

1 **Remote sensing the spatial and temporal structure of**  
2 **magnetopause and magnetotail reconnection from**  
3 **the ionosphere**

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4 **Abstract.** Magnetic reconnection is the most significant process that re-  
5 sults in the transport of magnetised plasma into, and out of, the Earth's magnetosphere-  
6 ionosphere system. There is also compelling observational evidence that it  
7 plays a major role in the dynamics of the solar corona, and it may also be

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8 important for understanding cosmic rays, accretion disks, magnetic dynamos,  
9 and star formation. The Earth's magnetosphere and ionosphere are presently  
10 the most accessible natural plasma environments where magnetic recon-  
11 necting and its consequences can be measured, either in situ, or by remote sens-  
12 ing. This paper presents a complete methodology for the remote sensing of  
13 magnetic reconnection in the magnetosphere from the ionosphere. This method  
14 combines measurements of ionospheric plasma convection and the ionospheric  
15 footprint of the reconnection separatrix. Techniques for measuring both the  
16 ionospheric plasma flow and the location and motion of the reconnection sep-  
17 aratrix are reviewed, and the associated assumptions and uncertainties as-  
18 sessed, using new analyses where required. Application of the overall method-  
19 ology is demonstrated by the study of a 2-hour interval from 26 December  
20 2000 using a wide range of spacecraft and ground-based measurements of the  
21 northern hemisphere ionosphere. This example illustrates how spatial and  
22 temporal variations in the reconnection rate, as well as changes in the bal-  
23 ance of magnetopause (dayside) and magnetotail (nightside) reconnection,  
24 can be routinely monitored, affording new opportunities for understanding  
25 the universal reconnection process and its influence on all aspects of space  
26 weather.

## 1. Introduction

27 It has been estimated that over 99.99% of the universe is made up of plasma - the fourth  
28 state of matter, composed of free ions and electrons. Despite its universal importance, our  
29 understanding of natural plasmas is limited by our ability to observe their behaviour and  
30 measure their properties. The most accessible natural plasma environment for study is  
31 the Earth's magnetosphere-ionosphere system. The Earth's magnetosphere is that region  
32 of near-Earth space which is permeated by the Earth's magnetic field. The plasma in the  
33 magnetosphere is controlled mainly by magnetic and electric forces that are much stronger  
34 here than gravity or the effect of collisions. The magnetosphere is embedded in the  
35 outflowing plasma of the solar corona, known as the solar wind, and its associated magnetic  
36 field, the interplanetary magnetic field (IMF). Because of the high conductivity of the  
37 solar wind and magnetospheric plasmas, their respective magnetic fields are effectively  
38 "frozen-in" to the plasma (like in a superconductor). The frozen-in nature of these two  
39 plasmas means that the solar wind cannot easily penetrate the Earth's magnetic field  
40 but is mostly deflected around it. This results in the distortion of the magnetosphere  
41 and the two plasmas end up being separated by a boundary, the magnetopause. The  
42 magnetopause is roughly bullet-shaped and extends to  $\sim 10$ - $12$  Earth radii ( $R_E$ ) on the  
43 dayside of the Earth, and stretches out into a long tail, the magnetotail, which extends to  
44 hundreds of  $R_E$  on the nightside of the Earth. However, the two plasma regions are not  
45 totally isolated as the process of magnetic reconnection allows the transmission of solar  
46 wind mass, energy, and momentum across the magnetopause, and into the magnetosphere.

47 Magnetic reconnection (or merging) is a physical process [*Priest and Forbes, 2000*] which  
48 involves a change in the connectivity of magnetic field lines (or magnetic flux) that fa-  
49 cilitates the transfer of mass, momentum and energy. The resultant splicing together  
50 of different magnetic domains changes the overall topology of the magnetic field. If we  
51 consider a magnetic topology with antiparallel magnetic field lines frozen into two adjoin-  
52 ing plasmas, where the plasma and magnetic field lines on both sides are moving toward  
53 each other, this results in a current sheet separating these regions, with a large change  
54 in the magnetic field across it. The frozen-in field approximation breaks down in this  
55 current sheet allowing magnetic field lines to diffuse across the plasma. This diffusion  
56 allows oppositely-directed magnetic fields to annihilate at certain points. This results in  
57 X-type configurations of the magnetic field, as shown in the schematic representation of  
58 a two-dimensional reconnection region in fig.1. Here, the magnetic field strength is zero  
59 at the centre of the X, termed the magnetic neutral point. The magnetic field lines form-  
60 ing the X, and passing through the neutral point, are called the separatrix. Plasma and  
61 magnetic field lines are transported toward the neutral point from either side as shown  
62 by the blue arrows in fig.1. Reconnection of the field lines occurs at the neutral point  
63 and the merged field lines, populated by a mixture of plasma from both regions, are ex-  
64 pelled from the neutral point approximately perpendicular to their inflow direction. This  
65 process of magnetic reconnection is fundamental to the behaviour of the natural plasmas  
66 of many astrophysical environments. For example, solar flares, the largest explosion in  
67 the solar system, are caused by the reconnection of large systems of magnetic flux on the  
68 Sun, releasing in minutes the energy that has been stored in the solar magnetic field over  
69 a period of weeks to years. Reconnection is also important to the science of controlled

70 nuclear fusion as it is one mechanism preventing the magnetic confinement of the fusion  
71 fuel.

72 At the Earth's magnetopause magnetic reconnection is the major process through which  
73 solar wind mass, energy and momentum are transferred from the solar wind into the  
74 magnetospheric system. Together with reconnection within the magnetotail, this drives a  
75 global circulation of plasma and magnetic flux within the magnetosphere and ionosphere  
76 [*Dungey, 1961*]. Figure 2 presents a schematic representation of the magnetosphere in  
77 the noon-midnight meridian plane which highlights the topology of the Earth's magnetic  
78 field and its connection to the IMF. Point  $N_1$  marks an example location of a reconnection  
79 neutral point on the dayside magnetopause, with an IMF field line (marked 1) reconnecting  
80 with a geomagnetic field line (marked 1'). Typically, the connectivity of geomagnetic field  
81 lines is of two types: Open - one end of the magnetic field line is connected to the Earth,  
82 the other to the IMF. Closed - both ends are connected to the Earth. Geomagnetic field  
83 line 1' represents the last closed field line in the dayside magnetosphere. As a result of  
84 the magnetopause reconnection two open field lines are created (marked 2 and 2') which  
85 are dragged by the solar wind flow to the nightside of the magnetosphere and into the  
86 magnetotail (to points 3 and 3'). Here, the existence of the anti-parallel magnetic field  
87 configuration results in magnetotail reconnection (at neutral point  $N_2$  in fig.2). In three  
88 dimensions, the reconnection X-points depicted as  $N_1$  and  $N_2$  in fig.2 are thought to  
89 extend along the magnetopause and magnetotail current sheets in lines known as X-lines.  
90 Figure 3 presents a 3-dimensional schematic representation of the magnetosphere which  
91 highlights these extended X-lines.

92 Accurate measurement of both the magnetopause and magnetotail reconnection rates,  
93 and an understanding of the factors that influence them has been a major scientific goal  
94 for many years. The reconnection rate (or equivalently the reconnection electric field)  
95 is defined as the rate of transfer of magnetic flux across unit length of the separatrix  
96 between the unreconnected and reconnected field lines. In the magnetospheric environ-  
97 ment, important outstanding questions concerning reconnection, which can be addressed  
98 by reconnection rate measurements, include: Where is the typical location, and what is  
99 the typical extent (in both time and space), of both the magnetopause and magneto-  
100 tail X-lines? How does the reconnection rate vary along these X-lines, and with time?  
101 How do these things change with changing interplanetary magnetic field and geomagnetic  
102 conditions?

103 The reconnection rate can be measured by spacecraft in the reconnecting current sheet,  
104 local to the neutral points, by measuring the electric field tangential to the reconnection X-  
105 line [*Sonnerup et al.*, 1981; *Lindqvist and Mozer*, 1990]. Such studies have shown evidence  
106 for a fast reconnection rate (inflow speed / Alfvén speed  $\sim 0.1$ ) [*Priest and Forbes*, 2000].  
107 However, it is generally difficult to measure the reconnection rate with satellites because  
108 it must be measured in the frame of reference of the separatrix, which is often in motion.  
109 Hence, such measurements are typically sparse in space and time, limited to the location  
110 and time of each spacecraft crossing of the current sheet.

111 More continuous and extensive measurements of reconnection in time and space can  
112 presently be achieved only by remotely sensing magnetic reconnection in the magneto-  
113 sphere from the ionosphere. The ionosphere, located at altitudes of  $\sim 80$ -2000 km, forms  
114 the base of the magnetospheric plasma environment. It is the transition region from the

115 fully-ionized magnetospheric plasma to the neutral atmosphere of the Earth. As can be  
116 seen in fig.3, the focussing effect of the Earth's dipole-like magnetic field projects recon-  
117 nection signatures from the vast volume of the magnetosphere onto the relatively small  
118 area of the polar ionospheres, where they can be measured by ground- and space-based  
119 instruments. Hence, the ionospheric perspective is immensely valuable as a window to  
120 the huge outer magnetosphere and the reconnection processes occurring there.

121 In simple quasi-steady-state reconnection scenarios for different IMF orientations  
122 [*Dungey*, 1961, 1963; *Russell*, 1972; *Cowley*, 1981], and in the absence of other (e.g.,  
123 viscous) transport processes [*Axford and Hines*, 1961], the total globally-integrated re-  
124 connection rate is equal to the maximum electric potential difference across the polar  
125 ionosphere. This can be measured every  $\sim 100$  min by low-altitude polar-orbiting satel-  
126 lites [*Reiff et al.*, 1981] or at higher cadence by ground-based radar and magnetometer  
127 networks [*Ruohoniemi and Baker*, 1998; *Richmond and Kamide*, 1988]. Such studies have  
128 investigated the functional dependence of the integrated reconnection rate on the relative  
129 orientation of the reconnecting magnetic fields [*Reiff et al.*, 1981; *Freeman et al.*, 1993].

130 More generally, imbalance of the integrated reconnection rates at the magnetopause  
131 and in the magnetotail results in a change in the relative proportions of open and closed  
132 magnetic flux [*Siscoe and Huang*, 1985; *Cowley and Lockwood*, 1992]. Thus, for unbalanced  
133 reconnection, the difference in the two integrated reconnection rates can be measured from  
134 the rate of change of polar cap area (the area of incompressible open magnetic flux that  
135 threads the polar ionospheres). Estimates of both the magnetopause and magnetotail  
136 reconnection rates can then be made whenever one or the other reconnection rate can  
137 be estimated [*Lewis et al.*, 1998], or is negligible [*Milan et al.*, 2003], or by summing the

138 difference measurement with an estimate of the average of the two reconnection rates given  
139 by the cross-polar cap potential [*Cowley and Lockwood, 1992*]. Such studies have revealed  
140 and quantified the variation of global magnetopause and magnetotail reconnection through  
141 the substorm cycle [*Milan et al., 2007*].

142 On shorter time scales, local reconnection rates have been inferred from low-altitude  
143 spacecraft observations of the dispersion of ions from the reconnection site precipitating  
144 into the ionosphere on newly-opened magnetic field lines [*Lockwood and Smith, 1992*].  
145 These observations provide a temporal profile of the reconnection rate at a single location  
146 for the duration of the satellite pass ( $\sim 10$  min). Such studies show the reconnection rate  
147 to vary on timescales of minutes, as suggested by the in-situ observation of flux transfer  
148 events (instances of transient reconnection) at the magnetopause [*Russell and Elphic,*  
149 *1978*].

150 Most generally, the reconnection rate is measured from the ionosphere by first detect-  
151 ing the ionospheric projections of regions of different magnetic connectivity (e.g., open  
152 and closed magnetospheric field lines) and then measuring the transport of magnetic flux  
153 between them. The reconnection rate equates to the component of the ionospheric convec-  
154 tion electric field tangential to the ionospheric projection of the reconnection separatrix,  
155 in the frame of the reconnection separatrix. Hence, in a ground-based measurement frame,  
156 contributions can arise from (1) plasma convecting across the separatrix, and (2) move-  
157 ment of the separatrix in the measurement frame. As shown schematically in fig.3, the  
158 reconnection separatrix (yellow and green shaded areas) maps down magnetic field lines  
159 from the in-situ reconnection X-lines (bold blue lines in space) to regions in the polar iono-  
160 spheres termed “merging lines” (bold blue lines in the ionosphere). The different magnetic

161 field topologies in the two regions either side of the separatrix give rise to different plasma  
162 properties in each region, which can be detected at the ionospheric footprints. During  
163 southward IMF conditions, when magnetopause reconnection occurs preferentially on the  
164 low-latitude magnetopause (as in figs.2 and 3), the dayside merging line is co-located  
165 with the ionospheric projection of the open-closed magnetic field line boundary (OCB),  
166 alternatively termed the polar cap boundary. During strong northward IMF conditions,  
167 when reconnection occurs at high latitudes on the magnetotail lobe magnetopause, the  
168 reconnection separatrix is typically located some distance poleward of the OCB, within  
169 the polar cap, at the point where the lobe magnetopause maps into the ionosphere. On  
170 the nightside of the Earth the merging line associated with the most-distant magnetotail  
171 X-line is always co-located with the OCB. Reconnection is also thought to occur Earth-  
172 ward of this far-tail X-line (at a near-Earth neutral line) but there is not as yet a clear  
173 signature of the ionospheric projection of this X-line.

174 The first reconnection rate measurements of this type were made in the nightside iono-  
175 sphere by *de la Beaujardière et al.* [1991] using Sondrestrom Incoherent Scatter Radar  
176 (ISR) measurements. Using a single meridional radar beam they measured the plasma  
177 velocity across the OCB in the OCB rest frame. The location of the OCB was estimated  
178 by identifying strong electron density gradients which occur at ionospheric *E*-region al-  
179 titudes along the poleward boundary of the auroral oval. These are thought to be a  
180 good proxy for the OCB in the nightside ionosphere. *Blanchard et al.* [1996, 1997] later  
181 refined these measurements by locating the OCB using both *E*-region electron density  
182 measurements and 630 nm auroral emissions measured by ground-based optical instru-  
183 ments. They investigated how the magnetotail reconnection rate varied with magnetic

184 local time, with variations in the IMF, and with substorm activity. Since then, a number  
185 of studies have used single radar beams to make single-point reconnection rate measure-  
186 ments of this type in both the dayside and nightside ionospheres [*Pinnock et al.*, 1999;  
187 *Blanchard et al.*, 2001; *Østgaard et al.*, 2005]. These studies have used a range of different  
188 techniques to determine the OCB location and motion. However, the employment of a  
189 single meridional radar beam in the above studies meant that no investigation could be  
190 made of spatial variations in the reconnection rate.

191 *Baker et al.* [1997] first measured the reconnection rate across an extended longitudinal  
192 region. They used the technique of L-shell fitting [*Ruohoniemi et al.*, 1989] to estimate  
193 two-dimensional ionospheric convection velocity vectors from line-of-sight velocity mea-  
194 surements made by a single radar of the Super Dual Auroral Radar Network (SuperDARN)  
195 [*Greenwald et al.*, 1995; *Chisham et al.*, 2007]. They also used variations in the Doppler  
196 spectral width characteristics measured by the radar to estimate the OCB location. Since  
197 then, the advent of large networks of ionospheric radars which can measure the plasma  
198 convection velocity over large regions of the ionosphere has made extensive measurements  
199 of the reconnection rate a reality. Recent studies [*Pinnock et al.*, 2003; *Milan et al.*,  
200 2003; *Chisham et al.*, 2004b; *Hubert et al.*, 2006; *Imber et al.*, 2006] have employed the  
201 technique of SuperDARN global convection mapping to measure the convection velocity  
202 across large regions of the polar ionospheres for a range of IMF conditions. Combined with  
203 measurements of the location and motion of the ionospheric footprint of the reconnection  
204 separatrix from a range of different instrumentation, these studies have illustrated that  
205 the magnetopause reconnection rate not only varies with time but also with longitudinal

206 location along the merging line. The magnetotail reconnection rate has also been studied  
207 in a similar way [*Lam et al.*, 2006; *Hubert et al.*, 2006].

208 The purpose of this paper is to build on these previous studies and to present a standard  
209 methodology for reconnection rate determination which can be easily implemented. To  
210 this end we:

211 (1) Set out in full a complete methodology for remote sensing of the reconnection rate.

212 (2) Review the techniques for determining the ionospheric convection velocity field and  
213 the ionospheric projection of the reconnection separatrix.

214 (3) Highlight and discuss problems and uncertainties concerning the methodology and  
215 techniques.

216 (4) Present an example of a global application of this methodology.

## 2. Methodology for estimating the reconnection rate

217 In this section we outline mathematically the methodology for determining reconnection  
218 rates using ionospheric measurements. We also review the instrumentation and analysis  
219 techniques used to make these ionospheric measurements. The application of many of  
220 these techniques is described by considering a 2-hour interval of data from 26 December  
221 2000. The results of the reconnection rate analysis using the combined data sets from this  
222 interval are presented in section 3.

### 2.1. Theory

#### 2.1.1. General formulation

224 The principle of remote measurement of the reconnection electric field was first pre-  
225 sented by *Vasyliunas* [1984] who argued that the potential variation along the ionospheric

226 projection of the reconnection separatrix (the merging line) related directly to that along  
 227 the in-situ reconnection X-line. The reconnection electric field in the ionosphere equates  
 228 to the component of the ionospheric convection electric field that is directed tangential to  
 229 the ionospheric projection of the reconnection separatrix, in the frame of the separatrix.  
 230 This equates to the rate of flux transfer across the reconnection separatrix, assuming that  
 231 the magnetic field is frozen in to the plasma. It is assumed that the plasma flow in the  
 232 polar ionosphere is dominated by the convection electric field and that the convection  
 233 velocity field is divergence-free.

234 The reconnection rate, or electric field ( $E_{rec}$ ), in the ionosphere at any point  $s$  along  
 235 the reconnection separatrix at a time  $t$  can be written

$$236 \quad E_{rec}(s, t) = \mathbf{E}'(s, t) \cdot \hat{\mathbf{T}}(s, t) \quad (1)$$

237 where  $\mathbf{E}'(s, t)$  is the convection electric field at the separatrix, in the frame of the separa-  
 238 trix, and

$$239 \quad \hat{\mathbf{T}}(s, t) = \frac{d\mathbf{P}(s, t)}{ds} \quad (2)$$

240 represents the tangent to the separatrix, where  $\mathbf{P}(s, t)$  describes the location of the sepa-  
 241 ratrix.

242 We can relate the convection electric field to the ionospheric convection velocity field if  
 243 we assume the ideal magnetohydrodynamic approximation of Ohm's law

$$244 \quad \mathbf{E}'(s, t) = -(\mathbf{V}'(s, t) \times \mathbf{B}(s)) \quad (3)$$

245 where  $\mathbf{V}'(s, t)$  is the convection velocity at locations along the separatrix, in the frame of  
 246 the separatrix (a one-dimensional path through the convection velocity field  $\mathbf{V}'(\mathbf{x}, t)$ ), and  
 247  $\mathbf{B}(s) = B_z(s)\hat{\mathbf{z}}$  is the magnetic field (approximated as being vertical and time invariant).

