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4 OCEANOGRAPHIC CURRENTS AND THE CONVEXITY  
5 OF THE UPPERMOST CONTINENTAL SLOPE

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## ABSTRACT

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2       Immediately below the shelf edge where sea-level lay during the Last Glacial  
3 Maximum (LGM), the uppermost continental slope in many areas has a smooth,  
4 convex-upwards rounded shape in profile. This shape is an example of a clinoform  
5 "rollover", a sedimentary feature that arises in general terms from how declining  
6 "energy" with water depth allows sediments to steepen. Computer models using the  
7 diffusion transport equation with mobility  $K$  declining with depth can produce rollover  
8 shapes, but the models have yet to be properly justified and the controls on  $K$  have been  
9 unclear. In this contribution, aspects of morphologic datasets from the USA and Iberian  
10 Atlantic margins are shown to be indeed compatible with the diffusion model. From  
11 experiments and theory, the gravity effect on saltating particles leads to a downslope  
12 flux that is proportional to local bed gradient, as required by the diffusion model, if the  
13 bed is agitated by oscillating currents of small residual current, by contour-parallel  
14 currents, or by a combination of both. The predicted mobility  $K$  is then an increasing  
15 function of the current's average speed. Near-bottom current-meter data reveal how  
16 currents, enhanced around the shelf edge, decline with water depth in a way that is  
17 generally compatible with the rollover morphology. During the LGM, bed currents due  
18 to tides and surface waves were stronger than at present. Although difficult to predict,  
19 they are expected to produce a more sharply declining mobility with depth that would  
20 be compatible with the limited depth range below the shelf edge over which sand and  
21 gravel have deposited.

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## 1. INTRODUCTION

1           The shelf edge or break was defined originally in terms of the increase in  
2 gradient associated with it. For example, Heezen et al. (1959) mentioned that "The  
3 continental shelf ... extends from the shore line to the shelf break where the seaward  
4 gradient sharply increases to greater than 1:40." Although the shelf edge may have  
5 seemed abrupt with the vertical exaggeration typical of the older records from wide-  
6 beam echo sounders, in detail the bathymetry steepens gradually between shelf and  
7 slope (Bennett and Nelsen 1983; Field et al. 1983). In the higher-resolution bathymetry  
8 shown here, and in other datasets that we and others have studied (e.g., Adams and  
9 Schlager 2000), the uppermost slope from where sea level lay at  $\sim 120$  m during the  
10 LGM down to a few hundred meters depth commonly has a convex form with gradually  
11 varying gradient. Where continental slopes have prograded, they form giant sigmoidal  
12 clinofolds, with this convex uppermost surface its "rollover" (Pirmez et al. 1998;  
13 Sangree and Widmier 1977).

14           Rollovers arise generally from a gradual variation in energy of the environment:  
15 in shallow water, strong currents due to tides and waves flatten sediment topography,  
16 whereas in deeper water, where currents are weaker, sediment can form steeper  
17 deposits. The analysis presented here is intended to contribute to developing a more  
18 quantitative basis for this general statement, using information from theory and  
19 experiments to suggest how bedload sediment should be mobilized by currents. Such  
20 models potentially allow variations in seabed morphology to be linked with variations  
21 of environment.

22           Although concerning mud rather than sand as here, previous modelling of  
23 rollovers illustrate the trade-off between energy and gradient. Friedrichs and Wright  
24 (2004) showed how shelf mud, when kept suspended by waves, can form a seaward-

1 travelling gravity flow that deposits as wave agitation decreases where the flow extends  
2 beyond surface influences. Their model deposits form rollovers typical of deltas found  
3 at muddy river mouths. In models for freshwater delta fronts (Bitzer and Harbaugh  
4 1987; Pirmez et al. 1998), spreading and slowing of river outflow reduces bed shear  
5 stress, causing fine suspended sediment to deposit, over time also creating rollovers.

6 Diffusion transport models in which the mobility  $K$  declines with depth can also  
7 produce rollovers (Flemings and Grotzinger 1997; Kaufman et al. 1991; Rivenaes 1992;  
8 Rivenaes 1997; Schlager and Adams 2001; Syvitski and Daughney 1992). In our view,  
9 these models have not been well justified in marine settings because transport by many  
10 of the processes claimed to be represented by the models is inconsistent with the  
11 model's assumptions (Mitchell and Huthnance 2007). However, we show here how the  
12 effect of gravity on saltating sand could potentially lead to diffusion, suggesting a  
13 restricted application. By deriving the diffusion equation from first principles, a  
14 relationship of the mobility  $K$  to the speed of currents is found, thus allowing  
15 measurements of the modern currents to be compared via modelling with morphology,  
16 linking oceanographic environment to seabed evolution.

17 This paper is structured as follows. We first examine the logic behind the  
18 diffusion model. We then outline theory and experiments showing how the gravity  
19 effect on saltating particles does potentially lead to diffusion of seabed topography. A  
20 simple forward model illustrates how sandy rollovers could arise from the gravity  
21 effect. Using data from two sides of the Atlantic, we then describe and interpret  
22 observations of uppermost slope morphology that are consistent with the model, while  
23 also compiling data on modern bed currents to assess the extent to which currents  
24 intensify towards the shelf edge and contribute to the rollover form. The analysis then

1 examines how stronger, more sharply varying bottom currents during earlier times of  
 2 lowered sea level provide a better explanation for how sand has deposited over a limited  
 3 extent of the uppermost slope, interpreting the rollover form as a relic of LGM  
 4 conditions.

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## THEORY

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### *Diffusion Transport Models*

8 In these models, a diffusion equation in surface topography  $H$  is used to  
 9 represent how down-slope sediment transport processes tend to fill in basins over time  
 10 (e.g., Driscoll and Karner 1999; Flemings and Grotzinger 1997; Granjeon and Joseph  
 11 1999; Jordan and Flemings 1991; Mitchell 1995; Mitchell 1996; Penn and Harbaugh  
 12 1999; Quiquerez et al. 2004; Wolfe et al. 1994). The equation often used is

$$13 \quad \frac{\partial H}{\partial t} = K \nabla^2 H \quad (1),$$

14 where  $K$  is a mobility parameter ( $\text{m}^2/\text{s}$ ). The Laplacian  $\nabla^2 H$  represents the terrain's  
 15 curvature. In these models, sediment accumulates in depressions because areas of  
 16 positive  $\nabla^2 H$  imply positive  $\partial H/\partial t$  in equation (1). In the absence of other effects  
 17 generating relief (e.g., channelled erosion or tectonics), the model topography becomes  
 18 smooth over time.

19 The model originates in hillslope studies by combining an argument for how  
 20 soils creep down-slope with an assumption that mass is locally conserved (Culling  
 21 1960; Culling 1963; Kirkby 1971). In linear creep (Small et al. 1999), soil moves at  
 22 rates simply proportional to the local topographic gradient:

$$23 \quad Q = -K\rho_s \partial H/\partial y \quad (2)$$

24 where  $Q$  ( $\text{kg}/\text{m}/\text{s}$ ) is the mass flux in the down-slope direction ( $y$  (m)) per unit width of

1 slope and  $\rho_s$  ( $\text{kg/m}^3$ ) is the soil density. The continuity relation represents how a spatial  
 2 change in soil flux implies erosion or deposition (conservation of mass):

$$3 \quad \frac{\partial H}{\partial t} = -1/\rho_s \frac{\partial Q}{\partial y} \quad (3)$$

4 Differentiating Equation 2 in  $y$  and substituting in Equation 3 then leads to a diffusion  
 5 equation in soil topography:

$$6 \quad \frac{\partial H}{\partial t} = \frac{\partial}{\partial y} \left( K \frac{\partial H}{\partial y} \right) \quad (4a)$$

$$7 \quad \text{or } \frac{\partial H}{\partial t} = K \frac{\partial^2 H}{\partial y^2} \quad (4b)$$

8 if  $K$  is constant or varies gradually so that  $\frac{\partial K}{\partial y} \cdot \frac{\partial H}{\partial y} \ll K \frac{\partial^2 H}{\partial y^2}$ . Equation (1) can  
 9 be derived by repeating this analysis in two dimensions.

10 If the model were to apply in marine settings, the sediment flux would need to  
 11 occur in the down-slope direction and to have a magnitude proportional to the bed  
 12 gradient (Equation 2). As outlined elsewhere (Mitchell and Huthnance 2007), the  
 13 effects of many down-slope processes driven by gravity are unlikely to follow Equation  
 14 2 exactly, for example, slope failure and creep of clays involve threshold shear stresses  
 15 so their fluxes are not simply proportional to gradient. Sedimentary flows possess  
 16 momentum, so they are affected by upslope as well as local topography, and the  
 17 processes by which they deposit sediment are complex. Fine-grained particles deposit  
 18 at rates that are not necessarily related to bed gradient, but rather to bed shear stress  
 19 (McCave and Swift 1976) and to factors stabilizing the surface against intermittently  
 20 high stress (McCave 1984), so muddy clinofolds are better modelled using other  
 21 schemes. The diffusion model therefore does not describe marine sediment transport  
 22 generally, and its use should be limited to situations where its assumptions can be  
 23 shown to be followed.

## *Gravity Effect on Saltating Particles*

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In as much as there is presently no general review of the gravity effect available, we summarize the literature in electronic supplement ES1 and reproduce key points here. Figure 1A shows a conceptual model for a fully developed bedload (Bagnold 1963), in which particles are mobile where the shear stress due to particle impacts with the bed exceeds a critical stress  $\tau_0$ . The reaction to particle impacts effectively sets up a dispersive pressure which keeps particles water-borne. Ignoring initially the direct effect of the current, the force of gravity acting on particles then leads to a net stress on the mobile layer parallel to the bed causing down-slope movement that is stabilized by friction. According to this model, a greater thickness of particles (and greater flux) can be expected if the driving stress is larger because more particles will experience stresses above their critical value  $\tau_0$ .

Generalizing this conceptual model to two dimensions to include both the direct current and gravity effects, the total bedload flux  $\mathbf{Q}_b$  is:

$$\mathbf{Q}_b = S |\mathbf{u}|^2 (\mathbf{u} - \lambda |\mathbf{u}| \nabla \mathbf{H}) / g \quad (5),$$

where  $S$  is a constant,  $\lambda = 1/\tan\phi_s$ , and  $\nabla \mathbf{H}$  is bed gradient (bold symbols represent vectors,  $|\dots|$  the vector magnitude and  $\tan\phi_s$  is the sediment friction coefficient) (Bailard and Inman 1981; Huthnance 1982a; Huthnance 1982b).

Of interest for morphological modelling, Equation 5 leads to sand flux simply proportional to bed gradient (and hence topographic diffusion similar to Equation 1) in two situations. First, where the current continually reverses, such as under surface waves, internal tides or topographic waves, Equation 5 is dominated by the term  $\lambda |\mathbf{u}| \nabla \mathbf{H}$  if the vector average of  $\mathbf{u}$  (i.e., the residual current) is small. Second, the current  $\mathbf{u}$  is

1 commonly orthogonal to the gradient vector  $\nabla\mathbf{H}$  (e.g., geostrophic residual currents  
 2 flowing parallel to contours). Provided that the contour current is uniform along  
 3 contours, the down-gradient component of  $\mathbf{Q}_b$  is then proportional to the bed gradient  
 4 and a diffusion equation can be constructed in the down-slope direction. Both of these  
 5 situations are common near the shelf edge.

6 Although Bagnold's original approach has been criticized, in particular for  
 7 weakly developed bedloads, these concepts help to visualize the origins of diffusion and  
 8 why sediment mobility relates to current strength. The experimental results in Figure 2  
 9 reinforce this theory. In Figure 2A, bedload data collected using a longitudinal flume  
 10 (Damgaard et al. 1997) show enhanced flux when flow was down-gradient and reduced  
 11 flux when up-gradient, with almost a linear variation with gradient on average. The  
 12 change in flux is relatively small for a small change in gradient (e.g., over  $10^\circ$ )  
 13 compared with the flux when the flume was horizontal, so the direct current effect (term  
 14 in  $\mathbf{u}$  in Equation 5) can easily dominate over the gravity effect (term in  $\lambda|\mathbf{u}|\nabla\mathbf{H}$ ). The  
 15 reason why the gravity effect can be effective in the oceans, leading to diffusion,  
 16 however, is that many currents oscillate so that the direct effect cancels out. The results  
 17 shown in Figure 2B (Damgaard et al. 2003) are complicated by a stronger current  
 18 leading to suspension and bed rippling, but they nevertheless also show a gravity effect.

19 Sekine and Parker (1992) summarized models of bedload on slopes dipping  
 20 transverse to the current (i.e., contour-following currents). They suggested the  
 21 following equation for the ratio of down-gradient flux  $q_n$  to along-current flux  $q_s$ :

$$22 \quad q_n/q_s = -B |\nabla\mathbf{H}|; \quad B = B_0(\tau_c/\tau_b)^m \quad (6),$$

23 where  $B_0$  and  $\tau_b$  are constants and  $\tau_c$  is the current shear stress. It also suggests a linear  
 24 increase in the down-gradient flux with gradient  $|\nabla\mathbf{H}|$  and that the flux increases with



1 the current strength. Sekine and Parker (1992) suggested that the main group of  
 2 experimental data compiled in Figure 2C show that  $q_n$  is similarly or somewhat less  
 3 rapidly varying with current stress than the  $q_s$ . Because the direct current flux  $q_s$   
 4 increases with  $u^3$  or less (depending on importance of the threshold of motion) (Soulsby  
 5 1997),  $q_n$  is also proportional to  $u^3$  or less. Based on all the information available  
 6 (electronic supplement ES1), diffusion probably occurs with  $K$  proportional to between  
 7 roughly  $u^2$  and  $u^3$ , implying a strong sensitivity to bottom current strength.

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### *Forward Simulation*

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A numerical model was used to illustrate how rollovers could persist as steady  
 11 state features of depth-declining currents, if sea level, wave climate, ocean currents, and  
 12 supplied sediment flux and texture were all steady. Only the gravity effect on bedload  
 13 was accounted for. Although simple compared with natural systems, the simulations are  
 14 intended to illustrate first-order controls, and the results are similar to those with  
 15 sinusoidally varying water level (Kaufman et al. 1991).

16

In the model (Figure 3), sand was supplied at a constant flux  $Q_0$  from the left  
 17 boundary and its evolving surface was represented by an equally spaced array of  
 18 elevation values, initially a simple ramp of gradient  $\tan\gamma_0$ . The variation of mean  
 19 current speed  $\langle|\mathbf{u}|\rangle$  with depth  $d$  was approximated by a power law:  $\langle|\mathbf{u}|\rangle \propto d^\beta$  (which  
 20 will be shown later to approximate currents on the USA Atlantic slope). The down-  
 21 gradient flux of bedload was given by  $Q_{by} \propto -\langle|\mathbf{u}|\rangle^n \cdot \partial H / \partial y$ , where  $\partial H / \partial y$  is the offshore  
 22 bed gradient and  $n = 2$ . Thus,  $Q_{by} \propto -d^{2\beta} \partial H / \partial y$  was used to compute how the local flux  
 23 varies with both current strength and bed gradient.

