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#### SURGE PREDICTION AT BARROW-IN-FURNESS

BY M. AMIN, R.A. FLATHER, K.P. HUBBERT AND J.B. RAE

> REPORT NO. 4 1988

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PROUDMAN OCEANOGRAPHIC LABORATORY

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## PROUDMAN OCEANOGRAPHIC LABORATORY REPORT No. 4

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#### DOCUMENT DATA SHEET

AUTHOR	PUBLICATION
AMIN, M., FLATHER, R.A., HUBBERT, K.P. AND RAE, J.B.	DATE 1988

TITLE

Surge prediction at Barrow-in-Furness

#### REFERENCE

Proudman Oceanographic Laboratory Report, No. 4, 112pp

#### **ABSTRACT**

Over a period of 18 months starting September 1985, simultaneous sea-level measurements have been taken at Barrow-in-Furness, at two locations to the north and south of Walney Island, at Roa Island, and at an offshore position to the south of Walney Island. Subsequently, statistical formulae have been evolved relating the surge at each observational point to the surge at Heysham and to local meteorological variables. Using the forecast surge at Heysham, obtained from the Continental Shelf Model running in real time, a regression model has been developed to predict surges in the vicinity of Barrow-in-Furness. Emphasis has been placed on the correct reproduction of negative surges. Experimental runs have been carried out with a regional model of Morecambe Bay to assess the influence of local winds on sea level differences within the Bay.

This work has been carried out under contract to the Ministry of Defence. The results may be used in the formulation of Government policy, but at this stage they do not necessarily represent Government policy.

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KEYWORDS BARROW-IN-FURNESS	MODELLING	CONTRACT NSN 21A/88977		
TIDE MEASUREMENT STORM SURGE PREDICTION	MORECAMBE BAY REGRESSION ANALYSIS	PROJECT 3310 M1K-57-1		
SEA LEVEL MEASUREMENT	NEGATIVE STORM SURGES	PRICE £27		

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#### 1. OBJECTIVE

The main objective of this work has been to develop a scheme for the prediction of negative storm surge heights during spring tides at Barrow-in-Furness and on a southerly sea route from that port as far as the 10 metre depth contour.

#### 2. SYNOPSIS

Over a period of eighteen months beginning September 1985, simultaneous sea-level measurements have been taken at Barrow-in-Furness, at two locations to the north and south of Walney Island respectively, at Roa Island, and at an offshore position to the south of Walney Island near to the Halfway Shoals Buoy.

Subsequently, statistical formulae have been evolved relating the surge at each observational point to the surge at Heysham and to local meteorological variables. Using the forecast surge at Heysham, obtained from the Continental Shelf Model running in real time, a regression model has been developed to predict surges in the vicinity of Barrow within two hours of a HW at HW Springs  $(\pm\ 4\ \text{days})$ . Emphasis has been placed on the correct reproduction of negative surges.

To assist in the development of the prediction scheme a number of experimental runs have been carried out with a regional model of Morecambe Bay, to assess the influence of local winds on sea-level differences within the Bay. Earlier model simulations of negative surges within the Bay have also been examined.

#### 3. SUMMARY OF THE WORK

a. Hourly surge values for Heysham, Holyhead and Port Patrick, derived from the Continental Shelf Model running in real time, have been collected continuously between September 1984 and December 1987. Special arrangements were made with the Meteorological Office to run the model during the summer months involved, thereby avoiding a break in the series of surge values. A sub-set of this data from October 1985 to December 1986 was used for the statistical analysis of negative surges.

- b. EHM hourly tidal predictions for Heysham, Holyhead and Port Patrick have been prepared for the period January 1986 to May 1987. These were subtracted from observed hourly values to provide hourly residuals for each port.
- c. Model and observed surge values for Heysham have been compared statistically to assess the accuracy of the model forecasts near to High Water Springs. This statistical analysis of residual surges is necessary so that Heysham can be used as a reference port. Regression of the observed surge against the model forecast provides some improvement in the surge forecast. Frequency bands of high residual energy were isolated to explain those components of the surge which were not predicted properly by the model.
- d. In June 1985 an Aanderaa recorder was attached to the existing bubbler tide gauge at Ramsden Dock. In September 1985 bubbler tide gauges with Aanderaa recorders were installed at Lowsy Point and Roa Island, and an Aanderaa recorder was attached to a bubbler gauge at Hawes Point. Simultaneous records were collected from all of these recorders for nineteen months until April 1987. The gauges at Ramsden Dock and Roa Island covered the full tidal range, but there was some ponding at the Lowsy Point gauge and the gauge at Hawes Point dried out at low spring tides. These gauges were levelled in and maintained every four months when the data tapes and batteries were changed.

Also in September 1985 offshore tide gauges were deployed near the Halfway Shoals and Lightning Knoll buoys. These gauges were deployed in fixed frames with surface moorings so that the pressure recorders could be recovered from the frames and redeployed by divers every four months. The Lightning Knoll gauge was dragged from its position by a ship, its mooring lost, and a number of recovery attempts proved to be unsuccessful. The Halfway Shoals gauge was successful and was finally recovered on 30 October 1987.

Precision laboratory calibrations of all the pressure recorders were carried out before installation and after recovery.

e. Tidal analyses were carried out on the data obtained from each installed recorder and hourly residuals have been extracted for the eighteen month period from September 1985 to February 1987.

- f. Curves have been derived giving the probability of occurrence of surges at Heysham on a seasonal and state-of-tide basis. Twenty-two years of data were used for this purpose.
- g. All of the available data has been collated and negative surges observed in the vicinity of Barrow-in-Furness during October 1985 to December 1986 have been statistically analysed. The response of the sea to meteorological forces is frequency dependent, reaching a peak level in the 0.25-0.50 cycles per day band. Compilation of amplitude and phase responses in the tidal bands were not reliable because noise levels were high due to cusps and humps in the spectrum resulting from interaction between low frequency noise and tides. Although some variations were observed, an average 80 per cent of the surge energy was in the low frequency region below 0.5 cycles per day.

A regression formula for forecasting negative surges has been derived. The coefficient of air pressure is slightly less than the inverted barometric effect, and linear winds from 10°T are the most effective in generating negative surges. Numerical models underestimate surges at Roa Island and at Ramsden Dock by about 4 per cent, and by 1 per cent at Halfway Shoals. The performance is quite good at low frequencies where it accounted for more than 75 per cent of the energy. In the diurnal band efficiency decreased to 33 per cent and in the semi-diurnal and high frequency regions of the spectrum it reduced to zero. If only meteorological variables were used as input to the regression model the efficiency was marginally less than that of numerical models, the difference being mainly in the diurnal band.

h. Experiments were carried out with a regional model of Morecambe Bay to investigate the variations within the Bay arising from combinations of local wind, externally generated surge, and tide. An understanding of these variations and their causes could provide a basis for deriving improved surge estimates at points along the approach channel to Ramsden Dock from surge forecasts for Heysham produced by the operational shelf model running at the Meteorological Office. The Morecambe Bay model was used to obtain results for the M2 constituent of the tide and the model solution was verified against observations. Results were examined for spring tide conditions, with uniform winds from the north and east acting over the Bay, and for an externally generated negative surge introduced at the open boundary of the model. Simulation of a negative

surge in the period 29 January to 7 February 1986 was also carried out.

#### 4. SEA LEVEL MEASUREMENTS

The sea level measurements used in this work were from the three permanent tide gauges at Heysham, Holyhead and Port Patrick, from specially installed coastal gauges at Lowsy Point, Ramsden Dock, Roa Island and Hawes Point, and from an offshore gauge deployed at Halfway Shoals (Figure 1).

The gauges at Heysham, Holyhead and Port Patrick are part of the UK permanent tide gauge network. Heysham and Port Patrick are both stilling well and float gauges with Lea chart recorders. The installation at Holyhead has been upgraded to the modernised standard for the permanent network and integrated fifteen minute digital data is obtained by telephone link from a potentiometer unit connected to a float in a stilling well and from a differential pressure sensor connected to a bubbler system (PALIN & RAE 1987).

The coastal tide gauges installed at Lowsy Point, Ramsden Dock, Roa Island and Hawes Point all used air bubbling systems to transfer pressure from a pressure point, fixed at a known datum below low water level, to a pressure recording instrument on land. Aanderaa differential pressure recording instruments were used to record the pressure differences between the air bubbling tube and atmosphere every fifteen minutes. Measurements of sea water density allow mean values to be estimated for each site and these were used in conjunction with accurate laboratory calibrations of the pressure transducers to compute sea levels above the pressure points from the recorded data.

At Ramsden Dock permission was obtained to attach a differential pressure recorder to an existing air bubbler gauge operated by Associated British Ports. The pressure point was installed by Associated British Ports at Admiralty Chart Datum. This recorder and a POL air control unit were installed on 7 January 1985, and the instrument was maintained and data tapes retrieved on 29 April and 15 September in 1985, on 17 February, 13 May and 23 September in 1986, and on 11 February in 1987. The recorder was removed on 29 April 1987. During the first year some loss of data was caused by the compressed air supply running out, and on 21 October 1985 the air cylinders used by Associated British Ports were replaced by a POL compressor which overcame the problem.

At Lowsy Point a bubbling system with compressed air cylinders, air control unit and differential pressure recorder were installed on 14 September 1985. The datum of the pressure point was at 8.54 metres below a POL bench mark and ponding occurred at low spring tides. This installation was maintained and the data tape replaced on 18 February, 13 May and 23 September in 1986, and on 11 February in 1987. An air supply leak was responsible for loss of data after 31 July 1986 until the maintenance visit on 23 September 1986. The installation was removed on 29 April 1987.

With permission from the Royal National Lifeboat Institution the gauge at Roa Island was installed at the Barrow Lifeboat Station with the pressure point at the end of the slipway, 4.37 metres below Ordnance Datum Newlyn. The pressure point, tubing, compressed air bottles, air control unit and differential pressure recorder were installed on 16 September 1985. Due to engineering work on the slipway the air line to the pressure point had to be repositioned on 12 December 1985 but there was no evidence of significant data loss at this time. The installation was maintained and the data tape replaced on 18 February, 14 May and 23 September in 1986, and on 12 February in 1987. There was some loss of data between 14 May 1986 until the maintenance visit on 23 September 1986 due to tape problems and an air leak in the bubbling system. The installation was removed on 30 April 1987.

On 17 September 1985 a differential pressure recorder and an air control unit were attached to the bubbling system operated by Vickers at Hawes Point. The pressure point and air line of this gauge were moved by Vickers to another structure on 24 September 1985, and difficulties were reported in purging water from the air line until about 20 October 1985. The datum of the pressure point was reported as being 2.81 metres below Ordnance Datum Newlyn and there was drying out at low spring tides. This installation was maintained and the data tape replaced on 19 February, 14 May and 23 September in 1986, and on 11 February in 1987. There were some problems with data tapes between 19 February and 14 May 1986 and between 24 September and 11 February 1987. The Aanderaa recorder and air control unit were removed on 30 April 1987. Water samples were taken at each of these sites and a value of water density derived so that the pressure measurements could be converted to sea levels.

Offshore tide gauges were deployed at Halfway Shoals and at Lightning Knoll,

consisting of Aanderaa absolute pressure recording instruments mounted in heavy steel bottom frames. The frames were anchored and marked by surface buoys and pellet lines (Figure 2). Both gauges were deployed on 24 September 1985 using the Associated British Ports Hydrographic Survey Launch the Dova Haw, POL boats and a POL diving team. The Halfway Shoals gauge was deployed at position 54°01.5N, 3°11.5W, about 2.6 metres below Chart Datum, and the Lightning Knoll gauge at 53°59.7N, 3°16.0W, about 11.5 metres below Chart Datum. These sites were agreed with Associated British Ports and Trinity House, and Notices to Mariners were published and distributed to appropriate authorities and organisations (Figures 3 and 4).

On 4 December 1985 the Halfway Shoals surface buoy was reported missing, and was later recovered from Kirkcudbright. The gauge remained in position and was relocated on 21 February 1986 when POL divers retrieved the pressure recording instrument, which was maintained and replaced in the bottom frame. The surface buoy and pellet floats were replaced at the same time. The Lightning Knoll surface buoy was reported to be in position and flashing correctly on 4 December 1985, but was found floating freely and recovered by a local fisherman off Roa Island on 24 December 1985. Efforts to relocate this gauge and to replace the surface buoy were delayed by non-coincidence of good weather, tidal conditions, ship and diver availability.

The Halfway Shoals pressure recorder was again recovered and redeployed in its frame on 2 June 1986 using the Dova Haw and POL divers. The divers also carried out an unsuccessful bottom search for the Lightning Knoll frame.

On 25 September 1986 POL divers again used the Dova Haw to recover and redeploy the Halfway Shoals pressure recorder. At the same time the acoustic telemetry signal from the Lightning Knoll gauge was picked up on a hydrophone, and a marker pellet was deployed at the expected position. Attempts at dragging for the ground line were unsuccessful and acoustic contact only gave a location within about 50 metres. The Dova Haw was not available on 26 September and a 50 foot boat was hired from the Bay Towage and Salvage Company. Further acoustic contact was made with the Lightning Knoll gauge, but an extensive diver survey and further dragging revealed nothing. To have a reasonable chance of recovery by diver search the gauge would have to be located within a radius of about 5 metres by use of a double hydrophone system. Some tests were subsequently

carried out indicating that this could be feasible.

The surface marker from the Halfway Shoals gauge was reported to be on a beach at Hawes Point in April 1987 and was subsequently recovered. On 6 May 1987 attempts were made to recover the pressure recorder at Halfway Shoals and to re-locate the gauge at Lightning Knoll, using the Dova Haw fitted with a Hi-fix positioning system. At the Halfway Shoals position the divers were unable to locate any part of the gauge or its mooring within a 40 metre radius, although acoustic transmissions were received by a hydrophone system on the ship. Due to high noise levels the hydrophone system was unable to provide directional information and further diver survey was not possible. Acoustic transmissions were also received at the Lightning Knoll position but again it did not prove possible to obtain directional information without which it was considered that a further diver search would be unproductive.

On 30 October 1987 a further attempt was made to recover the two offshore tide gauges using the Dova Haw. The Halfway Shoals gauge was located on its original position and the pressure recorder was successfully recovered by POL divers. At this time it was not possible to locate the Lightning Knoll gauge and it is now considered that further recovery attempts would be unproductive since the recorder battery will be exhausted, resulting in the loss of acoustic transsissions.

A summary of the data recovered from these installed and deployed tide gauges is given in Table 1.

#### 5. SEA LEVEL DATA PROCESSING

Charts from the Lea tide gauge at Heysham have been digitised and processed to hourly levels above Admiralty Chart Datum for the period 1 January 1986 to 25 May 1987. The data was analysed using the Tidal Elevation Reduction Package (GRAFF & KARUNARATNE 1980) to provide daily, monthly, and annual mean sea levels (Table 2), monthly and annual maxima and minima elevations (Table 3), and hourly residuals (Figure 5). The residuals were obtained by comparing the hourly values derived from measurements with predicted values based on an analysis of 8 years of data starting 1 January 1964, giving 112 harmonic constants (Table 4). Also, sea levels at Heysham between 1964 and 1986 were analysed to show the probability

of surges occurring at high waters (Figure 6), at low waters (Figure 7), and on a monthly basis (Figure 8).

Similarly, charts from the Lea tide gauge at Port Patrick were digitised and processed to hourly values above 3 metres below ACD for the period 1 January 1986 to 27 April 1987. Daily, monthly, and annual mean sea levels (Table 5), monthly and annual maxima and minima elevations (Table 6), and hourly residuals (Figure 9) were calculated. The predicted hourly values were based on an analysis of 9 years of data starting 2 January 1968, giving 111 harmonic constants (Table 7).

For Holyhead, hourly heights above ACD for the period 1 January 1986 to 12 May 1987 were filtered from 15 minutes levels obtained from the differential pressure sensor and bubbler system mounted outside of the stilling well. Daily, monthly, and annual mean sea levels (Table 8), monthly and annual maxima and minima (Table 9), and hourly residuals (Figure 10) were calculated. The predicted hourly values were based on an analysis of 8 years of data starting 1 January 1964, giving 115 harmonic constants (Table 10).

At Ramsden Dock, Lowsy Point, Roa Island, Hawes Point and Halfway Shoals the output from pressure sensors, integrated over 40 seconds, was recorded on magnetic tape every 15 minutes. After translation from the data tapes the 15 minute values were converted to pressure values by application of the appropriate pressure sensor calibration data. The pressure values were then converted to sea levels using the density values derived from sea water samples taken from each of the sites. The 15 minute values were then filtered to hourly values and the resulting series tidally analysed to provide the harmonic constants listed in Tables 11 to 15. These harmonic constants were then used to calculate predicted hourly values for the period of the observations. The predicted hourly values were then subtracted from the observed hourly values to provide the residuals, examples of which are shown in Figures 11 to 15.

#### 6. STATISTICAL ANALYSIS OF SURGE DATA

#### 6.1 Introduction

Sea level responds to meteorological forces, affecting the local conditions almost instantaneously whereas the response to distant change is delayed. The

positive surge, that is the increase in sea level above the predicted tidal level due to meteorological conditions, brings floods, and negative surges, or the decrease in sea level below the predicted level, is a navigational hazard. To determine the true sea level a good surge forecast is as essential as accurate DOODSON (1924) made an extensive correlation between daily tidal predictions. mean sea level, air pressure and wind, and applied the regression technique to compute the contribution of pressure gradient to daily and monthly mean sea DARBYSHIRE & DARBYSHIRE (1956) applied the regression technique to investigate storm surges in the North Sea and detected external surges which travel from outside. HUNT (1972) and TOWNSEND (1975) applied similar regression techniques to surges on the east coast of Great Britain with additional terms to account for the effects of external surges. The response of the deep ocean to air pressure is static, but in shallow and coastal areas, wind stress and boundary conditions have significant influence on the sea level. Opinions differ on whether a linear or quadratic form of wind stress gives the best results. WELANDER (1961) used the quadratic wind stress for compilation of surges in the North Sea but suggested a very low value for the frictional constant. DAVIES ET AL (1985) have argued for a higher frictional constant in certain regions. DARBYSHIRE & DARBYSHIRE (1956) have shown that a linear wind stress gives as good results as a quadratic form. Locally, meteorological conditions may be normal, but changes which take place far away from the area under consideration can influence the sea level. To account for these external surges the areas where meteorological conditions influence surges at a port should be investigated. A simple approach is to compute the effect of external surges and to correlate surges at different ports. Surges at a port where the surge leads can then be used to update the surge at ports where it lags by estimating time lags and amplification factors. This technique can be applied if surges are consistent in The approach worked well for positive surges on the east coast of Britain (DARBYSHIRE & DARBYSHIRE, 1956). However, progression of negative surges differ from those of positive surges in that the amplification factor and rate of progression is found to vary from surge to surge (TOWNSEND, 1975).

Statistical methods are unable to deal with the decaying process of a surge when meteorological forces are removed, with surge-tide interaction or with the dynamics of the system. HEAPS (1969) introduced a numerical method and used a numerical model based on a finite difference scheme to study the dynamics of surges and tides. The Celtic Sea and the Irish Sea are now extensively explored

by these numerical techniques (PROCTOR, 1987). At present, numerical models have been developed to the stage where an operational model (FLATHER, 1981) is regularly used for computing surges in the Irish Sea.

The main objectives of the present work are: (a) to develop a regression model for forecasting surges, negative surges in particular, in the vicinity of Barrow-in-Furness; (b) to examine the efficiency of numerical and regression models and to locate the areas where differences arise.

#### 6.2 Analysis of observed surges and meteorological data

of surge elevations, air pressures, east-west (u) Time series north-south (v) components of winds have been statistically examined for changes both in the time and frequency domains. Surges from all stations are strongly correlated (Table 16) and surges at Holyhead lead others by about one hour. Typical cross-correlation functions between observed surges at Heysham, Port and Halfway Shoals are shown in Figure 16a. Patrick. Ramsden Dock between surges and air pressure, and surges and the Cross-correlations v-component of winds are very strong (Figure 16b). However, correlations between surges and the u-component of winds are weak but are still above the level of These cross-correlations further suggest that surges lead air significance. pressure. Depressions, which are responsible for time-variation of air pressure, often travel eastward and the response of the sea is faster than the rate of travel of these depressions. This tendency for sea level to lead air pressure changes was first identified in Newlyn observations by DOODSON (1924). lead of surge elevations is considered to be due to winds which are correlated with, and anticipate, pressure changes. The sub-tidal energy is continuous across the spectrum and accounts for over 80% of the energy (Figure 17). The spectrum of air pressure energy is much steeper than those of the wind This suggests that the contribution of air pressure to surges is relatively large at low frequencies.

#### 6.3 Regression technique

Under normal meteorological conditions, variations in the sea level are due to the influence of well-defined tide-generating forces and the interaction of waves due to these forces. These changes in the sea level can be predicted on

any time scale. The changing pressure fields and associated winds over the sea surface introduce new forces into the system and sea level adjusts itself to accommodate these forces. Under the combined influence of tidal and meteorological forces, sea level at time t, measured from the mean sea level at a port, can be expressed as

$$\zeta_{t} = \zeta_{t}^{(T)} + S_{t} + Z_{t}$$
 (1)

where  $\zeta_t^{(T)}$  is the tidal component,  $S_t$  is the surge component,  $Z_t$  is the noise due to forces which are not accounted for here.

Since  $\zeta^{(T)}$  can be estimated quite accurately, the surge and changes due to meteorological forces can be separated as

$$R_{t} = \zeta_{t} - \zeta_{t}^{(T)} = S_{t} + Z_{t}$$
 (2)

In the previous section, it is shown that surge elevations are correlated with air pressure as well as with winds, and it is difficult to distinguish between the contribution of one input force from that of the other. The response to these inputs is frequency dependent and the error on estimated values increases with frequency. A better approach is to use a multi-regression technique in which surge elevations are regressed with simultaneous air pressure and wind components as

$$R_{t} = a_{1}P_{t-\tau_{1}} + a_{2}u_{t-\tau_{2}} + a_{3}v_{t-\tau_{3}} + Z_{t}$$
(3)

for a time sequence  $t_s=[s=0(1)m]$ , if  $1 \le m$  meteorological variables are included, equation (3) gives a system of equations which can be written as

$$\underline{R}_{t} = \underline{Ma} + \underline{Z} \tag{4}$$

since  $\underline{Z}$  has no direct relationship with the surge, the least squares solution of the system of equations (3) gives

$$a = [M'M]^{-1} M'R$$
 (5)

where  $\underline{\underline{M}}$ ' is the transpose of  $\underline{\underline{M}}$ .

Regression coefficients computed from the observed input meteorological variables and the output surges, give the response of the sea level to individual forces. Some further refinement can be made to optimise the solution by replacing the linear wind by a quadratic wind stress and by changing the time lags so that the efficiency of the model is maximised.

The effectiveness of meteorological variables and their relative importance in the generation of surges at different ports is clearly demonstrated by the high level of correlations in Figure 16. To maximise the efficiency of the regression model, meteorological inputs and surge output are filtered to remove high frequencies (> 1.5 cpd) which are not correlated. However, it is found that this filtering process does not affect the results very much as energy in the high frequency region is very small (Figure 17).

The surge at Holyhead has the greatest time lead over the surge at Ramsden Dock, being of the order of one hour, and this could not be included in the model as a spatial variable. The surge at Fishguard could not be included because of poor quality data.

For these reasons the regression model was based on meteorological inputs from Squires Gate. First, equation (4) was solved for all surges in bi-monthly sets, with wind input in the linear form, and the resulting coefficients are listed in Table 17. Coefficients were also estimated by using wind in the quadratic form and by adjusting the time lags. The results shown in Table 17 are for the optimal solution when winds are in the linear form, with air pressure leading the surge by one hour, and the v-component of wind leading the surge by 6 hours. The response of sea level to the u-component of wind is instantaneous. Time lags, computed from the simultaneous solution for air pressure, v-component and u-component of wind, are significantly different from those given by the correlation functions in Figure 16, thus suggesting that the contribution of one variable has considerable influence on the function of the other.

Air pressure has an almost inverted barometric effect on the sea level. The v-component of the wind is four times more effective than the u-component in the generation of surges around Barrow. The most effective directions of winds for negative and positive surges are 10°T and 190°T respectively.

Averaged coefficients were used to compute Oct-Dec 1985 surges, which were not used in the evaluation of regression coefficients. Statistics in Table 18 show that the regression model gives almost as good results as a numerical model.

When equation (4) is solved to compute the regression coefficients for only negative surges in 1986, a considerable change in the response of the sea level is observed. Coefficients in Table 19 show that the response to wind is doubled although the influence of air pressure is almost unchanged. The most effective wind direction for the generation of negative surges is 17°T. There may be a small time lag between meteorological inputs and surge output but this is not detected because the scanning interval is 3 hours and the response of the sea level appears to be instantaneous.

Surges reproduced by using the regression coefficients in Table 19 are shown in Figure 18. Visually, it is difficult to establish whether regression model surges or numerical model surges are best. Mathematically, the superiority of numerical models is quite clearly shown by the variance of unpredicted surges (Table 20).

