R_{t} = A + A \times_{t+7_{1}}^{(1)} + A \times_{t+7_{2}}^{(2)} + \dots + X_{t}^{(2)}$$
(4.3a)

where

$$\underset{0}{\propto} = \overline{R} - (\underset{1}{\sqrt{x^{(1)}}} + \underset{2}{\sqrt{x^{(2)}}} + \dots)$$

giving

$$S_{t} = \int_{0}^{\infty} + \int_{1}^{\infty} X_{t+7_{1}}^{(1)} + \int_{2}^{\infty} X_{t+7_{2}}^{(2)} + \dots$$
 (4.3b)

When the 'noise' term Z_t is neglected from equation (4.3a), we get $\hat{R}_t = S_t$, i.e. the estimate \hat{R}_t of residual R_t should approximate the recorded surge S_t , and furthermore if all possible meteorological parameters are not included in equation (4.3b) (i.e. only finite number of terms are retained in it) then equation (4.3b) gives:

$$\hat{R}_{t} = \hat{S}_{t} = \emptyset + \emptyset X_{t+\tau_{1}}^{(1)} + \dots \emptyset X_{t+\tau_{m}}^{(m)}$$
(4.3c)

where \hat{S}_{t} is a surge estimate or predictable surge.

In equation (4.2) the residual elevations R_1 and meteorological parameters, barometric pressure and wind speed $X^{(1)}$, $X^{(2)}$, ..., are in different units. This creates difficulties in making any comparison between values of the regression coefficients \mathcal{L}_1 , \mathcal{L}_2 , etc. and the selection of criteria for neglecting those meteorological variables to which sea level has little or no response. It is, therefore, useful to convert all these variables into dimensionless quantities by normalising them with respect to their standard deviations. The equations (4.3) and (4.3a) can be rewritten:

$$\frac{R_{t}-R}{s_{p}} = A_{1} \frac{(x_{t+71}^{(1)} - \overline{x^{(1)}})}{s_{1}} + A_{2} \frac{(x_{t+72}^{(2)} - \overline{x^{(2)}})}{s_{2}} + \cdots + Z_{t}$$
 (4.4)

$$\frac{R_{t}}{s_{R}} = A_{0} + A_{1} \frac{X_{t+1}^{(1)}}{s_{1}} + A_{2} \frac{X_{t+1}^{(2)}}{s_{2}} + \dots Z_{t}$$
 (4.4a)

where
$$A_0 = \frac{R}{s_R} - (\frac{A_1}{s_1} \times \frac{(1)}{s_2} + \frac{A_2}{s_2} \times \frac{(2)}{s_2} + \dots$$
 and

 S_R , s_1 , are standard deviations of R, $X^{(1)}$, respectively, it is seen that $\mathcal{L}_1 = A_1 s_R/s_1$, (4.4b) and equation (4.3b) enables one to compute \mathcal{L}_1 's from A's.

Statisticians find preference in equations of type (4.3) and (4.4) which have only m regression coefficients for m independent variables. These equations cannot be used in surge forecasting because the means \overline{R} , $\overline{X}^{(1)}$,, which always vary from one surge to another surge, will be unknown. In analysis, these means are also heavily biased by short and variable duration of surges and introduce some error in regression coefficients. The errors in these regression coefficients can be linearly combined to give A_0 , by rearranging equation (4.4a). For these reasons, it is preferable to use equation (4.4a) with equation (4.4a) for analysis of surges since the means are known, and equations (4.3c) for forecasting, using method described later in this section to estimate

In the time subset (t=0,1,2...N), equation (4.4a) will give a set of N+1 equations (augmenting every meteorological series according to its time lag) which in matrix form, if m variables are included, can be written as:

R = XA + Zwhere R, X and A are transpose of R, X' and A' respectively.

$$\mathbf{X}' = \begin{bmatrix} 1 & 1 & \dots & 1 \\ x_{(1)}^{(1)} & x_{(1)}^{(1)} & \dots & x_{(1)}^{(1)} \\ \frac{\gamma_1}{s_1} & \frac{\gamma_{1+1}}{s_1} & \dots & x_{s_1}^{(1)} \\ x^{(2)} & x^{(2)} & \dots & x^{(1)} \\ \frac{\gamma_2}{s_2} & \frac{\gamma_2}{s_2} & \dots & \frac{\gamma_{2+N}}{s_2} \end{bmatrix} \quad \mathbf{N} \times \mathbf{m} \quad (4.6)$$

$$\mathbf{X}^{(m)} & \mathbf{X}^{(m)} & \dots & \mathbf{X}^{(m)} \\ \frac{\gamma_m}{s_m} & \frac{\gamma_{m+1}}{s_m} & \dots & \frac{\gamma_{m+N}}{s_m} \end{bmatrix}$$

$$\mathbf{R}' = \left(\frac{\frac{R_0}{s_R}}{\frac{1}{s_R}}\right) \frac{\frac{R_1}{s_R}}{\frac{1}{s_R}}$$
 (4.7)

$$\mathbf{A} = \begin{pmatrix} A_0 & A_1 & \dots & A_m \end{pmatrix} \tag{4.8}$$

Since Z is assumed as uncorrelated with the input variables, therefore, the least squares solution of the system of normal equations (4.5), will by minimising the $((R-S)^2)$ give;

$$\mathbf{X}\mathbf{X} \quad \mathbf{A} = \mathbf{X}\mathbf{R} \tag{4.9}$$

$$A = (XX)^{-1}(XR) \tag{4.10}$$

The quality of estimate of A from equation (4.10) depends upon the noise level and the inclusion of all possible meteorological variables which contribute to the surge, however, this is clearly not possible. Equation (4.4b) is used to calculate A from A. In system of equations (4.6), one lag is used for each meteorological variable, but any number of lags which are present can be introduced for each variable by simply inserting additional rows in A and A. Hence equation (4.3c) will give an estimate of residuals or surge (R=S), because of the finite number of input variables.

Application of Multiple Regression techniques

To apply the multiple regression technique to forecast the surges at all Torres Strait stations requires:

- (1) establishing a correlation between high frequency (>0.8 cycles per day) components of surges and meteorological variables.
- (2) subgrouping of stations so that surges at various stations within each subgroup have common characteristics.
- (3) choosing effective meteorological variables (e.g. barometric pressure u-component or v-component of surface wind speed, from various meteorological stations), and
- (4) determining the mean value of each variable which depends upon the selected interval of the surge.

The preliminary study of extreme surges at the various stations, together with the available meteorological data, failed to establish any significant relationships between high frequency components of surge and the corresponding spectral components of meteorological variables. Reference to Figure 3 shows that there are clearly defined peaks at the frequencies of 1, 2 cycles/day in the spectra of meteorological observations, due to the atmospheric tides. The effects of these peaks in weather spectra on sea level must have been accounted for by harmonic constituents of the same frequency as in the tidal analysis. It has been observed that often barometric pressures were not recorded for 12 hours at an interval of one week. Attempts to interpolate these values were not successful because some values before these gaps were also suspicious. This artificial modulation resulted in side peaks which are separated by a period of about one week. However the spectrum of tidal residuals shows that energy is distributed in wide bands across the same frequencies, indicating a complex distribution which precludes the computation of satisfactory regression coefficients with the meteorological events. Cartwright (1968) was able to obtain relationships by prior elimination of the tidal bands. There is no simple relationship between the high frequency regions of sea level residual spectrum and weather spectra if one includes the tidal bands. The meteorological data were filtered to separate both the high and low frequency components and the interaction of these components with the surges was examined by cross correlation techniques. The results established that the high frequency components of meteorological data bore little relationship to a generated surge, but instead, a high correlation existed between a generated surge and the low frequency component of meteorological parameters. This result suggests that the high frequency components of a surge must be mainly due to a tide-surge interaction or some other non-linear mechanism. To further provide the necessary span of meteorological data in a low frequency form it was desirable to "filter" the original digital data by a technique which did not incur the usual setback of filtering processes, namely, the truncation of data at either end of the series. A suitable procedure was found by using the method of least squares to fit a second degree polynomial function to the meteorological data. This function, with a period of 24 hours is used in a stepwise process to compute the necessary low frequency data required. This method also allows one to incorporate any forecast data available for a particular meteorological parameter, and in turn to self-predict these data if the meteorological data is not available. In a "real time" situation an iterative process is required to continuously match (update) the self-predicted meteorological parameters with any new

station forecast of these parameters.