1           Bed gradients  $\partial H/\partial y$  were derived from finite differences of the topography and  
2 elevations adjusted iteratively using the continuity relation ( $\partial H/\partial t = -\partial Q_{by}/\partial y \cdot 1/\rho_s$ ).  
3 Because this scheme leads to sediment becoming infinitely mobile at sea level, a  
4 constant value for  $d^{2\beta}$  was imposed above a certain depth to maintain stability.  
5 (Coordinates are omitted from Figure 3 because we wish to emphasize how changes in  
6 parameters affect morphology but essentially the limiting depth for  $d^{2\beta}$  lies along the  
7 tops of the graphs.)

8           Figure 3A shows a simple developing clinoform, and the graph to its right shows  
9 bed gradients calculated from the final topography. In Figure 3B, the current speeds  
10 were varied more sharply with depth (double  $\beta$ ), creating a markedly sharper rollover.  
11 With a doubling of  $Q_0$  (Figure 3C), the rollover was also sharper. In Figure 3D, the  
12 ramp angle was doubled, producing a somewhat sharper rollover. The convexity of a  
13 sandy rollover therefore depends, not merely on the sharpness of the variation of  
14 currents with depth but also on the sediment input and, to a lesser degree, on the shape  
15 of the space in which the sediment accumulates.

16           The model rollover is only marginally below sea level, so the model does not  
17 predict the existence of a shelf. Clearly other processes generate shelves, such as  
18 subaerial erosion during sea-level lowstands. If gravity-driven bedload transport plays  
19 an important role, progradation of the uppermost slope occurs primarily during  
20 conditions of lowered sea level (with sea level intersecting the upper face of the rollover  
21 as in Figure 3) because extreme currents are needed in the shallow water to move the  
22 sediment on small gradients. Alternatively, if progradation is significant during high-  
23 stand conditions, other processes are needed to export sediment from the shelf.

1           These simulations represent sand only, but in practice mud depositing below the  
2 rollover (Chin et al. 1988; Deibert et al. 2003; Dunbar and Barrett 2005) forms a  
3 boundary condition to the gravity-driven transport of sand above. Mud depositing  
4 below the sand effectively elevates the clinoform face compared with its level if there  
5 were no mud available. Its long-term effect is therefore similar to the sand prograding  
6 over a shallower substrate, reducing convexity of the rollover.

7           Although the uncertainties in boundary conditions prevent subtle differences in  
8 rollover shapes from being interpreted, the observed rollover shape may reflect a  
9 particular pattern of currents. For example, the power-law depth-varying currents lead  
10 to steepening gradient-depth graphs, whereas a simulation developed using  
11 exponentially varying currents with depth (Figure 3E), such as might occur under waves  
12 with dominant height and period, has a flattening gradient-depth graph. As shown later,  
13 actual gradient trends are intermediate between these extremes.

14

### 15                                   **3. MODERN CURRENTS**

16           Near-bed measurements are compiled (Figure 4) to represent the average  
17 variation of bottom current speeds with depth (Figure 5). Data sources are given in  
18 electronic supplement ES2, which discusses measurement issues. The analysis mostly  
19 concerns USA Atlantic data collected over a year. Measurements were made at various  
20 altitudes but are left uncorrected because of insufficient information on bed roughness  
21 and boundary-layer development. The data in Figure 5 represent the effects of all  
22 current components including some oscillations under surface waves but primarily  
23 longer period oscillations, because surface waves have minor effect at depths of the  
24 continental slope and the meters tend to average out short period oscillations. The data

1 represent the average of the current speed, i.e., the scalar not the vector of current  
2 velocity.

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### 3.1. *USA Atlantic*

5        Currents intensify up the USA slope towards the shelf edge, where they  
6 resuspend silt (Churchill et al. 1994). The dotted line in Figure 5A represents the  
7 average power-law trend of the near-bed data (solid symbols) below 150 m. The  
8 records for these sites show the different oceanographic influences, varying from long-  
9 period topographic Rossby waves (Gulf Stream eddy rings with 5 to 29 day periods) to  
10 high-frequency surface (wind) waves, with residual currents primarily along-slope  
11 (Aikman et al. 1988; Beardsley et al. 1985; Butman 1988; Butman et al. 1979; Csanady  
12 et al. 1988; Fratantoni et al. 2001; McClennen 1973; McGregor 1979; Shaw et al. 1994).  
13 Separating the data by frequency, Csanady et al. (1988) showed how the influence of  
14 the different oscillations varies: Rossby-wave currents affect the whole slope, whereas  
15 wind-driven upwelling or downwelling currents, tidal currents, and currents under  
16 surface waves are important over the upper slope but decline to 1000 m. Internal tides  
17 are enhanced near the shelf edge where a front between the shelf and slope water bodies  
18 intersects the seabed (Aikman et al. 1988; Flagg 1988; Ou and Maas 1988). Cacchione  
19 et al. (2002) showed how bed stresses from internal waves intensify where the bed  
20 gradient approaches the characteristic gradient of the waves, modulating how fine  
21 sediment deposits on the slope.

22        Somewhat different currents might be expected between sites, but comparisons  
23 between current meters suggests that, away from major canyons, the regression in  
24 Figure 5A approximates the typical uppermost slope enhancement. Figure 6 compares

1 the current variances computed by Csanady et al. (1988) for different frequency bands  
2 (see figure caption). The sites near 1000 m depth show a similar influence of Rossby  
3 waves. Higher-frequency currents in shelf-edge sites A and SF in Figure 4 are also  
4 comparable.

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### *Iberia Atlantic*

7 The fewer measurements made off Iberia are compiled in Figure 5B (electronic  
8 supplement ES2). The solid lines in Figure 5B show currents derived from 10 days of  
9 ship acoustic Doppler measurements (electronic supplement ES3; bold line is median  
10 average, and fine lines represent the inter-quartile range of current speed). The power-  
11 law trend (dotted line) was derived from all bottom-measured data below 150 m depth,  
12 including measurements from 100 m altitude above bottom to compensate for data  
13 scarcity. It suggests a more sharply varying speed with depth than off the USA.  
14 Although this difference is unresolved statistically, a sharp variation might be expected  
15 because of this area's exposure to Atlantic swell (Vitorino et al. 2002) and strong  
16 internal waves on the shelf (Jeans and Sherwin 2001; Sherwin et al. 2002; Vitorino et al.  
17 2002).

18 Different wind directions in winter and summer lead to sustained downwelling  
19 and upwelling, respectively (Vitorino et al. 2002). On such easterly ocean margins, an  
20 equatorward wind stress induces an Ekman spiral (a Coriolis effect on the currents) and  
21 transport of surface water offshore relative to the water below. Upwelling of underlying  
22 water replaces surface water blown offshore. The sea surface is lowered at the coast,  
23 leading to an equatorward geostrophic current developing to balance the surface  
24 gradient, a current that is enhanced by the equatorward wind stress. Downwelling

1 occurs during the opposite conditions. Numerical models show that upwelling and  
2 downwelling lead to bed currents declining seawards from the shelf edge (Davies et al.  
3 2002; Xing and Davies 2002), contributing to the trends observed in Figure 5B.

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## 5 **GEOLOGY AND MORPHOLOGICAL OBSERVATIONS**

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### *USA Atlantic Margin*

7 Figure 7A shows bathymetry derived with continuous coverage of multibeam  
8 echo sounders. Above where the slope is incised by canyons, the topography is  
9 remarkably smooth and ridges between canyons are rounded rather than sharp. Figure  
10 7B shows the median gradient (50%) and inter-quartile range of gradients (25% to 75%)  
11 for the area outlined in Figure 7A (where gradients were derived from differences in  
12 elevation in offshore and along-slope directions over a 50 m lengthscale after smoothing  
13 the bathymetry grid with a 250 m by 250 m filter (Wessel and Smith 1991)). Median  
14 gradient increases almost linearly with depth to 500 m, a variation implying that the  
15 morphology is exponential-like in profile, which is illustrated by the dashed exponential  
16 curves fitted by least-squares to the profiles shown in Figure 7C.

17 Figure 7B shows median grain sizes derived from grab sampling at sites located  
18 by solid star symbols in Figure 7A. Coinciding with the smooth morphology, the  
19 seabed is sandy at the surface, with a transition to mud at 300 m to 350 m. Published  
20 maps show this pattern of grading continuing along-strike (e.g., Keller et al. 1979;  
21 Southard and Stanley 1976; Stanley et al. 1983; Stanley and Wear 1978). Subsurface  
22 lithologies sampled at AMCOR 6007 drilled on the outer shelf (Figure 7A) include  
23 mostly sand of Pleistocene to Miocene age (Figure 7F) (Hathaway et al. 1979;  
24 Hathaway et al. 1976). From an ALVIN dive 50 km NE of Figure 7A, Malahoff et al.

1 (1982) noted an upwards change to coarser sand with pebbles, cobbles, and even some  
2 boulders above 380 m depth.

3 Two seismic reflection lines show a stratigraphic pattern typical of seaward  
4 progradation along with aggradation on the outer shelf. The multichannel data in Figure  
5 7D, collected along the dashed line in Figure 7A (Schlee et al. 1976), show shallow-  
6 dipping foresets subparallel to the modern seabed. The single-channel data in Figure 7E  
7 also shows subparallel foresets but that the shelf edge stratigraphy overlies strata  
8 deeping shallowly seawards. Nevertheless, it confirms a lateral extension of the  
9 stratigraphy beneath the uppermost slope in Figure 7D, a pattern that is also mimicked  
10 in other seismic data collected nearby (McGregor et al. 1979; Schlee et al. 1979).

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### 12 *Iberian Atlantic Margin*

13 Figure 8A shows bathymetry also collected with a multibeam echo sounder  
14 (NERC 2001). The morphology shallower than 500 m is smooth, similar to Figure 7A.  
15 Profiles "a" and "b" in Figure 8B also show a rounded shape. Median gradient (Figure  
16 8C) of data from the area outlined in Figure 8A reveals a quasi-linear steepening with  
17 depth to 700 m, but with the rate of steepening only half that in Figure 7C.  
18 Multichannel seismic reflection data collected along the "Ewing" track shown in Figure  
19 8A (Pérez Gussinyé 2000, her Figure 2.2) show reflectors beneath the outer shelf  
20 subparallel to the seabed to around 1 km sediment depth. Bottom photographs collected  
21 near 200 m depth (located by open circles in Figure 8A) show a bioturbated muddy sand  
22 (NERC 2001). Samples recovered near there and immediately shallower are fine-  
23 grained sands with < 25% silt and clay (mean grain size 2-3  $\phi$ ) (Dias et al. 2002;  
24 Jouanneau et al. 2002; van Weering et al. 2002).

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### *Interpretation of Morphology*

Many of the topographic characteristics observed are typical of diffusion (Mitchell and Huthnance 2007). For example, the smoothness of the terrain is expected because, from Equation 1, bumps (negative  $\nabla^2 H$ ) and depressions (positive  $\nabla^2 H$ ) progressively attenuate (locations of negative and positive  $\partial H/\partial t$ , respectively) if not maintained by other effects. Furthermore, parabolic surfaces between canyon heads are also typical (though not necessarily diagnostic) of diffusion because the parabola is the steady state solution to the diffusion equation when material is removed constantly at the channels. Where the bed is sandy, we ascribe these observations to the gravity effect on saltating sand and true diffusion (Mitchell and Huthnance 2007).

The seismic data show that the morphology has prograded, so sand has been exported from the shelf persistently and spilled over the shelf edge. Spilled sand was mobilized by currents affecting the uppermost slope, leading to a gravity-driven movement of particles and a stratigraphic evolution similar to that illustrated in Figure 3.

In later analysis, we further assume that areas below present 150 m depth lay persistently below sea level during the LGM, based on work elsewhere (Yokoyama et al. 2000). A lack of significant glacio-isostasy in the area of Figure 7A is suggested by depths of submerged shorelines (Dillon and Oldale 1977), and a depth of 150 m keeps our analysis away from possible beach shoreface effects of the LGM.

### **DERIVING A MODEL $K$ FROM MORPHOLOGY**



1           We develop a kinematic model to invert the morphology for diffusion mobility  
 2  $K$ , which then allows us to compare the variation in the derived  $K$  with the currents,  
 3 assuming that sediment mobility simply originates from the gravity effect on saltating  
 4 particles. The results are not unique, so the exercise is intended rather to identify the  
 5 range of values consistent with the model. An assumption of long-term steady state is  
 6 required. In as much as seismic reflectors parallel the modern seafloor in these areas,  
 7 the morphology is probably steady state over 100 ky to My timescales, depending on  
 8 data resolution, but not necessarily so over shorter timescales.

9           Much of the following analysis is possible analytically because the uppermost  
 10 slope is nearly exponential:

$$11 \quad d' = d_0 \exp(sy) \quad (7),$$

12 where  $d' = d - d_r$  is depth below a reference depth  $d_r$  such that gradient  $\partial H / \partial y = -s d'$  (i.e.,  
 13 linear with depth, Figure 2a),  $s$  is the rate of bed steepening with depth (herein called the  
 14 convexity parameter) and  $y$  is distance offshore from where  $d' = 0$ . Parameters  $d_r = 111$   
 15 and 136 m and  $s = 0.000679$  and  $0.000328$  were obtained by least-squares regression of  
 16 median gradient on depth from Figures 7B and 8B, respectively.

17

#### 18           *Deriving $K_y$ Assuming that Sand Bypasses*

19           If all sand exported from the shelf bypasses and none deposits, the offshore  
 20 component of flux,  $Q_{b,y}$ , is then spatially uniform and  $K_y$  can be obtained simply by  
 21 inverting Equation 1 (i.e.,  $K \propto 1/(|\nabla H|)$ ). This is unrealistic, because sand has deposited  
 22 over a restricted area beyond the outer shelf, but nevertheless the predicted variation in  
 23  $K_y$  shown in the first two graphs for  $K_y$  in Figure 9A (continuous lines "uniform  $Q$ ")  
 24 provides a limiting trend. (Here and in other graphs in Figure 9, values of  $K_y$  are shown

1 as both  $K_y^{1/3}$  and  $K_y^{1/2}$  to compare with the mean current speeds, assuming bedload  
 2 models in which  $Q_{by} \propto \langle |\mathbf{u}| \rangle^3 |\nabla \mathbf{H}|$  and  $Q_{by} \propto \langle |\mathbf{u}| \rangle^2 |\nabla \mathbf{H}|$ , respectively. Values were also  
 3 normalized by dividing by the value for  $K_y$  at  $d' = 100$  m.)