#### 6.4 Relationship between negative surge and tide phases

The phases of observed surges are examined for their relationship with the phase of tide. No particular relationship is observed as surge peaks are shown to occur at rising as well as falling tides (Figure 19). Some troughs of surges are also seen to occur at high tides and others at low tides. Also troughs of negative surges are underestimated in magnitude in that forecast surges are always higher than the minima of observed surges.

#### 6.5 Numerical Model

Numerical models can take the dynamics of the system into account and can therefore deal with natural oscillations and the decaying process of the surge when meteorological forces are removed. Regression models have no mechanism to deal with these problems (PROUDMAN & DOODSON, 1924). Numerical models can also deal better with external surges and their progression as compared with regression models. An operational model of the Irish Sea (FLATHER, 1981) was used to forecast surges for the 1985-86 period. A comparison between the spectra

of the observed and model surges (Figure 20a) shows that the model underestimates the surge energy throughout the spectrum. Differences between the regression model and the numerical model occur in the diurnal band where the numerical model is more efficient. The amplitude responses of the Heysham model to observed negative surges are given in Table 21. The response of the surge to input from the model (Figure 21) confirms the result that model surges are underestimated and lag observed surges. Also, models are not efficient enough to deal with the frequency dependence of the response functions. The performance of the numerical model in different frequency bands is shown in Figure 20b. This suggests that models collapse in semi-diurnal and higher frequency regions where surge-tide interaction is more important than the direct influence of meteorological forces. On average the numerical model is about 5% more efficient than the regression model (Table 18).

#### 6.6 Conclusions

- (1) The efficiencies of the numerical model and of the regression model in reproducing surges vary from surge to surge. On average, the numerical model can account for 65% and the regression model for 59% of the variance of a surge.
- (2) In the regression model, the response of the sea level to air pressure is about -0.81cm mb<sup>-1</sup>, and winds from  $10^{\circ}$ T (190°) are the most effective for the generation of negative or positive surges.
- (3) The regression model performs better with linear winds than with quadratic winds.
- (4) Spatial gradients of air pressure were always small and could not improve the regression model.
- (5) In the frequency domain, both the numerical model and the regression model are quite efficient at low frequencies where they can account for over 75% of the surge variance. In the diurnal band the efficiency drops to 33% for the numerical model and to 25% for the regression model.
- (6) Both the numerical and the regression models are unable to reproduce semi-diurnal surges or surges resulting from surge-tide interaction.

- (7) The numerical model surges are underestimated by 4% at Ramsden Dock and at Roa Island and by 1% at Halfway Shoals.
- (8) In the case of negative surges, the efficiency of both the numerical and regression models decreases further. The influence of wind is almost twice as much as that for all surges, but the response to air pressure is unchanged. The effective wind direction for negative surges is 17°T. However, a change in this direction has only a small effect, possibly because of the uncertainty due to the small sample size.

#### 7. NUMERICAL MODEL OF MORECAMBE BAY

#### 7.1 Introduction

In this section, we describe some experiments with a regional model of Morecambe Bay. The aim of the experiments was to investigate the variations within the Bay arising from combinations of local wind, externally generated surge and tide. An understanding of these variations and their causes could provide a basis for deriving improved surge estimates at points along the approach channel to Ramsden Dock from surge forecasts for Heysham produced by the operational shelf model running at the Meteorological Office.

In the following sub-sections, we give an outline of the model; describe results obtained for the  $\mathrm{M}_2$  constituent of the tide, with verification of the model solution against observations; and give results for spring tide conditions, uniform winds from the north and east acting over the Bay, and for an externally generated negative surge introduced at the open boundary of the model. Simulation of a negative surge in the period 29 January to 7 February 1986 is also described.

#### 7.2 Outline of the model

The model used in the investigations is based on the depth-averaged equations expressed in spherical polar co-ordinates, which take the form:

Continuity

$$\frac{\partial \zeta}{\partial t} + \frac{1}{R\cos\emptyset} \left\{ \frac{\partial}{\partial \chi} (DU) + \frac{\partial}{\partial \emptyset} (DV\cos\emptyset) \right\} = 0 \tag{1}$$

U equation of motion

$$\frac{\partial U}{\partial t} - 2\omega \sin \phi V + \frac{U}{R\cos \phi} \frac{\partial U}{\partial \chi} - \frac{UV}{R} \tan \phi + \frac{V}{R} \frac{\partial U}{\partial \phi}$$

$$= -\frac{g}{R\cos \phi} \frac{\partial \zeta}{\partial \chi} - \frac{1}{\rho R\cos \phi} \frac{\partial p_a}{\partial \chi} + \frac{\tau_{sx}}{\rho D} - \frac{\tau_{bx}}{\rho D}$$
(2)

V equation of motion

$$\frac{\partial V}{\partial t} + 2\omega \sin \phi U + \frac{V}{R} \frac{\partial V}{\partial \phi} + \frac{U^2 \tan \phi}{R} + \frac{U}{R \cos \phi} \frac{\partial V}{\partial \chi}$$

$$= -\frac{g}{R} \frac{\partial \zeta}{\partial \phi} - \frac{1}{\rho R} \frac{\partial \rho a}{\partial \phi} + \frac{\tau_{sy}}{\rho D} - \frac{\tau_{by}}{\rho D}$$
(3)

where the notation is:

 $\chi, \phi$  east-longitude and latitude, respectively,

t time

ς elevation of sea surface above the undisturbed level,

h undisturbed depth of water,

 $D=h+\zeta$  total depth of water,

R radius of the Earth,

 $\omega$  angular speed of the Earths rotation,

ρ density of sea water,

g acceleration due to gravity,

 $\tau_{sx}$ ,  $\tau_{sy}$  components of surface wind stress to the east and north respectively,

 $\tau_{\rm bx}, \tau_{\rm by}$  components of bottom stress to the east and north resp.,

P<sub>a</sub> atmospheric pressure at the sea surface, U,V components of depth mean current given by

$$U = \frac{1}{d} \int_{-h}^{\zeta} u(z) dz \qquad , \qquad V = \frac{1}{d} \int_{-h}^{\zeta} v(z) dz \qquad (4)$$

u(z),v(z) components of current in the directions of increasing  $\chi, \emptyset$  respectively, at a depth z below the undisturbed sea surface.

The surface stress,  $\tau_s$ , is assumed to be related to the surface wind velocity at 10m, w, by a quadratic law:

$$\tau_{s} = c_{D} \rho_{a} w w$$
(5)

where  $ho_{
m a}$  is the density of air and  $m C_{
m D}$  is a surface drag coefficient, itself related to wind speed by

$$C_{D} = (0.63 + 0.066 | w|).10^{-3}$$
 (6)

(SMITH & BANKE, 1975).

A quadratic law of bottom friction is used to relate the bottom stress,  $\tau_b$ , to the depth mean current:

$$\tau_{b} = k\rho \underbrace{\bigcup}_{i=1}^{n} \underbrace{\bigcup}_{i=$$

where k takes a constant value of 0.0025.

In the equations of motion, the surface and bottom stresses are divided by the total water depth, D. In order to prevent these terms from becoming infinite in the shallow water areas where drying occurs, a minimum value for D of 1.0m is used in these terms.

Boundary conditions of zero normal flow

$$q_{\perp} = 0 \tag{8}$$

are applied on coastal or land boundaries, where  $\mathbf{q}_n$  is the normal component of depth mean current. On open-sea boundaries, either elevation is specified as a function of position and time

$$\zeta = \hat{\zeta}(\chi, \emptyset, t) \tag{9}$$

or a "radiation" condition

$$q_n = \hat{q}_n - \frac{c}{h}(\zeta - \hat{\zeta}) \tag{10}$$

is applied, where  $\hat{q}_n$  and  $\hat{\zeta}$  are specified and  $c=(gh)^{\frac{1}{2}}$ .

The equations are solved by means of an explicit finite-difference technique, incorporating the essential elements of the schemes described in FLATHER & HEAPS (1975) and DAVIES & FLATHER (1978). An important feature of the system is that it allows for the displacement of the coastal boundary, so permitting the exposure of drying banks with the falling tide and their subsequent submergence as the tide rises again to be represented in the model solution. The approach used was developed by FLATHER & HEAPS (1975) and

incorporates a critical elevation difference between adjacent grid boxes. This was set to be 0.1m.

The computational grid, covering Morecambe Bay and part of the neighbouring eastern Irish Sea, is shown in Figure 22 and is an adaptation and improvement of that used by STEPHENS (1983). The resolution has 54 grid elements per degree of longitude and 81 per degree of latitude, giving a grid size of 1.21 km E-W and 1.37 km N-S. This is sufficient to represent the main features of the bathymetry of the Bay but does not allow the narrow channels, such as that between Ramsden Dock and Hawes Point to be represented in detail: a grid size of no more than 100m would be required for this. The model bathymetry is plotted in Figure 23. The important features to note are the Lune Deep with a maximum depth of 47m, which forms a deep water channel to Heysham, the extensive area of shallow banks in the northern part of the Bay and the channel through to Barrow. The timestep used in the model calculations was 37.26 s.

#### 7.3 Results for M<sub>2</sub> and spring tides

Calculations were carried out first to reproduce the main  $\rm M_2$  constituent of the tide. Open boundary input data for use in the (preferred) radiation condition (10) were taken from STEPHENS (1983). Starting from an initial state of zero surface elevation and no motion, the model was run for a total of 12 cycles of  $\rm M_2$  to establish the tidal regime. Data, comprising arrays of computed surface elevation and depth-mean current were stored at intervals of 1/4 lunar hour during the final cycle for subsequent analysis.

Figure 24 shows contours of amplitude and phase of  $\rm M_2$  obtained from this analysis. It is closely similar to the distributions previously published, but amplitudes are slightly (~10cm) larger than those obtained by FLATHER & HEAPS (1978) and slightly (~5cm) smaller than those produced by STEPHENS (1983).

A comparison between computed and observed values of the amplitude and phase of  $\rm M_2$  is given in Table 22, along with the source of the "observed" data. The observed values from DOODSON & CORKAN (1932) are, in fact, estimates which are less reliable than values derived from harmonic analyses. It should also be noted that some comparisons, indicated by \*, are affected by the fact that either the relevant model grid point dries out near low water or the tide gauge is

located in an area subject to "ponding" or both.

Overall, the agreement is excellent, particularly along the approach channel to Barrow (see results for Ramsden Dock, Roa Island and Halfway Shoals). The phase differences between Ramsden Dock and Halfway Shoals (6.0° in the model and 6.1° from the observations) and the equivalent amplification of the  $\rm M_2$  constituent (1.044 in the model and 1.038 from observations) suggest that the model reproduces the tidal propagation extremely accurately, remarkably so given the rather coarse representation of the channel mentioned earlier.

Having established the ability of the model to reproduce the  $\mathrm{M}_2$  tide accurately, consideration was given to modelling spring tide conditions. Two alternative approaches were available: (i) introduce an additional constituent,  $\mathrm{S}_2$ , which, combined with  $\mathrm{M}_2$  gives a variation in the tidal range from approximately mean spring to mean neap conditions; (ii) scale the  $\mathrm{M}_2$  tidal input by an appropriate factor so as to approximate mean spring tides.

For investigation of the response of the Bay to surges at spring tides, the first option has the disadvantage of yielding a continually varying tidal range, which presents some difficulties in sychronising spring tides and the surge effects to be investigated. The second approach, on the other hand, would give perpetual spring tide conditions, effectively removing this difficulty. Consequently the second approach was adopted for this purpose whereas the first approach was used in simulating a specific surge event as described later.

An examination of observed tidal ranges at Barrow, Heysham, Liverpool and Holyhead suggested that the appropriate scaling factor was 4/3 and the input values of elevation and depth-mean current for  $\mathrm{M}_2$  were consequently multiplied by this factor to approximate mean spring conditions. The model was then re-run, in similar fashion to that described earlier for  $\mathrm{M}_2$ , except that arrays of elevation and current at every timestep during the final tidal cycle were stored, permitting a detailed examination of the results. The maximum and minimum values of computed elevation were then extracted and the difference taken, giving an estimate of the mean spring tidal range from the model. Equivalent values from observations are not readily available, and indeed, mean high water springs (MHWS) and mean low water springs (MLWS) are parameters which cannot be derived easily from a set of harmonic constants nor from a tidal record. However,

approximate values are published in the Admiralty Tide Tables, and a fair estimate can be derived from harmonic constants by taking twice the sum of the amplitudes of  $\rm M_2$  and  $\rm S_2$ . Table 23 gives a comparison of the various estimates available for locations not affected by drying (in the model) or ponding. The agreement overall is very good. In particular, the model reproduces the varying range of spring tide along the approach channel to Barrow remarkably accurately.

#### 7.4 Response of Morecambe Bay to local winds and externally generated surges

Having established that the model is capable of representing the tides, and in particular, spring tides with good accuracy, the next stage in the investigation was to consider surge effects. Surges will, in general, be made up of a component generated with the Bay, mainly by the local winds acting over its surface, and a component generated outside the Bay in the eastern Irish Sea and beyond. Previous work on surge variations within Morecambe Bay (FLATHER 1981) suggested that there could be significant local variability associated with drying and other processes, and that resolution could be important in determining how a model represented these effects. The grid size of the present model is finer (by a factor of 3) than the finest model used by FLATHER (1981) and so should give a more realistic representation of these effects than obtained previously.

Three basic model runs were carried out to determine the response of the Bay to:

- (i) a uniform easterly wind stress acting over the interior;
- (ii) a uniform northerly wind stress; and
- (iii) an external surge, constant in time and uniform in magnitude, introduced at the open boundary.

In cases (i) and (ii), the wind stress magnitude was taken to be 1  $N/m^2$ , which, adopting the drag coefficient due to SMITH & BANKE (1975) as used in the operational storm surge model (e.g. FLATHER, 1984), corresponds to a wind speed of about 20m/s, which is gale force. In case (iii), the external surge magnitude was taken to be -1m. In every case, the storm surge response was computed together with the spring tide so as to take account of interaction effects.

The procedure adopted was to start from the solution for spring tides established previously and to switch on the appropriate forcing. For case (iii), using the radiation condition (10), the external surge contribution to  $\hat{\zeta}$  was taken to be -1m at all open boundary points, and the corresponding contribution to  $\hat{q}_n$  was assumed to be zero. The model was then run for a further 3 tidal cycles to allow the solution to adjust to the additional forcing. During this period, data were stored at intervals of 1/4 lunar hour and at every timestep during the final cycle. A corresponding run without meteorological forcing or external surge input gave the solution for spring tides alone, which could be subtracted from the combined solution to give the surge residual.

The evolution of the surge residuals for a sample of grid points shown in Figure 25 is plotted in Figures 26 (east wind), 27 (north wind) and 28 (external surge) for the 3 tidal cycles during which the forcing was applied. It is clear from Figures 26-28 that the adjustment of the Bay was very rapid, taking only a few (perhaps 2-3) hours. This is an important point, since it suggests that, except for local winds or external surges that vary rapidly in time, the response of the Bay will be nearly stationary. The surge repsonses do nevertheless show very significant variations with time, but these variations are clearly related to the tidal cycle and repeat with the tidal period. They can, therefore, be attributed to surge-tide interactions. The most extreme manifestation of these effects can be seen in Figure 28, where, for some locations zero (or near-zero) residuals occur during part of each tidal cycle when the grid point is "dry".

The response to easterly winds tends to be small except, predictably, near the eastern side of the Bay, where residuals are typically -25cm; see, for example, point (32,23) corresponding to Heysham. Here, the residuals are slightly enhanced near low waters and decreased near high waters, consistent with the variability in the forcing term,  $\tau_{\rm S}/{\rm D}$ , implied by tidal changes in total water depth, D. At shallower points in the east of the Bay, the tidal variation is much stronger, with residuals reaching -70cm in the early stages of the rising tide. These effects are associated with a phase lag of the low water of tide and surge on that due to tide alone.

Detailed responses, comprising variations of tide alone, tide with easterly winds and residual plotted using values stored at every timestep during the final cycle for points located along the approach channel from Halfway Shoals to Barrow

are shown in Figure 29. These plots show a number of interesting features. First, a distortion of the tidal curve, increasing towards Ramsden Dock, and producing not only the expected lengthening of the period of falling tide and shortening of the rising tide but a marked "bumpiness" in the 2-3 hours before high water. This may be due to interaction between the flows entering the channel from the north and the south. The effect is closely similar in both tide surge and tide only solutions. Also apparent are shorter period oscillations, again affecting both tide only and tide + surge solutions in These oscillations are seiching motions set up in sections of the channel by the drying out or flooding of neighbouring model elements. Their periods, typically a few minutes, depend on the water depth in the particular section of channel affected. Both of these effects could be influenced by the rather coarse model resolution and the lack of detailed bathymetric data for the channel from Ramsden Dock to Lowsy Point. However, the main conclusion is that the residuals due to easterly winds acting over the Bay are small, only about -10cm in magnitude near high water.

The response to winds from the north tends to be larger at points in the northern part of the Bay, with values reaching -100cm at some locations and certain times. The detailed plots, Figure 30, show that the largest residuals, occurring in the early stages of the rising tide, increase in magnitude towards Ramsden Dock reaching a maximum of -65cm there. However, the residuals near high water are substantially smaller, typically -20cm, although the "bumpiness" and seiching effects mentioned earlier cause some variability. The model results for winds from the east and north are, therefore, consistent with those from the analysis of observations in suggesting that the wind direction most likely to produce negative surges at Barrow is roughly NNE.

Finally, Figures 28 and 31 show equivalent results for the externally generated surge. The responses are substantially greater than those typical of local wind effects, reaching a maximum magnitude of about -180cm. There is a marked contrast between the results at locations in deeper water close to the main body of the Bay such as Heysham (32,23), Halfway Shoals (18,23) and Wyre Light (27,29), and at points in the shallower regions, for example Ramsden Dock (17,18). At deeper points, the response is fairly constant and equal to the input value, with small variations of order 10cm. At shallower locations, the variations, closely related to the tides, are dominant. Figure 31 shows very

clearly the development of the interaction between Halfway Shoals and Ramsden Dock. The greatest variation in the residual, from -45cm to -172cm at Ramsden Dock, occurs near low water but significant residual oscillations with amplitude 10-20cm persist up to the time of high water. It would appear, therefore, that tide-surge interactions which develop along the approach channel to Barrow will be very important in determining surges and total water levels at Ramsden Dock. The fact that the operational surge model, with resolution 30km, is unable to even begin to resolve this channel implies that it would not on its own be able to predict these variations.

It is of interest, then, to examine the possibility that the present model, taking account of those interaction effects, might give improved predictions for Ramsden Dock. This question is examined in the next section.

#### 7.4 Simulation of a negative surge using the Morecambe Bay model

In order to examine further the development of surges in the approaches to Ramsden Dock and to determine whether the Morecambe Bay model might improve on the predictions produced by the operational shelf model, a simulation of the period 29 January to 7 February 1986 was carried out with the model. This period contained the largest negative surge registered at Ramsden Dock during the period of the measurements.

Two model runs were carried out: the first for tide alone, with open boundary input representing the  $\rm M_2$  and  $\rm S_2$  constituents. The  $\rm S_2$  data required were inferred from the  $\rm M_2$  data by assuming a constant amplitude ratio  $(\rm S_2/\rm M_2)$  of 0.324, and a constant phase difference  $(\rm S_2-\rm M_2)$  of -315.850; these values being derived from tidal analyses for Ramsden Dock. Specification of two input constituents yields a tide with a spring-neap variation (as discussed earlier) approximating the true tide during the period of interest. Figure 32 shows the model-predicted tides for representative locations. The second model run was for tide and surge together. In this, the externally generated surge, introduced with the tide on the model open boundary was assumed to be given by the surge predicted by the operational model at the nearest grid point to Morecambe Bay. Output distributions of surface wind and pressure computed by the Met. Office's 15-level weather prediction model were processed to provide forcing by components of wind stress (using (5) and (6)) and variations in surface atmospheric

pressure.

Model computed distributions of elevation and depth-mean current in components from both solutions were stored at intervals of 1 hour. Differences, giving the surge component, were then computed. Time series of computed surge for points along the channel from Halfway Shoals to Ramsden Dock and for Heysham are plotted in Figure 33, with hourly observed residuals at Halfway Shoals, Ramsden Dock and Heysham also included. As might be expected from results presented in the preceding section, there is increasing variability in the form of short period oscillations with amplitude O(20cm) towards Ramsden Dock.

Figure 34 shows, on a larger scale, for Halfway Shoals and Ramsden Dock, the surge residuals derived from observations, from the present solution, and from the operational shelf model. The times of tidal high water are indicated by a circle on the nearest hourly observed residual. At Halfway Shoals there are differences of up to 7cm between the surge computed using the Morecambe Bay model and that from the shelf model with, perhaps, some small improvement in accuracy on the basis of comparison with the observations. However, this improvement is small compared with the largest errors, which are up to 30cm.

For Ramsden Dock, there are much greater differences - up to 20cm - between the surge computed using the present model and that from the shelf model. These differences are substantially due to the oscillations which occur in the Morecambe Bay model solution and which, on the basis of the results of the preceding section, are associated with tide-surge interaction effects in the approach Channel. However, there is also a more slowly varying component which does appear to give better agreement with observations than provided by the shelf model; in particular near the peak of the negative surge early on 2 January.

The accuracy to which the surges at Halfway Shoals and Ramsden Dock can be predicted is clearly dependent upon the accuracy of the externally generated surge open boundary input. This is illustrated in Figure 34 on the second day of the storm (30 January 1986) when both the Morecambe Bay and operational models considerably underestimate the magnitude of the negative surge.

#### 7.5 Conclusions

- 1. The Morecambe Bay model is able to reproduce the  $\mathrm{M}_2$  component of the tide with good accuracy. Spring tide conditions also seem to be reproduced very well.
- 2. The model was used to investigate the responses of the Bay to local winds and to externally generated surges. The adjustment time of the Bay to imposed forcing was found to be short, perhaps 2-3 hours.
- 3. The wind responses were consistent with the findings of the statistical analysis in suggesting that winds from NNE would be most effective in generating negative surges at Barrow.
- 4. There are significant "tidal" variations in the surge residuals taking the form of damped oscillations which increase in magnitude along the approach channel to Barrow. These effects appear to be due to tide-surge interactions.
- 5. The computed responses suggest that these locally generated variations will be significant in determining surge residuals at Ramsden Dock. The effect of local winds blowing over the Bay was to produce negative surges at Ramsden Dock at high water in the range 10-20 cm. The response at Ramsden Dock to an externally generated negative surge of 1m also included variations in the surge residual of this magnitude near tidal high water.
- 6. Simulation of surge and tide motion during the period 29 January to 7 February 1986 gave results consistent with those expected on the basis of the analysis of responses.
- 7. Significant local variations were predicted by the model and there was some indication that the results were marginally better than those from the operational shelf model. However, a substantial contribution to the total error arose from the surge introduced on the open boundary of the Morecambe Bay model, taken directly from the shelf model.

- 8. If surges along the approach channel to Barrow are to be predicted with typical accuracy better than 20cm, improved estimates of the externally generated surge component and the ability to take account of the local surge-tide interactions will be needed.
- 9. The limitations of the present model in resolving the approaches to Barrow must be borne in mind. It would be useful to construct and experiment with a high resolution (~100m grid) model to confirm (or otherwise) the importance of the surge-tide interactions found here.
- 10. A very high resolution model could also provide information on currents which could be useful for navigation and dredging purposes.

#### 8. RECOMMENDATIONS

Regarding the requirement for practical forecasts, both the regression model and the operational surge model can provide useful information. It is suggested that both approaches be implemented and the "worst case", whether this results from the regression model or the dynamical model, be used. It should be noted that both techniques tend to underestimate the magnitude of negative surges on some occasions.

The experiments with the Morecambe Bay model suggested that effects due to local winds and interaction in the approaches to Ramsden Dock must be significant. Further work might provide a better understanding of these local influences, leading eventually to a more satisfactory forecast procedure.

#### 9. ACKNOWLEDGEMENTS

This work has been carried out by the Proudman Oceanographic Laboratory under contract to the Ministry of Defence. The authors gratefully acknowledge the contributions of a number of colleagues at POL, especially those involved in the hard work of measurement and processing of the tidal data required.

