

1 **Ray tracing of penetrating chorus and its**  
2 **implications for the radiation belts**

J. Bortnik, R. M. Thorne

3 Department of Atmospheric and Oceanic Sciences, University of California,  
4 Los Angeles, California, USA.

N. P. Meredith

5 British Antarctic Survey, Natural Environment Research Council,  
6 Cambridge, UK.

O. Santolik

7 Faculty of Mathematics and Physics, Charles University, Prague and  
8 IAP/ASCR, Prague, Czech Republic.

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J. Bortnik, and R. M. Thorne, Department of Atmospheric and Oceanic Sciences, University of California, Los Angeles, CA 90095-1565, USA. (jbortnik@gmail.com, rmt@atmos.ucla.edu)

N. P. Meredith, British Antarctic Survey, Natural Environment Research Council, Madingley Road, Cambridge, CB3 0ET, UK. (nmer@bas.ac.uk)

O. Santolik, Faculty of Mathematics and Physics, Charles University, Prague and IAP/ASCR, Prague, Czech Republic. (ondrej.santolik@mff.cuni.cz)

9 Using ray tracing and suprathermal electron distributions from CRRES,  
10 the final propagation latitudes of typical chorus rays are calculated as a func-  
11 tion of  $L$ , MLT, AE, and initial wave normal angle. Rays initiated within  
12 a certain range of wave normals  $\psi_P \sim -0.8\psi_G$  to  $-0.6\psi_G$  (where  $\psi_G$  is  
13 the Gendrin angle) propagate to very high latitudes, largely avoiding Lan-  
14 dau damping whilst remaining roughly field-aligned for large portions of their  
15 propagation paths. The relative wave power of such penetrating chorus may  
16 increase above its initial value due to the low damping rates and magnetic  
17 field line convergence. By considering 4 representative rays with  $f = 0.3f_{ce}$ ,  
18 and calculating the resonant energies at the edge of the loss-cone, it is shown  
19 that penetrating chorus readily interacts with electrons in the  $> 1$  MeV  
20 energy range, and may thus contribute to the previously reported relativis-  
21 tic electron microbursts.

## 1. Introduction

22 Chorus waves are intense, naturally-generated electromagnetic emissions, typically oc-  
23 ccurring outside the plasmopause, in the magnetic local time (MLT) range  $\sim 23 - 15$ h,  
24 with frequencies of  $\sim 0.1 - 10$  kHz [*Meredith et al.*, 2001; *Santolik et al.*, 2004]. Interest in  
25 chorus has recently increased due to the recognition of this wave's importance in control-  
26 ling radiation-belt dynamics [e.g., *Horne and Thorne*, 2003; *Horne et al.*, 2005; *Thorne et*  
27 *al.* 2005; *Meredith et al.*, 2002]. Chorus can act as a mediating agent, transferring energy  
28 from the lower energy ( $\sim 10 - 100$  keV) electrons which are predominantly precipitated,  
29 to the relativistic ( $\sim 1$  MeV) electrons which are predominantly accelerated [e.g. *Mered-*  
30 *ith et al.*, 2002; *Horne and Thorne*, 2003; *Horne et al.*, 2005]. Since the pitch-angle and  
31 energy diffusion rates used in studying radiation-belt dynamics are critically dependent  
32 on the chorus wave power distribution and wave normal characteristics, accurate knowl-  
33 edge of the propagation of chorus waves (power, damping, wave normal evolution, etc.)  
34 is essential for an accurate evaluation.

35 In the present paper, the effects of suprathermal electron fluxes (which lead to Landau  
36 damping) upon chorus propagation are examined using a combination of measured fluxes,  
37 and ray tracing. Section 2 summarizes our methodology, and Section 3 presents the  
38 results of ray tracing, investigating the dependence of chorus propagation on the initial  
39 wave normal angle. In Section 4 the ray tracing results are related to energetic electron  
40 scattering, and Section 5 summarizes our findings.