4

### 5 *Deriving $K_y$ for Prograding Geometries*

6 Figure 10 shows the geometry used to calculate  $K_y$  more generally. This is done  
 7 essentially by working out how average deposition rates have varied spatially and then  
 8 deriving transport flux using the continuity relation.  $K$  is subsequently obtained from  
 9 the flux and bed gradient (Equation 2).

10 If the uppermost slope aggrades uniformly,  $\partial H/\partial t = A$  is uniform (Figure 10A).

11 If instead the uppermost slope progrades (Figure 10B), deposition rates increase away  
 12 from the outer shelf. Their values required to advance the morphology uniformly at rate  
 13  $\partial y/\partial t$  (i.e., to maintain a steady state shape) are given by

$$14 \quad \partial H/\partial t = -\partial d'/\partial y \cdot \partial y/\partial t \quad (8)$$

15 If the rollover both aggrades and progrades (Figure 10C),  $A$  is added:

$$16 \quad \partial H/\partial t = A - \partial d'/\partial y \cdot \partial y/\partial t \quad (9a),$$

$$17 \quad \text{or} \quad \partial H/\partial t = A + s d' \cdot \partial y/\partial t \quad (9b)$$

18 by replacing  $\partial d'/\partial y$  with  $-s d'$ . We define a parameter  $\tan \alpha = A/(\partial y/\partial t)$  representing the  
 19 ratio of upwards to seawards growth of the rollover. Physically,  $\alpha$  is the rollover's  
 20 climbing angle, which in principle can be measured from seismic reflection data (Figure  
 21 10C). Replacing  $\partial y/\partial t$  with  $A/\tan \alpha$  then leads to

$$22 \quad \frac{\partial H}{\partial t} = A \left( 1 + \frac{d' s}{\tan \alpha} \right) \quad (10)$$

1 in which deposition rates increase linearly with depth change  $d'$ . (At larger scale,  
2 deposition rates decline down the continental slope (e.g., Sanford et al. 1990), but this is  
3 beyond the sandy area of interest.)

4 Equation 10 also shows that the convexity parameter  $s$  reflects how time-  
5 averaged deposition rates have varied. If the rollover is sharply convex (large  $s$ ),  
6 sharply varying deposition rates are required to maintain the morphology.

7 Spatial variations in the time-averaged flux  $Q_y$  are derived by applying the  
8 continuity relation in  $y$ . Replacing  $\partial H/\partial t$  of Equation 10 with  $-1/\rho_s \partial Q_y/\partial y$  from  
9 Equation 3 and integrating in  $y$  produces

$$10 \quad Q_y(y) = Q_{y0} - A\rho_s \left( y + \frac{d_0'}{\tan \alpha} (e^{sy} - 1) \right) \quad (11)$$

11 where  $Q_{y0}$  is the offshore component of flux on the outer shelf (at  $y = y_0$  corresponding  
12 to where  $d' = d_0'$ ). Replacing  $y$  using Equation 7 leads to

$$13 \quad Q_y(d') = Q_{y0} - A\rho_s \left( \frac{\ln(d'/d_0')}{s} + \frac{(d' - d_0')}{\tan \alpha} \right) \quad (12).$$

14 If all flux  $Q_y$  occurs as gravity-driven bedload,  $K_y$  can be obtained from Equation  
15 12. Because finer-grained material around the mudline is transported in suspension,  
16 obeying different transport rules, Equation 12 under-represents the sharpness of the true  
17 decline in sand  $Q_y$  with  $d'$ . Our interpretation therefore focuses on the upper part of the  
18 rollover.

19  $K_y$  is derived from Equation 2,  $\partial H/\partial y = -sd'$  and Equation 12 for  $Q_y$ :

$$20 \quad K_y(d') = \frac{A\rho_s}{sd'} \left( \frac{Q_{y0}}{A\rho_s} - \frac{\ln(d'/d_0')}{s} - \frac{d' - d_0'}{\tan \alpha} \right) \quad (13)$$

21 The form of  $K_y(d')$  thus depends on  $Q_{y0}$ ,  $A$ ,  $\rho_s$ ,  $s$ ,  $d_0'$ , and  $\alpha$ , of which  $s$  can be derived  
22 from bathymetry and  $\alpha$  can in principle be estimated from seismic data. Although  $A$ ,

1  $Q_{y0}$ , and  $\rho_s$  could each be estimated separately if adequate stratigraphic and physical  
2 property data were available, we instead use their ratio  $Q_{y0}/A\rho_s$  which is a lengthscale  
3 over which sediment of flux  $Q_{y0}$  would deposit at average rate  $A$ .  $d_0'$  was set to 1 m.

#### 5 *Comparing Inversion Results to Modern Current Data and LGM Conditions*

6 Figures 9A and 9B show inversion results along with (dotted lines in graphs) the  
7 mean current speed variation from Figure 5A. Although the latter is only the mean,  
8 peak speeds (more relevant to mobilizing bedload) probably have a similar power-law  
9 trend, as suggested by the curves of Doppler data in Figure 5B in which the upper  
10 quartile parallels the median average. Threshold-of-motion effects should be  
11 considered in refinements of this model. From Figures 7D and 7E, the rollover  
12 climbing angle  $\alpha$  is  $11^\circ$  to  $16^\circ$  (inversion results with  $\alpha = 10^\circ$  are most relevant, though  
13 others are shown to illustrate effect of uncertainty in  $\alpha$ ).

14 Figure 9B shows a relatively moderate decline in  $K$  with depth if the lengthscale  
15  $Q_{y0}/A\rho_s$  is large compared with the uppermost slope region of interest. The trend is  
16 somewhat steeper than the modern current data, although the difference may be less  
17 significant if thresholds of motion effects are considered (i.e., if the amount by which  
18 speed exceeds threshold decreases more greatly from 100 m to 300 m than the mean  
19 speed). There is little evidence that sand deposits over this lengthscale, however, based  
20 on the distance across the rollover to the sand/mud transition (Figure 7). More  
21 realistically, sand has deposited over a short distance of a few kilometers beyond the  
22 outer-shelf parts of the profiles in Figure 7C, so  $K_y$  must vary sharply with depth, as in  
23 Figure 9A, where trends are steeper than the current speed data.

1           Because much of the outer shelf sediment was deposited during the LGM  
2 (Southard and Stanley 1976), the uppermost slope morphology could reflect the stronger  
3 currents at that time. Although difficult to quantify, conditions during the LGM should  
4 have led to more sharply varying currents with depth than at present, consistent with the  
5 more steeply varying  $K_y$ . Bottom currents due to surface waves will have been more  
6 strongly felt with depressed sea level. Surface waves mobilizing sand to 200 m depth  
7 (Komar et al. 1972) could have affected the bed below present-day 300 m during the  
8 LGM. Figure 9C shows variations in peak bottom current speed  $u_s$  produced by 20 s  
9 and 10 s period storm waves with sea level depressed by 120 m (calculated with a deep-  
10 water approximation), which more closely match the inversion data in Figure 9A with  $\alpha$   
11 = 10°. Storms may also have been more frequent and vigorous based on enhanced NaCl  
12 and dust in ice cores (Mayewski et al. 1994).

13           It is difficult to say if other oceanographic currents would have had the same  
14 relation to the uppermost slope as in the modern data (Figure 5) because little is known  
15 about atmospheric forcing and ocean density stratification. Salinities of sediment pore  
16 waters suggest that the LGM oceans had a different density structure (Adkins et al.  
17 2002), which could have affected internal-wave dynamics. An LGM tidal model  
18 (Egbert et al. 2004) suggests that  $M_2$  tidal amplitudes were greater off the USA Atlantic  
19 coast by a factor of two, and may have been larger if the oceans were less density  
20 stratified than at present, e.g., because of lower surface temperature. Tidal flows at the  
21 shelf edge would have been further intensified because they supplied the high to low  
22 water volume via shallower depth over the outer shelf when sea level was lowered.  
23 Thus, although difficult to test formally, currents are expected to have been more

1 sharply varying with depth during the LGM, as we also suspect from the inversions of  
 2 morphology and short deposition distance of the sand.

### 4 *Effects of an Offshore Residual Current*

5 If the residual (vectorally averaged) current has a finite component  
 6 perpendicular to the shelf edge and it declines down the slope, an additional  
 7 convergence of its associated sediment flux also contributes to prograding the  
 8 uppermost slope (e.g., Quiquerez et al. 2004). Figure 11A shows such a decline in the  
 9 mean offshore component of current-meter measurements from the two margins  
 10 (Csanady et al. 1988; Huthnance et al. 2002).

11 A rough comparison with the gravity-driven offshore flux can be made using  
 12 Equation 5. It suggests that the offshore current component dominates if  $\langle u_y \rangle / \langle |\mathbf{u}| \rangle >$   
 13  $|\nabla \mathbf{H}| / \tan \phi_s$ . The dashed and dotted lines in Figure 11B show  $|\nabla \mathbf{H}| / \tan \phi_s$  computed from  
 14 the median gradients in Figures 7 and 8, respectively, and with  $\tan \phi_s = 0.63$  (Soulsby  
 15 1997). A change from current-driven to gravity-driven transport with depth is  
 16 suggested by the USA data values greater than  $|\nabla \mathbf{H}| / \tan \phi_s$  at  $\sim 200$  m but less than  
 17  $|\nabla \mathbf{H}| / \tan \phi_s$  at 500 m. The Iberian values are both greater than  $|\nabla \mathbf{H}| / \tan \phi_s$ , however,  
 18 suggesting that sand bedload transport is driven mainly by downwelling at present.

### 20 *Diffusion in 2D*

21 A diffusion equation with  $K$  declining with depth was applied to the bathymetry  
 22 to explore tendencies of erosion or accumulation that would result if it were to apply  
 23 universally above 300 to 350 m where sand exists. The calculation ignores how local

1 topography affects the currents, so only a general tendency implied by the variation of  $K$   
 2 with depth is sought, not one that applies exactly to all locations.

3 The bathymetry data (Figure 7A) were re-projected and smoothed with a 250 m  
 4 filter. Local sand flux was calculated from  $\mathbf{Q} = -K\nabla\mathbf{H}$ , where gradient  $\nabla\mathbf{H}$  (Figure  
 5 12A) was derived from finite differences of the bathymetry. The mobility was  
 6 decreased inversely with depth  $d$ :  $K = K_0(d/d_0)^{-1}$  where  $d_0 = 1$  m is a reference depth.  
 7 ( $K \propto d^{-1}$  is nearly equivalent to using the trend in Figure 5A ( $\beta = 0.36$ ) with  $n = 3$ .)  
 8 Changes in topography were then calculated from continuity,  $\partial H/\partial t = -\nabla \cdot \mathbf{Q}$ . The  
 9 calculation was repeated iteratively, each time adjusting the bathymetry and re-  
 10 calculating bed gradients to quantify  $\mathbf{Q}$ . The resulting depth change values are omitted  
 11 from Figure 12B to highlight the pattern of relative change rather than absolute values,  
 12 and results below 400 m are censored because the model is not relevant to the muddy  
 13 slope sediments.

14 If Equation 1 were to apply uniformly with constant  $K$ , the spurs between  
 15 canyon heads (areas of negative curvature) would erode (negative  $\partial H/\partial t$ ) relative to the  
 16 outermost shelf, where straight contours indicate smaller curvature. Figure 12B instead  
 17 shows little bed change across the uppermost slope away from canyon heads because  $K$   
 18 decreasing sharply with depth compensates for increasing terrain curvature. Where the  
 19 uppermost slope is sandy, therefore, the persistence of morphologic features of differing  
 20 curvature may imply persistence in bottom current patterns too.

21

22

## DISCUSSION

23

24

Previous studies reproducing clinoform rollovers with diffusion models (e.g.,  
 Flemings and Grotzinger 1997; Kaufman et al. 1991; Rivenaes 1997; Schlager and

1 Adams 2001) have, in our view, not adequately justified using the diffusion equation.  
2 From the justification using the gravity effect on saltating particles identified here, the  
3 bed shear stress or bottom current speed strongly control sediment mobility. It is  
4 probably not adequate to simulate the effects of sea-level fluctuations on transport by  
5 changing water depth alone (Flemings and Grotzinger 1997; Kaufman et al. 1991;  
6 Rivenaes 1997; Schlager and Adams 2001), because changing water depth also varies  
7 the tidal currents and because greater frequency of storms during the LGM implies a  
8 different influence of surface waves. The rounding of the shelf edge suggested as due to  
9 varying sea level or wave base level (Adams and Schlager 2000; Schlager and Adams  
10 2001) is suggested here instead to reflect the way in which bed shear stress varies with  
11 depth, a more gradually curved rollover arising from gradually varying shear stress with  
12 depth. Furthermore, sharp rollovers have been produced with models in which  $K$  is  
13 constant in the water column and interpreted as representing a lack of near-surface  
14 influences (Schlager and Adams 2001). In such models, however, an abruptly increased  
15  $K$  above the water line is often used to simulate high mobility of sediment where  
16 exposed subaerially, so such models should prompt us to consider whether sharp  
17 rollovers in data imply abruptly varying  $K$ , not necessarily a lack of near-surface  
18 influences.

19         The sensitivity of  $K$  to current speeds has implications for interpreting relative  
20 sea-level change from margin sequences (Vail et al. 1977). Flemings and Grotzinger  
21 (1997) illustrated how fluctuations in sediment supply can generate sequences of  
22 character similar to those generated by sea-level fluctuations (Christie-Blick and  
23 Driscoll 1995). If the enhanced salt concentrations in ice cores (Mayewski et al. 1994)  
24 implies an enhanced storm frequency and/or severity, the mean bed current speed in



1 wave-dominated environments should be enhanced, implying an increase in mobility  $K$ .  
2 For example, a doubling of storm frequency would imply doubling of  $\langle |\mathbf{u}| \rangle$ , increasing  
3  $K$  by a factor 4 to 8 (from  $K \propto \langle |\mathbf{u}|^2 \rangle$  to  $K \propto \langle |\mathbf{u}|^3 \rangle$ ). Combined with varying residual  
4 currents, variations in "oceanic climate" can potentially affect unconformities and  
5 obscure simple effects of sea-level fluctuation on sequences, which are often guided by  
6 geometry of strata around the rollover (Steckler et al. 1999).

7         Although the single-component model developed here usefully provides  
8 insights, it lacks many effects which need further investigation before incorporating  
9 them into more complete models (e.g., Quiquerez et al. 2004). To include bedload  
10 transport by residual currents, we would need to predict upwelling or downwelling  
11 currents of earlier periods when less information on wind conditions are available. How  
12 mud components within the rollover and below it contribute to rollover convexity are  
13 difficult to address because of difficulty in predicting biological and physical  
14 stabilisation under time-varying currents (McCave 1984; Sanford and Maa 2001).

