

1 **Relating *in situ* hydraulic conductivity, particle size and relative** 2 **density of superficial deposits in a heterogeneous catchment**

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11 **Abstract**

12 Estimating the permeability of superficial deposits is fundamental to many aspects of catchment
13 science, but can be problematic where insufficient *in situ* measurements are available from pumping
14 tests in piezometers. Consequently, common practice is to estimate permeability from the material
15 description or, where available, particle size distribution using a formula such as Hazen. In this
16 study, we examine the relationships between particle size, relative density and hydraulic
17 conductivity in superficial deposits in Morayshire, Northern Scotland: a heterogeneous environment
18 typical of many catchments subject to previous glaciations. The superficial deposits comprise
19 glaciofluvial sands and gravels, glacial tills and moraines, raised marine sediments, and blown sands.
20 Thirty-eight sites were investigated: hydraulic conductivity measurements were made using
21 repeated Guelph Permeameter measurements, cone resistance was measured *in situ* with a Panda
22 dynamic cone penetrometer; material descriptions were made in accordance with BS5930:1999; and
23 disturbed samples were taken for particle size analysis. Overall hydraulic conductivity (K) varied
24 from 0.001 m/d to > 40 m/d; glacial till had the lowest K (median 0.027 m/d) and glacial moraine the
25 highest K (median 30 m/d). However, within each geological unit there was great variability in
26 measured hydraulic conductivity values. Multiple Linear regression of the data indicated that $\log d_{10}$

27 and relative density (indicated by cone resistance or BS5930:1999 soil state description) were
28 independent predictors of log K and together gave a relationship with an R^2 of 0.80. Material
29 description using the largest fraction (e.g. sand or gravel) had little predictive power. Therefore, in
30 heterogeneous catchments, the permeability of superficial deposits is most strongly related to the
31 finest fraction (d_{10}) and relative density of the material. *In situ* Guelph permeameter
32 measurements at outcrops with good geological characterisation provide an easy and reliable
33 method of determining the permeability of particular units of superficial deposits.

34 *Keywords: Permeability; Superficial deposits, Particle Size, Permeameter, Relative density, Hydraulic*
35 *conductivity*

36

37 1. Introduction

38 Estimating the permeability of superficial deposits is fundamental to many aspects of catchment
39 science and hydrogeology. It is critical to characterising groundwater/surface water interaction and
40 in particular baseflow to upland rivers (e.g. Morrice et al., 1997; Soulsby et al., 2007); groundwater
41 vulnerability assessments (Gogu RC and Dassargues 2000; Lake et al., 2003; Ó Dochartaigh et al.,
42 2005); urban hydrogeology (Bruce and McMahon, 1996; Chilton, 1999); groundwater recharge
43 (Lloyd et al., 1981; Cuthbert et al., 2009; Misstear et al. 2009; Griffiths et al., 2011) and increasingly
44 for predicting and mitigating flooding (Macdonald et al., 2008). Where sufficiently permeable and
45 saturated, superficial deposits form aquifers which can be developed for both private and public
46 water supply (e.g. Maupin and Barber, 2005; MacDonald et al., 2005).

47 The most obvious, and reliable, way to estimate permeability is through testing the saturated
48 portion of the aquifer using constant rate pumping tests in piezometers (e.g. Melville et al., 1991;
49 Jones et al., 1992; Jones, 1993; Meinken and Stobar, 2003). However, there are a number of
50 difficulties in relying solely on piezometers for characterising the permeability of superficial deposits:
51 (1) superficial deposits are highly complex, and sufficient boreholes are not generally available for
52 testing; (2) the deposits are often unsaturated (pumping tests are only applicable below the water-
53 table); (3) permeability can be too low to measure easily with standard pumping tests (Jones, 1993;
54 Renard, 2005); (4) the complexity of superficial sequences can mean that it is difficult to control
55 which units are being tested, and (5) fine-grained material can smear borehole walls causing
56 permeability to be underestimated (McKay et al., 1993). Various methods have been designed to
57 directly measure *in situ* permeability within soil, for example disc permeameters and infiltrometers
58 (Perroux and White, 1988; Angulo-Jaramillo et al., 2000), constant head permeameter (Amoozegar
59 1989; Elrick et al. 1989); but these methods are rarely used below the top soil.

60 Therefore, due to a lack of directly measured permeability data , surrogate information is used – for
61 example particle size analysis (e.g. Song et al., 2009), or permeability is inferred from the geological
62 description (e.g. McCloskey and Finnemore, 1996; Fogg et al., 1998; McMillan et al., 2000). The
63 relationship between permeability and particle size is well established and has been used as a
64 predictive tool since the 19th century (e.g. Hazen, 1892; Schlichter, 1899). These relationships are
65 still used today, and in a review of 19 studies of particle size and permeability Shepherd (1989)
66 demonstrated the clear trend of increasing permeability with increasing particle size. D_{10} (the
67 particle diameter that 10 % of the sample is finer than) is often seen as the best predictor of
68 permeability and central to many formulae used for calculating permeability (e.g. Hazen, 1892;
69 Kozeny, 1927; later modified by Carman, 1937, Carrier, 2003). However, many different methods
70 predict permeability using particle size data. For example, Alyamani and Şen (1993) used the full
71 distribution of particle sizes, rather than just the D_{10} ; and Cronican and Gribb (2004) developed a
72 method of determining permeability from particle size information in materials containing more
73 than 70 % sand. Permeability values derived from particle size analysis are different depending upon
74 which formulae are used (Vuković and Soro, 1992; Milham and Howes, 1995; Odong, 2007; Song et
75 al., 2009; Vienken and Dietrich, 2011). It is generally agreed that determining permeability using
76 particle size analysis is best suited to loose sand and gravel dominated sediments and is less suited
77 to deposits dominated by silt and clay (Vokovic and Soro, 1992; Chapuis, 2004).

78 It is clear that particle size alone does not determine permeability, and the wider factors controlling
79 permeability are the subject of ongoing study. Permeability of unconsolidated deposits is affected
80 by the particle shape, particle packing and degree of compaction (e.g. Sperry and Peirce, 1995;
81 Koltermann and Gorelick, 1995). Permeability is much higher in loose sediments than in compact
82 (dense) sediments, which have lower porosity and a less well developed network of interconnected
83 voids (Summers and Weber, 1984; Taylor et al., 1990; Koltermann and Gorelick, 1995; Watabe et al.,
84 2000; Hubbard and Maltman, 2000; Mondol et al., 2007). These complicating factors are more

85 significant in heterogeneous material, where the clay content, compaction and deformation of the
86 deposits are variable. In many catchments, and in particular those that have been subject to
87 glaciation, superficial deposits are highly heterogeneous and therefore it is often not appropriate to
88 use standard particle size models to reliably predict permeability.

89 Scale effects, and ensuring that permeability measurements relate to the same material that
90 engineering data (e.g. particle size analysis, relative density) have been collected for, provide
91 additional problems for developing robust models. Removing material to carry out permeability
92 measurements in a laboratory allows good control over the material on which the tests are being
93 carried out, but compromises the *in situ* characteristics of packing and density. Removing the
94 material as a core can partially overcome these issues, but the material needs very careful handling
95 to avoid deformation; also if the material is taken as a core then normally only vertical permeability
96 can be measured, and thus be limited by the lowest permeability layer within the sequence. *In situ*
97 tests such as pumping tests or slug tests sample a larger area and often report higher permeabilities
98 than laboratory tests, mainly due to the presence of fracturing (Daniel, 1989; Neuzil, 1994; Schulze-
99 Makuch et al., 1999; Gierczak et al., 2006). This is particularly common within very low permeability
100 till material (e.g. Hendry, 1982; Keller et al., 1988; Fredericia, 1990; McKay et al., 1993; Nilsson et al.,
101 2001). If tills are not fractured, then scale effects are less of an issue (Keller et al., 1989).

102 In this study, we examine a variety of superficial deposits from Morayshire, Northern Scotland,
103 measuring *in situ* saturated hydraulic conductivity, taking samples for particle size analysis, making
104 soil descriptions, and measuring *in situ* cone resistance. The aim is to examine the relationships
105 between particle size, relative density and hydraulic conductivity, and to determine how well the
106 surrogate data predict hydraulic conductivity in this heterogeneous suite of deposits, typical of many
107 catchments that were subject to Quaternary glaciations.

108

109 2. Study area

110 The northeast coast of Scotland, between Inverness and Aberdeen, has interesting hydrology and
111 geology, which have a significant impact on land use and society. Several major rivers flow
112 northward from the Grampian highlands in the south towards the Moray Firth (Figure 1). These
113 rivers are prone to flooding (McEwen and Werrity, 2007), and considerable effort and resource is
114 being invested in developing flood alleviation schemes to protect the coastal towns of Elgin and
115 Forres. Previous glaciation of this area has resulted in the formation of a coastal strip of flat land
116 approximately 10 – 20 km wide. This ground is underlain by 10s of metres of superficial deposits
117 which form fertile soils and enable high-value agriculture. The coastal strip receives relatively little
118 rainfall compared to the rest of Scotland (< 600mm) and groundwater is widely abstracted for
119 agricultural and industrial use, and in some locations for public supply (Ó Dochartaigh et al., 2010).
120 Characterising the permeability of the strata is fundamental to helping to predict and mitigate
121 flooding, assess the risk of groundwater flooding, and also assess the potential of the superficial
122 materials for sustaining large scale groundwater abstraction.

123 The area is underlain by a complex succession of Glacial and Post Glacial strata (Figure 1) that have
124 mainly accumulated during the last 25,000 years. These range in thickness from a few to many tens
125 of metres. The sandstone and ancient crystalline bedrock is generally concealed beneath a variable
126 thickness of glacial till (Figure 1 and 2). Much of this till was laid down during the Main Late
127 Devensian ice-sheet glaciation of Scotland, although some sandy tills and associated moraines in the
128 coastal area were deposited by re-advances of a major fast-flowing glacier that occupied the Moray
129 Firth after the surrounding uplands had become ice free. Most of the glacial tills crop out in steep
130 river cliffs, where they are seen to be overlain by a considerable thickness of sand and gravel that
131 were deposited by glacial meltwaters as the ice decayed. Mounds and ridges of poorly sorted
132 cobble and boulder gravel were laid down in contact with the ice, whereas the well stratified sand

133 and gravel that forms terraces up to 15 m in height on the flanks of the present valleys were
134 deposited by meltwater rivers beyond the ice margins. In the coastal area meltwater flowed into
135 what is now the Inner Moray Firth, where it mixed with seawater and laid down sandy and silty
136 glaciomarine sediments many metres in thickness.

137 Much of the outcrop of the glacial, glaciofluvial and glaciomarine deposits is concealed by Post
138 Glacial sediments (Figure 2). Along the coast, the glaciomarine sediments are largely buried beneath
139 Post Glacial raised shoreline deposits of silt and sand, and both are locally concealed beneath
140 extensive dunes of blown sand. Inland glacial, glaciolacustrine and glaciofluvial sediments have been
141 reworked by rivers and streams to form spreads of sandy and gravelly alluvium and river terraces
142 along the major valleys; silty lacustrine deposits and peat infill many ice scoured hollows and
143 kettleholes, and blanket peat is still accumulating on the higher ground.