It was possible to sub-divide the six Torres Strait stations into two groups by examining the evidence as indicated in;

- (a) Table 3 of residual variance,
- (b) cross-correlation functions in Figure 4 and,
- (c) filtered components of individual surges in Figure 5a, obtained by applying a low pass filter of response shown in Figure 5b.

One sub-group will consist of Frederick Point and Twin Island and the other sub-group will include Booby Island, Goods Island and Turtle Head. Ince Point behaves in a remarkable way, in that weather effects seem to have very little influence on the sea level there. The surges in each group have common characteristics in that they are almost in phase and can be related, one to another, by an almost constant amplitude ratio. Thus if a surge at one station in a group is predicted, the surges generated at the other stations in that group can be estimated.

In order to determine the regression coefficients, Frederick Point and Booby Island surges were selected because of their high residual variances in the respective groups. Meteorological data (barometric pressure, u-component and v-component of wind) from three stations, Thursday Island, Port Moresby and Willis Island were used as input for the analysis of Frederick Point surges. Initially, each meteorological variable was correlated with the surge individually for a first approximation of the cross-correlations. A simultaneous solution was then sought for regression coefficients using the normal system of equations (4.10). For an optimal solution of the system a slight variation in the time lags obtained by the first approximation was also allowed. For an optimal solution at Frederick Point, the equation (4.3c) assumed the form

$$\hat{S}_{t} = \alpha_{1} x_{t+7_{1}}^{(1)} + \alpha_{2} x_{t+7_{2}}^{(2)} + \alpha_{3} x_{t+7_{3}}^{(3)}$$
(5.1)

where $X^{(1)}$ is the u-component of wind at Thursday Island, $X^{(2)}$ is the u-component of wind at Willis Island and

 $X^{(3)}$ is the v-component of wind at Willis Island.

Other parameters have little or no contribution to the generation of surges. The computed estimates of partial regression coefficients* averaged over the different surges are as follows:

A similar fitting operation was carried out on Booby Island surges with meteorological data from four stations, Thursday Island, Weipa, N.E. Island and Cape Wessel. The regression model was tested with both linear and squared wind speed as input to account for the large magnitude of surges. In this case an optimal solution was achieved when equation (4.3c) assumed the form

$$\hat{S}_{t} = \mathcal{A}_{1} X_{t+7_{1}}^{(1)} + \mathcal{A}_{2} X_{t+7_{2}}^{(2)}$$
(5.2)

where $X^{(1)} = U_1 \cdot W_1$, U_1 is u-component of wind speed W_1 at Thursday Island, $X^{(2)} = U_2 \cdot W_2$, U_2 is u-component of wind speed W_2 at Cape Wessel, $C_1 = 0.0014$ $C_2 = 0.0018$ $C_3 = 0.0018$

Equations (5.1) and (5.2) show that surges at Frederick Point are linearly proportional to wind speed whereas surges at Booby Island are proportional to the square of the wind speed, but in both cases the major contribution arises from the east-west wind. The forecast surges based on equations (5.1) and (5.2) are shown in Figures 6a and 6b. It is worth noting that the constant \mathcal{L}_0 as defined in equation (4.3c) is not given in equations (5.1) and (5.2). During the analyses of various surges it was found that \mathcal{L}_0 varied enormously from surge to surge, and consequently, it was difficult to include it into these equations which represent an average response. When regression analysis was based on equation (4.4) which does not have A_0 , then the scatter of A_0 is considered to be distributed in A_1 and A_2 and their values obtained from different surges have greater variation than the corresponding values which were computed using equation (4.4a). This is, in fact, the main reason for using

^{*} when u-component and v-component are in metre/second, and R and S are in metres.

equation (4.4a) in place of equation (4.4) in the analysis. It is evident that the problem of defining the surge datum remains unresolved so long as δ_0 is not known. Physically, this means there are low frequency variations in sea level not due to weather (e.g. steric variations). In addition, the diurnal and semidiurnal components, considered as being due to surge tide interaction required further attention. To investigate this, an autoregressive technique was applied to the residual surge $S_t^{(r)} (=R_t - \hat{S}_t)$. The procedure of Hunt (1972) and Townsend (1975) as applied to a surge propagating in space was modified for auto predictions in the time domain. In the application of the autoregressive technique it was assumed that diurnal and semi-diurnal components, originating from surge-tide interaction would develop, and disappear slowly. This assumption was made on the basis of visual examination of these components when separated after filtering. Thus an estimate can be obtained from the previous tidal cycle to improve the meteorological surge estimate of the next tidal cycle 12 hours in advance. In auto-regression, any future value is expressed in terms of present and past observations as:

$$S_{t}^{(r)} = b_{1}S_{t-1}^{(r)} + b_{2}S_{t-2}^{(r)} + \cdots$$
 (5.3)

The best estimation $S^{(r)}$ of residual surge was obtained when equation (5.3) assumed the form;

for Frederick Point
$$s_{t+12}^{(r)} = 0.10 \ s_{t}^{(r)} + 0.65 \ s_{t-12}^{(r)}$$
 (5.4)
and for Booby Island $s_{t+12}^{(r)} = 0.20 \ s_{t}^{(r)} + 0.55 \ s_{t-12}^{(r)}$ (5.4b)

Therefore the improved surge forecast $S^{(I)}$ will be given by

$$\mathbf{S}_{\mathbf{t}}^{(\mathbf{I})} = \mathbf{S}_{\mathbf{t}}^{\wedge} + \mathbf{S}_{\mathbf{t}}^{(\mathbf{r})} \tag{5.5}$$

While this process is able to account for both on and the component resulting from surge-tide interaction to a sufficient accuracy, it has one shortcoming in that it may introduce some error when the surge behaves in an abnormal fashion. This is clear from the surge at Booby Island on January 15, 1975, see Figure 6b, when it fell unexpectedly on 16th January conflicting with the meteorologically forecasted surge, and thus introducing an error in the improved surge forecast (based on auto-regression) for 17th of January. A scheme to compute surges is given in Appendix A.

