Importance of plasma injection events for energization of relativistic electrons in the Jovian magnetosphere

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[1] Effects of density decrease in plasma injection regions and a latitude-dependent wave normal angle distribution on the energization of electrons by whistler mode waves at Jupiter are investigated. Previous work showed that whistler mode waves could enhance the fluxes of a few MeV electrons by an order of magnitude on a time scale of 30 days. However, density decrease in plasma injection regions and latitude dependence of the wave normal angle distribution of waves were not considered. Because this information is difficult to obtain from available observations, we perform a sensitivity study to demonstrate that the effect of density decrease on energization of electrons becomes important when the density inside injection regions is reduced to 25% of that outside. We also investigate the effect of a latitude-dependent wave normal angle distribution on energization of electrons using a ray tracing program and demonstrate that a realistic latitude-dependent wave normal angle distribution increases the rate of pitch angle diffusion near the loss cone, and thus enhances the loss rate, of 1–3 MeV electrons. However, the flux of 10 MeV electrons is not significantly affected. Results of the work are useful for understanding energization of MeV electrons at Jupiter, especially when combined with observations from future missions.


1. Introduction

[2] Resonant interactions between electrons and whistler mode waves play a controlling role on terrestrial radiation belt dynamics [Kennel and Petschek, 1966; Lyons and Thorne, 1973; Summers et al., 1998; Horne and Thorne, 1998; Horne et al., 2005b]. The resonant interactions occur when the Doppler-shifted wave frequency felt by an electron is equal to a multiple of electron’s cyclotron frequency [e.g., Stix, 1992]. These interactions have been shown to be responsible for the energization of relativistic electrons in the outer radiation belt after a geomagnetic storm [Horne et al., 2005b; Shprits et al., 2006], and the refilling of the electron slot between the inner and outer radiation belts [Thorne et al., 2007].

[3] Strong whistler mode waves have also been observed at Jupiter [Gurnett et al., 1996; Thorne et al., 1997; Bolton et al., 1997; Xiao et al., 2003]. Recently, Horne et al. [2008] demonstrated that interactions between electrons and whistler mode waves in the Jovian magnetosphere cause significant acceleration of MeV electrons on a time scale of 30 days. Using wave power spectral density from Galileo measurements, Horne et al. [2008] calculated quasi-linear pitch angle and energy diffusion coefficients and solved a two dimensional diffusion equation at 10 RJ. They showed that fluxes of 1–6 MeV electrons increased by more than an order of magnitude within 30 days.

[4] In the calculation of Horne et al. [2008], an empirical electron density model was used in calculation of diffusion coefficients. The empirical electron density model, however, does not consider the observed density decrease within plasma injection regions. Jupiter’s magnetosphere, similar to Saturn’s magnetosphere, is dominated by the centrifugal force because of its rapid rotation. Inward transport of hot and tenuous plasma and outward transport of cold and dense plasma has been proposed theoretically as a result of the centrifugal force dominated convection and an internal plasma source [Hill, 1976; Hill et al., 1981]. Inside local plasma injection regions, electron density is typically smaller than the average ambient density by more than a factor of two, as argued by Thorne et al. [1997] and Kivelson et al. [1997]. Similar density cavities have been observed by Cassini at Saturn [e.g., Menietti et al., 2008b; Rymer et al., 2009]. A
A decrease in electron density has been shown to favor local stochastic energization [Horne et al., 2003]. Consequently taking the density decrease inside injection regions into consideration would be important to quantify the energization time scale.

The wave normal angle distribution of chorus wave power is another important factor that is hard to determine from observation, but is required in the calculation of the diffusion coefficients. Horne et al. [2008] assumed that the wave power peaks around wave normal angle $\psi = 0^\circ$, based on previous studies on terrestrial whistler mode chorus waves [Horne et al., 2005a; Li et al., 2007]. However, several ray tracing studies and observations have shown that whistler waves tend to become more oblique at higher latitudes even when starting parallel from the equator [Bortnik et al., 2008; Li et al., 2008, 2009; Haque et al., 2010]. Since the wave power might not always peak around $\psi = 0^\circ$, we will analyze the effect of a different wave normal angle distribution of whistler wave power on our results.