144

145 **3. Methods**

146 **3.1 General/Site selection**

147 Twenty-five sections of superficial deposits for which the geology is well characterised were selected
148 in an area of approximately 250 km² (Figure 1). The sites were chosen to include all the main types
149 of superficial deposits present. Sections were between 2 and 20 m high, and at some sections
150 several different types of superficial deposits were present and were sampled. Figure 3 shows a
151 photograph of a typical section. In total, 38 different deposits were sampled at the 25 sections of
152 which 14 were glacial tills, 3 were glacial moraines, 7 were glaciofluvial sands and gravels, 3 were
153 glaciolacustrine deposits, 8 were raised marine deposits, and 3 were blown sand deposits.

154 Each site was visited by a team including a Quaternary geologist, hydrogeologist and engineering
155 geologist. The Guelph permeameter was used to obtain an *in situ* measurement of the hydraulic

156 conductivity of the deposits. The cone resistance of the material was measured *in situ* with a Panda
157 dynamic cone penetrometer to give an indication of relative density, superficial deposit descriptions
158 were made at the outcrop in accordance with BS5930:1999 (British Standards Institute, 1999a); and
159 disturbed samples were taken for particle size analysis. At each site, *in situ* Guelph permeameter
160 and Panda cone penetrometer measurements were carried at the same place within the outcrop
161 and within the same material, which was then sampled for particle size analysis.

162 **3.2 Guelph permeameter field methods**

163 The Guelph permeameter measures the field saturated hydraulic conductivity of unsaturated
164 deposits and involves measuring the volume of water required to maintain a steady-state constant
165 head using a Mariotte bottle system constructed of plastic tubes (Figures 3 and 4, see Reynolds and
166 Elrick (1985) for a full description of the apparatus and procedure). The major advantage of this type
167 of test is that the material is *in situ* so a more representative volume of material can be tested than
168 in the laboratory (Daniel, 1989). In this study, the one head method was used (Elrick et al., 1989;
169 Reynolds et al., 1992) which should generally give results within 25% of the two head method. The
170 permeameter used has an approximate quoted range of 10^{-7} to 10^{-4} m/s; however we found the
171 permeameter to have repeatable results slightly outside this range and determined a practical range
172 of 0.001 to 40 m/d (1.2×10^{-8} to 5×10^{-4} m/s). Others have also used the Guelph permeameter
173 within this expanded range (e.g. Lee et al., 1985; Mohanty et al., 1995).

174 Six sections were sampled in September 2008 and the remaining sections were sampled in June
175 2009. At each measuring point a flat ledge was excavated into the exposure at least one metre
176 below the soil (Figures 3 and 4). The ledge extended into the face ensuring that measurements were
177 not affected by small scale fracturing at the edge of the ledge, or by the roots of any vegetation
178 present at the top of the outcrop. A hole of constant diameter (which ranged from 5 to 6 cm
179 between test sites) with a depth of 6 to 10 cm was excavated into the ledge. In clayey materials the

180 walls were de-smearred using a sharp metal spoon and small wire brush (Bagarello et al., 1997). The
181 Guelph Permeameter was placed in the hole immediately after excavation with a small pack of 5 –
182 10 mm pea gravel to prevent the sides of the hole collapsing. Water was released from the Guelph
183 Permeameter to obtain a constant head of 4 to 5 cm in the hole. Gradations on the Guelph
184 Permeameter were read at regular intervals to determine the rate of water input required to
185 maintain the head. Readings were taken at intervals determined by the rate of water movement
186 and varied from every 5 seconds to every 15 minutes depending upon the permeability of the
187 deposit. In the highest permeability deposits measurements were made until the reservoir emptied,
188 but in other deposits measurements continued until a regular rate of water input was consistently
189 observed.

190 At most sampling locations a second measurement was made in the same deposit, and if there were
191 substantial variations between the two measurements or some other problem (e.g. flooding,
192 collapse, or cracking of the material surrounding the hole), a third measurement was made. The
193 repeated measurements were made on a new ledge constructed at the same depth and into the
194 same material as the first. Occasionally it was only possible to obtain one reliable measurement in a
195 deposit type because of the geometry of the section, or because the permeability was below the
196 measuring capacity of the permeameter. Hydraulic conductivity was calculated from the data using
197 the software G-Perm1 which is based on the formulae outlined in Reynolds and Elrick (1985).

198 **3.3 Soil description field method**

199 Soil descriptions, in accordance with British Standards BS5930:1999 (British Standards Institution
200 1999a) and BS5930:1999 amendment 1 (British Standards Institution, 1999b), were made for all the
201 superficial deposits encountered at each section by an engineering geologist. The standards
202 systematically describe the state, structure, colour and the size and relative proportions of
203 composite particles. Particular emphasis was given to the descriptions of *soil state* which directly

204 describes relative density (for coarse soils) or is directly related to relative density (for fine soils).
205 Descriptions of fine soils were made in accordance with BS5930:1999 amendment 1 such that the
206 *soil state* of silt and clay was described from very soft through soft, firm and stiff to very stiff.
207 Descriptions of coarse soils were made in accordance with BS5930:1999 such that the *soil state* of
208 sand and gravel was described from very loose through loose, medium dense, dense to very dense.
209 Descriptions of all soil properties were based solely on field observation.

210 In order to allow the relationship between soil *state* and hydraulic conductivity to be quantified a
211 Soil State Description Value (SSD) was derived. The coarse *soil state* descriptions were numerically
212 ranked from 1 to 5, very loose to very dense. The *soil state* descriptions for fine deposits were
213 numerically ranked from 1 to 5 from very soft to very stiff.

214

215 **3.4 Particle size distribution sampling and analysis**

216 Large disturbed bulk samples were taken from each superficial deposit, at each location, in
217 accordance with BS5930:1999 amendment 1 (British Standards Institution, 1999b). Large cobbles
218 and boulders were not sampled due to limitations on the mass of material that could be obtained at
219 each outcrop. Instead, a note of any omission of large cobbles and boulders was made for each
220 sample where it occurred, and the mass percentage of cobbles and boulders was estimated and
221 added to the soil description. The particle size distribution analysis data does not include particles
222 larger than cobble size (>200 mm). The sample material was obtained adjacent to *in situ* test
223 locations to ensure they were representative of the deposits tested by both the Guelph
224 permeameter and Panda penetrometer.

225 Thirty-four samples were tested for particle size distribution in accordance with BS1377:Part 2:1990
226 (British Standards Institution, 1990) and Eurocode 7: Part 2 (2007). The analysis was undertaken
227 using the wet sieving method. Where a significant fraction (>10%) of material <63 μm remained,

228 further analysis was undertaken to separate the silt and clay fraction. Fine particle analysis was
229 undertaken, in accordance with Eurocode 7 (2007), by x-ray monitored gravity sedimentation using a
230 Micromeritics SediGraph III. As part of the analysis the d_{10} , d_{15} , d_{30} and d_{60} for each sample was
231 calculated, corresponding respectively to the 10th, 15th, 30th and 60th percentile of the particle size
232 distribution.

233

234 3.5 Panda penetrometer field methods

235 Dynamic cone penetrometer measurements were undertaken for thirty deposits at 23 locations. This
236 technique measures the *in situ* dynamic cone resistance (in megapascals - MPa) of the soil through
237 which the cone is passing and is, therefore, directly related to the relative density of the deposit. The
238 test was undertaken by driving a 4 cm² steel cone on the end of a set of 0.5 m long threaded steel
239 rods through the target deposit using a fixed weight hammer. The Panda2 measures the velocity of
240 the hammer impact on the head of the rods and the depth of cone penetration in order to
241 determine the dynamic cone resistance using a modified form of the Dutch Formula (Langton, 1999).
242 The method can reach depths of up to 6 m in soils with a resistance up to 20 MPa. It is relatively
243 lightweight (20 kg) and portable thereby making it ideal for testing soils *in situ*. A more detailed
244 explanation of the Panda Penetrometer testing methodology and correlations with other dynamic
245 and static cone penetration tests can be found in Langton (1999).

246 The thirty *in situ* Panda Penetrometer tests were carried out in two field seasons: Sept/Oct 2008 and
247 June 2009. The tests were undertaken adjacent to the location of the Guelph permeameter tests to
248 ensure the deposits tested were representative of those tested by the Guelph permeameter.
249 However, tests were performed sufficiently far apart (in the order of 1 – 5 m), in order to minimise
250 the interference effects. Panda penetrometer tests were also not performed at the same time as
251 Guelph permeameter so that vibration did not affect deposits being tested by the Guelph

252 permeameter. At each location an initial attempt was made to test the entire exposed section by
253 probing from the top of the section to the base. Where this was not possible then a flat shelf or
254 series of shelves were dug at appropriate intervals so as to intersect the target strata (Figure 5). The
255 test was terminated once effective refusal was reached (where cone resistance was consistently >20
256 MPa) or once the rod length was below the level of the exposed section. Where effective refusal
257 occurred as the likely result of an isolated obstacle, such as a cobble or boulder, then a repeat test
258 was conducted at the same level but offset by a few metres to avoid the obstacle. Where refusal
259 occurred in dense and/or cobbly and bouldery strata (i.e. where obstacles were not isolated) then a
260 second test was undertaken, where possible, on a flat excavated shelf or surface below the level of
261 the dense and/or coarse stratum.

262 The dynamic cone resistance measured at each test location was recorded by the Panda2 unit as a
263 single sounding. Examples of typical soundings from two sites are shown in Figure 6. There is
264 variability in the dynamic cone resistance measured by each separate hammer blow, which is to be
265 expected in heterogeneous deposits. However, it is possible to correlate sections of the Panda
266 sounding with separate layers identified as part of the geological descriptions made in the field. The
267 median value of the section referring to the target geological unit was used in the analysis. Where
268 more than one Panda test was undertaken in a deposit, the average was used.

269 **4. Results**

270 **4.1 Guelph permeameter results**

271 The field data produced consistent plots of water-level through time indicating the steady infiltration
272 rate of water during the test required for analysis (Figure 7). Figure 8 shows that repeat samples in
273 the same deposit type at the same outcrop give similar hydraulic conductivity ($R^2 = 0.9$) indicating
274 that the measurements are reproducible. For the 28 sample sites where 2 or more reliable hydraulic
275 conductivity values were obtained, a mean hydraulic conductivity for the site was used for further

276 analysis. Since Figure 8 indicates a high degree of reproducibility in the data, the 10 sampling sites
277 for which only one measurement could be made were also used in the further data analysis
278 described below.

279 The results for the 38 sampling sites are presented in Table 1 and Figure 9. Hydraulic conductivity is
280 highly variable within, as well as between, particular types of superficial deposits from different
281 sample locations reflecting the heterogeneity of these types of materials. Glacial tills had the lowest
282 hydraulic conductivity with a median of 0.027 m/d, but a range of < 0.001 m/d to approximately 1
283 m/d. Glacial fluvial deposits, (comprising both fluvial and lacustrine deposits) had a much higher
284 hydraulic conductivity with a median of 2.5 m/d, but again a wide range, < 0.1 to > 40 m/d. The
285 raised marine deposits showed fairly consistent hydraulic conductivity with median 1.7 m/d and
286 interquartile range of 0.9 – 3 m/d. Raised Marine deposits in this area are variable in composition
287 and include sands and gravels with relatively high permeability, and the Ardersier Silt Formation
288 which varies in composition from sands to silts. Two sites were in the raised marine Ardersier Silt
289 Formation where it is predominantly silt and these had lower permeability than other sites in Raised
290 Marine deposits. There were few sites in blown sand and glacial moraines. The three available
291 blown sand results were consistent and varied from 4.5 to 9.5 m/d reflecting the uniform nature of
292 the material. The three sites testing glacial moraine deposits showed variable permeability 0.15 to >
293 40 m/d, and one site had the highest permeability recorded in Morayshire, exceeding the measuring
294 capacity of the Guelph permeameter.