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Location	Visits	Data Recovery	Comments			
Lowsy Point	14 Sept 85 18 Feb 86 13 May 86 23 Sept 86 11 Feb 87 29 Apr 87	14 Sept - 16 Feb 18 Feb - 13 May 13 May - 31 July 23 Sept - 11 Feb 11 Feb - 29 Apr	Installed (ponding) Tape run out Air supply leak Data loss			
Remades Dock	7 Jan 85		(tape problems)  Aanderaa installed			
Ramsden Dock	29 Apr 85 15 Sept 85 17 Feb 86 13 May 86 24 Sept 86 11 Feb 87	7 Jan - 29 Apr 29 Apr - 15 Sept 15 Sept - 17 Feb 17 Feb - 13 May 13 May - 24 Sept 24 Sept - 11 Feb	Air supply problems Compressor fitted			
	29 Apr 87	11 Feb - 29 Apr	22 extra scans			
Roa Island	16 Sept 85 18 Feb 86 14 May 86	16 Sept - 12 Feb 18 Feb - 14 May	Installed Tape run out			
	23 Sept 86 12 Feb 87 30 Apr 87	14 May - 23 Sept 23 Sept - 12 Feb 12 Feb - 30 Apr	Air leak, errors  Some data loss (tape)			
		12 Feb = 30 Apt				
Hawes Point	17 Sept 85 19 Feb 86 14 May 86	20 Oct - 19 Feb 19 Feb - 14 May	Installed (dries) Air supply problems			
	24 Sept 86 11 Feb 87 30 Apr 87	14 May - 24 Sept 24 Sept - 11 Feb 11 Feb - 30 Apr	6 extra scans			
Halfway Shoals	23 Sept 85 21 Feb 86 2 June 86	23 Sept - 15 Feb 21 Feb - 2 June	Deployed Tape run out			
	25 Sept 86 6 May 87 30 Oct 87	2 June - 25 Sept 25 Sept - 4 Aug	Set to 30 min sampling Recovery attempt Recovered			
Lightning Knoll	23 Sept 85 21 Feb 86 2 June 86		Deployed Recovery attempt " "			
	25/26 Sept 86 6 May 87 30 Oct 87		11 11 11 11.			

Table 1: Data recovery from POL installed tide gauges

### MEAN SEA LEVEL PRINT-OUT

PORT - HEYSHAM YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

4.975 5.111	4.871 5.177 5.316 5.513	5.117 4.895 5.524 5.453	4.963 5.029 5.678 5.607	5.111 5.030	5.519 5.042	5.461 5.160	5.249 5.140	5.519 5.234	5.816 5.115	5.108 4.721
4.683 MONTHLY MEAN FEBRUARY	SEA LEVEL	5.204	NO OF DAYS	31						
4.494 4.504	4.807 4.913 5.091 5.150 SEA LEVEL								4.901	5.014
4.643 4.891	5.147 5.455 5.156 5.089	5.427 5.328 5.515 5.115	5.133 5.174 5.393 5.381	5.123 5.344	5.017 5.166	5.027 5.209	5.072 5.460	5.097 5.399	5.138 5.232	5.152 5.192
MONTHLY MEAN APRIL	SEA LEVEL	5.194	NO OF DAYS	31						
5.181 5.107 5.061 4.936 MONTHLY MEAN	4.989 4.940 5.132 5.224 SEA LEVEL	4.869 4.771 5.334 5.273 5.041	4.608 4.589 5.271 5.235 NO OF DAYS	4.645 5.195 30	4.603 6 5.113	4.883 5.132	4.999 5.133	5.099 5.224	5.149 5.169	5.147 5.214
MAY 5.119 5.108 5.154 5.350 5.101	5.151 5.144 5.390 5.081	5.195 5.217 5.200 5.483	5.238 5.192 5.379 5.300	5.217 5.285	5.494 5.360	5.362 5.274	5.513 5.470	5.418 5.130	5.311 5.017	5.268 5.076
MONTHLY MEAN JUNE	SEA LEVEL	5.258	NO OF DAYS	31						
5.070 5.071	5.134 5.108 5.037 5.020 SEA LEVEL									
5.122 5.154	5.181 5.239 5.002 5.042	5.239 5.227 5.121 5.116	5.168 5.120 5.114 5.116	5.110 5.119	5.074 5.194	5.030 5.244	5.027 5.280	5.036 5.276	5.051 5.285	5.051 5.281
MONTHLY MEAN AUGUST	SEA LEVEL	5.149	NO OF DAYS	31						
5.271 5.537	5.123 5.130 5.098 5.066									
MONTHLY MEAN SEPTEMBER	SEA LEVEL	5.128	NO OF DAYS	31						
5.197 5.218 5.006 4.942 MONTHLY MEAN OCTOBER	5.051 5.023 4.839 4.941 SEA LEVEL	5.076 5.095 5.028 5.099 5.074	5.085 5.034 5.098 5.074 NO OF DAYS	5.054 5.052 30	5.075 5.079	5.072 5.150	5.084 5.196	5.148 5.190	5.129 5.086	5.039 5.071
5.139 5.057	5.025 5.015 5.357 5.482	5.103 5.101 5.489 5.498	5.149 5.113 5.592 5.392	5.282 5.699	5.222 5.810	5.121 5.232	5.141 5.357	5.178 5.391	5.159 5.447	5.039 5.601
MONTHLY MEAN NOVEMBER	SEA LEVEL	5.273	NO OF DAYS	31						
4.977 5.077	5.097 5.097 5.442 5.309 SEA LEVEL	5.287 5.116 5.248 5.287 5.345	5.414 5.420 5.886 5.512 NO OF DAYS	5.725 5.477 30	5.676 5.620	5.299 5.424	5.290 5.193	5.436 5.168	5.402 5.097	5.381 5.128
DECEMBER 5.304 5.337 5.441 5.510 5.374	5.616 5.530 5.581 5.448	5.594 5.314 5.193 5.015	5.519 5.425 4.884 4.958	5.292 5.151	5.364 5.168	5.506 5.266	5.433 5.268	5.493 5.435	5.311 5.446	5.641 5.570
MONTHLY MEAN	SEA LEVEL	5.367	NO OF DAYS	31						
ANNUAL MEAN	SEA LEVEL	5.171	NO OF DAYS	365						

#### EXTREME HOURLY ELEVATIONS PRINT-OUT

PORT - HEYSHAM YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

MONTH	I I	MI HEIGHT	NIMA DAY	HR.	I I	MA HEIGHT	XIMA DAY	HR.
JANUARY FEBRUARY MARCH APRIL MAY JUNE JULY AUGUST SEPTEMBER OCTOBER NOVEMBER DECEMBER		0.879 0.379 0.810 0.597 0.916 0.962 0.828 0.806 0.675 0.684 0.699 0.896	30 27 26 25 24 23 24 21 19 6 4	21 20 18 18 18 6 7 6 7 7		10.319 9.793 10.720 10.159 10.180 9.803 9.880 9.963 9.821 10.000 10.439	14 11 27 26 25 24 21 20 19 5	14 13 12 12 12 0 0 0 0 13 12
ANNUAL	I	0.379	27	20	I	10.720	27	12

#### DATUM = ORDNANCE DATUM (NEWLYN)

MONTH I	MI HEIGHT	NIMA DAY	HR.	I I I	MA HEIGHT	XIMA DAY	HR.
JANUARY I FEBRUARY I MARCH I APRIL I MAY I JUNE I JULY I AUGUST I SEPTEMBER I OCTOBER I NOVEMBER I DECEMBER I	-4.021 -4.521 -4.090 -4.303 -3.988 -4.072 -4.094 -4.225 -4.216 -4.201 -4.004	30 27 26 25 24 23 21 19 6 4	21 20 18 18 18 6 7 6 7 7		5.419 4.893 5.820 5.259 5.280 4.980 5.063 4.921 5.100 5.190 5.539	14 11 27 26 25 24 21 20 19 5	14 13 12 12 12 0 1 0 0 0 13 12
ANNUAL I	-4.521	27	20	I	5.820	27	12

0.249 m

PORT TITLE ENGLAND, WEST COAST - HEYSHAM

IOS ATT THR COUNTRY SEA LATITUDE. LONGTTIDE PORT NO PORT NO SHEET NO CODE CODE

50 441 74 19 54 2' 0.3"N 2 54' 42.3" W

DATA

I.ENGTH TYP D M YEAR CONSTANTS UNTT TIME TIME SOURCE RECORD (DAYS) NDC OTH SWC ZONE STEP NUMBER

7064 0 01 1 1964 91 -47 GMT 3.0 POL

TIDE GAUGE OBSERVATION ADMIRALTY CHART SO ZERO (TGZ) DATUM (OBD) DATUM (ACD) (TO OBD) ODN + 0.000 m TG2 + 0.000 m ODN - 4.90 m

ACD + 4.900 m 7.190 m TGBM -

TGBM : BOLT SOUTH QUAY SD 4030 6012

NODAL CORRECTIONS U AND F OF DOODSON CONSTANTS SET TO 0. AND 1. FOR PREDICTIONS

\*\*\* CONSTITUENTS \*\*\* \*\*\* CONSTITUENTS \*\*\* н G STG NΩ NAME H G SIG NO NAME 0.095 239.77 0.04107 SA 0.012 263.5: SN4 58.43973 0.025 127.93 0.08214 SSA 0.115 294.20 58.98410 MS4 50 0.013 205.66 0.54437 MM 0.033 300.53 59.06624 0.020 226.79 1.01590 MSE 0.014 335.14 60.00000 52 Ç٨ 0.023 216.30 1.09803 MF SK4 0.008 60.08214 345.65 53 0.007 291.36 12.85429 2Q1 0.010 350.85 86.40794 54 2MN6 0.037 345.69 13,39866 8 0.019 11.65 86.95231 351.72 0.009 13.47151 RH01 MSN6 0.006 41.45 87,42383 56 0.111 42.70 13.94304 10 01 0.020 56.13 87.96821 57 2MS6 0.011 277 77 14.02517 11 MP1 0.006 56.90 88.05035 58 2MK6 0.011 265.00 14.49205 12 М1 0.004 94.07 88.98410 59 2SM6 0.003 133.73 14.91786 PIl 14 0.004 107.93 89.06624 60 MSK6 0.044 183.33 14.95893 15 **P1** 0.005 203.02 26,40794 2MN2S2 61 16 17 0.012 101.80 15,00000 S1 0.010 224.84 26.87018 0.121 15.04107 191.54 K1 0.017 215.72 26.95231 63 3M2S2 0.005 143.50 15.08214 18 PSI1 0.004 249.23 28.35759 65 SNK2 0.003 190.17 15.12321 19 PHI1 0.005 248.96 42.38277 68 моз 0.003 221.83 15.51259 20 THETA1 0.003 341.85 43.00928 2MP3 69 0.004 290.16 15.58544 21 J1 0.004 172.04 44.56955 70 2M03 0.006 19.33 16.05696 22 SO1 71 72 0.007 7.29 56.87018 3MK4 0.003 334.83 16.13910 23 001 0.012 12.40 56.95231 3MS4 24 25 0.012 256.57 27.34170 0Q2 0.005 65.20 57.88607 2MSK4 73 0.009 85.12 27.42383 MNS2 0.005 232.60 73.00928 76 3MO5 0.079 278.81 27.89535 26 2N2 0.003 316.39 86.48079 82 2MV6 0.023 67.27 27.96821 27 257.57 88.51258 3MSN6 0.003 85 0.600 301.63 28.43973 28 N2 177.02 0.004 114.84767 87 2(MN)8 29 30 0.137 300.84 28.51258 NII2 0.011 200.27 115.39204 88 3MN8 0.012 OP2 293.89 0.015 225.39 115.93642 89 M8 3.150 325.31 28.98410 31 M2 2MSN8 0.009 237.85 116.40794 90 0.010 MKS2 138.55 29.06624 32 0.021 271.61 116.95231 3MS8 0.058 337.02 29.45563 LAMDA 2 0.005 275.93 117.03445 92 3MK8 0.141 343.50 29.52848 34 L2 0.008 301.87 117,96821 94 2 (MS) 8 0.057 358.25 29.95893 35 Т2 0.004 314.79 118.05035 95 2MSK8 1.026 7.73 30.00000 36 S2 0.003 28.91 145.93642 4MS10 0.011 9.92 37 30.04107 R2 27.49669 27.88607 0.008 71.71 101 MVS2 0.294 6.74 30.08214 38 K2 97.72 2MK2 0.032 102 0.031 212.71 30.54437 39 MSN2 0.021 277.82 28.94304 103 MA2 0.007 30,62651 222.44 40 KJ2 0.009 9.09 29.02517 MA2\* 104 0.035 232.46 31.01590 41 2SM2 0.016 229.98 31.09803 106 SKM2 0.013 275.99 42.92714 моз 0.006 335.36 56.40794 107 2MNS4 0.036 311.99 43.47616 43 мз 220.30 57.49669 0.021 108 MV4 0.010 340.81 43.94304 44 S03 0.017 91.94 58.51258 109 3MN4 0.013 54.80 44.02517 45 MK3 331.39 147.94 0.011 59.52848 110 2MSN4 0.014 100.64 45.04107 46 SK3 28.39866 NA2 0.008 111 0.072 47 214.99 57.42383 MN4 0.003 333.39 28.48080 NA2\* 0.195 243.90 57.96821 48 M4