15         The activity of fish and other organisms can also affect seabed morphology over  
16 geological periods, and the gravity effect on biologically resuspended particles  
17 potentially contributes to topographic diffusion (Mitchell and Huthnance 2007).  
18 Because lateral sediment fluxes from by biological activity have not been quantified, its  
19 morphological effect is difficult to assess quantitatively, but bio-mixing rates of  
20 radiometric tracers in cores typically decline below the shelf edge mimicking the  
21 decline in current speeds (Anderson et al. 1988; Henderson et al. 1999; Middelburg et  
22 al. 1997; Schmidt et al. 2002; Soetaert et al. 1996).

23         Examining the geometry of older strata can potentially inform this problem  
24 because transport consistent with a diffusion-type model implies that strata should

1 steepen if sediment flux increases (Schlager and Adams 2001). This can be seen from  
2 Equation 2:  $\partial H/\partial y$  increases if  $K$  and  $\rho$  are constant but  $Q$  increases. Alternatively, if  $Q$   
3 were constant but there were a change in oceanographic conditions, then  $K$  could vary  
4 and also affect the steepness of strata.

5 In some seismic datasets, the ancient rollover is more rounded than the modern  
6 rollover, possibly reflecting effects of  $K$  and  $Q$ . This can be seen, for example, in data  
7 collected across the shelf edge in the South Western Approaches to the UK and France,  
8 where Pleistocene sediments have a markedly sharper rollover than their underlying  
9 upper Miocene (Bourillet et al. 2003), which largely comprises sand (Evans and Hughes  
10 1984; Pantin and Evans 1984). The modern surface is consistent with diffusion  
11 (Mitchell and Huthnance 2007), being smooth aside from bedform relief (Cunningham  
12 et al. 2005).

13 A similar sharpening, from Late Oligocene towards Pleistocene, can be seen in  
14 the New Jersey shelf edge of Steckler et al. (1999). Their reconstructions suggest that  
15 the uppermost slope was more gradually curved (e.g.,  $s' = 2 \times 10^{-4} \text{ m}^{-1}$  for their m6  
16 surface) than we find for the area in Figure 7 ( $s' = 6.74 \times 10^{-4} \text{ m}^{-1}$ ). Evidence that  
17 bedload transport and hence the gravity effect was involved in creating these rollovers  
18 includes rounding of grains sampled in the Miocene strata (Pope et al. 1990).

19 These two examples could potentially reflect changes in oceanographic  
20 conditions. The Miocene and earlier periods were times of more stable sea level with  
21 variations of  $< 50 \text{ m}$  (John et al. 2004; Kominz et al. 1998; Kominz and Pekar 2001;  
22 Miller et al. 1998; Van Sickle et al. 2004) and extreme low-stands rarely reaching 100  
23 m based on foraminiferal  $\delta^{18}\text{O}$  (John et al. 2004; Lear et al. 2004). The enhanced tidal  
24 currents and oscillating currents due to storm-induced waves for the LGM shelf edge

1 should therefore have been less frequent during these previous periods compared with  
2 the Pleistocene. Thus, before the Pleistocene, more stable conditions imply long  
3 periods with a more gradually varying mobility with depth, in turn leading to a more  
4 gradually curved uppermost slope.

5 Sediment fluxes to the margins also generally increased into the Pleistocene  
6 associated with enhanced continental erosion of the glacial world, potentially leading to  
7 sharpened rollovers of sand. Enhanced fluxes are suggested, for example, by deposition  
8 rates in marginal basins dramatically increasing globally during the last 2 to 4 Ma  
9 [Zhang, 2001 #2454]. Furthermore, in Steckler et al.'s (1999) reconstructions, the shelf  
10 edge is sharper in the Middle Miocene than in the Late Oligocene, tracking an increased  
11 rate of sediment supply implied by the margin progradation rate.

12

13

### CONCLUSIONS

14 The morphology of the uppermost slope is consistent with having been modified  
15 as though by a diffusion equation with mobility  $K$  declining with depth, generating the  
16 rollover and smooth, parabolic regions between canyon heads. Given the presence of  
17 sand and how modern currents decline with depth, the gravity effect on saltating  
18 particles provides a plausible explanation for this apparent diffusion. The sand has  
19 deposited relatively close to the outermost shelf, which implies that mobility declines  
20 sharply with depth. This could be consistent with stronger currents that declined more  
21 rapidly with depth during the Last Glacial Maximum. The models imply that both the  
22 sharpness of the uppermost slope rollover in profile and morphology in plan view  
23 depend on how the currents vary spatially, as well as on sediment flux to the slope and  
24 accommodation space.

1

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14

### 15 **Figure captions**

16 Figure 1. A) Illustration of particle motions in a bedload active on a slope. The long-  
17 dash line separates the bedload from the immobile bed below, defined as the level at  
18 which shear stresses equal the threshold of motion. B) Down-gradient movement arises  
19 because the momentum transfer from grain to grain collisions keeping the bedload  
20 mobile acts perpendicular to the bed on average ("dispersive pressure"), whereas the  
21 bedload weight acts vertically, leading to a net pressure acting parallel to the bed (gray  
22 vector) which becomes balanced by friction. Current shear stress components are  
23 omitted.

24

1 Figure 2. A) Measurements of sediment flux  $Q$  as a function of longitudinal gradient for  
 2 experiments (Damgaard et al. 1997) with the bed Shields stress  $\theta$  values shown.  
 3 Enlarged symbols represent average  $Q$  for given gradient groupings (plus and gray-  
 4 filled symbols only). The oblique lines are least-squares regressions of  $Q$  on gradient  
 5 for the different stresses excluding data for  $-29^\circ$ , which show enhanced  $Q$  near the  
 6 sediment angle of repose. B) Experiments similar to Part A made at higher flow stress  
 7 and with flux measured using a sediment trap (plus symbols) and with instruments  
 8 designed to measure suspended particle flux (gray-filled circles). Bold plus symbols  
 9 represent average  $Q$  calculated for groups of gradient. Dashed line is least-squares  
 10 regression of the trap fluxes. C) Measurements of transverse bed-load flux against bed  
 11 shear stress (Sekine and Parker 1992). Plus symbols: data collected in air (Yamasaka et  
 12 al. 1987). Solid circles: data collected in water (Hasegawa 1981). Dashed lines  
 13 represent graph trends expected with  $m$  of Equation ES10 equal to the values shown.

14  
 15 Figure 3. Results of numerical models exploring the effect of parameters on the shape  
 16 of a sandy clinoform, assuming that sediment movements occur only because of the  
 17 gravity effect on saltating particles. Initial bed topography is a simple ramp of gradient  
 18  $\tan\gamma_0$  and sand is supplied from the left boundary with constant flux. Graph A is the  
 19 reference model and B, C and D show the effects of varying the gradient of current  
 20 speed with depth, input flux and ramp angle, respectively. Graphs to right show the  
 21 final bed gradient versus depth (gradients in Part B are reduced by a factor of 20). The  
 22 convexity  $s$  values shown were derived by least-squares regression of the gradients with  
 23 depth over the depth intervals above the dashed lines. Lowermost graph was produced  
 24 with current speeds varying exponentially with depth.

1  
2 Figure 4. Locations of the study areas in Figures 7 and 8 (gray-filled boxes) and  
3 current-meter deployments. Gray depth contours shown annotated in kilometers were  
4 derived from Smith and Sandwell (1997). Black contour represents 200 m depth,  
5 marking the shelf edge. For the USA side, symbols represent data reported by (solid  
6 squares) Csanady et al. (1988) and (solid diamonds) Butman (1988). Plus symbols  
7 represent further data collected above 150 m depth, included for completeness (Butman  
8 1988; Butman et al. 1979; Csanady et al. 1988; McClennen 1973). Open squares and  
9 diamonds represent data (Csanady et al. 1988; Butman et al. 1988) collected at altitudes  
10 above bottom of 100 m and ~ 50 m, respectively. Current meters at sites 5, F, A, and  
11 SF provided the data in Figure 6. Black star next to "Fig 2" locates the AMCOR 6007  
12 well (Hathaway et al. 1976). For the Iberian margin, symbols represent data reported by  
13 (solid squares) Huthnance et al. (2002) and (solid circles) Thomsen et al. (2002), and  
14 other data collected during (star symbols) the WOCE and (solid diamonds) OMEX-II  
15 experiments (details in electronic supplement ES2). Fine solid line is path of  
16 measurements with a hull-mounted Doppler current profiler used to derive the trends in  
17 Figure 5B (electronic supplement ES3).

18  
19 Figure 5. Mean values of current speeds measured with bottom-moored current meters,  
20 from the sources given in electronic supplement ES2 and at the locations in Figure 4  
21 (identified with corresponding symbols). Data are shown at the local water depth of the  
22 mooring rather than instrument depth (heights above bottom are given in electronic  
23 supplement ES2). Dotted lines show trend of  $\log_{10}\langle|\mathbf{u}|\rangle$  versus  $\log_{10}d$  obtained from  
24 data below 150 m depth by least squares. Lines in Part B are median (bold, 50%) and

1 inter-quartile range (fine lines, 25%, 75%) of further near-bed current speeds derived  
2 from a hull-mounted acoustic Doppler current profiler (electronic supplement ES3).

3

4 Figure 6. Comparison of current variance at different locations along the USA margin.

5 Variance was derived (Csanady et al. 1988) by multiplying power spectral density of  
6 current velocity by the width of each period bands. Period bands are 5.4 to 29.3 days

7 (T, topographic waves), 30 h to 5.4 days (WD, wind-driven), 15.2 to 30 h (I/D, inertial-  
8 diurnal), 10.6 to 15.1 h (SD, semidiurnal), and < 10.6 h (HF, high frequency). A)

9 Comparison of slope sites (solid symbols) MASAR-F and (open symbols) SEEP-I site

10 5. B) Comparison of shelf-edge sites (solid symbols) NASACS-SF and (open symbols)

11 MASAR-A. Sites are located in Figure 4.

12

13 Figure 7. A) Map of the uppermost slope off the central Atlantic USA derived from  
14 continuous multibeam sonar data (National Geophysical Data Center Coastal Relief

15 Model, [www.ngdc.noaa.gov](http://www.ngdc.noaa.gov)). B) Median and inter-quartile range of seabed gradient

16  $|\nabla H|$  and median grain size versus depth. Gradients were calculated from the data

17 outlined in Part A. Grain sizes were measured by NOAA scientists from grab samples

18 collected at sites located by solid star symbols in Part A. C) Sections across the

19 uppermost slope between the diamond symbols in Part A, along with (dashed curves)

20 Equation 7 fitted to the topography by least squares. D) Multichannel seismic section

21 (Schlee et al. 1976; Schlee et al. 1979). E) Single channel seismic section collected

22 along the continuous line in Part A by Lamont-Doherty scientists. F) Summary of

23 sediments recovered at well AMCOR 6021 (Hathaway et al. 1976) with gray-scale

1 representing (white) sand, (light gray) silty and clayey sand, (mid-gray) silty clay, and  
 2 (dark gray) clay. Vertical solid bar marks the vertical extent of the well.

3

4 Figure 8. A) Bathymetry of the Iberian Atlantic upper slope derived from multibeam  
 5 echo-sounder data (NERC 2001). Solid line is the path of a multichannel seismic  
 6 section (Pérez Gussinyé 2000, her Figure 2.2). Open circles mark bottom-photograph  
 7 sites (NERC 2001). Two open star symbols mark sites of bottom-current measurements  
 8 (Huthnance et al. 2002). B) Sections through the lines "a" and "b" marked Part A. C)  
 9 Median (bold) and inter-quartile range of bed gradient calculated for the area outlined in  
 10 Part A.

11

12 Figure 9. Variation of  $K$  with depth derived from the morphology. To compare with  
 13 the current data, each pair of graphs shows the variation in  $K^{1/3}$  and  $K^{1/2}$ , corresponding  
 14 to bedload models in which  $Q_{by} \propto \langle |\mathbf{u}| \rangle^3 |\nabla \mathbf{H}|$  and  $Q_{by} \propto \langle |\mathbf{u}| \rangle^2 |\nabla \mathbf{H}|$ , respectively.  
 15 Dotted line is the regression of Figure 5A for comparison. A)  $K$  varies sharply with  
 16 depth if sediment has deposited over a short lengthscale, implying a more sharply  
 17 varying current speed with depth than presently observed. Also shown are curves  
 18 assuming the sediment simply bypasses (uniform  $Q$  assumption). B)  $K$  varies more  
 19 slowly with depth if the sediment deposits over a (probably unrealistic) longer  
 20 lengthscale. C) Peak speed of bottom currents produced by extreme surface waves with  
 21 the amplitudes and periods shown and with sea level 120 m lower than present (deep-  
 22 water approximation).

23



1 Figure 10. Geometrical relationships for deriving the pattern of deposition rate required  
2 to maintain the rollover as a steady-state feature. A) The rollover grows vertically by  
3 aggrading uniformly at rate  $A$ . B) The rollover progrades at a uniform rate  $dy/dt$ . C)  
4 The rollover both aggrades and progrades, climbing at angle  $\alpha$ .

5

6 Figure 11. A) The mean offshore current velocity of (solid circles) Csanady et al.  
7 (1988) for the USA sites and (solid stars) Huthnance et al. (2002) for the two Iberian  
8 sites (Figure 8A). The two open circles represent Csanady et al.'s data from their sites  
9 A and F located in Figure 4. B) The ratio of the mean offshore velocity to mean speed.  
10 All near-bottom data are shown, including those collected 100 m above bottom. Depths  
11 represent local water depths of measurements. Dashed and dotted lines represent  
12 thresholds between current- and gravity-dominated transport for the USA and Iberia  
13 areas, respectively (see main text for explanation).

14

15 Figure 12. A) Bed gradient in degrees calculated from the USA bathymetry (Figure 7).  
16 Contours are annotated in meters. B) Relative changes in bed topography predicted  
17 with the diffusion model with mobility  $K$  decreasing with depth. Data below 400 m  
18 have been censored, because the model does not apply to the slope muds. Note lack of  
19 change on spurs between canyon heads.

20

21

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1 Electronic Supplements

2 **ES1. GRAVITY EFFECT ON SANDY BEDLOAD**

3 The following section outlines present understanding of how gravity affects  
 4 bedload transport flux. The initial models based on Bagnold's (1963) work are  
 5 described first, because they provide a useful framework for understanding the influence  
 6 on bed morphology. Bagnold's approach is considered valid only for highly developed,  
 7 dense bedloads (Leeder 1979), so more recent work describing effects of individual  
 8 saltating particles is also described.