295 **4.2 Engineering data**

296 Summary graphs displaying particle size distribution analysis envelopes for each superficial deposit
297 are presented in Figure 10. The d_{10} , d_{60} and sample descriptions are given in Table 1. The graphs
298 demonstrate a consistency of particle size distribution in the glacial tills, glacial moraine and blown
299 sand; however, there is greater variability in the particle size distribution of the glaciofluvial and the

300 raised marine deposits. Moraine and blown sand are coarse deposits with no significant silt or clay
301 components. Raised marine, glaciofluvial and glacial till are mixed fine and coarse deposits with
302 significant proportions of silt and clay.

303 The soil state descriptions (SSD) of the superficial deposits described at each section are given in
304 Table 1. They display a high degree of variability both between superficial deposit types and, in many
305 cases, within a single superficial deposit category. A comparison of SSD indicates: glacial till to be
306 highly variable but generally denser than other deposits; raised marine and glaciofluvial deposits
307 have moderate SSD (with greater intra-deposit variability than glaciofluvial deposits). Blown sand
308 and moraines have the lowest SSD and appear to have less intra deposit variability, although this
309 could be due to the low sample number.

310 The dynamic cone resistance values are shown in Table 1. There is high variability within each
311 superficial deposit type, with the exception of blown sand deposits. In general, till deposits have the
312 highest resistance, followed by glaciofluvial, raised marine, moraine and then finally blown sand
313 deposits.

314

315 **4.3 Multiple Linear Regression**

316 The engineering and hydraulic conductivity data were analysed together using multiple linear
317 regression (MLR) and Pearson correlation tests. Since particle size and hydraulic conductivity are
318 both logarithmically distributed, they were log transformed before analysis. There were 27 sites
319 which had sufficient data to be included in the analysis (Table 1). Table 2 shows the results of the
320 Pearson correlation tests. All parameters, (except d_{60}) were significantly correlated with hydraulic
321 conductivity. Unsurprisingly there is a high degree of correlation between many of the input
322 parameters, particularly d_{10} , d_{15} and d_{30} .

323 The results of stepwise multiple linear regression for hydraulic conductivity, particle size and cone
324 resistance (CR) are shown in Table 3. The analysis indicates that, for this dataset, cone resistance
325 and $\log d_{10}$ are the only independent predictors of $\log K$. The relationship for the 27 sites is described
326 as:

$$327 \log K = 0.97 \log(d_{10}) + (2 - 0.11CR) \quad \text{Equation [1]}$$

328 Where D_{10} is in mm, CR in MPa and K in m/d. The statistical relationship is strong, with $R^2 = 0.80$
329 when adjusted for the size of the dataset (Figure 11). Independently, $\log d_{10}$ and CR predict $\log K$
330 with an R^2 of 0.6 and 0.35 respectively. Using soil state description, rather than CR allows a slightly
331 larger dataset of 34 for the analysis. A similar relationship is given :

$$332 \log k = 0.79 \log d_{10} + (2.1 - 0.38 SSD) \quad \text{Equation [2]}$$

333 with a similar strength of correlation as for Cone Resistance ($R^2 = 0.78$). Figure 12 illustrates how
334 field descriptions of density together with D10 relate to hydraulic conductivity.

335 The proportion of each fraction, (clay, silt, sand, gravel and cobbles) was also calculated for each
336 sample, and is reported in Table 1 in the material description. Figure 13 demonstrates an overall
337 relationship between the particle size of the largest fraction and hydraulic conductivity, but its
338 overall predictive power is weak, as demonstrated by the 4 orders of magnitude between 10th and
339 90th percentile for sand, and the weak correlation ($R^2 = 0.16$).

340

341 5. Discussion

342 This study of the hydraulic conductivity of heterogeneous superficial deposits, typical of many
343 glaciated catchments of NW Europe, has provided useful information on the dominant factors
344 controlling permeability across the different deposits, and therefore which properties should be

345 measured to help characterise hydraulic conductivity. In addition, the methodologies developed
346 within this study have proved an effective way of characterising permeability in a complex
347 catchment: the integrated geological, hydrogeological and engineering approach; and the field
348 methods for measuring *in-situ* hydraulic conductivity.

349

350 The smallest 10% of particle sizes within the deposit and the relative density of the material together
351 explain much of the variance in hydraulic conductivity for this heterogeneous catchment. Therefore,
352 modified Hazen formulae, which account for relative density as well as d_{10} , are likely to be the best
353 method for estimating permeability in these glaciated environments. This is probably due to the
354 range of deposits present, and also to the large variability in the relative density of materials formed
355 within a glaciated environment, where over consolidated glacial tills co-exist next to loose glacial
356 moraines, or modern alluvium. Additional information on the particle size distribution such as those
357 found useful by Alyamani and Şen (1993), were found not to help predict hydraulic conductivity.
358 Our results are consistent with previous studies which highlight the importance of d_{10} in grain size
359 analysis to determine hydraulic conductivity (e.g. Hazen, 1892; Vuković and Soro, 1992; Odong,
360 2007) and the effect of varying degrees of compaction on hydraulic conductivity (e.g. Watabe et al.,
361 2000; Lu, 2007). These two parameters appear to be the dominant controls on permeability when
362 considering a wide range of different and heterogeneous superficial deposits. The relationship
363 remains strong across the range of materials tested and is therefore useful for this heterogeneous
364 environment. However, for more detailed work in one particular type of material a specific
365 relationship may give more accurate results (e.g. Vinken and Deitrich 2011).

366

367 The size of the largest fraction had little predictive power. Therefore, using the bulk descriptors
368 SAND, SILT, or GRAVEL, to help classify the permeability is of limited use. This was also observed in a
369 study by Fogg et al. (1998) who found only a weak correlation between these sorts of bulk

370 descriptors and hydraulic conductivity. Particular attention must therefore be given to the presence
371 of silt or clay, and the degree of consolidation of the material. For this reason, where detailed
372 information is not available for a catchment, building a conceptual understanding of the superficial
373 geology, and the palaeo-environment and nature of deposition, can help to generate more
374 information on the likely presence of fines and the degree of compaction (see Griffiths et al., 2011).
375 The influence of the finest 10% of the material also has relevance for sampling. Drillers logs, and
376 samples taken from the drilling and installation of piezometers, often do not record much of the
377 finest fraction. The fines are held in suspension, or washed away by the drilling process. Therefore
378 samples are best taken from outcrop, or from cores.

379
380 The methodology developed to measure hydraulic conductivity of the superficial deposits proved to
381 be robust and relatively rapid to undertake. Targeting measurements to distinct geological outcrops
382 identified by a Quaternary geologist ensured that heterogeneity of the catchment could be
383 confidently reflected in the sampling. Also the repeated Guelph permeameter measurements gave
384 reassuringly similar results at each outcrop ($R^2 = 0.9$) and could be undertaken rapidly. Therefore,
385 despite the robust relationship between d_{10} , relative density and hydraulic conductivity, it may be
386 more effective to carry out repeated Guelph permeameter measurements at characteristic outcrops
387 than gathering surrogate information and estimating permeability.

388 The use of soil state descriptors proved reliable, and as significant a predictor when correlated with
389 d_{10} as cone resistance (Table 2). Therefore, given the difficulties in making *in situ* measurements of
390 cone resistance, and the wide availability of *soil state* descriptions in borehole and trial pit logs,
391 observations made in accordance with BS5930:1999 can be used as an adequate substitute for the
392 measurement of relative density.

393 The wide range and heterogeneous nature of the deposits tested suggests that our findings may be
394 fairly widely applicable in superficial deposits. However it would be useful to obtain more data in

395 blown sand and glacial moraine deposits and other deposit types that were not tested (e.g. fluvial
396 deposits).

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398 6. Conclusions

399 This study has investigated the hydraulic conductivity of superficial deposits in a heterogeneous
400 catchment in northern Scotland, typical of many catchments subjected to past glaciations in North
401 West Europe. In total, 38 different deposits were sampled at 25 sections. The deposits comprised:
402 glacial tills and moraines; glaciofluvial and glaciolacustrine deposits; raised marine deposits; and
403 blown sand. Hydraulic conductivity measurements were made using repeated Guelph Permeameter
404 measurements, cone resistance was measured *in situ* with a Panda dynamic cone penetrometer (to
405 give an indication of relative density); material descriptions were made in accordance with
406 BS5930:1999; and disturbed samples were taken for particle size analysis. The following conclusions
407 can be drawn:

- 408 1. *In situ* measurements of hydraulic conductivity made with a Guelph permeameter at deposit
409 outcrops proved highly repeatable ($R^2 = 0.9$).
- 410 2. Hydraulic conductivity (K) ranged from 0.001 m/d to > 40 m/d; glacial till had the lowest K
411 (median 0.027 m/d) and glacial moraine the highest K (median 30 m/d).
- 412 3. The results of stepwise multiple linear regression for hydraulic conductivity, particle size and
413 cone resistance indicate that, for this dataset, cone resistance and $\log d_{10}$ are the only
414 independent predictors of $\log K$ [$\log K = 0.97 \log(d_{10}) + (2 - 0.11CR)$], where d_{10} is in mm, CR in
415 MPa and K in m/d. The statistical relationship is strong, with $R^2 = 0.80$ when adjusted for the size
416 of the dataset.
- 417 4. Using soil state material descriptions made in accordance with BS5930:1999 instead of the cone
418 resistance to give an indication of relative density gave a similar relationship and strength of
419 correlation ($R^2 = 0.78$). Therefore high quality soil state descriptions are a good surrogate for
420 cone resistance measurements.

421 5. The size of the largest fraction had little predictive power. Therefore, using the bulk descriptors
422 SAND, SILT, or GRAVEL, to help classify the permeability of unconsolidated heterogeneous
423 sediments is of only limited use.

424 6. *In situ* Guelph permeameter measurements at outcrops with careful geological characterisation
425 provide a good method of determining the permeability characteristics of superficial deposits
426 where large-scale permeability testing is not feasible.

427 With the growing recognition of the importance of the hydraulic conductivity of superficial deposits
428 to many aspects of catchment hydrology and hydrogeology, robust methods of characterising
429 hydraulic conductivity will become increasingly important. The methodologies and relationships
430 developed within this paper should help to inform future studies of catchment permeability.

431

432

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437

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593 **Figure Captions**

594

595 Figure 1: Simplified superficial geological map of the study area.

596 Figure 2: Schematic cross section across the area illustrating the general succession of deposits.

597 Figure 3: Guelph Permeameter measuring hydraulic conductivity of the grey coloured Ardersier Silts
598 at Cloddymoss (locality 20, Figure 1) with ledges below excavated into the underlying orange
599 coloured till.

600 Figure 4: Ledge and hole excavated into raised marine sands.

601 Figure 5: Panda Penetrometer test undertaken in till

602 Figure 6: Results of cone resistance tests using the Panda2 instrument at the Grangehall Ditch
603 glaciofluvial site (site 11 on Figure 1) and the Ardersier Silt Race Track site (Site 15 on Figure 1).

604 Figure 7: Example plots of water depth in the Guelph Permeameter reservoir with time used to
605 determine the steady intake rate of water, with the resulting hydraulic conductivity values (K).