## 2. Methodology

41 The methodology used to investigate the propagation characteristics and damping of  
 42 chorus waves has been described in detail by *Bortnik et al.* [2007], and consists of 3 steps:

43 1. *Suprathermal electron distribution*: Suprathermal electron flux observations from  
 44 CRRES were used to create statistical distributions as a function of  $L$ -shell ( $L = 1$  to 7,  
 45 in  $0.1L$  bins), MLT (in 1 hour bins), and AE (in 3 bins: quiet AE  $< 100$  nT, moderate 100  
 46  $< AE < 300$  nT, and disturbed AE  $> 300$  nT), in 4 energy channels: 0.213, 1.09, 4.25,  
 47 and 16.5 keV. Only flux measurements outside the plasmopause were included consistent  
 48 with typical chorus wave location (see *Meredith et al.* [2004] for the sorting criterion).

49 2. *Parameter fitting*: For each  $L$ , MLT, and AE bin, the 4 flux values (i.e., the 4 energy  
 50 channels above) were fitted with an assumed (isotropic) phase space density function of  
 51 the form  $f(v) = A_N/v^n$ .

52 3. *Ray tracing and Landau damping*: The set of functions  $f(v)$  were used to calculate  
 53 the Landau damping rates [*Brinca, 1972*] of rays injected at the geomagnetic equator  
 54 [*Santolik et al., 2004*] from the appropriate ( $L$ , MLT) bin. The equatorial electron density  
 55 was modeled with a plasmopause located at  $L \sim 2.5$  (reflecting disturbed conditions,  
 56  $Kp_{\max} \sim 6.7$ ) after *Carpenter and Anderson* [1992], with off-equatorial density distributed  
 57 according to the diffusive equilibrium model [*Angerami and Thomas, 1964*], and a dipole  
 58 magnetic field. The Stanford VLF ray tracing program [*Inan and Bell, 1977*] was used  
 59 in the computation of the ray paths. Magnetic field line convergence is included by  
 60 multiplying the local power density by the ratio of azimuthal arc-lengths at the ray versus  
 61 the initial value,  $r_0 \cos(\lambda_0)/r \cos(\lambda)$ , where  $r$  and  $\lambda$  are the radial distance and latitude of  
 62 the ray and the subscript ‘0’ represents initial values.

63 A typical chorus ray path (see legend) is shown in Figure 1a. The fitted electron  
 64 distribution  $f(v)$  (at the chosen  $L$ -MLT location) was used to calculate the path-integrated  
 65 Landau damping, shown together with the ray latitude as a function of group time in  
 66 Figure 1b. We define the ray termination point when the ray power reaches 1% of its  
 67 initial value, which defines the ray lifetime ( $\tau_f$ ), final latitude ( $\lambda_f$ ), and final distance  
 68 ( $d_f$ ). The evolution of the wave normal angle  $\psi(\lambda)$  as a function of latitude is shown in  
 69 panel (c) indicating that even though the ray is injected with  $\psi_0 = 0^\circ$ , it quickly becomes  
 70 oblique leading to severe damping.

71 In the following section the effect of varying  $\psi_0$  upon  $\lambda_f$  is investigated. The angle  $\psi_0$   
 72 is normalized to the Gendrin angle  $\psi_G$  (the value of  $\psi$  at which the group vector becomes  
 73 field aligned, calculated using *Bortnik et al.* [2006a], Eq. (1)) and varied from (Earthward  
 74 directed)  $-1\psi_G$  to (antiEarthward directed)  $+1\psi_G$  in steps of  $0.2\psi_G$ . These  $\psi_0$  values,  
 75 their group rays, and the refractive index surface are shown in Figure 1d.

### 3. Results

76 A summary of final latitude  $\lambda_f(\text{MLT}, L)$  is shown in Figure 2, parameterized by geomag-  
 77 netic activity and  $\psi_0$ . Each ray is injected at  $\lambda = 0^\circ$ ,  $f = 0.3f_{ce}$ . The common colorbar  
 78 for  $\lambda_f$  is given at the bottom of the figure.

79 The principal properties of the chorus distribution are:

- 80 • The tendency of  $\lambda_f$  to decrease with increasing  $L$ , due to the lower ratio between  
 81 Landau resonant suprathermal particles and cold particles ( $n_h/n_0$ ).

82 • The effect of geomagnetic activity upon the MLT distribution of  $\lambda_f$ . As AE increases,  
 83 for a given  $L$ ,  $\lambda_f$  becomes progressively more asymmetric with MLT, with maximum  $\lambda_f$   
 84 on the day-side, consistent with observational results.