9 For a simple horizontal sandy bed affected by a strong uniform, steady current,  
 10 Bagnold's original formula is still considered reasonably accurate (Soulsby 1997):

11 
$$Q_b \text{ (kg/m/s)} \propto \tau_b^{1/2} (\tau_b - \tau_0); \quad \tau_b > \tau_0 \quad \text{(ES1)}$$

12 where  $\tau_b$  is the shear stress imposed by bottom current on the bed and  $\tau_0$  is a threshold  
 13 stress for sediment motion (the symbol " $\propto$ " means "is proportional to", i.e., constants  
 14 are left out for simplicity). Equation ES1 follows a similar relation found empirically in  
 15 earlier flume experiments (Meyer-Peter and Muller 1948). Because the bed shear stress  
 16  $\tau_b = C_d \rho_w U^2$ , where  $C_d$  is a bed friction factor,  $\rho_w$  is seawater density, and  $U$  is mean  
 17 flow velocity above the bottom boundary layer, Equation ES1 can also be written  $Q_b \propto$   
 18  $C_d^{3/2} U (U^2 - U_0^2)$  where  $U_0$  corresponds with  $\tau_0$ . Thus, for a bed of uniform and  
 19 unchanging  $C_d$ , flow significantly faster than  $U_0$  leads to approximately  $Q_b \propto U^3$ .

20 Nielsen (1992) described how Equation ES1 could arise based on Bagnold's  
 21 original arguments. The mobile bedload imposes a normal stress  $\sigma_e$  on the lower  
 22 immobile bed equal to the submerged weight of the bedload (allowing for buoyancy):

23 
$$\sigma_e = (\rho_g - \rho_w) g \int_0^\infty C(z) dz \quad \text{(ES2)}.$$



1 where  $\rho_g$  is the sediment grain density,  $g$  is the gravitational acceleration, and  $C$  is the  
 2 sediment volumetric density. Assuming that a simple Mohr-Coulomb yield criterion  
 3 applies to the top of the immobile layer (dashed line in Figure 1A) and that the shear  
 4 stress at that level equals the shear stress imposed by the current (i.e., the solid phase  
 5 acquires the current shear stress perfectly through grain to grain collisions (Bagnold  
 6 1963)), the flow-imposed shear stress is

$$7 \quad \tau = \tau_0 + \sigma_e \tan \phi_s \quad (\text{ES3}).$$

8 where  $\phi_s$  is the sediment's angle of internal friction. The amount of bedload mobilized  
 9 then relates to the excess imposed shear stress:

$$10 \quad \int_0^\infty C(z) dz = \frac{\tau_b - \tau_0}{(\rho_g - \rho_w) g \tan \phi_s} \quad (\text{ES4}).$$

11 Thus, the term  $(\tau_b - \tau_0)$  in Equation ES1 could arise from friction - a larger imposed stress  
 12 mobilizes a greater amount of sand, leading to greater bedload flux. Nielsen noted that  
 13 too few data are available on the velocities of individual grains to then predict the  
 14 resulting bedload flux, but the fact that various flux measurements follow Equation ES1  
 15 (Bagnold 1980; Nielsen 1992) suggests that mean particle velocities scale with flow  
 16 shear velocity, as found by tracking particles using high-speed film (Fernandez Luque  
 17 and van Beek 1976).

18 The effect of sloping beds is illustrated in Figure 1 (shear stress due to the  
 19 current is omitted for simplicity). For a longitudinal gradient, the normal stress in  
 20 Equation ES2 is modified by the factor  $\cos \gamma$  and the total shear stress acting on the  
 21 threshold surface includes the component of bedload weight. Equation ES3 then  
 22 becomes (Bagnold 1963):

$$23 \quad \tau = \tau_0 + (\tan \phi_s + \tan \gamma) \cos \gamma (\rho_g - \rho_w) g \int_0^\infty C(z) dz \quad (\text{ES5}).$$

1 ( $\gamma$  here is negative for a down-gradient.) The amount of bedload of Equation ES4  
 2 should then be modified, with greater amounts mobilized on down-gradients:

$$3 \quad \int_0^{\infty} C(z) dz = \frac{\tau_b - \tau_0}{(\tan \phi_s + \tan \gamma) \cos \gamma (\rho_g - \rho_w) g} \quad (\text{ES6}).$$

4 Bagnold (1963) derived Equation ES1 by assuming that the power expended by  
 5 the shearing bedload was a simple proportion of the power expended by the current.  
 6 Bagnold's energetics argument was extended to arbitrary slopes (Bailard and Inman  
 7 1981; Huthnance 1982a, 1982b) by assuming that the flux magnitude is proportional to  
 8 the current's power expenditure but flux direction is governed by the vectorally  
 9 combined stresses due to the current and down-gradient component of bedload weight.  
 10 The bedload flux  $\mathbf{Q}_b$  is then:

$$11 \quad \mathbf{Q}_b = S |\mathbf{u}|^2 (\mathbf{u} - \lambda |\mathbf{u}| \nabla \mathbf{H}) / g \quad (\text{ES7})$$

12 where  $S$  is a constant,  $\lambda = 1/\tan \phi_s$  and  $\nabla \mathbf{H}$  is bed gradient (bold symbols represent  
 13 vectors and  $|\dots|$  the vector magnitude).

14 Criticisms have been made concerning Bagnold's approach. In his model, fluid  
 15 momentum is transferred to moving particles so that the fluid shear stress becomes  
 16 insignificant at the base of the mobile layer. This only occurs, however, if the bedload  
 17 is well-developed, otherwise the bedload is better described as isolated saltating  
 18 particles than as a continuous layer (McEwan et al. 1999; Niño and Garcia 1998;  
 19 Seminara et al. 2002). Saltation models of varying complexity have been developed  
 20 (McEwan et al. 1999; Niño and Garcia 1994; Niño and Garcia 1998; Wiberg and Smith  
 21 1985, 1989), which variously incorporate particle extraction from the bed, trajectory,  
 22 rebound or deposition, and dislodgement of bed particles. Trajectories are potentially  
 23 affected by lift caused by fluid shear or particle rotation (Leeder 1979). Despite their

1 complexity, these models can reproduce the variations in Equation ES1 remarkably well  
 2 (e.g., McEwan et al. 1999).

3 Sekine and Parker (1992) summarized models of bedload on transverse slopes.  
 4 They suggested that the components of flux down-gradient  $q_n$  and in the direction of the  
 5 current  $q_s$  can be separated. If there is no current down-gradient, their ratio is

$$6 \quad q_n/q_s = -B \tan \gamma, \quad B = B_0(\tau_c/\tau_b)^m \quad (\text{ES8}).$$

7 Depending on the model, the coefficient  $B_0$  incorporates the sand friction coefficient  
 8 and other parameters. The different models summarized by Sekine and Parker  
 9 (Engelund 1974; Hasegawa 1981; Ikeda 1982; Kikkawa et al. 1976; Parker 1984;  
 10 Struiksma et al. 1985), their own results of numerical simulations of saltation, and a  
 11 more recent model based on entrainment rates varying with shear stress (Parker et al.  
 12 2003) predict  $m = 0$  to  $1.0$ . If  $q_s \propto \tau_b^{1.5}$  (Equation ES1, omitting the threshold for  
 13 simplicity), such values of  $m$  imply that the down-gradient flux variation lies between  $q_n$   
 14  $\propto \tau_b^{1.5}$  (i.e.,  $q_n \propto u^3$ ) and  $q_n \propto \tau_b^{0.5}$  ( $q_n \propto u^1$ ). The wind-tunnel data of Ikeda (1982) and  
 15 recent model of Parker et al. (2003) are consistent with  $q_n \propto \tau_b^{1.0}$  ( $q_n \propto u^2$ ) for large  $\tau_b$ .

16 Given the diversity of theoretical predictions, experiments are needed to inform  
 17 this question, but few are available and most were carried out with longitudinal  
 18 gradients. Damgaard and co-workers (Damgaard et al. 2003; Damgaard et al. 1997)  
 19 used a recirculating flume in which flow rate was held fixed but the longitudinal  
 20 gradient varied. In the first set, fine sand (median diameter  $d_{50} = 208 \mu\text{m}$  or  $\phi = 2.3$ )  
 21 was injected into the base of the flume with a piston controlled such that the injection  
 22 rate exactly matched removal as bedload. Bedload fluxes derived from sand pickup rate  
 23 are shown in Figure 2A for three different sets of experiments made with different flow

1 rates. They show the expected increasing flux with increasing down-slope gradient,  
2 with an abrupt increase towards the sand angle of repose.

3 In their second study at higher flow rates (Damgaard et al. 2003), sediment-trap  
4 measurements (representing largely bedload) show a systematic variation with bed  
5 gradient. Ripples, however, formed on the bed, significantly affecting suspended  
6 sediment fluxes because of sand thrown into suspension at ripple crests. Hence,  
7 suspended sediment fluxes (gray-filled circles in Figure 2B) are varied and peak at  $-5^\circ$   
8 rather than at maximum gradient. The effect of ripples was complex because different  
9 ripple morphologies formed at different bed gradient, leading to varied suspension.  
10 Their flow speed of 0.35 m/s measured 13 cm above bed is comparable with maximum  
11 speeds measured near the shelf edge (Huthnance et al. 2002). Considering that ripples  
12 are observed around the shelf edge (Yorath et al. 1979), varied suspension could be a  
13 further complication, but Figure 2B nevertheless shows a general tendency for fluxes to  
14 increase with increasing down-gradient.

15 Further experiments (Fernandez Luque and van Beek 1976; Smart 1984)  
16 documented effects of longitudinal gradients. In Smart's experiment, flux increased  
17 with  $S^{0.6}$  (where  $S$  is bed gradient) but included some suspended transport. Fernandez  
18 Luque and van Beek's experiments recorded an effect of gradient on the threshold of  
19 motion, and bedload flux correlated moderately well with excess stress corrected for the  
20 gradient effect.

21 Japanese experimental results with transverse gradients (Hasegawa 1981;  
22 Yamasaka et al. 1987) shown in Sekine and Parker (1992) are reproduced in Figure 2C  
23 (those of Hasegawa were carried out in water whereas those of Yamasaka et al. were  
24 carried out in air). Based on Equation ES10, the trend in the data should reveal the

1 value of the exponent  $m$ . The main group of data were claimed (Sekine and Parker  
2 1992) to be consistent with  $m = 0.25$ , which implies  $q_n \propto t_b^{1.25}$  ( $q_n \propto u^{2.5}$ ).

3 The theoretical and experimental results therefore suggest that bedload flux  
4 should be affected by bed gradient, with a component down-gradient,  $Q_b = -K|\nabla H|$ .  
5 Although not well constrained, the Japanese data suggest that the dependence of  $K$  on  
6 current speed  $u$  probably lies between  $K \propto u^2$  and  $K \propto u^3$ . If threshold effects are also  
7 considered, a variation  $K \propto (u-u_0)^2$  could produce morphological results similar to  $K \propto$   
8  $u^3$ . As the published current meter data do not allow threshold effects to be fully  
9 accounted for, we have compared current variations with morphology assuming that  $K$   
10 lies between  $K \propto u^2$  and  $K \propto u^3$ , but threshold effects may need to be considered in  
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12

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## ES2: CURRENT-METER STATION LIST AND VALUES

Station ID	Latitude (degrees N)	Longitude (degrees W)	Depth (m)	Measure-ment altitude (m)	Dura-tion (days)	Mean speed (cm/s)	Source	Symbol in Fig. 4
USA Atlantic margin								
SEEP-5/1983 <sup>1</sup>	39.805	70.9217	1250	10	197	6.1	Csanady et al. (1988)	square (solid)
SEEP-5/1984 <sup>1</sup>	39.805	70.9217	1250	10	173	5.6	Csanady et al. (1988)	square (solid)
NASACS-SA <sup>1</sup>	40.08	68.5583	485	7	148	8.	Butman et al. (1988)	diamond (solid)
NASACS-SE <sup>1</sup>	39.8967	70.0617	491	7	141	9.9	Butman et al. (1988)	diamond (solid)
NASACS-SE <sup>1</sup>	39.8967	70.0617	504	7	244	6.2	Butman et al. (1988)	diamond (solid)
NASACS-SF <sup>1</sup>	39.9617	70.015	202	7	98	13.8	Butman et al. (1988)	diamond (solid)
NASACS-SF <sup>1</sup>	39.9617	70.015	204	7	129	11.6	Butman et al. (1988)	diamond (solid)
NASACS-SA <sup>1</sup>	40.08	68.5583	479	6	149	7.9	Csanady et al. (1988)	square (solid)
NASACS-SF <sup>1</sup>	39.9617	70.015	204	7	143	11.6	Csanady et al. (1988)	square (solid)
NASACS-SG <sup>1</sup>	39.8083	70.0833	1150	7	246	8.4	Butman et al. (1988)	diamond (solid)
NASACS-SH <sup>1</sup>	39.842	70.0283	1220	7	171	5.4	Csanady et al. (1988)	square (solid)
MASAR-A <sup>1</sup>	39.704	73.063	225	5	116	12.4	Csanady et al. (1988)	square (solid)
LCI <sup>1</sup>	40.38	67.5517	250	5	148	9.81	Butman et al. (1988)	diamond (solid)
LCI <sup>1</sup>	40.38	67.5517	250	5	146	8.86	Butman et al. (1988)	diamond (solid)
LCI <sup>1</sup>	40.38	67.5517	247	5	125	9.93	Butman et al. (1988)	diamond (solid)
LCI <sup>1</sup>	40.38	67.5517	249	6	157	11.95	Butman et al. (1988)	diamond (solid)
Atlantic data also plotted but not used in the speed-depth regression:								
A <sup>1</sup>	39.48	72.98	59	1.5-2.0	11.92	10.7	McClennen (1973)	plus
C <sup>1</sup>	39.06	74.0767	30	1.5-2.0	8.88	12.	McClennen (1973)	plus
D <sup>1</sup>	38.8467	73.16	74	1.5-2.0	10.79	11.7	McClennen (1973)	plus
B <sup>1</sup>	39.25	72.5667	143	1.5-2.0	10.13	17.8	McClennen (1973)	plus
T <sup>1</sup>	40.1817	69.9717	100	7	117	10.95	Butman et al. (1988)	plus
SEEP-2/1983 <sup>1</sup>	40.2417	70.9167	125	5	146	10.3	Csanady et al. (1988)	plus
Aa <sup>1</sup>	39.3917	72.9917	60	-	36	8	Butman (1979)	plus
Ab <sup>1</sup>	39.3917	72.9917	65	-	23	7	Butman (1979)	plus
B <sup>1</sup>	38.7083	73.6333	60	-	68	9	Butman	plus