248 The normal to the separatrix at a fixed ionospheric height can be written as,

$$249 \quad \hat{\mathbf{N}}(s, t) = -(\hat{\mathbf{z}} \times \hat{\mathbf{T}}(s, t)) \quad (4)$$

250 and hence, combining (1), (3), and (4), the reconnection electric field, (1), can be rewritten  
251 as,

$$252 \quad E_{rec}(s, t) = B_z(s) (\mathbf{V}'(s, t) \cdot \hat{\mathbf{N}}(s, t)) \quad (5)$$

253 The ionospheric convection velocity is not typically measured in the frame of the sep-  
254 aratrix and hence we need to convert convection velocity measurements  $\mathbf{V}(s, t)$  into this  
255 frame using the transformation,

$$256 \quad \mathbf{V}'(s, t) = \mathbf{V}(s, t) - \frac{d\mathbf{P}(s, t)}{dt} \quad (6)$$

257 By combining (5) and (6) we can write the reconnection electric field as,

$$258 \quad E_{rec}(s, t) = B_z(s) \left[ \left( \mathbf{V}(s, t) - \frac{d\mathbf{P}(s, t)}{dt} \right) \cdot \hat{\mathbf{N}}(s, t) \right] \quad (7)$$

259 The total rate of flux transfer ( $dF_{12}(t)/dt$ ) along a merging line connecting points  $P_1$   
260 and  $P_2$  is given by the integrated reconnection rate, or reconnection voltage ( $\phi_{12}(t)$ ), which  
261 is determined by integrating the reconnection electric field along this merging line.

$$262 \quad \begin{aligned} \phi_{12}(t) &= \frac{dF_{12}(t)}{dt} \\ 263 \quad &= \int_{P_1}^{P_2} E_{rec}(s, t) ds \\ 264 \quad &= \int_{P_1}^{P_2} B_z(s) \left[ \left( \mathbf{V}(s, t) - \frac{d\mathbf{P}(s, t)}{dt} \right) \cdot \hat{\mathbf{N}}(s, t) \right] ds \end{aligned} \quad (8)$$

265 Typically, reconnection at the magnetopause increases open magnetic flux whereas  
266 reconnection in the magnetotail decreases open flux. Consequently the total globally-  
267 integrated reconnection rate in the magnetospheric system is given by the rate of change

268 of open magnetic flux in the polar cap

$$269 \quad \frac{dF_{pc}}{dt} = B_i \frac{dA_{pc}}{dt} = \phi_d + \phi_n \quad (9)$$

270 where  $\phi_d$  and  $\phi_n$  are the total reconnection voltages along the magnetopause and magne-  
 271 totail X-lines, respectively, and  $A_{pc}$  is the area of open flux in the ionosphere. Measuring  
 272 the reconnection rate from the ionosphere offers the advantages that  $A_{pc}$  is minimized  
 273 and  $B_i$  is approximately constant and hence can be described by a static empirical model.  
 274 Thus, by measuring changes in polar cap area, the measurement of either of the magne-  
 275 topause or magnetotail reconnection voltages allows estimation of the other [*Milan et al.*,  
 276 2003].

### 277 2.1.2. Discrete formulation

278 Actual measurements of the convection velocity ( $\mathbf{V}$ ) and the reconnection separatrix  
 279 position in the ionosphere ( $\mathbf{P}$ ) typically comprise sparse discrete observations, rather than  
 280 continuous functions. Consequently, for practical purposes we rewrite (7) in a discrete  
 281 form as,

$$282 \quad E_{rec_i}(t) = B_{z_i} [(\mathbf{V}_i(t) - \mathbf{V}_{\mathbf{P}_i}(t)) \cdot \hat{\mathbf{N}}_i(t)] \quad (10)$$

283 where subscript  $i$  refers to a discrete velocity vector measurement and where the motion  
 284 of the separatrix has been simplified as  $\mathbf{V}_{\mathbf{P}_i}$  (the meridional component of the separatrix  
 285 velocity at the location of velocity vector  $i$ ). For ease of calculation we rewrite this as,

$$286 \quad E_{rec_i}(t) = B_{z_i} [|\mathbf{V}_i(t)| \cos \theta_i(t) - |\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t)] \quad (11)$$

287 where  $\theta_i$  is the angle between the velocity vector and the normal to the separatrix and  $\alpha_i$   
 288 is the angle between the meridional direction and the normal to the separatrix. Hence,  
 289 estimates of the reconnection rate require measurements of the vertical magnetic field

290 strength, the separatrix location and motion, and the convection velocity. The magnetic  
 291 field strength varies little in the incompressible ionosphere and so values from the Altitude-  
 292 Adjusted Corrected Geomagnetic (AACGM) field model [*Baker and Wing, 1989*] can be  
 293 assumed. The AACGM model is also used as the geomagnetic coordinate system in this  
 294 analysis.

295 Generally, our discrete measured velocity vectors will not be co-located with the mea-  
 296 sured separatrix location. Hence, we consider velocity vectors close to the separatrix to  
 297 be the best estimate of the velocity field at the separatrix. Typically, those within half  
 298 the latitudinal resolution of the velocity measurements are most suitable. Fig.4 presents  
 299 a basic schematic representation of the scenario at each discrete measurement point  $i$ .  
 300 Figure 4a presents an example scenario of the actual measured quantities. We have suit-  
 301 able velocity vectors  $\mathbf{V}_i = \mathbf{V}(\lambda_i, \phi_i)$  at  $N$  discrete locations with AACGM latitude  $\lambda_i$   
 302 and AACGM longitude  $\phi_i$  ( $i = 1 \dots N$ ) and separatrix identifications  $\mathbf{P}_j = \mathbf{P}(\lambda_j, \phi_j)$  at  
 303  $M$  discrete positions with AACGM latitude  $\lambda_j$  and AACGM longitude  $\phi_j$  ( $j = 1 \dots M$ ).  
 304 Figure 4b shows the derived quantities that are used as input to equation (11) for the  
 305 same example as in fig.4a. For each velocity vector we assume that the measured velocity  
 306 is a good approximation for the velocity at the separatrix at the same AACGM longitude.  
 307  $\mathbf{P}_i$  is an estimate of the separatrix position at AACGM longitude  $\phi_i$ , the latitude of which  
 308 can be approximated by the linear interpolation of neighbouring separatrix measurements  
 309  $(\lambda_{j_1}, \phi_{j_1})$  and  $(\lambda_{j_2}, \phi_{j_2})$ ,

$$310 \quad \lambda(\mathbf{P}_i) = \lambda_{j_1} + \left( \frac{\lambda_{j_2} - \lambda_{j_1}}{\phi_{j_2} - \phi_{j_1}} \right) (\phi_i - \phi_{j_1}) \quad (12)$$

311 If the discrete separatrix points are not too far apart then we can assume a locally linear  
 312 approximation. Therefore, the angle  $\alpha_i = \alpha(\mathbf{P}_i)$  between the normal to the separatrix

313 and the meridional direction can be given as,

$$314 \quad \alpha_i = \tan^{-1} \left[ \frac{\lambda_{j_2} - \lambda_{j_1}}{(\phi_{j_2} - \phi_{j_1}) \cos \lambda_{j_2}} \right]. \quad (13)$$

315 Alternatively,  $\lambda(\mathbf{P}_i)$  and  $\alpha_i$  can be estimated by a higher order method (see section 2.3.6).

316 The angle between the velocity vector  $\mathbf{V}_i$  and the meridian direction is given by  $\theta_{\mathbf{V}_i} =$   
 317  $\theta_{\mathbf{V}}(\lambda_i, \phi_i)$ . Hence, the angle between the velocity vector and the normal to the separatrix  
 318 is given by,

$$319 \quad \theta_i = \theta_{\mathbf{V}_i} - \alpha_i \quad (14)$$

320 We assume for simplicity that the separatrix motion in the ionosphere is purely latitu-  
 321 dinal and hence the magnitude of the separatrix velocity at AACGM longitude  $\phi_i$  is given  
 322 by,

$$323 \quad |\mathbf{V}_{\mathbf{P}_i}(t)| = \frac{(R_E + h) [\lambda(\mathbf{P}_i(t)) - \lambda(\mathbf{P}_i(t - \Delta t))]}{\Delta t} \quad (15)$$

324 where  $R_E$  is the radius of the Earth,  $h$  is the altitude of the observations, and  $\Delta t$  is the  
 325 time between successive separatrix estimates.

326 Entering single point measurements into (11) allows us to make localised estimates of  
 327 the reconnection electric field [*Pinnock et al.*, 1999; *Blanchard et al.*, 2001]. However, if we  
 328 wish to determine the spatiotemporal structure of the electric field or make an estimate of  
 329 the reconnection voltage along a merging line, we need to make as many measurements as  
 330 possible along the merging line. If we assume  $N_{vec}$  discrete velocity vector measurements  
 331 along a merging line, the total rate of flux transfer, or reconnection voltage, for that  
 332 merging line can be estimated from,

$$333 \quad \phi_{rec}(t) = \sum_{i=1}^{N_{vec}} E_{rec_i}(t) \Delta s_i(t) \quad (16)$$

where  $\Delta s_i(t)$  represents the length of the separatrix portion at measurement location  $i$ , which for closely-spaced measurements can be approximated by,

$$\Delta s_i(t) \approx \left( \frac{|\mathbf{P}_{i+1}(t) - \mathbf{P}_{i-1}(t)|}{2} \right) \quad (17)$$

### 2.1.3. Error analysis

In order to gain a quantitative feel for reconnection rate estimates we need to have an appreciation of the uncertainties in the measured quantities. We can estimate the uncertainty, or error, in a single measurement of the reconnection electric field at measurement point  $i$  as,

$$\varepsilon \langle E_{rec_i}(t) \rangle \approx B_{z_i} \left( \varepsilon \langle |\mathbf{V}_i(t)| \cos \theta_i(t) \rangle^2 + \varepsilon \langle |\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t) \rangle^2 \right)^{\frac{1}{2}} \quad (18)$$

where  $\varepsilon \langle x \rangle$  represents the uncertainty in the measurement of parameter  $x$ . (This representation assumes that the uncertainty in the magnetic field ( $\varepsilon \langle B_{z_i} \rangle$ ) is negligible.) This uncertainty should only be viewed as an estimate as strictly the formulation requires that  $|\mathbf{V}_i(t)| \cos \theta_i(t)$  and  $|\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t)$  are independent and uncorrelated. This is not strictly true since both have some dependence on the normal to the separatrix ( $\hat{\mathbf{N}}_i(t)$ ). From (18), the uncertainty in  $E_{rec_i}(t)$  is dependent on: (1)  $\varepsilon \langle |\mathbf{V}_i(t)| \cos \theta_i(t) \rangle$ , the uncertainty in the convection velocity measurement, and (2)  $\varepsilon \langle |\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t) \rangle$ , the uncertainty in the measurement of the separatrix motion.

The uncertainty in the convection velocity measurement can be approximated as,

$$\varepsilon \langle |\mathbf{V}_i(t)| \cos \theta_i(t) \rangle \approx \left( \cos^2 \theta_i(t) \varepsilon \langle |\mathbf{V}_i(t)| \rangle^2 + |\mathbf{V}_i(t)|^2 \sin^2 \theta_i(t) \varepsilon \langle \theta_i(t) \rangle^2 \right)^{\frac{1}{2}} \quad (19)$$

which again assumes that the uncertainties in  $|\mathbf{V}_i(t)|$  and  $\theta_i(t)$  are independent and uncorrelated. The uncertainties in the velocity magnitude ( $\varepsilon \langle |\mathbf{V}_i(t)| \rangle$ ) and in the angle that the velocity vector makes with the separatrix normal ( $\varepsilon \langle \theta_i(t) \rangle$ ) are inherently difficult to

356 estimate and depend largely on the technique being employed to determine the convection  
 357 velocity. However, it is possible to simplify our uncertainty estimates to allow a rough  
 358 estimate of the level of uncertainty. If we assume that the uncertainty in the velocity  
 359 magnitude is proportional to the magnitude ( $\varepsilon\langle|\mathbf{V}_i(t)|\rangle = a_1|\mathbf{V}_i(t)|$ , where  $a_1$  is a con-  
 360 stant), and that the uncertainty in the angle can be given by  $\varepsilon\langle\theta_i(t)\rangle = a_2$  (where  $a_2$  is in  
 361 radians), then the uncertainty in the convection velocity measurement can be rewritten  
 362 as,

$$363 \quad \varepsilon\langle|\mathbf{V}_i(t)| \cos \theta_i(t)\rangle \approx |\mathbf{V}_i(t)| \left[ a_1^2 \cos^2 \theta_i(t) + a_2^2 \sin^2 \theta_i(t) \right]^{\frac{1}{2}}. \quad (20)$$

364 To illustrate the range of possible uncertainties we consider the limits of equation (20): If  
 365  $\theta_i(t) = 0^\circ$  (the velocity vector is perpendicular to the separatrix), equation (20) reduces  
 366 to,

$$367 \quad \varepsilon\langle|\mathbf{V}_i(t)| \cos \theta_i(t)\rangle \approx a_1|\mathbf{V}_i(t)| \quad (21)$$

368 which implies that the uncertainty relates solely to the uncertainty in the velocity vector  
 369 magnitude. If  $\theta_i(t) = 90^\circ$  (the velocity vector is parallel to the separatrix), this reduces  
 370 to,

$$371 \quad \varepsilon\langle|\mathbf{V}_i(t)| \cos \theta_i(t)\rangle \approx a_2|\mathbf{V}_i(t)| \quad (22)$$

372 which implies that the uncertainty relates solely to the uncertainty in the direction of the  
 373 velocity vector.

374 The uncertainty in the separatrix motion at a measurement point,  $i$ , can be given by,

$$375 \quad \varepsilon\langle|\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t)\rangle \approx \left( \cos^2 \alpha_i(t) \varepsilon\langle|\mathbf{V}_{\mathbf{P}_i}(t)|\rangle^2 + |\mathbf{V}_{\mathbf{P}_i}(t)|^2 \sin^2 \alpha_i(t) \varepsilon\langle\alpha_i(t)\rangle^2 \right)^{\frac{1}{2}} \quad (23)$$

376 Hence, this uncertainty can be written in terms of the uncertainty in the difference in  
 377 the temporal separatrix positions, and the uncertainty in the angle that the separatrix

normal makes with the meridional direction. If we make the assumption that both  $\alpha_i(t)$  and  $\varepsilon\langle\alpha_i(t)\rangle$  are likely to be small (i.e., the separatrix normal will be aligned close to the meridional direction and is likely to be well defined), then we can simplify (23) to,

$$\varepsilon\langle|\mathbf{V}_{\mathbf{P}_i}(t)| \cos \alpha_i(t)\rangle \approx \varepsilon\langle|\mathbf{V}_{\mathbf{P}_i}(t)|\rangle = \frac{1}{\Delta t}(R_E + h)\varepsilon\langle\lambda(\mathbf{P}_i(t)) - \lambda(\mathbf{P}_i(t - \Delta t))\rangle \quad (24)$$

Hence, the uncertainty depends heavily on  $\Delta t$ . As the temporal resolution of the measurements increases ( $\Delta t$  decreases) the uncertainty in the separatrix motion will increase. Hence, increasing the time resolution of measurements requires an increase in the accuracy of the separatrix measurements to keep the level of uncertainty low. The uncertainty in the difference in the separatrix positions is heavily dependent on the spatial resolution of the measurement technique.

## 2.2. Measuring the ionospheric convection velocity field

A complete picture of the reconnection scenario requires continuous and extensive measurement of the ionospheric convection velocity in space and time. At present, there are two techniques in regular use which can provide such a picture of the convection velocity field across the complete polar ionosphere.

(1) The Assimilative Mapping of Ionospheric Electrodynamics (AMIE) technique. AMIE is an inversion technique used to derive the mathematical fields of physical variables for the global ionosphere at a given time from spatially irregular measurements of these variables or related quantities [Richmond and Kamide, 1988]. The field variables are the electrostatic potential, electric field, height-integrated current density and conductivity, and field-aligned current density at a given height. Measurements are made by magnetometers on the ground and on low-altitude satellites, ground-based radars, plasma drift

399 and particle detectors on low-altitude satellites, and optical instruments on the ground  
400 and on satellites.

401 (2) The SuperDARN Global Convection Mapping (or Map Potential) technique. Super-  
402 DARN global convection maps are produced by fitting line-of-sight velocity information  
403 measured by the SuperDARN radars to an expansion of an electrostatic potential function  
404 expressed in terms of spherical harmonics [Ruohoniemi and Baker, 1998]. This method  
405 uses all of the available line-of-sight velocity data from the SuperDARN HF radar network.  
406 It can also accept ion drift velocity data from low-altitude spacecraft as input.

407 *Lu et al.* [2001] showed that convection maps derived using the AMIE and SuperDARN  
408 global convection mapping techniques, using the same radar data as input, were nearly  
409 identical over areas of extensive radar coverage. However, significant differences arose  
410 where data were sparse or absent because different statistical models were used by each  
411 technique to constrain the global solution in these regions. Furthermore, they derived  
412 AMIE convection maps using SuperDARN radar data and magnetometer data separately,  
413 the coverage of which was concentrated in different regions. These also showed significant  
414 differences in regions where data were sparse or absent in one or other data set and values  
415 of the cross-polar cap potential that differed by  $\sim 65\%$ . We are aware of only two studies in  
416 which the AMIE technique has been used to identify the reconnection separatrix [Taylor  
417 *et al.*, 1996] and the flow across it [Lu *et al.*, 1995] whereas SuperDARN global convection  
418 mapping has regularly been used for these purposes [Pinnock *et al.*, 2003; Milan *et al.*,  
419 2003; Chisham *et al.*, 2004b; Hubert *et al.*, 2006].

420 For the event study in this paper we use the SuperDARN global convection mapping  
421 technique to provide our estimate of the ionospheric convection velocity field, because it is

422 specifically designed to measure the convection electric field. Full details of the technique  
423 (and the data-preprocessing it requires) can be found in *Ruohoniemi and Baker* [1998],  
424 *Shepherd and Ruohoniemi* [2000], *Chisham and Pinnock* [2002], and *Chisham et al.* [2002].  
425 The technique provides an estimate of the convection potential ( $\Phi(\lambda, \phi)$ ) and electric field  
426 ( $E = -\nabla\Phi(\lambda, \phi)$ ) across the whole polar ionosphere in the Earth's rest frame and can  
427 be used to study large-scale characteristics (e.g., the cross-polar cap potential [*Shepherd*  
428 *and Ruohoniemi, 2000*]) or mesoscale features (e.g., flow vortices, convection reversal  
429 boundaries [*Huang et al., 2000*]). The scale of resolvable structure is limited by the order  
430 of the spherical harmonic fit and the grid cell size of the radar measurements. In practice,  
431 the technique is generally not suitable for small-scale structure ( $< \sim 100$  km - the basic grid  
432 cell size). The analytical solution for the convection electric field can be used to determine  
433 the reconnection rate at all points on the merging lines [*Milan et al., 2003; Hubert et al.,*  
434 *2006*]. However, the accuracy of these estimates is likely to be poor in regions with no  
435 SuperDARN data. We recommend that reconnection rates are only determined in regions  
436 where SuperDARN data have contributed to the global convection electric field solution.

437 Whereas a solution is provided for the convection electric field across the whole polar  
438 ionosphere, velocity vectors are only determined in regions where SuperDARN backscatter  
439 have contributed to the fitting process. At these locations, the global convection mapping  
440 technique provides two alternative methods for determining velocity vectors, which have  
441 been termed 'fit' and 'true' vectors.

442 'Fit' velocity vectors represent the  $\mathbf{E} \times \mathbf{B}$  drift velocities of the convection electric field  
443 solution at each grid cell  $(\lambda_i, \phi_i)$  which contributed line-of-sight velocity information to

444 the mapping process and are hence given by

$$445 \quad \mathbf{V}_{fit}(\lambda_i, \phi_i) = \frac{-\nabla\Phi(\lambda_i, \phi_i) \times \mathbf{B}(\lambda_i, \phi_i)}{|\mathbf{B}(\lambda_i, \phi_i)|^2}. \quad (25)$$

446 The fit vectors are always tangential to equipotentials of the convection electric field  
 447 solution and are divergence-free. However, the fit vector is often inconsistent with the  
 448 corresponding line-of-sight velocity measured by radar  $r$  in that grid cell ( $\mathbf{V}_{los}(\lambda_i, \phi_i, r)$ ),  
 449 as the fit vector is determined by the global solution and not solely the local observations.  
 450 The correlation between the two becomes better as the order of the spherical harmonic  
 451 fit is increased and more of the mesoscale variations in the velocity measurements can be  
 452 fitted to.