DISCUSSION ON RESULTS AND CONCLUSIONS

The statistical analyses of surges and meteorological observations show that easterly winds are dominant in the region of the Torres Strait. The weather maps are generally complex with multiple depressions and adjoining high pressure systems. This fact made it difficult to establish any relationship between the spatial pressure gradients and the associated storm surges. The east-west component of wind is mainly responsible for the generation of surges, however it has no significant effect on sea level when its magnitude is less than 12 metres/second. Therefore only those periods when the u-component of wind speed remained above 12 metres/second for more than 3 hours were investigated. Booby Island, Goods Island and Turtle Head (i.e. on the west of Ince Point) surges are positive with a westerly wind and negative with an easterly wind, while the opposite is true of surges at Frederick Point and Twin Island. The cross-correlation functions of Booby Island residuals with residuals from other stations computed from data extending over one year, shown in Figure 4, provide evidence that this relationship must be true, in general, even for very small sea level variations which under ordinary circumstances may not look like surges. Frederick Point surges are linearly proportional to the wind speed while Booby Island surges are proportional to wind stress (i.e. proportional to the square of the wind speed). Although surges in a subgroup have common relationships, these relationships do not hold when surges are very small. A few anomalies which were noted in forecast surges are discussed here:

January 8-27, 1975 Surge:

This is the largest surge observed in a one and a half year period (from July 1974 to December 1975). At its peak it exceeded the tidal predictions by 74cm. It commenced with the development of strong westerly winds (from south) on the north west coast and Cape Wessel on January 13 which reached their maximum on 14th. Two minor depressions simultaneously developed on the 14th January, one near Kowanyama and the other near Cooktown. These started levelling off soon and at about 18.00 hours local time, a new depression known as Gloria, started developing in the middle of Cairn and Cooktown. This new depression deepened and at the same time started moving towards the south-east at a speed of about 15 knots. At noon, on 15th January, its speed decreased and when it approached the position Lat. 17°-30', Long. 148°-30', the barometric pressure was nearly 990.7 m.b. and its speed about 5 knots. By midnight this depression was at the deepest level of 988.8 m.b. This moving field of low

pressure gave rise to a very strong westerly wind at Thursday Island which reached its maximum at about midnight of 15th January and continued almost at the same level for one day. The depression started moving further south-east in the early hours of the 17th January and the wind speed at Thursday Island started decreasing. The forecast surge is in good agreement with the observed surge until the surge reached its peak after which recorded and forecast values started diverging. The forecast surge then remained near its peak for one day, as expected from the weather, while the observed surge started decreasing as soon as its maximum was attained. This anomaly is difficult to explain within the limits of the present model, but it may be due to ; (a) a north south pressure gradient or (b) the set up of a sea level gradient, since only a small surge was expected in the south of Booby Island near Kowanyama because of winds of less strength in this region. These aspects of the model could not be investigated because of the inadequacy of the meteorological data. According to the synoptic charts, barometric pressure at Kowanyama was expected to be lower than that of Thursday Island but digitized records show that these were similar in magnitude. It is interesting to note that the forecast of Frederick Point surge during this period is reasonably good.

February 6-25, 1975 Surge:

The forecast of this surge was inaccurate both at Booby Island and Frederick Point. It is worth noting that there was -20cm and 15cm difference in mean sea level at Booby Island and Frederick Point respectively during calm local weather on 5th to 8th February. Obviously, some external forces were acting which led to the mass transport of water from outside thus upsetting the balance of local forces.

A similar discrepancy is observed in September 1-14, 1975, surge at Frederick Point on September 9-14.

It has been found that the problems of the difference in mean sea level, oscillations in Booby Island surges of period 3-4 days and occurrence of surges in calm weather conditions, are observed frequently. The free period of the Gulf of Carpentaria, as computed by Melville and Buchwald (1976) is 30-40 hours. The oscillations of 3 to 4 day period, displayed in Figure 3 and figure 5a, have no contribution from the local meteorology and must have been excited by external forces. Wunsch and Gill (1976) observed similar 4-day oscillations in the

equatorial region (bounded by 10th parallels) of the Pacific. They could not establish any relationship between weather spectra and the spectrum of tidal residuals at 4-day cycle which led them to conclude that it could be due to oceanic resonance. However it would be difficult to establish that Booby Island oscillations of 3-1 days period are transported from the Pacific because firstly. no such oscillation is observed at Frederick Point, secondly, as already discussed, the shallow reefs near Ince Point are acting almost as a barrier which tends to stop any communication between the Pacific and the Gulf of Carpentaria. These oscillations are generally damped but appear to be magnified when they occur after the surge which shows they are locally generated seiches. The period of these oscillations differ from surge to surge, varying from 3 to 4 days. This variation in period of oscillation has limited the accuracy of the autoregression process used to estimate the surge-tide interaction. The difference in mean values between the forecast and observed surges, together with the oscillations described above would suggest the presence of a strong current around Cape Wessel. Also the opposite surges observed at Frederick Point and Booby Island will tend to set up a sea level gradient, again resulting in a strong current in the vicinity of Ince Point. It is difficult to answer these questions within the scope of the present regression model. However, it is suggested that if currents were monitored in the regions of Cape Wessel and Ince Point it would provide valuable information to make some qualitative assessment about the interference of external surges. Although the relationships between the surges and wind at distant places have been established, the actual physics of the process requires more research. In general, all these unsolved problems could only be examined by a comprehensive model capable of simulating the physics of the whole system including the related areas beyond the Torres Strait and the Gulf of Carpentaria.

APPENDIX A

ALGORITHM FOR FORECASTING SURGES

east/

When a weather forecast is expected to generate a surge, i.e. the west component of surface wind at any related meteorological stations exceeds 12 metres/second, then

A For Frederick Point:

- (1) Obtain the surface wind observations of Thursday Island and Willis Island from previous three days as well as those winds forecast.
- (2) Resolve each into u and v components.
- (3) Smooth these components by the least squares technique fitting a second degree polynomial to observations of one day (9 three hourly values), selecting 12 hours on either side of the value to be estimated. This smoothing operation is not unique, any other procedure can be used even graphic smoothing can achieve similar result. The smooth estimations for the last 12 hours should be computed from the last polynomial and updated as soon as a new forecast is available.
- (4) Compute the meteorological surge estimate \hat{S} using equation (5.1).
- (5) Calculate tidal residuals R by subtracting tidal predictions from tidal observations for the same interval as meteorological observations are collected.
- (6) Compute the residual surge $S_t^{(r)} (=R_t \hat{S}_t)$.
- (7) Predict the residual surge $S^{(r)}$ by equation (5.3).
- (8) Compute the final improved surge estimate $S^{(I)}$ using equation (5.5).

B For Twin Island surges:

If local tidal observations are available then follow the same steps as in A except step 5 where the tidal observations and predictions of <u>Twin Island should be used.</u>

If local observations are not available then follow the steps 1-6 as in A and then to compute the improved surge estimate use equation,

$$s_{t}^{(I)} = 0.85 (\hat{s}_{t} + \frac{0.8}{13} \sum_{t=0}^{-12} s_{t}^{(r)})$$

C For Booby Island Surges:

- (1) Obtain the surface wind observations of Thursday Island and Cape Wessel for the previous three days together with those winds forecast.
- (2) Resolve each into u and v components.
- (3) Same as step 3 in A.
- (4) Compute meteorological surge estimate \hat{S} , using equation (5.2).
- (5) Compute tidal residuals R, by subtracting Booby Island tidal predictions from its observations for the same interval as meteorological observations are collected.
- (6) Compute the residual surge $S_t^{(r)} (= R_t \hat{S}_t)$.
- (7) Predict residual surge $S^{(r)}$ by auto-regression formula as in equation (5.4).
- (8) Compute the final improved surge estimate $S^{(I)}$ using equation (5.5).

D For Goods Island and Turtle Head Surges:

If local tidal observations are available, then proceed as for Booby Island surges but modifying steps 4 and 5 as:-

Goods Island

- (4) Compute the meteorological surge estimate \hat{S} using equation (5.2) and then set $\hat{S}_t = 0.8\hat{S}_t$
- (5) Compute R, using local predictions and tidal observations.

Turtle Head

- (4) Compute meteorological surge estimate \hat{S} using equation (5.2) and then set $\hat{S}_t = 0.5\hat{S}_t$
- (5) Compute R, using local tidal predictions and observations.