85 • The agreement of the observed statistical distribution of chorus wave power with  
 86 those rays originating at essentially field-aligned ( $\psi_0 = 0^\circ$ ) directions [*Bortnik et al.*,  
 87 2007].

88 Figure 2 shows that the Landau damping of chorus is strongly dependent upon  $\psi_0$ . For  
 89  $\psi_0 \geq 0^\circ$ , the degree of Landau damping increases and  $\lambda_f$  becomes progressively smaller  
 90 with increasing  $\psi_0$ . However, when  $\psi_0 \leq 0^\circ$ ,  $\lambda_f$  increases dramatically. At  $\psi_0 \sim -0.6\psi_G$ ,  
 91  $\lambda_f(L < 6) > 60^\circ$  and the wave penetrates to very low altitudes (henceforth referred to  
 92 as ‘penetrating chorus’). As  $\psi_0$  is decreased further,  $\lambda_f$  decreases, and at  $\psi_0 = -1\psi_G$   
 93 it is sensitively dependent upon  $f(v)$ , becoming either very large ( $\lambda_f > 60^\circ$ ) at low  $L$   
 94 and in some parts of the afternoon sector, or very short ( $\lambda_f < 10^\circ$ ) elsewhere, with few  
 95 intermediate values.

96 To examine the development of penetrating chorus, 4 rays are plotted in Figure 3.  
 97 Columns (A)-(D), correspond to rays injected at  $L = 4.45$ ,  $f = 0.3f_{ce}$ , MLT = 9.5 h, AE  
 98  $> 300$  nT, with  $\psi_0 = -1\psi_G$ ,  $-0.65\psi_G$ ,  $0.0\psi_G$ , and  $+0.5\psi_G$  respectively. The top row (a),  
 99 shows ray paths in red and wave normal vectors as short black line-segments attached  
 100 to the ray path. Rows (b) and (c) show the corresponding damping as a function of  
 101 group time, and  $\psi(\lambda)$  respectively. For  $\psi_0 = -\psi_G$  the initial damping is very severe,  
 102 and  $\lambda_f = 2.9^\circ$ . For  $\psi_0 = -0.65\psi_G$ , although the initial Landau damping is relatively  
 103 strong, it is substantially weaker than case (A), and avoids being extinguished close to

104 its origin. The wave normal becomes field-aligned near  $\lambda \sim 18^\circ$  (no Landau damping),  
 105 and the wave power subsequently increases due to field line convergence. In addition, the  
 106 ray propagates in such a way that  $\psi$  remains low and the wave can reach the ionosphere  
 107 approximately field-aligned. When  $\psi_0$  is increased further (columns (C),(D)),  $\psi(\lambda)$  quickly  
 108 rotates anti-Earthward as it propagates, resulting in severe damping and decreasing  $\lambda_f$ .

109 Our results indicate that waves injected over a limited range of  $\psi_0$  are able to avoid both  
 110 the initial intense Landau damping (c.f. column (A)), and the mid-latitude damping (c.f.  
 111 columns (C) and (D)). From column (B) and Figure 2, the range of penetrating chorus  
 112 initial angles is  $\psi_P \sim -0.8\psi_G$  to  $-0.6\psi_G$ . Moreover, the final wave normal angle  $\psi(\lambda_f)$   
 113 is sensitively dependent upon  $\psi_0$ . At some critical angle  $\psi_B$  (bifurcation angle [*Thorne*  
 114 *and Kennel*, 1967; *Chum and Santolik*, 2005]) within the  $\psi_P$  range,  $\psi(\lambda_f) \sim 0^\circ$  (also close  
 115 to local vertical at high latitudes) and the ray is able (in principle) to propagate through  
 116 the ionosphere to the ground. For  $\psi_0 < \psi_B$ ,  $\psi(\lambda_f)$  becomes very oblique in the negative  
 117 direction, whereas for  $\psi_0 > \psi_B$ ,  $\psi(\lambda_f)$  becomes very oblique in the positive direction.  
 118 This tendency of the rays to bifurcate at low altitudes based upon their initial  $\psi$  has been  
 119 reported previously [*Chum and Santolik*, 2005; *Santolik et al.*, 2006] and associated with  
 120 the possible formation of ELF hiss at high latitudes, but inclusion of Landau damping  
 121 with realistic suprathermal fluxes has not been considered until the present study.