453 ‘True’ velocity vectors represent a combination of the line-of-sight velocity measured at  
 454 each grid cell with the component of the fit velocity vector which is perpendicular to the  
 455 line-of-sight direction and are hence given by

$$456 \quad \mathbf{V}_{true}(\lambda_i, \phi_i, r) = |\mathbf{V}_{fit}(\lambda_i, \phi_i) \times \hat{\mathbf{V}}_{los}(\lambda_i, \phi_i, r)| \left( \hat{\mathbf{V}}_{los}(\lambda_i, \phi_i, r) \times \hat{\mathbf{z}} \right) + \mathbf{V}_{los}(\lambda_i, \phi_i, r) \quad (26)$$

457 The true vectors typically provide a better mesoscale representation of the ionospheric  
 458 convection flows [*Chisham et al.*, 2002; *Provan et al.*, 2002]. For this reason, some pre-  
 459 vious studies which have used SuperDARN global convection mapping to determine the  
 460 reconnection electric field [*Pinnock et al.*, 2003; *Chisham et al.*, 2004b] have used true  
 461 vectors, and we will do so here. However, the true vector velocity field is not guaranteed  
 462 to be divergence free and there is also the possibility of an ambiguity in the true vector  
 463 magnitude and direction if a grid cell contains line-of-sight velocity information from more  
 464 than one SuperDARN radar. As the goodness of the spherical harmonic fit increases, the  
 465 true vectors become increasingly closer to agreement with the fit vectors.

466 Figure 5 presents the northern hemisphere convection map for a 1-minute interval (2017–  
467 2018 UT) on 26 December 2000 determined using the SuperDARN global convection  
468 mapping technique. The velocity vectors are true vectors, with a length proportional  
469 to the velocity magnitude. The equipotential contours of the solution ( $\Phi(\lambda, \phi)$ ) which  
470 results from the spherical harmonic fitting are shown by the dashed (morning convection  
471 cell) and dotted (afternoon convection cell) contour lines. The spatial coverage of the  
472 vectors highlights the region of the convection map where actual SuperDARN data exist.  
473 The equipotential contours in regions where no data exist are heavily influenced by data  
474 from the statistical model of *Ruohoniemi and Greenwald* [1996] and hence only provide a  
475 statistical estimate of the true convection in these regions. However, the model does serve  
476 to constrain the spherical harmonic fit to provide a realistic estimate of convection at the  
477 boundaries of the measured data set. In the example event studied in this paper we only  
478 estimate reconnection rates in regions where we have measured true velocity vectors.

479 The SuperDARN global convection mapping technique often provides an extensive rep-  
480 resentation of the convection electric field as shown in figure 5. However, uncertainties in  
481 the magnitude and direction of the velocity vectors are not readily expressed. There are  
482 a number of aspects of the technique which introduce uncertainty into the output (aside  
483 from the uncertainties in the input line-of-sight velocity values), as discussed below:

484 (1) Before processing the data for a particular interval, the line-of-sight velocities are  
485 generally median filtered, both spatially (across a  $\sim 100$  km square grid cell) and tempo-  
486 rally (across three successive radar scans -  $\sim 3$ -6 min) to increase the statistical significance  
487 of the output. Hence, localized or short bursts of strong flow on these scales can be par-

488 tially averaged away. This will ultimately lead to some smoothing of the spatial and  
489 temporal reconnection rate variations.

490 (2) The least-squares fitting is dependent on two user-selected parameters; (i) the order  
491 of the spherical harmonic fit, and (ii) the spatial region over which the fit is performed  
492 (primarily the low-latitude boundary of ionospheric convection). Variations in these fit  
493 parameters lead to differences in the final solution [*Ruohoniemi and Baker, 1998; Shepherd*  
494 *and Ruohoniemi, 2000*]. Higher order fits produce convection maps that better match the  
495 line-of-sight velocity input, but which have lower statistical significance.

496 (3) Pre-inspection of the data can be important if the determination of mesoscale fea-  
497 tures of convection is required. Care must be taken to ensure that all the backscatter being  
498 used in the convection mapping process has arisen from  $F$ -region irregularities moving un-  
499 der the influence of the convection electric field. Presently, some ground and  $E$ -region  
500 backscatter typically remain after default preprocessing of the SuperDARN data. This  
501 can increase the uncertainties in the reconnection rate calculations. These uncertainties  
502 can be reduced by careful inspection of the line-of-sight velocity data and by filtering  
503 the data in range gate-velocity space to remove non- $F$ -region data before applying the  
504 mapping technique [*Chisham and Pinnock, 2002*].

### 2.3. Identifying the location and motion of the reconnection separatrix

505 The ionospheric footprint of the reconnection separatrix (the merging line) is usually  
506 determined using well-established proxies. The reliability of these proxies is variable and is  
507 affected by IMF variations, geomagnetic conditions, and spatial location in the ionosphere.  
508 During intervals when reconnection is occurring on the lobe magnetopause, i.e., when the  
509 IMF is close to being northward directed (IMF  $B_z > 0$ ;  $B_y \sim 0$ ), the dayside merging line

510 typically lies some distance poleward of the OCB, within the polar cap. In this paper we  
511 only consider intervals where reconnection is occurring on regions of the magnetopause  
512 sunward of the magnetospheric cusps (i.e., when the IMF is not strongly northward), and  
513 hence when the dayside merging line is co-located with the OCB [*Cowley and Lockwood,*  
514 1992]. In the nightside ionosphere the reconnection separatrix for far-tail reconnection is  
515 always co-located with the OCB. Hence, for most conditions and locations we are trying  
516 to measure proxies for the OCB. The methodology presented here is still applicable to the  
517 estimation of reconnection rates away from the OCB (such as at the ionospheric footprint  
518 of lobe reconnection during northward IMF conditions [*Chisham et al., 2004b*], or at the  
519 ionospheric footprint of the near-Earth neutral line in the tail), but the identification of  
520 the reconnection separatrix in these cases is less established, as will be discussed in section  
521 4.

### 522 **2.3.1. Particle precipitation boundaries**

523 The high-latitude ionosphere, through its magnetic connection to the outer magneto-  
524 sphere, provides an image of magnetospheric regions and boundaries and the physical  
525 processes occurring there. From numerous observations made by the DMSP low-altitude  
526 satellites, the energy spectra of precipitating ions and electrons have been categorised  
527 into different types. These types correspond to different plasma regions in the Earth's  
528 magnetosphere whose ionospheric footprints can consequently be identified in an objec-  
529 tive way [*Newell et al., 1991; Newell and Meng, 1992; Newell et al., 1996*]. Some plasma  
530 regions are typically located on open magnetic field lines and others on closed [*Sotirelis*  
531 *and Newell, 2000*] and hence, one can use these low-altitude measurements to identify  
532 the OCB location. In the dayside ionosphere, the OCB is best identified by a transi-

tion between the precipitation regions typically thought to be associated with open (i.e.,  
cusp, mantle, polar rain) and closed (i.e., central plasma sheet, boundary plasma sheet,  
low-latitude boundary layer) field lines [Newell *et al.*, 1991]. In the nightside ionosphere,  
the best OCB proxy is the b6 precipitation boundary [Newell *et al.*, 1996] which marks  
the poleward edge of the sub-visual drizzle region. As discussed earlier, there are times  
when the OCB is not co-located with the separatrix. In these cases the magnetopause  
reconnection separatrix can be identified by the high-energy edge of velocity dispersed ion  
precipitation [Rosenbauer *et al.*, 1975; Hill and Reiff, 1977; Burch *et al.*, 1980].

Relative to other ionospheric proxies, low-altitude spacecraft particle precipitation ob-  
servations provide a more direct measurement of the reconnection separatrix in the iono-  
sphere. However, they only provide limited point measurements of the boundary location  
as the spacecraft pass across each of the polar regions once in their orbits (typically  $\sim 100$ -  
min for DMSP spacecraft). Nevertheless, as the most reliable boundary indicators they  
have an important role in calibrating other proxies, both in single event studies, and on a  
more statistical basis. The following sections discuss some of these large-scale statistical  
calibrations.

### 2.3.2. Auroral observations

When magnetospheric particles precipitate into the denser regions of the lower iono-  
sphere they collide with other particles to give off light, causing the aurora. The intensity  
and wavelength of auroral emissions depends partially on the flux, energy and species  
of the precipitating particles, which is different on either side of the OCB as discussed  
above. These auroral emissions can be detected with both ground-based and space-based  
imagers. Observations of the aurora, particularly in the visible and ultraviolet (UV)

556 frequency bands, provide information about the geographical distributions of the precip-  
557 itating particles and their source regions.

558 Auroral observations are made from the ground using all-sky cameras and photometers.  
559 The altitude from which most auroral luminosity is emitted is  $\sim 110$  km (the ionospheric  $E$ -  
560 region) [Rees, 1963], and therefore the greatest distance at which aurora can theoretically  
561 be observed (the viewing horizon) is slightly over 1000 km. In practice, the effects of  
562 landscape, vegetation, and optical effects at low elevation angles reduce this viewing  
563 horizon to  $\sim 300$  km. Ground observations can achieve high spatial resolution at the  
564 zenith of the camera, but the resolution drops sharply towards the edges of the field-  
565 of-view. The temporal resolution of observations can be very high, though is typically  
566  $\sim 1$  min. Uncertainties in the altitude of the auroral emission can lead to inaccuracies in  
567 mapping the observations to a geographical grid, and these uncertainties increase away  
568 from the zenith. Ground-based cameras cannot make observations in inclement weather,  
569 nor when the sun is up or during full moon. Consequently, study of the dayside auroral  
570 oval is limited to a short observational window (a few weeks) near winter solstice, from  
571 restricted locations (e.g. Svalbard in the northern hemisphere).

572 Auroral observations by spacecraft have a potentially complete field-of-view of a single  
573 hemisphere. Satellite-based imagers, such as Polar UVI [Torr *et al.*, 1995], can image the  
574 aurora over an entire polar ionosphere at low spatial resolution ( $\sim 30$  km square at orbit  
575 apogee) with better than 1-min temporal resolution for prolonged periods of  $\sim 9$  hours  
576 per 18-hour orbit. A major advantage of spacecraft imagers is the ability to measure  
577 UV emissions, which cannot be detected at the ground due to atmospheric absorption.

578 UV imagers have the advantage of being able to make observations in sunlight, although  
579 dayglow can dominate over the auroral emission at times.

580 An understanding of the particle precipitation giving rise to the observed auroral lumi-  
581 nosity allows the probable source regions, and hence the boundaries between regions, to  
582 be identified. The more energetic (harder) particles typical of the outer magnetosphere  
583 penetrate more deeply into the atmosphere before dissipating their energy than the less  
584 energetic (softer) particles found, for example, in the magnetosheath [e.g., *Rees*, 1963]. In  
585 the dayside ionosphere the OCB is often identified on the ground as the poleward edge of  
586 luminosity dominated by green-line emissions (557.7 nm - characteristic of the *E*-region)  
587 resulting from harder precipitation in the magnetosphere and the equatorward edge of  
588 red-line dominated luminosity (630.0 nm - characteristic of the *F*-region) resulting from  
589 softer magnetosheath precipitation [*Lockwood et al.*, 1993]. The ratio of the luminosity  
590 of the red- and green-lines at a certain location gives an indication of the characteris-  
591 tic energy of the precipitating particles. In the nightside ionosphere, both the red- and  
592 green-line emissions correspond to precipitation on closed field lines and the open field line  
593 region is typically void of auroral emissions. Thus the OCB is identified as the poleward  
594 boundary of either of these emissions, although the red line is thought to be the best  
595 indicator [*Blanchard et al.*, 1995].

596 Space-based observations have been made in a range of UV wavelength bands. Al-  
597 though the auroral oval is typically clearly displayed at most UV wavelengths, it is not a  
598 trivial task to determine the OCB from these images. It is uncertain whether the OCB  
599 corresponds best to an absolute auroral intensity threshold or to a fraction of a maximum  
600 intensity. There have been few inter-instrument comparisons which have addressed this

601 uncertainty. However, a comprehensive comparison of Polar UVI and DMSP particle pre-  
602 cipitation boundaries by *Carbary et al.* [2003], using images in the Lyman-Birge-Hopfield  
603 long (LBHL) auroral emission band ( $\sim 160\text{-}180$  nm), showed that the poleward edge of  
604 the auroral oval in the dayside ionosphere was co-located with the OCB. (The intensity  
605 in the LBHL band is considered to be proportional to the energy flux of precipitating  
606 electrons [*Germany et al.*, 1997].) The method of *Carbary et al.* [2003] fits a Gaussian  
607 plus a background quadratic function to a latitudinal profile of the UVI-LBHL auroral  
608 image intensity in a 1-hr MLT bin, and then locates the boundary estimate at a fixed  
609 point on this function (at a distance equivalent to the full-width-at-half-maximum of the  
610 Gaussian poleward of the Gaussian peak). The LBHL boundary also matches well to the  
611 OCB for much of the nightside ionosphere, although an offset ( $\sim 3^\circ$ ) exists in the early  
612 morning sector [*Kauristie et al.*, 1999; *Baker et al.*, 2000; *Carbary et al.*, 2003]. In this sec-  
613 tor, the poleward boundary of shorter wavelength UV emissions in the 130-140 nm range  
614 appears to provide a more reliable proxy for the OCB [*Wild et al.*, 2004]. During active  
615 geomagnetic conditions, such as the substorm expansion phase, the nightside boundary is  
616 relatively clear, as the substorm auroral bulge is a well-defined feature that can be readily  
617 identified in auroral imagery. During more quiescent times, however, the nightside oval  
618 can become relatively faint, such that it is difficult to identify the poleward edge of the  
619 oval with any great certainty. At these times, the accuracy of the OCB determination  
620 will depend on the sensitivity of the auroral imager.

621 For our example event study we use the OCB proxy identified in auroral images mea-  
622 sured by Polar UVI in the LBHL emission range. Suitable ground-based auroral obser-  
623 vations were not available for this interval. In fig.6 we show the auroral image measured

624 by Polar UVI-LBHL at 2017:34 UT on 26 December 2000 (overlapping the time interval  
625 of the convection map shown in fig.5). The orbital position of the polar spacecraft means  
626 that the image coverage is restricted predominantly to the nightside auroral oval. The  
627 viewing angle of the spacecraft at this time is such that the resolution in the morning  
628 sector is poorer, and hence more uncertainties will be introduced here. The auroral oval  
629 is clearly visible, being characterised by the higher intensity emissions. The UVI proxy  
630 for the OCB is determined by averaging the image intensities measured in  $1^\circ$  latitude by  
631 1-hr MLT sectors and then using the method of *Carbary et al.* [2003], fitting a function  
632 to the latitudinal intensity profiles, as discussed above.

633 Figure 7 presents examples of these fits from the 0100-0200, 1800-1900, and 2300-2400  
634 MLT sectors (those regions marked with the blue radial lines in fig.6). The top two pan-  
635 els illustrate locations where the fit (dotted line) to the auroral intensity profile (solid  
636 histogram) is very good, although in one case the auroral region covers a much larger  
637 latitudinal range than the other. The boundaries determined in these cases (dashed ver-  
638 tical line) appear reasonable and would match closely with other boundary determination  
639 methods. In the final panel the intensity variation appears double-peaked and so the fit is  
640 not so good (although the fit does pass the quality controls set by *Carbary et al.* [2003]).  
641 As a result, the boundary is placed at a slightly higher latitude than may result from  
642 other techniques. This highlights that this technique has a weakness when the latitudinal  
643 intensity profile is characterised by more than one peak. A more sophisticated technique  
644 which is suitable for fitting more than one peak may be an improvement on this method.  
645 Notwithstanding this potential weakness in this technique, we still use this method of

646 boundary determination in this paper as it is the only one which has been calibrated with  
647 an independent OCB data set.

648 The boundaries determined in this way are shown as black symbols in fig.6. We further  
649 use the statistical boundary offsets determined by *Carbary et al.* [2003] to adjust our  
650 measured boundaries to provide more accurate estimates of the OCB. (This is especially  
651 significant for the measurements in the early morning sector ionosphere). The adjusted  
652 boundaries are shown as red symbols in fig.6. Hence, the UVI observations at this time  
653 provide us with OCB estimates across much of the nightside ionosphere. However, they  
654 provide no information about the OCB in the 0700–1700 MLT range.

### 655 **2.3.3. The Doppler spectral width boundary**

656 The Doppler spectral width of backscatter measured by the SuperDARN HF radar net-  
657 work is a parameter that reflects the spatial and temporal structure of ionospheric elec-  
658 tron density irregularities convecting in the ionospheric convection electric field [*André*  
659 *et al.*, 2000]. As with precipitating particles and auroral observations, the spectral width  
660 varies between regions of different magnetic connectivity and hence across the recon-  
661 nexion separatrix/OCB, although the physical reasons for these variations are not yet fully  
662 understood [*Ponomarenko and Waters*, 2003]. *Baker et al.* [1995] first showed that re-  
663 gions of enhanced Doppler spectral width were associated with regions of cusp particle  
664 precipitation and that the spectral width was reduced equatorward of the cusp. The tran-  
665 sition between these low and high spectral width regions has been termed the spectral  
666 width boundary (SWB) and has subsequently been shown to be a typical feature at all  
667 MLTs and not just in the cusp regions [*Chisham and Freeman*, 2004]. If the SWB was  
668 co-located with the OCB at all MLTs then the extensive spatial and temporal coverage

669 of the SuperDARN radars would allow for the possibility of prolonged monitoring of the  
670 separatrix location and motion. However, methods of detection of the SWB and a full  
671 understanding of how the boundary relates to the OCB have a history of confusion with  
672 conflicting conclusions drawn in different studies.

673 Threshold techniques have been employed to objectively identify the SWB in cusp-region  
674 SuperDARN backscatter for some years [*Baker et al.*, 1997; *Chisham et al.*, 2001]. These  
675 techniques involve choosing a spectral width threshold value above which the spectral  
676 width values are more likely to originate from the distribution of spectral width values  
677 typically found poleward of the OCB, and developing an algorithm that searches poleward  
678 along a radar beam until this threshold is exceeded. *Chisham and Freeman* [2003] showed  
679 that this technique can be inaccurate in its simplest form as the probability distributions  
680 of the spectral width values poleward and equatorward of the SWB are typically broad  
681 and have considerable overlap. They showed that the inclusion of additional rules in the  
682 threshold algorithm, such as spatially and temporally median filtering the spectral width  
683 data, increased the accuracy of the estimation of the SWB location. They termed their  
684 method the ‘C-F threshold technique’, and that is what we use for our example event  
685 analysis in this paper. *Chisham and Freeman* [2004] further showed that the technique  
686 could be objectively applied to SWBs at all MLTs. However, SWBs rarely approximate  
687 infinitely sharp latitudinal transitions in spectral width, and hence, the latitude of the  
688 SWB is dependent on the spectral width threshold used [*Chisham and Freeman*, 2004].

689 To investigate the reliability of the SWBs determined by this method as proxies for the  
690 OCB, *Chisham et al.* [2004a, 2005a, c] compared five years of SWBs (determined using  
691 spectral width thresholds of 150 and 200 m/s) with the particle precipitation signature

692 of the OCB measured by the DMSP low-altitude spacecraft [*Sotirelis and Newell, 2000*].  
693 These studies showed that the SWB is a good proxy for the OCB at most MLTs, with  
694 the exception being in the early morning sector (0200–0800 MLT). (Comparing with  
695 the *Carbary et al. [2003]* study, it was found that the SWB is in fact co-located with  
696 the poleward edge of the LBHL auroral oval). The SWB is most clearly observed in  
697 meridionally-aligned SuperDARN radar beams. As beams become more zonally-aligned,  
698 geometrical factors can become major causes of enhanced spectral width and so can place  
699 the SWB far equatorward of the OCB location [*Chisham et al., 2005b*].

700 For the event being studied in this paper, SWBs were available from a number of the  
701 meridionally-aligned SuperDARN radar beams. Importantly, the SWBs measured by the  
702 Kapuskasing, Kodiak, and Prince George SuperDARN radars provided estimates of the  
703 OCB in the dayside region of the ionosphere not covered by the Polar UVI observations.  
704 In fig.8 we illustrate how the C-F threshold technique estimates the SWB for one of these  
705 radars at our time of interest (2017 UT on 26 December 2000). Fig.8a presents the raw  
706 spectral width values measured by the Kapuskasing radar at this time. Only data from  
707 within  $\pm 4$  beams of the meridional direction are shown and used. The dashed meridional  
708 line shows the location of the 1500 MLT meridian. The spectral width values are highly  
709 variable and appear to be higher in the western side of the field-of-view than in the eastern.  
710 Fig.8b shows the spectral width variation at this time after the data has been spatially  
711 and temporally median filtered. The data are spatially filtered across 3 adjacent beams  
712 and temporally filtered across 5 adjacent scans, as described by *Chisham and Freeman*  
713 [2004]. In fig.8b the longitudinal change in spectral width has become clearer as well as

714 the latitudinal transition from low to high spectral width around  $73^\circ$  which provides our  
715 estimate of the OCB.