606 Repeated measurements (A and B) within the same deposit at the same site show largely consistent
607 results.

608 Figure 8: Comparison of duplicate hydraulic conductivity measurements (A and B) taken in the same
609 material at the same section, generally sampled within 5 m of each other.

610 Figure 9: Box plot of hydraulic conductivity (one value per site) for superficial deposits in Morayshire.
611 The number of sites where hydraulic conductivity was measured is shown in brackets. (Glaciofluvial
612 material includes both fluvial and lacustrine deposits).

613 Figure 10: Particle Size Distribution envelopes for each superficial deposit type.

614 Figure 11: Relationship between *predicted* hydraulic conductivity (using d_{10} and Cone Resistance
615 (CR)) and *measured* hydraulic conductivity (K) for 27 sites in heterogeneous superficial deposits in
616 Morayshire.

617 Figure 12: Relationship between hydraulic conductivity, d_{10} and soil state descriptor as observed in
618 the field.

619 Figure 13: Box plots of hydraulic conductivity plotted for particle size of the largest fraction in each
620 sample. Note that this has much less predictive power ($R^2 = 0.16$) than using d_{10} and CR ($R^2 = 0.8$).

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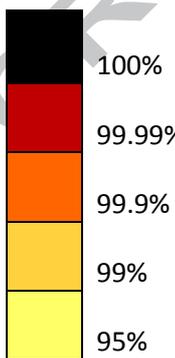
Table 1: Results

Locality (and site number on Fig. 1)	Lithology	Strength description	<i>In situ</i> k (m/day)	<i>In situ</i> Cone Resistance (Mpa)	d ₁₀	d ₆₀	Material Description
Rivermeads (1)	Glacial Till	Dense	0.102	6.2	0.0060	0.5894	Gravelly (f-c) very silty SAND (f-m) with some COBBLES
Rivermeads (1)	Glaciofluvial	Loose	1.04	2.32	0.0019	0.1700	Gravelly (f-m) very silty SAND (f-m)
Highland Boath (2)	Glacial Moraine	Very Loose	26.8		0.4104	16.8732	SAND (f-c) and GRAVEL (m-c) with some cobbles
Riereach Burn Site 1 (3)	Glacial Till	Very Dense	0.01	10.555	0.0011	0.7693	Very clayey very gravelly (f-c) SAND (f-c)
Riereach Burn Site 1 (3)	Glacial Till	Very Dense	0.051	9.52	0.0096	1.3623	Silty very gravelly (f-c) SAND (f-c)
Riereach Burn Sand Pit (4)	Glaciofluvial	Loose	31.1	3.61	0.1863	0.5880	N/A
Drynachan (5)	Glacial Till	Dense	1.3	6.21	0.0186	0.3025	Gravelly (f-m) very silty SAND (f-m)
Drynachan (5)	Glacial Till	Dense	0.054	7.52			Gravelly (f-m) very silty SAND (f-m)
Drynachan (5)	Glacial Till	Very Dense	0.015	12.63	0.0106	0.3534	Gravelly (f-m) very silty SAND (f-c)
Riereach Burn Site 2 (6)	Glacial Till	Dense - Very Dense	0.12	9.99	0.0024	0.7711	Very silty very gravelly (f-c) SAND (f-c)
Dunearn (7)	Glaciolacustrine	Firm	0.042	9.08	0.0010	0.0083	Slightly clayey SILT
Dunearn (7)	Glaciolacustrine	Loose	2.51		0.0232	0.1383	Silty SAND (f)
Dunearn (7)	Glaciolacustrine	Loose	30.2		0.2581	0.5153	SAND (m-c)
Easterton (8)	Glacial Till	Loose - Med. Dense	0.151	2.84	0.0038	0.2498	Gravelly (f-c) very silty SAND (f-m) with some cobbles
Findhorn Raised Marine (9)	Raised Marine	Medium Dense	3.2	12.545	0.1759	16.6746	SAND (f-m) and GRAVEL (m-c)
Findhorn Raised Marine (9)	Raised Marine	Very Loose	4.97	1.11	0.1355	0.2045	SAND (f-m)
Chapleton Mountain Bike (10)	Glaciofluvial	Medium Dense	1.77	7.575	0.2653	11.3743	Very sandy (f-c) GRAVEL (f-c) with a little cobbles
Grange Hall Ditch (11)	Glaciofluvial	Loose	0.432	3.22			Gravelly SAND (not fully recorded)
Grange Hall Ditch (11)	Glaciofluvial	Loose	0.048	1.595	0.0025	0.3045	Silty gravelly (f-c) SAND (f-m)
Findhorn Blown Sand (12)	Blown Sand	Very Loose	8.55	0.75	0.1339	0.2043	SAND (f-m)
Findhorn Blown Sand 2 (13)	Blown Sand	Very Loose	9.46	0.65			SAND (f-m)
Ardersier Silt (14)	Raised Marine	Soft - Firm	0.575	2.98	0.0015	0.0279	Slightly sandy slightly clayey SILT
Ardersier Silt Race Track (15)	Raised Marine	Very Loose	2.33	4.98	0.0388	0.1780	Silty SAND (f-m)
Dunearn Pit (16)	Glaciofluvial	Loose	8.06	1.48	0.1113	0.2039	SAND (f-m)
Dunearn Pit (16)	Glaciofluvial	Dense	5.53		0.7146	33.7607	Very sandy (m-c) GRAVEL (f-c) with some cobbles
Riereach Road Moraine (17)	Glacial Moraine	Very Loose	>40	2.6	0.6856	6.0503	Very sandy (m-c) GRAVEL (f-c)
Riereach Road Moraine (17)	Glacial Moraine	Loose - Med. Dense	0.147	13.68	0.1175	12.1595	Silty very gravelly (c) SAND (f-c)
Culbin Forest (18)	Blown Sand	Very Loose	4.41	0.99	0.1491	0.2207	SAND (f-m)
Grange Hill (19)	Glacial Till	Dense - Very Dense	0.027	3.33	0.0010	0.2077	Gravelly (f-m) very silty SAND (f-m)
Cloddymoss (20)	Glacial Till	Dense	0.0012	9.8	0.0019	0.2935	Gravelly (f-c) very silty SAND (f-c)
Cloddymoss (20)	Raised Marine	Stiff	0.013	2.695	0.0010	0.0176	Slightly sandy (f) slightly clayey SILT
Cothall (21)	Glaciofluvial	Loose	4.93		0.1727	0.4087	Slightly gravelly (f) slightly silty SAND (m)
Cothall (21)	Glacial Till	Firm - Stiff	0.006	11.87	0.0010	0.2175	Slightly gravelly (f-m) slightly clayey sandy (f-c) SILT
Croft Road Wood (22)	Raised Marine	Loose	1.1	3.74	0.0289	0.1619	Slightly clayey silty SAND (f-m)
Altyre Estate Site No. 3 (23)	Glacial Till	Very Dense	0.004				Slightly silty gravelly (f-c) SAND (f-c)
Altyre Estate Site No. 1 (24)	Glacial Till	Dense	0.004		0.0051	0.5129	Very silty very gravelly (f-c) SAND (f-m)
Wind Farm (25)	Raised Marine	Loose	2.94	1.46	0.1365	0.2106	SAND (f-m)
Wind Farm (25)	Raised Marine	Loose	1.04		0.2457	22.2066	Very sandy (m) GRAVEL (m-c)

Table 2: Pearson correlation matrix for *in situ* hydraulic conductivity and engineering parameters for 27 samples in Morayshire

	Cone Resistance	Soil State Description	Log d ₁₀	Log d ₁₅	Log d ₃₀	Log d ₆₀	Log K
Cone Resistance	1.00	0.64	-0.21	-0.23	-0.05	0.42	-0.53
Soil State Description	0.64	1.00	-0.60	-0.59	-0.34	0.04	-0.74
Log d ₁₀	-0.21	-0.60	1.00	0.94	0.78	0.56	0.83
Log d ₁₅	-0.23	-0.59	0.94	1.00	0.87	0.62	0.78
Log d ₃₀	-0.05	-0.34	0.78	0.87	1.00	0.82	0.61
Log d ₆₀	0.42	0.04	0.56	0.62	0.82	1.00	0.25
Log K	-0.53	-0.74	0.83	0.78	0.61	0.25	1.00

Significance level



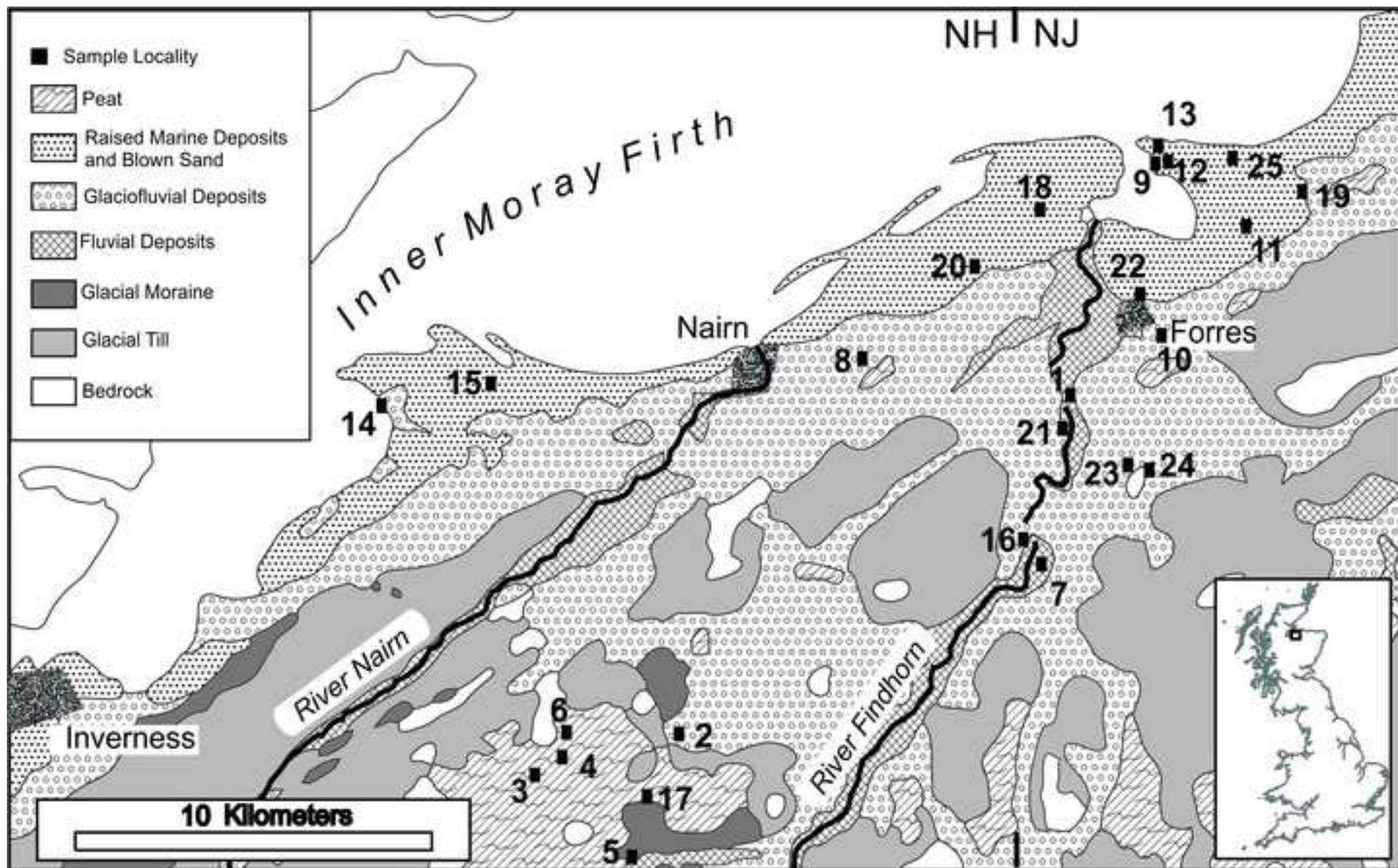
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99.99%
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95%