In this work, we follow the modeling of Horne et al. [2008], but also take into consideration cross diffusion terms $D_{\psi\phi}$ which have been shown to be important for quantifying wave particle interactions in the terrestrial magnetosphere [Albert and Young, 2005; Tao et al., 2008, 2009; Xiao et al., 2009]. The sensitivity of the main conclusions of Horne et al. [2008] to the amount of density decrease inside the local plasma injection regions is analyzed in section 3.2. A ray tracing code HOTRAY [Horne, 1989] is then used to trace several whistler wave rays from the equator to higher latitudes to investigate change of their wave normal angle. The results are used to construct a latitude-dependent wave normal angle distribution model, which is then used to calculate quasi-linear diffusion coefficients. The effect of the latitude-dependent wave normal

Figure 1. Average whistler mode wave intensities measured by Galileo as a function of (a) radial distance, (b) magnetic latitude, and (c) local time. (d) The Galileo orbits are plotted together with color-coded whistler mode wave intensities (power flux).
Figure 2. Bounce-averaged diffusion rates ($d^{-1}$) obtained using a density model outside injection regions assuming that the wave normal angle distribution is centered around 0°. (bottom right) The sign of $D_{\alpha\rho}$.

Figure 3. Same as Figure 2 but for $D_{\rho\rho}$ (the plasma density is assumed to be half of that used in calculating $D_{\alpha\rho}$).
angle distribution on electron flux evolution is described in section 3.3. Finally, we summarize our work in section 4.

2. Observed Wave Power Distribution and Quasi-Linear Diffusion Coefficients

[7] We use a survey of all wave data recorded by the Galileo Plasma Wave Subsystem (PWS) instrument [Gurnett et al., 1992] from 27 June 1996 to 5 November 2002. The wave power distribution of whistler mode waves in Jupiter’s inner magnetosphere is shown in Figure 1, as a function of magnetic latitude or local time at 10 R\(_J\), or radial distance. Also shown in Figure 1d is the wave power flux plotted together with Galileo orbits. It is seen from Figure 1 that strong waves are detected between 6 R\(_J\) and 18 R\(_J\), peaking between 8 R\(_J\) and 10 R\(_J\). The whistler wave power peaks between 2° and 4° in latitude, and decreases by an order of magnitude at the highest latitude (∼12°) sampled by Galileo. The wave power flux distribution also shows a day-night asymmetry and is slightly stronger in the dayside near local noon. A more detailed analysis of whistler mode chorus waves observed by Galileo could be found in work by Menietti et al. [2008a].

[8] As argued by Horne et al. [2008], the preferred location for strong electron energization is outside the Io torus, where the electron density is low and wave activity is strong. The ratio of electron plasma frequency to cyclotron frequency \(\omega_{pe}/\omega_{ce}\) is about 5 at 10 R\(_J\). Also due to the strong centrifugal force, plasma is confined to the centrifugal equator, thus \(\omega_{pe}/\omega_{ce}\) falls to a relatively low value at higher latitudes. We follow Horne et al. [2008] and use a plasma density model by Bagenal [1994] for the electron density distribution along a magnetic field line outside injection events at Jupiter. Because there are insufficient measure-

Figure 4. Electron fluxes (color coded) at (left) 0 days, (middle) 15 days, and (right) 30 days as a function of \(\alpha\) and \(E\) for (a) \(D_\alpha\), (b) \(0.9D_\alpha + 0.1D_{hd}\), (c) \(0.7D_\alpha + 0.3D_{hd}\) and (d) \(0.5D_\alpha + 0.5D_{hd}\).
ments of electron density inside plasma injection regions, we will assume the electron density inside injection regions to be either half or one quarter of the electron density outside injection events to test the sensitivity of our results to the density decrease in injection regions.