716 A threshold method is now applied to the spectral width data in fig.8b to provide our  
717 estimates for the OCB location. Fig.8c shows the result of thresholding the spectral width  
718 data at 150 m/s (the most suitable spectral width threshold value for this MLT sector).  
719 The grey region highlights where the spectral width was less than 150 m/s, the black region  
720 where it was greater than 150 m/s. The threshold technique involves searching poleward  
721 up each radar beam and finding the first range gate at which the spectral width is greater  
722 than 150 m/s and for which two of the subsequent three range gates also have spectral  
723 width values greater than 150 m/s. For this time, SWBs could only be determined for the  
724 four beams to the western side of the field-of-view. The SWB locations are highlighted  
725 by the four white squares in fig.8c. (Note that the absence of a measurable SWB on the  
726 eastern side of the field-of-view does not imply the absence of the OCB).

#### 727 **2.3.4. Other proxies**

728 Here, we briefly discuss two further proxies for the OCB that we do not make use  
729 of in the event study presented here but which are potentially useful OCB proxies for  
730 reconnection rate measurement studies.

731 The convection reversal boundary (CRB) is located where the ionospheric convection  
732 changes from being sunward (typical of closed field lines) to antisunward (typical of open  
733 field lines). If all closed field lines flowed sunward and all open field lines flowed anti-  
734 sunward then the CRB and the OCB would coincide. However, there are other factors  
735 that influence where one determines the CRB, namely the reference frame of observa-  
736 tion (corotating vs. inertial), and the effect of viscous convection cells [*Reiff and Burch,*

1985]. The change in reference frame from inertial to the corotational frame of the Super-DARN observations moves the latitude of the CRB poleward. Considering the contribution from a viscous cell would also move the CRB latitude poleward. *Newell et al.* [1991] showed that the CRB in the inertial frame in the dayside ionosphere was typically located within the LLBL, on closed field lines. *Sotirelis et al.* [2005] performed a large statistical comparison of OCB and CRB locations in the corotation frame at all MLTs and showed that the CRB correlates well with the OCB. They did identify an equatorward offset of the CRB relative to the OCB that varied from zero near noon to  $\sim 1^\circ$  near dawn and dusk and to  $\sim 2^\circ$  near midnight.

It is also possible to use incoherent scatter radar (ISR) measurements to estimate the OCB location. *Doe et al.* [1997] used ISR to measure the characteristic energies of precipitating electrons across a range of latitudes. Sharp latitudinal gradients in the characteristic energy can be used to estimate the OCB location. Latitudinal transitions in ionospheric electron density measured by ISR can also be used as OCB proxies. Particle precipitation in the auroral oval enhances the electron density in the ionosphere through enhanced ionization. In the nightside ionosphere the poleward boundary of the auroral oval is characterised by a sharp latitudinal cut-off of electron density in the E-region. This density proxy was used in estimating reconnection rates by *de la Beaujardière et al.* [1991] and *Blanchard et al.* [1997].

### 2.3.5. The effect of convection on offsetting proxies from the true separatrix

In regions where reconnection is ongoing, there is an argument as to how the effects of the convection of newly-reconnected field lines affect the reliability of the ionospheric proxies for the reconnection separatrix. It has been suggested that there typically exists a

760 small ( $<1^\circ$ ) latitudinal displacement between the true separatrix location and the proxy  
761 due to the effects of the convection of newly-reconnected field lines. In the cusp, for  
762 example, the fastest precipitating magnetosheath-like ions which characterise the newly-  
763 opened field lines take a finite time to travel from the reconnection site (assuming this to  
764 be their place of origin) to the ionosphere, during which time the footprints of the field  
765 lines down which these ions are traveling have been convected away from the separatrix  
766 location [Rodger and Pinnock, 1997; Lockwood, 1997; Rodger, 2000]. Hence, the ionospheric  
767 signature of these ions will be observed poleward of the footprint of the field line which  
768 presently connects to the reconnection X-line. Here, we assume that any offset due to  
769 these effects is smaller than the latitudinal resolution of our velocity vector measurements  
770 ( $\sim 1^\circ$  latitude).

### 771 **2.3.6. Estimating the complete separatrix location and motion from discrete** 772 **observations**

773 The instrumental techniques described above generally provide discrete measurements  
774 of the OCB location at a number of particular times and locations. For small-scale  
775 reconnection rate determinations, closely-spaced discrete measurements of the OCB can  
776 be employed using the techniques outlined in section 2.1.2. To measure the reconnection  
777 rate on a more global scale requires either global OCB measurements or some method of  
778 interpolation of sparse measurements of the OCB. The simplest assumption that can be  
779 realistically used when interpolating ionospheric OCB estimates is that the OCB can be  
780 approximated by a circle (used in calculating reconnection rates by Pinnock *et al.* [2003]).  
781 Holzworth and Meng [1975] and Meng *et al.* [1977] showed that an off-centre circle in  
782 geomagnetic co-ordinates was a good fit to the poleward boundary of quiet auroral arcs

783 and hence, provided a good global estimate of the OCB. However, if the MLT coverage  
 784 of OCB estimates is relatively extensive then there are better techniques which allow a  
 785 more accurate characterisation of the boundary.

786 It is possible to approximate the OCB in terms of a Fourier series of order  $N_t$ ,

$$787 \quad \lambda(\mathbf{P}(\phi)) = A_0 + \sum_{n=1}^{N_t} A_n \cos(n\phi + \psi_n) \quad (27)$$

788 where  $A_0$ ,  $A_n$  and  $\psi_n$  are constants of the fit. With sparse measurements of the OCB  
 789 location a global OCB estimate can be determined by least squares fitting a low order  
 790 ( $N_t < 3$ ) Fourier series to the measured OCB locations, similar to the approach taken by  
 791 Holzworth and Meng (1975) for describing the auroral oval. When estimates of the OCB  
 792 location are available from a wider range of MLTs, higher order Fourier series can be used  
 793 to better describe the data. However, fitting to such higher order Fourier series is fraught  
 794 with problems due to the many  $(2n+1)$  free parameters, and local minima in the  $2n+1$   
 795 parameter space.

796 Instead, following the example of *Milan et al.* [2003], we adopt a Fourier series derived  
 797 from a truncated Fourier transform of the estimated OCB locations. First we divide the  
 798 polar ionosphere into  $N_b$  equally sized MLT bins (the choice of  $N_b$  is typically dependent  
 799 on the spatial and temporal resolution of the available boundary data). For bins where  
 800 one or more estimates of the OCB exist we take the mean of those estimates as the OCB  
 801 location at the center of that bin ( $\lambda(\mathbf{P}_i), i = 1 \dots N_b$ ). (This can be a weighted mean  
 802 if required, e.g., if the estimates from one instrumental source are more reliable than  
 803 another). For bins where no estimate exists we interpolate between the OCB locations  
 804 on either side to obtain an estimate of the OCB location for that bin. We then take the  
 805 Fourier transform of these values and ignore the higher order terms (those greater than

806  $N_t$ , the order of the Fourier series that we require). This truncated Fourier series can then  
807 be used to define the OCB at any MLT. The reason for removing the higher order terms  
808 is that a complete Fourier series gives an exact fit to the input estimates and for locations  
809 away from the bin centres spurious results may exist (much in the same way as fitting an  
810 exact polynomial to data with uncertainties can give rise to unrealistic estimates between  
811 data points). It is worth noting that the truncated Fourier series is equivalent to a least  
812 squares fit of a Fourier series of this order.

813 As an example of this process, in fig.9 we illustrate how we determine the global OCB  
814 variation for the interval 2017–2018 UT on 26 December 2000 (the same interval as in  
815 previous figures). Often, due to the coarse latitudinal resolution of many techniques used  
816 to locate the OCB, the measurement of the OCB latitude contains significant quantization  
817 noise which is amplified when determining the time derivative for the boundary motion  
818 [Pinnock *et al.*, 1999]. Therefore, it is often advisable to temporally smooth the time series  
819 of the boundary location in some way to reduce this effect. Here, we have achieved this  
820 by mean filtering across a 3-min interval centred on our minute of interest. The squares  
821 in fig.9 show all the UVI boundaries measured for the 3-min interval centred on this time.  
822 Similarly, the diamonds show all the SWBs measured for the 3-min interval centred on  
823 this time. We take the mean latitude value in each 1-hr MLT sector to determine the  
824 global boundary (using  $N_b = 24$ ). This spatiotemporal smoothing provides a level of  
825 statistical reliability to the values used in our Fourier expansion, as well as reducing the  
826 uncertainty in our individual estimates of the boundary location (we assume this to be  
827 by a factor of  $\sqrt{N}$ , where  $N$  is the number of OCB estimates in the bin). In fig.9 we also  
828 present the results of characterising the OCB as a truncated Fourier series with  $N_t = 6$

829 (6th order - dashed line) and  $N_t = 10$  (10th order - bold solid line), as explained above.  
830 Obviously, the wider the extent of the data coverage, the higher the order of the Fourier  
831 expansion can be. In this case, where the global coverage is quite good it can be clearly  
832 seen that on the nightside, the 10th order expansion fits better to the observed data than  
833 does the 6th order. The fits to the data elsewhere are very similar for both orders. Hence  
834 we use the 10th order expansion in this study.

835 It is instructive to study how using different instrumentation, assumptions, and data  
836 resolution affects the velocity of the OCB that we ultimately determine and use in the  
837 reconnection rate calculations. One way to study this is to look at the distributions of  
838 the boundary velocities that we observe in different cases. In fig.10a we show boundary  
839 velocity distributions determined from the raw Polar UVI observations for our complete  
840 event interval (2000-2200 UT). The solid line shows the distribution of boundary velocities  
841 determined using temporally adjacent boundary measurements (every  $\sim 37$  s). Any effects  
842 due to noise/random errors in the determination of the OCB latitude from the UVI data  
843 will be clearest in this distribution (i.e., the uncertainties will be largest, equation (24)).  
844 The distribution is very broad with significant numbers of velocities with magnitudes  
845 of  $\sim 4000$  m/s or higher (this velocity is equivalent to  $\sim 2^\circ$  latitude in a minute). The  
846 dashed line shows the distribution of boundary velocities determined using measurements  
847 that are 2 samples apart (every  $\sim 74$  s). It is clear that the width of the distribution  
848 has been reduced. Similarly, the dotted line shows the distribution of boundary velocities  
849 determined using measurements that are 4 samples apart (every  $\sim 148$  s). Again, the width  
850 of the distribution has been reduced such that there are very few boundary velocities  
851 measured greater than  $\sim 2000$  m/s. This figure shows how data of different temporal

852 resolution, from the same data set, will provide a very different distribution of boundary  
853 velocities.

854 In fig.10b we show boundary velocity distributions determined from the filtered Polar  
855 UVI observations for the complete event interval (2000-2200 UT). The solid line shows the  
856 distribution of boundary velocities when using the mean-filtered UVI data (3-min averag-  
857 ing window at 1-min resolution). The filtering has the effect of thinning the distribution  
858 in a similar way to a reduction in the temporal resolution. This is a result of the reduction  
859 of the effects of noise and random errors in the data following this averaging process (as  
860 well as the reduction of genuine rapid, large amplitude fluctuations). The dashed and  
861 dotted lines in fig.10b present the boundary velocity distributions determined from the  
862 6th and 10th order Fourier series OCBs, respectively. These two distributions are almost  
863 identical and hence there is no sign of an enhanced level of fluctuations being introduced  
864 for the higher order Fourier series. This further supports our use of the 10th order Fourier  
865 expansion in this study.

866 As discussed in section 2.1.1, the variation in the polar cap area provides information  
867 about the net reconnection voltage. Having a global representation of the OCB allows  
868 this area to be easily estimated. Assuming a spherical Earth, the polar cap area can be  
869 estimated by,

$$870 \quad A_{pc} = \int_0^{2\pi} (R_E + h)^2 (1 - \sin \lambda(\mathbf{P}(\phi))) d\phi \quad (28)$$

871 In a discrete form, assuming  $N$  OCB estimates equally spaced in AACGM longitude  $\phi$   
872 we can write this as,

$$873 \quad A_{pc} = \frac{2\pi(R_E + h)^2}{N} \sum_{i=0}^{N-1} (1 - \sin \lambda(\mathbf{P}_i)) \quad (29)$$

874 We can apply these techniques to study the polar cap area for the whole of the two-hour  
875 interval being studied on this day (2000–2200 UT) (see following section for complete  
876 results).

877 In fig.11 we present 1-min snapshots of the estimated OCB made every 10 min during  
878 this interval. The squares represent the UVI and SWB boundaries used to determine the  
879 OCB at each time. The bold lines represent 10th order Fourier expansions at each time.  
880 For most of the interval the data coverage is particularly good leading to very reliable  
881 global boundary estimates. However, towards the end of the interval the data coverage  
882 is more patchy and so the global OCB estimates are less reliable. From fig.11 we can  
883 see that initially, the approximately circular polar cap expands, reaching its largest size  
884 around  $\sim 2040$  UT. At this point the polar cap starts to shrink and becomes more oval  
885 shaped around  $\sim 2110$  UT. Towards the end of the interval the polar cap shrinks to a  
886 small size and the boundary is distinctly non-circular. We quantify this polar cap size  
887 variation further in the following section.

### 3. Reconnection rate measurements

#### 3.1. Spatial variation of the reconnection rate

888 By combining measurements of the ionospheric convection velocity and of the OCB  
889 location and motion at a particular time, we can determine the spatial variation of the  
890 reconnection rate at that time using the techniques outlined in section 2.1. In figure 12 we  
891 show again the northern hemisphere SuperDARN convection map, originally presented in  
892 figure 5, for the 1-min interval that we have focussed on (2017–2018 UT) on 26 December  
893 2000. Overplotted on the convection map is the global OCB location (bold line) as  
894 determined for this same interval as shown in fig.9. The next step is to select discrete

895 velocity vectors on, or close to, the OCB which will be used in the reconnection rate  
 896 estimation. This is a trivial exercise in regions where the vectors are co-located with  
 897 the OCB. However, there are some regions where the selected vectors are, by necessity,  
 898  $\sim 0.5^\circ$ - $1.0^\circ$  away from the OCB. The grey shading in fig.12 highlights the velocity vectors  
 899 selected for this example interval. Whereas the overlap of vectors with the OCB is good  
 900 on the dayside (from  $\sim 0800$  MLT through to  $1800$  MLT), the coverage on the nightside  
 901 is not so good with the vectors being sparse from  $\sim 2230$  to  $\sim 0300$  MLT and being absent  
 902 from  $\sim 0300$  to  $\sim 0600$  MLT. This is the case for most of the interval under study.

903 In fig.13 we present the spatial variation (with MLT) of the reconnection rate measure-  
 904 ments. Positive reconnection rates relate to flux being added to the polar cap whereas  
 905 negative reconnection rates relate to flux being removed from the polar cap. Hence for  
 906 most IMF conditions, including the IMF  $B_y$ -dominated conditions observed at this time  
 907 (see fig.14 for full details of the IMF conditions), we would typically expect positive recon-  
 908 nection rates in the dayside ionosphere and negative reconnection rates in the nightside  
 909 ionosphere. We present the total estimated reconnection rate for our 1-min interval in  
 910 fig.13a, but we also separate the measurements into the contributions from the plasma flow  
 911 ( $B_{z_i}|\mathbf{V}_i|\cos\theta_i$  in equation 11) (fig.13b) and the contributions from the boundary motion  
 912 ( $B_{z_i}|\mathbf{V}_{P_i}|\cos\alpha$  in equation 11) (fig.13c). The bold black line and grey shaded region in  
 913 fig.13a represent the mean and standard deviation of the reconnection rate measurements  
 914 measured in a 2-hour MLT sliding window. This helps to illustrate the gross features in  
 915 the spatial variation of the reconnection rate.

916 The contributions from the plasma flow (panel b) are much as expected for most IMF  
 917 conditions reflecting the standard two-cell ionospheric convection pattern; poleward flow

918 across the OCB in the dayside ionosphere and equatorward flow across the OCB in the  
 919 nightside ionosphere. The uncertainties in these measurements are estimated as shown in  
 920 section 2.1.3. Using the results of *Provan et al.* [2002] as a guide for estimating the uncer-  
 921 tainties in ‘true’ velocity vectors, we estimate the uncertainty in the velocity magnitude  
 922 as  $\sim 25\%$  ( $a_1 = 0.25$ ) and the uncertainty in the angle the vector makes with the normal  
 923 to the separatrix as  $\sim 45^\circ$  ( $a_2 = \pi/4 \approx 0.79$ ). We can then rewrite the error equation (20)  
 924 as,

$$925 \quad \varepsilon \langle |\mathbf{V}_i(t)| \cos \theta_i(t) \rangle \approx |\mathbf{V}_i(t)| \left( 0.0625 \cos^2 \theta_i(t) - 0.617 \sin^2 \theta_i(t) \right)^{\frac{1}{2}}. \quad (30)$$

926 and so the uncertainty values range from  $0.25|\mathbf{V}_i(t)|$  when  $\theta_i(t) = 0^\circ$  to  $0.79|\mathbf{V}_i(t)|$  when  
 927  $\theta_i(t) = 90^\circ$ . Hence, the largest uncertainties in the contribution from the plasma flow  
 928 occur around  $\sim 1500$  MLT where the convection flows are aligned close to parallel with  
 929 the estimated OCB.

930 The contributions from the boundary motion (fig.13c) are characterised by larger uncer-  
 931 tainties. We assume that the latitudinal uncertainty in our raw OCB measurements (from  
 932 both Polar UVI and SuperDARN SWBs) is  $\sim 0.5^\circ$  ( $\sim 50$  km), as discussed in previous sec-  
 933 tions. As measurements are made every minute, then using equation (24) to provide an  
 934 estimate of the uncertainty in the separatrix motion would give  $\sim 830$  m/s. However, this  
 935 is reduced by dividing by  $\sqrt{N}$  to account for the temporal smoothing over  $N$  boundary  
 936 estimates, as discussed in section 2.3.6. (As an aside, if measurements are made every 5  
 937 minutes then the basic uncertainty reduces to  $\sim 165$  m/s.) It must also be remembered  
 938 that there are regions of the boundary (shown by the bold symbols in fig.13c) where  
 939 gaps in the raw OCB data exist and where the boundary has been interpolated. Hence,  
 940 the boundary estimates in these regions may be questionable. Figure 13c suggests that

941 the contributions to the total reconnection rate from the boundary motion are as large  
942 as those from the plasma flow, but that the magnitude of the contribution is spatially  
943 variable.

944 We can describe the spatial variations in the reconnection rate as shown in figure fig.13a  
945 in the following way. In the dayside ionosphere we expect positive reconnection rates  
946 which represent magnetic flux being added to the polar cap following reconnection on the  
947 dayside magnetopause. This is generally the case in fig.13a although the reconnection  
948 rate appears to reduce to zero close to noon. This spatial variation in reconnection  
949 rate is consistent with a split reconnection X-line on the magnetopause and matches the  
950 variation predicted by the anti-parallel merging hypothesis during conditions dominated  
951 by the IMF  $B_y$  component close to the winter solstice [*Coleman et al.*, 2001; *Chisham*  
952 *et al.*, 2002], matching the conditions for this example event (see section 3.2). In the  
953 nightside ionosphere we expect negative reconnection rates which represent magnetic flux  
954 being removed from the polar cap following reconnection in the magnetotail. This is  
955 generally the case for most of this interval although there are a couple of regions ( $\sim$ 1830–  
956 2000 MLT and  $\sim$ 0200–0300 MLT) where positive reconnection rates are measured. Most  
957 of the contribution towards these positive reconnection rates comes from the boundary  
958 motion. As it is unlikely that flux is being added to the polar cap at these locations it  
959 is therefore likely that the estimation of the boundary motion is in error and hence, that  
960 the uncertainties in the boundary motion have been underestimated in these regions. As  
961 discussed in section 2.1.3, measuring reconnection rates at a high temporal resolution (e.g.,  
962 at the 1-min sampling rate used here) requires a significant accuracy of measurements of  
963 the OCB location and motion. The large uncertainties in our results suggest that there are

964 still some improvements to be made before the boundary measurements can be measured  
965 accurately enough to fully match the requirements of the 1-min convection measurements.