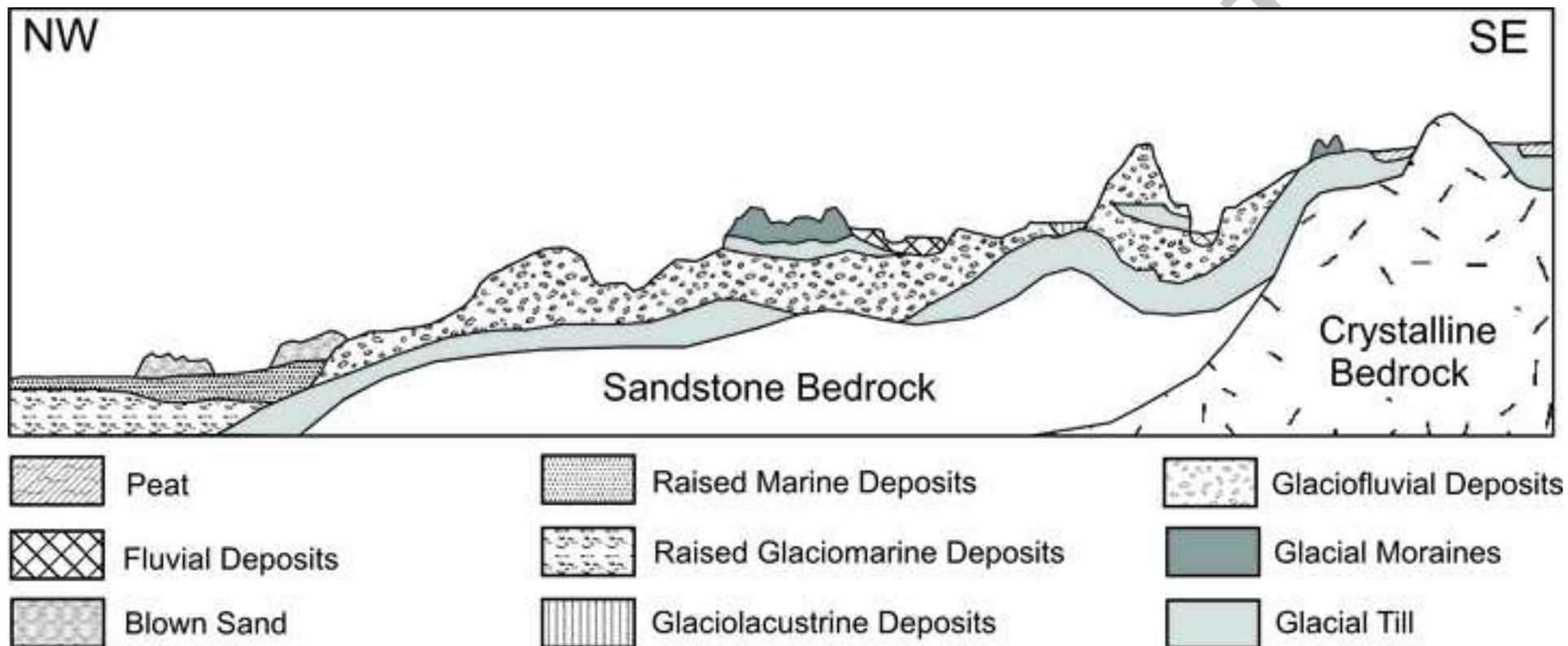
Table 3: P values for multiple linear regression analysis of the Morayshire dataset for log K and various material properties. The sign indicates whether the predictor is directly (+) or inversely (-) related.

Source	Value	Standard error	t	Pr > t
logd10	1.123	0.349	3.216	0.004
Cone Res (MPa)	-0.096	0.046	-2.091	0.049
logd15	-0.313	0.519	-0.602	0.553
logd30	0.456	0.630	0.723	0.478
logd60	-0.235	0.430	-0.547	0.590

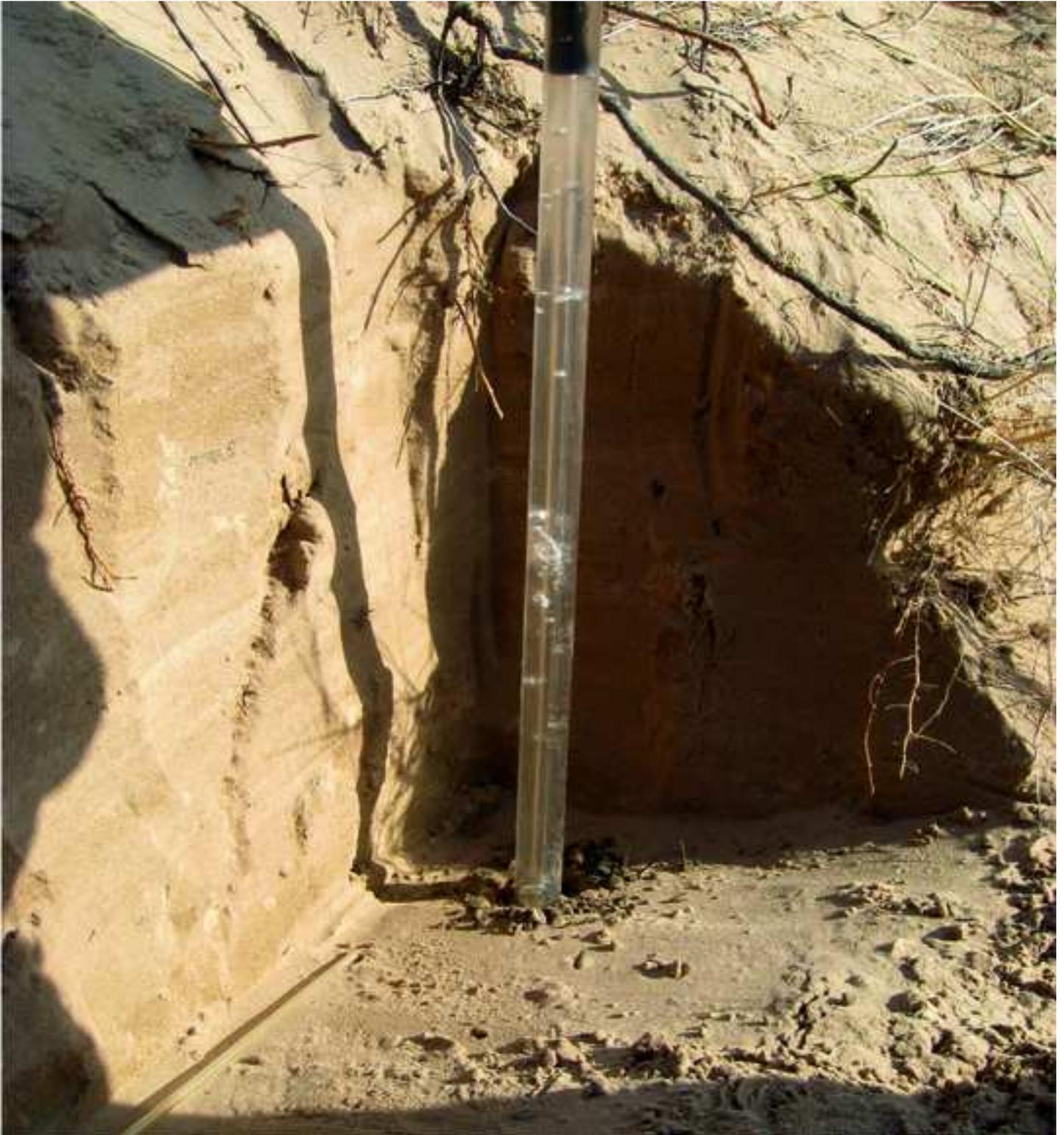
Bold are those significant at the 95% level

Figure 1

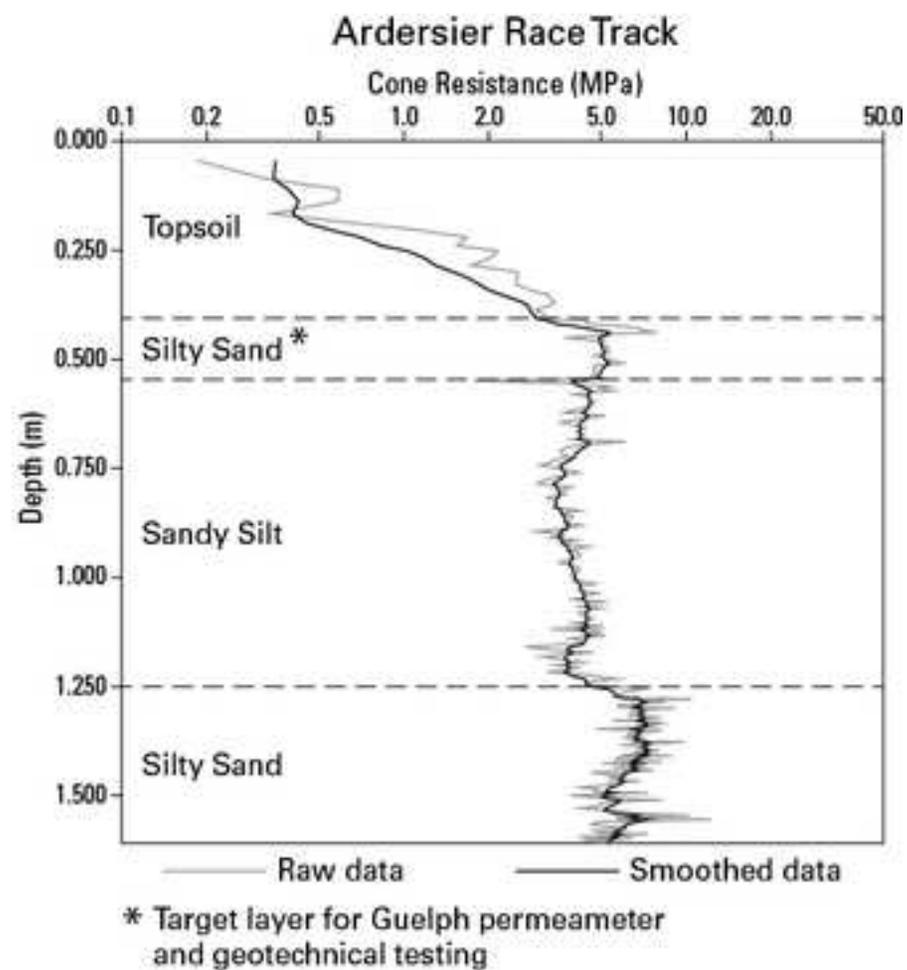
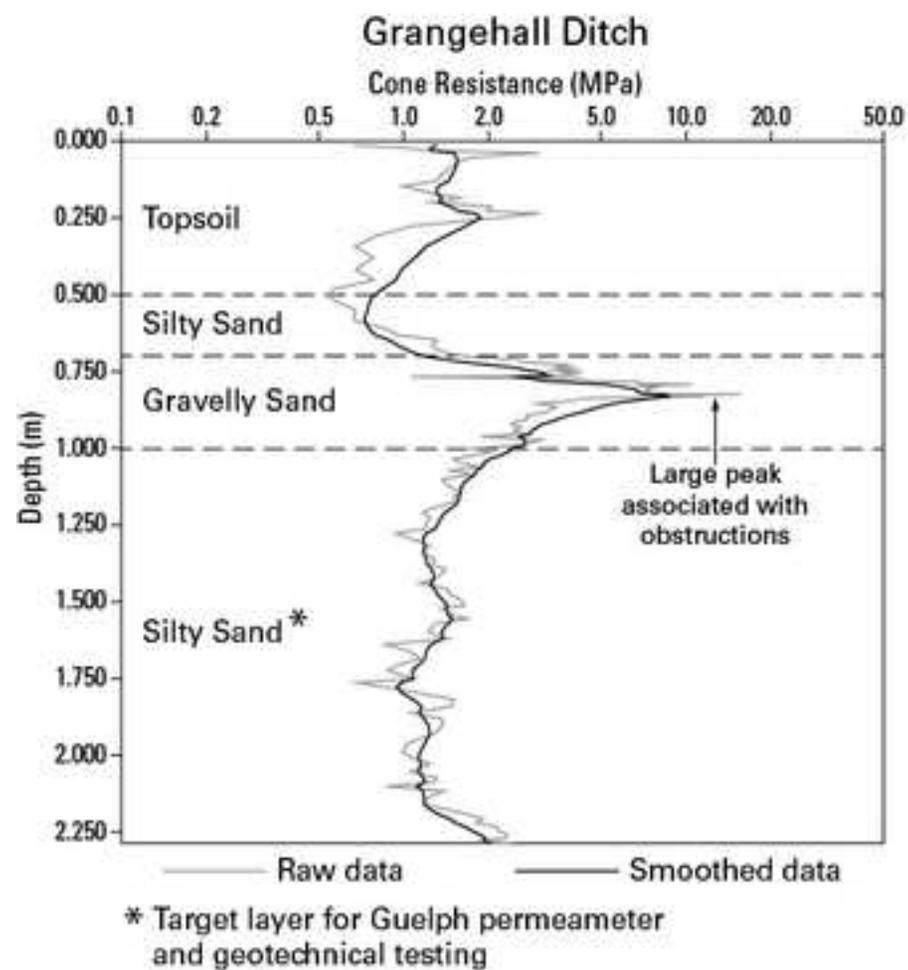