If local tidal observations are not available then repeat step 1-6 as in C and compute the improved surge estimate as:-

(7)
$$S_{t}^{(I)} = 0.8 \left(\hat{S}_{t} + \frac{0.8^{-12}}{13} \sum_{t=0}^{t} S_{t}^{(r)} \right)$$
 (7) $S_{t}^{(I)} = 0.5 \left(\hat{S}_{t} + \frac{0.8^{-12}}{13} \sum_{t=0}^{t} S_{t}^{(r)} \right)$

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FIGURE CAPTIONS

Figure 1	Map of Torres Strait showing the locations of tidal and meteorological stations.
Figure 2	A simple system with multiple input and a single output.
Figure 3	Spectra of tidal residuals of Booby Island, and meteorological observations of Thursday Island, over the period August 1974 to December 1975: R, tidal residuals; u, u-component of wind; v, v-component of wind and P, barometric pressure.
Figure 4	Cross-correlations function of Booby Island tidal residuals with; (a) Frederick Point, (b) Twin Island, (c) Ince Point, (d) Turtle Head and (e) Goods Island.
Figure 5a	Surges passed through low-pass filter; (i) tidal surges (a) Booby Island, (b) Turtle Head, (c) Frederick Point, (d) Twin Island, and (ii) meteorological surges of Thursday Island, (e) barometric pressures, (f) v-component of wind, (g) u-component of wind.
Figure 5b	The response of the low-pass filter used to eliminate high frequency components of surges and meteorological observations.
Figure 6a	Storm surges at Frederick Point;
	observed storm surge,
	xxxxxxxx meteorological surge forecast computed from meteorological observations only, and
	meteorological surge forecast after improving by autoregression.
Figure 6b	Storm surges at Booby Island;
	observed storm surge,
	xxxxxxxx meteorological surge forecast computed from meteorological observations only, and
	meteorological surge forecast after improving by autoregression.

 $$\operatorname{TABLE}\ 1$$. A list of tidal and meteorological stations for which observations are used in surge study of Torres Strait.

<u>Station</u>	Lat. South	Long. East	Data	Recording Times
Frederick Point (Albany Island)	10-43,	142-35	Tide	hourly
Twin Island	10-27.5,	142-26	Tide	hourly
Ince Point (Wednesday Island)	10-30,	142-18.5	Tide	hourly
Turtle Head	10-31.5	142-12.5	Tide	hourly
Goods Island	10-34,	142-09	Tide	hourly
Booby Island	10-36.5,	141-54.5	Tide	hourly
Willis Island M.O.	16-18,	149-59	(Barometric Pressu (surface wind	are 3 hourly
Port Moresby	09-27,	147-12	(Barometric Pressu (surface wind	ure 3 hourly
Iron Range Aero	12-47	143-18	(Barometric Pressu (surface wind	re 3 hourly
Thursday Island M.O.	10-35,	142-13	(Barometric Pressu (surface wind	re 3 hourly
Weipa	12-47,	141-53	(Barometric Pressu (surface wind	re 6 hourly
Cape Wessel	11-01,	136-43	(Barometric Pressu (surface wind	re 3 hourly
N.E. Island	13-39,	136-57	(Barometric Pressu (surface wind	re 3 hourly

TABLE 2

List of constituents resolved from tidal observations. Time zone = 'U'.

			. Island	Goods	Island	Turt	Turtle Head	Ince	Ince Point	Twin	Island	Freder	Frederick Point
Name	Speed (deg.hr ⁻¹)		H g (mm) (deg)	H (mm)	g (deg)	H (mm)	(geb)	H (mm)	g (deg)	H (mm)	g (deg)	H (mm)	g (deg)
1 Sa	0.04107	284	311.34	077	316.00	147	313.88	220	339.54	045	35.42	039	48.79
2 Ssa	0.08214	950	332.51	029	358.06	024	57.91	028	41.79	053	62.56	055	73.86
3 Mm	0.54437	025	40.07	027	53.02	015	191.22	800	266.88	013	281.92	020	254.28
4 Msf	1.01590	028	355.05	023	358.37	950	185.07	011	37.71	800	329.74	900	104.74
5 Mf	1.09803	030	278.15	021	260.65	023	229.72	003	2.60	000	62.89	900	123.36
6 29,	12.85429	018	270.43	021	284.47	800	289.05	900	305.70	200	316.60	003	312.84
7 0,	12.92714	013	335.31	014	324.23	600	103.57	200	82.82	600	95.04	800	118.93
8 o.j	13.39866	088	322.93	620	330.48	290	338.83	050	342.30	640	353.69	038	351.17
9 6	13,47151	018	308.87	019	353.92	017	330.24	015	355.35	013	4.59	012	2.23
10 0 ₁	13.94304	442	351.84	417	358.85	357	5.73	273	9.37	234	15.15	214	16.11
$11 \mathrm{MP}_1$	14.02517	024	87.71	920	103.82	028	133.50	031	161.02	034	167.73	029	171.12
12 M ₁	14.49205	014	9.75	020	26.62	013	27.55	010	32.10	200	59.30	800	50.05
13 X $_1$	14.56955	200	355.06	021	36.15	011	346.57	800	33.05	900	29.83	800	24.01
14 71	14.91786	016	44.73	025	104.60	017	52,21	013	69.33	013	74.31	012	60.37
15 P ₁	14.95893	187	37.97	181	45.20	169	48.26	148	54.55	144	56.81	135	55.88
16 S ₁	15.00000	035	250.75	045	270.25	025	257.11	023	247.54	017	256.27	011	237.52
17 K ₁	15.04107	715	43.78	629	50.72	629	24.40	94/5	57.52	501	59.30	991/	57.92

;	,	Boob	Booby Island	Goods	Island	Turt	Turtle Head	Ince	Point	Twin	Island	Frede	Frederick Point
Name	Speed (deg.hr ⁻¹)	H (IIII)	н g (mm) (deg)	(IIIII)	(deb)	H (mm)	(deb)	H (mm)	g (deg)	H (mm)	(deb)	H (mm)	g (deg)
18 4	15.08214	016	50.53	020	169.77	012	88.82	014	20.09	015	65.60	010	60.28
19 p ₁	15.12321	014	72.65	029	84.90	013	107.92	010	90.38	600	96.40	600	74.10
20 6 1	15.51259	010	34.05	4,00	110.87	200	42.03	005	36.39	900	9.20	002	8.32
$21 \ J_1$	15.58544	014	74.14	013	78.75	017	122.60	014	131.06	019	134.47	017	114.56
22 so_1	16.05696	029	278.80	035	286.55	013	220.68	017	208.82	020	163.91	018	153.88
23 001	16.13910	045	133.68	94/0	141.73	045	135.62	960	141.88	750	138.60	032	131.96
$24 2MN2S_2$	76204-97	003	152.74	400	164.79	700	210.29	002	193.04	002	198.17	005	198.15
25 3M(SK)_2	26.87018	002	235.55	011	228.35	1,00	289.54	4,00	300.05	200	305.45	002	349.59
26 3M(2S)_2	26.95232	003	101.43	003	55.17	700	296.65	400	324.76	400	348.84	700	325.17
27 002	27.34171	011	326.27	010	323.68	010	2.04	4,00	335.03	005	332.65	002	334.46
28 MNS_2	27,42383	900	195.89	700	341.94	003	5.22	011	24,041	013	351.86	010	359.77
29 M3S2	52.49669	003	134.74	002	35.11	003	353.58	200	42.81	900	32.83	700	44.21
30 2N ₂	27.89536	038	128.55	980	136.45	220	126.30	029	93.61	920	74.75	025	50.16
31 / 2	27.96822	4,00	5.79	600	246.60	038	35.40	053	89*+,+,	061	33.25	055	33.31
$32^{\circ} SNK_2$	28.35759	900	45.34	023	185.00	003	22. •72	900	150.80	010	181.10	005	152.55
33 NA_2	28,39867	700	10.96	022	119.38	400	105.69	900	134.05	013	196.83	005	213.71
34 N ₂	28.43973	171	158.29	153	158.27	133	115.65	166	88.74	196	69.41	500	49.81
$35 \boldsymbol{\vartheta}_2$	28.51257	032	166.96	030	18/t.16	970	131.23	024	108.83	031	75.80	037	50.77
$36 \mathrm{OP}_2$	28,90198	600	22.78	600	110.06	021	8.59	015	58.74	600	57.27	015	71.37