### 3.2. Temporal variation of the reconnection potential

966 Figure 14 presents the temporal variation of the average reconnection rate from both  
967 the dayside and nightside ionosphere corresponding to magnetopause and magnetotail  
968 reconnection, respectively. To place the reconnection rate measurements in context, panel  
969 14a shows the  $B_y$  and  $B_z$  components of the IMF for this interval as measured by the ACE  
970 spacecraft located upstream in the solar wind. The IMF variations have been shifted by  
971 63 min to account for the solar wind travel time between the spacecraft and the Earth's  
972 magnetosphere. Panel 14b shows the associated IMF clock angle. At the start of the  
973 interval the IMF is in transition from being predominantly southward (not shown) to being  
974 dawnward (at  $\sim 2010$  UT). For the rest of the 2-hour interval, although the  $B_z$  component  
975 is positive, the IMF is very much  $B_y$ -dominated with the IMF clock angle fluctuating  
976 between  $-70^\circ$  and  $-90^\circ$ . Although the IMF is slightly northward, the existence of normal  
977 two-cell convection at this time (and the previous observations of two-cell convection for  
978 these IMF conditions [*Freeman et al.*, 1993; *Ruohoniemi and Greenwald*, 1996]), suggests  
979 that reconnection is occurring sunward of the cusp region for these conditions, rather than  
980 on the lobe magnetopause. Hence, magnetopause reconnection will be responsible for the  
981 addition of flux to the polar cap at the OCB during this interval. The two vertical dashed  
982 lines in fig.14 show the timing of a substorm onset and a substorm intensification identified  
983 from a combination of auroral brightenings in the Polar UVI data, the occurrence of Pi2  
984 pulsations and the initiation of negative bays in ground-based magnetometer data. These  
985 events would be expected to be associated with enhanced reconnection in the magnetotail.

986 Figure 14c presents the variation in polar cap area during this interval, estimated using  
987 the techniques outlined in section 2.3.6. At the start of the interval ( $\sim 2000$ - $2040$  UT),  
988 following the interval of southward IMF, the polar cap is expanding, indicating that  
989 magnetic flux is being added to the polar cap by magnetopause reconnection at a faster  
990 rate than it is being removed by magnetotail reconnection. Following a substorm onset at  
991  $\sim 2037$  UT (and hence enhanced magnetotail reconnection) the polar cap starts to contract  
992 at  $\sim 2040$  UT. Following a substorm intensification at  $\sim 2051$  UT the rate of contraction  
993 increases before the polar cap size stabilizes at  $\sim 2100$  UT. At around  $\sim 2120$  UT the polar  
994 cap appears to start contracting again (although the polar cap areas are less reliable at  
995 this time because of the reduction in the global coverage of the OCB estimates). The polar  
996 cap reaches a steady, minimum size at  $\sim 2130$  UT. The measured change in the polar cap  
997 area across this interval provides a good estimate of the net reconnection voltage and it is  
998 generally clear from the gradient of the curve as to whether magnetopause or magnetotail  
999 reconnection is the dominant process at any one time.

1000 If we want to study the temporal variation of the reconnection rate (or voltage) in more  
1001 detail then we need to be able to differentiate between the magnetopause (dayside) and  
1002 magnetotail (nightside) reconnection rates. Because we do not always have a full comple-  
1003 ment of velocity vectors along each of the merging lines it is often difficult to calculate  
1004 a complete reconnection voltage for either the magnetopause or magnetotail X-line. One  
1005 alternative, when limited data are available, is to present the average reconnection rate  
1006 ( $\langle E_{rec} \rangle$ ) measured along the portions of each merging line over which the measurements  
1007 were made. If an estimate of the total length of the merging line can also be made then  
1008 this allows an estimate of the total reconnection voltage along the merging line.

1009 In figs.14d and 14e we present the temporal variations of the average dayside and night-  
1010 side reconnection rates, respectively (bold black lines). The average dayside (nightside)  
1011 rates were calculated from vectors sunward (anti-sunward) of the 0600-1800 MLT line.  
1012 For both the dayside and nightside reconnection rates the level of fluctuation is quite high  
1013 with the point-to-point variability being of similar size to the average electric field values.  
1014 However, it is difficult to assess how much of this fluctuation is real, caused by tempo-  
1015 ral burstiness of the reconnection process, and how much is caused by uncertainties in  
1016 the measured quantities. The occurrence of ‘unphysical’ negative reconnection rate mea-  
1017 surements in the dayside ionosphere and positive reconnection rate measurements in the  
1018 nightside ionosphere suggests that there are times when the measurements may be inade-  
1019 quate. This supports our previous suggestion that the OCB cannot presently be measured  
1020 accurately enough to match the requirements of 1-min convection measurements.

1021 The white lines in figs.14d and 14e present the variation of the average of the average  
1022 reconnection rates measured within a 15-min sliding window (the grey region represents  
1023 the average of the error estimates in the same window). The white lines act to highlight  
1024 the general trends in the reconnection rate variations by removing the point-to-point  
1025 variability. At the beginning of the interval the average dayside reconnection rate is  $\sim 20$   
1026 mV/m whereas that on the nightside varies between 0 and -10 mV/m. The dayside rate  
1027 decreases slightly with time to  $\sim 10$  mV/m, whereas, following the substorm onset, the  
1028 nightside rate changes to  $\sim -40$  mV/m, dominating the dayside rate. At this time, the size  
1029 of the fluctuations in the nightside rate become much larger, although this may be due  
1030 to the reduction in the size of the measurable nightside merging line. Towards the end of

1031 the interval the average nightside reconnection rate appears to reduce to a similar level  
1032 as the dayside rate leading to a stability in the polar cap area.

1033 It is possible, using equation (9), to perform a consistency check on the polar cap  
1034 area and average reconnection rate measurements. Since this requires knowledge of the  
1035 magnetopause and magnetotail reconnection voltages, we need to assume lengths for the  
1036 dayside and nightside merging lines. Here, we have derived a large number of polar cap  
1037 area variations from the average reconnection rate measurements (black lines in fig.14d  
1038 and e) by assuming merging line lengths from 0.1 hours of MLT to 12.0 hours of MLT (in  
1039 0.1 hour steps). Using a least squares fit we have then determined which of these variations  
1040 best matches the observed polar cap area variation. In fig.15a we present the observed  
1041 polar cap area variation (as shown in fig.14c). We also show (dashed line) the best fit  
1042 polar cap area variation determined from the average reconnection rate measurements.  
1043 The best fit occurred when a dayside merging line length of 12 hours of MLT, and a  
1044 nightside merging line length of 7.6 hours of MLT, were assumed. Although the general  
1045 variation of the two curves in fig.15a is very similar, the gradients in the three distinct  
1046 regions of the curve are slightly different, leading to offsets between the curves at the  
1047 beginning and end of the data sets.

1048 It is fair to assume that the merging line lengths are unlikely to be constant across  
1049 the whole of this interval. Consequently, we have split the data set into three distinct  
1050 sections before repeating the fitting process on each section. The sections were selected  
1051 by the gradients in the polar cap area variation - where the area is clearly increasing,  
1052 where the area is sharply decreasing, and where the area is stable or gradually decreasing.  
1053 Figure 15b presents the best fit polar cap area variations determined from the average

1054 reconnection rate measurements in each of these sections. The fits in each section are now  
1055 very good and follow the measured variations in the polar cap area closely. The merging  
1056 line lengths which provide the best fits are different in each section. At the beginning  
1057 of the interval, where the polar cap is expanding and the dayside reconnection rate is  
1058 dominant over the nightside reconnection rate, the length of the dayside and nightside  
1059 merging lines are predicted to be 8.0 and 3.2 hours of MLT, respectively. When the polar  
1060 cap starts to contract at  $\sim 2040$  UT not only does the average nightside reconnection  
1061 rate increase (as shown in fig.14e), but the predicted length of the nightside merging line  
1062 also increases to 9.2 hours of MLT. The predicted length of the dayside merging line also  
1063 increases but by a smaller amount to 10.0 hours of MLT. When the speed of contraction  
1064 of the polar cap reduces at  $\sim 2105$  UT the predicted length of the nightside merging line  
1065 reduces slightly to 7.2 hours of MLT, whereas that of the dayside merging line increases  
1066 slightly to 12.0 hours of MLT.

#### 4. Discussion and Conclusions

1067 So far in this paper we have provided a synthesis of the techniques for measuring the  
1068 ionospheric projection of the magnetic reconnection rate (section 2) and given an example  
1069 of its application (section 3). The final stage of ionospheric remote sensing of reconec-  
1070 tion is mapping of the measurements in the ionosphere to the reconnection site on the  
1071 magnetopause or magnetotail. This mapping is essential for a full understanding of the  
1072 reconnection process because it is at these locations that reconnection actually takes place.  
1073 However, in our view, it is not yet clear how best to do this mapping and it is also prob-  
1074 ably subject to large systematic and random uncertainty. For this reason, we have not

1075 included mapping in the main technique section but instead discuss here the two main  
1076 options and their associated problems and uncertainties.

1077 Ideally, one would like to perform an inverse mapping of ionospheric measurements of  
1078 the reconnection electric field to the reconnection site to provide an estimate of the in-situ  
1079 reconnection rate [*Pinnock et al.*, 2003; *Chisham et al.*, 2004b]. This may be achieved using  
1080 a magnetospheric magnetic field model under the assumption that the electric potential  
1081 is invariant along a magnetic field line. At present, the state of the art in magnetosphere  
1082 models is the Tsyganenko model [*Tsyganenko*, 1995; *Tsyganenko and Stern*, 1996], the  
1083 most widely used model in this context. The major difficulty with a magnetic field model  
1084 such as the Tsyganenko model is that it is derived in part from large sets of spacecraft data,  
1085 and represents the average configuration of the magnetospheric field, given a particular  
1086 set of input parameters. The magnetic field at a particular instant may deviate from this  
1087 configuration, rendering the field line tracing inaccurate. Furthermore, any error in the  
1088 initial position in the ionosphere is amplified under inverse mapping due to the general  
1089 divergence of the magnetic field with altitude. Inverse mapping is most reliable in the  
1090 steady state (when variations in the magnetospheric field are small) and in the dayside  
1091 ionosphere (where the model fields are typically more reliable), such as in the remote  
1092 sensing studies of *Pinnock et al.* [2003] and *Chisham et al.* [2004b]. However, inverse  
1093 mapping has not been applied to the remote sensing of magnetotail reconnection during  
1094 a substorm, such as the case study presented in this paper and that presented by *Lam*  
1095 *et al.* [2006], because the magnetic field model of the magnetotail will be unreliable at  
1096 times of rapidly changing magnetic field (e.g., at substorm onset). The accuracy of, and  
1097 confidence in, inverse mapping can be improved by calibrating with in-situ spacecraft

1098 measurements where available. For example, *Pinnock et al.* [2003] used magnetopause  
1099 crossings identified by the Geotail and Equator-S satellites to re-scale the size of the  
1100 Tsyganenko model used in their mapping (by adjusting the solar wind dynamic pressure  
1101 input) and showed that the remotely sensed reconnection rate was consistent with in-situ  
1102 point samples in location and magnitude. The importance of accurate inverse mapping to  
1103 the interpretation of observations is well illustrated in the results of *Chisham et al.* [2002]  
1104 where the reconnection electric field in the ionosphere is highly asymmetric (being high  
1105 in the post-noon sector, and low in the pre-noon sector) but is relatively symmetric when  
1106 mapped to the magnetopause [*Freeman et al.*, 2007].

1107 Currently, the more reliable way of using the ionospheric remote sensing technique to  
1108 study reconnection problems is to use a forward mapping method. In this approach a  
1109 reconnection model or scenario is tested by predicting the ionospheric projection of the  
1110 reconnection electric field for direct comparison with the remote sensing observations. This  
1111 has the advantage over inverse mapping in that positional uncertainties at the reconnection  
1112 site decrease on mapping to the ionosphere rather than grow. In addition, the effects of  
1113 instrument error, data gaps, and data assimilation methods can be more readily simulated.  
1114 Even better is to use forward mapping to test alternative reconnection models within a  
1115 common global framework. In this case the different reconnection models are both subject  
1116 to similar errors from the magnetic field model and other effects in the forward mapping.  
1117 Hence, the acceptance of a reconnection model is based on relative, rather than absolute,  
1118 agreement with the observations. This was effectively the approach used by *Coleman et al.*  
1119 [2001] and *Chisham et al.* [2002] to differentiate between the subsolar and anti-parallel  
1120 models of reconnection. In these studies a distinctive difference in the variation of the

1121 electric field along the ionospheric projection of the magnetopause X-line was identified  
1122 between the two reconnection models for specific IMF, magnetic dipole tilt, and polar  
1123 hemisphere conditions that, when compared to observations, provided evidence in favour  
1124 of the anti-parallel reconnection model.

1125 Whether using inverse or forward mapping, ionospheric remote sensing of reconnection  
1126 relies on a connection between the reconnection site and the ionosphere by a magnetic  
1127 field line. If multiple reconnection X-lines exist simultaneously, this can mean that some  
1128 of these sites are effectively invisible to the ground. For example, during the substorm  
1129 expansion phase, near-Earth and distant magnetotail reconnection sites are expected to  
1130 co-exist. Assuming dawn-dusk symmetry, near-Earth reconnection initially reconnects  
1131 closed magnetic flux created by the distant reconnection site and both sites are connected  
1132 to the ionosphere, but at a later time near-Earth reconnection reconnects open magnetic  
1133 flux and detaches the distant reconnection site from the ionosphere. In the case of self-  
1134 organised criticality or turbulent reconnection, numerous reconnection sites are expected  
1135 to co-exist [*Klimas et al.*, 2000] and it is unlikely that all of these will connect to the  
1136 ionosphere. Thus an inverse mapping of the ionospheric reconnection electric field will  
1137 not give a valid representation of the reconnection scenario, but it may be possible to  
1138 predict the structure of the ionospheric projection of the reconnection electric field using  
1139 forward mapping, to compare with observation.

1140 Assuming that a connection between the reconnection X-line and the ionosphere exists,  
1141 it is crucial to be able to identify the ground-based projection of the reconnection X-  
1142 line. As discussed in section 2.3, doing this usually involves exploiting the differences  
1143 in the particle precipitation signatures between open and closed magnetic field lines.

1144 However, when reconnection only reconfigures magnetic field lines, and does not change  
1145 the magnetic topology (such as with lobe reconnection during northward IMF conditions),  
1146 then other identifiers are required. For northward IMF conditions, a suitable identifier  
1147 can be the velocity dispersion of precipitating ions from the reconnection site. Similar  
1148 velocity-dispersed ion signatures are also seen in the nightside auroral zone and could be  
1149 an identifier for near-earth reconnection during the early substorm expansion phase.

1150 In conclusion, we have provided a synthesis of the technique for remotely sensing the  
1151 magnetic reconnection rate from the ionosphere and discussed associated problems and  
1152 uncertainties. In doing so, we have shown how the remote sensing technique has developed  
1153 from single point measurements to covering a wide range of spatial scales almost up to the  
1154 global scale. The example event presented here demonstrates that remote sensing of an  
1155 entire reconnection X-line is viable by a combination of the existing SuperDARN network  
1156 and spacecraft auroral imagers, which would be unfeasible by in-situ spacecraft. Further  
1157 expansion of SuperDARN in both the northern and southern hemispheres is planned  
1158 [*Chisham et al.*, 2007]. This coincides with an era of unprecedented auroral imaging with  
1159 the forthcoming NASA Themis mission and its associated ground-based instruments, and  
1160 future missions such as the Chinese (and European) Space Agency Kuafu spacecraft.  
1161 These will give continuous observations of the auroral oval in one hemisphere and regular  
1162 observations of the auroral oval in both hemispheres. This expansion in instrumentation  
1163 should allow remote sensing of both magnetopause and magnetotail reconnection sites  
1164 completely and simultaneously.

1165 This remote sensing capability opens up new opportunities for understanding the re-  
1166 connection process that is fundamental to the behaviour of not only the Earth's magne-

1167 tosphere but to many natural astrophysical environments and artificial fusion reactors.  
1168 Progress has already been made in using the remote sensing technique to address the  
1169 outstanding reconnection questions of the Earth's environment posed in the Introduction,  
1170 concerning the location, extent and controlling factors of reconnection: The reconnection  
1171 X-line at the magnetopause has been found to extend over  $38 R_E$  under stable due south-  
1172 ward IMF conditions, corresponding to the entire dayside equatorial magnetopause and  
1173 beyond the dawn and dusk flanks into the magnetotail [Pinnock *et al.*, 2003]. In contrast,  
1174 for stable due northward IMF the reconnection X-line was found to be limited to 6-11  $R_E$   
1175 in the high-latitude lobes of the magnetotail [Chisham *et al.*, 2004b]. For intermediate  
1176 IMF orientations, the remote sensing technique has provided evidence that the recon-  
1177 tion X-line at the magnetopause is bifurcated, existing in two distinct regions on the high  
1178 latitude magnetopause equatorward of the cusps [Coleman *et al.*, 2001; Chisham *et al.*,  
1179 2002]. This is in contrast to the single magnetopause X-line extending between these  
1180 regions through the subsolar region that is inferred for these IMF conditions from in-situ  
1181 spacecraft observations [Fear *et al.*, 2005]. This paradox needs to be reconciled. In the  
1182 magnetotail, the ionospheric projection of the reconnection X-line is found to increase  
1183 in length following substorm onset, in one case from 3.2 hours of MLT in the substorm  
1184 growth phase to 9.2 hours of MLT in the substorm expansion phase (see example discussed  
1185 in previous section) and in another from 4 hours to 7 hours of MLT in the first 15 min of  
1186 the expansion phase [Lam *et al.*, 2006], although the corresponding location and length  
1187 of the reconnection X-line in the magnetotail has not been estimated in these cases (as  
1188 discussed above).

1189 The reconnection questions being addressed in the terrestrial context have relevance  
1190 to more general reconnection problems. For example, the remote sensing measurements  
1191 of magnetopause reconnection summarised above argue that reconnection is restricted to  
1192 regions of high magnetic shear and that consequently the relative geometry of magnetic  
1193 fields is the principal factor determining the overall reconnection rate [*Freeman et al.*,  
1194 2007], and hence, the dynamical behaviour of magnetised plasmas in general, an assump-  
1195 tion that is invoked in the context of the solar corona [*Hughes et al.*, 2003]. With the  
1196 development of the remote sensing technique and the existing and forthcoming data from  
1197 SuperDARN and auroral imagers, measurement of reconnection could become increasingly  
1198 efficient and routine. This should allow us to address more conclusively the particularly  
1199 important problem of the general structure of reconnection in time and space, including  
1200 its temporal continuity and stability [*Phan et al.*, 2000; *Abel and Freeman*, 2002], and the  
1201 relative prevalence and causes of single, dual, or multiple reconnection sites with partic-  
1202 ular scales, or of scale-free reconnection structure [*Lazarian and Vishniac*, 1999; *Klimas*  
1203 *et al.*, 2000; *Coleman et al.*, 2001; *Chisham et al.*, 2002; *Coleman and Freeman*, 2005;  
1204 *Phan et al.*, 2006].

## Glossary

1205 **Altitude-adjusted corrected geomagnetic (AACGM):** A geomagnetic coordinate  
1206 system defined to be the same as the corrected geomagnetic coordinate (CGM) system at  
1207 0 km altitude. At all other altitudes the system is defined so that latitude and longitude  
1208 are invariant along a magnetic field line.

1209 **Aurora:** Natural coloured-light displays in the polar regions caused by the collision of  
1210 charged particles from the Earth's magnetosphere with atoms in the upper atmosphere.

1211 **Closed field line:** A geomagnetic field line that has both ends connected to the Earth.

1212 **Coherent scatter radar:** Coherent scatter radar is a volume scattering technique  
1213 where the radar detects energy scattered from within a medium when there are regular  
1214 spatial variations of the refractive index due to density irregularities. This is the analogue  
1215 of Bragg scattering of X-rays from crystals. The term “coherent” applies to the construc-  
1216 tive interference possible when there is a scattering structure with an organized spatial  
1217 content at half the radar wavelength.

1218 **Convection reversal boundary (CRB):** This is located where ionospheric convec-  
1219 tion changes from being sunward to antisunward.

1220 **Cross-polar cap potential:** The electric potential difference measured from dawn to  
1221 dusk across the polar cap.