#### MEAN SEA LEVEL PRINT-OUT

PORT - PORTPATRICK YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

```
JANUARY
     5.308 5.186 4.999 5.311 5.221 5.004 5.217 5.197 5.229 5.572 5.357 5.136 5.345 5.317 4.866
4.912 5.053 5.199 5.273 5.337 5.326 5.505 5.302 4.835 4.958 5.128 5.056 5.168 5.083 4.787
   MONTHLY MEAN SEA LEVEL
                                                  5.159
                                                                   NO OF DAYS
                                                                                         31
FEBRUARY
   4.621 4.598 4.835 4.918 4.944 4.890 4.859 4.946 4.981 5.080 5.102 5.051 5.095 5.110 5.153 5.091 5.064 5.085 5.104 5.117 5.186 5.087 4.997 5.009 5.024 4.957 4.855 4.781 MONTHLY MEAN SEA LEVEL 4.984 NO OF DAYS 28
MARCH
     4.738 4.910 5.147 5.368 5.349 5.216 5.064 5.202 5.100 4.971 5.010 5.072 5.113 5.163 5.181 5.154 5.086 5.127 5.040 5.372 4.988 5.288 5.211 5.191 4.980 5.102 5.364 5.299 5.104 5.097 5.146
   MONTHLY MEAN SEA LEVEL
                                                  5.134
                                                                   NO OF DAYS
                                                                                         31
APRIL
     5.054 4.998 4.905 4.855 4.790 4.729 4.634 4.615 4.655 4.646 4.823 4.929 5.050 5.133 5.060 4.914 4.845 5.040 5.162 5.247 5.219 5.193 5.155 5.103 5.045 5.081 5.075 5.202 5.125 5.170
   MONTHLY MEAN SEA LEVEL
                                                  4.982
                                                                   NO OF DAYS
MAY
     5.120 5.066 5.047 5.107 5.166 5.179 5.193 5.145 5.175 5.387 5.242 5.427 5.280 5.219 5.133 5.082 5.297 5.293 5.033 5.163 5.374 5.260 5.203 5.188 5.260 5.180 5.259 4.992 4.904 4.978
   MONTHLY MEAN SEA LEVEL
                                                  5,172
                                                                   NO OF DAYS
                                                                                         31
JUNE
   4.954 4.981 5.014 4.979 4.975 5.007 5.062 5.164 5.318 5.156 5.010 5.062 5.016 4.932 4.944 5.042 5.013 4.981 5.027 4.975 4.994 5.060 5.084 5.149 5.092 5.012 5.025 5.002 4.998 5.054 MONTHLY MEAN SEA LEVEL 5.036 NO OF DAYS 30
JULY
     5.078 5.125 5.127 5.176 5.185 5.161 5.105 5.057 5.065 5.033 5.005 5.005 5.016 5.025 5.038 5.191 5.037 4.959 4.999 5.054 5.064 5.044 5.035 5.075 5.140 5.201 5.237 5.220 5.150 5.207
     5.165
   MONTHLY MEAN SEA LEVEL
                                                  5.096
                                                                   NO OF DAYS
AUGUST
(INCOMPLETE)
5.191 5.352 5.069 5.096 5.111 5.279 5.073 5.010 5.008 4.998 4.975 5.014 5.141 5.237 5.289
5.160 5.083 5.045 5.010 5.003 5.096 5.078 0.000 0.000 0.000 0.000 0.000 0.000
     0.000
   MONTHLY MEAN SEA LEVEL
                                                  5.105
                                                                   NO OF DAYS
                                                                                         22
SEPTEMBER
(INCOMPLETE)
     0.000 0.000 0.000 4.947 4.981 5.012 5.001 4.978 5.006 5.022 5.033 5.048 5.111 5.059 4.964 4.938 4.880 4.792 4.890 4.967 5.023 5.037 5.022 5.007 5.044 5.100 5.137 5.130 5.035 5.055
                                                  5.008
   MONTHLY MEAN SEA LEVEL
                                                                   NO OF DAYS
OCTOBER
     5.090 4.993 4.970 5.002 5.060 5.034 5.056 5.085 5.231 5.163 5.069 5.119 5.154 5.143 5.014
4.955 5.087 5.287 5.295 5.303 5.322 5.401 5.199 5.563 5.399 5.100 5.353 5.262 5.264 5.396
     5.094
   MONTHLY MEAN SEA LEVEL
                                                   5.176
                                                                   NO OF DAYS
                                                                                         31
NOVEMBER
     4.936 5.019 5.006 4.977 5.126 5.021 5.283 5.194 5.659 5.554 5.217 5.306 5.483 5.386 5.352
   5.501 5.302 5.321 5.207 5.170 5.238 5.722 5.225 5.280 5.434 5.211 5.085 5.109 5.029 5.073 MONTHLY MEAN SEA LEVEL 5.248 NO OF DAYS 30
DECEMBER
     5.177 5.218 5.484 5.375 5.373 5.248 5.523 5.293 5.148 5.317 5.411 5.445 5.413 5.236 5.542 5.233 5.299 5.356 5.132 4.949 4.868 4.802 4.878 5.063 5.059 5.084 5.043 5.211 5.268 5.423 5.229
   MONTHLY MEAN SEA LEVEL
                                                  5.229
                                                                   NO OF DAYS
                                                                                         31
   ANNUAL MEAN SEA LEVEL
                                                                   NO OF DAYS 353
                                                  5.111
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### EXTREME HOURLY ELEVATIONS PRINT-OUT

PORT - PORTPATRICK YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

MONTH	I I	MI HEIGHT	NIMA DAY	HR.	I I	M/ HEIGHT	AXIMA DAY	HR.
JANUARY FEBRUARY MARCH APRIL MAY JUNE JULY AUGUST SEPTEMBER OCTOBER NOVEMBER DECEMBER		3.059 2.959 3.036 2.914 3.185 3.061 3.060 2.942 3.159 3.090 3.182	30 28 1 7 28 26 23 20 18 6 4	21 20 21 17 9 7 6 5 7		7.439 7.048 7.413 7.037 7.111 7.006 7.120 7.103 6.970 7.192 7.150 7.373	10 11 27 26 25 25 25 22 21 19 16 12	11 13 12 13 0 1 2 1 0 11 21
ANNUAL	I	2.914	7	17	I	7.439	10	11

#### DATUM = ORDNANCE DATUM (NEWLYN)

MONTH	I I	MEIGHT	INIMA DAY	HR.	Ĭ	MA HEIGHT	AXIMA DAY	HR.
JANUARY FEBRUARY MARCH APRIL MAY JUNE JULY AUGUST SEPTEMBER OCTOBER NOVEMBER DECEMBER	ĪIIIIIIIIIIIII	-1.741 -1.841 -1.764 -1.886 -1.604 -1.739 -1.740 -1.858 -1.641 -1.710 -1.618	30 28 1 7 28 26 23 20 18 6 4	21 20 21 17 99 76 57 65		2.639 2.248 2.613 2.237 2.311 2.206 2.320 2.320 2.303 2.170 2.392 2.350 2.573	10 11 27 26 25 25 25 22 21 19 16 12	11 13 12 13 0 1 2 1 0 1 0 1 2
ANNUAL	I	-1.886	7	17	I	2.639	10	11

PORT TITLE : SCOTLAND, WEST COAST - PORTPATRICK

TOS ATT THR COUNTRY SEA LATITUDE LONGITUDE PORT NO SHEET NO PORT NO CODE CODE 63 18 54 50' 32.7" N 5 7' 8.0" W DATA LENGTH TYP D M YEAR CONSTANTS UNIT TIME TIME SOURCE RECORD (DAYS) NDC OTH SWC ZONE STEP NUMBER 3287 1 1968 93 0 2 0 GMT 3.0 TOS 160 TIDE GAUGE OBSERVATION ADMIRALTY CHART S0 ZERO (TGZ) DATUM (OBD) DATUM (ACD) (TO OBD) ODN -4.800 m TGZ + 0.000 m ODN - 1.80 m 5.115 m ACD -3.000 m

MSL IS THE MEAN OF NINE YEARS - 1968 - 1976 (INCLUSIVE) TGEM: OSEM (BOLT) ON TOP OF HARBOUR WALL (NW99765421)

TGBM -

9.820 m

\*\*\* CONSTITUENTS \*\*\* \*\*\* CONSTITUENTS \*\*\* H G SIG NO NAME H G SIG NO NAME 0.082 238.07 0.003 92.09 59.06624 MK4 0.04107 SA 0.032 180.15 0.08214 SSA 0.003 227.71 60.00000 52 **S4** SK4 0.020 209.89 0.54437 3 MM 0.002 225.97 60.08214 53 2MN6 1.01590 86.40794 54 0.011 226.37 MSF 0.002 221.09 0.020 183.06 86.95231 55 1.09803 MF 0.003 231.36 0.007 286.47 12.85429 0.001 237.15 87.42383 56 MSN6 201 0.001 184.17 12.92714 SIGMA1 0.005 257.66 87.96821 57 2MS6 2MK6 0.033 257.07 58 341.83 13,39866 8 01 0.001 88.05035 RH01 0.007 351.01 13.47151 0.003 203.91 26.40794 61 2MN2S2 13.94304 42.77 0.005 255.41 26.87018 62 3M(SK)2 0.100 10 01 63 65 0.008 285.59 14.02517 11 MP1 0.011 242.21 26.95231 3M2S2 SNK2 0.001 132.82 14.56955 13 CHI1 0.002 246.68 28.35759 155.46 0.002 14.91786 14 PI1 0.001 334.56 29.91786 66 2SK2 0.037 184.75 14.95893 P1 0.002 0.17 42.38277 68 MQ3 0.015 104.47 15.00000 16 S1 0.003 350.96 43.00928 69 2MP3 44.56955 70 2M03 0.106 190.11 15,04107 17 K1 0.001 334.62 0.004 147.55 56.95231 72 3MS4 15.08214 18 PSI1 0.003 149.13 0.003 247.52 20 72.46026 M5 15.51259 THETA1 0.001 0.003 295.41 15.58544 21 J1 0.001 322.58 85.39204 78 3MNS6 4MS6 0.004 52.05 16.05696 22 S01 0.001 348.85 85.93642 86.48079 80 23 0.001 359.34 16.13910 223.47 82 001 0.001 0.008 270.31 27.34170 24 0.001 23.14 86.87018 83 3MSK6 0Q2 0.011 118.76 27.42383 25 MNS2 0.001 73.01 87.49669 84 4MN6 104.34 187.45 3MSN6 0.033 280.45 27.89535 26 2N2 0.001 88.51258 85 0.034 27 129.61 27.96821 MU2 114.84767 87 2(MN)8 0.001 0.253 305.98 28.43973 28 215.78 115.39204 3MN8 N2 0.001 0.064 