122 Although the bulk of the chorus power corresponds to rays with  $\psi_0 \sim 0^\circ$  [*Bortnik et al.*,  
 123 2007], chorus is nevertheless routinely observed with high  $\psi$  at the source [*Hayakawa et*  
 124 *al.*, 1990] and on low altitude spacecraft (e.g., *Santolik et al.*, [2006]). An example from the  
 125 DEMETER satellite is shown in Figure 4, observed at an altitude of 709 km. Panels (a)-(d)

126 show the magnetic and electric power spectrograms, and  $\mathbf{k}$ -vector angles ( $\psi_{\text{BK}}$ , azimuth  
 127 angle relative to  $+\mathbf{B}$ ,  $\phi_{\text{BK}}$ , zenith angle measured anticlockwise relative to  $+\mathbf{B}$  with  $0^\circ$   
 128 pointing to higher  $L$ -shells). The chorus elements contain significant electromagnetic wave  
 129 power, have clearly propagated to much higher latitudes than typical chorus waves, and  
 130 have  $\psi_{\text{BK}} \sim 30^\circ$ , similar to the values obtained in Figure 2, column (B). The ray tracing  
 131 shown in the present paper, as well as previous studies [*Chum and Santolik, 2005*] confirms  
 132 that these waves are penetrating chorus.

#### 4. Implications for particle scattering

133 Figure 3 row (d) shows the resonant energies of electrons near the edge of the loss-cone  
 134 for each ray as a function of latitude [e.g., *Bortnik et al., 2006b*, Eq. (2)]. Included are co-  
 135 streaming cyclotron resonances  $m = -5$  to  $-1$  (red), the co-streaming Landau resonance  
 136  $m = 0$  (black), and counter-streaming resonances  $m = 1 - 5$  (blue). The dominant  $m = 1$   
 137 resonance is shown as the thick blue line in each of the plots.

138 To indicate regions of field-aligned propagation (and hence most efficient wave-particle  
 139 interaction), we chose an arbitrary limit of  $|\psi| = 30^\circ$ , and highlighted this region for  
 140 each ray in rows (c) and (d). As shown, penetrating chorus (B) readily resonates with  
 141 MeV electrons at  $\lambda \sim 30^\circ$  with  $\psi \leq 30^\circ$ , and may thus contribute to the formation of  
 142 relativistic electron microbursts [*Lorentzen et al., 2001*] which have been shown to be  
 143 an effective radiation-belt loss mechanism [*Thorne et al., 2005*]. We note that if the  
 144 wave frequency is decreased (not shown), a greater range of  $\psi_0$  will be able to access  
 145 high latitudes and scatter MeV electrons into the loss-cone, contributing to microburst

146 formation, but chorus wave power simultaneously decreases and essentially vanishes below  
 147  $f \sim 0.1f_{ce}$ .

## 5. Conclusions

148 Using ray tracing and suprathermal electron distributions from the CRRES satellite,  
 149 the final propagation latitudes  $\lambda_f$  of typical chorus rays have been calculated as a function  
 150 of  $L$ , MLT, AE, and  $\psi_0$ . While the bulk of chorus wave power was previously shown to be  
 151 consistent with rays injected at  $\psi_0 = 0^\circ$  [Bortnik et al., 2007], the present study shows that  
 152 rays initiated within a certain range of wave normals  $\psi_P \sim -0.8\psi_G$  to  $-0.6\psi_G$  are able  
 153 to propagate to very high latitudes and low altitudes (‘penetrating chorus’). Penetrating  
 154 chorus avoids the initial large damping associated with large oblique  $\psi$  by quickly rotating  
 155 towards  $\psi \sim 0^\circ$ , and also avoids the large damping at mid-latitudes associated with  $\psi$   
 156 rotating to oblique values. In addition, the relative wave power of penetrating chorus  
 157 may increase above its initial value due to magnetic field line convergence. An example of  
 158 chorus waves observed on the DEMETER satellite at an altitude of 709 km was presented,  
 159 consistent with penetrating chorus.