1222 **Cusp:** A region of the dayside magnetosphere in which the entry of magnetosheath  
1223 plasma to low altitudes is most direct.

1224 **Defense meteorological satellite program (DMSP):** A series of low-altitude space-  
1225 craft which monitor meteorological, oceanographic, and solar-terrestrial physics for the  
1226 United States Department of Defense.

1227 **Doppler spectral width:** The width of Doppler spectra of ionospheric density irreg-  
1228 ularities measured by the SuperDARN radars.

1229 **E-region:** A layer of the ionosphere that exists at about 90-150 km altitude.

1230 **F-region:** A layer of the ionosphere that exists at about 150-800 km altitude.

1231 **Flux transfer events (FTE):** Bursty and/or patchy reconnection events that occur  
1232 on the dayside magnetopause.

1233 **Incoherent scatter radar:** Incoherent scatter radar is a technique where radio signals  
1234 are scattered from a large number of individual electrons in random thermal motion in  
1235 the ionosphere. The technique allows measurements of the density, temperature, velocity,  
1236 and composition of ionospheric ions and electrons.

1237 **Interplanetary magnetic field (IMF):** The Sun's magnetic field carried by the solar  
1238 wind through the solar system.

1239 **Ionosphere:** The ionized region of the upper atmosphere, forming the lower boundary  
1240 of the magnetosphere.

1241 **Ionospheric irregularities:** Density structures in the E- and F-region ionosphere  
1242 which act as backscatter targets for coherent scatter radar signals.

1243 **Lobes:** Regions of low density plasma in the Earth's magnetotail. They are constituted  
1244 of open geomagnetic field lines which originate in both polar ionospheres.

1245 **Magnetic local time (MLT):** A measurement of local time (i.e., a position relative  
1246 to the Earth-Sun direction) in the AACGM coordinate system.

1247 **Magnetic reconnection:** A process which changes the connectivity and topology of  
1248 magnetic field line regions and facilitates the transfer of mass, momentum and energy  
1249 between these regions.

1250 **Magnetopause:** The outer limit of the magnetosphere where the magnetic pressure  
1251 of the magnetosphere is balanced by the kinetic pressure of the solar wind.

1252 **Magnetosphere:** The region of near-Earth space where the geomagnetic field has  
1253 dominant control over the motion of plasma.

1254 **Magnetotail:** That part of the magnetosphere that is stretched out anti-sunward of  
1255 the Earth by the solar wind.

1256 **Merging line:** The ionospheric projection of the reconnection separatrix.

1257 **Near-Earth neutral line (NENL):** A neutral line (X-line) that is thought to occur  
1258 earthward of the magnetotail X-line around the time of substorm onset.

1259 **Neutral point:** The point at the centre of a region of magnetic reconnection where  
1260 the field strength is effectively zero.

1261 **Open field line:** A geomagnetic field line that has only one end connected to the  
1262 Earth, and which also forms part of the interplanetary magnetic field.

1263 **Open-closed field line boundary (OCB):** The boundary between open and closed  
1264 geomagnetic field lines which is equivalent to the reconnection separatrix for most IMF  
1265 conditions.

1266 **Plasma:** An ionized gas composed of electrons and ions.

1267 **Polar cap:** The ionospheric footprint of the region of open geomagnetic field lines.  
1268 Polar caps exist in both the northern and southern hemisphere ionospheres.

1269 **Polar cap boundary:** The ionospheric footprint of the open-closed field line boundary.

1270 **Polar ultra-violet imager (UVI):** An instrument on the NASA Polar satellite which  
1271 takes global-scale images of the aurora at ultra-violet wavelengths.

1272 **Reconnection rate:** The reconnection rate (or reconnection electric field) is defined  
1273 as the rate of transfer of magnetic flux across unit length of the reconnection separatrix.  
1274 The units of reconnection rate are V/m or Wb/s/m.

1275 **Reconnection separatrix:** Separatrix surfaces divide different magnetized plasma  
1276 domains. The reconnection separatrix is the boundary between unreconnected and recon-  
1277 nected magnetic field lines.

1278 **Reconnection voltage:** The reconnection voltage (or integrated reconnection rate) is  
1279 the magnetic flux transfer associated with an extended X-line. The units of reconnection  
1280 voltage are V or Wb/s.

1281 **Solar wind:** A stream of plasma, ejected from the upper atmosphere of the Sun, which  
1282 flows radially outward through interplanetary space.

1283 **Space weather:** Space weather describes the conditions in space that affect the Earth  
1284 and its technological systems, and is affected by factors such as the behavior of the Sun  
1285 and the nature of the Earth's magnetic field.

1286 **Spectral width boundary (SWB):** The boundary between ionospheric backscatter  
1287 spectra with high and low spectral widths as measured by the SuperDARN HF radar  
1288 network. This boundary is often a good proxy for the open-closed field line boundary.

1289 **Substorm cycle:** The slow build-up and rapid release of magnetic energy within the  
1290 Earth's magnetosphere.

1291 **SuperDARN:** The Super Dual Auroral Radar Network - an international radar net-  
1292 work for studying the upper atmosphere and ionosphere, comprised of twelve radars in  
1293 the northern hemisphere and seven in the southern hemisphere that operate in the High  
1294 Frequency (HF) bands between 8 and 22 MHz. The radars measure the Doppler velocity  
1295 of plasma density irregularities in the ionosphere.

1296 **SuperDARN global convection mapping:** This technique (also known as Map  
1297 Potential) fits line-of-sight velocity data from multiple SuperDARN radars to an expansion  
1298 of the ionospheric electric potential in spherical harmonics to produce global ionospheric  
1299 convection maps.

1300 **Tsyganenko model:** The Tsyganenko model is a semi-empirical best-fit representation  
1301 for the Earth's magnetic field, based on a large number of near-Earth satellite observations.

1302 **X-line:** An extended line of X-type neutral points along the reconnection separatrix.

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**Figure 1.** A 2-dimensional schematic representation of a reconnection X-line. The black lines portray the magnetic field configuration around the neutral point. The blue arrows illustrate the plasma inflow into, and outflow from, the neutral point. The current flow (green) is shown as being directed out of the page. (taken from [http://en.wikipedia.org/wiki/Image:Reconnection\\_Illustrations.png](http://en.wikipedia.org/wiki/Image:Reconnection_Illustrations.png))

**Figure 2.** A 2-dimensional schematic representation of the magnetosphere as shown in the noon-midnight meridian plane during an interval of southward-directed interplanetary magnetic field. The black lines represent the Earth's magnetic field. The neutral points at the points labelled  $N_1$  and  $N_2$  highlight the locations of magnetopause (dayside) and magnetotail (nightside) reconnection for these conditions. (taken from <http://en.wikipedia.org/wiki/Image:Substorm.jpg>)

**Figure 3.** A 3-dimensional schematic representation illustrating the reconnection separatrix (yellow and green shaded regions). The separatrix extends from the magnetopause and magnetotail X-lines (bold blue lines in space), down converging magnetic field lines (red lines) into the ionosphere. The ionospheric projections of the reconnection separatrix are termed the merging lines (bold blue lines in the ionosphere). In the pictured scenario the interplanetary magnetic field is assumed to be in a southward direction and in this case the reconnection separatrix is co-located with the open-closed magnetic field line boundary.

**Figure 4.** Schematic diagrams of the measurement scenario at a longitude  $\phi_i$ , (a) showing the measured quantities, velocity vector  $V_i$  located at  $(\lambda_i, \phi_i)$  and reconnection separatrix  $\mathbf{P}(t)$ , (b) showing the derived quantities,  $\alpha_i$ ,  $\theta_i$ , and  $V_{\mathbf{P}_i}$  at separatrix location  $\mathbf{P}_i$ .

**Figure 5.** A northern hemisphere SuperDARN global convection map from 2017 UT on 26 December 2000. The vectors are ‘true’ vectors with a length proportional to the velocity magnitude. The dashed (morning cell) and dotted (afternoon cell) lines illustrate the convection electric potential solution at this time.

**Figure 6.** A Polar UVI image of the northern hemisphere auroral oval measured at 2017:34 UT on 26 December 2000. The black symbols represent the poleward edge of the auroral oval as estimated using the method of *Carbary et al.* [2003]. The red symbols represent these estimates corrected to provide the best estimates for the OCB using the corrections of *Carbary et al.* [2003]. The radial blue lines highlight the MLT sectors for which latitudinal auroral intensity profiles are presented in fig.7.

**Figure 7.** Latitudinal auroral intensity profiles (solid histograms), taken from the Polar UVI auroral image presented in fig.6 in three MLT sectors. The dotted lines illustrate the *Carbary et al.* [2003] fits to the latitudinal profiles and the vertical dashed line highlights the poleward edge as determined using the *Carbary et al.* [2003] algorithm.

**Figure 8.** The Doppler spectral width measured by beams 7-14 of the Kapuskasing SuperDARN radar at 2017 UT on 26 December 2000. (a) The raw spectral width data, (b) the spatially and temporally median-filtered spectral width data, and (c) the proportion of the filtered data set that was  $>150$  m/s (black). The dashed line represents the 1500 MLT meridian. The white squares in (c) highlight the locations of spectral width boundaries that were determined in this data.

**Figure 9.** An example of using a truncated Fourier series to describe the OCB (at 2017-2018 UT on 26 December 2000). The squares represent UVI boundary measurements made between 2016 and 2019 UT and the diamonds represent SWBs measured by the Kapuskasing, Kodiak, and Prince George SuperDARN radars during the same interval. The solid (dotted) line represents a 10th (6th) order Fourier series.

**Figure 10.** (a) The distribution of Polar UVI boundary velocity in the 2000-2200 UT interval on 26 December 2000 determined from temporally adjacent samples (solid line), at a temporal spacing of 2 samples (dashed line), and at a temporal spacing of 4 samples (dotted line). (b) The distribution of Polar UVI boundary velocity for the same interval determined from the temporally-filtered UVI observations (solid line), and the distributions of boundary velocity for the 6th order (dashed line) and 10th order (dotted line) Fourier series representations of the OCB.

**Figure 11.** A time series of polar plots showing the development of the OCB and the polar cap over the interval 2000-2200 UT on 26 December 2000. Each frame shows the fitted OCB (bold line) and the raw Polar UVI and SWB boundaries used to determine the OCB (squares). The frames represent a 1-min interval separated every 10 min.

**Figure 12.** A combination of the convection map presented in fig.5 with the OCB estimate presented in fig.9 (bold line). The grey shaded regions highlight velocity vectors located close to the OCB that are used to determine the reconnection rate.

**Figure 13.** The spatial variation of the reconnection rate (with MLT). (a) The variation of the total reconnection rate. The bold black line and grey shaded region represent the variation of the mean and standard deviation of the reconnection rate measurements determined in a 2-hour MLT sliding window. (b) The contribution to the total reconnection rate that comes from measurements of the plasma flow. (c) The contribution to the total reconnection rate that comes from the boundary motion.

**Figure 14.** (a) The temporal variation in IMF  $B_y$  (bold line) and IMF  $B_z$  (solid line) as measured by the ACE spacecraft, shifted by 63 min to account for the solar wind propagation from ACE. (b) The IMF clock angle measured by ACE, shifted by 63 min to account for the solar wind propagation from ACE. (c) The polar cap area variation estimated from the global OCB determinations. (d) The average dayside reconnection rate (black line). The white line represents the mean measurement determined in a 15-min sliding window. (e) The average nightside reconnection rate (black line). The white line represents the mean measurement determined in a 15-min sliding window. The two vertical dashed lines represent the estimated times of a substorm onset and a substorm intensification.

**Figure 15.** A comparison of the measured variation in polar cap area (solid line) with that predicted by the measured reconnection rate variations (dashed line), assuming certain dayside and nightside merging line lengths. (a) Assuming fixed merging line lengths for the whole 2-hour interval. (b) Assuming different merging line lengths in three different time periods within the interval. The assumed merging line lengths for the dayside and nightside are displayed on the figure as  $L_d$  and  $L_n$  respectively.