310.33 28,51258 29 NU<sub>2</sub> 0.002 257.49 115.93642 89 M8 2MSN8 0.008 339.44 28,90197 30 OP2 0.001 294.46 116.40794 90 31 1.332 332.43 28.98410 M2 326.24 116.95231 91 0.003 0.007 155.89 352.45 29.06624 32 MKS2 0.001 333.58 117.03445 92 3MK8 29.45563 33 LAMDA2 0.001 13.52 117.96821 94 2 (MS)8 0.064 357.65 29.52848 34 L2 2MSK8 118.05035 95 0.001 39.15 0.023 8.12 29.95893 35 T2 0.002 352.47 145.93642 96 4MS10 0.375 16.32 30.00000 36 S2 146.95231 97 3M2S10 0.001 35.35 0.002 36.59 30.04107 37 174.92052 175.93642 R2 0.001 233.41 qq 5MS12 0.108 15.02 30.08214 38 K2 4M2S12 100 0.001 265.58 0.019 234.57 30.54437 MSN2 27.49669 101 MVS2 0.007 93.94 0.002 187.78 30.62651 40 K 12 0.021 120.77 27.88607 102 2MK 2 0.024 258.29 31.01590 41 2SM2 0.009 292.04 28.94304 103 MA2 0.006 26.98 42.92714 42 MO3 29.02517 MA2\* 0.003 13.01 104 0.020 98.95 43.47616 43 30.47152 MSV2 МЗ 0.002 50.31 0.003 120.60 43.94304 44 SO3 0.011 252.24 31.09803 106 SKM2 0.008 194.98 44.02517 45 MK3 2MNS4 0.001 127.20 56.40794 107 0.006 274.38 45.04107 SK3 58.51258 109 3MN4 0.002 165.76 0.003 153.69 57.42383 47 MN4 59.52848 2MSN4 0.001 116.30 0.003 57.96821 305.13 48 Μ4 0.004 188.15 28.39866 111 NA2 0.008 87.96 58.98410 50 MS4

Table 7

### MEAN SEA LEVEL PRINT-OUT

PORT - HOLYHEAD

YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

JANUARY										
3.437 3.340	3.154 3.397 3.289 3.403	3.329 3.150 3.396 3.390	3.359 3.302 3.569 3.417	3.260 3.052	3.497 3.107	3.349 3.204	3.169 3.143	3.341 3.248	3.378 3.211	3.037 2.960
MONTHLY MEAN FEBRUARY	SEA LEVEL	3.258	NO OF DAYS	31						
2,795 2,790	3.240 3.232	3.098 3.031 3.260 3.314 3.106	2.997 3.058 3.212 3.124 NO OF DAYS	3.054 3.135 28	3.121 3.132	3.124 3.044	3.120 2.936	3.187 2.891	3.211	3.270
2.864 3.029 3.220 3.186 3.275	3.213 3.149	3.405 3.320 3.350 3.090	3.170 3.227 3.330 3.312	3.174 3.350	3.069 3.097	3.083 3.204	3.153 3.394	3.169 3.343	3.182 3.170	3.219 3.198
MONTHLY MEAN APRIL		3.212	NO OF DAYS	31						
3.211 3.156 3.210 3.088 MONTHLY MEAN MAY	3.410 3.493	2.957 2.888 3.353 3.382 3.126	2.809 2.812 3.324 3.277 NO OF DAYS	2.811 3.222 30	2.800 3.137	2.932 3.144	3.048 3.154	3.169 3.257	3.298 3.187	3.335 3.199
3.183 3.220 3.237 3.428 3.101	3.323 3.140	3.313 3.306 3.253 3.393	3.290 3.229 3.259 3.222	3.248 3.206	3.398 3.253	3.306 3.209	3.445 3.268	3.336 3.082	3.329 3.018	3.268 3.074
MONTHLY MEAN JUNE		3.254	NO OF DAYS	31						
3.091 3.108 3.192 3.152 MONTHLY MEAN JULY	J. TTO J. T/T	3.131 3.153 3.130 3.147 3.163	3.200 3.259 3.185 3.201 NO OF DAYS	3.380 3.241 30	3.279 3.166	3.140 3.133	3.150 3.154	3.114 3.129	3.058 3.158	3.105 3.183
3.203 3.236 3.235 3.116 3.300	3.009 3.093	3.292 3.261 3.145 3.152	3.205 3.174 3.136 3.130	3.159 3.163	3.136 3.228	3.116 3.270	3.109 3.301	3.115 3.349	3.127 3.290	3.136 3.361
MONTHLY MEAN AUGUST		3.197	NO OF DAYS	31						
3.202	3.101 3.116	3.109 3.213	3.180 3.118 3.218 3.145	3.124 3.130	3.125 3.297	3.109 3.139	3.147 3.173	3.268 3.226	3.347 3.183	3.372 3.157
MONTHLY MEAN SEPTEMBER		3.212	NO OF DAYS	31						
3.219 3.214 3.103 3.038 MONTHLY MEAN OCTOBER	2.930 2.993	3.094 3.124 3.051 3.103 3.153	3.123 3.123 3.141 3.169 NO OF DAYS	3.144 3.185 30	3.171 3.213	3.206 3.270	3.225 3.285	3.287 3.240	3.244 3.165	3.163 3.170
3.201 3.126 3.084 3.167 3.273	3.300 3.404	3.414 3.443	3.165 3.197 3.521 3.357	3.333 3.662	3.310 3.506	3.220 3.273	3.262 3.470	3.296 3.407	3.265 3.338	3.134 3.429
MONTHLY MEAN NOVEMBER		3.295	NO OF DAYS	31						
3.139 3.120 3.518 3.392 MONTHLY MEAN DECEMBER	2.447 2.303	3.197 3.130 3.324 3.387 3.342	3.359 3.324 3.657 3.312 NO OF DAYS	3.652 3.416 30	3.584 3.548	3.371 3.315	3.418 3.163	3.564 3.179	3.521 3.125	3.433 3.143
3.233 3.253 3.323 3.394 3.358	3.400 3.202	3.448 3.329 3.143 3.081	3.557 3.494 2.990 3.042	3.319 3.165	3.444 3.186	3.494 3.214	3.505 3.169	3.491 3.300	3.371 3.390	3.587 3.543
MONTHLY MEAN		3.339	NO OF DAYS	31						
ANNUAL MEAN S	SEA LEVEL	3.221	NO OF DAYS	365						

### EXTREME HOURLY ELEVATIONS PRINT-OUT

PORT - HOLYHEAD YEAR - 86 UNITS - M

DATUM = DATUM OF DATA

MONTH I	MI HEIGHT	NIMA DAY	HR.	I Į	M/ HEIGHT	AXIMA DAY	HR.
JANUARY Î FEBRUARY I MARCH I APRIL I MAY I JUNE I JULY I AUGUST I SEPTEMBER I OCTOBER I NOVEMBER I DECEMBER I	0.442 0.219 0.413 0.265 0.503 0.632 0.442 0.461 0.292 0.428 0.297	12 27 29 25 25 23 24 21 18 5	18 18 6 17 17 5 6 5 4 5 4		6.141 5.791 6.227 5.912 5.906 5.770 5.789 5.710 5.915 5.798 6.051	10 11 27 24 25 23 25 21 19 18 2	10 12 11 10 11 23 23 23 23 23 21
ANNUAL I	0.219	27	18	I	6.227	27	11

#### DATUM = ORDNANCE DATUM (NEWLYN)

MONTH	I I	MI HEIGHT	NIMA DAY	HR.	I I	MA HEIGHT	AXIMA DAY	HR.
JANUARY FEBRUARY MARCH APRIL MAY JUNE JULY AUGUST SEPTEMBER OCTOBER NOVEMBER DECEMBER		-2.608 -2.831 -2.637 -2.785 -2.547 -2.418 -2.608 -2.758 -2.758 -2.758 -2.622 -2.753 -2.598	12 27 29 25 25 23 24 21 18 5 4	18 18 6 17 17 5 6 5 4 5 4		3.091 2.741 3.177 2.862 2.856 2.720 2.739 2.881 2.660 2.865 2.748 3.001	10 11 27 24 25 23 25 21 19 18 2	10 12 11 10 11 23 23 23 23 22 11
ANNUAL :	I	-2.831	27	18	I	3.177	27	11

PORT TITLE : WALES - HOLYHEAD

IOS ATT IHB COUNTRY SEA PORT NO PORT NO SHEET NO CODE CODE LATITUDE LONGITUDE

478 74 19 53 18' 27.1" N 4 37' 48.0" W

DATA
LENGTH TYP D M YEAR CONSTANTS UNIT TIME TIME ZONE STEP SOURCE RECORD (DAYS) NDC OTH SWC

2918 0 01 01 1964 107 0 0 GMT 3.0 IOS 20

ADMIRALTY CHART DATUM (ACD) TIDE GAUGE OBSERVATION SO ZERO (TGZ) DATUM (OBD) (TO OBD)

ODN - 6.831 m ACD - 3.783 m TGBM - 11.573 m 6.990 m TGZ + 0.000 m ODN - 3.05 m

CONSTANTS : FROM ANALYSIS OF DATA 1964-71 ZO : AVERAGE OF M.S.L. 1961-71 TGBM : O.S.B.M. (BOLT) SH 24798221 SITED AT S.W. ANGLE OF ATR HUT

	*** CONS	TITUENTS **	k*			*** CO	nstituents *	**	•
Н	G	sig	NO	NAME	н	G	sig	NO	NAME
0.069	230.61	0.04107	1	SA	0.02	264.07	87.96821	57	2MS6
0.011	121.90	0.08214	2	SSA	0.00	263.72	88.05035	58	2MK6
0.027	238.77	0.54437	3	MM	0.00	322.42	88.98410	59	2SM6
0.030	211.23	1.01590	4	MSF	0.00	2 292.64	89.06624	60	MSK6
0.024	205.11	1.09803	5	MF	0.00	183.07	26.40794	61	2MN2S2
0.006	279.43	12.85429	6	2Q1	0.00	3 234.94	26.87018	62	3M(SK)2
0.001	153.37	12.92714	7	SIGMA1	0.00	218.67	26.95231	63	3M2S2
0.033	334.90	13.39866	8	Q1	0.00		28.35759	65	SNK2
0.007	349.91	13.47151	9	RHO1	0.00		29.91786	66	2SK2
0.098	29.73	13.94304	10	01	0.00		42.38277	68	MQ3
0.010	288.09	14.02517	11	MP1	0.00		43.00928	69	2MP3
0.002	95.45	14.56955	13	CHIL	0.00		44.56955	70	2MQ3
0.002	126.40	14.91786	14	PI1	0.00		56.87018	71	3MK4
0.038	169.68	14.95893	15	P1	0.00		56.95231	72	3MS4
0.013	118.86	15.00000	16	S1	0.00		57.88607	73	2MSK4
0.101	175.26	15.04107	17	K1	0.00		71.91124	74	3MK5
0.006	136.35	15.08214	18	PSI1	0.00		72.46026	75	M5 3MO5
0.002	191.97	15.12321	19	PHI1	0.00		73.00928 84.84767	76 77	2 (MN) S6
0.002	84.35	15.51259	20	THETA1	0.00		85.39204	78	3MNS6
0.004	275.72	15.58544	21 22	J <u>1</u> SO1	0.00		85.85428	79	4MK6
0.005 0.003	18.25 334.14	16.05696 16.13910	23	001	0.00		85.93642	80	4MS6
0.003	240.83	27.34170	24	0Q2	0.00		86.32580	81	2MSNK6
0.000	129.10	27.42383	25	MNS2	0.00		86.48079	82	2MV6
0.048	241.87	27.89535	26	2N2	0.00		86.87018	83	3MSK6
0.038	181.40	27.96821	27	MU2	0.00		87.49669	84	4MN6
0.360	265.90	28.43973	28	N2	0.00		88.51258	85	3MSN6
0.073	274.13	28.51258	29	NU2	0.00		88.59472	86	MKL6
0.008	305.00	28.90197	30	OP2	0.00		115.39204	88	3MN8
1.810	291.88	28.98410	31	M2	0.00	2 31.66	115.93642	89	M8
0.005	195.23	29.06624	32	MKS2	0.00	1 18.22	116.40794	90	2MSN8
0.025	326.79	29.45563	33	LAMDA2	0.00	2 61.67	116.95231	91	3MS8
0.047	312.02	29.52848	34	L2	0.00		117.96821	94	2(MS)8
0.032	320.66	29.95893	35	T2	0.00		118.05035	95	2MSK8
0.596	327.81	30.00000	36	S2	0.00		145.93642	96	4MS10
0.006	3.79	30.04107	37	R2	0.00		146.95231	97	3M2S10
0.172	326.53	30.08214	38	K2 MSN2	0.00		174.37615	98	4MSN12
0.010	209.06	30.54437 30.62651	39 40	KJ2	0.00		174.92052	99 100	5MS12 4M2S12
0.008 0.016	155.14 221.74	31.01590	41	2SM2	0.00 0.00		175.93642 27.49669	101	MVS2
0.018	255.24	42.92714	42	MO3	0.00		27.88607	102	2MK2
0.019	246.05	43.47616	43	M3	0.01		28.94304	103	MA2
0.003	299.26	43.94304	44	803	0.00		29.02517	104	MA2*
0.001	91.34	44.02517	45	MK3	0.00		30.47152	105	MSV2