160 By considering 4 representative ray paths with  $f = 0.3f_{ce}$ , it was shown that penetrat-  
 161 ing chorus can resonate efficiently with electrons in the  $> 1$  MeV range, and may thus  
 162 contribute to the previously reported relativistic electron microbursts.

163 Finally, since penetrating chorus is able to propagate to low altitudes with  $\psi \sim 0^\circ$ ,  
 164 the chorus observed on the ground does not necessarily need to be guided in field-aligned  
 165 ducts, but can propagate entirely in an unducted mode. The bifurcation of wave normal  
 166 angles (and thus ray directions) at low altitudes may further lead to connections with

167 other waves types (e.g., ELF hiss) as suggested by *Parrot et al.*, 2004, *Chum and Santolik*  
168 [2005], and *Santolik et al.* [2006].

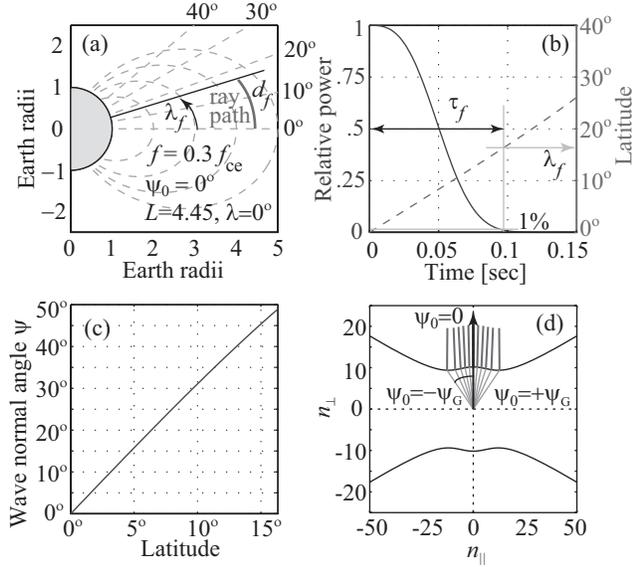
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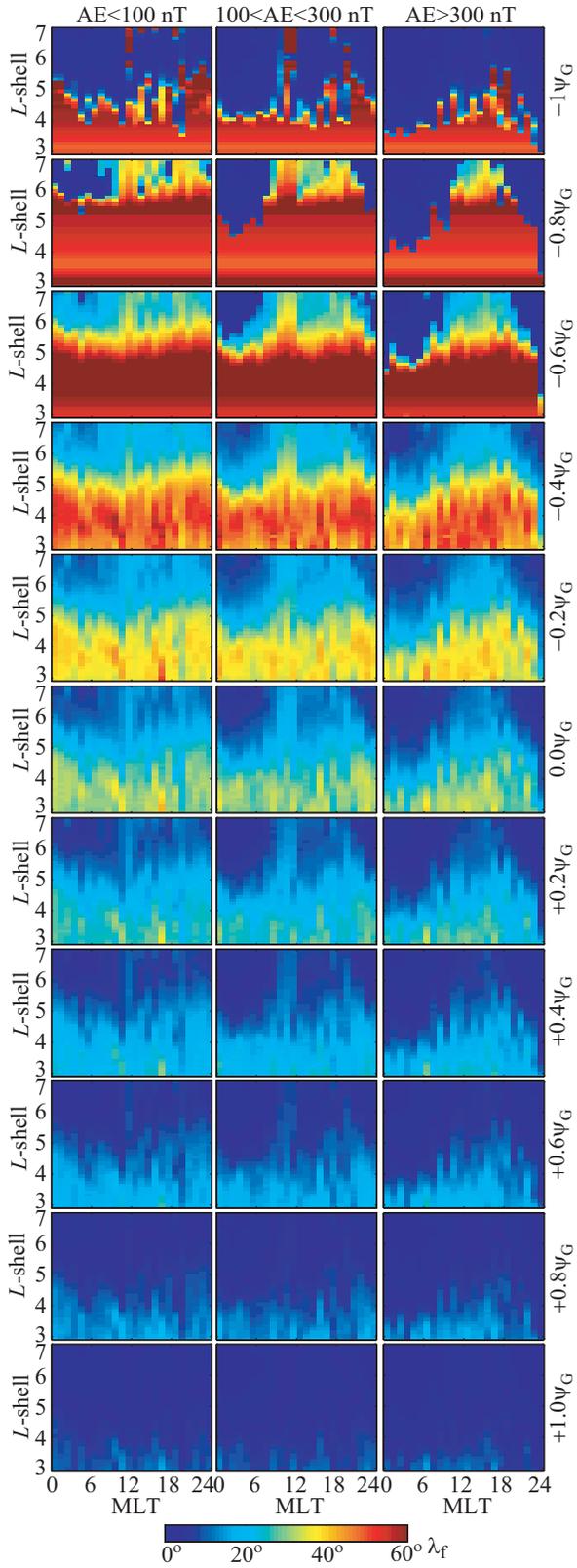