							(1979)	
Ca <sup>1</sup>	38.5417	73.5083	80	-	36	13	Butman (1979)	plus
Cb <sup>1</sup>	38.5417	73.5083	87	-	14	6	Butman (1979)	plus
MASAR-F <sup>1</sup>	36.836	74.576	1005	100	210	6.5	Csanady et al. (1988)	square (open)
NASACS-SA <sup>1</sup>	40.08	68.5583	475	100	337	10.4	Csanady et al. (1988)	square (open)
NASACS-SD <sup>1</sup>	40.284	67.730	485	100	328	11.4	Csanady et al. (1988)	square (open)
NASACS-SE <sup>1</sup>	39.8967	70.0617	500	100	350	9.5	Csanady et al. (1988)	square (open)
NASACS-SE <sup>1</sup>	39.8967	70.0617	510	100	142	9.9	Csanady et al. (1988)	square (open)
NASACS-SE <sup>1</sup>	39.8967	70.0617	504	100	245	8.8	Csanady et al. (1988)	square (open)
LCI <sup>1</sup>	40.38	67.5517	250	55	148	9.46	Butman et al. (1988)	diamond (open)
LCI <sup>1</sup>	40.38	67.5517	249	50	157	8.97	Butman et al. (1988)	diamond (open)
Iberian Atlantic margin:								
stablecd110 <sup>1</sup>	42.6783	9.50833	202	0.21-0.91	18	13	Huthnance et al. (2002)	square (solid)
stablecd114 <sup>1</sup>	42.6667	9.50833	200	0.21-0.91	18.5	10	Huthnance et al. (2002)	square (solid)
rcm03192 <sup>3</sup>	40.999	9.475	1293	99	730.6	10.62	Malena (WOCE) (2)	star (solid)
rcm02590 <sup>3</sup>	42.218	9.509	1338	100	387	3.95	Malena (WOCE) (2)	star (solid)
b0530652 <sup>3</sup>	41.315	8.9867	84.0	2.	75.	8.87	OMEX-II(1)	diamond (solid)
b0530720 <sup>3</sup>	41.3183	8.9817	84	3.	139.	9.35	OMEX-II(1)	diamond (solid)
- <sup>2</sup>	42.33	9.38	853	0.05-0.4	-	6.6	Thomsen et al. (2002)	circle (solid)
- <sup>2</sup>	42.33	9.38	194	0.05-0.4	-	18.75	Thomsen et al. (2002)	circle (solid)
- <sup>2</sup>	42.33	9.38	97	0.05-0.4	-	27	Thomsen et al. (2002)	circle (solid)
- <sup>2</sup>	43.05	9.52	155	0.05-0.4	-	31.4	Thomsen et al. (2002)	circle (solid)
OTHER W EUROPE ATLANTIC MARGIN								
Hebrides <sup>1</sup>	56.45	9.05	210	0.21-0.91	27	12	Huthnance et al. (2002)	circle (open)
Hebrides <sup>1</sup>	56.46	9.04667	204	0.21-0.91	15	14	Huthnance et al. (2002)	circle (open)
Goban Spur <sup>1</sup>	49.3917	11.6667	879	0.21-0.91	10	11	Huthnance et al. (2002)	circle (open)
Chapelle Bank <sup>1</sup>	47.47	6.54667	388	0.21-0.91	8	17	Huthnance et al. (2002)	circle (open)

1  
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3  
4  
5

"Station ID" is the identifier used in the data sources.

(1) Ocean Margin Exchange (OMEX) Project, OMEX-II Project data set (CD-ROM, British Oceanographic Data Centre, Liverpool, UK (NERC)). Original data attributed to Instituto Hidrografico, Portugal.

(2) Data calculated from current velocity data supplied as part of the WOCE compilation, attributed to ACM27 and ACM28 ("Morena" experiment). Originally collected by scientists of the University of Lisbon and the Spanish Institute of Oceanography. Related publication: Fiúza, A. F. G., Hamann, M., Ambar, I., Díaz del Río, G., González, N., and Cabanas, J. M., 1998, Water masses and their circulation off western Iberia during May 1993: *Deep-Sea Res. I.*, v. 45, p. 1127-1160.

Superscripts in Station ID column refer to the type of measuring instrument:

<sup>1</sup>Mechanical: rotor(s) with direction vane.

<sup>2</sup>Acoustic doppler current profiler.

<sup>3</sup>Unknown.

#### Notes on accuracy

As the above results include measurements made with different current meters, the relative performance of the different instruments could be a cause for concern. In particular, the mean current measured with mechanical current meters is known to be affected by superimposed oscillating currents, such as from surface waves, because of the finite response time of the rotors and direction vane. The instruments measure the wave current when it adds to the mean current but under-record when the wave-current reverses, leading to a net bias. In one study (Beardsley 1987), when wave currents had root-mean-squared amplitudes equal to half the mean current velocity, the measured current was in error by 10% and greater for larger oscillating current amplitudes. These measurements will also not be particularly representative of the instantaneous current speed (due to both wave and mean current) in such situations. These issues are not expected to affect the arguments in this paper greatly because we are concerned with variations below 150 m where high-frequency oscillating currents tend not to penetrate.

Potential errors in the calibration formulae that have been used at Woods Hole Oceanographic Institution to relate rotor speed to current speed have been noted by Lentz et al. (1995). Their comparison of a mechanical current meter with an acoustic current meter suggested that the error increased linearly to around 2.5 cm/s at a speed of 30 cm/s. If it had affected the results of Csanady et al. (1988) and Butman et al. (1988) (these papers unfortunately lack calibration details), the values in Fig. 5A will have been exaggerated by around 1 cm/s at 10 cm/s mean speed and less at depth. This will have steepened the graph slightly but not sufficiently to affect the arguments in the paper.

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### 1           **ES3. BOTTOM CURRENTS FROM SHIP ADCP DATA OFF IBERIA**

2           Data were collected with a hull-mounted acoustic Doppler current profiler  
3 (ADCP) during a cruise off the Iberian margin shown in Figure ES3 (Huthnance 1997).  
4 The ship traversed the margin repeatedly, crossing the 200 m contour at 20 random  
5 times with respect to the tidal cycle. Although the 10 day period of the cruise is short  
6 compared with some oceanographic variations, these data provide a further indication of  
7 how the magnitude of seabed oscillations varies with water depth, in relatively mild  
8 June conditions (Huthnance 1997).

9           The ADCP vector currents were corrected for ship motion and converted to  
10 current vector magnitudes. Bathymetry along the ship tracks was derived by  
11 interpolating (Smith and Wessel 1990) 50 m contours of the General Bathymetric Chart  
12 of the Ocean (GEBCO) above 200 m depth (IOC, IHO and BODC, 2003) along with  
13 multibeam bathymetry of the slope (NERC 2001). To derive near-bed current speeds,  
14 while allowing for bathymetry inaccuracy due to incomplete coverage, we selected all  
15 current data within 60 m of the seabed. The solid line in Figure 5B then represents the  
16 median average near-bed current as a function of the local water depth and dotted lines  
17 show the inter-quartile range of current speeds.

18           Because the ADCP averages current data over typically 5 minutes, the trend in  
19 Figure 5B excludes effects of long-period surface waves (swell), affecting the shallower  
20 depths. Northerly winds during the cruise favored upwelling, and interestingly this  
21 should have produced currents decreasing inversely with water depths, similar to those  
22 observed. The Ekman surface current is expected to have a volumetric transport flux  
23 relative to its underlying water that relates to the wind stress rather than depth, but its  
24 squeezing into shallow water leads to stronger currents. If the upwelling flux is  $Q$ , the

1 bottom-layer onshore current is  $u_b$ , total depth  $H$ , and upper water layer thickness  $h_u$ ,  
2 then the absolute upper-layer flux offshore is  $Q - u_b h_u$ . The lower-layer flux onshore is  
3  $u_b(H - h_u)$ . These two transport fluxes cancel at the coast, so combining the above  
4 suggests  $u_b = Q/H$ , i.e. flow in the lower layer inversely proportional to water depth,  
5 similar to that observed in Figure 5B. This analysis applies over shelf depths 100 to 200  
6 m, but friction affects flow in shallower depths and upwelling can occur mid-depth in  
7 deeper water.

8

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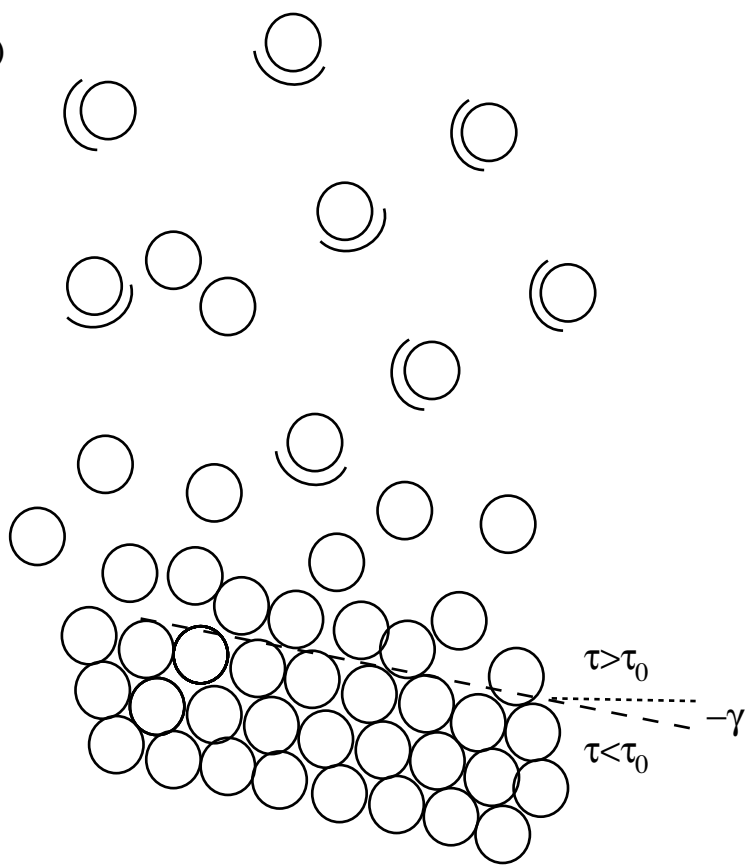
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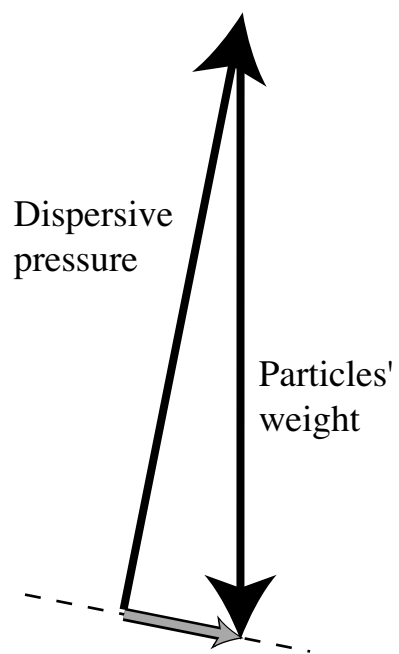
23 Figure ES3. Path of RRS Charles Darwin during cruise 105 while operating its hull-  
24 mounted ADCP.



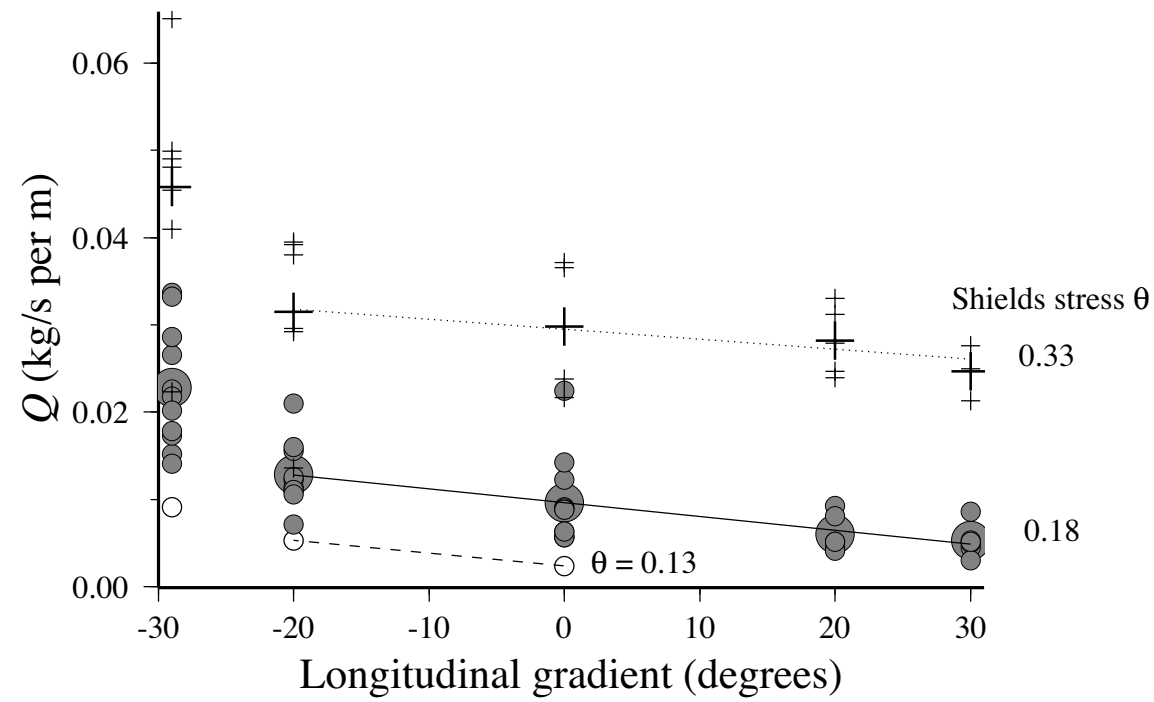
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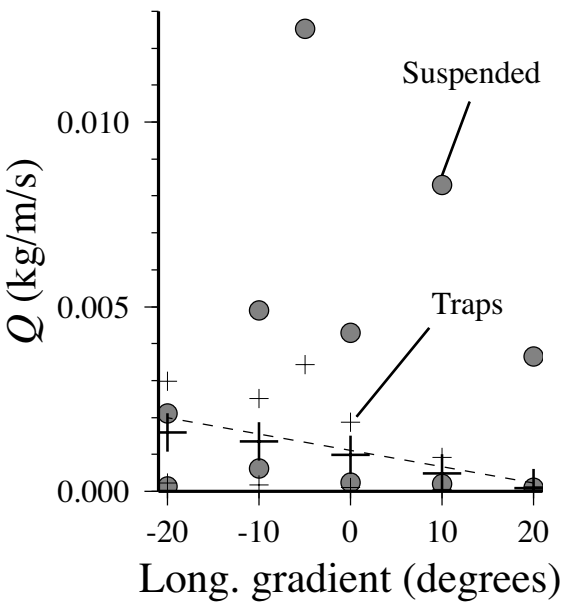
B)