0.002	47.78	45.04107	46	SK3	0.00		31.09803	106	SKM2
0.015	8.47	57.42383	47	MN4	0.00		56.40794	107	2MNS4
0.034	41.97	57.96821	48	M4	0.00		57.49669	108	MV4
0.001	121.25	58.43973	49	SN4	0.00		58.51258	109	3MN4
0.010	95.26	58.98410	50	MS4	0.00	1 82.99	59.52848	110	2MSN4
0.003	72.25	59.06624	51	MK4	0.00		28.39866	111	NA2
0.001	189.50	60.00000	52	S4	0.00		72.92714	113	MSO5
0.013	197.97	86.40794	54	2MN6	0.00		74.02517	114	MSK5
0.023	225.02	86.95231	55	M6	0.02	6 356.73	29.52848	115	2MN2
0.005	224.12	87.42383	56	MSN6					

Table 10

#### PROUDMAN OCEANOGRAPHIC LABORATORY (BIDSTON OBSERVATORY) HARMONIC TIDAL ANALYSIS.

PORT: BARROW: RAMSDEN DOCK

LATITUDE: 54 06' N LONGITUDE: 3 12' W TIME ZONE: GMT LENGTH: 2 YEARS

FROM: 7TH JANUARY,1985 TO: 11TH FEBRUARY,1987

UNITS: METRES A0: 5.004

FILTERED HOURLY DATA FROM 15 MINUTE OBSERVATIONS RECORDED BY AANDERAA WLR5. DATUM OF OBSERVATIONS = CHART DATUM = 4.75 METRES BELOW ORDNANCE DATUM (NEWLYN) OBSERVATION MEAN = 0.5007D+01 RESIDUAL MEAN = -0.8764D-04 STD = 0.2303D+01 STD = 0.2210D+00

	H	G		SIGMA	**	_
SA SSA MM MSF MF 201 SIGMA1 01	0.051 0.056 0.058 0.028 0.043 0.012	227.67 132.47 226.51 220.10 204.03 266.37	2MN2S2 3M(SK)2 3M2S2 SNK2 MQ3 2MP3 2MQ3	26.40794 26.87018 26.95231 28.35759 42.38277 43.00928 44.56955	H 0.006 0.010 0.017 0.001 0.007 0.002 0.006	G 225.06 227.67 208.43 39.93 242.18 36.31
RHO1 O1 O1 O1 O1 M1 CHI1 P1 S1 S1 FS1 FS1 FS1 FS1 FS1 FS1 FS1 FS1	0.088 0.0066 0.0003 0.0046 0.0003 0.0049 0.0005 0.0019 0.005 0.005833 0.007145 0.005883 0.007145 0.0031 0.0031 0.0015 0.0	346.43 350.902 2887.676.56 287.656.43 184.38 195.478 197.63 325.478 127.63 325.47 341.76 60.83 267.73 341.76 60.83 30.96 308.38 30.96 308.38 30.96 308.38 30.96 308.49 308	3MK4 3MK4 3MK5 M5 3MK5 3MK5 3MO5 2(MN) S6 3MNS6 4MK6 4MS6 2MSNK6 2MSK6 4MN6 MKL6 3MSK6 2(MN) 8 3MS8 3MS8 3MS8 3MS8 3MS8 3MS8 3MS8 3MS	56.87018 56.95231 57.88607 71.91124 72.460928 84.84767 85.85428 85.93642 86.32580 86.487079 86.87018 87.49669 115.93642 116.40794 115.93642 117.03445 117.0345 117.03445 117.03445 117.03445 117.03445 117.03445 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.0345 117.035 117.0	0.013 0.0002 0.005 0.001 0.003 0.001 0.0003 0.001 0.0001 0.0	242.18 31.38 97.88 705.71 279.65 115.27 237.65 268.237 424.88 232.447.423 337.424.88 424.88 152.41.267 2246.345 2273.7763 228.277.763 229.623 2273.7763 227.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 222.42 2273.7763 227.7763
MN4 M4 SN4 MS4 MK4 S4 SK4	0.084 0.211 0.019 0.128 0.039 0.020 0.012	218.14 247.36 267.83 294.95 290.81 328.47 325.02				
2MN6 M6 MSN6 2MS6 2MK6 2SM6 MSK6	0.016 0.026 0.011 0.025 0.008 0.009 0.006	35.68 56.10 81.92 98.21 91.03 149.34 136.34				

Table 11

PROUDMAN OCEANOGRAPHIC LABORATORY (BIDSTON OBSERVATORY) HARMONIC TIDAL ANALYSIS.

PORT: LOWSY POINT

LATITUDE: 54 09.5' N

LONGITUDE: 3 14.5' W

TIME ZONE: GMT

LENGTH: 15 MONTHS

FROM: 14TH SEPTEMBER,1985 TO: 7TH FEBRUARY,1987

UNITS: METRES A0: 2.809

15 MINUTE OBSERVATIONS RECORDED BY AANDERAA WLR5.

DATUM OF OBSERVATIONS = TIDE GAUGE ZERO = 8.54 METRES BELOW LOCAL BM

OBSERVATION MEAN = 0.3648D+01 STD = 0.1506D+01

N.B. DRIES OUT AT LOW WATER. DATA HAS BEEN CLIPPED FOR ANALYSIS.

	и.в.	DKIES	OUT AT	LLOW	WATER.	DATA	HAS	BEEN	CLIF	PED	FOR	ANALYS	SI:
		H	G					SIGM	A	H		G	
SAA MM MSF 1010 MM		0.071 0.076 0.090 0.140 0.019 0.008 0.040 0.008 0.011 0.012 0.006 0.033 0.011 0.005 0.011 0.005 0.011 0.005 0.011 0.005 0.011 0.005 0.011 0.005 0.003 0.011 0.014 0.005 0.014 0.014 0.014 0.014 0.015 0.014 0.014 0.015 0.014 0.014 0.015 0.014 0.015 0.014 0.015 0.014 0.015 0.016 0.017	235.016.607.86.07.07.86.07.07.07.07.07.07.07.07.07.07.07.07.07.	59563652242460284470544950432984749130577	M.			28.943 29.02		0.00		251.97 39.78	,
MN4 M4 SN4 MS4 MK4 SK4 SK4		0.149 0.453 0.042 0.266 0.098 0.035 0.021	233.28 261.70 183.33 301.83 292.33 321.93 296.74	) L 7									
2MN6 M6 MSN6 2MS6 2MK6 2SM6 MSK6		0.049 0.111 0.027 0.084 0.034 0.023 0.015	70.81 92.36 11.09 128.56 118.85 145.11 104.67										

### PROUDMAN OCEANOGRAPHIC LABORATORY (BIDSTON OBSERVATORY) HARMONIC TIDAL ANALYSIS.

PORT: ROA ISLAND
LATITUDE: 54 04' N
LONGITUDE: 3 10' W
TIME ZONE: GMT
LENGTH: 11.5 MONTHS

FROM: 16TH SEPTEMBER, 1985 TO: 12TH FEBRUARY, 1987

UNITS: METRES A0: 4.623

FILTERED HOURLY DATA FROM 15 MINUTE OBSERVATIONS RECORDED BY AANDERAA WLR5. DATUM OF OBSERVATIONS = CHART DATUM = 4.373 METRES BELOW ORDNANCE DATUM (NEWLYN)

OBSERVATION MEAN = 0.4623D+01 RESIDUAL MEAN = 0.4276D-06 STD = 0.2298D+01 STD = 0.2432D+00

	Н	G		SIGMA	Н	G	
SA SSA MMSF MFF 2016 M101 01 MP1 CHI1 PHI1 PHI1 THE T THET THET THET THET THET THET NO12 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO22 NO33	0.060 0.117 0.039 0.050 0.0218 0.0250 0.0046 0.0020 0.00115 0.00110 0.	158.33 150.55 219.134 2001.39 2401.14 358.73 328.45 309.80 1502.21 291.36 102.291.36 102.291.36 206.20 207.80 207.80 208.65 209.28 206.70 207.80 208.65 208.65 305.73 305.73 306.24 305.73 306.24 307.80 307.	2MN2S2 3M(SK)2 3M(SK)2 3M(SS2) SMK2 2SK2 MO3 2MP3 2MP3 2MS4 2MSK4 2MSK4 2MSK6 4MK6 3MNS6 4MK6 2MNS6 4MN6 3MSK6 4MN6 3MSK6 2MN8 8MS N8 3MS8 3MS8 8MS N8 3MS8 2MSK8 4MS10 3MSK8 4MS10 3MS2 MSV2 SKMS10 MSV2 MSV2 MSV2 MSV2 MSV2 MSV3 MSV3 MSV3 MSV3 MSV3 MSV3 MSV8 MSV8 MSV8 MSV8 MSV8 MSV8 MSV8 MSV8	26. 40794 26. 87018 26. 87018 28. 357759 29. 91786 42. 38277 43. 00928 44. 56955 56. 87018 85. 39204 85. 39204 85. 39204 85. 393642 86. 32580 86. 48079 88. 51258 88. 51258 88. 59472 114. 84769 115. 93642 116. 40794 117. 50597 117. 50597 117. 50597 117. 96821 117. 03445 117. 50597 117. 96821 127. 49669 28. 94304 29. 47152 31. 09803 57. 49669 28. 95231 27. 49669 28. 94304 29. 292714 74. 02517	0.006 0.009 0.013 0.008 0.002 0.005 0.006 0.001 0.003	224.38 225.85 230.34 347.57 241.01 27.83 53.91 324.43 74.43 250.64 26.29 185.47 27.77 163.29 173.29 123.86 173.29 123.86 173.29 123.86 173.29 124.43 26.29 185.45 27.77 163.97 125.86 173.29 121.86 123.89 124.89 125.89 126.89 127.06 185.49 185.4	
MN4 M4 SN4 MS4 MK4 S4 SK4	0.081 0.214 0.019 0.132 0.039 0.018 0.010	215.82 244.08 274.46 291.87 286.30 327.89 320.59					
2MN6 M6 MSN6 2MS6 2MK6 2SM6 MSK6	0.014 0.023 0.009 0.021 0.008 0.006	1.74 24.07 58.96 64.69 66.12 116.58 108.70					

Table 13

PROUDMAN OCEANOGRAPHIC LABORATORY (BIDSTON OBSERVATORY) HARMONIC TIDAL ANALYSIS.

PORT: HAWES POINT LATITUDE: 54 03' N LONGITUDE: 3 10' W TIME ZONE: GMT LENGTH: 11 MONTHS

FROM: 20TH OCTOBER, 1985 TO: 30TH APRIL, 1987

UNITS: METRES A0: 2.465

15 MINUTE OBSERVATIONS RECORDED BY AANDERAA WLR5.

DATUM OF OBSERVATIONS = TGZ = 2.81 METRES BELOW ORDNANCE DATUM (NEWLYN)

OBSERVATION MEAN = 0.3359D+01 STD = 0.1742D+01

N.B. DRIES OUT AT LOW WATER. DATA HAS BEEN CLIPPED FOR ANALYSIS.

	N.B.	DRIES	OUT	AT	LOW	WATER	. DATA	HAS	BEEN	CLIP	PED FOR	ANALYSIS
		H		G					SIGM	A.	H	G
SASA MMSF 166 MMSF 10101 MMMCHI1 SK1SIIIE SK1SIII	L L FA1	0.070 0.070 0.080 0.041 0.041 0.041 0.003 0.040 0.	1848-0001-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1	.38 .56 .56 .44 .64			MA2 MB2		28.94, 29.02		0.048	237.36 34.42
MN4 M4 SN4 MS4 MK4 S4 SK4		0.076 0.238 0.022 0.152 0.047 0.032 0.010	212 249 113 290 286 298 293	.83 .81 .21 .58								
2MN6 M6 MSN6 2MS6 2MK6 2SM6 MSK6	1	0.009 0.019 0.020 0.025 0.003 0.018 0.009	300 17 282 28 309 63	.21 .94 .17								

### PROUDMAN OCEANOGRAPHIC LABORATORY (BIDSTON OBSERVATORY) HARMONIC TIDAL ANALYSIS.

PORT: HALFWAY SHOALS LATITUDE: 54 01.5' N LONGITUDE: 3 11.5' W

TIME ZONE: GMT LENGTH: 1 YEAR

FROM: 24TH SEPTEMBER,1985 TO: 24TH SEPTEMBER,1986

UNITS: METRES A0: 6.831

FILTERED HOURLY DATA FROM 15 MINUTE OBSERVATIONS RECORDED BY AANDERAA WLR5.

DATUM OF OBSERVATIONS = TIDE GAUGE ZERO

OBSERVATION MEAN = 0.6829D+01 RESIDUAL MEAN = 0.6913D-06 STD = 0.2239D+01 STD = 0.2013D+00

	H	G		SIGMA	H	G