To calculate quasi-linear diffusion coefficients, we assume the wave power to be Gaussian in frequency [Glaeuer and Horne, 2005]. Horne et al. [2008] showed that chorus is strongest near 0.1 ~ 0.2ωce. We follow Horne et al. [2008] and assume that the wave power peaks at 0.15ωce with a width of 0.05ωce. The wave normal angle distribution in \( \chi \equiv \tan \psi \) is assumed to be Gaussian, similar to chorus waves at Earth, with a width \( \chi = \tan 30^\circ \). The wave power is first assumed to be centered at \( \chi = 0^\circ \), but we also investigate effects of a latitude-dependent wave normal angle distribution on electron energization in section 3.3. Using the Full Diffusion Code [Shprits and Ni, 2009; Ni et al., 2008], we first calculate the diffusion coefficients outside injection events (hereafter denoted as \( D_o \)) as shown in Figure 2.

3. Evolution of Electron Phase Space Densities

3.1. Description of the Numerical Model

A 2-D bounce-averaged diffusion equation is used to model the evolution of electron phase space density (\( f \)) as a function of equatorial pitch angle (\( \alpha \)) and momentum (\( p \)):

\[
\frac{\partial f}{\partial t} = \frac{1}{Gp} \frac{\partial}{\partial \chi} G \left( D_{oo} - \frac{1}{p} \frac{\partial f}{\partial \chi} + D_{op} \frac{\partial f}{\partial p} \right) + \frac{1}{G} \frac{\partial}{\partial p} \left( D_{op} - \frac{1}{p} \frac{\partial f}{\partial \chi} + D_{pp} \frac{\partial f}{\partial p} \right),
\]

Figure 5. Line plots of electron fluxes of (top) 1 MeV, (middle) 3 MeV, and (bottom) 10 MeV at (left) 15 days and (right) 30 days due to different combinations of \( D_o \) and \( D_{ud} \) indicated by different colors. Initial conditions are shown by dashed lines.
where $D_{aa}$, $D_{ap}$ and $D_{pp}$ are bounce-averaged pitch angle, mixed and momentum diffusion coefficients. Here $G$ is a Jacobian factor, $G = p^2 T(a) \sin(a) \cos(a)$, and $T(a) \approx 1.30 - 0.56 \sin(a)$ is the normalized bounce period. In work by Horne et al. [2008], the equation is solved without mixed terms $D_{ap}$. However, the importance of $D_{ap}$ has been shown by previous work and several methods have also been proposed to solve equation (1) [Albert and Young, 2005; Tao et al., 2008, 2009; Xiao et al., 2009]. In this work, we use the numerical method of Albert and Young [2005] to solve equation (1) with $D_{ap}$ included.

The initial and boundary conditions are chosen to be the same as those of Horne et al. [2008]. To minimize effects of wave particle interactions in the initial distribution at 10 RJ, the average electron flux from Pioneer and Voyager data at 15.75 RJ is used to calculate the initial electron flux at 10 RJ, assuming a dipole magnetic field and loss-free inward radial diffusion to 10 RJ. The electron flux is then converted to phase space density using $f = j/p^2$. We fix phase space density at the lower energy boundary at $E = 300$ keV and set $f = 0$ at $E = 100$ MeV. We also assume that electrons scattered into the loss cone ($\alpha_{LC} = 1.5^\circ$) precipitate into the Jovian atmosphere within a quarter of the bounce time. At $\alpha = 90^\circ$, we assume $\partial f/\partial \alpha = 0$.

### 3.2. Sensitivity to Density Decrease During Local Plasma Injection Regions

Within plasma injection regions, the total plasma density is decreased by at least a factor of two, as inferred from enhancement of magnetic field inside the injection region and the requirement of the total pressure balance [Thorne et al., 1997; Kivelson et al., 1997]. A decrease in total electron density will affect both the resonance energy of electrons and the pitch angle and energy diffusion coefficients. A smaller electron density will result in larger wave phase speed and correspondingly will enhance energy diffusion. Thus including density decrease in the modeling may be important to calculate the time scale of electron energization.