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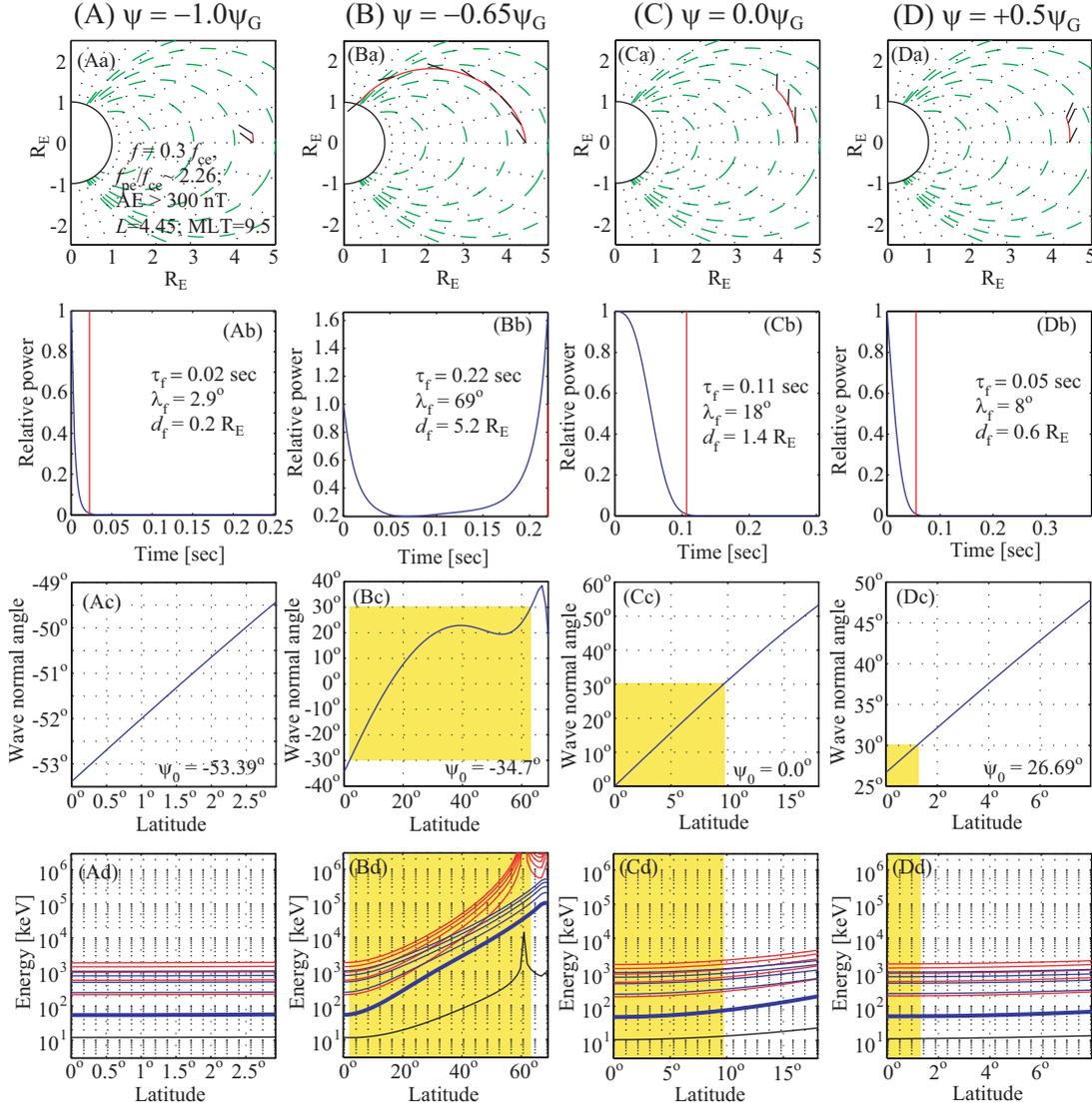
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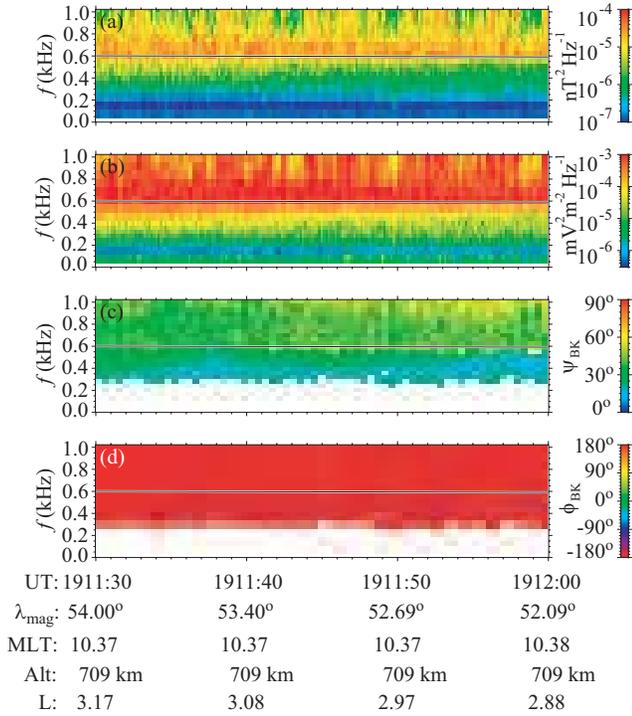
**Figure 1.** Illustration of ray propagation at  $L = 4.45$ ,  $MLT = 5.5$ ,  $\psi = 0^\circ$ ,  $f = 0.3f_{ce}$  and  $AE > 300$  nT. (a) ray path; (b) Relative wave power (solid line) and ray latitude (dashed line) vs. group time, showing the 1% power level which defines ray termination, giving  $\tau_f = 0.0971$  sec,  $\lambda_f = 16.34^\circ$ , and  $d_f = 1.28R_E$ ; (c)  $\psi(\lambda)$ ; and (d) refractive index surface  $n(\psi_0)$  showing  $\psi_0$  from  $-\psi_G$  to  $+\psi_G$ , in  $0.2\psi_G$  intervals. The wave normal and group vector in panels (a)-(c) is shown as the black line at  $\psi = 0^\circ$ .  $n_\parallel$  and  $n_\perp$  are the components of the refractive index parallel and perpendicular to the magnetic field, respectively.



**Figure 2.** Final propagation latitude  $\lambda_f(\text{MLT}, L)$ , parameterized by geomagnetic activity and  $\psi_0$ .



**Figure 3.** Individual ray characteristics. Columns (A)–(D) correspond to rays injected with  $\psi_0 = -1.0\psi_G$ ,  $-0.65\psi_G$ ,  $0.0\psi_G$ , and  $+0.5\psi_G$  respectively. Rows (a)–(d) correspond respectively to ray path, relative power of the ray vs. group time,  $\psi(\lambda)$ , and energies of resonant electrons, showing  $m < 0$  (red),  $m = 0$  (black), and  $m > 0$  (blue) resonance harmonics, with the dominant  $m = 1$  resonance indicated with a thick blue line.



**Figure 4.** Dynamic spectrogram of chorus elements observed on the DEMETER satellite. (a) wave magnetic field, (b) wave electric field, (c) zenith angle relative to  $+\mathbf{B}$ , and (d) azimuth angle measured anticlockwise about  $+\mathbf{B}$ , with  $\phi_{\text{BK}} = 0^\circ$  pointing to higher  $L$ -shells. The black line represents the value of the local proton gyrofrequency for reference.