cont

		Booby	Booby Island	Goods	Island	Turt	Turtle Head	Ince	Ince Point	Twin	Island	Frede	Frederick Point
Name	Speed (deg.hr ⁻¹)	H (mm)	H д (mm) (deg)	H (mm)	g (deg)	H (mm)	g (deg)	II (mm)	g (deg)	H (mm)	g (deg)	Н (шш)	g (deg)
37 MA,	28.9/130/1	023	171.35	024	327.04	031	169.33	024	260.40	720	279.25	017	278.50 *
38 m ,	28.98410	733	200.10	519	204-71	335	167.32	298	111.94	503	33.08	965	62.10
39 M B ,	29.02518	900	74.83	0/42	305.65	030	15.82	001	149.73	⁺ /CO	89.63	010	286.77 *
1,0 MKS,	429 9 0•62	003	299.39	025	319.60	014	354.70	011	28.34	010	105.39	012	65.89
111 A	29,45563	005	245.86	015	191.94	900	291.62	012	338.52	020	326.63	600	323.73
42 L ₃	29.52847	018	356.69	021	290.91	1/80	334.14	035	335.141t	84,0	343.69	043	334.23
43 2 SK 2	29.91786	903	223.40	019	175.26	1/CO	221.90	£00	350.19	900	156.58	900	26•902
1,14 T	29.95892	012	291.60	220	33.78	024	15.77	031	16.04	033	21.29	039	02*9
45 S,	30,00000	138	321.94	19/₊	5.78	566	27.36	1,119	38.86	503	37.97	512	27.81
46 R ₃	30.04108	4/∪0	317.33	918	326.50	014	236.67	600	32.99	800	29.6	900	12.17
47 K,	30.08214	54/0	290.12	062	337.95	1720	8.12	103	50.29	129	31.48	11/15	21.26
, 8 MS	30.47153	003	87.24	800	23,28	^{t}l	12.84	003	177-771	900	233.57	002	261.16
NSW 64	30.54437	္ပတ	302.77	- 018	304.23	003	233.8n	019	221.83	050	197.15	013	20/4.10
50 KJ,	30.62651	005	135.92	018	91.26	1,00	94.65	001	168.70	300	286.55	1/00	313.27
51 2SM,	31.01590	013	252.94	02^{4}	231.64	019	138.36	050	185.03	023	176.78	025	158.07
52 SKM,	31.09802	005	298.51	012	113.20	800	142.81	015	162,30	019	147.06	015	138.25
53 MQ,	1,2.38277	012	126.77	010	147.46	200	24.94	500	267.78	011	283.52	008	267.45
54 NO ₃	42.92714	620	029 163.27	4/50	172.01	016	27.63	008	276.31	017	306.79	012	308.41

* Values of g for constituents ${\rm MA}_2$ and ${\rm MB}_2$ are changed according to notes issued by Dr. D. E. Cartwright on November 15, 1977.

cont:

		Booby	Booby Island	Goods	Island	Turt	Turtle Head	Inc	Ince Point	Twin	Island	Frede	Frederick Point
Name	Speed (deg.hr-1)	H (mm)	H g (mm) (deg)	II (mm)	g (deg)	H (mm)	g (deg)	H (mm)	g (deg)	H (mm)	(gab.)	H (mm)	g (deg)
55 2MP ₃	82600*67	900	272.73	200	272.00	600	286.24	200	296-93	900	274.08	005	236.61
56 M ₃	43.47617	012	94.48	011	102,54	200	16.62	900	150.84	200	166.97	900	133.54
57 so ₃	1,081,681,1	022	250.20	021	262.98	050	305.86	035	284.65	030	283.40	016	254.59
58 MK ₃	44,02518	033	190.66	031	193.78	020	138.66	002	273.80	210	358.64	011	8.20
59 2MQ ₃	1,4,56955	00	219.28	003	5.59	001	279.85	005	105.09	7 00	115.70	000	291.50
60 SK ₃	45.04108	016	325.25	010	318.37	023	358.71	024	343.65	020	339.21	014	321.06
61 2MNS _{1,}	1,6204,*95	200	221.30	003	177.19	700	1/19.99	001	168.97	100	303.48	003	61.82
62 3MK,	56.87018	003	309.46	003	29.6	005	303.20	003	78.94	1 /00	95.23	005	3.65
63 3MS ₁₄	56.95232	002	207.24	900	171.95	900	197.69	003	334.94	200	346.10	003	1.58
64 MN ₁₄	57.42383	003	297.52	010	20.65	032	342.53	025	94,*84	970	52.75	600	31.25
65 MJ ₁	57.49669	001	273.59	002	159.69	700	330.78	900	82.94	900	50.92	003	27.61
66 2NSK4	57.88606	001	213.89	005	168.34	υο,	215.36	003	155.91	900	60.77	₁ 00	40.49
67 M4	57.96822	010	37.55	034	52.26	072	9.82	052	74.38	24,0	81.91	013	68.37
68 SN ₁₄	58.43973	900	115.56	800	106.60	010	31.36	800	37.28	011	13.52	008	335.86
69 3MN/ ₁	58.51257	005	125.70	800	4,0.56	200	25.63	003	358.01	011	330.51	200	312.73
70 MS,	58.98410	016	110.52	970	95.65	24/0	16.45	022	26.66	023	80.90	008	192.25
71 MK ₁₁	59.0662 ⁴	012	93.66	012	87.13	050	15.70	010	90*95	011	18.28	200	336.84
$72.2MSN_{l_1}$	59.52847	005	22,11	700	11,021	010	323.05	002	280.34	200	96•992	900	229.88
73 S ₁₁	00000-09	1,00	61.24	003	71.90	011	9.93	900	342.46	200	359.61	00/4	328.76

cont:

			Booby Island	Spoog	: Island	Turt	:le Head		Ince Point	Twin	Island	Frede	Frederick Point
Name	Speed (deg.hr ⁻¹)		н g (mm) (dea)	H (mm)	g (dea)	H (mm)	H g (mm)		H g (mm) (302)	H	g (40-)	H (g (
					S S S S S S S S S S S S S S S S S S S		(fign)		(fan)		(ded)		(deg)
74 SK_4	60.08214	001	117.17	005	283.71	200	329.21	900	280.41	200	308.93	200	296.39
75 2MO 5	71.91124	800	189.64	200	196.70	200	64.662	900	320.58	900	326.89	003	23.44
76 M ₅	72.46027	003	133.79	003	127.88	200	241.27	200	253.16	900	240.03	001	209.86
77 MSO_{5}	72.92714	011	303.63	600	327.73	013	39.94	011	ξυ•υ ¹ /	800	42.01	005	165.19
78 SMK 5	73.00928	002	246.22	600	256.86	013	332.12	011	349.13	800	344.38	003	198.04
79 MSK $\frac{5}{5}$	74,02518	012	183.31	011	200.82	013	247.22	600	242.11	400	218.09	200	51.33
$80.2(MN)s_6$	84.84767	000	242.29	100	192.62	000	107.93	001	345.09	100	54.45	001	77.70
81 3MNS_6	85.39204	001	330.21	8	196.98	000	272.62	100	139.94	003	137.97	003	129.80
82 4NK ₆	85.85428	005	139.64	002	50.09	200	28.13	003	339.11	003	300.55	700	267.22
83 4MS ₆	85.93642	001	35.23	000	225.10	200	26.34	001	187.14	003	206.08	003	180.87
84 2msnk	86,32581	001	355.34	005	1.12	001	55.29	003	133.17	200	154.99	001	153.69
85 2MN_6	46704.98	008	117.71	800	75.29	700	16.54	010	289.80	014	272.59	014	250.68
86 2MV	86.48079	001	77.85	005	124.54	001	48.73	005	253.18	003	223.48	003	226.91
87 3MSK ₆	86.87018	003	40.10	003	35.55	003	88.02	200	166.34	003	213.24	002	205.04
88 M ₆	86.95232	600	138.30	012	88.04	4700	15.97	910	304.31	021	291.80	018	272.32
89 MSN ₆	87.42383	200	91.34	⁴ 700	29.24	600	318.04	015	296.87	017	276.17	012	232.60
9 _{NM1} , 06	69967.28	001	123.46	001	162.71	4,00	39.91	1,00	4.63	400	332.57	003	259.42
$91^{2}MS_{6}$	87.96822	016	117.93	800	84.45	015	302,46	034	304.02	038	296.15	022	266.35
92^{2MK}	88.05035	1,00	113.29	4,00	55.78	200	340.49	ύοο	315.09	010	310.73	900	27/1.88
									O	cont:			

TABLE 3

Variance of observations and residuals (observed sea level-predictions) from various stations.

Station	Observation Variance (cm ²)	Residual Variance (cm ²)
Frederick Point	4967.4	63.5
Twin Island	4619.0	57.8
Ince Point	3844.6	33.5
Turtle Head	4088.9	66.1
Goods Island	5375•1	124.2
Booby Island	7129.0	150.1

TABLE 4

Means and variances of meteorological variables from recorded observations only.

	Barometr	Barometric Pressure		Wind Speed	peed	
			n-0	u-component	v-component	onent
	mean (mb)	$variance (mb)^2$	mean (m/sec)	variance $(m/\sec)^2$	mean (m/sec)	variance (m/sec) ²
Cape Wessel*	1006.81	5.64	-2.51	24.62	0.57	6.01
Port Moresby	1002.73	3.91	-0.58	3.45	09*0	2.13
Thursday Island	1002,01	2 13 8	-3.46	23.24	-0-32	1.36
Willis Island*	1008.91	10.55	-5.64	13.15	0.03	48.4

*Observations were not recorded at regular intervals and there were some gaps of up to a month when no observations were recorded, therefore these statistical parameters are biased.

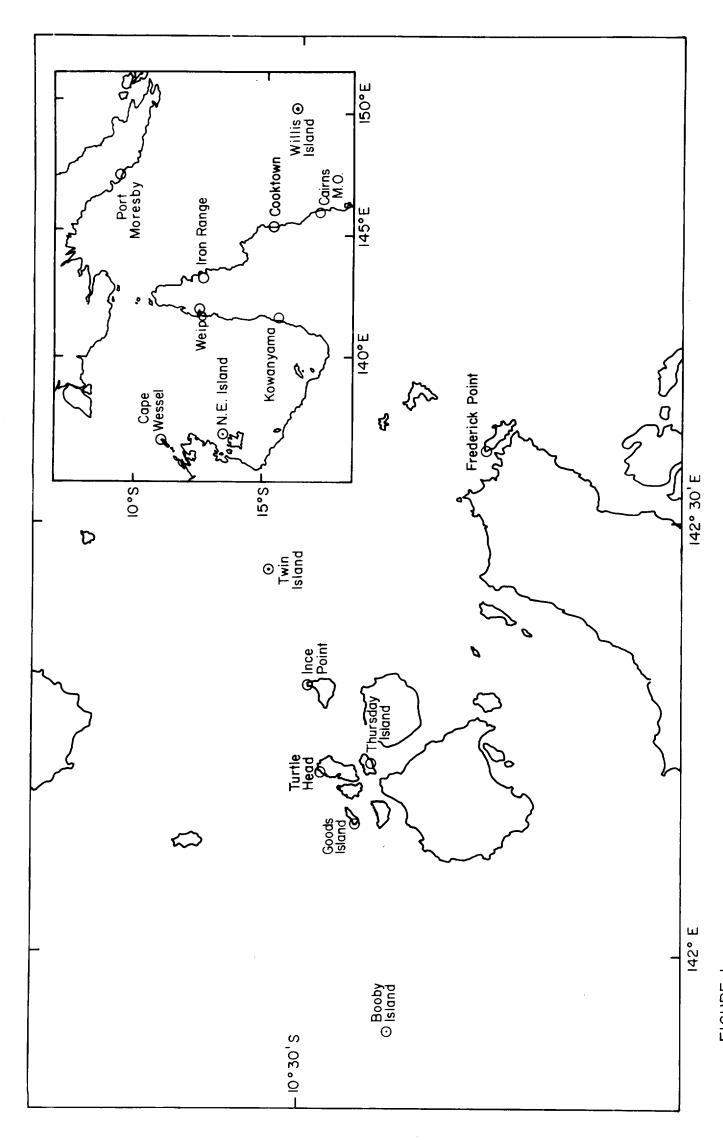


FIGURE 1.

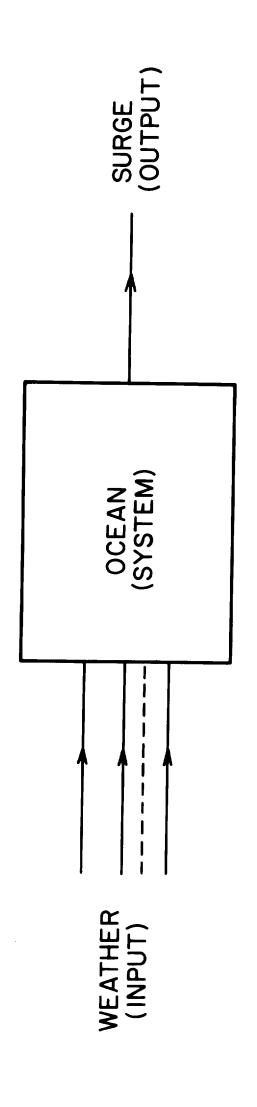


FIGURE 2.