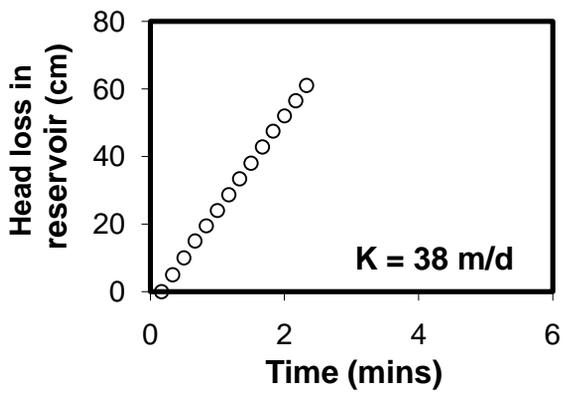




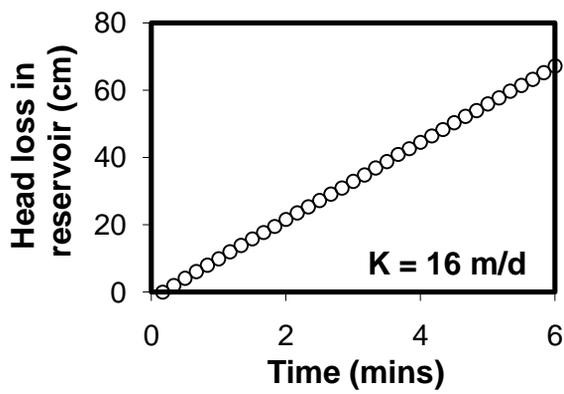




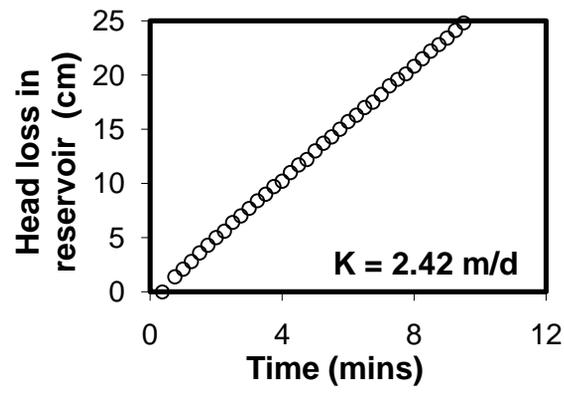
Highland Boath Moraine 1



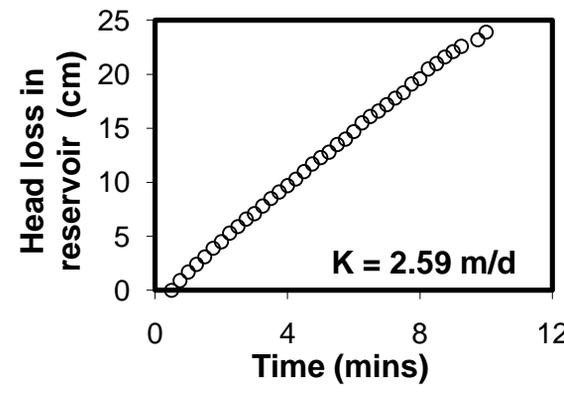
Highland Boath Moraine 2



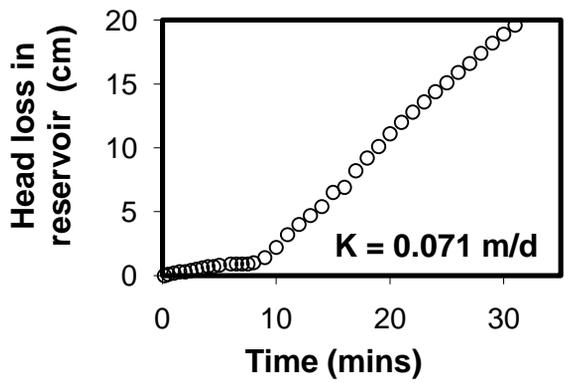
Dunearn Fine-Medium Sand 1



Dunearn Fine-Medium Sand 2



Grange Hill Red Till 1



Grange Hill Red Till 2

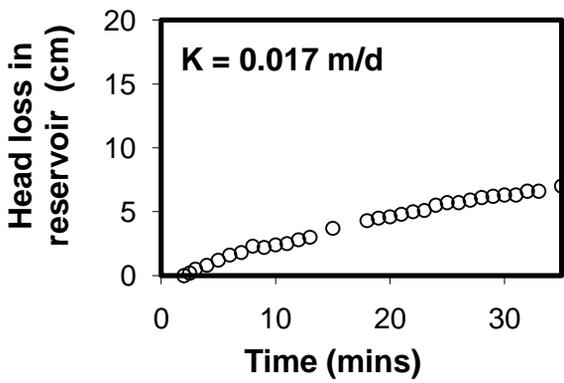
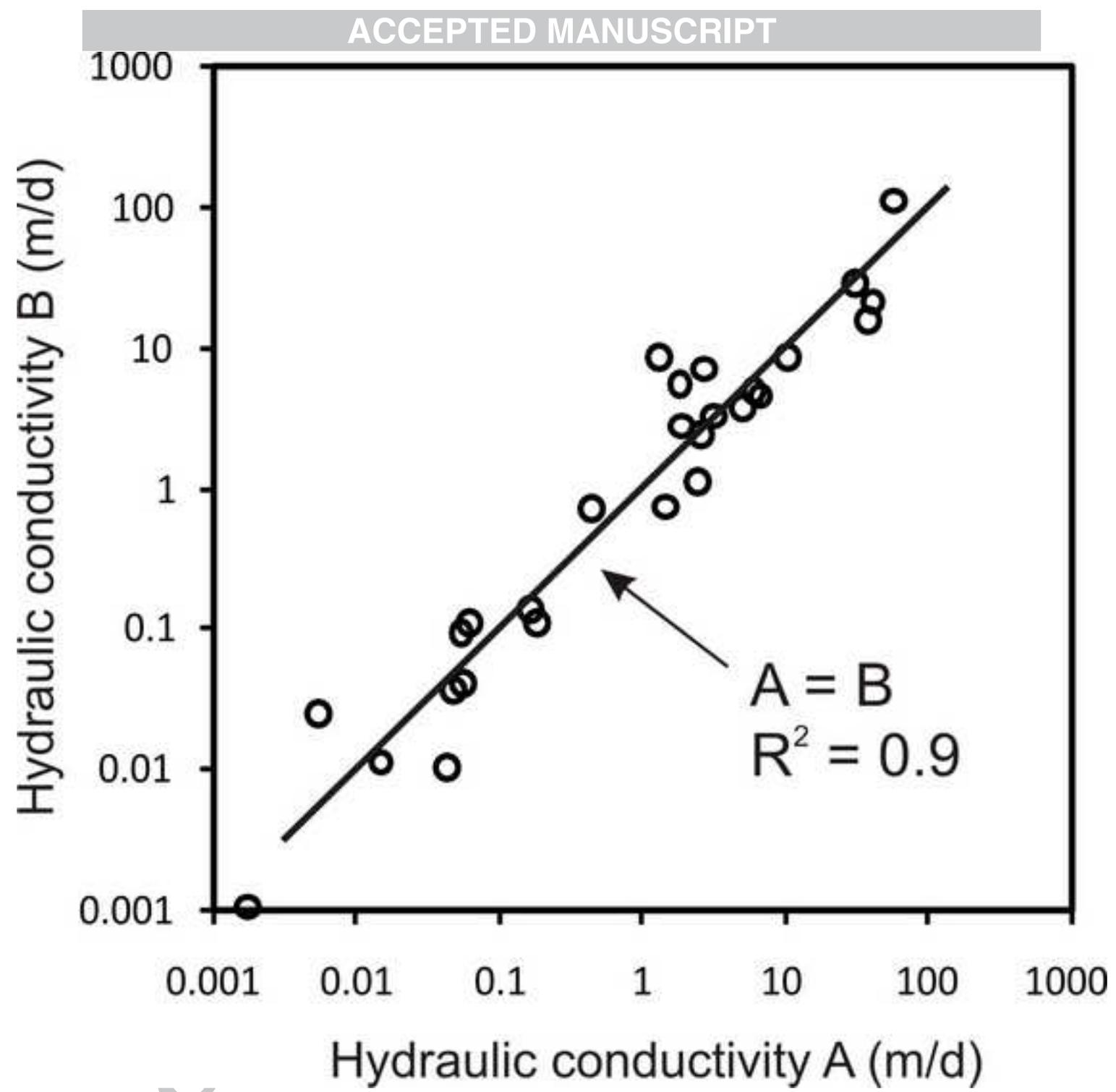
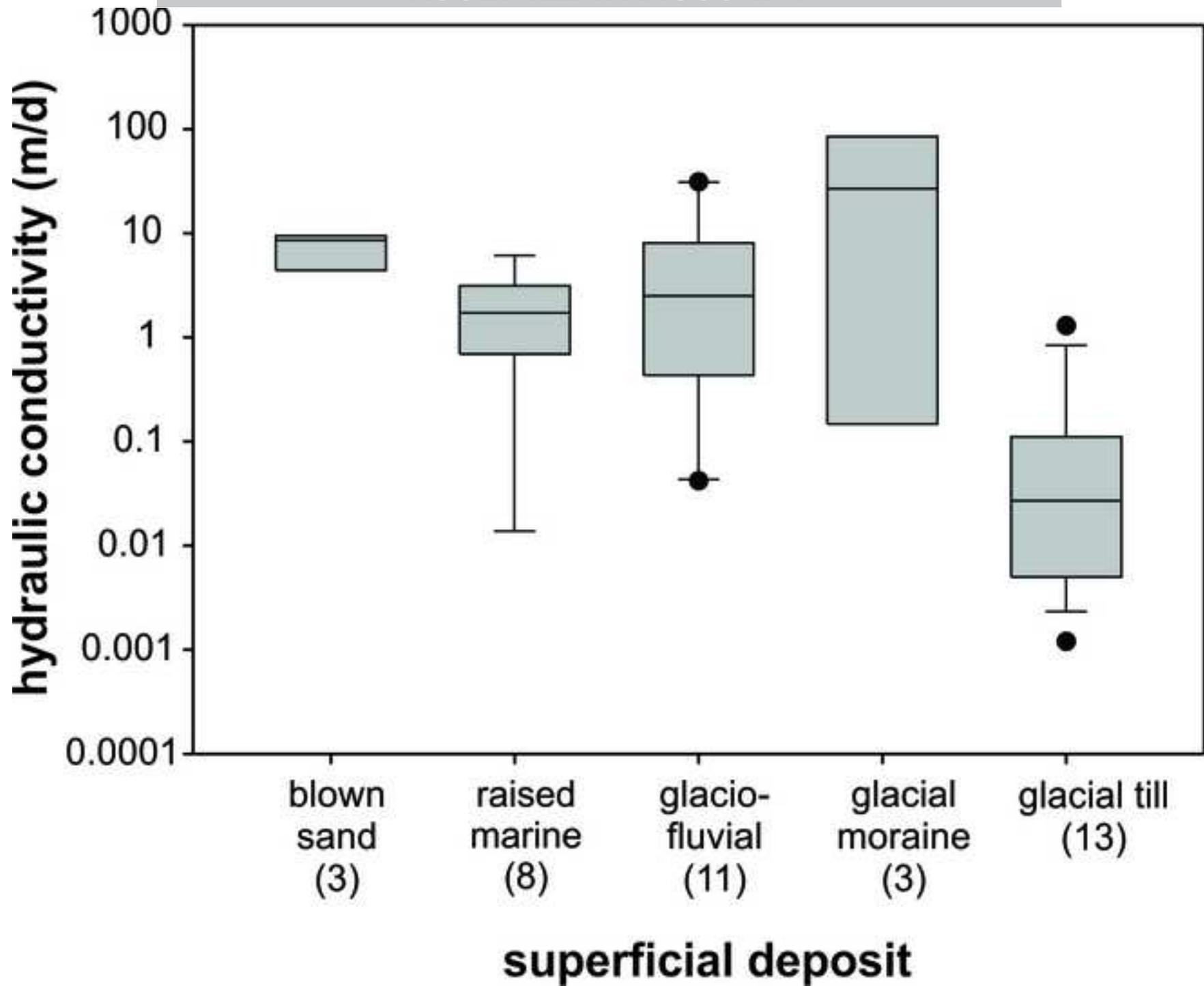