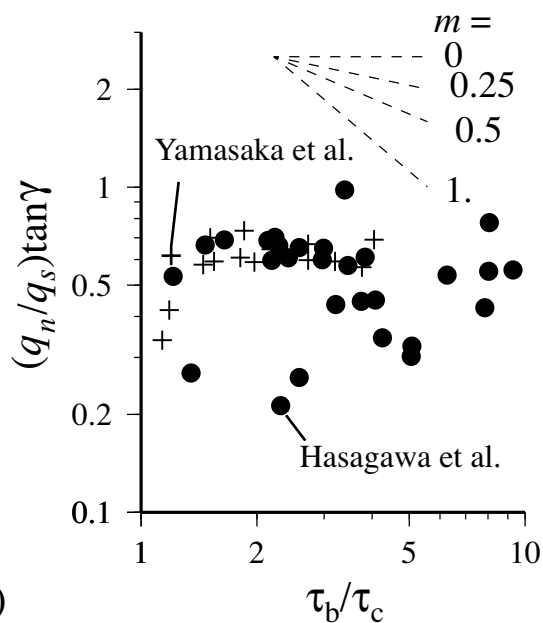
A) Damgaard et al. (1997)

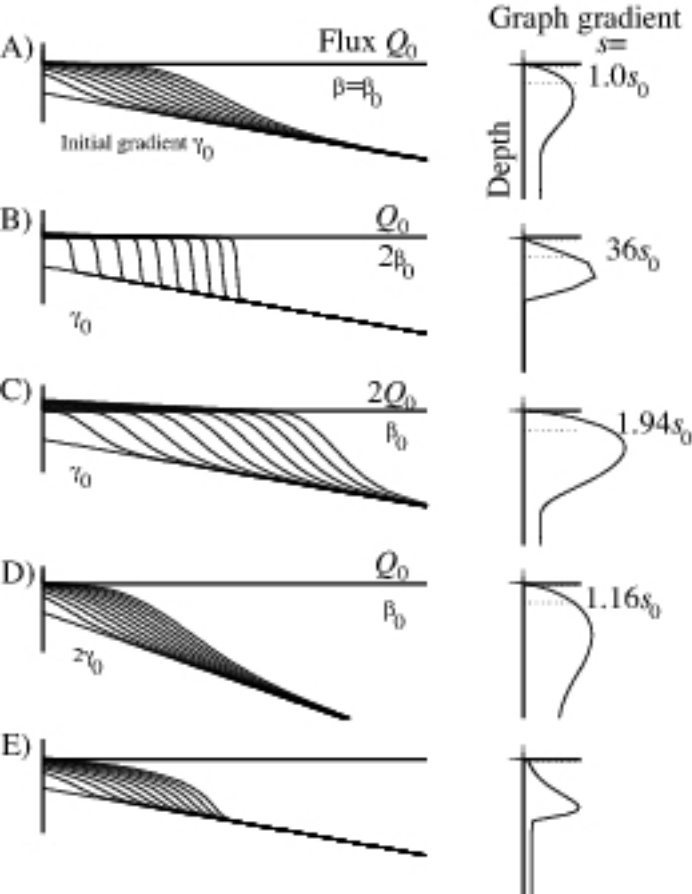


B) Damgaard et al. (2003)



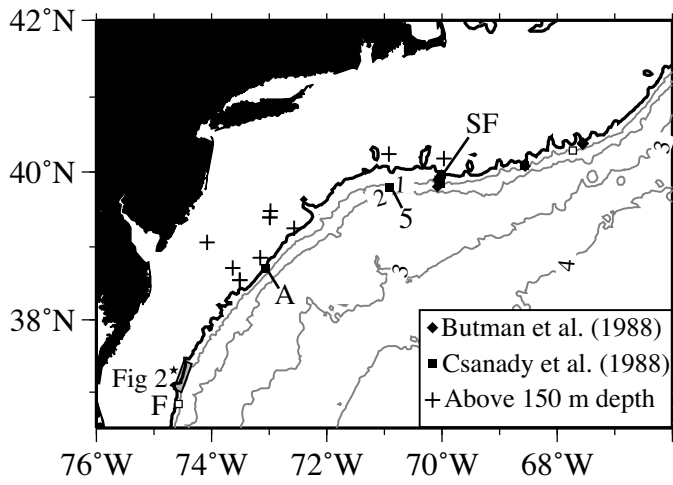
C) Sekine and Parker (1992)



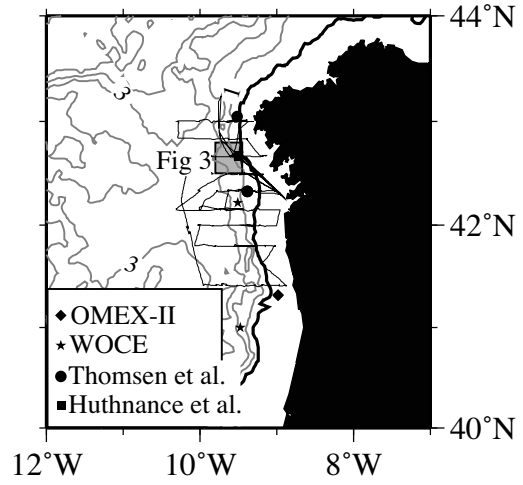


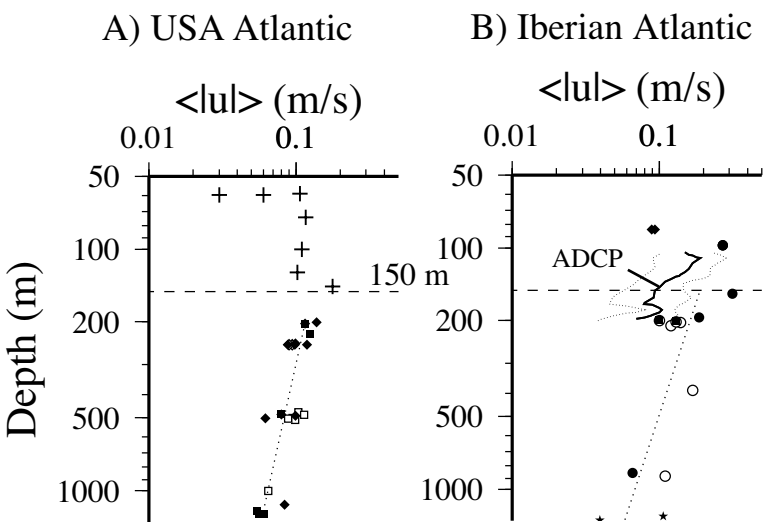


USA Atlantic margin

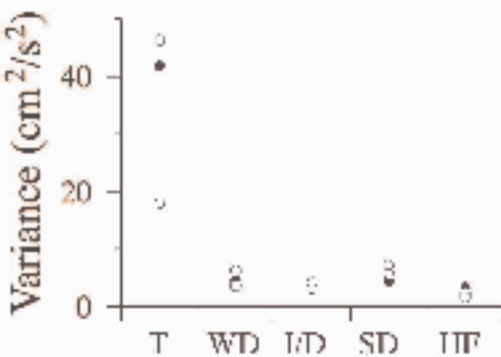


Iberia Atlantic margin

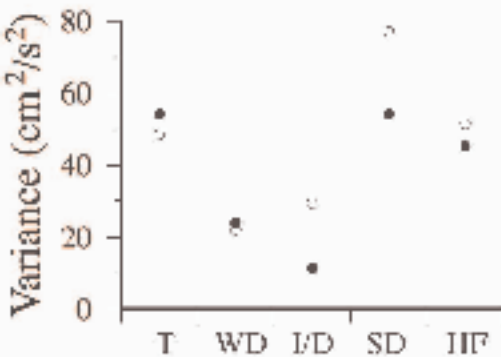


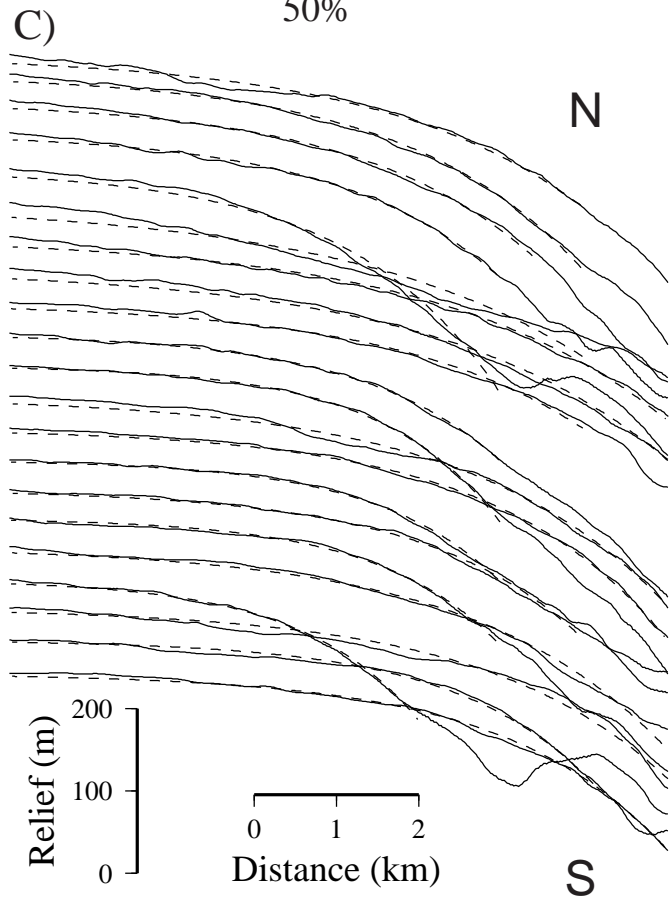
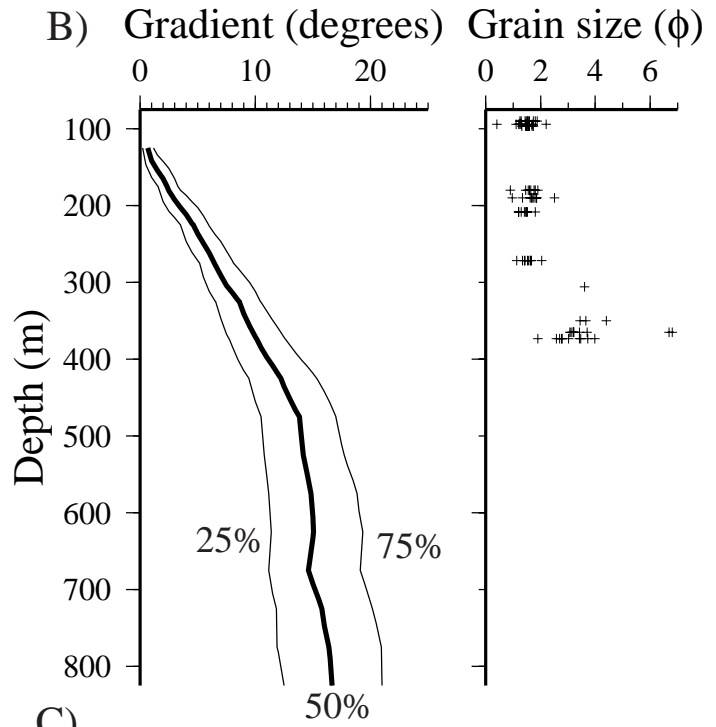
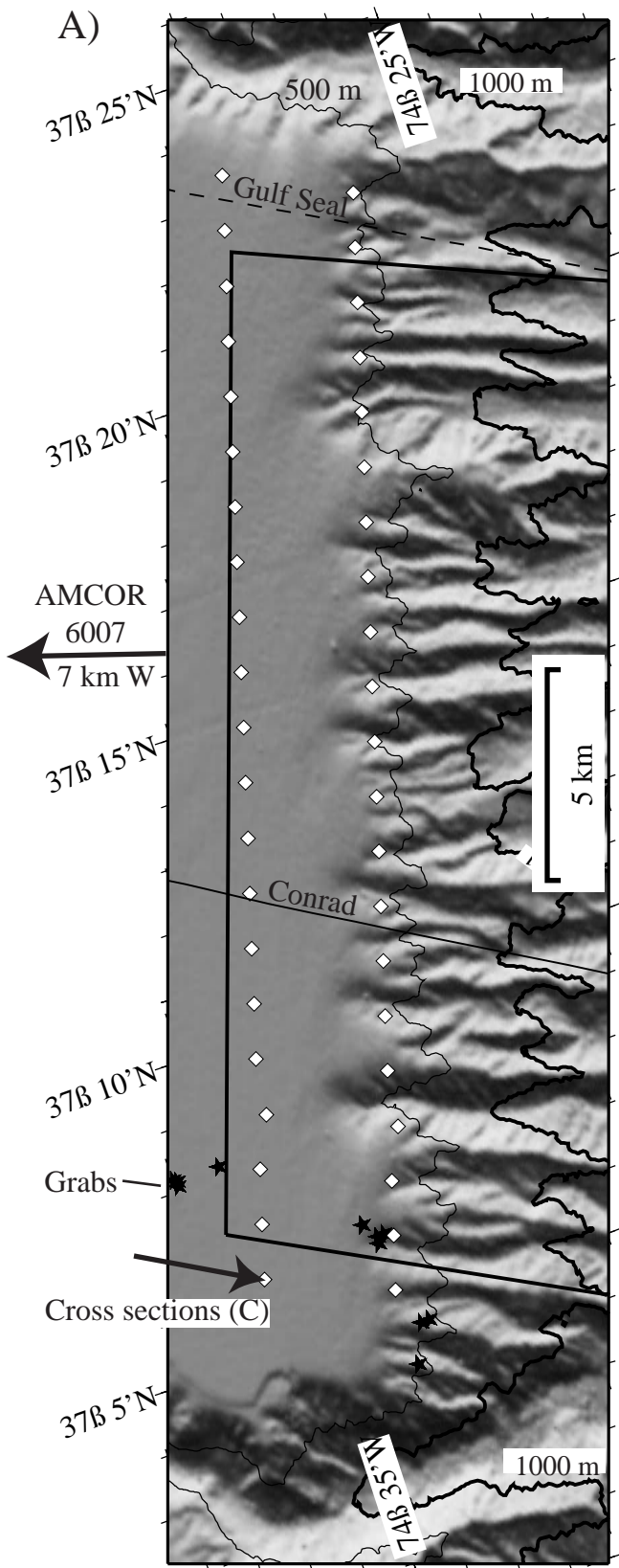


A) Slope sites ( $\sim 1000$  m depth)