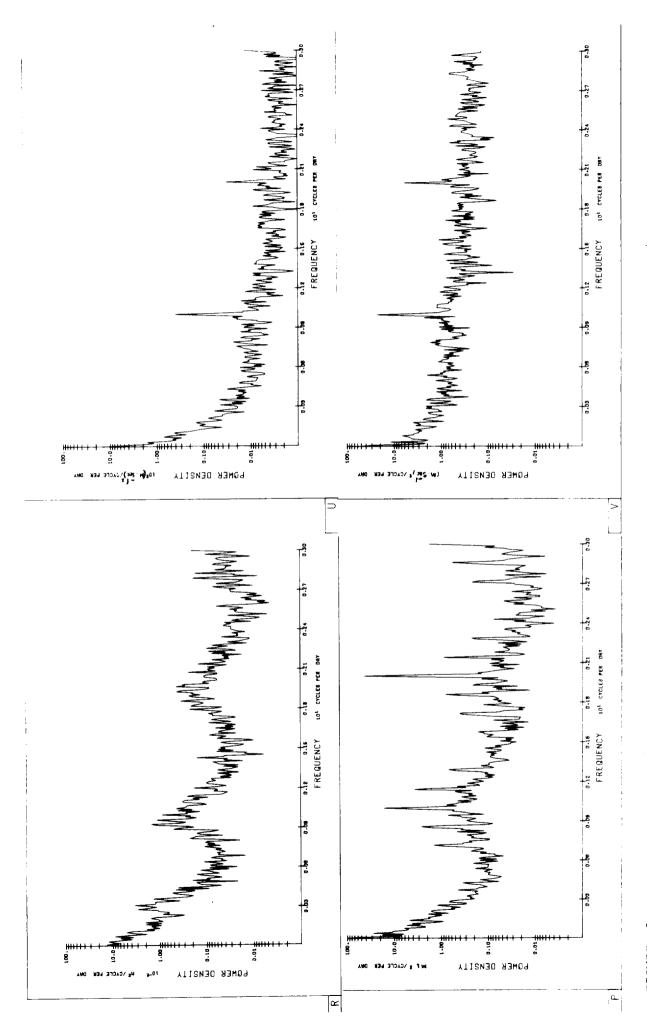


FIGURE 3

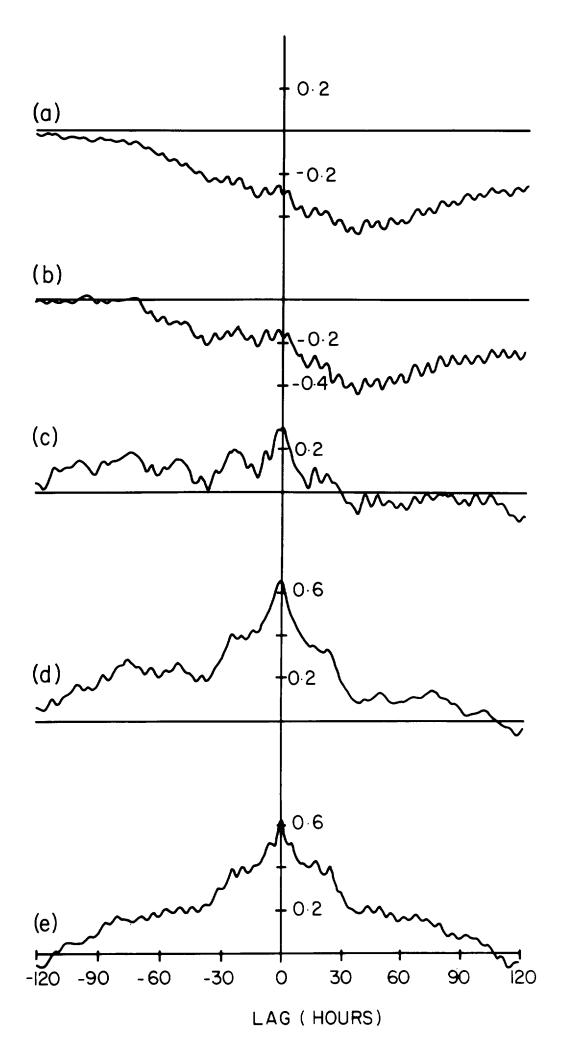


FIGURE 4.