However, as far as we are aware, there is no density model for plasma injection regions and no direct measurement of the fraction ($\chi_i$) of plasma injection regions in terms of local time. To investigate the effects of local plasma injections on the average rate of energization of electrons by whistler mode waves, we assume different values for $\chi_i$ and average densities $\rho_i$ of plasma injection regions. The drift-averaged diffusion coefficient used in equation (1) is $D = \chi_i D_i + (1 - \chi_i) D_o$, where $D_i$ is the diffusion coefficient inside an injection region.

#### 3.2.1. Case 1: $\rho_i = (1/2)\rho_o$

We calculate the diffusion coefficients using the wave model described in section 2 but with the electron density $\rho_i$ half of that outside ($\rho_o$) and three values for $\chi_i$. The resulting diffusion coefficient $D_i = D_{id}$ is shown in Figure 3. The evolution of electron fluxes is shown in Figure 4 with Figure 4a showing the results of using the diffusion coefficient $D_i$ discussed in section 2, and Figures 4b–4d exhibiting changes due to the increasing probability of observing an injection event. Corresponding line plots of fluxes of 1 MeV, 3 MeV, and 10 MeV electrons are shown in Figure 5, which indicated that increasing $\chi_i$ will increase fluxes at 3 MeV and 10 MeV electrons, mainly because of the increase of energy diffusion. However, fluxes at 1 MeV at larger pitch angles are slightly reduced because of the
increased pitch angle diffusion near loss cone. Overall, when \( \rho_i = (1/2)\rho_o \), including density decrease inside injection regions will slightly decrease fluxes of 1 MeV electrons at higher pitch angles and increase fluxes at 3 MeV and 10 MeV electrons by a factor of 1.5. Consequently the density decrease inside injection regions in the case of \( \rho_i = (1/2)\rho_o \) does not seem to significantly affect the time scale of energization.

3.2.2. Case 2: \( \rho_i = (1/4)\rho_o \)

For the case of \( \rho_i = (1/4)\rho_o \), the diffusion coefficient \( D_\rho = D_{qd} \) is presented in Figure 6, which shows both higher energy and pitch angle diffusion coefficients at higher energies (\( E > 1 \) MeV), compared with Figure 2. The evolution of 2-D electron fluxes due to different \( \chi_i \) with \( D_{qd} \) is shown in Figure 7, and the line plots of fluxes at 1 MeV, 3 MeV and 10 MeV are shown in Figure 8. Significant effects of including \( D_{qd} \) occur even when \( \chi_i = 0.1 \), where the electron flux at 10 MeV is increased due to increased energy diffusion, while that at 1 MeV is decreased due to increased pitch angle diffusion near the loss cone. When \( i_i \) is increased to 0.5, the electron flux at 10 MeV around 55° is increased by a factor of 5 at \( t = 30 \) days, and the electron flux at 1 MeV is decreased by a factor of 3 for pitch angles larger than about 20°. Overall, a density decrease by a factor of 4 inside injection regions would appear to have an important effect on the time scale of electron energization.

3.3. Effects of a Latitude-Dependent Wave Normal Angle Distribution

The wave normal distribution of chorus waves was assumed to be centered around 0° [e.g., Horne et al., 2008] in the above wave model used to calculate \( D_{\rho} \). However, several ray tracing studies [Bortnik et al., 2008; Li et al.,

Figure 7. Same as Figure 4 but due to combinations of \( D_\rho \) and \( D_{qd} \).
2008] have shown that the wave normal angle of an initially parallel propagating ray normally increases during its propagation away from the equator. Here, we use a ray tracing code HOTRAY [Horne, 1989] to show the propagation of whistler mode waves in the Jovian magnetosphere and subsequently take the effects of the latitude-dependent wave normal angle distribution into account in the calculation of quasi-linear diffusion coefficients.