Figure8





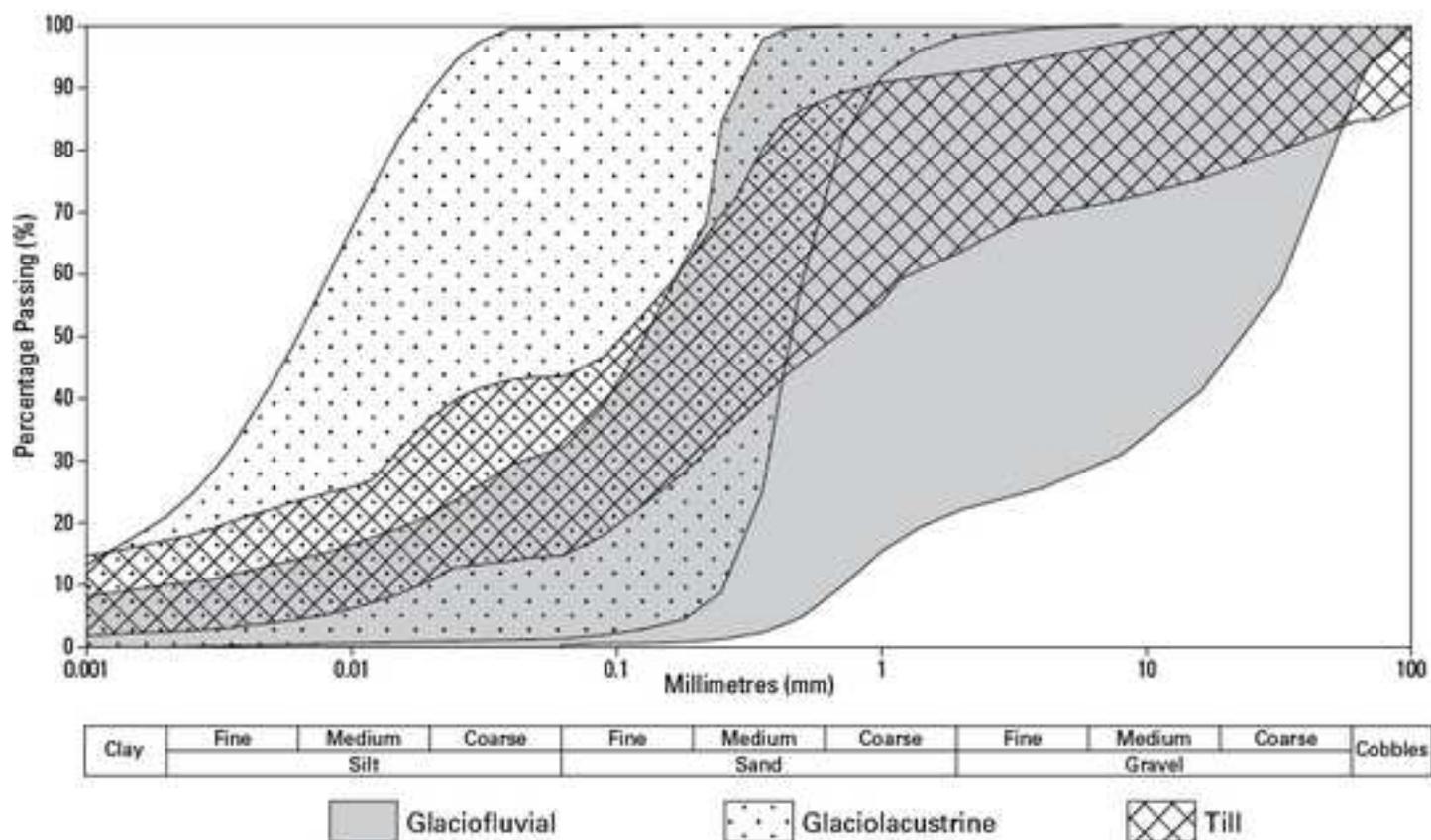
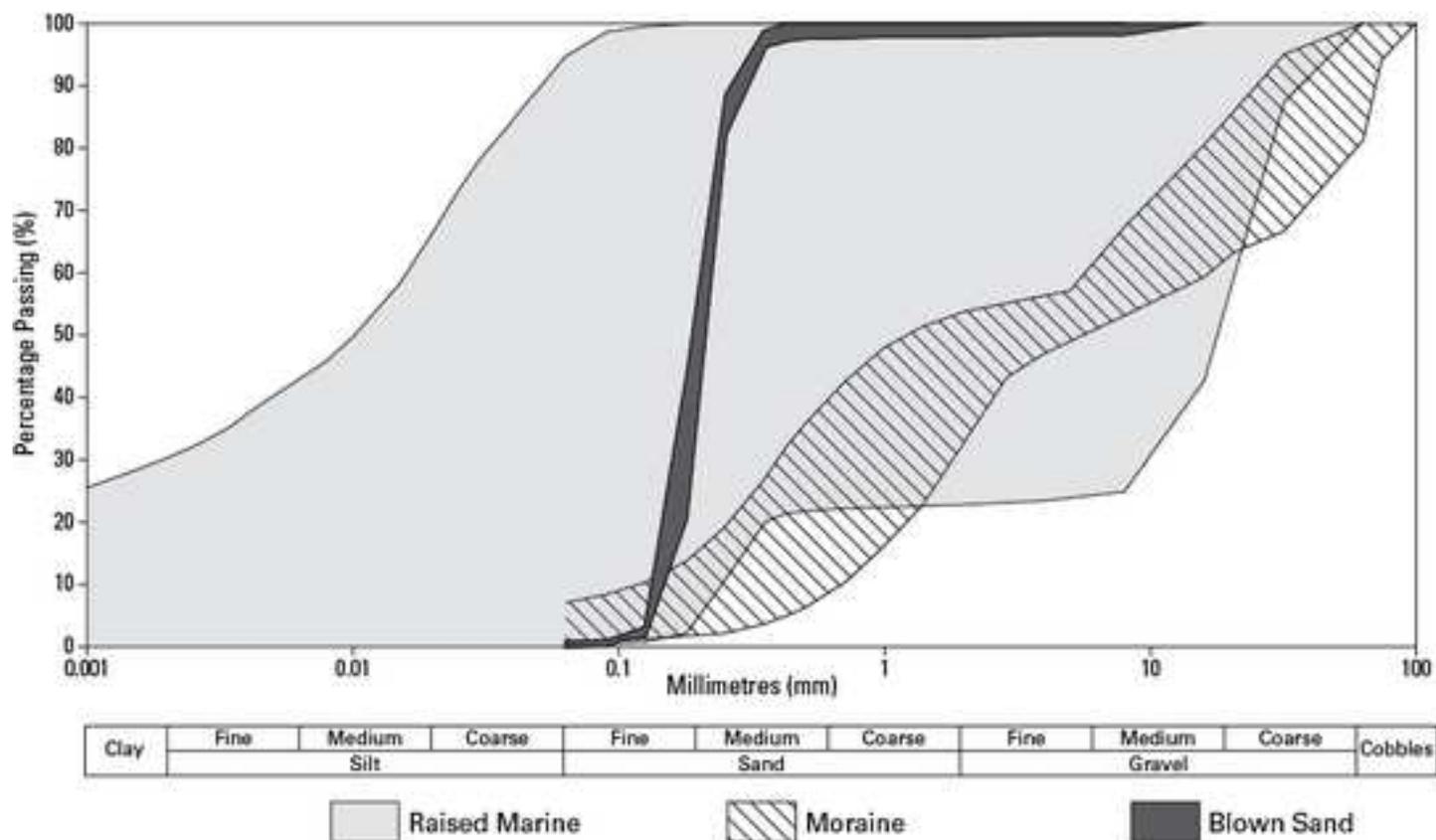
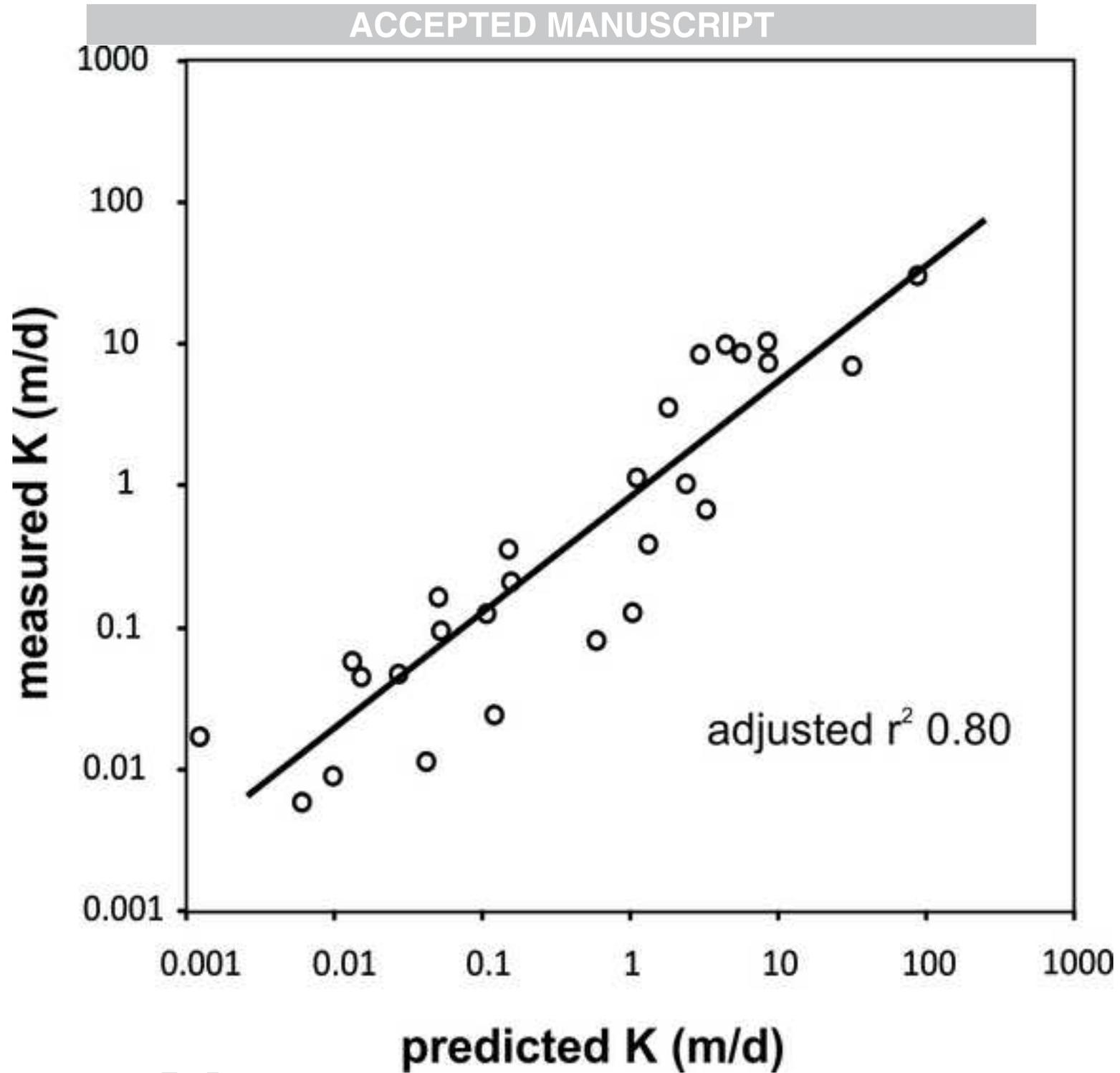
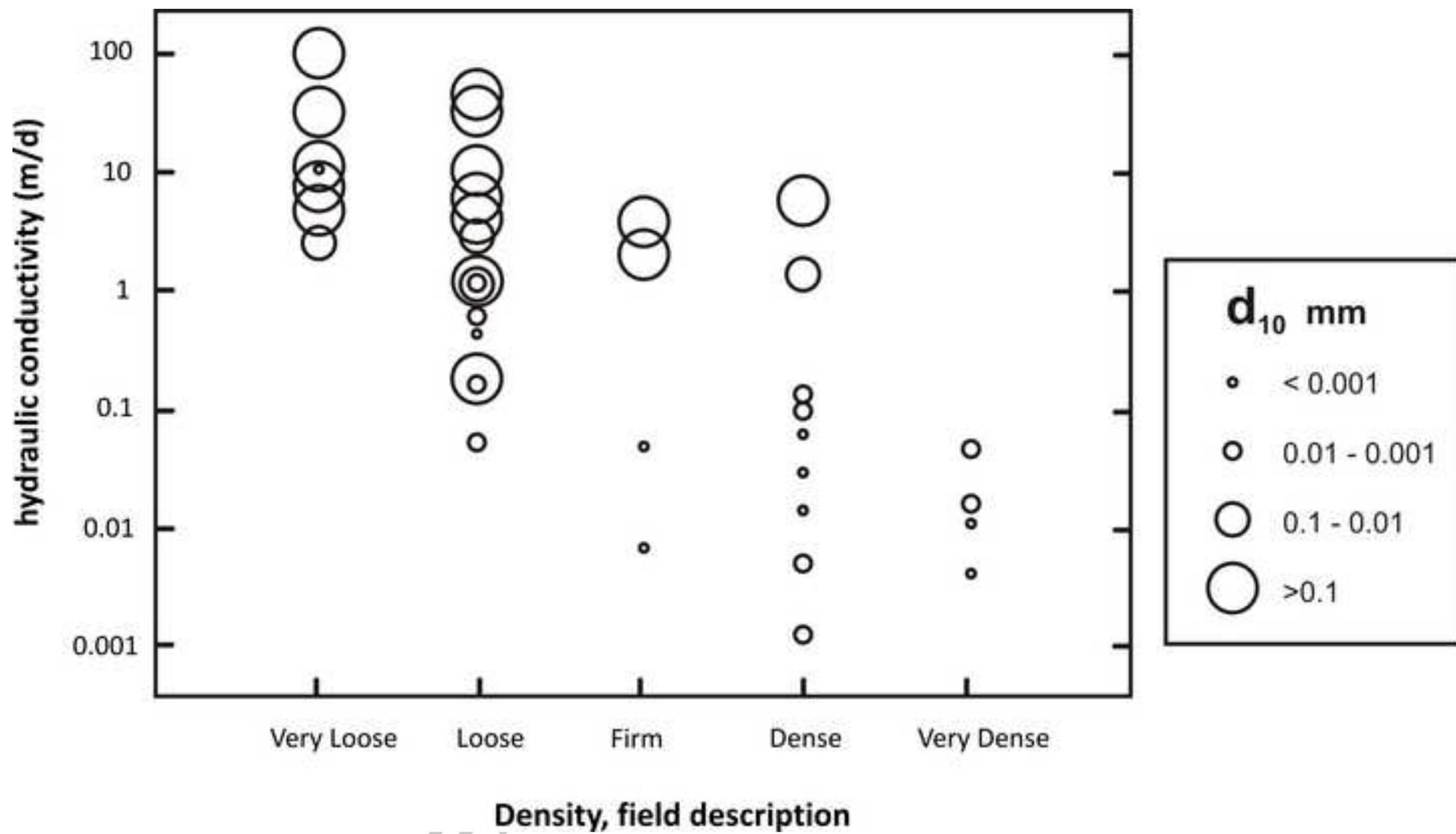
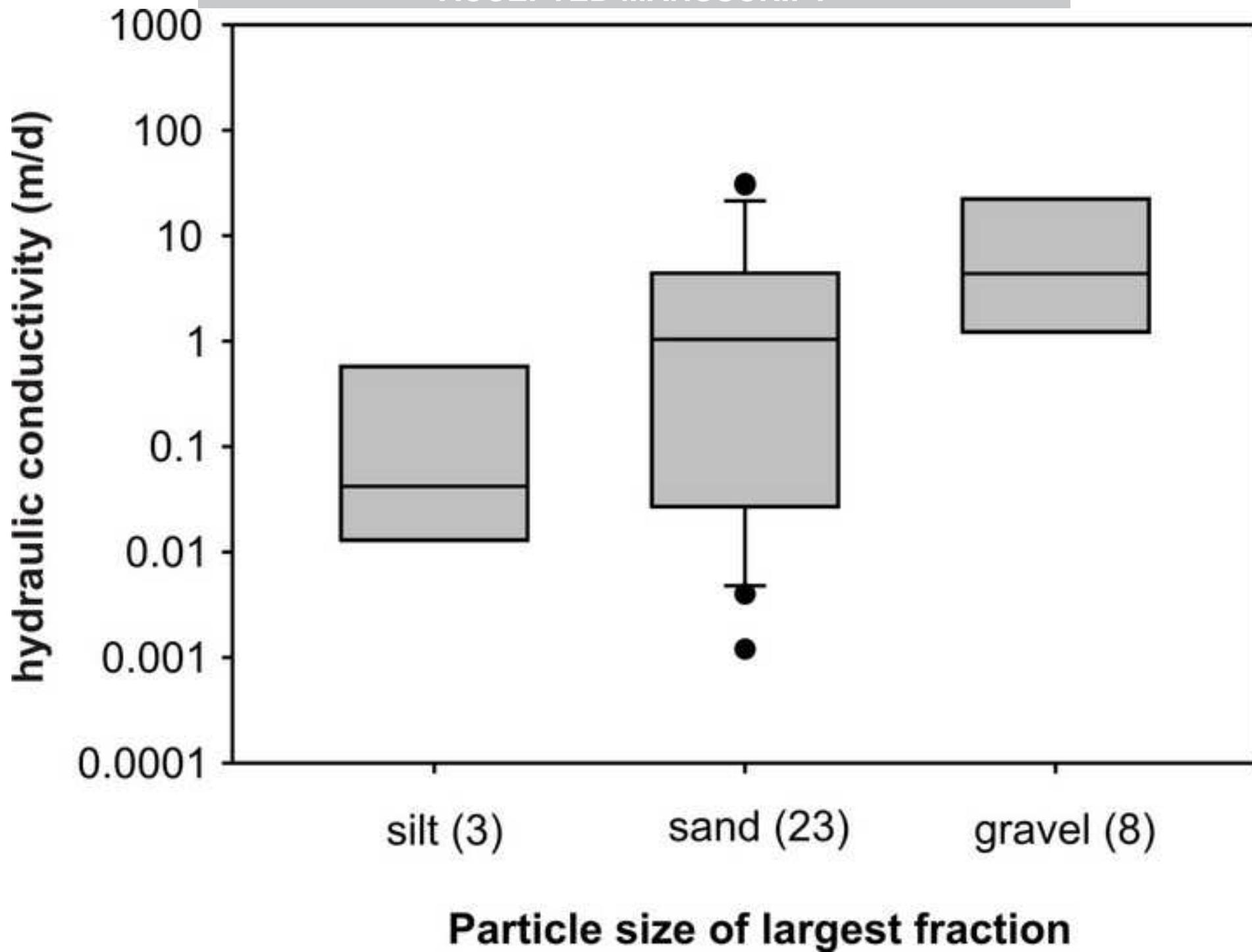


Figure11







Highlights

We examine the permeability of superficial deposits in a heterogeneous catchment

K ranges from 0.001 to > 40 m/d, highest in glacial moraine, lowest in till

MLR showed that K was related to $\log d_{10}$ and relative density with r^2 of 0.80

Material description of largest fraction had little predictive power of K

ACCEPTED MANUSCRIPT