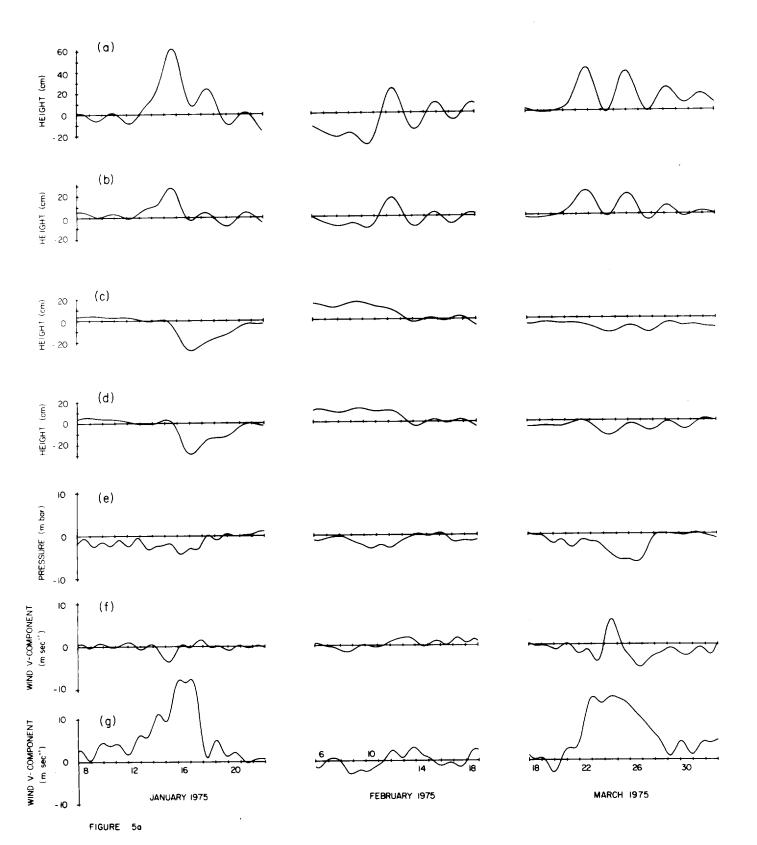


FIGURE 5b

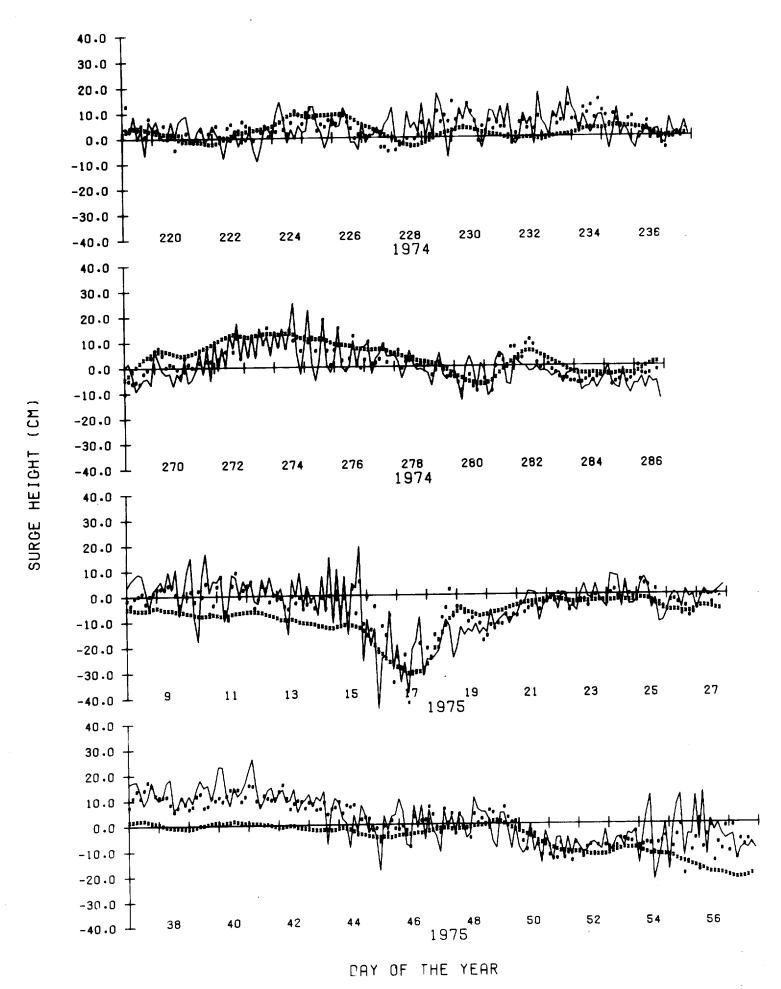


FIGURE 6a

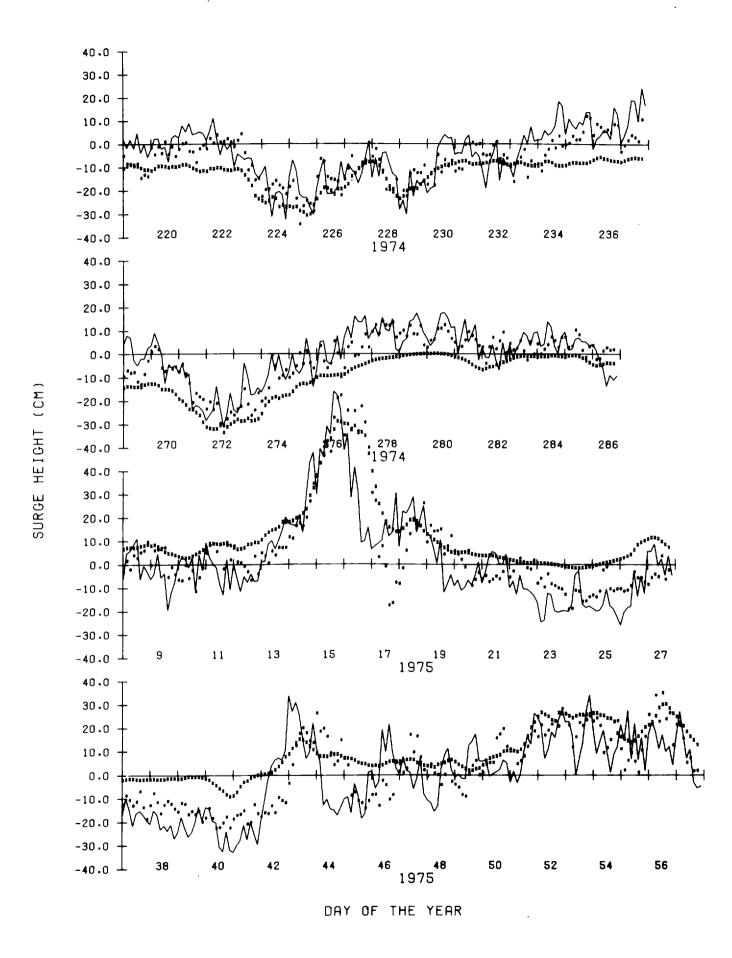
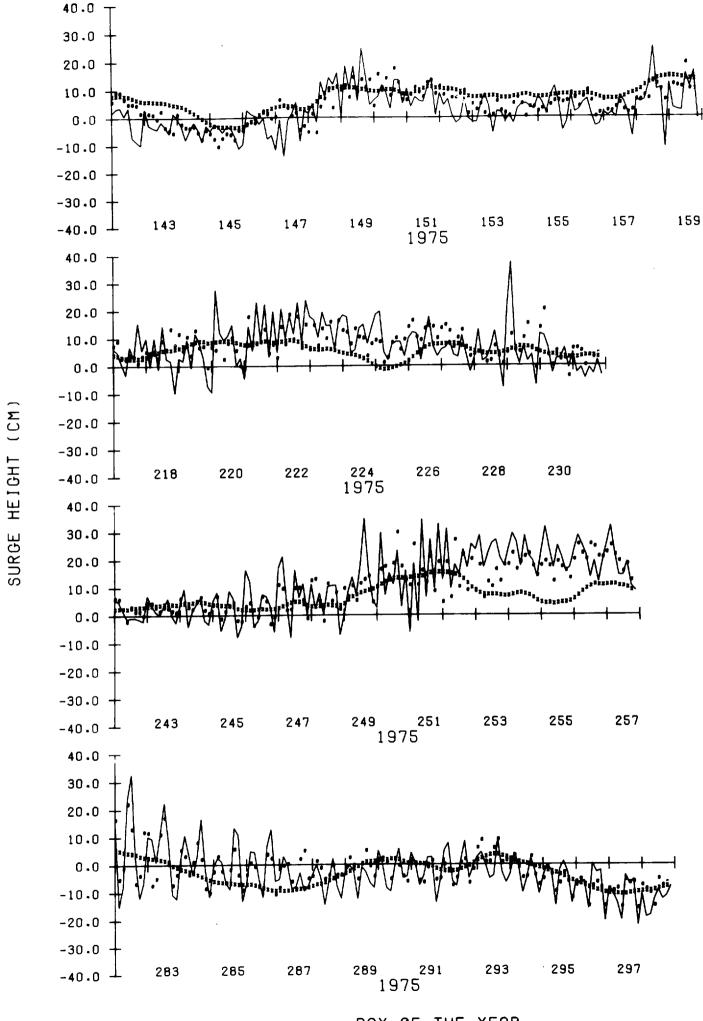
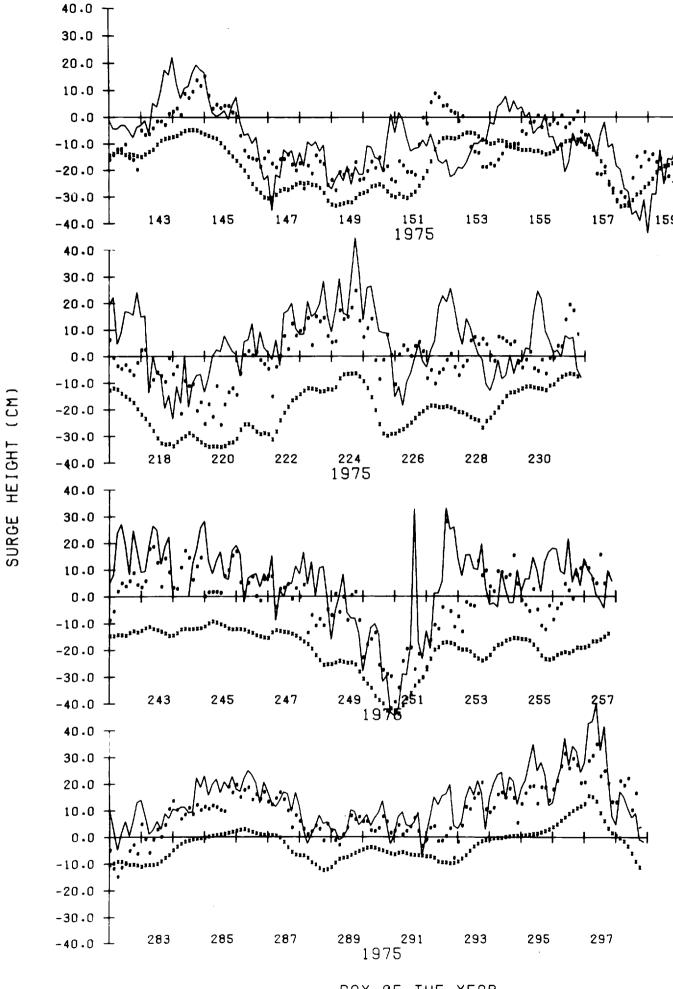


FIGURE 6b



DAY OF THE YEAR



CAY OF THE YEAR