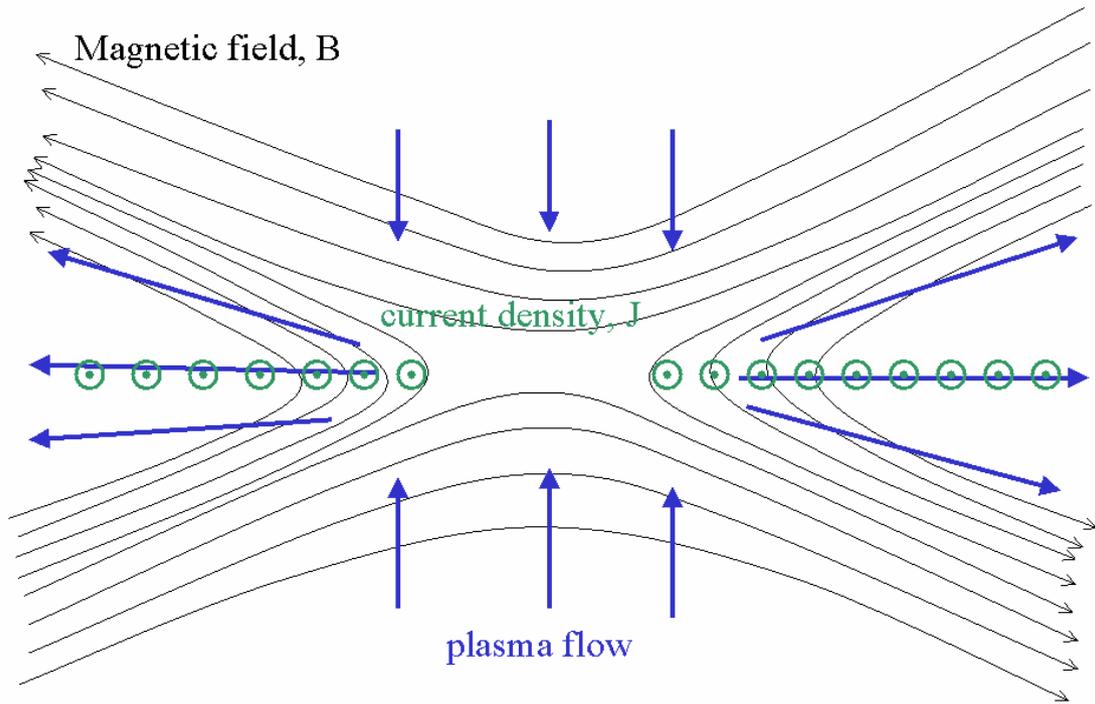


Figure 1

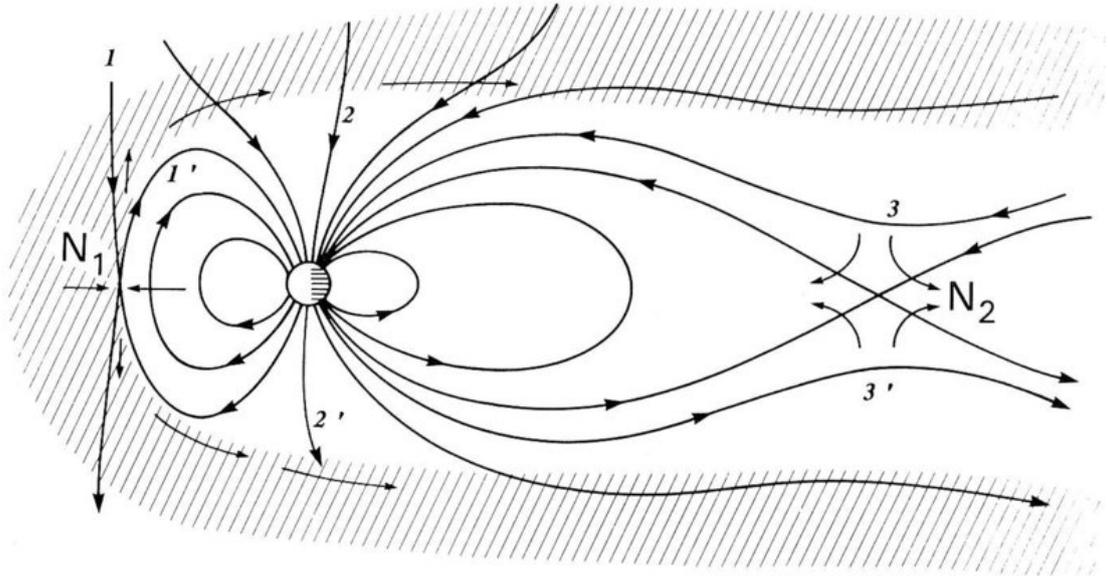


Figure 2

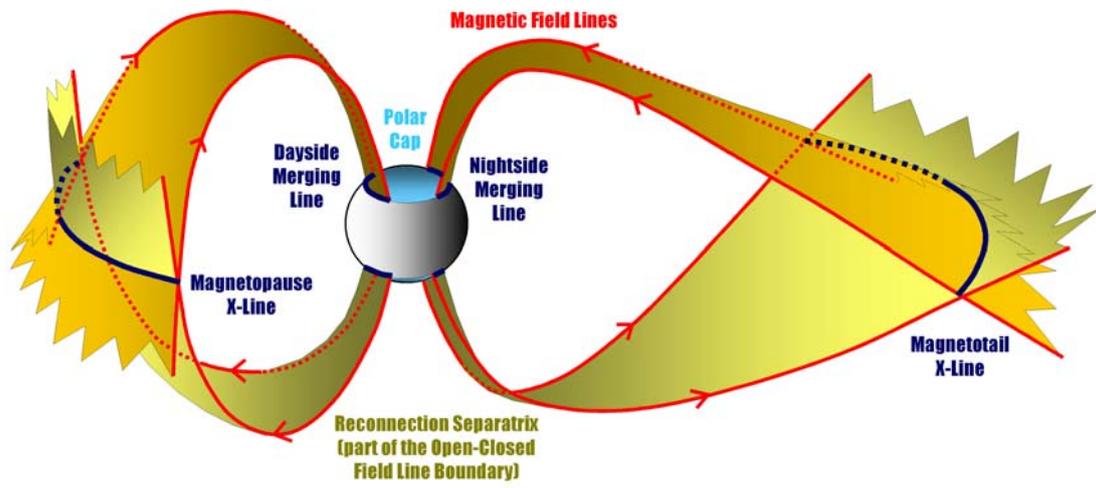


Figure 3

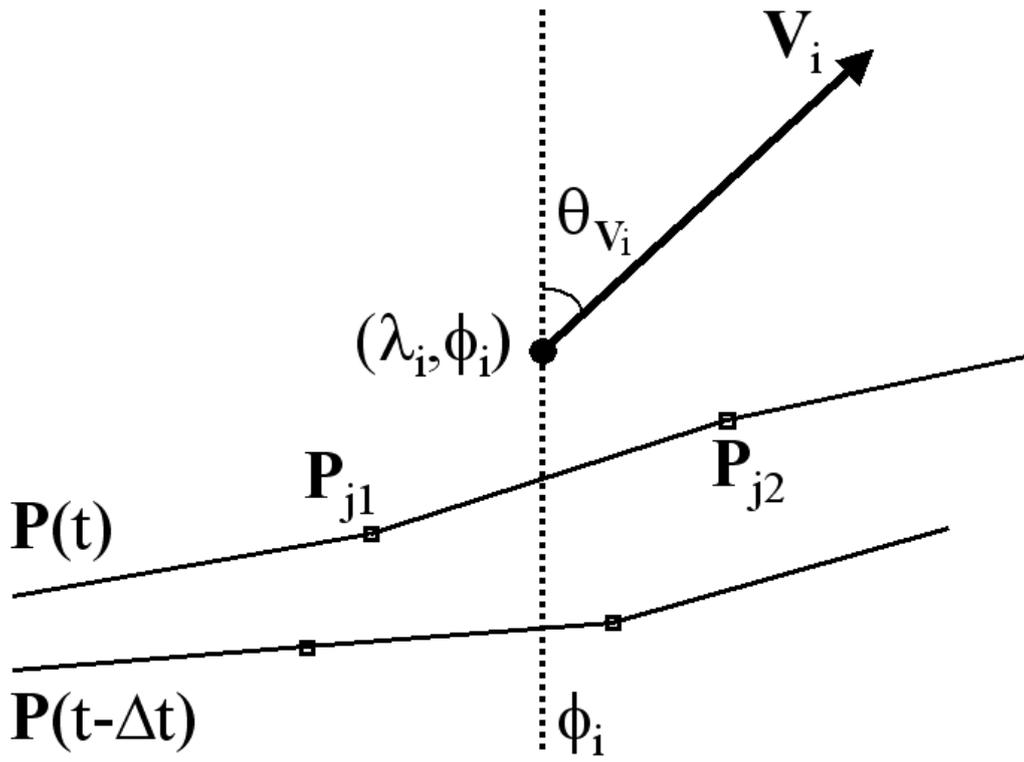


Figure 4a

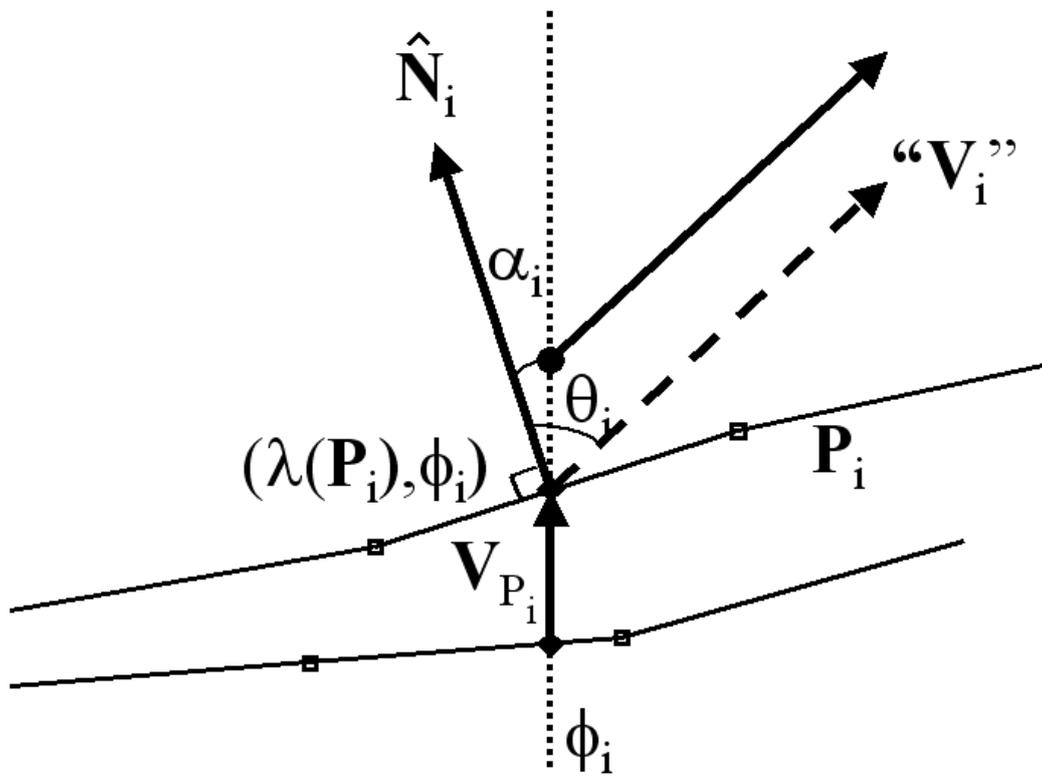


Figure 4b

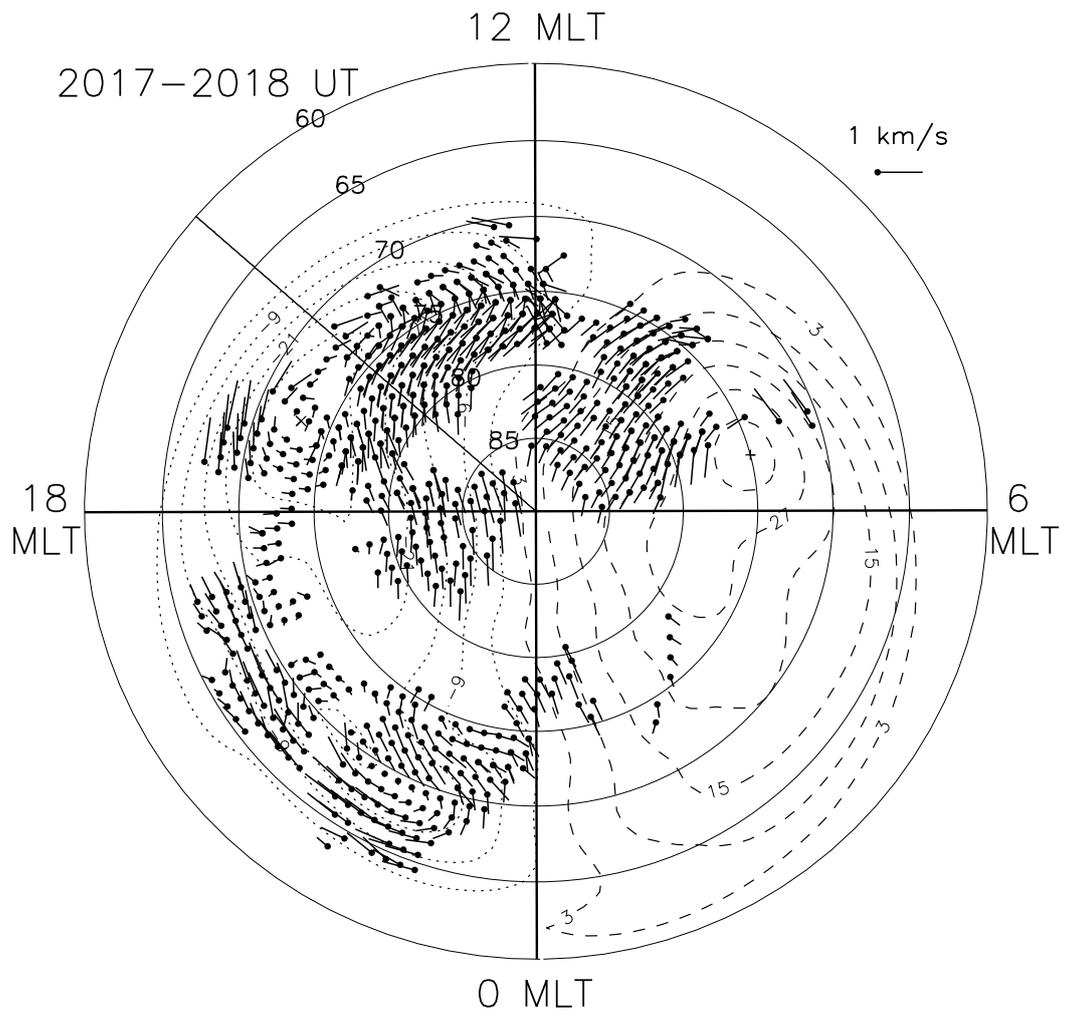


Figure 5

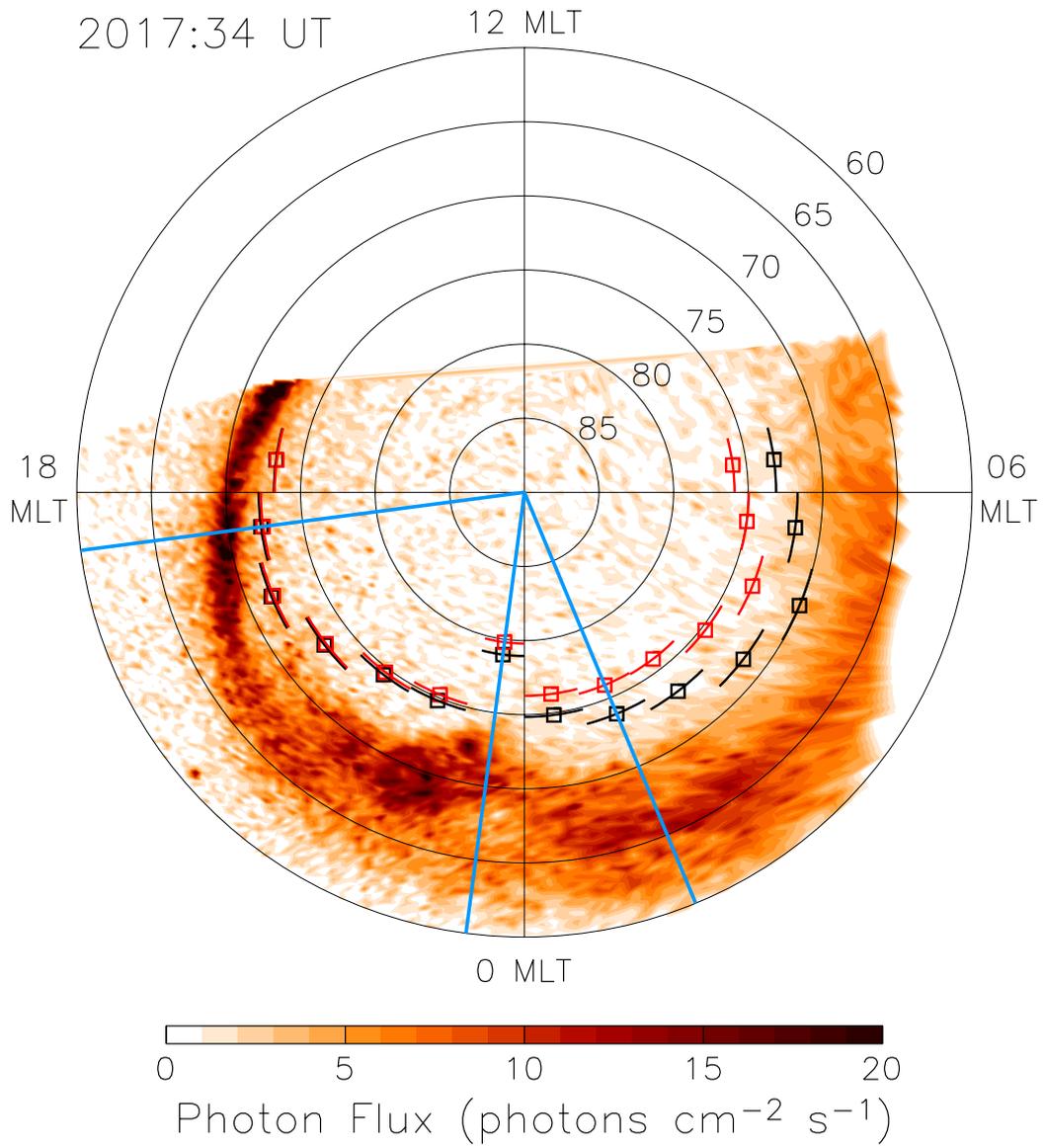


Figure 6

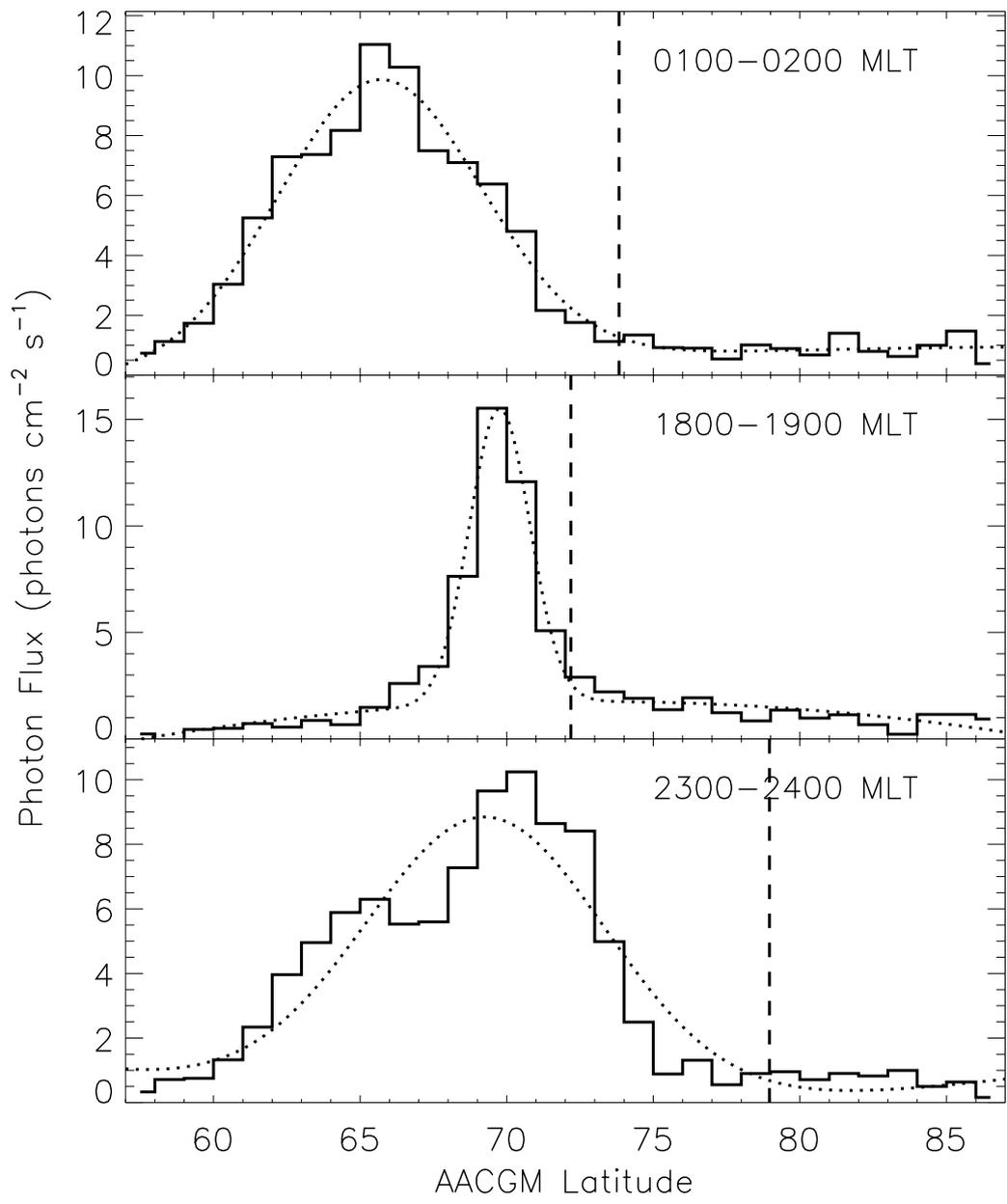


Figure 7