The HOTRAY code was developed by Horne [1989] to trace electromagnetic and electrostatic waves in a hot magnetized plasma. We use HOTRAY code to trace rays of whistler mode chorus waves of several frequencies, starting with \( \psi = 0^\circ \) from the equatorial plane at \( L = 10 \). The resulting variation of the wave normal angle with respect to latitude \( \lambda \) is shown in Figure 9, which shows that from \( \lambda = 0^\circ \) to \( 10^\circ \), the wave normal angles of all rays \( (f = 0.05f_{ce} \) to \( 0.25f_{ce} \) change from \( 0^\circ \) to about \( 40^\circ \). Consequently, we use a latitude-dependent wave normal distribution in the calculation of diffusion coefficients based on the ray tracing result \( (\psi_c = 0.36 + 5.04\lambda - 0.06\lambda^2 \) and \( \chi_c = \tan(\psi_c) \)). Other parameters of the wave model are the same as the one described in section 2. The resulting diffusion coefficient \( D_{\psi_c(\lambda)} \) is shown in Figure 10. The evolution of electron fluxes calculated using \( D_{\psi_c(\lambda)} \) at 1 MeV, 3 MeV, and 10 MeV is shown in Figure 11, compared with that due to \( D_o \). The fluxes of 10 MeV electrons calculated using \( D_{\psi_c(\lambda)} \) and \( D_o \) are almost the same. However, the pitch angle diffusion at lower pitch angles near the loss cone is increased when using \( D_{\psi_c(\lambda)} \), resulting in more losses of 1 MeV and 3 MeV electrons and a decrease in their fluxes.

4. Discussion and Summary

[18] We used a wave power distribution obtained from a survey of Galileo PWS wave records between 27 June 1996 and 5 November 2002 to investigate the effects of density...
decrease in injection regions and a latitude-dependent wave normal angle distribution of whistler mode waves on energization of electrons. We assumed two different average densities ($\rho_i$) of the injection regions and we demonstrated that if $\rho_i$ is half of the density outside ($\rho_o$), the effects of density decrease on the time scale of electron energization are negligible. However, if $\rho_i$ is a quarter of $\rho_o$, the effect of density decrease on the time scale of energization of higher-energy (10 MeV) electrons is important when the fraction ($\chi_i$) of plasma injection regions in local time is larger than 0.3. Also, including the injection regions will also enhance pitch angle diffusion of lower energy (1 MeV and 3 MeV) electrons near loss cone, thus reducing their fluxes. One thing that is missing from our model is the enhancement of whistler mode wave activity during plasma injection regions, which will be left to future work.

[19] The effect of a latitude-dependent wave normal angle distribution of whistler waves on evolution of electron phase space density was also investigated with the aid of a ray tracing code HOTRAY. We showed that rays of whistler waves initially parallel to local magnetic field have a wave normal angle of about 40° when reaching 10° in latitude. The latitude-dependent wave normal angle distribution has no obvious effect on 10 MeV electron fluxes. However, it increases pitch angle diffusion of 1 MeV and 3 MeV electrons near the loss cone and reduces their fluxes by about a factor of 3. Thus the change of wave normal angle of chorus waves during propagation should be taken into account when quantitatively modeling electron flux evolution of Jovian electrons.

[20] Other parameters that are potentially important but not discussed in this study are, e.g., initial conditions [Xiao et al., 2010], the width of the frequency and wave normal angle distributions. We used initial conditions calculated from observations, but it might also be possible to use kappa-type distributions [Xiao et al., 2008], which have been shown to fit very well with observed electron distributions at Earth. Investigating the importance of these parameters are left to future work. Overall, better information of these parameters might be provided by future missions to Jupiter, and the results of this work should be useful to understand relativistic electron dynamics at Jupiter when combined with more observations.

Figure 9. Evolution of the wave normal angle ($\psi$) of rays at different frequencies, indicated by different colors, as a function of latitude. The black dashed line is $\psi = -0.36 + 5.04\lambda - 0.06\lambda^2$.

Figure 10. Same as Figure 2 but for $D_{\psi}(\lambda)$ (the wave normal angle distribution is latitude dependent).
Figure 11. Evolution of electron fluxes at 15 and 30 days using $D_o$ (blue) and $D_{v_i}(\lambda)$ (red) for (top) 1 MeV, (middle) 3 MeV, and (bottom) 10 MeV.
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