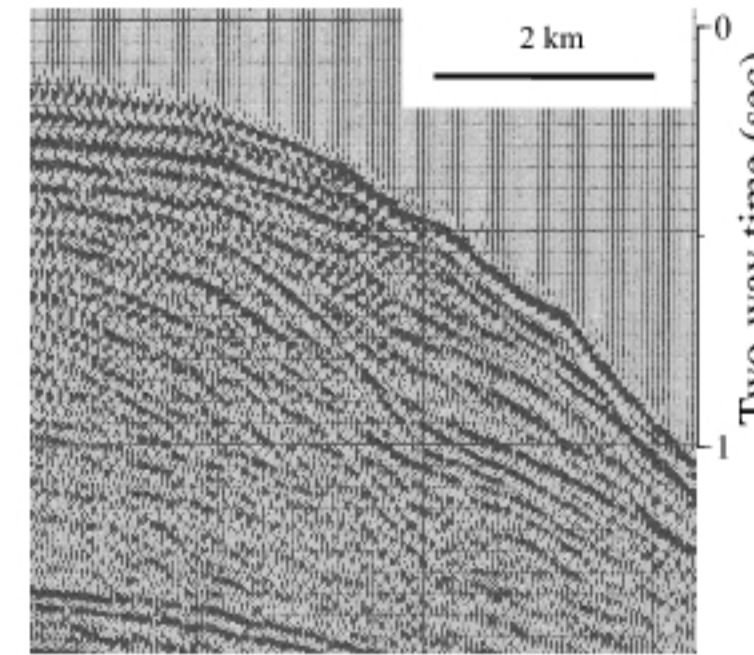


B) Shelf-edge sites ( $\sim 200$  m depth)

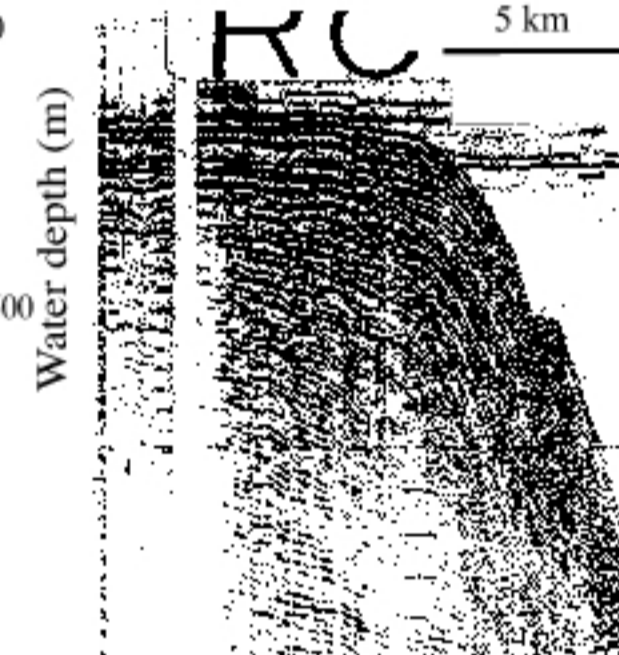




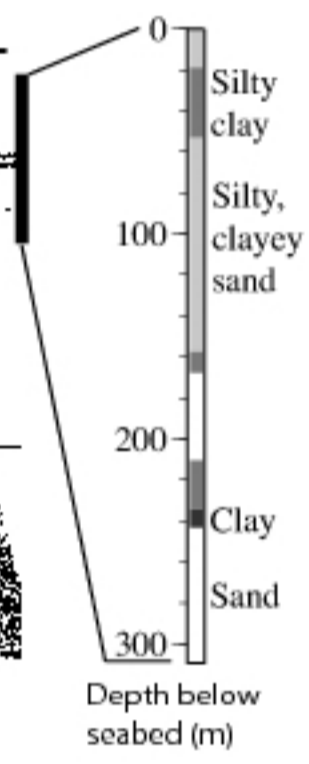
D) M/V Gulf Seal line

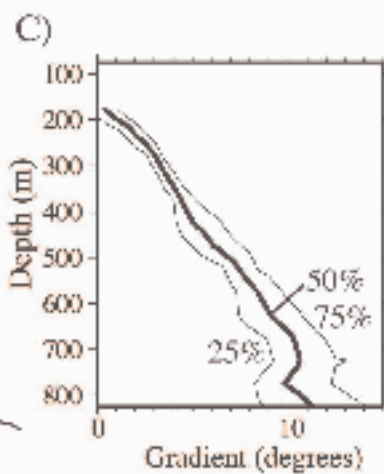
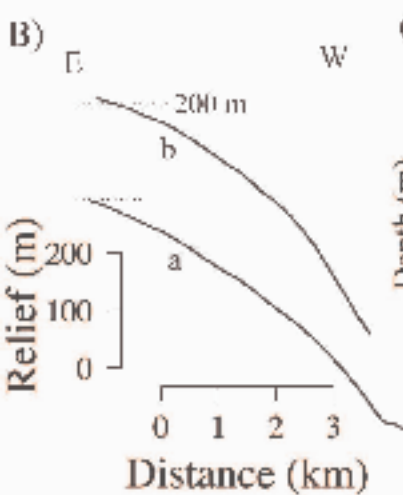
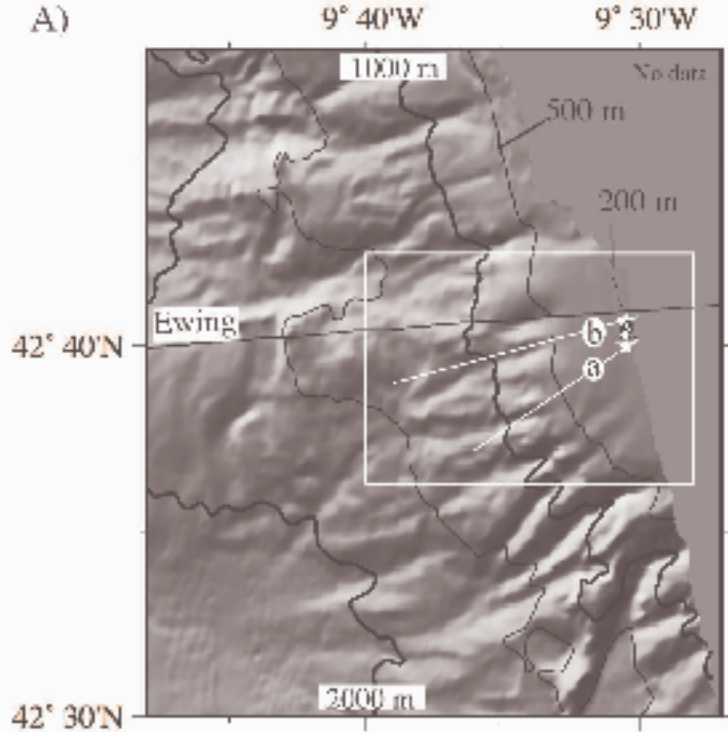


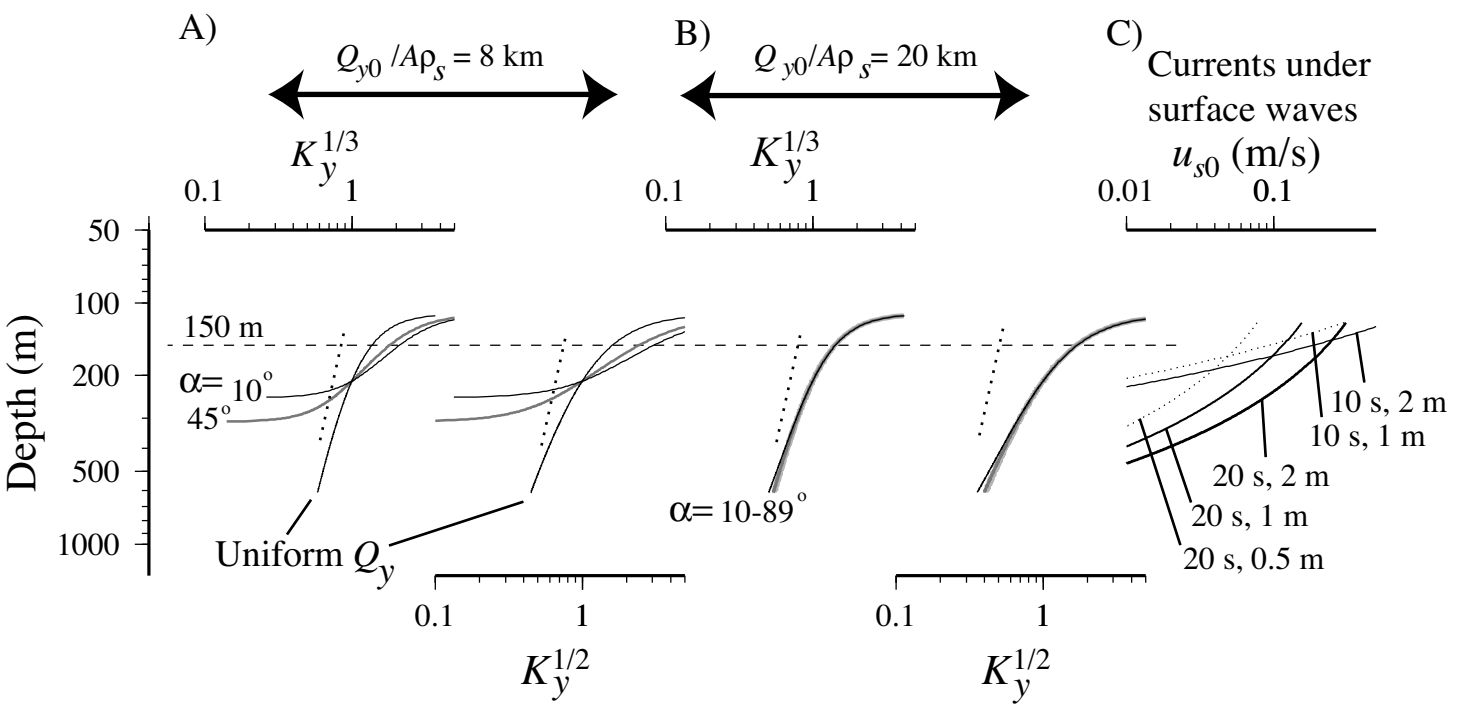
E) R/V Conrad line



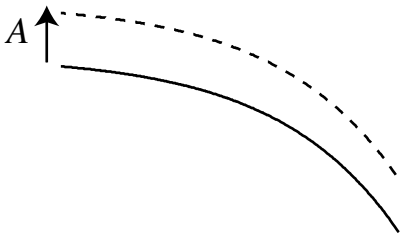
F) AMCOR 6007



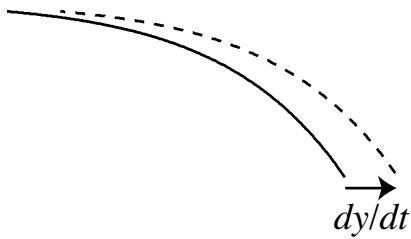




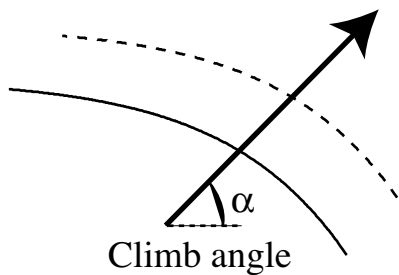
A) Uniform aggradation



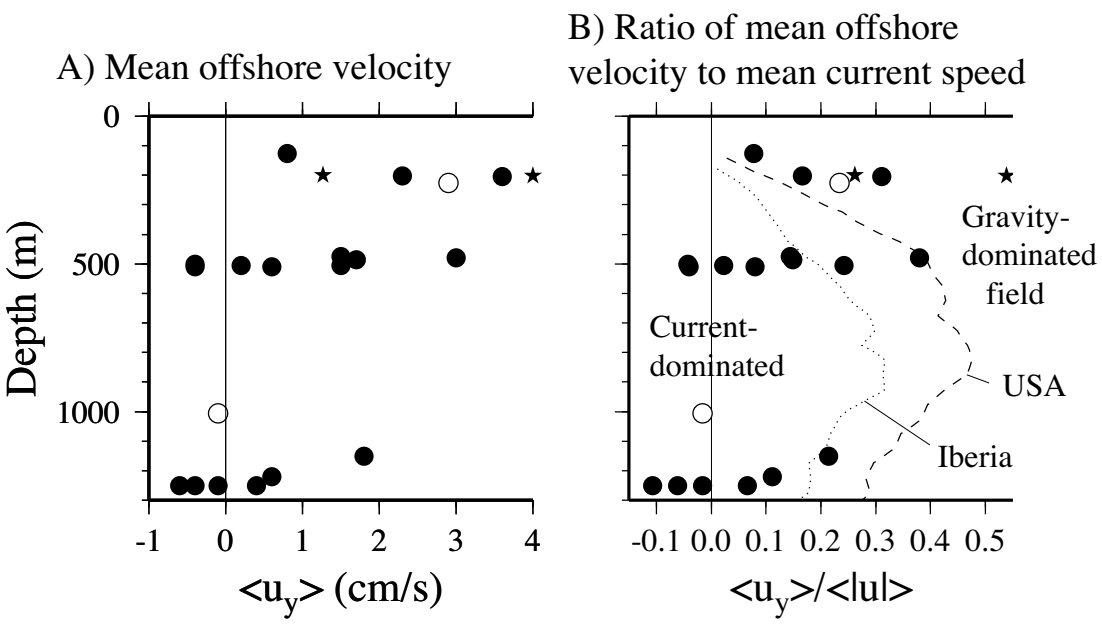
B) Uniform progradation



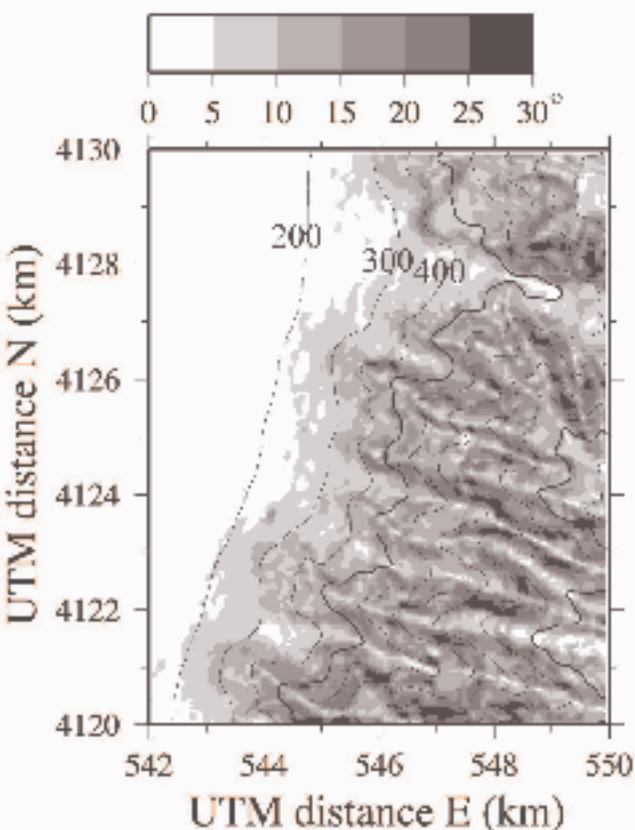
C) Aggradation and progradation







A) Bed gradient



B) Diffusion model