SA SSA MMSF MF 201 RH01 01 MP1 CHI1 PI1 PHI1 THE THE THE THE THE THE THE THE	0.033 0.0532 0.0346 0.00415 0.00410 0.00410 0.00410 0.000	280.90 145.84 2215.760 199.60 199.60 199.60 199.60 199.766 199	2MN2S2 3M(SK)2 3M2S2 SNK2 2SK2 MQ3 2MP3 2MP3 2MP3 3MS4 2MSK4 3MS5 3MO5 3MO5 3MO5 3MO5 3MS6 4MK6 4MS6 2MV6 3MSK6 2MV6 3MSK6 2MV6 3MSK6 2MSK6 4MN6 3MSK6 2MSK6 4MN6 3MSK6 2MSK6 4MN1 8 3MSR 3MSR 3MSR 3MSR 3MSR 3MSR 3MSR 3MSR	26.40794 26.87018 26.95231 28.35759 29.91786 42.38277 43.00928 44.56955 56.87018 56.95231 57.88607 71.91124 72.46026 73.00928 85.39204 85.39204 86.48079 86.87018 87.49669 88.51258 114.84767 115.93642 116.40794 116.95231 117.50597 117.96821 117.50597 117.96821 118.05035 145.93642 146.95231 27.49669 28.49669 28.49669 28.51258 14.84767 117.50597 117.96821 118.05035 145.93642 146.95231 27.49669 28.51258 147.292714 74.02517	0.008 0.008 0.0005 0.0005 0.0005 0.0001 0.000001 0.	222.10 236.15 2174.36 356.93 244.387 70.79 349.482 37.129 236.583 1791.975 1897.828 206.231 1897.828 206.231 1897.828 206.231 1897.828 2058.63 2144.87 2058.63 2057.128 2058.63 2059.63 2059.63 2059.65 2059.65 2059.65 2059.65
MN4 M4 SN4 MS4 MK4 S4 SK4	0.073 0.188 0.013 0.110 0.033 0.012 0.008	200.44 229.22 260.16 275.61 270.74 312.08 318.62				
2MN6 M6 MSN6 2MS6 2MK6 2SM6 MSK6	0.009 0.015 0.004 0.015 0.004 0.004	345.00 9.12 22.17 43.95 48.73 74.03 81.19				

	Ramsden	Roa Is.	Halfway S.	P Patrick	Holyhead
Heysham	0.879	0.851	0.848	0.849	0.774
Ramsden Dock		0.856	0.946	0.904	0.882
Roa Is.			0.951	0.879	0.879
Halfway S.				0.852	0.842
P. Patrick		•			0.852

Table 16: Cross-correlation of observed surges of May-June 1987

	P cm(mb)-1	coefficients of $cm(ms^{\frac{u}{1}})^{-1}$	v cm(ms <sup>-1</sup> ) <sup>-1</sup>
Jan-Feb 1985	-0.54(0.11)	0.99(0.22)	3.69(0.35)
Mar-Apr "	-0.82(0.11)	0.66(0.26)	3.28(0.32)
May-Jun "	-0.99(0.12)	0.31(0.17)	2.56(0.23)
Jul-Aug "	-0.69(0.12)	0.25(0.19)	2.81(0.24)
Sep-Oct "	-0.95(0.11)	0.36(0.26)	1.63(0.38)*
Nov-Dec "	-1.11(0.14)	0.08(0.28)*	3.44(0.37)
average	-0.83	0.52	2.89

<sup>\*</sup> These values are not included in average.

Table 17: Regression Coefficient of P, u and v (Squires Gate) for all surges at Ramsden Dock.

	Α		В		С	
	Mean (cm)	Variance (cm²)	Mean (cm)	Variance (cm²)	Mean (cm)	Variance (cm²)
Oct 1985	-5.9	473.9	-0.5	110.1	-1.7	111.4
Nov 1985	-13.4	597.4	-13.0	105.1	-10.5	142.9
Dec 1985	5.7	509.5	-6.6	137.4	<b>-</b> 5.9	196.2
Oct-Dec 1985	-4.3	595.8	<b>-</b> 6.9	143.8	-6.2	163.9

Table 18: Means and variances of observed surges and unpredicted component.

A observed surge; B unpredicted when NM is used; C unpredicted when RM is used.

Ramsden Dock

average

Halfway Shoals

2-9 Jan 1985

29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr

4-11 Apr

19-26 Aug

average

23-30 Jan

Period	cm mb-1	$cm(ms^{-1})$	$cm(ms^{-1})$
2-9 Jan 1985 23-30 Jan 29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr 19-26 Aug	-1.07(0.25) -0.83(0.19) -0.72(0.32) -0.20(0.39)* -0.14(0.78)* -0.67(0.47)	1.66(0.87) 0.52(0.49) 1.83(1.06) 1.18(0.90) 1.11(0.23) 0.75(0.65)	5.15(0.88) 3.61(0.60) 5.16(1.44) 4.44(1.03) 2.28(1.29) 4.81(1.32)
average	-0.82	1.22	4.24
Roa Island			
2-9 Jan 1985 23-30 Jan 29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr	-1.10(0.25) -0.77(0.19) -0.79(0.31) -0.14(0.37)* -0.16(0.75)*	1.81(0.71) 0.79(0.48) 1.90(1.05) 1.30(0.85) 1.51(0.63)	5.15(0.92) 3.73(0.60) 5.11(1.41) 4.37(1.03) 2.28(1.24)

-0.88

-1.06(0.23)

-0.71(0.18)

-0.35(0.32)\*

-0.18(0.72)**\*** 

-0.68(0.41)

-0.55(0.30) -0.35(0.32)\* -0.18(0.72)\*

-0.75

1.46

1.95(0.65)

1.24(1.00) 1.22(0.7)

1.62(0.60)

0.67(0.61)

-----

1.28

4.10

5.05(0.84)

3.55(0.60)

5.07(1.36)

4.44(0.89)

2.20(1.18)

4.33(1.22)

4.10

Table 19: Regression coefficient (standard error) of meteorological inputs (P, u and v at Squires Gate) for negative surge output).

<sup>\*</sup> These values, when error is bigger than coefficient, are not included in averages.

Ramsden Dock		Α		В		С
	m	var.	m	var.	m	var.
2-9 Jan 1985 23-30 Jan 29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr 19-26 Aug	-5.1 -4.1 -25.1 -2.1 -29.5	291.5 601.1 466.7 677.6 149.5 268.9	-10.0 -7.3 -3.7 8.1 -0.4 6.7	123.1 159.3 57.2 82.0 44.2 216.3	-9.3 -6.8 -2.9 5.0 3.7 12.1	91.4 140.3 149.1 186.6 101.7 115.4
Roa Island						
2-9 Jan 1985 23-30 Jan 29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr	-3.0 -3.3 -26.9 -0,3 -31.7	297.9 604.0 479.7 664.8 149.3	-7.9 -6.5 -5.5 9.8 -2.6	131.6 146.4 53.9 74.4 41.1	-7.3 -6.0 -4.7 6.8 1.5	98.0 125.4 145.1 180.6 95.4
Halfway Shoals						
2-9 Jan 1985 23-30 Jan 29 Jan-5 Feb 26 Feb-5 Mar 4-11 Apr 19-26 Aug	-3.9 -7.9 -30.0 -6.5 28.1 3.3	272.9 565.6 436.7 764.0 147.3 228.2	08.8 -11.1 -9.0 3.8 0.5 8.2	121.3 124.3 55.5 41.6 527.3 185.2	-7.2 -10.0 -8.6 0.4 2.8 13.3	87.1 111.8 144.1 89.4 85.3 88.6

Average air pressure (1013mb) is subtracted in calculation of surges with the regression formula.

Table 20: Means (cm) and variances (cm $^2$ ) of negative surges. A observed; B unpredicted component when NM is used; and C unpredicted component when RM is used.

Day No	Ramsden Dock	Roa Island	Halfway Shoals
317-330	1.19(0.06)	1.17(0.07)	1.13(0.06)
2-9	0.98(0.11)	0.98(0.12)	0.94(0.11)
29-39	1.09(0.06)	1.09(0.06)	1.06(0.07)
94-101	0.98(0.09)	0.98(0.09)	0.98(0.10)
219-226	0.91(0.12)		0.98(0.11)
	1.03	1.03	1.01

Table 21: Regression coefficients with Heysham model surge as input (for optimisation of surge output).

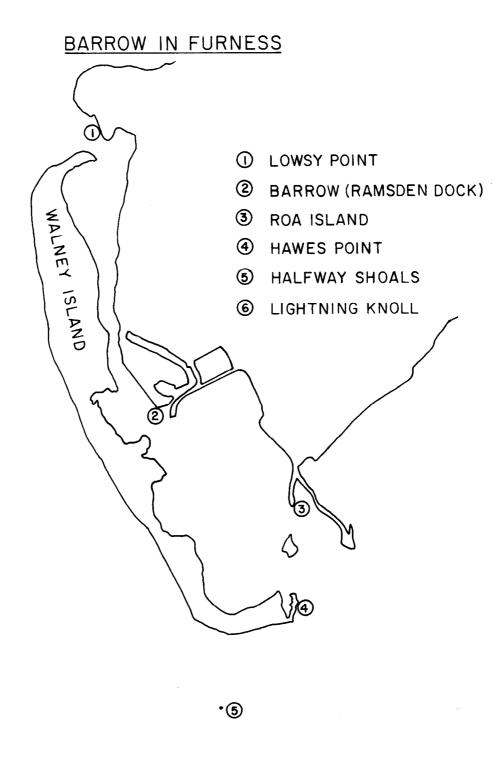
	Model grid point (I,J)	Computed	Observed	Source
Heysham HY	32,23	313.8 cm 325.7°	315.6 cm 325.7°	Amin,1982 8 yrs analysis
Fleetwood FL	28,31	306.7 cm 324.0°	304.8 cm 326.4°	IOS 1 yr analysis
Morecambe MO	34,19	306.2 cm 330.5°	308.0 cm 326.1°	Doodson & Corkan, 1932
Glasson Docks GD	35,26	227.9 cm* 344.0°	338.0 cm 326.1°	Doodson & Corkan, 1932
Wyre Light WL	27,29	305.5 cm 323.8°	310.0 cm 324.0°	Doodson & Corkan, 1932
Barrow, Ramsden Dock	17,18	308.7 cm 331.0°	307.7 cm 330.9°	7/1/85-11/2/87, 2 yrs
Roa Island RI	19,20) 20,20)	305.8 cm 329.1°	305.9 cm 328.6°	16/9/85-12/2/87, 11½ mths
Halfway Shoals HS	18,23	295.6 cm 325.0°	296.5 cm 324.8°	24/9/85-24/9/86, 1 yr
Lowsy Point LP	15,13	207.4 cm* 338.7°	235.9 cm* 335.3°	14/9/85-7/2/87, 15 mths
Hawes Point HP	20,21) 20,22)	303.2 cm 327.9°	291.8 cm* 327.3°	20/10/85-30/4/86, 11 mths

Table 22: Comparison between computed and observed amplitudes and phases of the  $\rm M_{\rm 2}$  tide.

<sup>\*</sup> location subject to drying or ponding

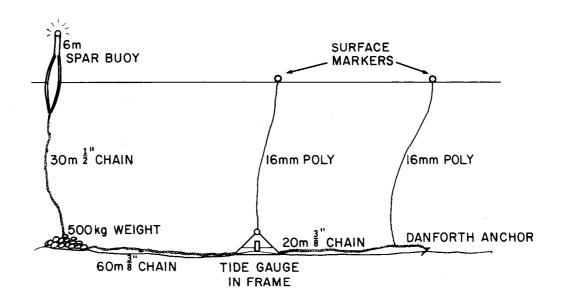
	Observed ATT	2(M <sub>2</sub> +S <sub>2</sub> )	Computed
Ramsden Dock	8.1	8.15	8.18
Roa Island	-	8.09	8.11
Halfway Shoals	-	7.87	7.87
Heysham	8.0	8.34	8.46
Fleetwood	8.2		8.32

Table 23: Comparison of observed and computed estimates of the mean spring tidal range (m) for locations not subject to drying or ponding. Observed values are taken from the Admiralty Tide Tables (ATT) or based on the sum of the amplitudes of the M $_2$  and S $_2$  constituents (2(M $_2$ +S $_2$ )).

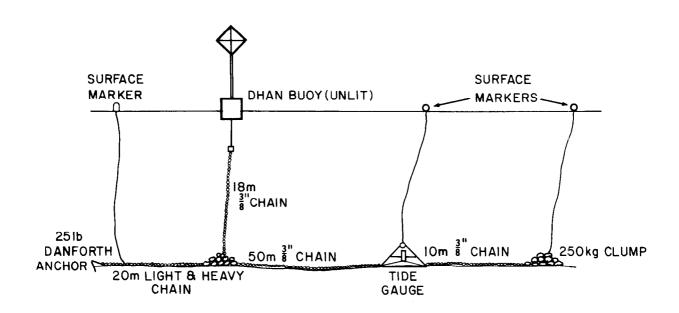


•6

Figure 1: POL installed tide gauge positions



### LIGHTNING KNOLL MOORING



### HALFWAY SHOALS MOORING

Figure 2

## NOTICE TO MARINERS

### WEST COAST - ENGLAND

### BARROW HARBOUR APPROACHES

Notice is hereby given that commencing September 1985 a bottom mounted tide gauge will be sited in the following position which lies near Halfway Buoy:

Latitude 54° OI.5' N approximately Longitude O3° II.9' W

The instrument will be marked by a yellow unlit buoy fitted with a radar reflector and will remain in position until October 1986.

Masters of vessels and small boats are requested to proceed with caution when in the vicinity of this buoy and give it a wide berth.

Institute of Oceanographic Sciences
Bidston, Birkenhead,
Merseyside L43 7RA
U.K. (051 - 653 8633)

# NOTICE TO MARINERS

WALNEY CHANNEL BARROW - IN - FURNESS
CUMBRIA

Commencing mid September 1985, a bottom mounted tide gauge will be deployed in approximate position 54° Ol·5'N, 3° 11·9'W, approximately I cable North by West of the Halfway Shoal Buoy. This instrument will be in position until October 1986, and will be marked by a yellow Dhan buoy, with radar reflector, which will be unlit.

To avoid fouling the mooring the Institute would be grateful if ships and fishing boats keep clear of this Dhan buoy.

Institute of Oceanographic Sciences
Bidston