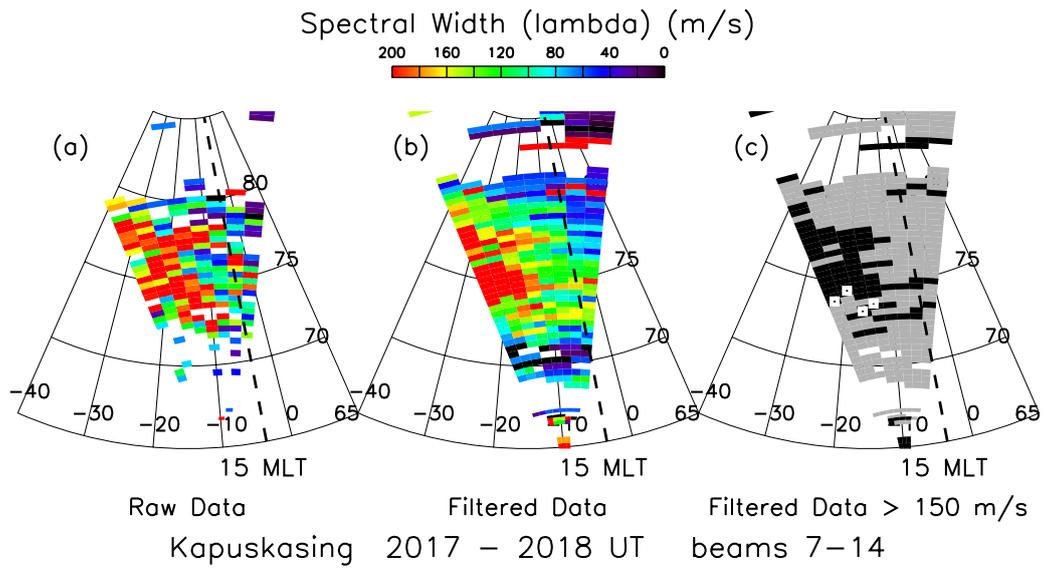


Figure 8

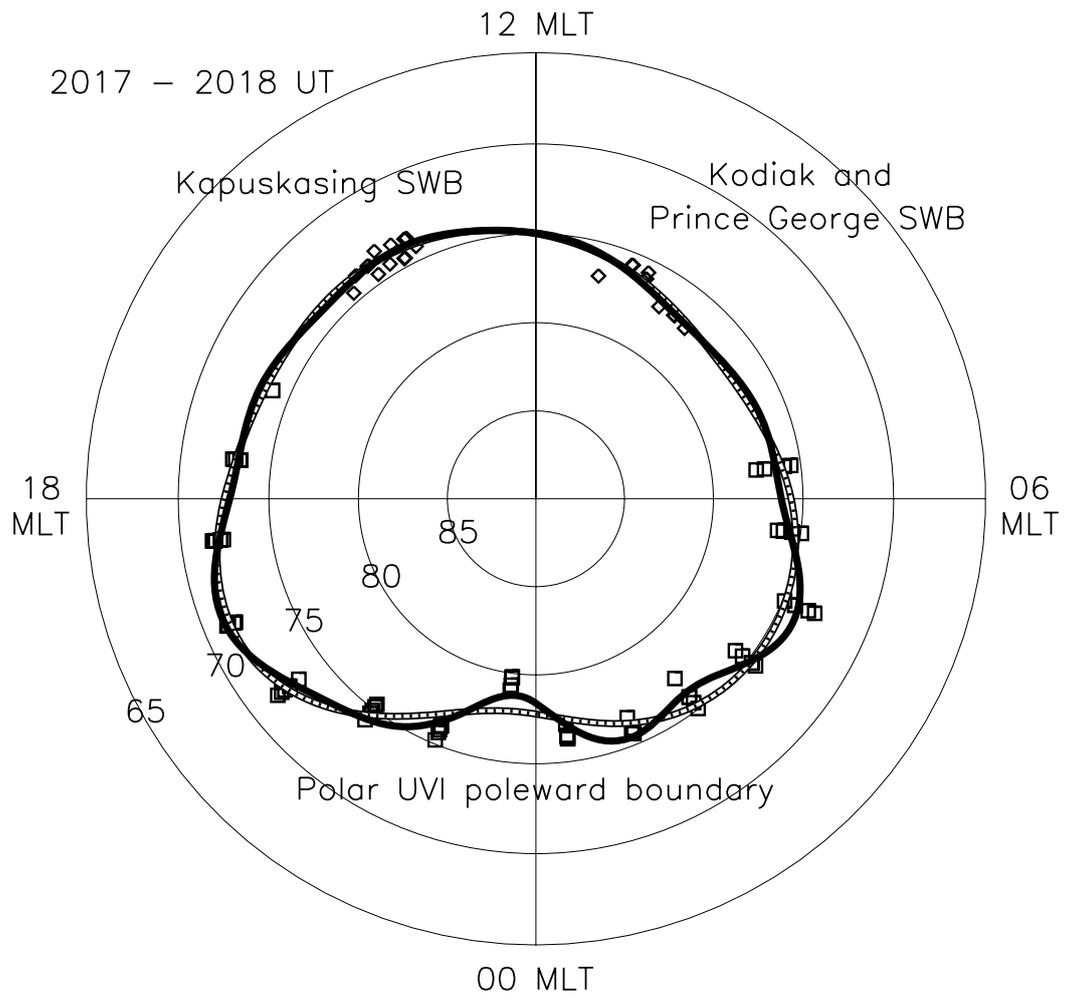


Figure 9

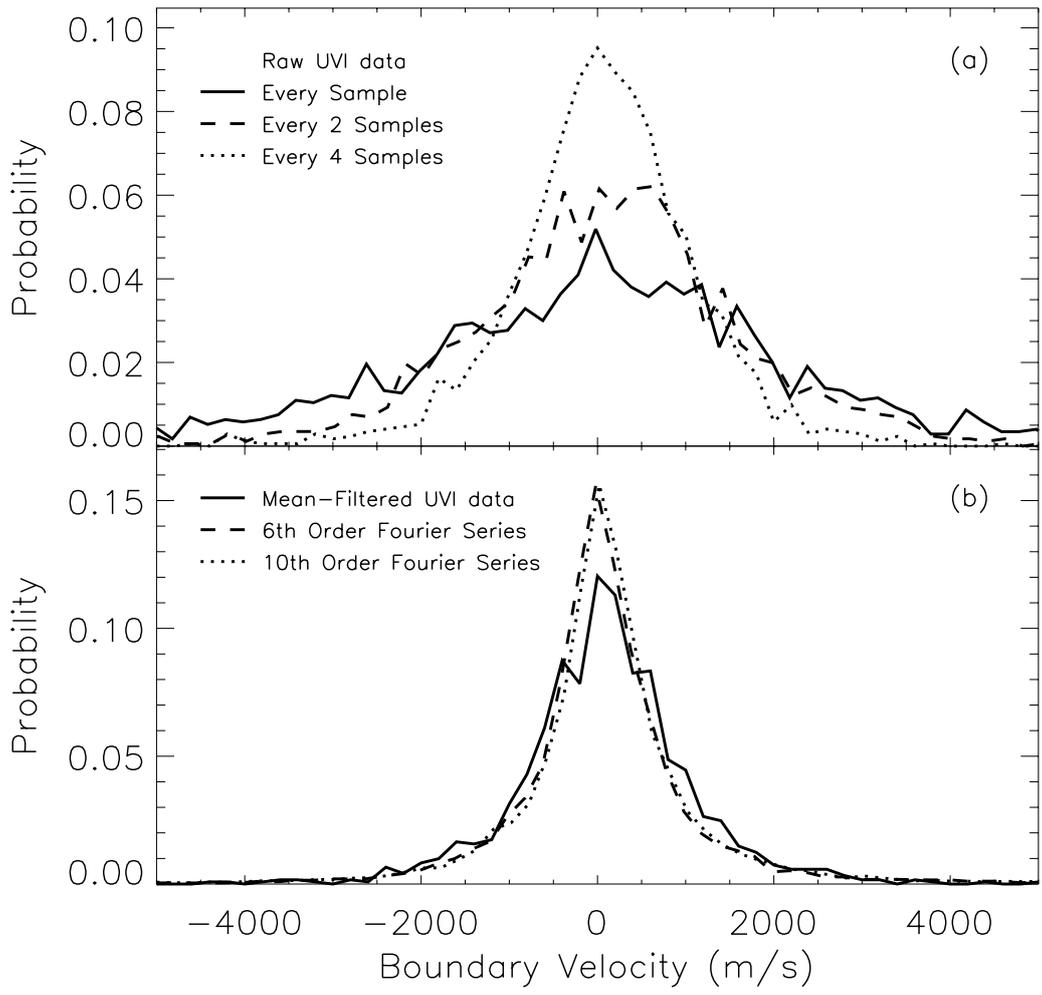


Figure 10

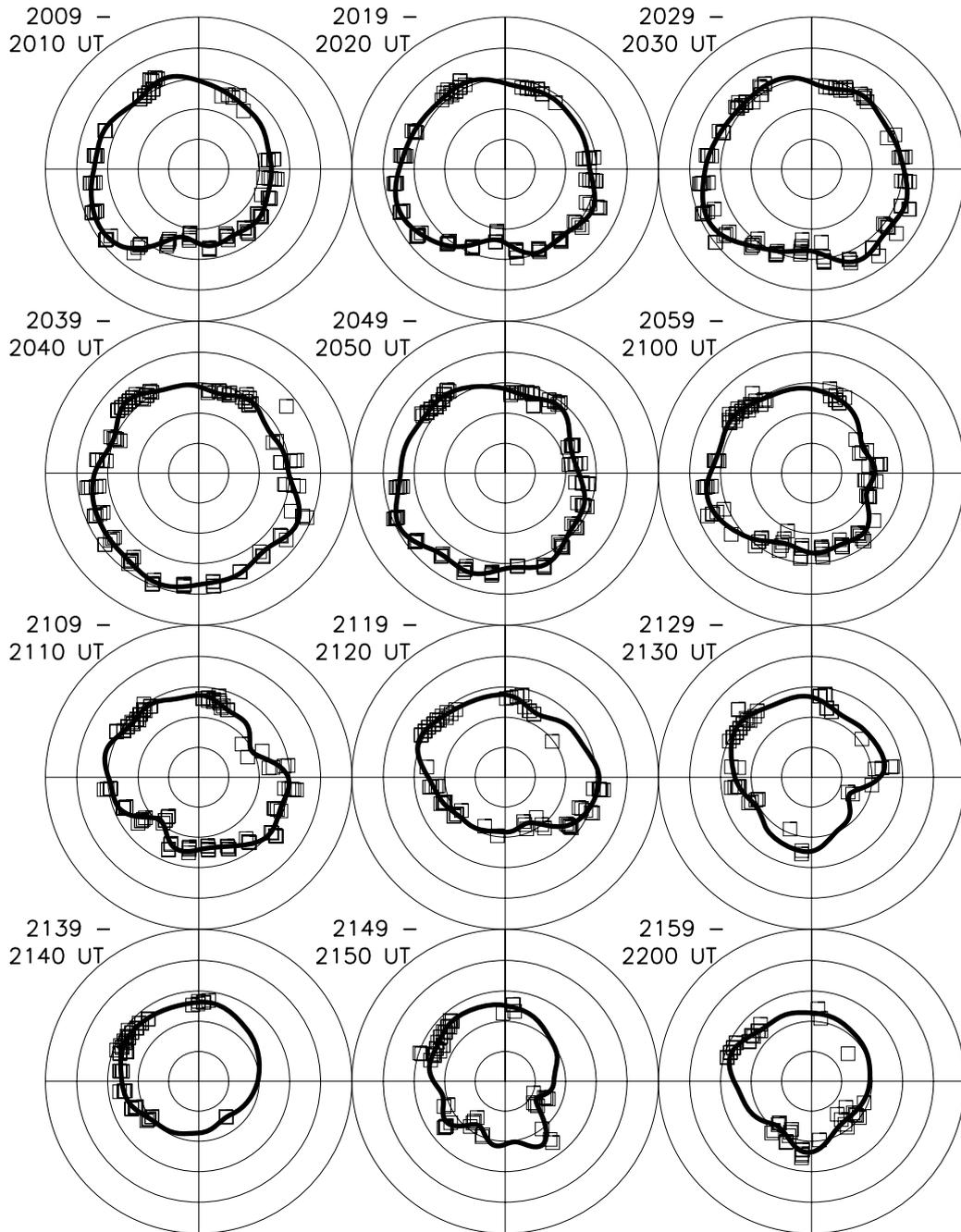


Figure 11

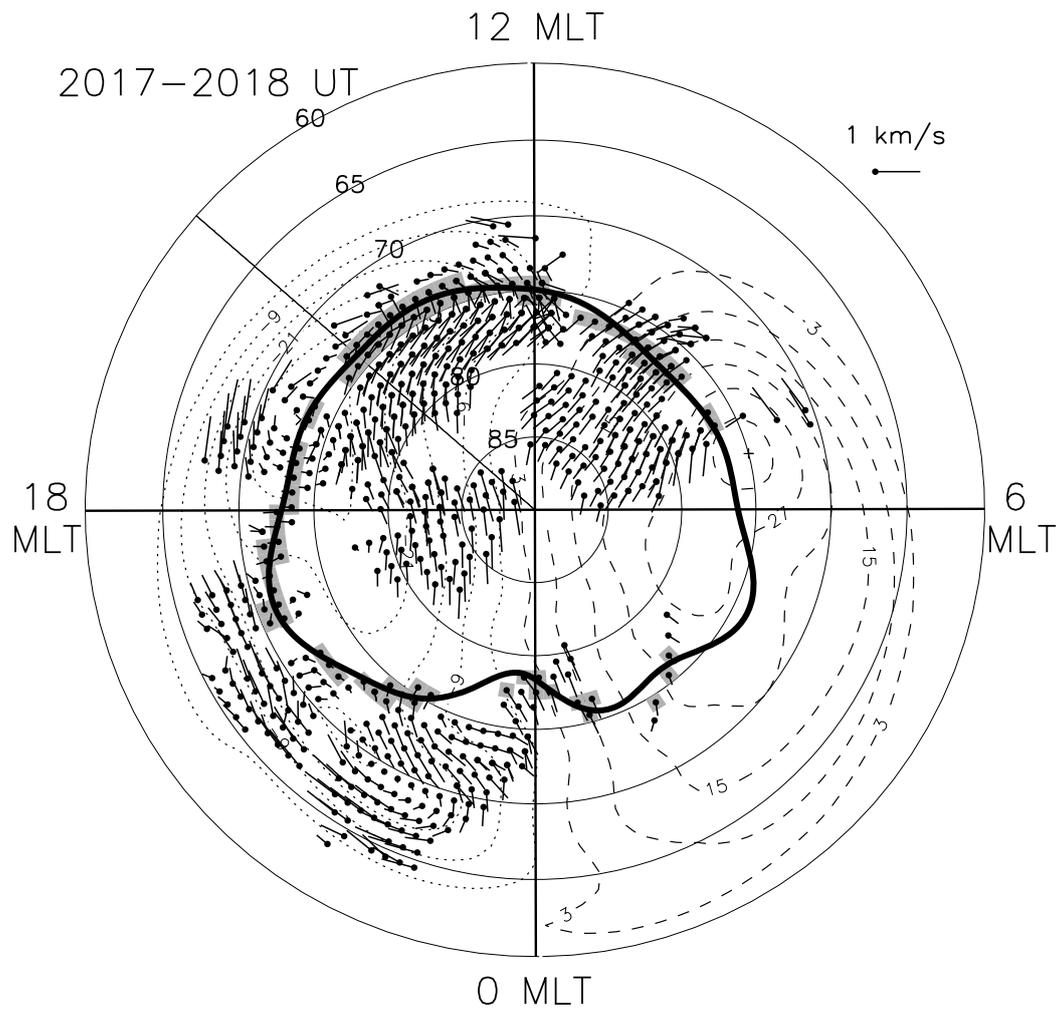


Figure 12

26 Dec 2000 – 20:17 UT

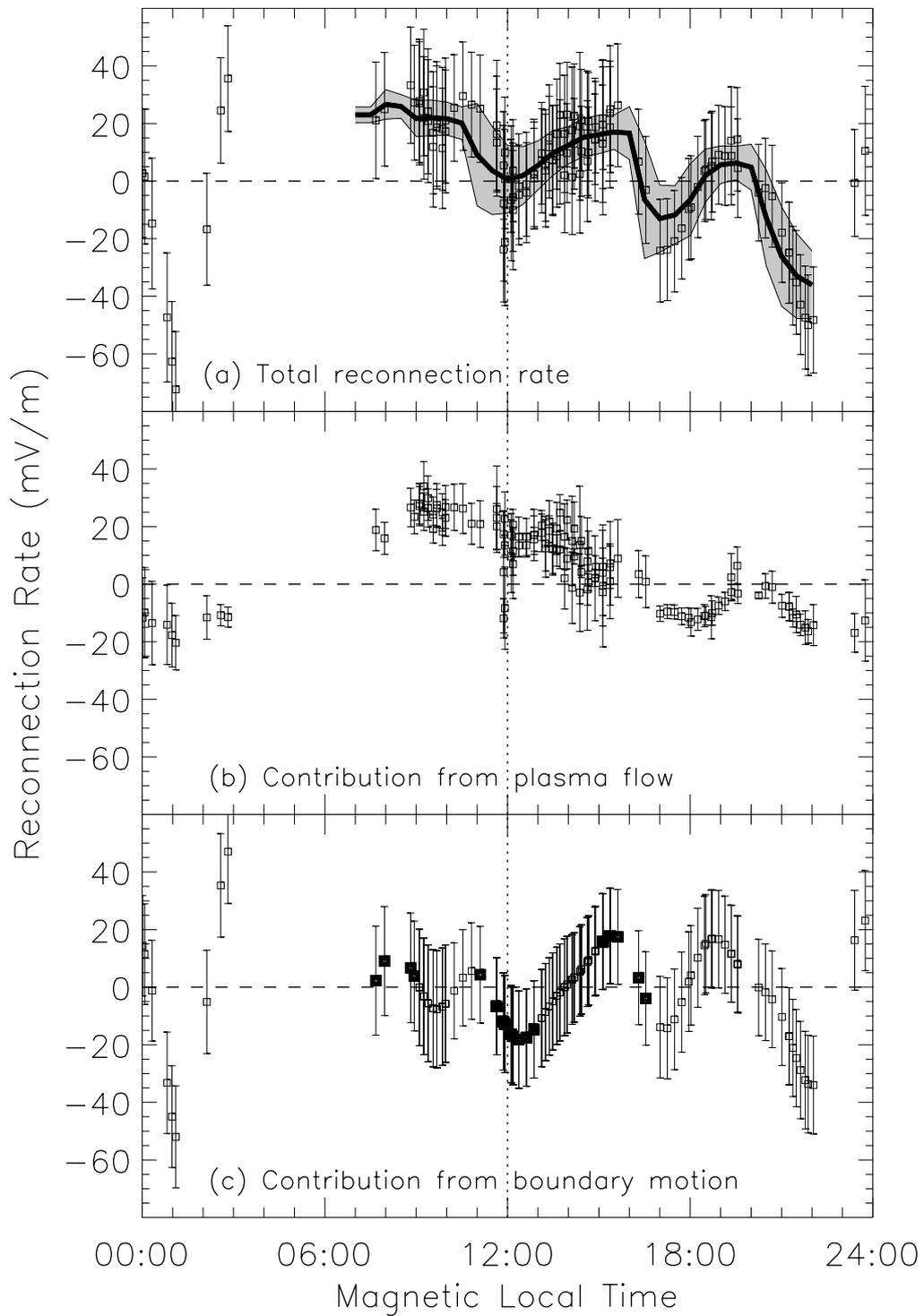


Figure 13

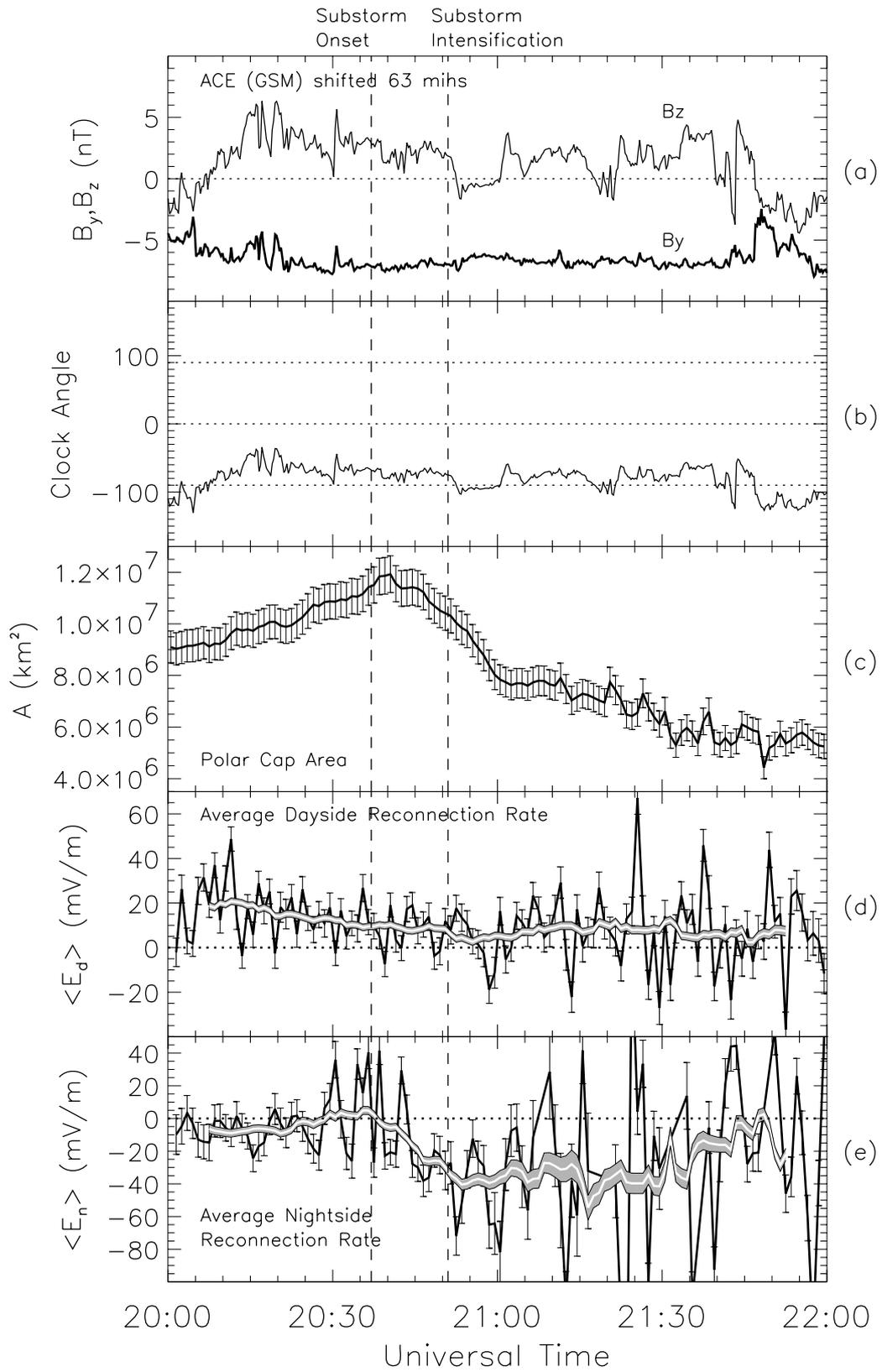


Figure 14

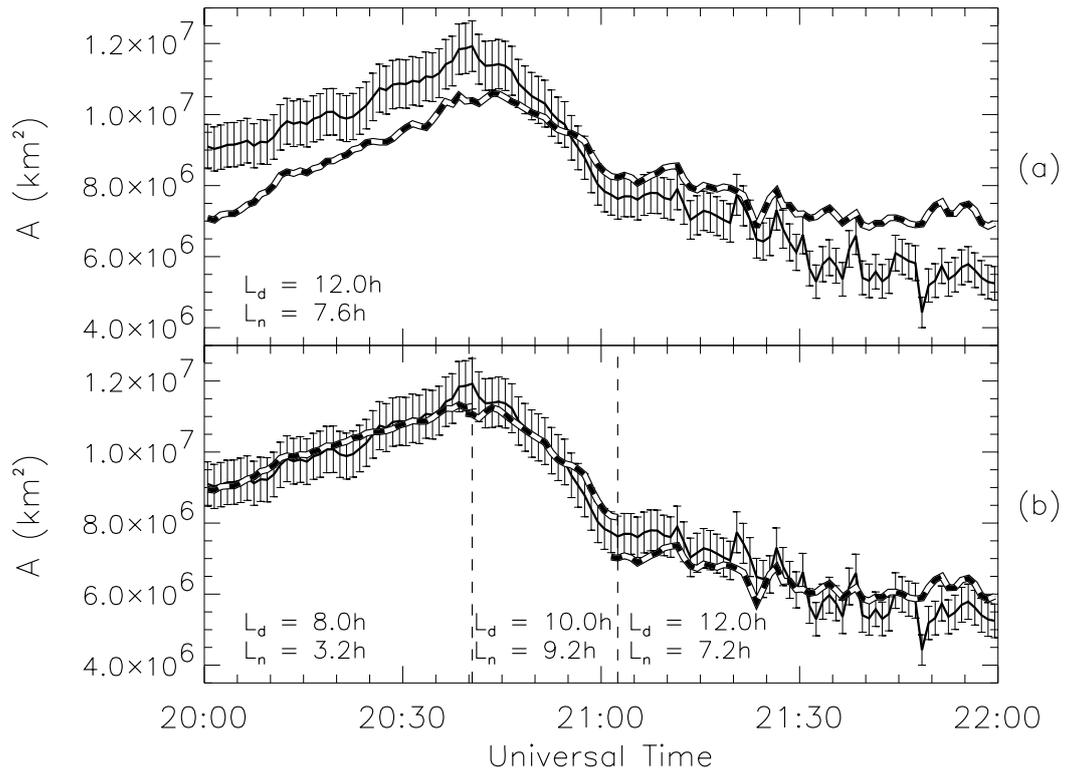


Figure 15