Merseyside L43 7RA
UK.

(051 - 653 - 8633)

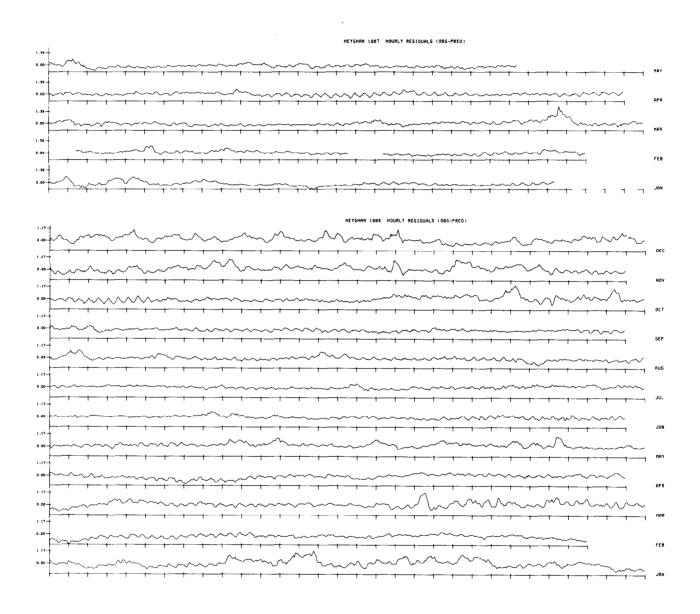


Figure 5: Heysham residuals January 1986 to May 1987

HEYSHAM : SURGE DISTRIBUTION (1964-86) HIGH WATER ±3 HOURS

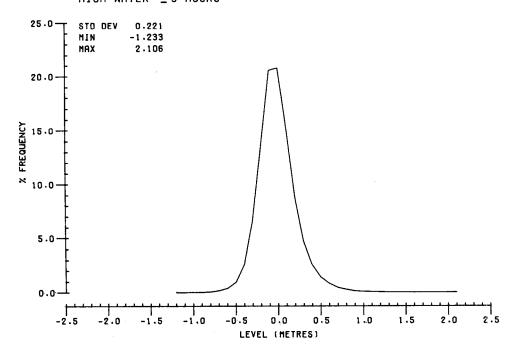


Figure 6

HEYSHAM : SURGE DISTRIBUTION (1964-86)
LOW WATER ±3 HOURS

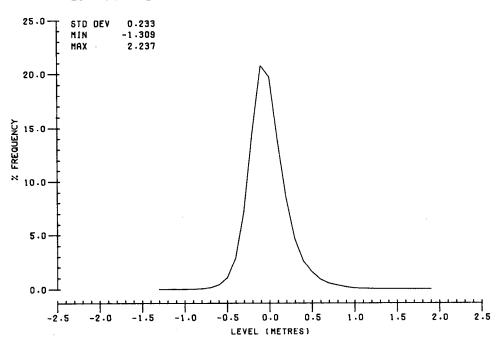


Figure 7

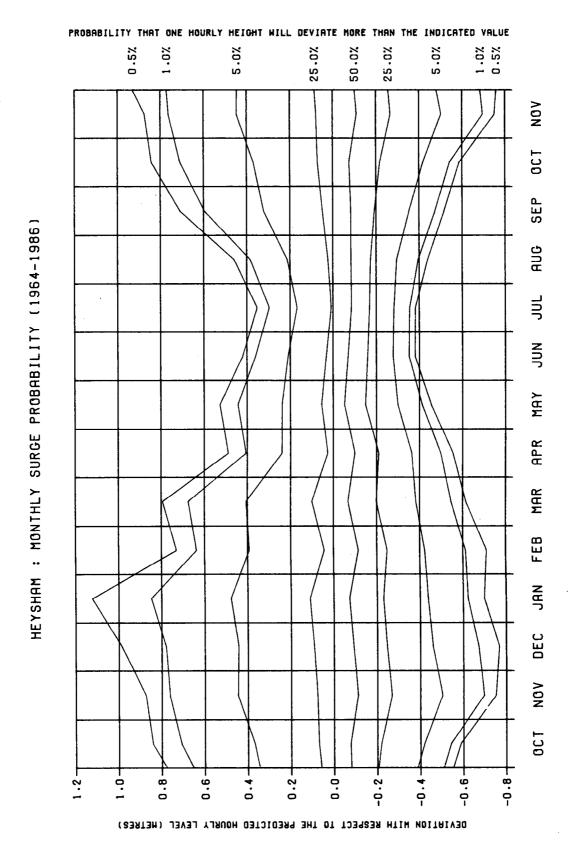


Figure 8

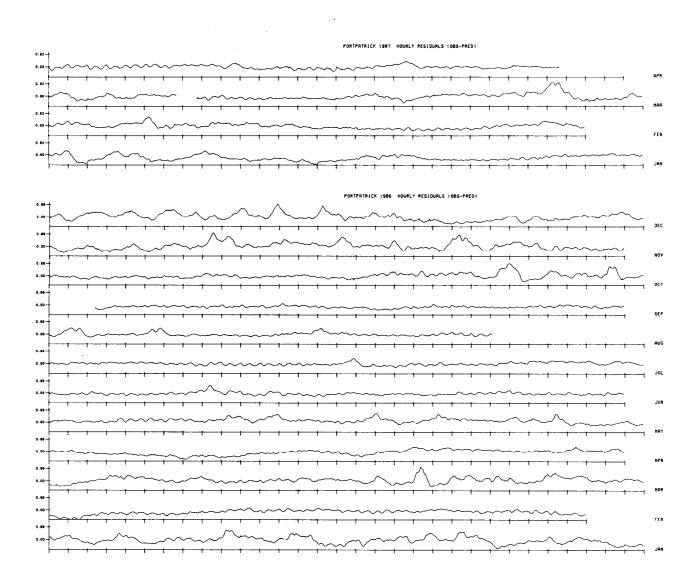


Figure 9: Port Patrick residuals January 1986 to April 1987

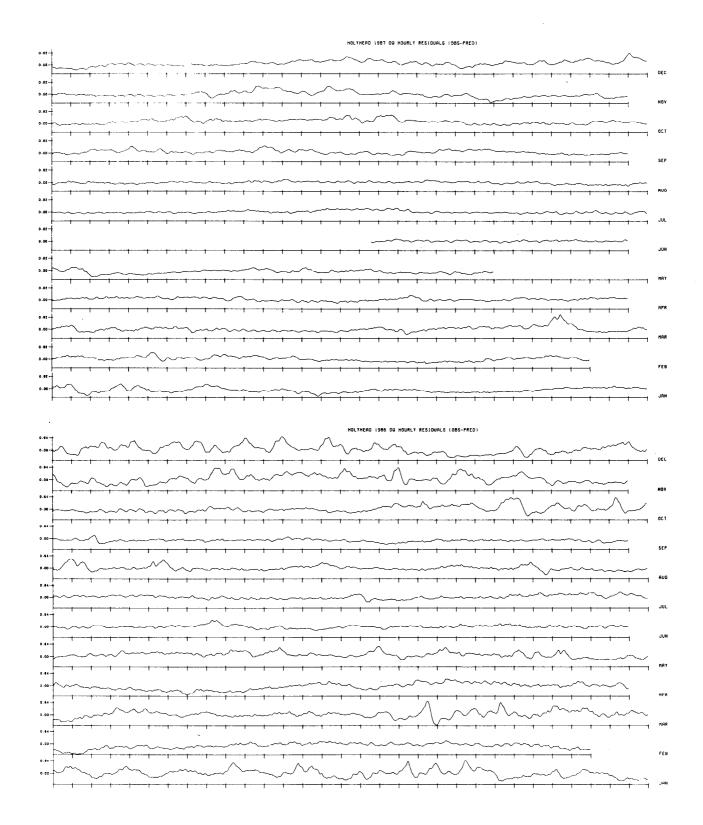


Figure 10: Holyhead residuals January 1986 to December 1987

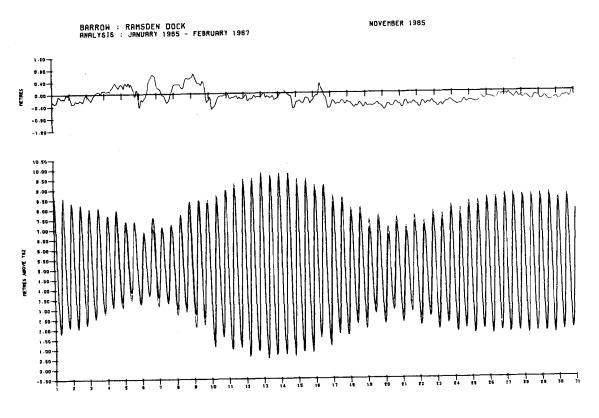


Figure 11

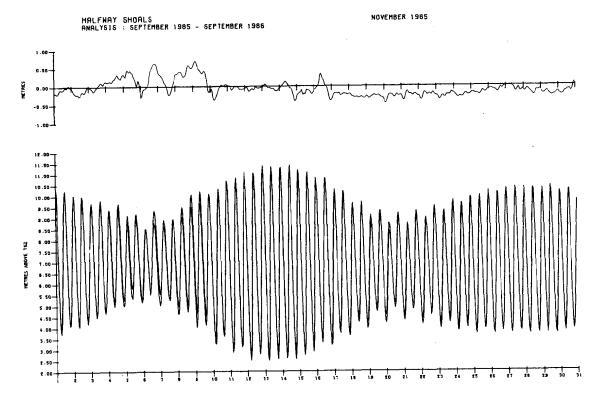
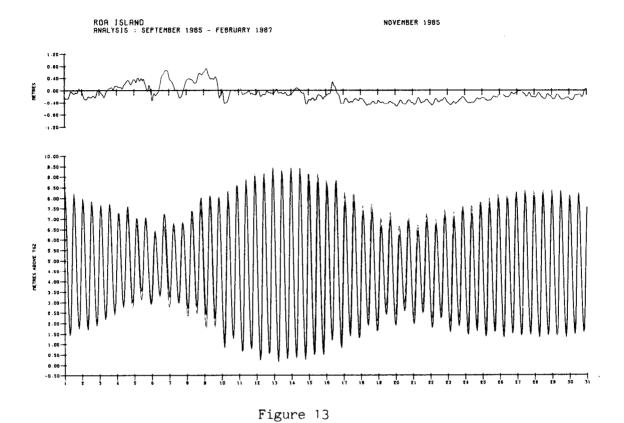
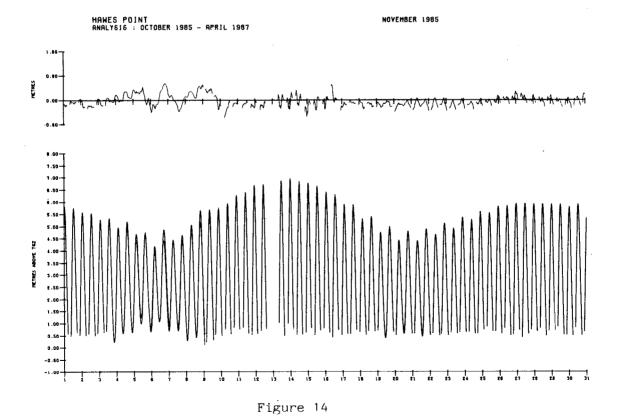


Figure 12





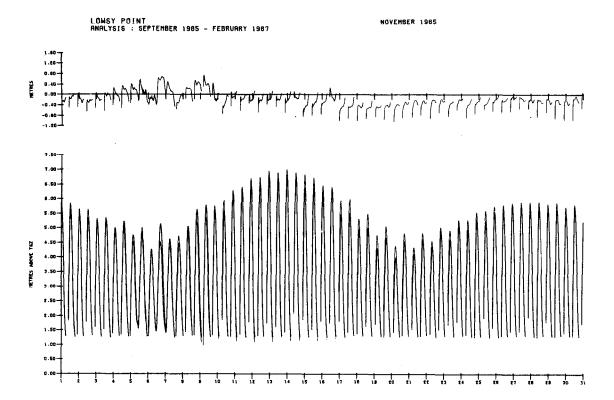


Figure 15

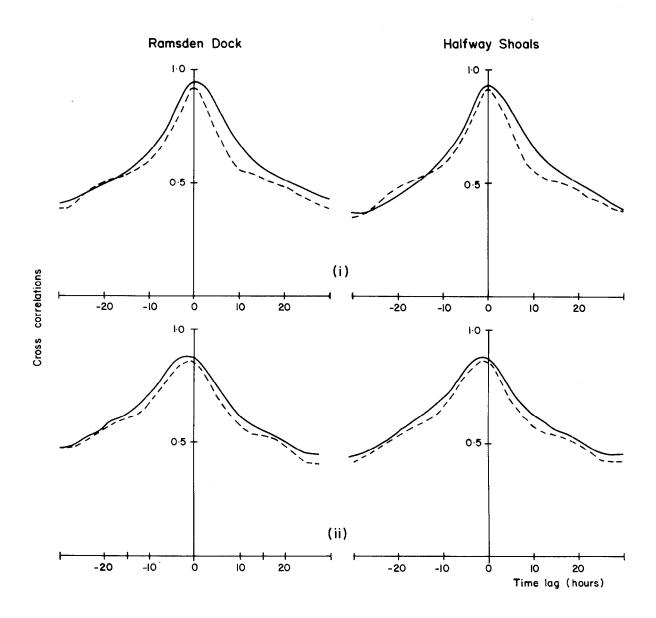


Figure 16a: Cross correlations between observed surges at Ramsden Dock and Halfway Shoals and

<sup>(</sup>i) observed surges at Heysham (----) and Portpatrick (----),

<sup>(</sup>ii) model (numerical) surges at Heysham and Portpatrick.

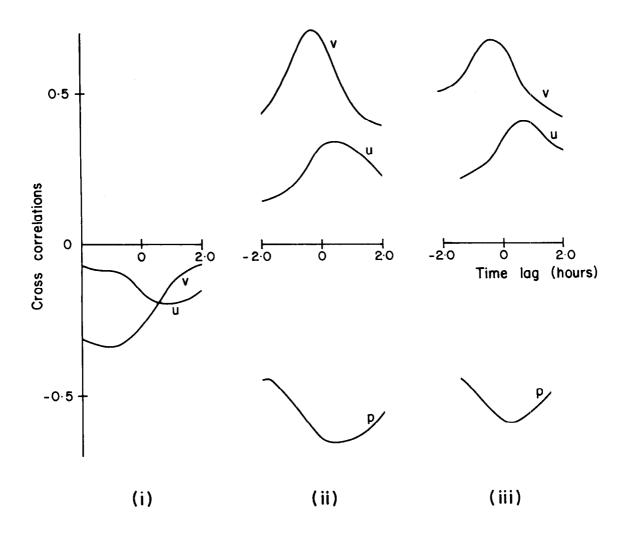


Figure 16b: Cross correlations between surge elevations at Ramsden Dock and air pressure, u-component and v-component of wind at Squires Gate:

- (i) between air pressure and u- and v-component of winds of (Nov-Dec, 1985),
- (ii) surge elevations and air pressure, u- and v-component of (Nov-Dec 1985),
- (iii) between surge elevations and air pressure, u-component and v-component of wind (Nov-Dec, 1986).

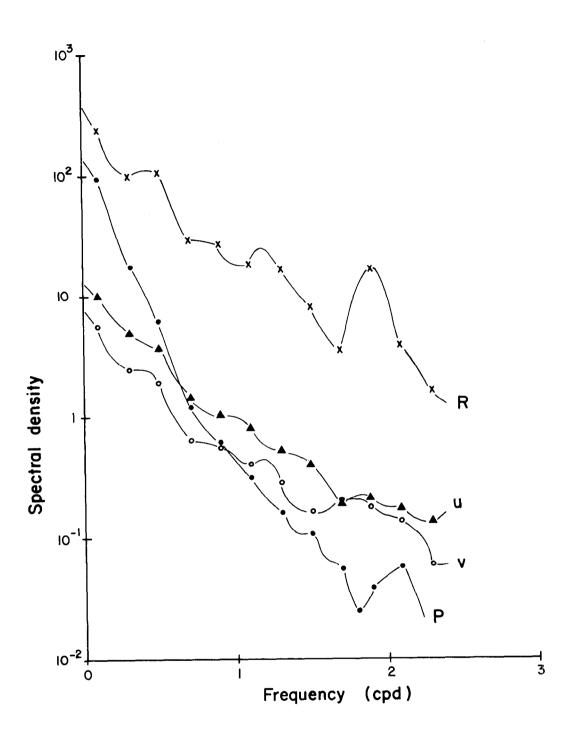


Figure 17: Spectral density of surge elevations at Ramsden Dock, air pressure, u-component and v-component of winds at Squires Cate from 3-hourly values of Oct-Dec 1986. Units are cm²(cpd) for elevations, mb²(cpd) for pressure and (ms 1)²(cpd) for winds.

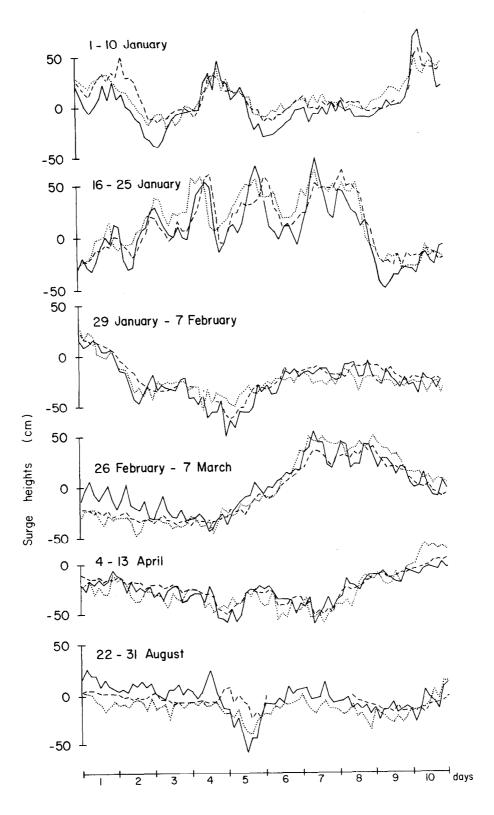


Figure 18: Observed and model surges at Ramsden Dock (3 hourly)

----, numerical model;
...., regression model.

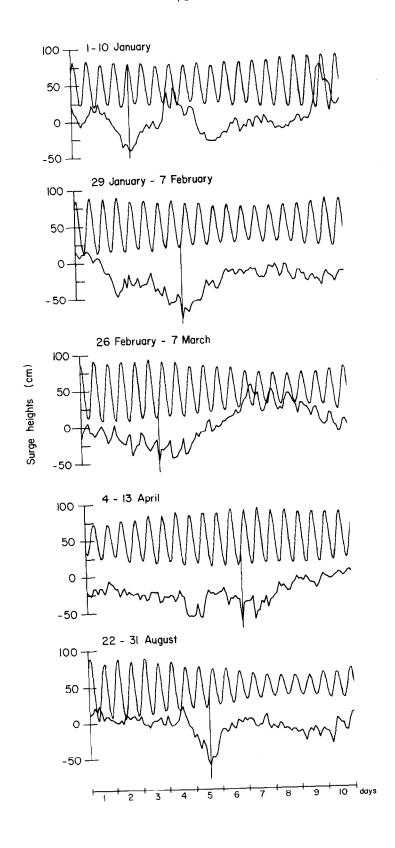


Figure 19: Relationship between the phase of the tide and minima of negative surges (hourly values)

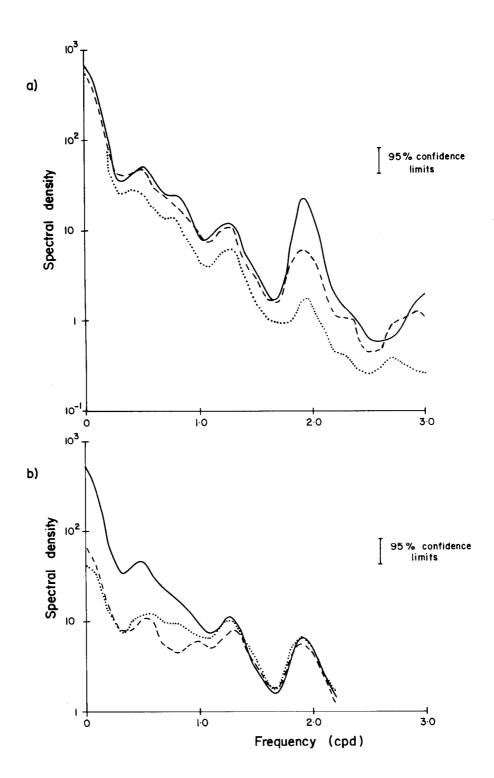


Figure 20: a) Spectral density of surges. Heysham (——), Ramsden Dock observed (----), and Heysham numerical model (....).

b) Spectral density functions. Observed surge elevations (——), unpredicted component of surge elevations when numerical model is used (----), and unpredicted component of surge elevations when regression model is used (....).

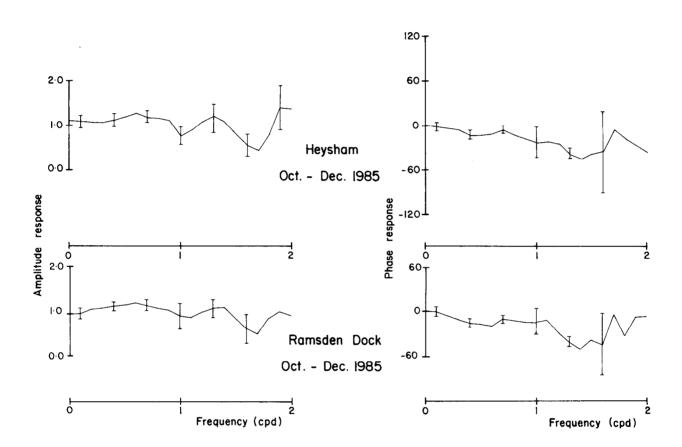


Figure 21: Transfer functions between the numerical model surge at Heysham (input) and observed surges at Heysham and Ramsden Dock (output).

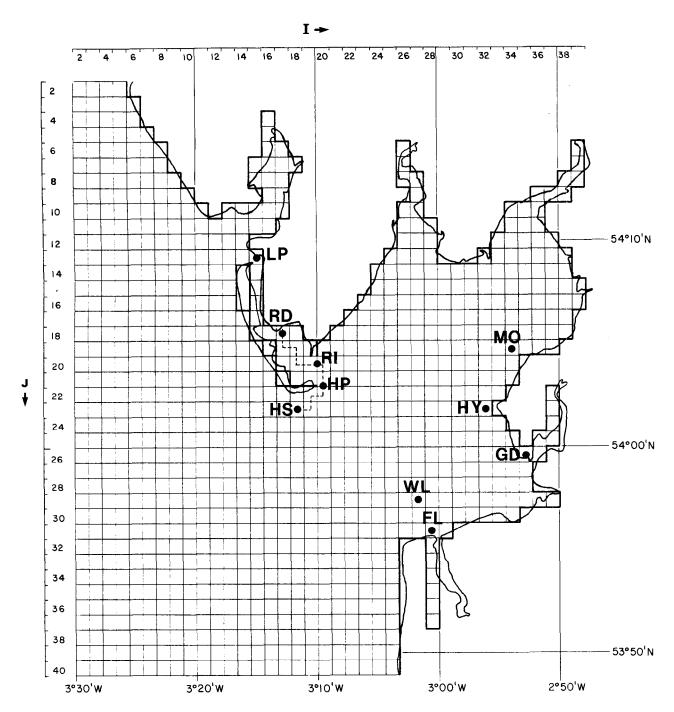


Figure 22: Computational grid for the Morecambe Bay model, with locations of points corresponding to tide gauges referred to in Table 22. The broken line indicates the approximation of the approach channel to Ramsden Dock. Grid points mentioned in the text may be identified by column (I) and row (J) numbers.

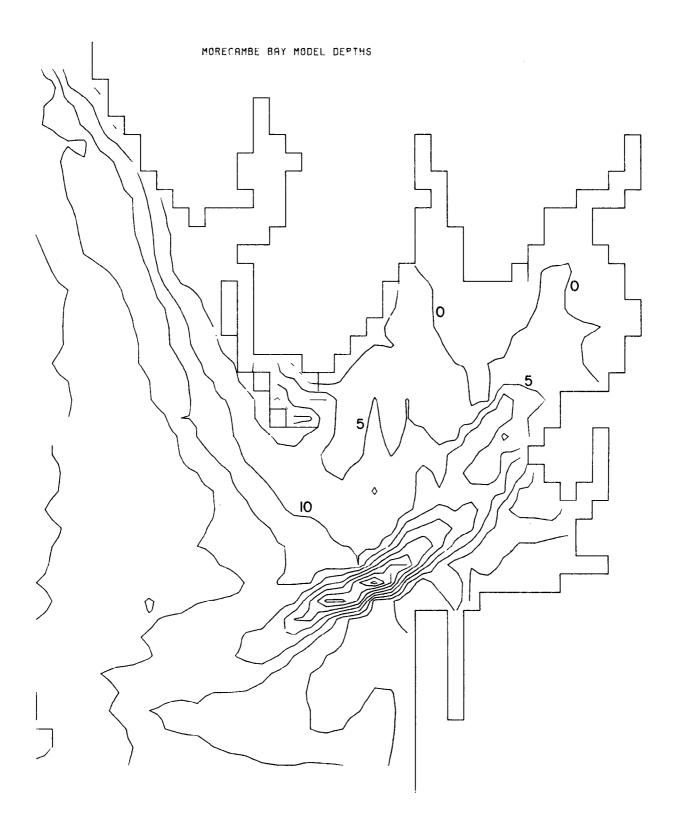


Figure 23: Bathymetry as represented in the Morecambe Bay model.

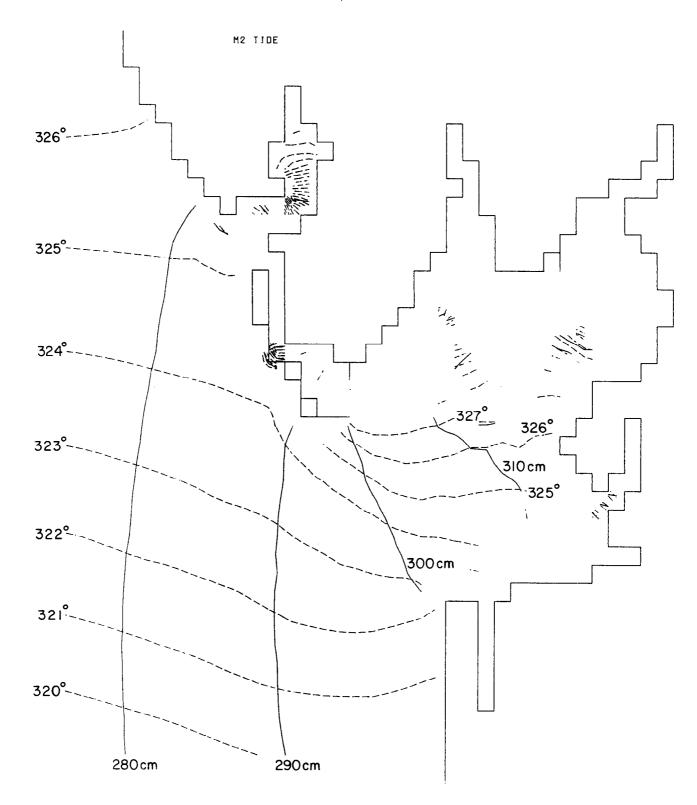


Figure 24: Chart of  $\rm M_2$  tide computed using the Morecambe Bay model, showing contours of amplitude (cm : continuous lines), and phase (degrees : broken lines) for those parts of the Bay not subject to drying.

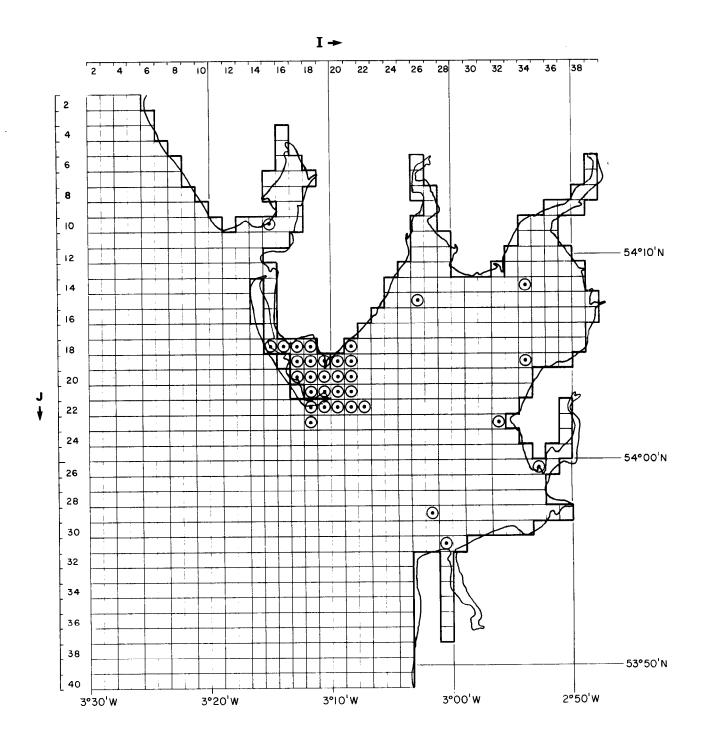


Figure 25: Locations of model grid points for which surge responses are plotted.

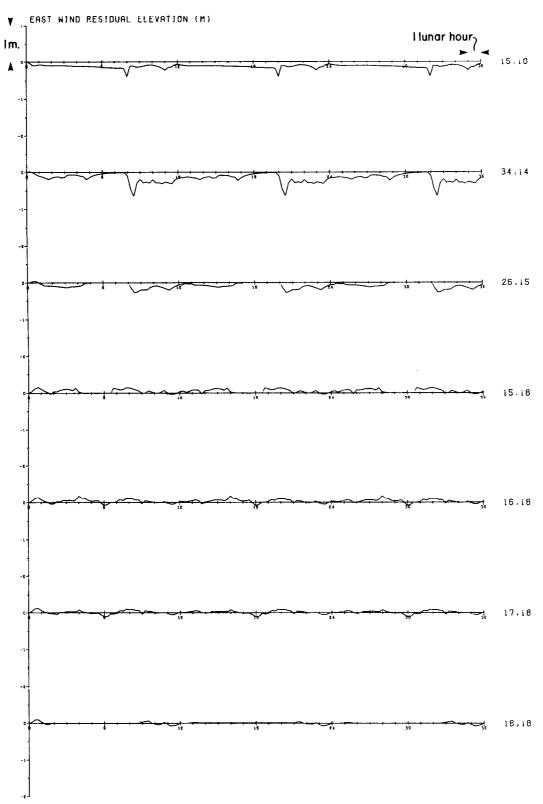


Figure 26: Variation with time of surge residual elevation produced by an easterly wind stress at grid points identified in Fig. 25; sampling is every 1/4 lunar hour over 3 tidal cycles.

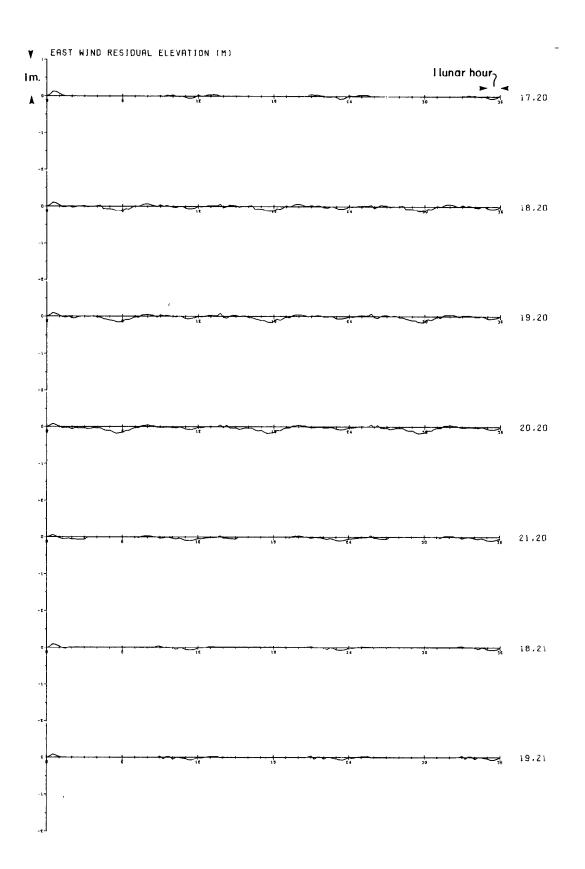


Figure 26: (CONT)

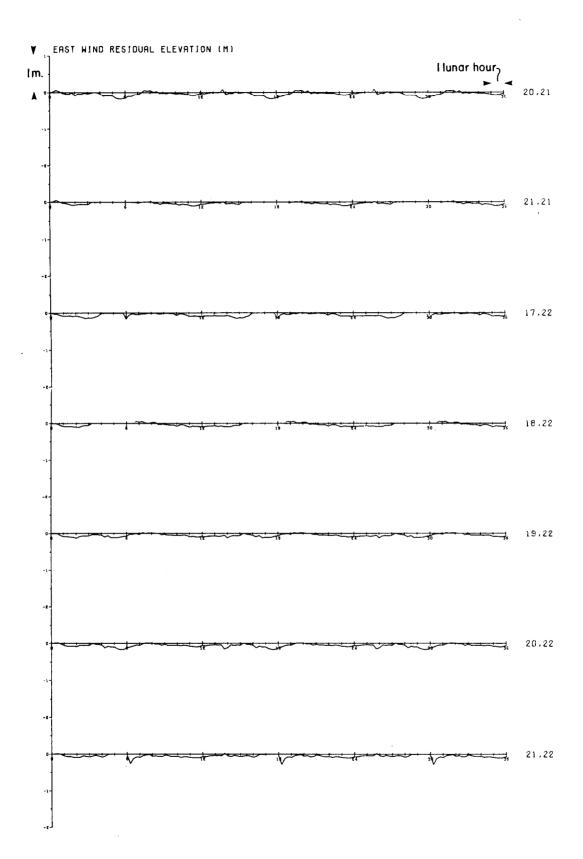


Figure 26: (CONT)

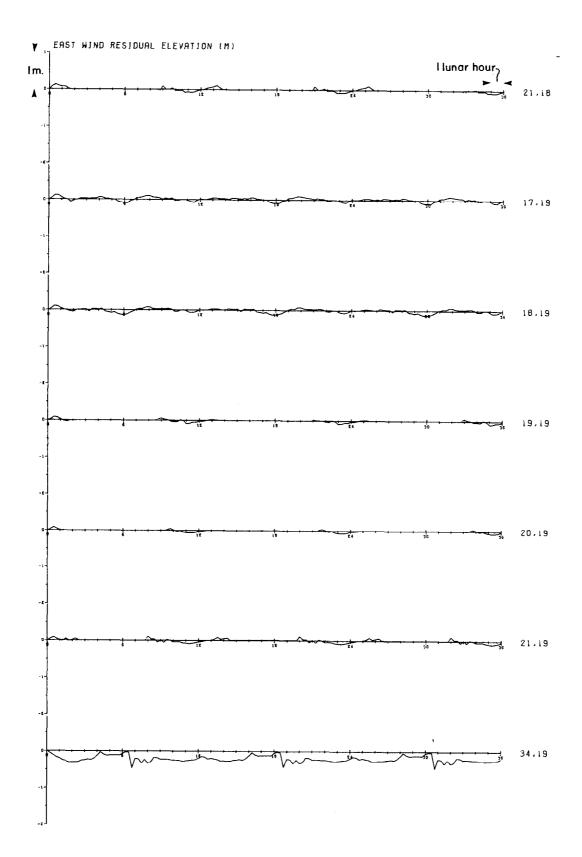


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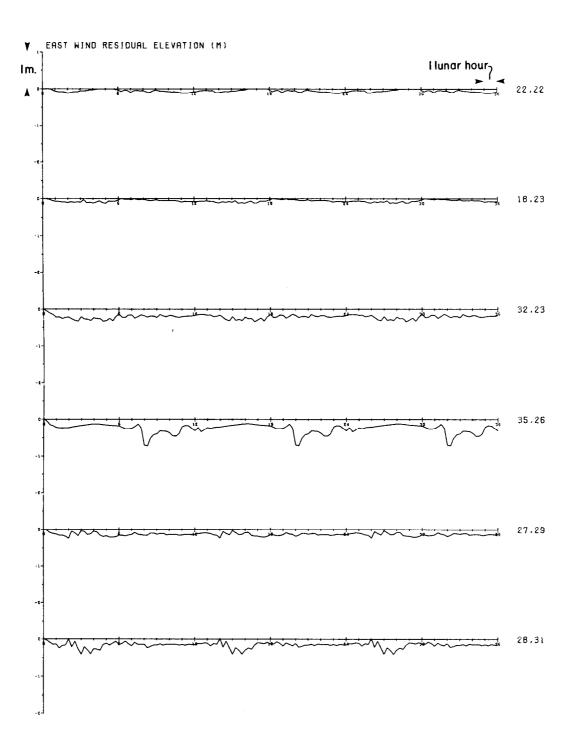


Figure 26: (CONT)

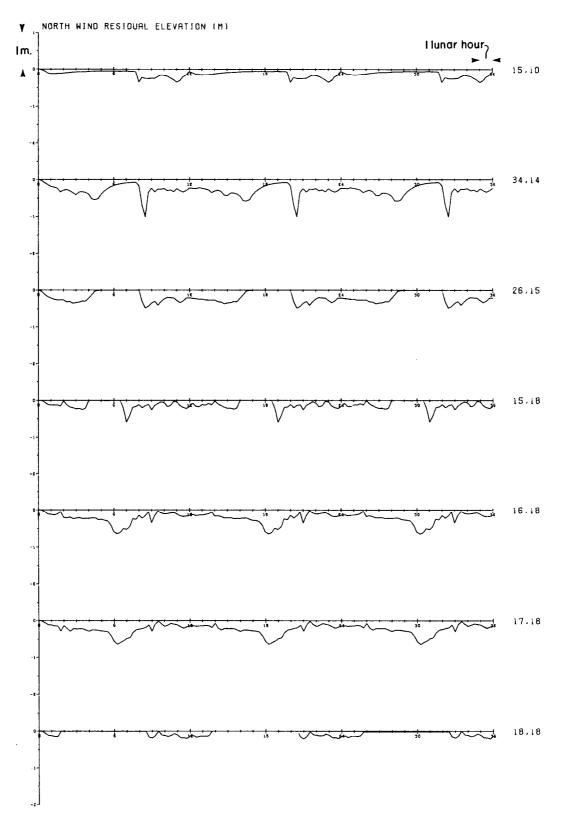


Figure 27: Variation with time of surge residual elevation produced by a northerly wind stress at grid points identified in Fig. 25; sampling is every 1/4 lunar hour over 3 tidal cycles.

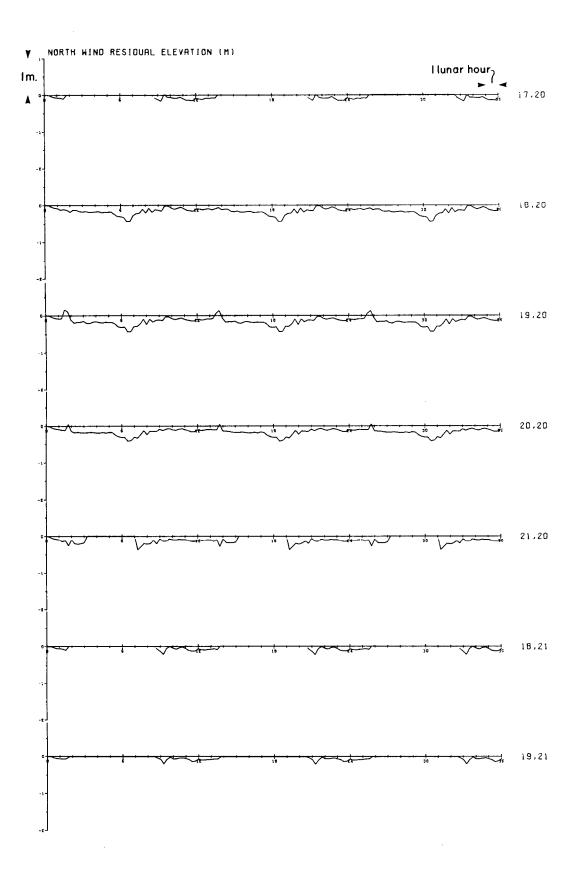


Figure 27: (CONT)

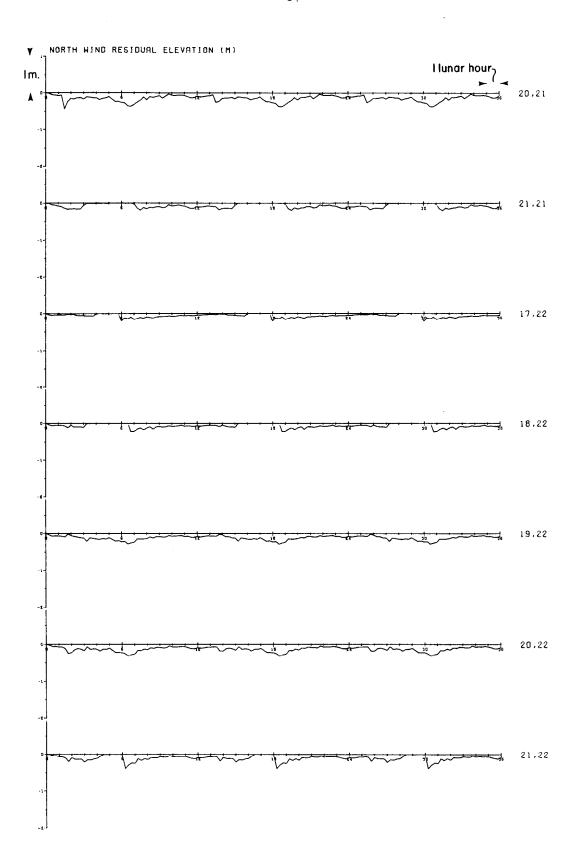


Figure 27: (CONT)

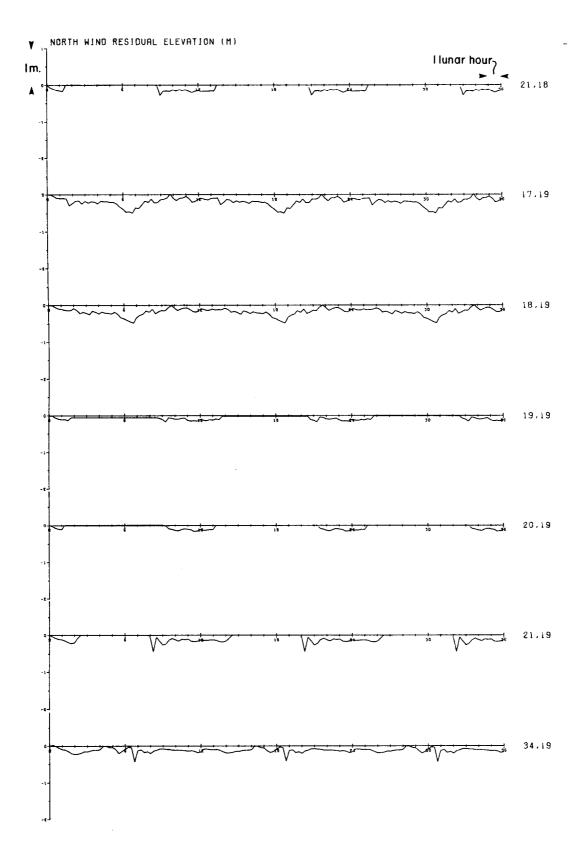


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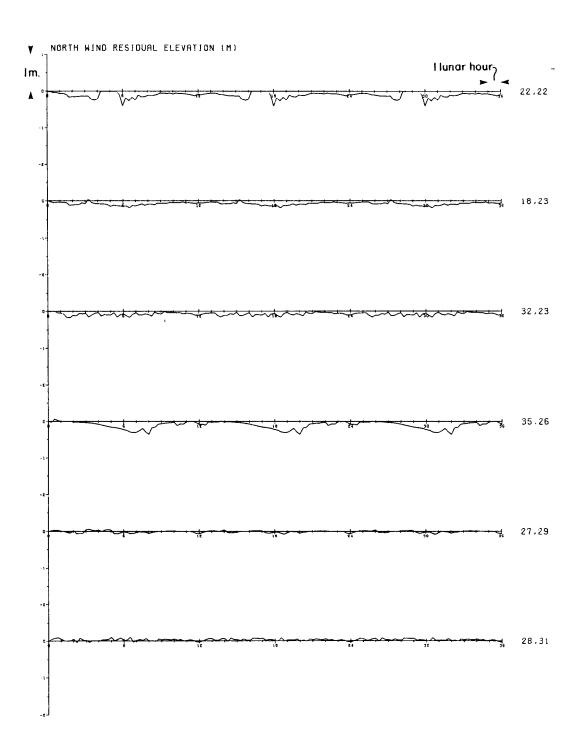


Figure 27: (CONT)

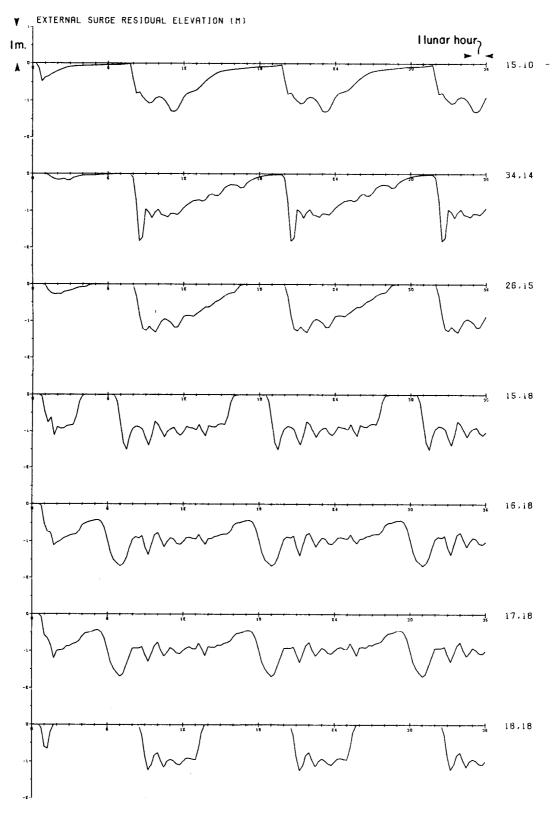


Figure 28: Variation with time of surge residual elevation produced by an external surge of -1m imposed at the model openboundary at grid points identified in Fig. 25; sampling is every 1/4 lunar hour over 3 tidal cycles.

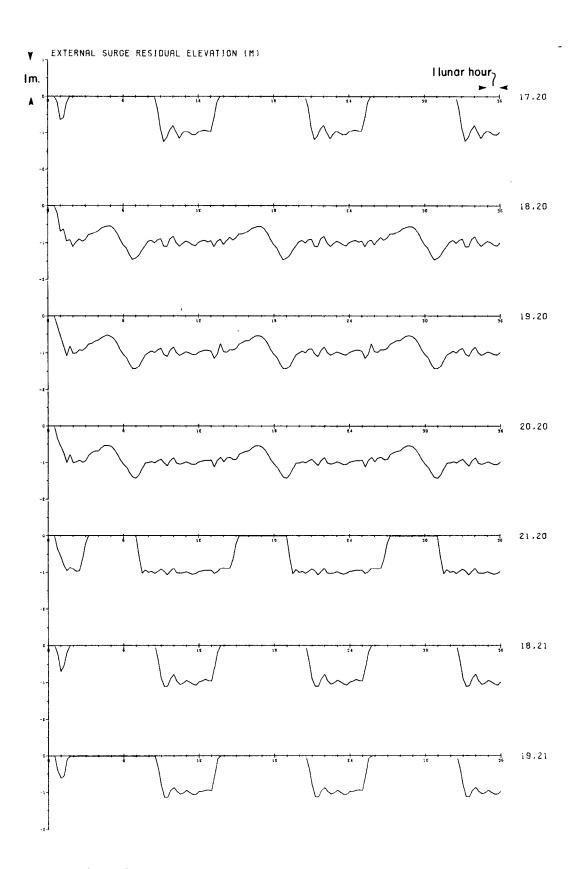


Figure 28: (CONT)

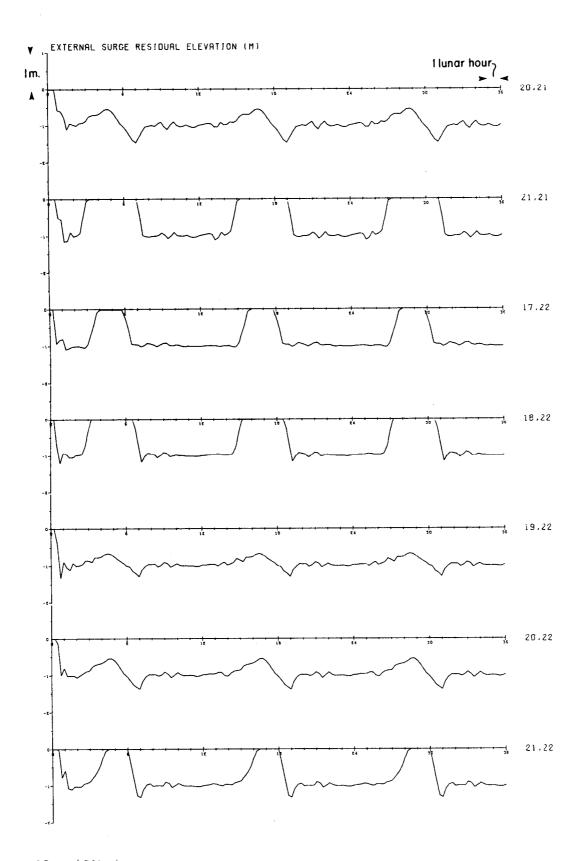


Figure 28: (CCL.)

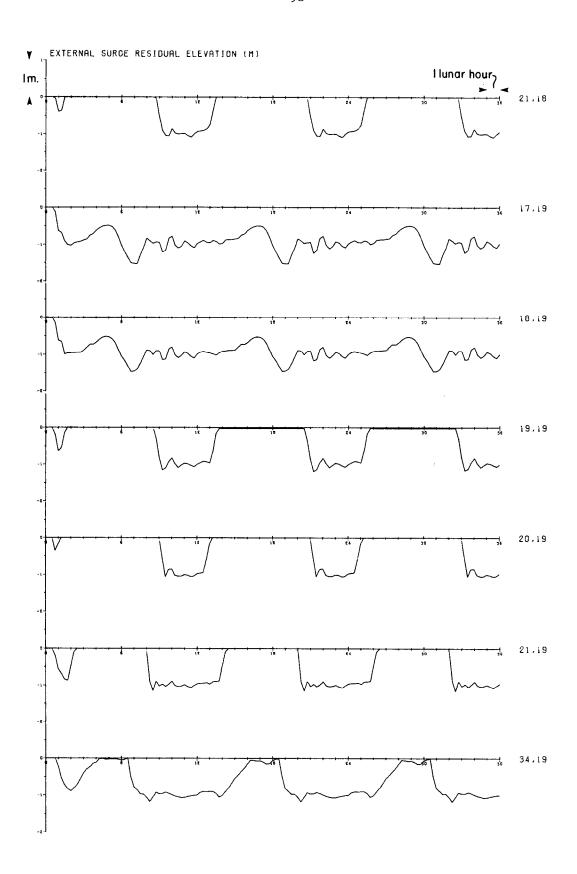


Figure 28: (CONT)

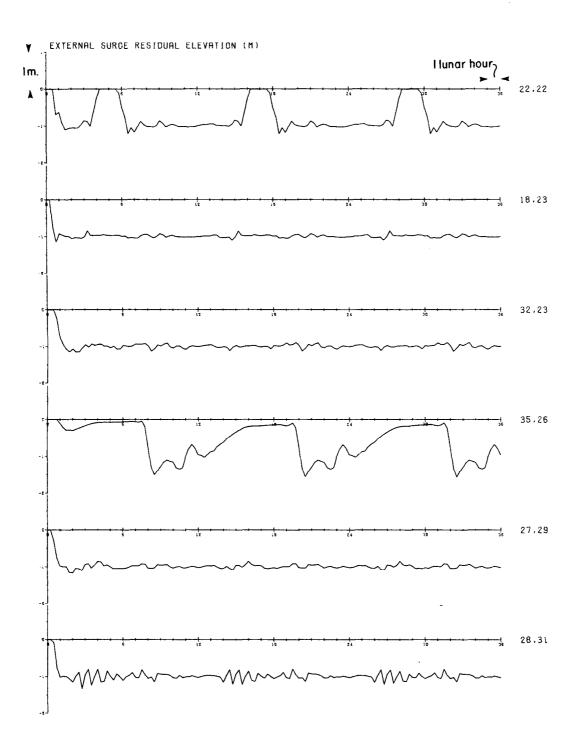
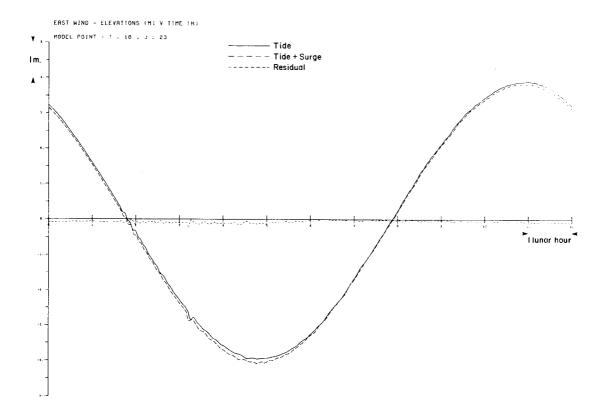


Figure 28: (CONT)



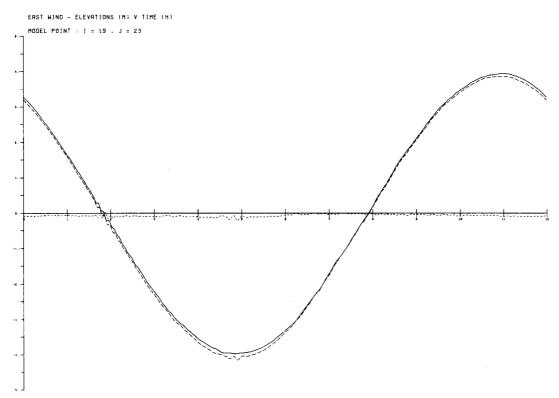
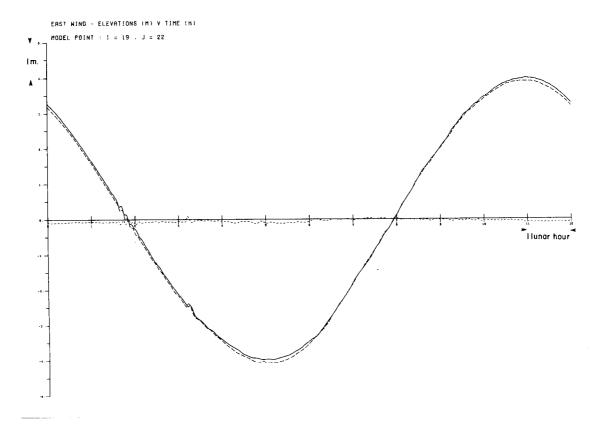


Figure 29: Variation of tide + surge (----), tide alone (----) and surge residual (....) produced by an easterly wind stress; sampling at every timestep over 1 tidal cycle.



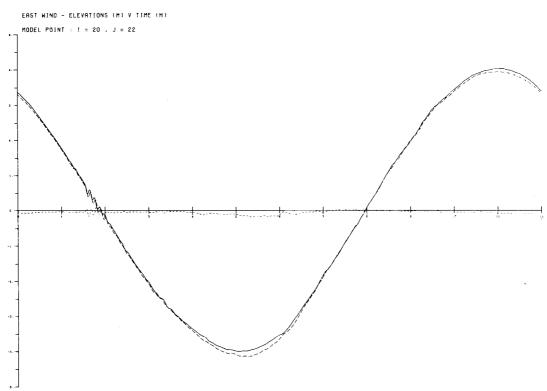
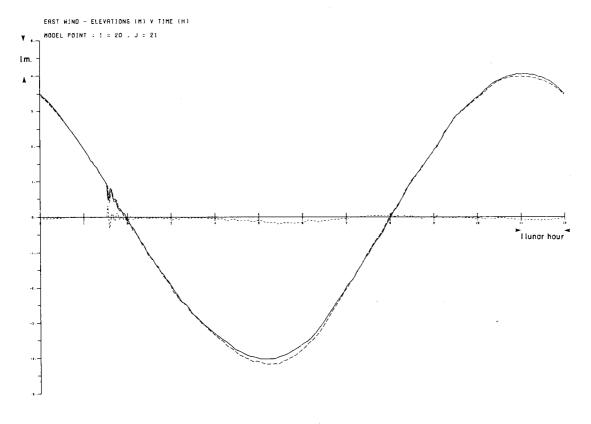


Figure 29: (CONT)



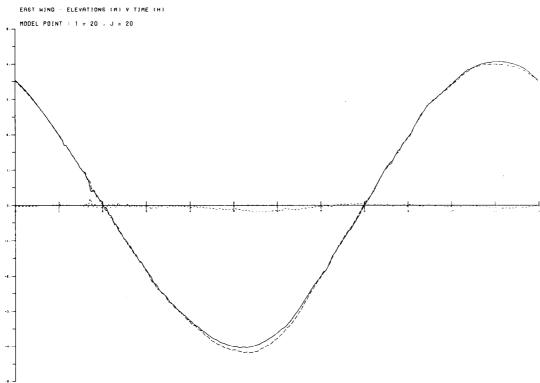


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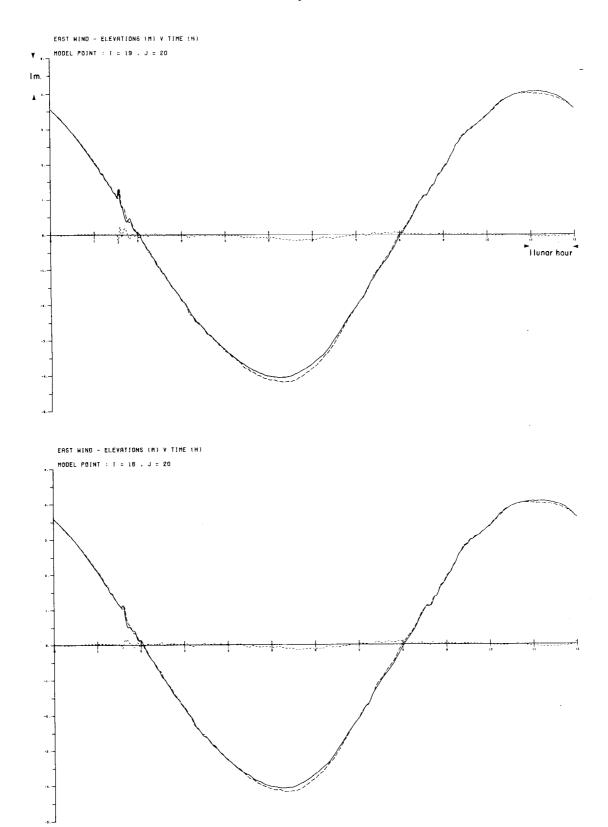
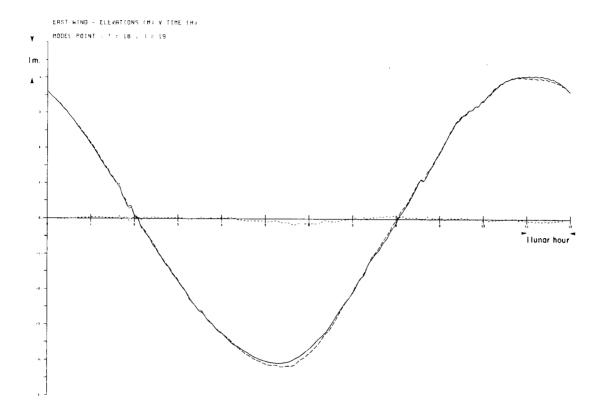


Figure 29: (CONT)



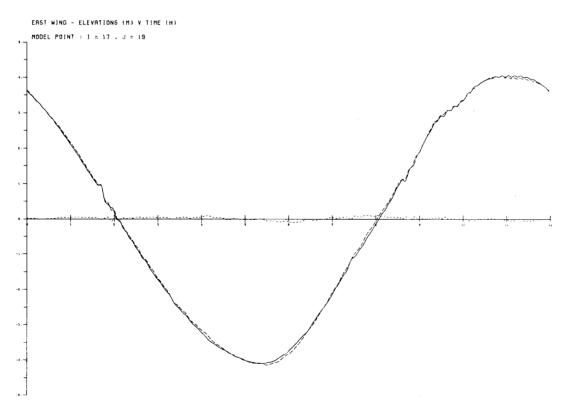


Figure 29: (CONT)

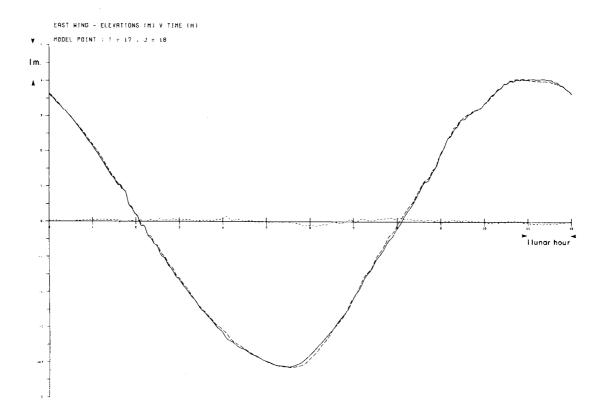
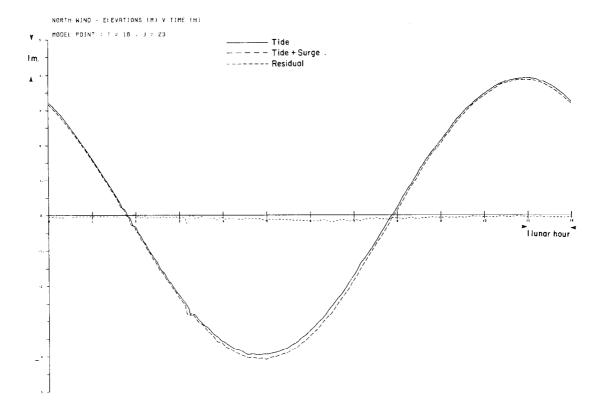


Figure 29: (CONT)



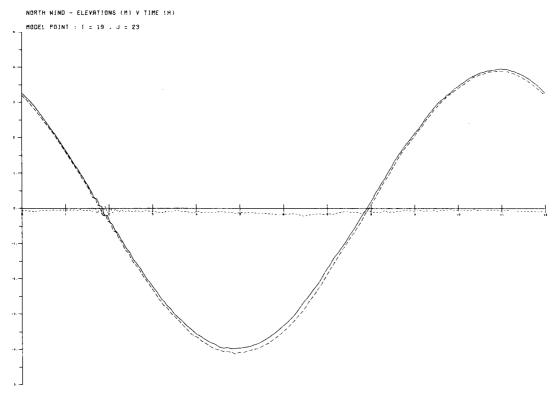
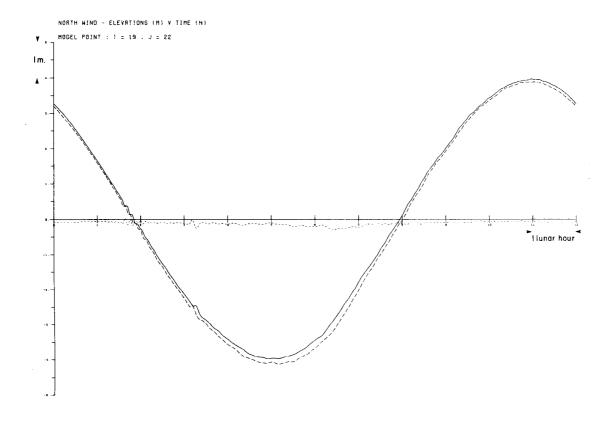


Figure 30: Variation of tide + surge (----), tide alone (----) and surge residual (....) produced by a northerly wind stress; sampling at every timestep over 1 tidal cycle.



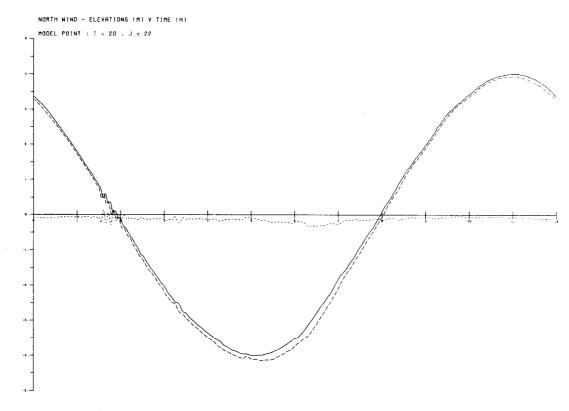
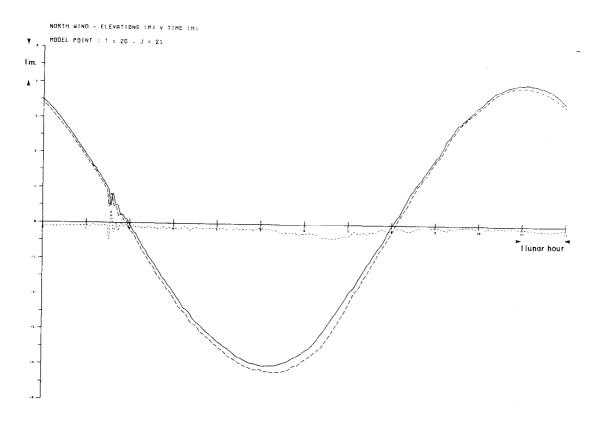


Figure 30: (CONT)



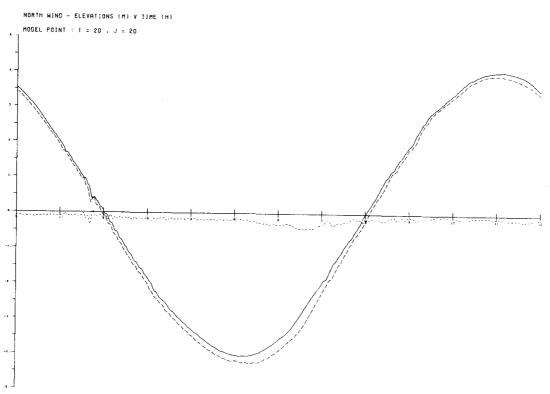
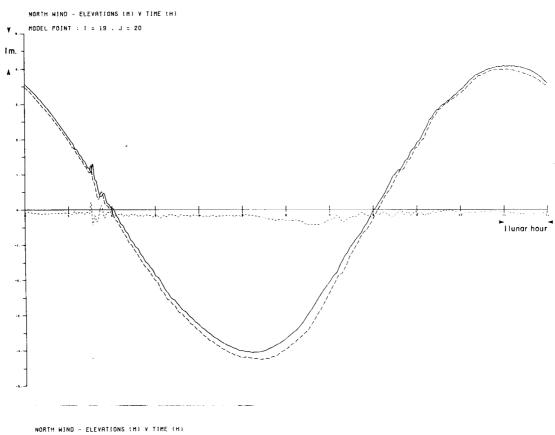


Figure 30: (CONT)



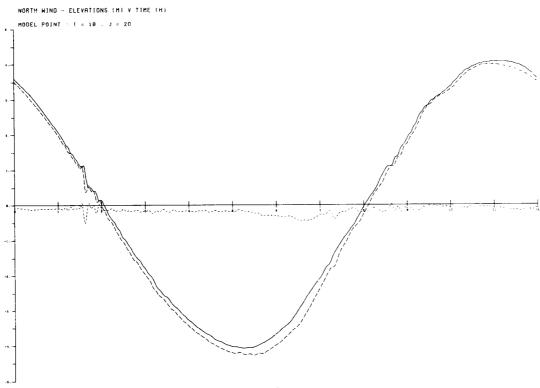


Figure 30: (CONT)

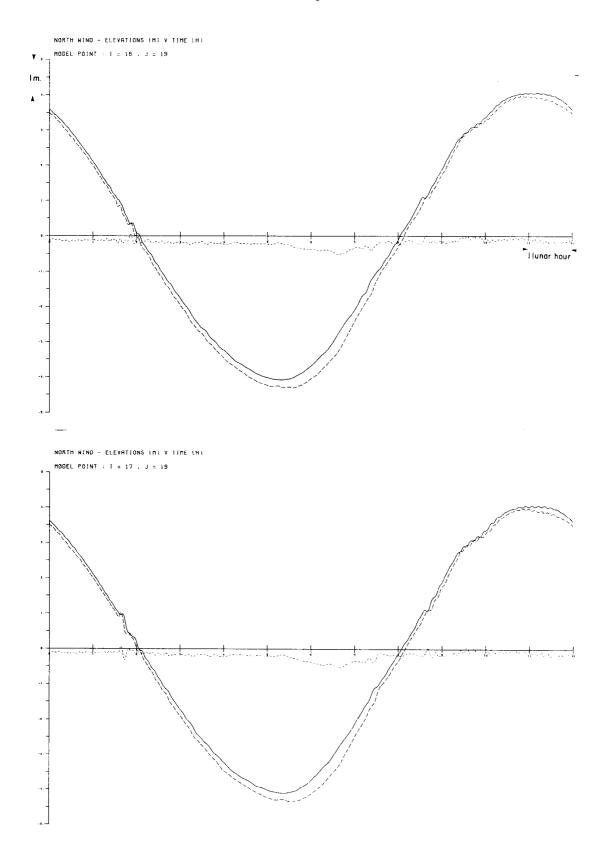


Figure 30: (CONT)

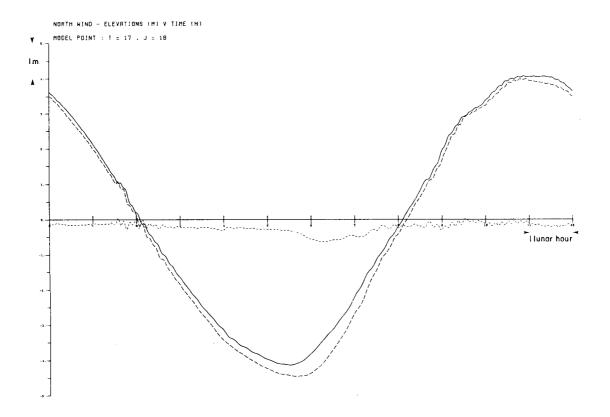


Figure 30: (CONT)

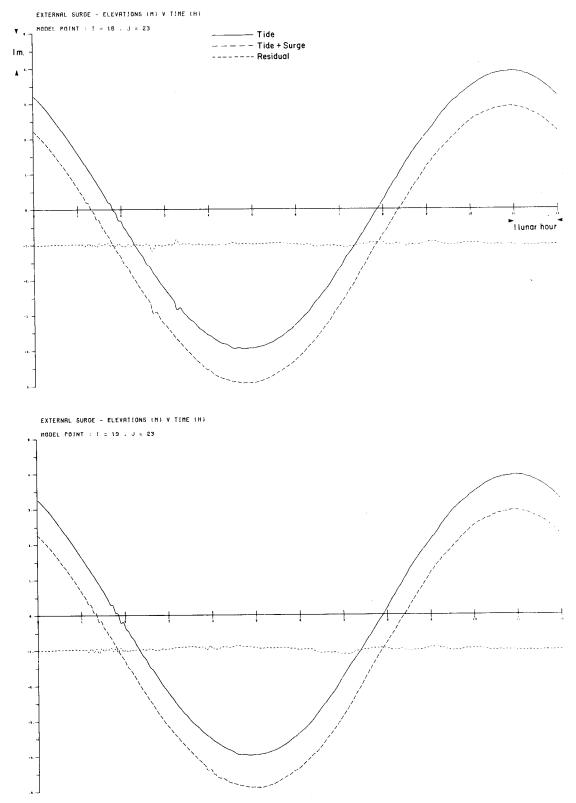
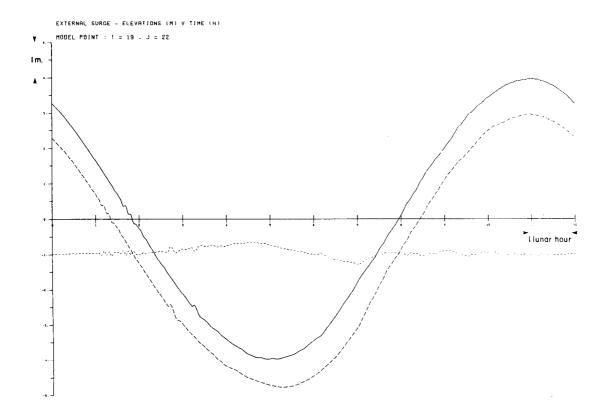


Figure 31: Variation of tide + surge (----), tide alone (----) and surge residual (·····) produced by a negative external surge; sampling at every timestep over 1 tidal cycle.



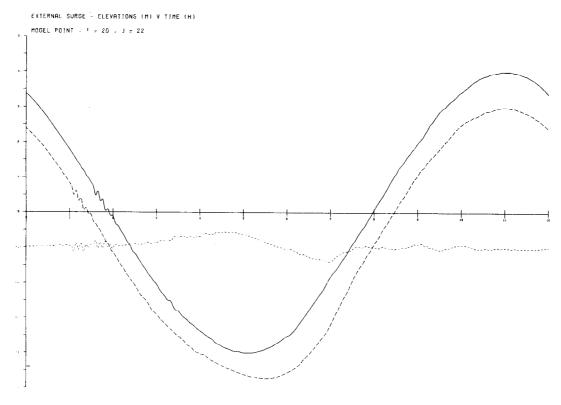
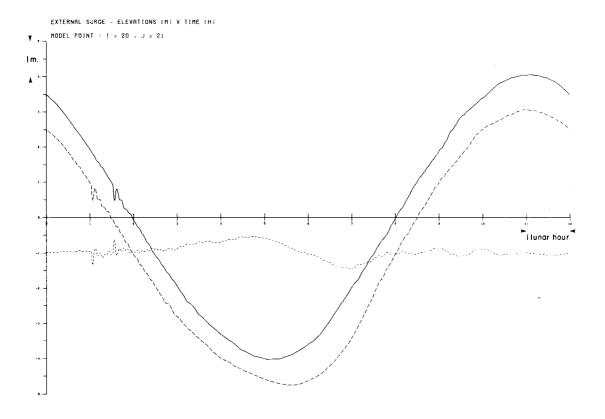


Figure 31: (CONT)



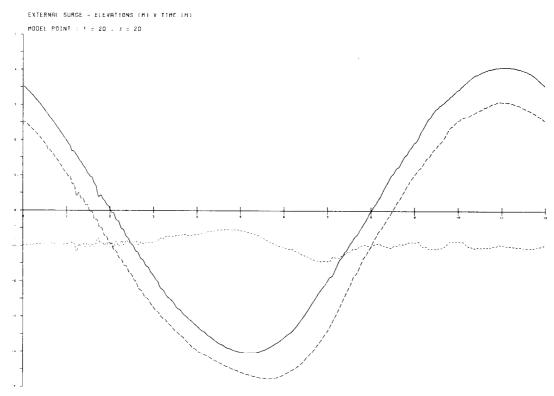


Figure 31: (CONT)

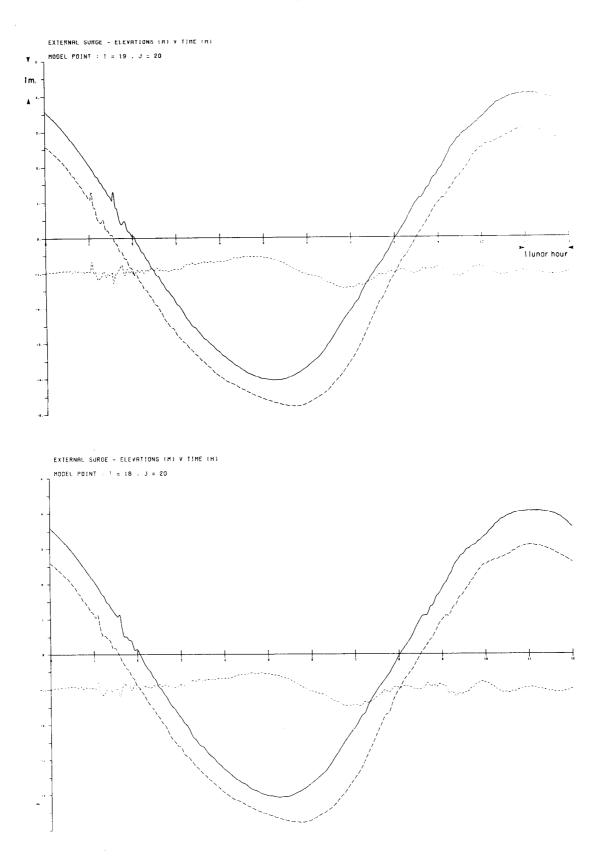
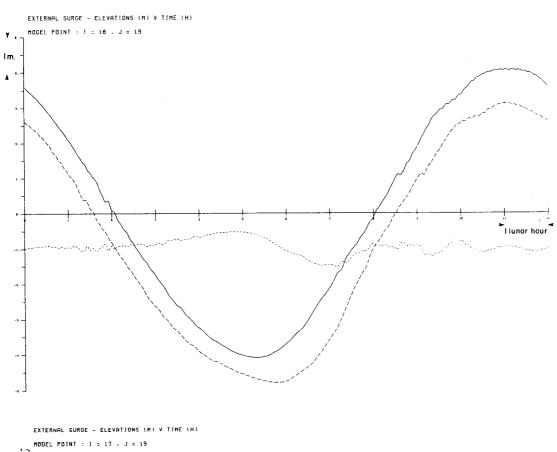


Figure 31: (CONT)



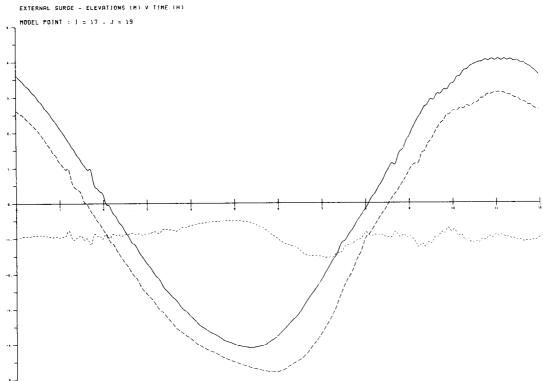


Figure 31: (CONT)

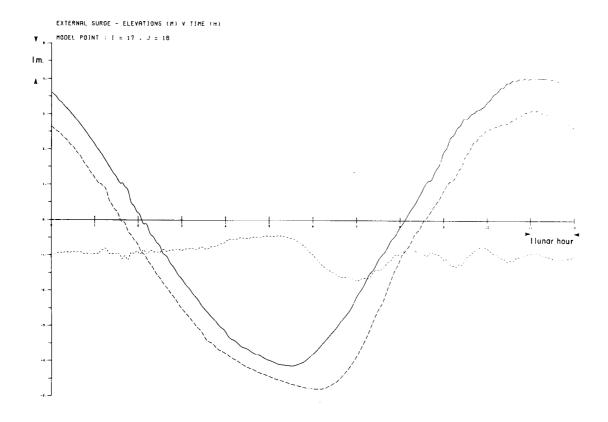


Figure 31: (CONT)

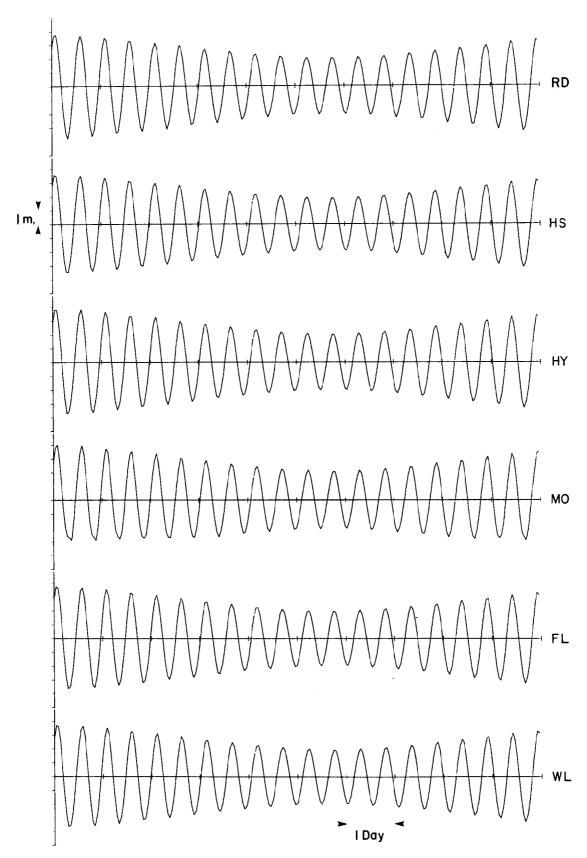


Figure 32: Computed tide at representative locations for the period 29 January to 7 February 1986.

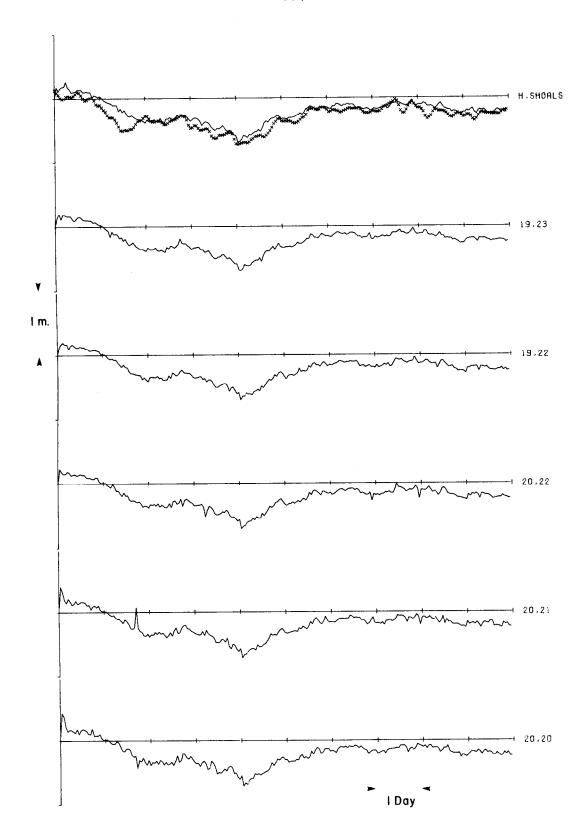


Figure 33: Time series of computed (\_\_\_\_\_) and observed (xxxxx) surge residuals for the period 29 January to 7 February 1986.

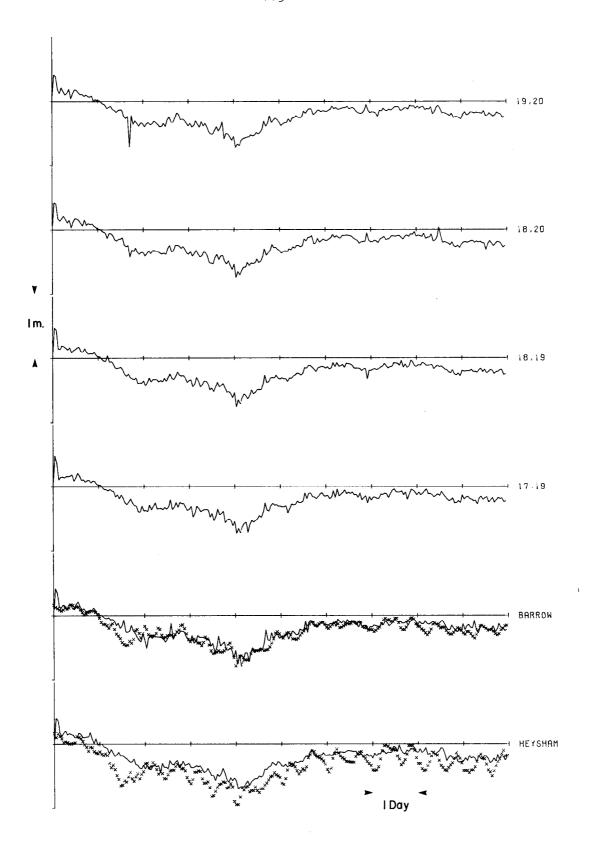


Figure 33: (CONT)

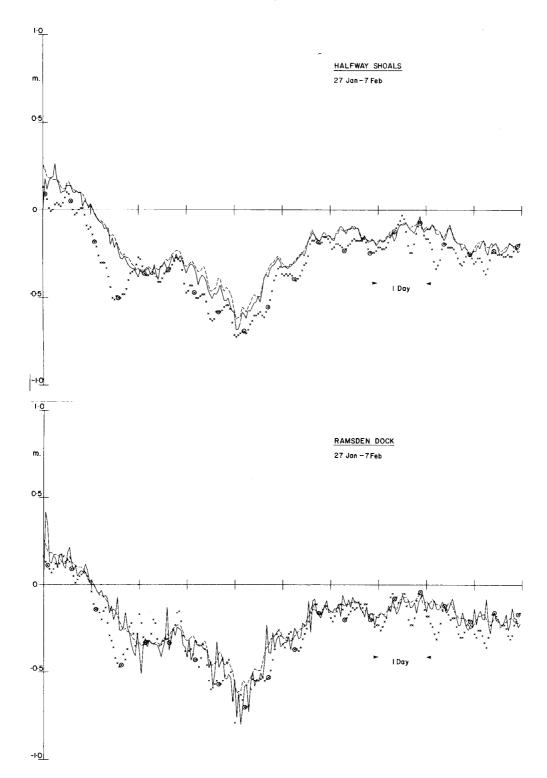


Figure 34: Comparisons of time series of surge residuals for Halfway Shoals and Ramsden Dock:

- a) derived from the present calculation (----);
- b) from observations (xxxxx), with circles indicating approximate times of tidal high water;
- c) from the nearest grid point of the operational surge forecast model (----).